



Segmentation & Grouping

Wed, Feb 9
Prof. Kristen Grauman
UT-Austin

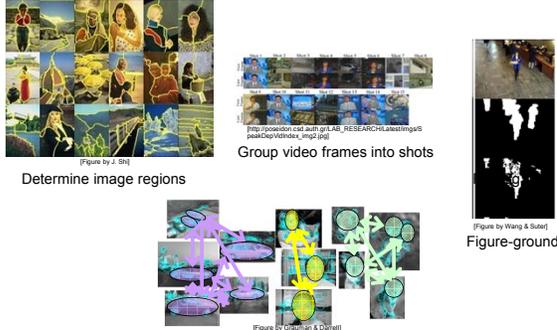
Outline

- What are grouping problems in vision?
- Inspiration from human perception
 - Gestalt properties
- Bottom-up segmentation via clustering
 - Algorithms:
 - Mode finding and mean shift: k-means, mean-shift
 - Graph-based: normalized cuts
 - Features: color, texture, ...
 - Quantization for texture summaries

Grouping in vision

- Goals:
 - Gather features that belong together
 - Obtain an intermediate representation that compactly describes key image or video parts

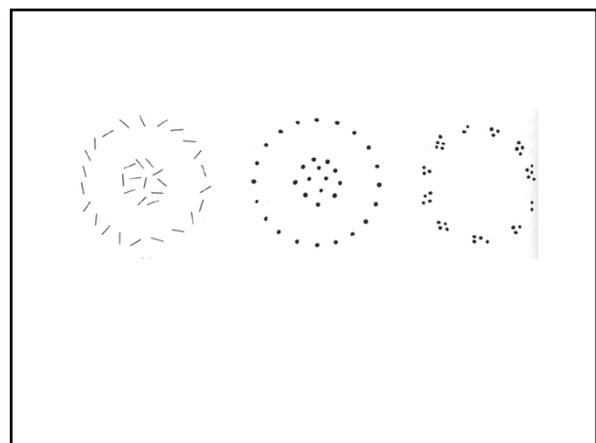
Examples of grouping in vision



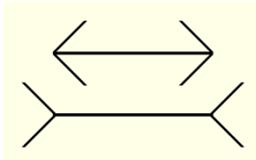
Determine image regions
Group video frames into shots
Figure-ground
Object-level grouping

Grouping in vision

- Goals:
 - Gather features that belong together
 - Obtain an intermediate representation that compactly describes key image (video) parts
- Top down vs. bottom up [segmentation](#)
 - Top down: pixels belong together because they are from the same object
 - Bottom up: pixels belong together because they look similar
- Hard to measure success
 - What is interesting depends on the app.



Muller-Lyer illusion



What things should be grouped?
What cues indicate groups?

Gestalt

- Gestalt: whole or group
 - Whole is greater than sum of its parts
 - Relationships among parts can yield new properties/features
- Psychologists identified series of factors that predispose set of elements to be grouped (by human visual system)

Similarity



Symmetry



Common fate



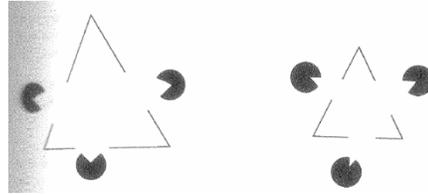
Image credit: Arthur-Bertrand (via F. Durand)

Proximity



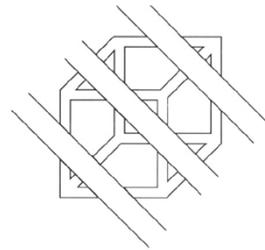
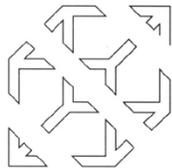
<http://www.capitol.edu/Resources/Images/outside/035.jpg>

Illusory/subjective contours

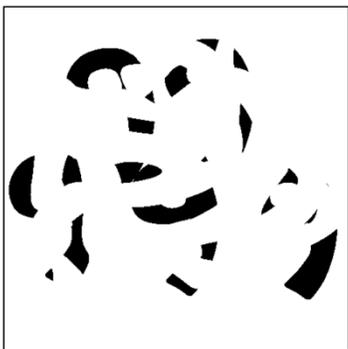


Interesting tendency to explain by occlusion

In Vision, D. Marr, 1982

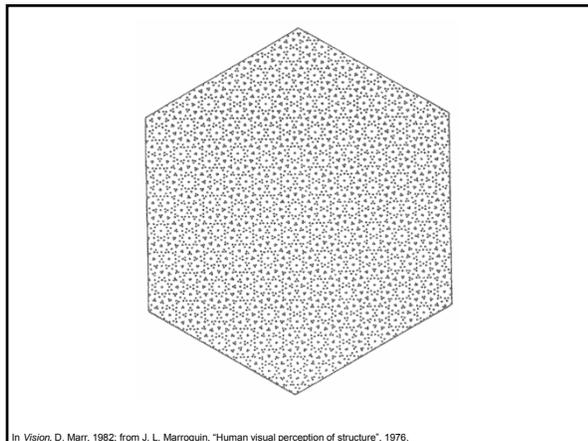
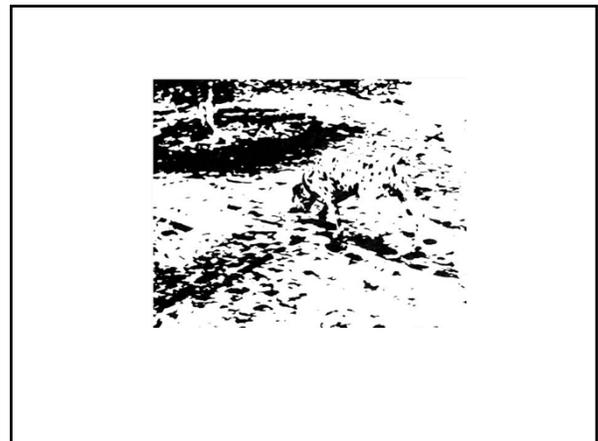
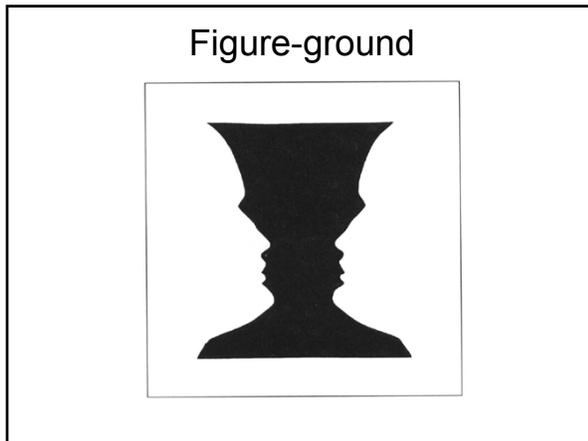


Continuity, explanation by occlusion



D. Forsyth





Grouping phenomena in real life

Forsyth & Ponce, Figure 14.7

Grouping phenomena in real life

Forsyth & Ponce, Figure 14.7

Gestalt

- Gestalt: whole or group
 - Whole is greater than sum of its parts
 - Relationships among parts can yield new properties/features
- Psychologists identified series of factors that predispose set of elements to be grouped (by human visual system)
- Inspiring observations/explanations; challenge remains how to best map to algorithms.

Outline

- What are grouping problems in vision?
- Inspiration from human perception
 - Gestalt properties
- Bottom-up segmentation via clustering
 - Algorithms:
 - Mode finding and mean shift: k-means, mean-shift
 - Graph-based: normalized cuts
 - Features: color, texture, ...
 - Quantization for texture summaries

The goals of segmentation

Separate image into coherent “objects”

image

human segmentation

Source: Lana Lazebnik

The goals of segmentation

Separate image into coherent “objects”

Group together similar-looking pixels for efficiency of further processing

“superpixels”

X. Ren and J. Malik. [Learning a classification model for segmentation](#), ICCV 2003.

Source: Lana Lazebnik

Image segmentation: toy example

input image

- These intensities define the three groups.
- We could label every pixel in the image according to which of these primary intensities it is.
 - i.e., *segment* the image based on the intensity feature.
- What if the image isn't quite so simple?

Kristen Grauman

input image

input image

Kristen Grauman

input image

- Now how to determine the three main intensities that define our groups?
- We need to *cluster*.

Kristen Grauman

0 190 255
intensity

- Goal: choose three "centers" as the **representative** intensities, and label every pixel according to which of these centers it is nearest to.
- Best cluster centers are those that minimize SSD between all points and their nearest cluster center c_i :

$$\sum_{\text{clusters } i} \sum_{\text{points } p \text{ in cluster } i} \|p - c_i\|^2$$

Kristen Grauman

Clustering

- With this objective, it is a "chicken and egg" problem:
 - If we knew the **cluster centers**, we could allocate points to groups by assigning each to its closest center.

- If we knew the **group memberships**, we could get the centers by computing the mean per group.

Kristen Grauman

K-means clustering

- Basic idea: randomly initialize the k cluster centers, and iterate between the two steps we just saw.
 1. Randomly initialize the cluster centers, c_1, \dots, c_k
 2. Given cluster centers, determine points in each cluster
 - For each point p , find the closest c_i . Put p into cluster i
 3. Given points in each cluster, solve for c_i
 - Set c_i to be the mean of points in cluster i
 4. If c_i have changed, repeat Step 2

Properties

- Will always converge to *some* solution
- Can be a "local minimum"
 - does not always find the global minimum of objective function:

$$\sum_{\text{clusters } i} \sum_{\text{points } p \text{ in cluster } i} \|p - c_i\|^2$$

Source: Steve Seitz

K-means

1. Ask user how many clusters they'd like. (e.g. $k=5$)

Andrew Moore

K-means

1. Ask user how many clusters they'd like. (e.g. $k=5$)
2. Randomly guess k cluster Center locations

Andrew Moore

K-means

1. Ask user how many clusters they'd like. (e.g. $k=5$)
2. Randomly guess k cluster Center locations
3. Each datapoint finds out which Center it's closest to. (Thus each Center "owns" a set of datapoints)

Andrew Moore

K-means

1. Ask user how many clusters they'd like. (e.g. $k=5$)
2. Randomly guess k cluster Center locations
3. Each datapoint finds out which Center it's closest to.
4. Each Center finds the centroid of the points it owns

Andrew Moore

K-means

1. Ask user how many clusters they'd like. (e.g. $k=5$)
2. Randomly guess k cluster Center locations
3. Each datapoint finds out which Center it's closest to.
4. Each Center finds the centroid of the points it owns...
5. ...and jumps there
6. ...Repeat until terminated!

Andrew Moore

K-means clustering

- Java demo:
<http://kovan.ceng.metu.edu.tr/~maya/kmeans/index.html>
http://home.dei.polimi.it/matteucc/Clustering/tutorial_html/AppletKM.html

K-means: pros and cons

Pros

- Simple, fast to compute
- Converges to local minimum of within-cluster squared error

Cons/issues

- Setting k ?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters
- Assuming means can be computed

An aside: Smoothing out cluster assignments

- Assigning a cluster label per pixel may yield outliers:

- How to ensure they are spatially smooth?

Segmentation as clustering

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **intensity** similarity

Feature space: intensity value (1-d)

quantization of the feature space; segmentation label map

Segmentation as clustering

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **color** similarity

Feature space: color value (3-d)

Kristen Grauman

Segmentation as clustering

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **intensity** similarity

Clusters based on intensity similarity don't have to be spatially coherent.

Kristen Grauman

Segmentation as clustering

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **intensity+position** similarity

Both regions are black, but if we also include **position (x,y)**, then we could group the two into distinct segments; way to encode both similarity & proximity.

Kristen Grauman

Segmentation as clustering

- Color, brightness, position alone are not enough to distinguish all regions...

Segmentation as clustering

Depending on what we choose as the *feature space*, we can group pixels in different ways.

Grouping pixels based on **texture** similarity

Feature space: filter bank responses (e.g., 24-d)

Recall: texture representation example

Windows with primarily horizontal edges

Both

Dimension 2 (mean d/dy value)

Dimension 1 (mean d/dx value)

Windows with small gradient in both directions

Windows with primarily vertical edges

statistics to summarize patterns in small windows

Kristen Grauman

Segmentation with texture features

- Find "textons" by clustering vectors of filter bank outputs
- Describe texture in a window based on *texton histogram*

Image

Texton map

Count

Texton index

Count

Texton index

Count

Texton index

Malik, Belongie, Leung and Shi. IJCV 2001.

Adapted from Lana Lazebnik

Image segmentation example

Texture-based regions

Color-based regions

Kristen Grauman

Pixel properties vs. neighborhood properties

query

query

These look very similar in terms of their color distributions (histograms).

How would their *texture* distributions compare?

Kristen Grauman

Material classification example

For an image of a single texture, we can classify it according to its global (image-wide) texton histogram.

Leaves

Wood

Grass

Foli

Veget

Stone

Labelled images complete training data

Figure from Varma & Zisserman, IJCV 2005

Material classification example

Nearest neighbor classification: label the input according to the nearest known example's label.

Query Image

Model

Plastic

Grass

$$\chi^2(h_i, h_j) = \frac{1}{2} \sum_{k=1}^K \frac{[h_i(k) - h_j(k)]^2}{h_i(k) + h_j(k)}$$

Manik Varma
<http://www.robots.ox.ac.uk/~vgg/research/textclass/with.html>

Outline

- What are grouping problems in vision?
- Inspiration from human perception
 - Gestalt properties
- Bottom-up segmentation via clustering
 - Algorithms:
 - Mode finding and mean shift: k-means, mean-shift
 - Graph-based: normalized cuts
 - Features: color, texture, ...
 - Quantization for texture summaries

K-means: pros and cons

Pros

- Simple, fast to compute
- Converges to local minimum of within-cluster squared error

Cons/issues

- Setting k?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters
- Assuming means can be computed

Mean shift algorithm

- The mean shift algorithm seeks *modes* or local maxima of density in the feature space

image

Feature space
($L^*u^*v^*$ color values)

Mean shift

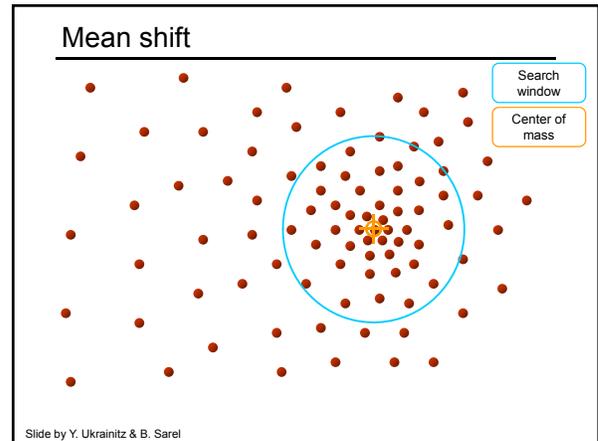
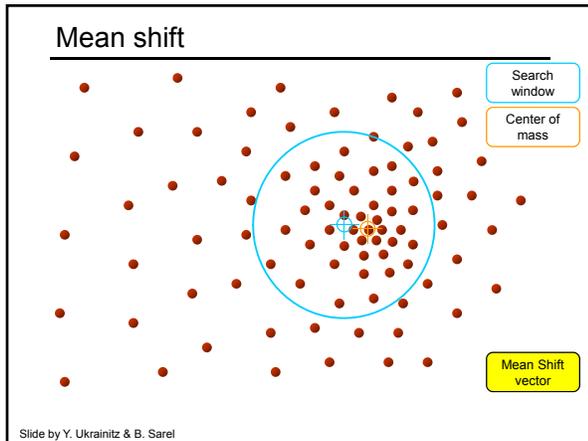
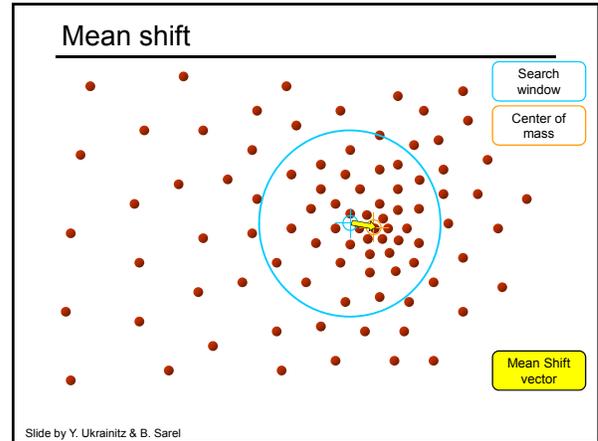
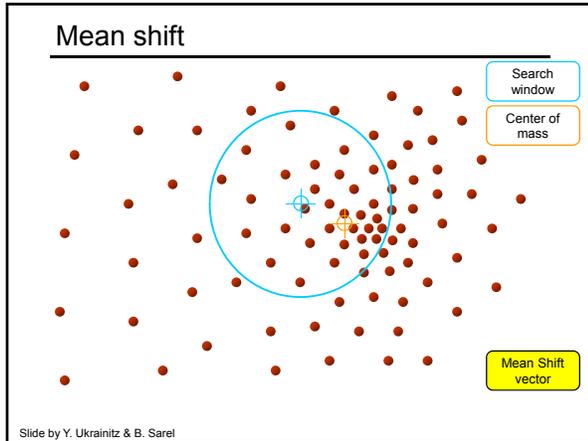
Slide by Y. Ukrainitz & B. Sarel

Mean shift

Slide by Y. Ukrainitz & B. Sarel

Mean shift

Slide by Y. Ukrainitz & B. Sarel



Mean shift clustering

- Cluster: all data points in the attraction basin of a mode
- Attraction basin: the region for which all trajectories lead to the same mode

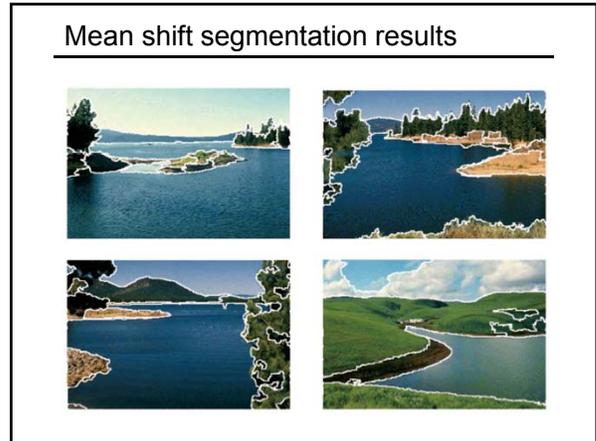
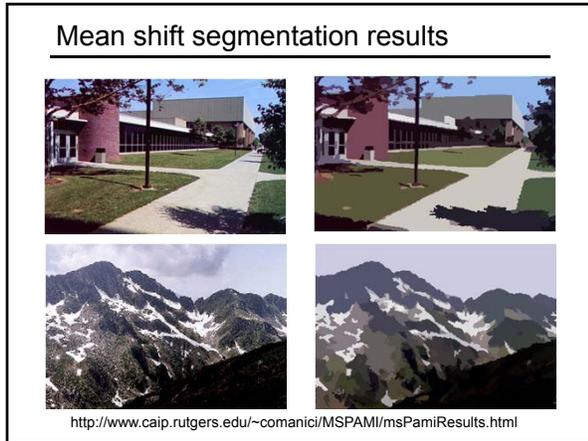
Slide by Y. Ukrainitz & B. Sarel

Mean shift clustering/segmentation

- Find features (color, gradients, texture, etc)
- Initialize windows at individual feature points
- Perform mean shift for each window until convergence
- Merge windows that end up near the same "peak" or mode

(a) (b)

Slide by Y. Ukrainitz & B. Sarel



- ### Mean shift
- **Pros:**
 - Does not assume shape on clusters
 - One parameter choice (window size)
 - Generic technique
 - Find multiple modes
 - **Cons:**
 - Selection of window size
 - Does not scale well with dimension of feature space
- Kristen Grauman

- ### Outline
- What are grouping problems in vision?
 - Inspiration from human perception
 - Gestalt properties
 - Bottom-up segmentation via clustering
 - Algorithms:
 - Mode finding and mean shift: k-means, mean-shift
 - Graph-based: normalized cuts
 - Features: color, texture, ...
 - Quantization for texture summaries

Images as graphs

Fully-connected graph

- node (vertex) for every pixel
- link between every pair of pixels, p, q
- affinity weight w_{pq} for each link (edge)
 - w_{pq} measures *similarity*
 - » similarity is *inversely proportional* to difference (in color and position...)

Source: Steve Seitz

Measuring affinity

- One possibility:

$$aff(x, y) = \exp\left\{-\left(\frac{1}{2\sigma_d^2}\right)(\|x - y\|^2)\right\}$$

Small sigma: group only nearby points

Large sigma: group distant points

Kristen Grauman

Measuring affinity

Data points

$\sigma=2$

Affinity matrices

$\sigma=1$ $\sigma=2$ $\sigma=1$

Segmentation by Graph Cuts

Break Graph into Segments

- Want to delete links that cross **between** segments
- Easiest to break links that have low similarity (low weight)
 - similar pixels should be in the same segments
 - dissimilar pixels should be in different segments

Source: Steve Seitz

Cuts in a graph: Min cut

Link Cut

- set of links whose removal makes a graph disconnected
- cost of a cut: $cut(A, B) = \sum_{p \in A, q \in B} w_{p,q}$

Find minimum cut

- gives you a segmentation
- fast algorithms exist for doing this

Source: Steve Seitz

Minimum cut

- Problem with minimum cut: Weight of cut proportional to number of edges in the cut; tends to produce small, isolated components.

Fig. 1. A case where minimum cut gives a bad partition.

[Shi & Malik, 2000 PAMI]

Cuts in a graph: Normalized cut

Normalized Cut

- fix bias of Min Cut by **normalizing** for size of segments:

$$Ncut(A, B) = \frac{cut(A, B)}{assoc(A, V)} + \frac{cut(A, B)}{assoc(B, V)}$$

$assoc(A, V)$ = sum of weights of all edges that touch A

- Ncut value small when we get two clusters with many edges with high weights, and few edges of low weight between them
- Approximate solution for minimizing the Ncut value : generalized eigenvalue problem.

Source: Steve Seitz

Example results

Results: Berkeley Segmentation Engine

<http://www.cs.berkeley.edu/~fowlkes/BSE/>

Normalized cuts: pros and cons

Pros:

- Generic framework, flexible to choice of function that computes weights ("affinities") between nodes
- Does not require model of the data distribution

Cons:

- Time complexity can be high
 - Dense, highly connected graphs → many affinity computations
 - Solving eigenvalue problem
- Preference for balanced partitions

Kristen Grauman

Segments as primitives for recognition

Multiple segmentations

B. Russell et al., "Using Multiple Segmentations to Discover Objects and their Extent in Image Collections," CVPR 2006 Slide credit: Lana Lazebnik

Top-down segmentation

E. Borenstein and S. Ullman, "Class-specific, top-down segmentation," ECCV 2002
 A. Levin and Y. Weiss, "Learning to Combine Bottom-Up and Top-Down Segmentation," ECCV 2006. Slide credit: Lana Lazebnik

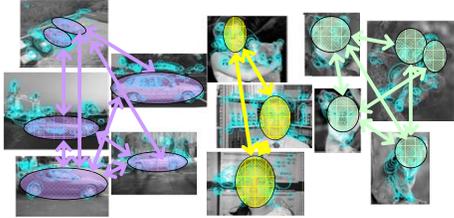
Top-down segmentation

E. Borenstein and S. Ullman, "Class-specific, top-down segmentation," ECCV 2002
 A. Levin and Y. Weiss, "Learning to Combine Bottom-Up and Top-Down Segmentation," ECCV 2006. Slide credit: Lana Lazebnik

Motion segmentation

A. Barbu, S.C. Zhu. Generalizing Swendsen-Wang to sampling arbitrary posterior probabilities, *IEEE Trans. PAMI*, August 2005.
Kristen Grauman

Image grouping



K. Grauman & T. Darrell, Unsupervised Learning of Categories from Sets of Partially Matching Image Features, CVPR 2006.
Kristen Grauman

Summary

- Segmentation to find object boundaries or mid-level regions, tokens.
- Bottom-up segmentation via clustering
 - General choices -- features, affinity functions, and clustering algorithms
- Grouping also useful for quantization, can create new feature summaries
 - Texton histograms for texture within local region
- Example clustering methods
 - K-means
 - Mean shift
 - Graph cut, normalized cuts

Coming up

- Pset 1 due Mon 11:59 PM
- Fitting
 - 4.3.2
 - 5.1.1

