

# Network Anomography

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Joint work with  
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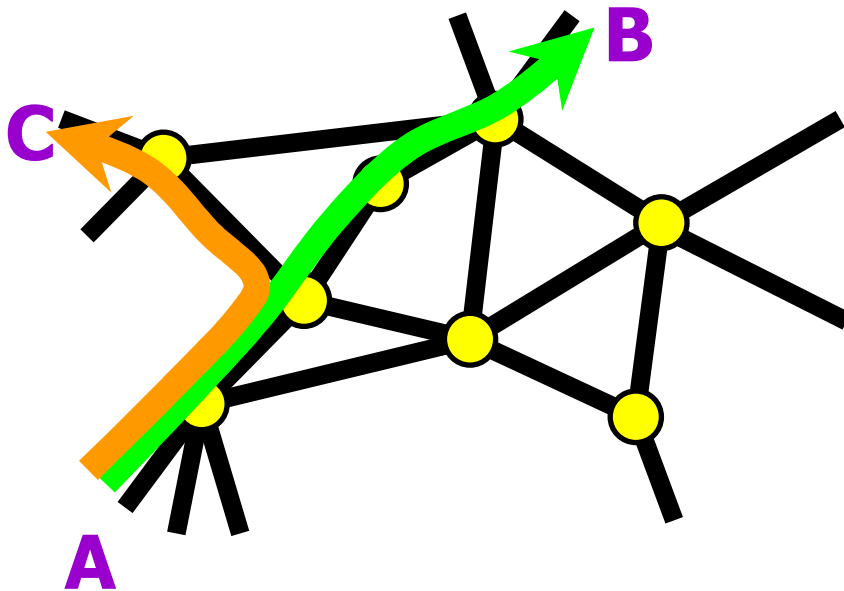
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Berkeley, CA, USA

# Network Anomaly Detection

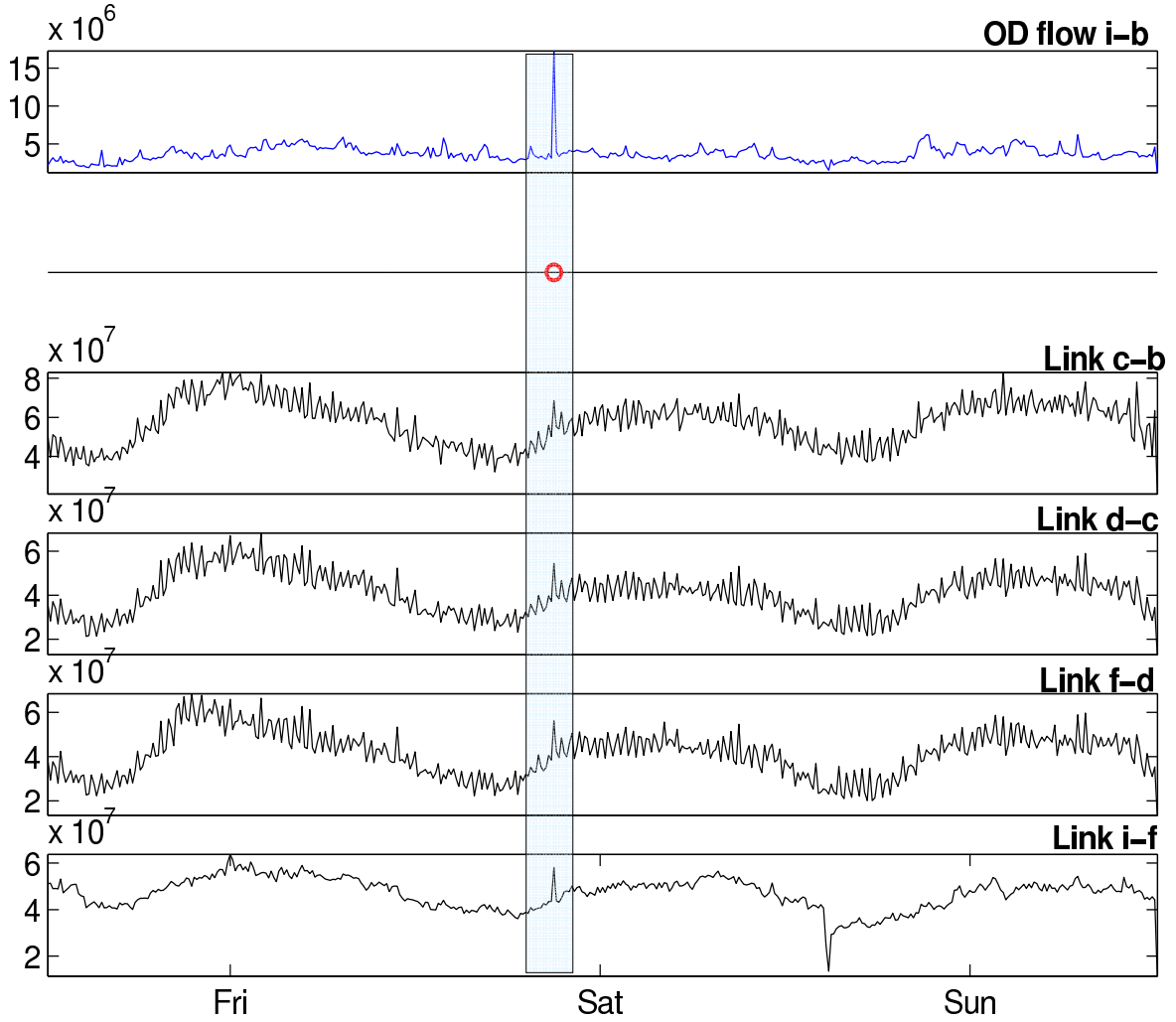
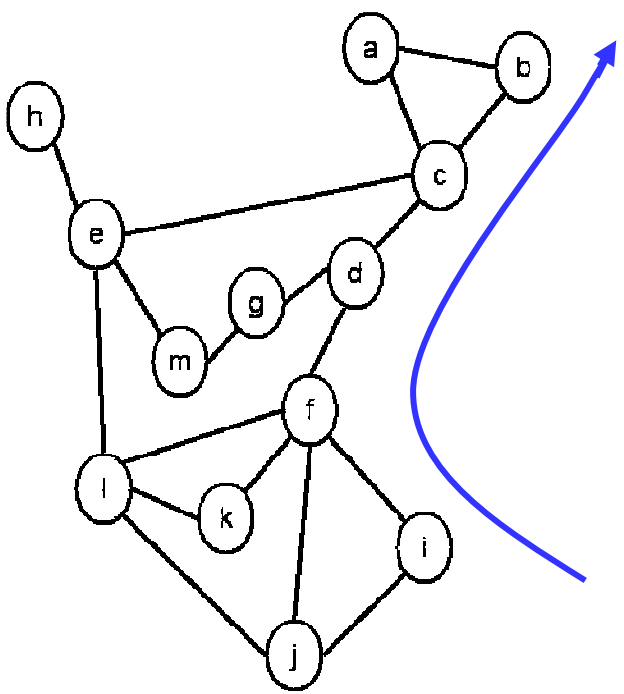
- Is the network experiencing unusual conditions?
  - Call these conditions anomalies
  - Anomalies can often indicate network problems
    - DDoS, worms, flash crowds, outages, misconfigurations ...
  - Need rapid detection and diagnosis
    - Want to fix the problem quickly
- Questions of interest
  - Detection
    - Is there an unusual event?
  - Identification
    - What's the best explanation?
  - Quantification
    - How serious is the problem?

# Network Anomography

- What we want
  - **Volume anomalies** [Lakhina04]  
Significant changes in an Origin-Destination flow, i.e., traffic matrix element
- What we have
  - **Link traffic measurements**
  - It is difficult to measure traffic matrix directly
- Network Anomography
  - Infer volume anomalies from link traffic measurements



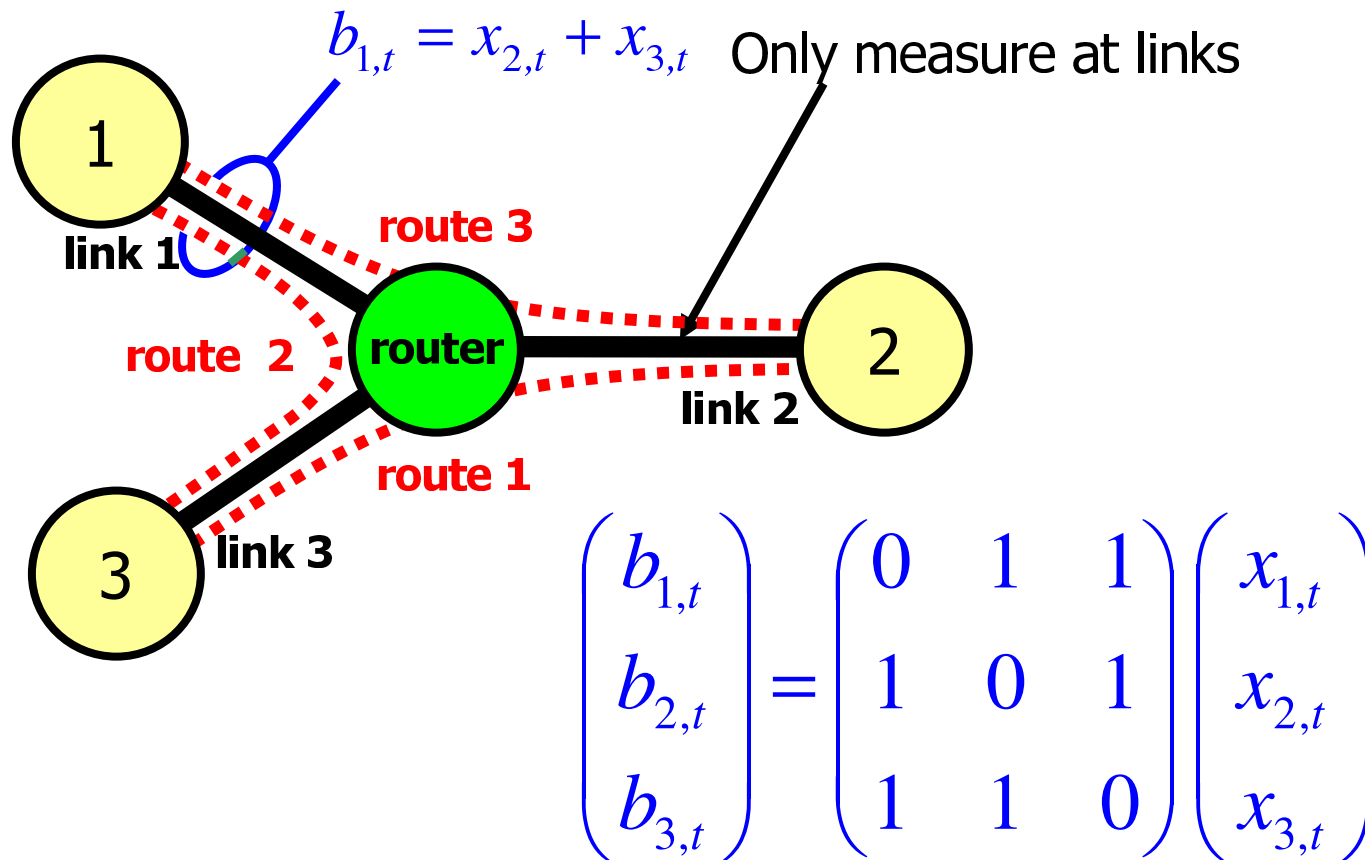
# An Illustration



Courtesy: Anukool Lakhina [Lakhina04]

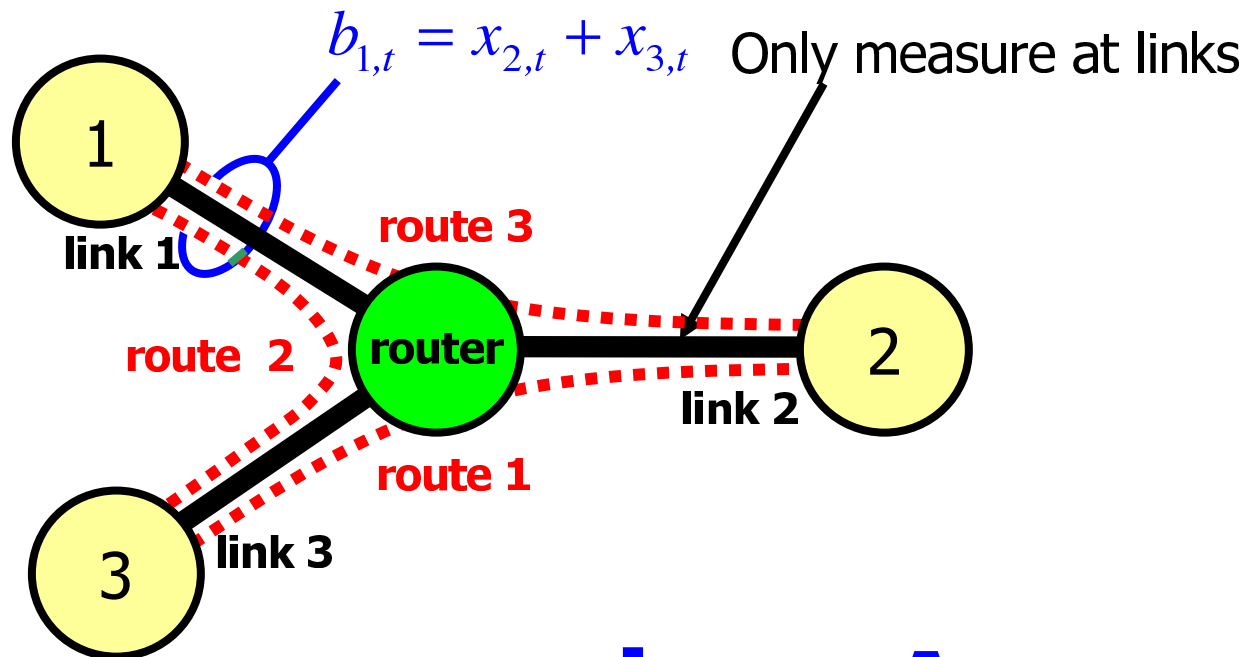
Anomography =  
Anomalies + Tomography

# Mathematical Formulation



Problem: Infer changes in TM elements ( $x_t$ ) given link measurements ( $b_t$ )

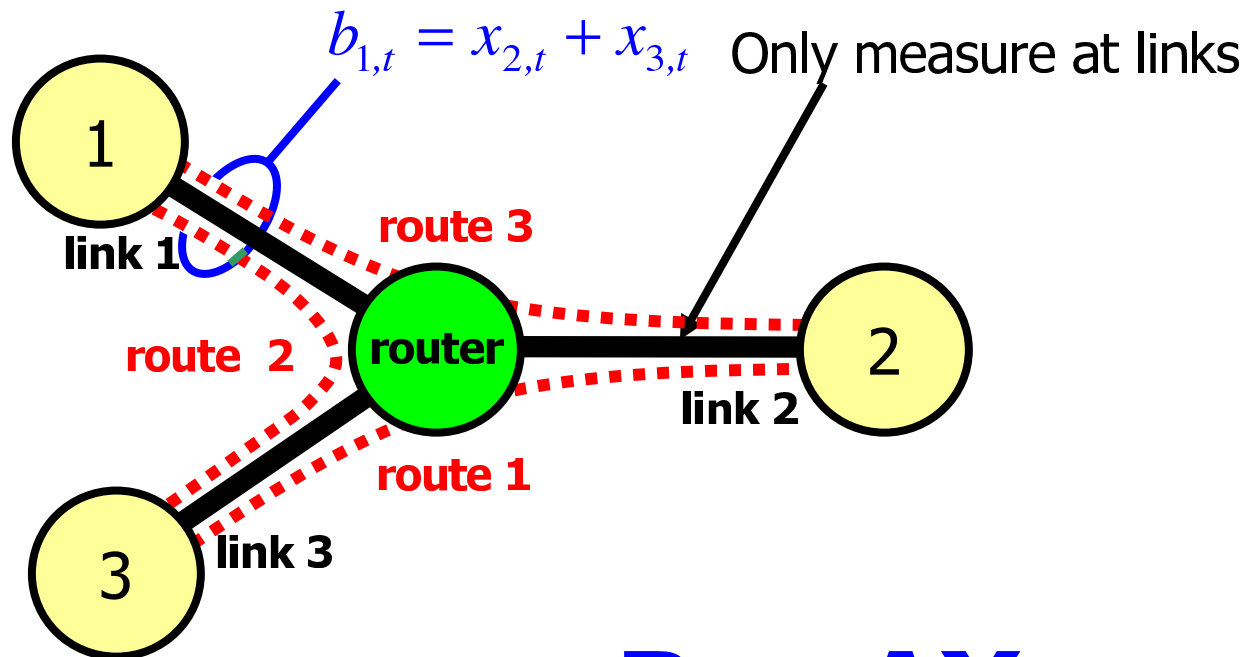
# Mathematical Formulation



$$\mathbf{b}_t = \mathbf{A}_t \mathbf{x}_t \quad (t=1, \dots, T)$$

Typically massively under-constrained!

# Static Network Anomography



$$\mathbf{B} = \mathbf{A}\mathbf{X}$$

Time-invariant  $A_t (= A)$ ,  $B = [b_1 \dots b_T]$ ,  $X = [x_1 \dots x_T]$



# Anomography Strategies

- Early Inverse

1. Inversion

- Infer OD flows  $X$  by solving  $b_t = Ax_t$

2. Anomaly extraction

- Extract volume anomalies  $\tilde{X}$  from inferred  $X$

**Drawback: errors in step 1 may contaminate step 2**

- Late Inverse

1. Anomaly extraction

- Extract link traffic anomalies  $\tilde{B}$  from  $B$

2. Inversion

- Infer volume anomalies  $\tilde{X}$  by solving  $\tilde{b}_t = A\tilde{x}_t$

**Idea: defer "lossy" inference to the last step**

# Extracting Link Anomalies $\tilde{B}$

- Temporal Anomography:  $\tilde{B} = BT$ 
  - ARIMA modeling
    - Diff:  $f_t = b_{t-1}$   $\tilde{b}_t = b_t - f_t$
    - EWMA:  $f_t = (1-\alpha) f_{t-1} + \alpha b_{t-1}$   $\tilde{b}_t = b_t - f_t$
  - Fourier / wavelet analysis
    - Link anomalies = the high frequency components
  - Temporal PCA
    - PCA = Principal Component Analysis
    - Project columns onto principal link column vectors
  
- Spatial Anomography:  $\tilde{B} = TB$ 
  - Spatial PCA [Lakhina04]
    - Project rows onto principal link row vectors

# Extracting Link Anomalies $\tilde{B}$

- Temporal Anomography:  $\tilde{B} = BT$ 
  - Self-consistent
    - Tomography equation:  $B = AX$
    - Post-multiply by T:  $BT = AXT$   
 $\tilde{B} = A\tilde{X}$
  
- Spatial Anomography:  $\tilde{B} = TB$ 
  - No longer self-consistent

## Solving $\tilde{\mathbf{b}}_t = \mathbf{A} \tilde{\mathbf{x}}_t$

- Pseudoinverse:  $\tilde{\mathbf{x}}_t = \text{pinv}(\mathbf{A}) \tilde{\mathbf{b}}_t$ 
  - Shortest minimal  $L_2$ -norm solution
    - Minimize  $|\tilde{\mathbf{x}}_t|_2$  subject to  $|\tilde{\mathbf{b}}_t - \mathbf{A} \tilde{\mathbf{x}}_t|_2$  is minimal
  
- Maximize sparsity (i.e. minimize  $|\tilde{\mathbf{x}}_t|_0$ )
  - $L_0$ -norm is not convex  $\Rightarrow$  hard to minimize
  - Greedy heuristic
    - Greedily add non-zero elements to  $\tilde{\mathbf{x}}_t$
    - Minimize  $|\tilde{\mathbf{b}}_t - \mathbf{A} \tilde{\mathbf{x}}_t|_2$  with given  $|\tilde{\mathbf{x}}_t|_0$
  - $L_1$ -norm approximation
    - Minimize  $|\tilde{\mathbf{x}}_t|_1$  (can be solved via LP)
    - With noise  $\Rightarrow$  minimize  $|\tilde{\mathbf{x}}_t|_1 + \lambda |\tilde{\mathbf{b}}_t - \mathbf{A} \tilde{\mathbf{x}}_t|_1$

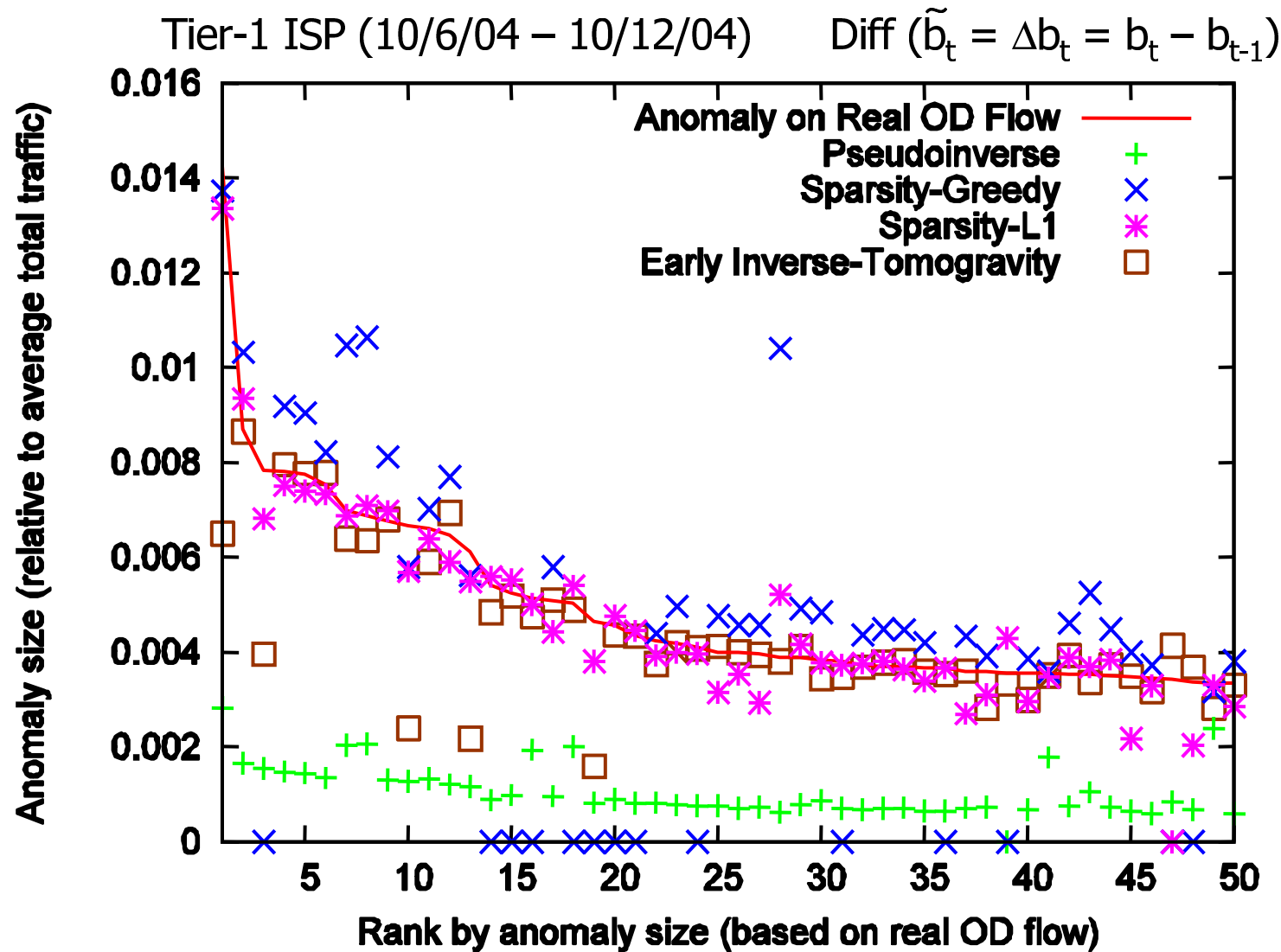
# Dynamic Network Anomography

- Time-varying  $A_t$  is common
  - Routing changes
  - Missing data
    - Missing traffic measurement on a link  $\Leftrightarrow$  setting the corresponding row of  $A_t$  to 0 in  $b_t = A_t x_t$
- Solution
  - Early inverse: Directly applicable
  - Late inverse: Apply ARIMA modeling
    - $L_1$ -norm minimization subject to link constraints
      - minimize  $|\tilde{x}_t|_1$
      - subject to  $\tilde{x}_t = x_t - x_{t-1}, b_t = A_t x_t, b_{t-1} = A_{t-1} x_{t-1}$
    - Reduce problem size by eliminating redundancy

# Performance Evaluation: Inversion

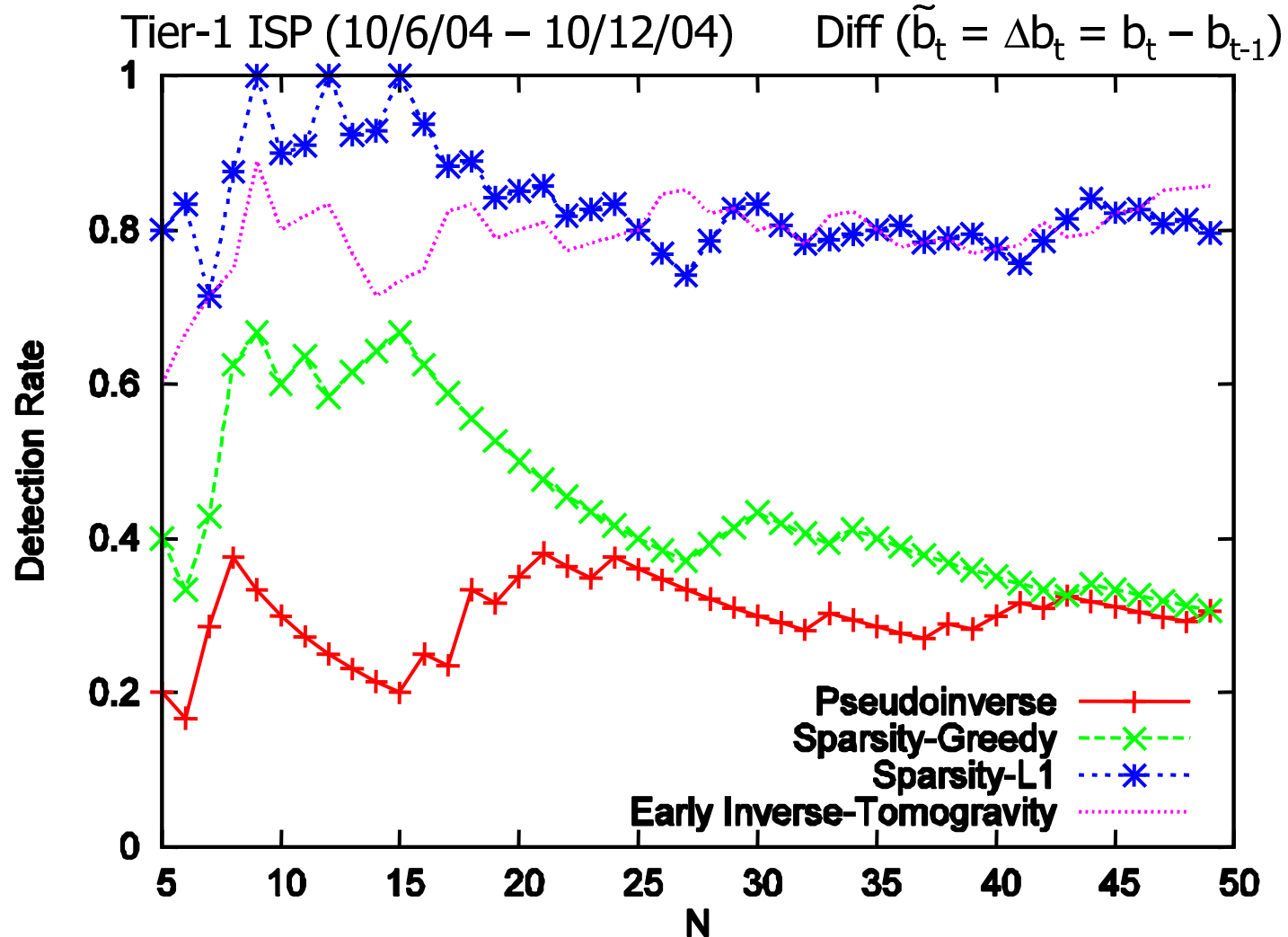
- Fix one anomaly extraction method
- Compare "real" and "inferred" anomalies
  - "real" anomalies: directly from OD flow data
  - "inferred" anomalies: from link data
- Order them by size
  - Compare the size
- How many of the top N do we find
  - Gives detection rate:  $| \text{top } N_{\text{real}} \cap \text{top } N_{\text{inferred}} | / N$

# Inference Accuracy



Sparsity-L1 works best among all inference techniques

# Inference Accuracy

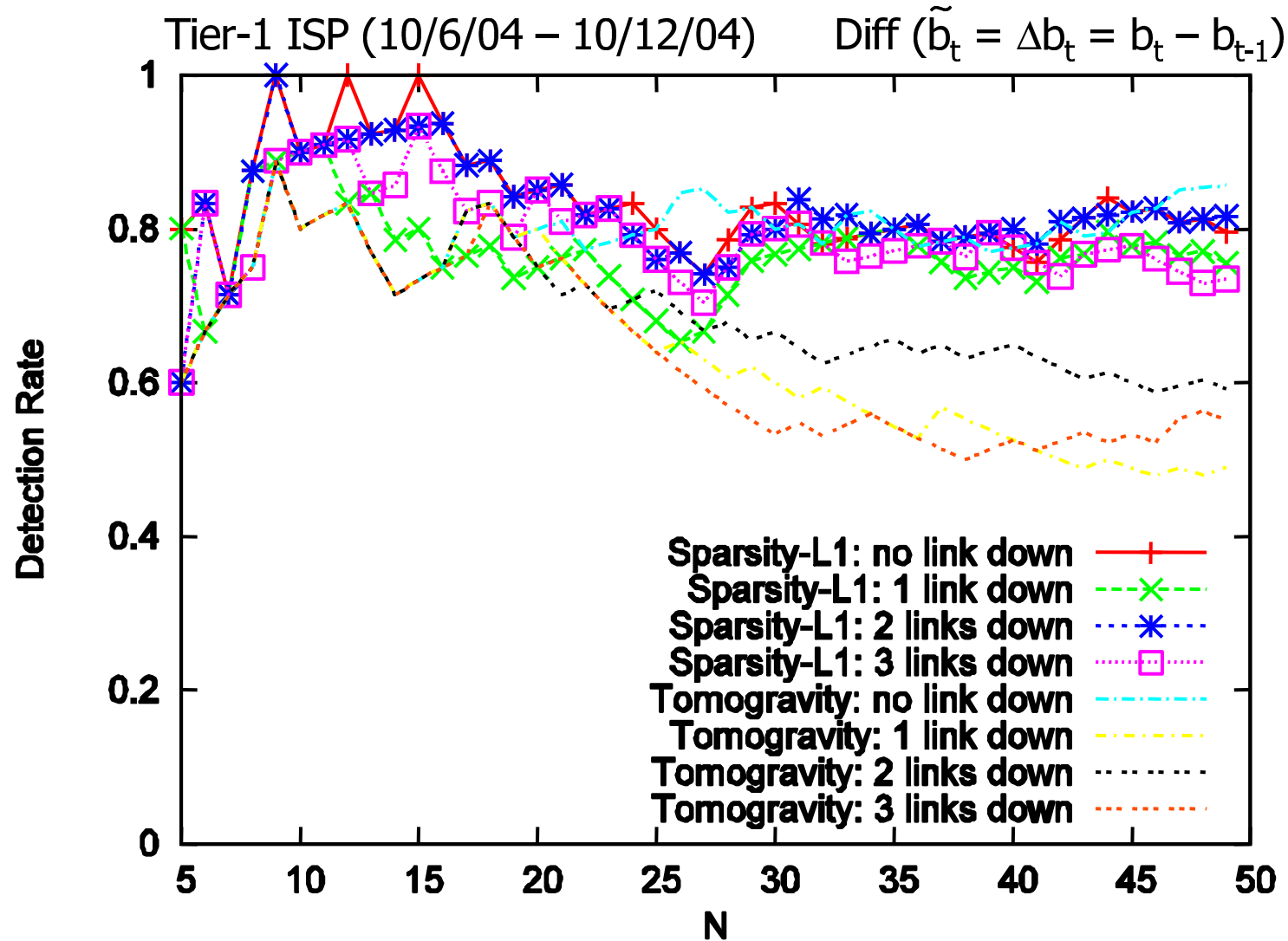


$$\text{detection rate} = | \text{top } N_{\text{real}} \cap \text{top } N_{\text{inferred}} | / N$$

Sparsity-L1 works best among all inference techniques



# Impact of Routing Changes



Late inverse (sparsity-L1) beats early inverse (tomogravity)

# Performance Evaluation: Anomography

- Hard to compare performance
  - Lack ground-truth: what is an anomaly?
- So compare events from different methods
  - Compute top  $M$  "benchmark" anomalies
    - Apply an anomaly extraction method directly on OD flow data
  - Compute top  $N$  "inferred" anomalies
    - Apply another anomography method on link data
  - Report  $\min(M, N) - | \text{top } M_{\text{benchmark}} \cap \text{top } N_{\text{inferred}} |$ 
    - $M < N \Rightarrow$  "false negatives"
      - # big "benchmark" anomalies not considered big by anomography
    - $M > N \Rightarrow$  "false positives"
      - # big "inferred" anomalies not considered big by benchmark method
  - Choose  $M, N$  similar to numbers of anomalies a provider is willing to investigate, e.g. 30-50 per week

# Anomography: "False Negatives"

Top 50 Inferred	"False Negatives" with Top 30 Benchmark							
	Diff	EWMA	H-W	ARIMA	Fourier	Wavelet	T-PCA	S-PCA
Diff	<u>0</u>	0	1	1	5	5	17	12
EWMA	0	<u>0</u>	1	1	5	5	17	12
Holt-Winters	1	1	<u>0</u>	0	6	4	18	12
ARIMA	1	1	0	<u>0</u>	6	4	18	12
Fourier	3	4	8	8	<u>1</u>	7	19	18
Wavelet	0	1	2	2	5	<u>0</u>	13	11
T-PCA	14	14	14	14	19	15	<u>3</u>	15
S-PCA	10	10	13	13	15	11	1	<u>13</u>

1. Diff/EWMA/H.-W./ARIMA/Fourier/Wavelet all largely consistent
2. PCA methods not consistent (even with each other)
  - PCA cannot detect anomalies in the "normal" subspace
  - PCA insensitive to reordering of  $[b_1 \dots b_T] \Rightarrow$  cannot utilize all temporal info
3. Spatial methods (e.g. spatial PCA) are not self-consistent

# Anomography: "False Positives"

Top 30 Inferred	"False Positives" with Top 50 Benchmark							
	Diff	EWMA	H-W	ARIMA	Fourier	Wavelet	T-PCA	S-PCA
Diff	<u>3</u>	3	6	6	6	4	14	14
EWMA	3	<u>3</u>	6	6	7	5	13	15
Holt-Winters	4	4	<u>1</u>	1	8	3	13	10
ARIMA	4	4	1	<u>1</u>	8	3	13	10
Fourier	6	6	7	6	<u>2</u>	6	19	18
Wavelet	6	6	6	6	8	<u>1</u>	13	12
T-PCA	17	17	17	17	20	13	<u>0</u>	14
S-PCA	18	18	18	18	20	14	1	<u>14</u>

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# Summary of Results

- Inversion methods
  - Sparsity-L1 beats Pseudoinverse and Sparsity-Greedy
  - Late-inverse beats early-inverse
- Anomography methods
  - Diff/EWMA/H-W/ARIMA/Fourier/Wavelet all largely consistent
  - PCA methods not consistent (even with each other)
    - PCA methods cannot detect anomalies in "normal" subspace
    - PCA methods cannot fully exploit temporal information in  $\{x_t\}$ 
      - Reordering of  $[b_1 \dots b_T]$  doesn't change results!
  - Spatial methods (e.g. spatial PCA) are not self-consistent
    - Temporal methods are
- The method of choice: ARIMA + Sparsity-L1
  - Accurate, consistent with Fourier/Wavelet
  - Robust against measurement noise, insensitive to choice of  $\lambda$
  - Works well in the presence of missing data, routing changes
  - Supports both online and offline analysis

# Conclusions

- **Anomography = Anomalies + Tomography**
  - Find anomalies in  $\{x_t\}$  given  $b_t = A_t x_t$  ( $t=1, \dots, T$ )
- **Contributions**
  1. A general framework for anomography methods
    - Decouple anomaly extraction and inference components
  2. A number of novel algorithms
    - Taking advantage of the range of choices for anomaly extraction and inference components
    - Choosing between spatial vs. temporal approaches
  3. The first algorithm for dynamic anomography
  4. Extensive evaluation on real traffic data
    - 6-month Abilene and 1-month Tier-1 ISP
- **The method of choice: ARIMA + Sparsity-L1**

# Future Work

- Correlate traffic with other types of data
  - BGP routing events
  - Router CPU utilization
- Anomaly response
  - Maybe with an effective response system, false positives become less important?
- Anomography for performance diagnosis
  - Inference of link performance based on end-to-end measurements can be formulated as  $b_t = Ax_t$
- Beyond networking
  - Detecting anomalies in other inverse problems
  - Are we just reinventing the wheel?

Thank you !