# A Tutorial on Feature Oriented Programming and the AHEAD Tool Suite

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**Abstract.** *Feature oriented programming (FOP)* is the study of feature modularity and its use in program synthesis. AHEAD is a theory of FOP that is based on a fundamental concept of generative programming that functions map programs. This enables the design of programs to be expressed compositionally as algebraic expressions, which are suited for automated analysis, manipulation, and program synthesis. This paper is a tutorial on FOP and AHEAD. We review AHEAD's theory and the tool set that implements it.

# **1** Introduction

*Software engineering (SE)* is in a perpetual crisis. Software products are increasing in complexity, the cost to develop and maintain systems is skyrocketing, and our ability to understand systems is decreasing. A basic goal of SE is to successfully manage and control *complexity*; the "crisis" indicates that SE technologies are failing to achieve this goal. There are many culprits. One surely is that today's software design and implementation techniques are simply too low-level, exposing far more detail than is necessary to make a program's design, construction, and ease of modification simple. Future software design technologies will need to do better, and it should not be surprising that they will be different from those of today.

Looking to the future, SE paradigms will likely embrace:

- generative programming (GP)
- domain-specific languages (DSLs)
- automatic programming (AP)

GP is about automating software development. Eliminating the task of writing mundane and rote programs is a motherhood to improved programmer productivity and program quality. Program synthesizers will transform input specifications into target programs. These specifications will not be written in Java or C# — which are too lowlevel — but rather in high-level notations called DSLs that are specific to a particular domain. DSL programs are known to be both easier to write and maintain than their low-level (e.g., Java) counterparts. Ideally, DSLs will be declarative, allowing their users to define *what* is needed and leave it up to the DSL compiler to produce an efficient program automatically that does the *how* part. But placing the burden of program synthesis on a DSL compiler should not be taken lightly. This involves the problem of AP; it is a technical problem of great difficulty, as little progress has been made in the last 25 years to produce demonstrably efficient programs from declarative specs. Advancement on all three fronts (GP, DSLs, and AP) are needed before the crisis in SE will noticeably diminish.

While it is wishful thinking that simultaneous advances on all three fronts is possible, it is worth noting that a spectacular example of this futuristic SE paradigm was realized over 25 years ago — ironically around the time when most people were giving up on AP [2]. Furthermore, this work had a fundamental impact on commercial applications. The example is relational query optimization [20]. SQL is a prototypical DSL: it is a *declarative language* for retrieving data from tables. An SQL compiler translates an SQL statement into a relational algebra expression. A query optimizer accomplishes the goal of *automatic programming* by applying algebraic identities to automatically rewrite — and hence optimize — relational algebra expressions. The task of translating an optimized expression into an efficient program is an example of *generative programming*.

Relational optimizers revolutionized databases: data retrieval programs that were hard to write, hard to optimize, and hard to maintain are now produced automatically. There is nothing special about data retrieval programs: all interesting programs are hard to write, optimize, and maintain. Thus if ever there was a "grand challenge" for SE, it would be to replicate the success of relational query optimization in other domains.

AHEAD is a theory of *feature oriented programming (FOP)* that shows how the concepts and framework of relational query optimization generalize to other domains. ATS is a suite of tools that implement the AHEAD theory.

### 1.1 Background

How do you describe a program that you've written to a prospective customer? You are unlikely to recite what DLLs you're using — because the customer would unlikely have any interest in such details. Instead, you would take a more promising tact of explaining the *features* — increments in program functionality — that your program offers its clients. This works because clients know their requirements and can see how features satisfy requirements.

Programs come in different flavors, e.g., entry-level through deluxe. The differences between these categories are the presence or absence of features (or more commonly, sets of features). Entry-level versions have a minimal feature set; deluxe advertises the most.

But if we describe programs by features or differentiate programs by features, why can't we build programs (or program families) from feature specifications? In fact, we can. This is the area of research called *product-lines*. The ability to add and remove features suggests that features can be modularized. While it is possible to construct product-lines without modularizing features (e.g., through the extensive use of **#if**-

**#endif** preprocessor declarations), we focus on a particular sub-topic of product-line research that deals with feature modularization. By making features first-class design and implementation entities, it is easier to add and remove features from applications. (In fact, this is a capability that most of us wish we had today — the ability to add and remove features from our programs. We don't have it now; the purpose of this paper is to explain how it can be done in a general way). It happens that feature modularity goes far beyond conventional notions of code modularity. This, among other things, makes it a very interesting topic.

*Feature oriented programming (FOP)* is the study of feature modularity and programming models that support feature modularity. A powerful form of FOP is based on a methodology called *step-wise development (SWD)*. SWD is both simple and ancient: it advocates that complex programs can be constructed from simple programs by incrementally adding details. When incremental units of change are features, FOP and SWD converge. This is the starting point of AHEAD and ATS. But what is a feature? How is it represented? And how are features and their compositions modeled?

#### 1.2 A Clue

Consider any Java class c. A class member could be a data field or a method. Class c below has four members m1—m4.

```
class C {
   member m1;
   member m2;
   member m3;
   member m4;
}
```

(1)

Have you ever noticed that there is no unique definition for c? The members of c could be defined in a single class as above, or distributed over an inheritance hierarchy of arbitrary height. One possibility is to have class c1 encapsulate member m1 and c23 encapsulate members m2 and m3:

```
class C1 { member m1; }
class C23 extends C1 {
    member m2;
    member m3;
}
class C4 extends C23 { member m4; }
class C extends C4 {}
    (2)
```

From a programmatic viewpoint, both definitions of c, namely (1) and (2), are indestinguishable. In fact, we could further decompose c23 to be:

```
class C2 extends C1 { member m2; }
class C3 extends C2 { member m3; }
class C23 extends C3 {}
```

and the definition of c would not change; it would still have members m1—m4. Moreover, there's nothing really special about the placement of member m1 (or m2...) in this hierarchy. If method m1 references other members, as long as these members are not defined lower in the inheritance chain than m1, m1 can appear in any class of that chain.

If you recall your high school or college courses on algebra, you may recognize these ideas. Consider sets and the union operation. We can define the sets:

```
C1 = { m1 }

C2 = { m2 }

C3 = { m3 }

C4 = { m4 }

C23 = C2 \cup C3

C = C1 \cup C23 \cup C4 = C1 \cup C2 \cup C3 \cup C4
```

Union is commutative, which means that the order in which the union of sets is taken doesn't matter. This is similar to, but not the same as, inheritance because as we saw, a method can be added only as long as members it references are not defined in subclasses.

Something a bit closer to inheritance are vectors and the vector operations of addition(+) and movement( $\rightarrow$ ). Suppose we define vectors in 4-space:

C1 = (m1,0,0,0) C2 = (0,m2,0,0) C3 = (0,0,m3,0)C4 = (0,0,0,m4)

You know about vector addition; vector movement is the path that is followed when laying vectors end-to-end. Vector addition is commutative; vector movement is not:

 $\begin{array}{rcl} C &= & (m1,m2,m3,m4) &= & C1 &+ & C2 &+ & C3 &+ & C4 \\ C1 &+ & C2 &+ & C3 &+ & C4 &= & C4 &+ & C3 &+ & C2 &+ & C1 \\ C1 &\to & C2 &\to & C3 &\to & C4 &\neq & C4 &\to & C3 &\to & C2 &\to & C1 \end{array}$ 

Inheritance has the flavor of both vector arithmetic and vector movement.

When you think about an *operation* for inheritance, what you are really defining is an operation for class extension. A *class extension* can add new members and extend existing methods of a class. Here's an example. Suppose a program  $\mathbf{P}$  has a single class  $\mathbf{B}$  that initially contains a single data member  $\mathbf{x}$ :

class B { int x; } // program P

Suppose an extension  $\mathbf{R}$  of program  $\mathbf{P}$  adds data member  $\mathbf{y}$  and method  $\mathbf{z}$  to class  $\mathbf{B}$ . Let us write this extension as:

```
refines class B { // extension R
int y;
void z() {...}
} (3)
```

where "refines" is a keyword modifier to mean extension. The composition of  $\mathbf{R}$  with  $\mathbf{P}$  defines a new program  $\mathbf{N}$  with a single class, namely  $\mathbf{B}$ , with three members:

In effect, this composition is expressed by the following inheritance chain, called an *extension chain*:

```
class B_P { int x; }

class B_R extends B_P {

int y;

void z() {...}

}

class B_N extends B_R {} (5)
```

where subscripts indicate the program or extension from which that fragment of  $\mathbf{B}$  is defined.

We can express these ideas algebraically in terms of "values" and "functions". Program P is a *value* — it defines a base artifact. An extension is a *function* that maps programs, so R is a function. A composition is an expression. We can model (5) as the equation N = R(P) or  $N = R^{\bullet}P$ , where  $\bullet$  denotes function composition.

We can express our previous example about class c in this manner. Here is one way: let c1 be a value and c2, c3, and c4 be the extensions:

```
class C { member m1; }// value C1refines class C { member m2; }// function C2refines class C { member m3; }// function C3refines class C { member m4; }// function C4
```

Now, class c of (1) can be synthesized by *evaluating* the expression  $c4 \cdot c3 \cdot c2 \cdot c1$ . The expression —  $c4 \cdot c3 \cdot c2 \cdot c1$  — is called the *design* of c. Taking this idea further, we see that c23 has an obvious representation as a composite function or composite extension:

C23 = C2•C3

which represents the code:

```
refines class C {
    member m2;
    member m3;
}
```

There are loose ends to tie up before a bigger picture emerges. First, there's scalability. The effects of a program extension need not be limited to a single Java class. In fact, it is common for a "large-scale" extension to encapsulate multiple class extensions as well as new classes. That is, such an extension would augment existing classes of a program with new members and extend existing methods, but would also introduce new classes that could be subsequently augmented.

(4)

Second, program extensions have meaning when they encapsulate the implementation of a feature. Have you ever added a new feature to an existing program? You discover that you often have to extend a number of classes, as well as add new classes to a program. Well, a feature is a "large scale" program extension.

Third, in product-line design, features are stereo-typical units of application design that can be composed with other features to produce customized programs. A model of a product-line — called a *domain model* — is a set of values and functions each representing a particular feature, that can be composed to synthesize customized programs.

Fourth, recall that a key to the success of relational query optimizers is that they used expressions to represent program designs. That is, a data retrieval program is defined by a composition of relational algebra operations. To see the generalization, a domain model is an *algebra* — a set of operations ("values" and "functions") whose compositions define the space of programs that can be synthesized. Given an algebra, there will always be algebraic identities among operations. These identities can be used to optimize algebraic expression definitions of programs, just like relational algebra expressions can be optimized. (Some domains will have more interesting optimizations than others).

Fifth, what is *design*? If you think about it, this is a *really* hard question to answer, because it is asking for a clear articulation of a deeply intuitive idea. Our discussions offer a simple answer: a program is a value. The design of a program is the expression that produces its value. If multiple expressions produce the same value, then these expressions represent equivalent designs of that program.

Now, let's consider a more precise way to express these ideas.

# 2 A Model of FOP

Salient ideas of FOP as expressed by two models: GenVoca and its successor AHEAD.

### 2.1 GenVoca

GenVoca is a design methodology for creating application families and architecturallyextensible software, i.e., software that is customizable via feature addition and removal [3]. It follows traditional step-wise development with one major difference: instead of composing thousands of microscopic program extensions (e.g.,  $x+1 \Rightarrow inc(x)$ ) to yield admittedly small programs, GenVoca scales extensions so that each adds a feature to a program, and composing few extensions yields an entire program.

In GenVoca, programs are *values* and program extensions are *functions*. Consider the following values that represent base programs with different features:

f	//	program	with	feature	f
a	11	program	with	feature	g

A program extension is a function that takes a program as input and produces a feature-augmented program as output:

i●x	11	adds	feature	i	to	program	х
j●x	//	adds	feature	j	to	program	x

A multi-featured application is an *equation* that is a named expression. Different equations define a family of applications, such as:

app1 = i●f	<pre>// app1 has features i and f</pre>
app2 = j●g	<pre>// app2 has features j and g</pre>
app3 = i●j●f	<pre>// app3 has features i, j, f</pre>

Thus, the features of an application can be determined by inspecting its equation.

Note that a function represents both a feature *and* its implementation — there can be different functions with different implementations of the *same* feature:

k₁●x	11	adds	k	with	implementation <sub>1</sub>	to	х
<b>k</b> ₂● <b>x</b>	11	adds	k	with	implementation <sub>2</sub>	to	x

When an application requires the use of feature  $\mathbf{k}$ , it is a problem of *expression optimization* to determine which implementation of  $\mathbf{k}$  is best (e.g., provides the best performance)<sup>1</sup>. It is possible to automatically design software (i.e., produce an expression that optimizes some criteria) given a set of constraints for a target application [8]. This is automatic programming.

Although GenVoca values and functions seem untyped, constraints do exist. *Design rules* are domain-specific constraints that capture syntactic and semantic constraints that govern legal compositions. It is common that the selection of a feature will disable or enable the selection of other features. More on design rules later.

### 2.2 AHEAD

AHEAD, or *Algebraic Hierarchical Equations for Application Design*, embodies four key generalizations of GenVoca. First, a program has many representations besides source code, including UML documents, makefiles, BNF grammars, documents, performance models, etc. A model of FOP must deal with all these representations.

Second, each representation is written in its own language or DSL. The code representation of a program may be represented in Java, a machine executable representation may be bytecodes, a makefile representation could be an ant XML file, a performance model may be a set of Mathematica equations, and so on. An FOP model must support an open-ended spectrum of languages to express arbitrary program representations.

Third, when a feature is added to a program, any or all of the program's representations may be updated. That is, the source code of a program changes (to implement the feature), makefiles change (to build the feature), Mathematica equations change (to pro-

<sup>1.</sup> Different equations represent different programs and equation optimization is over the space of semantically equivalent programs. This is identical to relational query optimization: a query is represented by a relational algebra expression, and this expression is optimized. Each expression represents a different, but semantically equivalent, query-evaluation program.

file the feature), etc. Thus, the concept of extension applies not only to source code representations, but other representations as well.

Fourth, FOP models must deal with a general notion of modularity: *a module is a containment hierarchy of related artifacts*. A class is a module (1-level hierarchy) that contains a set of data members and methods. A package or JAR file is a module (2level hierarchy) that contains a set of classes. A J2EE EAR file is a module (3-level hierarchy) that contains a set of packages, HTML files, and descriptor files. Going further, a client-server program is also a module (a multi-level hierarchy) that contains representations of both client and server programs.

Given the above, a generalization of GenVoca emerges. A "value" is a module that defines a containment hierarchy of related artifacts of different types written in potentially different languages. An "extension" is function that maps containment hierarchies. Thus, whenever an extension is applied to a program (i.e., an AHEAD value), any or all of the representations in this module (containment hierarchy) will be updated and new artifacts added. Thus, as AHEAD extensions are applied, all of the representations of the resulting program remain consistent. This is exactly what we need.

The notations of AHEAD extend those of GenVoca. A model m is a set of features that are "values" or "functions" called *units*:

$$M = \{a, b, c, d, ... \}$$

Individual units may themselves be sets, recursively:

The nesting of sets models a containment hierarchy or module. The composition of units is defined by the *Law of Composition*. That is, given units x and x:

$$\begin{array}{l} \mathbf{X} = \left\{ \begin{array}{l} \mathbf{a}_{x}, \ \mathbf{b}_{x}, \ \mathbf{c}_{x} \end{array} \right\} \\ \mathbf{Y} = \left\{ \begin{array}{l} \mathbf{a}_{y}, \ \mathbf{c}_{y}, \ \mathbf{d}_{y} \end{array} \right\} \end{array}$$

The composition of x and x, denoted  $x \bullet x$ , is formed by "aligning" the units of x and x that have the same name (ignoring subscripts) and composing:

 $Y \bullet X = \{ a_y \bullet a_x, b_x, c_y \bullet c_x, d_y \} // Law of Composition (6)$ 

That is, artifact **a** of  $\mathbf{y} \cdot \mathbf{x}$  is the original artifact  $\mathbf{a}_x$  composed with the extension  $\mathbf{a}_y$ ; artifact **b** of  $\mathbf{y} \cdot \mathbf{x}$  remains unchanged from its original definition  $\mathbf{b}_x$ , etc. Composition is recursive: if units represent sets, their compositions are expanded according to (6).

To see the connection with inheritance, consider the following inheritance hierarchy which is a class representation of (6). Assume **a** and **c** are methods, where  $\mathbf{a}_y$  and  $\mathbf{c}_y$  extend (or override) their super-methods  $\mathbf{a}_x$  and  $\mathbf{c}_x$ :

```
class X {
    member a<sub>x</sub>;
    member b<sub>x</sub>;
    member c<sub>x</sub>;
}
class Y extends X {
    member a<sub>y</sub>;
    member c<sub>y</sub>;
    member d<sub>y</sub>;
}
class Y•X extends Y {}
```

How the composition operator  $\bullet$  is defined depends on the artifact type.  $\bullet$  is polymorphic: it can be applied to all artifacts (i.e., all artifacts can be composed/extended) but what composition/extension means is artifact type dependent (i.e., how makefile artifacts are extended will be analogous to but not the same as how code artifacts are extended). This means that different tools implement  $\bullet$  for code and makefiles.

AHEAD representations lead to simple tools and implementations. While there are many ways in which containment hierarchies can be realized, the simplest way is to map containment hierarchies to file system directories. Thus a feature might encapsulate many Java files, class files, HTML files, etc. Feature composition corresponds to directory composition.

Recognize what AHEAD represents: it is a *structural model of information* — it is not just a model of code synthesis. Its premise is that if a program can be understood in terms of features, so too can all of its representations — code and otherwise. We can choose to interpret individual terms of AHEAD expressions as code files or code directories, but we are free to consider other representations as well. A familiarity with relational query optimization bares this out: the optimizer reasons about a program in terms of performance representations of relational operations (i.e., cost functions), while the code generator produces a program from code representations of these same operations [4]. Reasoning about programs often relies on different representations of programs. AHEAD provides a mathematical foundation for expressing their inter-relationships.

We'll explore examples of these ideas in the following sections.

# **3** A Simple Example

Consider a family of elementary post-fix calculators<sup>2</sup>. Calculators in this family are differentiated on (a) the arithmetic values **BigInteger** or **BigDecimal** that can be specified and (b) the set operations that can be performed on them, which includes addition, division, and subtraction.

An AHEAD model that describes this family is c:

<sup>2.</sup> Modeled after Hewlett-Packard calculators.

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The lone value in this model is **Base**, which defines an empty **calc** (short for "calculator") class (Figure 1a). The extensions **BigI** and **BigD** introduce a 3-level stack of **Big-Integer** or **BigDecimal** objects, respectively (Figure 1b-c).<sup>3</sup> **BigI** and **BigD** are mutually exclusive as the stack variables introduced by both have the same name, but are of different types. Thus, calculators either work on **BigInteger** or **BigDecimal** numbers, but not both.

The extensions Iadd, Idiv, and Isub respectively introduce the BigInteger addition, division, and subtraction methods to the calc class (Figure 1d-e). The extensions Dadd, Ddivd, Ddivu, and Dsub do the same for BigDecimal methods (Figure 1f-g). Note that



Figure 1. Files from the C model

3. A **BigInteger** is an unlimited precision integer; a **BigDecimal** is an unlimited-precision, signed decimal number.

there are two mutually exclusive **BigDecimal** division extensions: **Ddivd** and **Ddivu**. **Ddivd** rounds answers down, **Ddivu** rounds up.

As you may have already noticed, these files look like Java programs, but the language that we are using is not Java but an extended Java language called Jak (short for "Jakarta"). Jak files have .jak extensions, like Java files have .java extensions.

A calculator is defined by an equation. Here are a few calculator definitions:

```
i1 = Iadd@BigI@Base
i2 = Isub@Iadd@BigI@Base
i3 = Idiv@Iadd@BigI@Base
d1 = Dadd@BigD@Base
d2 = Dsub@Dadd@BigD@Base
d3 = Ddivd@Dadd@BigD@Base
```

Calculator i1 offers BigInteger addition. i2 also supports subtraction. i3 has BigInteger addition and division. d1—d3 are the corresponding calculators for BigDecimal numbers using rounded-down division. The code generated for the i3 calc class is shown in Figure 2.<sup>4</sup>

```
layer i3;
import java.math.BigInteger;
class calc {
  static BigInteger zero = BigInteger.ZERO;
   BigInteger e0 = zero, e1 = zero, e2 = zero;
   void add() {
      e0 = e0.add(e1);
      e1 = e2;
  }
   void clear() {
      e0 = e1 = e2 = zero;
   3
   void divide() {
      e0 = e0.divide( e1 );
      e1 = e2;
  }
   void enter( String val ) {
      e^2 = e^1:
      e1 = e0;
      e0 = new BigInteger(val);
  }
   String top() { return e0.toString(); }
}
              Figure 2. i3/calc.jak
```

<sup>4.</sup> Note: the term "layer" in Figure 2. is used interchangeably with "feature" in AHEAD.

### **Model Exercises**

- [1] What other calculator features could be added to c? What would be their Jak definitions? Look at the BigInteger and BigDecimal pages in the J2SDK documentation for possibilities.
- [2] Suppose the size of the stack was variable. How would this be expressed as an extension? What modifications of existing extensions would be needed?
- [3] Modify model c so that BigDecimal round-up and round-down are features, which could parameterize operations like division.
- [4] How would c be modified to permit the synthesis of a program that would invoke the calculator from the command-line? From a GUI?

### **Tool Exercises**

An AHEAD model c corresponds to a directory c, and each unit v in c corresponds to a subdirectory of c, namely c/v. The contents of a unit in our example is merely a calc.jak file. The AHEAD directory structure of c is:

C/Base/calc.jak	//	see	Figure	1a
C/BigI/calc.jak	//	see	Figure	$^{1b}$
C/BigD/calc.jak	//	see	Figure	1c
C/Iadd/calc.jak	//	see	Figure	1d
C/Idiv/calc.jak	//	see	Figure	1e
C/Isub/calc.jak				
C/Dadd/calc.jak	//	see	Figure	1d
C/Ddivd/calc.jak	//	see	Figure	1f
C/Ddivu/calc.jak				
C/Dsub/calc.jak				

Although we provide no calc.jak files for Isub and Dsub, they are easy to write. In fact, they are almost identical to the calc.jak files for Iadd and Dadd.<sup>5</sup>

The composer tool is used to evaluate equations and has many optional parameters. For our tutorial, we need to reset one of these parameters. Create in the model directory a file called composer.properties. Its contents is a single line (which says when composing Jak files, use the jampack tool):

unit.file.jak : JamPackFileUnit

To evaluate an equation, run composer in the model directory. The order in which model units are listed on the composer command line are inside-to-outside order, and the name of the composition is given by the target option. Thus, to evaluate is use:

> cd C
> composer --target=i3 Base BigI Idiv Iadd

<sup>5.</sup> So why not just define one layer to represent both? This could be done with our current tools, as they are preprocessors. In future tools, these files will be different, because the types of variables for **e1**—**e3** will need to be explicitly declared. When this occurs, the corresponding files will indeed be different.

The result of the composition is the directory c/i3, which contains a single file, calc.jak, shown in Figure 2. Note that the order in which units are listed on the composer command line is in *reverse* order in which they are listed in an equation — base first, outermost extension last. (This is a legacy oddity of AHEAD tools that has never been changed. Sigh.)

[5] Validate your Model Exercise solutions by implementing them using AHEAD tools.

#### 3.1 Translating to Java

The jak2 java tool converts Jak files to their Java counterparts:

> cd i3 > jak2java \*.jak

The above command-line translates all Jak files (in our case, there is only one file — calc.jak) to their Java equivalents. Of course, these generated files can be compiled in the usual way:

> javac \*.java

Note there are Jak files (i.e., those that refine classes and interfaces) that cannot be translated to Java, as they have no Java counterpart. jak2java translates only Jak classes and interfaces.

### 3.2 Design Rules

New arithmetic operations could be added to c to enlarge the family of calculators. At the same time, it becomes increasingly clear that not all compositions are meaningful. In fact, it is quite easy to deliberately or unintentionally specify meaningless compositions, but **composer** is usually quite happy to produce code for them. We need automated help to detect illegal compositions.

This is not a problem specific to calculators, but rather a fundamental problem in FOP. The use of a feature in a program can enable or disable other features. *Design rules* are domain-specific constraints that define composition correctness predicates for features. *Design rule checking (DRC)* is the process by which design rules are composed and their predicates validated. AHEAD offers two different tools for defining and evaluating design rules: drc and guidsl. drc is a first-generation tool [9]; guidsl is a next-generation tool that we will highlight here.

The theory behind both tools is the use of grammars to define legal sequences (i.e., compositions) of features. A grammar for model c is:

```
C : Type Base ;

Type : BigInt+ BigI

| BigDec+ BigD ;

BigI : Iadd | Idiv | Isub ;

BigD : Dadd | Ddivu | Ddivd | Dsub ; (7)
```

where tokens are units of c. A sentence of this grammar specifies a particular sequence or composition of features. The set of all sentences defines the model's *product-line*, i.e., the set of all possible expressions or compositions of features.

Like any grammar, some sentences are semantically invalid. To weed out incorrect sentences, a grammar is augmented with *attributes*. Conditions for correct sentences (or correct compositions) are predicates defined over these attributes. That is, these predicates filter out syntactically incorrect sentences. The core theory behind both tools are *attribute grammars*, a well-understood technology.

In the case of our c model, syntactic correctness is almost all that is needed. The only additional constraint — which is simple enough to have been expressed by an additional grammar rule — is the mutually exclusive nature of pdivu and pdivd; at most one of these features can appear in a decimal calculator.

As an aside, product-line researchers are familiar with feature diagrams, i.e., trees whose terminal nodes are primitive features and non-terminal nodes are compound features. So what is the connection between grammars and feature diagrams? Although feature diagrams were introduced by Kang, et al in the early 1990s [13] and "GenVoca" grammars, like (7), were introduced in 1992 [3], it was not until 2002 that de Jonge and Visser noticed that feature diagrams are graphical representations of grammars [11]. In fact, grammars provide an added benefit beyond feature diagrams in that they tell us the *order* in which features are composed, which is important to AHEAD and step-wise development. So if you're a fan of feature diagrams, you will see that the tools and ideas we present here are directly applicable to your interests.

#### 3.2.1 The guids1 Tool

guids1 is a next generation tool for design rule checking [10]. The key idea is that a tree grammar (i.e., a grammar where each token appears at most once in a sentence and which itself can be depicted as a tree) can be represented as a propositional formula. Moreover, *any* propositional constraints on the use of features can be added to this formula. Amazingly, an FOP domain model reduces to a single propositional formula, whose variables correspond to primitive and compound features!

Here's why this is important. First, we have a compact representation of an FOP domain model: it is a grammar (which encodes syntactic/ordering constraints) plus a set of propositional formulas that constrains sentences to legal compositions. The

```
Figure 3. C.m -- the guids1 Model of C
```

entire guids1 specification for the c model is shown in Figure 3. The ::Name phrase in a guids1 specification is a way to assign a name to a production.

Second, one of the hallmarks of feature oriented designs is the ability to declaratively specify programs in terms of the features that it offers. guids1 takes a model specification (a .m file) and synthesizes a Java GUI. As a user selects features in the GUI, guids1 uses a logic truth maintenance system to propagate constraints so that users cannot specify incorrect programs. (guids1 is, in effect, a syntax-directed editor that guarantees compilable programs [21]). Further, because a domain model is a propositional formula, satisfiability solvers (or SAT solvers) can be used to help debug models. (A SAT solver is a tool that determines if there is a truth assignment to boolean variables that will satisfy a propositional formula). We believe that SAT solvers will be invaluable assets in future FOP tools.

To generate a declarative language for our calculator, run guids1 on the c model file:

> guidsl c.m

The GUI that is synthesized is shown in Figure 4.

#### **Model Exercises**

[6] How would you change the guids1 file if both Add and Subtract operations were always included if either is selected? Similarly for Divide and Multiply?

#### **Tool Exercises**

- [7] Implement your solution to [6].
- [8] To see an explanation (in the form of a proof) why certain features have been automatically selected or deselected, run guids1, go to Help, and select "Display reason for variable selection". Now drag your cursor over a variable that has been greyed out (i.e., whose value was automatically selected). In the text area at the bottom of the selection panel, you'll see the explanation/proof for that variable's value.



[9] Alter the c.m file of Figure 3 by eliminating the propositional constraint and modifying the grammar specification to account for the mutual exclusion of *Ddivd* and *Ddivu*. Test your solution to see the impact of this change. (Hint: your GUI frontend will change).

### **4** Other ATS Tools and Program Representations

So far, you have seen the composer, jampack (which is called by composer), jak2java, and guids1 tools. Now let's look at the mixin, unmixin, and reform tools.

#### 4.1 mixin

mixin is another tool, besides jampack, that can compose Jak files. Edit the unit.file.jak line in the composer.properties file to be:

unit.file.jak : MixinFileUnit

This is the default setting for unit.file.jak. If composer doesn't see a composer.properties file, it uses mixin to compose Jak files.

Let's re-evaluate the i3 equation to see how mixin works:

```
> cd C
> composer --target=i3 Base BigI Idiv Iadd
```

This is the same command as before. However, the calc.jak file that is produced is quite different and is shown in Figure 5.

The idea behind mixin is simple: each extension is mapped to class in an extension (inheritance) chain. Each class is prefaced by a source statement which indicates the name of the feature and the actual file from which the class was derived. Thus, in Figure 5 four Jak files were composed to yield the calc class; this class is the terminal class of a four-class extension chain. All other classes are abstract — meaning that they can't be instantiated and whose purpose is only to contribute members to the final class in the chain. Note that class names are mangled (i.e., by appending \$\$<feature-Name>) to make them unique.

The intent of mixin and jampack is that you can use either tool to compose Jak files. As you'd expect, the programs of Figure 2 and Figure 5 are functionally equivalent.

Both mixin and jampack can compose files that they themselves have produced. That is, a jampack-produced Jak file can be composed with another jampack-produced Jak file. The same holds for mixin. Because jampack-produced Jak files have the same format as uncomposed Jak files, mixin can compose files produced by jampack. However, the reverse is not true: jampack cannot compose mixin-produced files.

#### 4.2 unmixin

So why use mixin? Why not always use jampack? Consider a typical debugging cycle: you compose files, use jak2java to translate Jak files to Java files, compile and run the Java files to discover bugs. The *composed* Jak files are patched and the cycle continues. Eventually, you'll want to back-propagate the changes you made to the composed files to their original feature definitions. Knowing what feature files to update won't always be easy — and the problem becomes worse as the number and size of the Jak files increases. Back-propagation is a tedious and error-prone process.

Because mixin preserves feature boundaries, it is easy to know what features to update. In fact, with source statements, the propagation of changes can be done automatically. That's the purpose of unmixin. The idea is that you compose a bunch of Jak files, edit the *composed* files, and run unmixin on the edited files to back-propagate the

```
layer i3;
import java.math.BigInteger;
SoUrCe RooT base ".../base/calc.jak";
abstract class calc$$base {}
SoUrCe BigI "../BigI/calc.jak";
abstract class calc$$BigI extends calc$$base {
    static BigInteger zero = BigInteger.ZERO;
BigInteger e0 = zero, e1 = zero, e2 = zero;
    void add() {
        e0 = e0.add( e1 );
        e1 = e2;
    }
    void clear() {
    e0 = e1 = e2 = zero;
    }
    void divide() {
        e0 = e0.divide( e1 );
        e1 = e2;
    }
    void enter( String val ) {
        e2 = e1;
        e1 = e0;
        e0 = new BigInteger( val );
    }
    String top() {
        return e0.toString();
    }
}
SoUrCe Iadd "../Iadd/calc.jak";
abstract class calc$$Iadd extends calc$$BigI {
    // adds BigIntegers
    void add() {
        // adds BigIntegers
        e0 = e0.add( e1 );
e1 = e2;
    }
}
SoUrCe Idiv "../Idiv/calc.jak";
class calc extends calc$$Iadd {
   void divide() {
        e0 = e0.divide( e1 );
        e1 = e2;
    }
}
```

Figure 5. mixin-produced .jak file

changes to the original feature files. For example, suppose we add a comment to the bottom-most class in the extension chain of Figure 5:

```
SoUrCe Idiv "../Idiv/calc.jak";
class calc extends calc$$Iadd {
   void divide() {
        // *new* divide and pop stack
        e0 = e0.divide( e1 );
        e1 = e2;
   }
}
```

By running unmixin, this change is propagated back to the Idiv/calc.jak file:

> cd C > unmixin calc.jak

See for yourself that the change was made. Here are things to remember about unmixin:

- it can take any number of Jak files on its command line,
- the body of the class or interface in the command-line file will replace the body of the class or interface in the original file,
- implements declarations are also propagated, and
- don't change the contents of the source statements!

unmixin updates the original uncomposed files only if changes to its composed counterpart have been updated.

#### 4.3 reform

**reform** is a pretty-printing tool that formats unruly Jak files (and Java files!) and makes them unbelievably beautiful. Consider the 1-line calc.jak file:

```
refines class calc { void divide() { e0 = e0.divide( e1 ); e1 = e2; } }
```

By running:

> reform calc.jak

reform copies the original file into calc.jak~ and updates calc.jak to be:

```
refines class calc {
    void divide() {
        e0 = e0.divide( e1 );
        e1 = e2;
    }
}
```

#### 4.4 Equation Files

As we said earlier, AHEAD is a theory for structuring and synthesizing documents of all kinds by composing features. We introduced Jak file (i.e., code) representations earlier, and now we introduce a second.

Typing in equations on the command line to **composer** can be tedious, particularly if equations involve more than a few terms. **composer** takes an alternative specification, called an *equation file*, which is a list of units. The order in which the units are listed is from inside-out, and the name of the equation is the name of the equation file.

For example, the equation  $\mathbf{A} = \mathbf{B} \cdot \mathbf{C}$  would be represented by the equation file  $\mathbf{A}$ .equation whose contents is:

```
# base feature listed first!
C
B
```

Where any line beginning with # is a comment. Like other AHEAD artifacts, equation files can be composed. File **A.equation** above is a "value". An equation file that is an extension has the special term **super** as one of its units. An extension of **A.equation** that puts **E** before **c** and **F** after **B** is **R.equation**:

E super F

A composition of the above files is:

> composer --target=c.equation A.equation R.equation

and yields file c.equation with contents:

E C B F

Intuitively, an equation file defines an *architectural representation* of a program as an expression. As all program representations are extendable, we now have a means by which to specify and manipulate program architectures. We will see how such representations are useful later.

# 5 More Features of Jak Files

There are three additional features of the Jak language that you should know: **super()** references, extension of constructors, and local identifiers.

### 5.1 The Super Construct

To invoke a method m(int x, float y) of a superclass in Java, you write:

super.m(x,y);

In Jak files, use the super construct instead:

Super(int,float).m(x,y);

super(<argument types>) prefaces a super call and lists the argument types of the method to be called. Consider the class foo and an extension:

```
class foo {
   void dosomething() { /*code*/ }
}
refines class foo {
   void dosomething() {
      /* more before */
      Super().dosomething();
      /* more later */
}
```

In this example, the super references the dosomething() method prior to its extension. A jampack composition of these definitions is shown in Figure 6a. Observe that the original dosomething() method is present in foo, except that it has been renamed, along with its references. The corresponding mixin composition is shown in Figure 6b. When jak2java translates Figure 6b, super(...) references are replaced by "super". In general, always use the super(...) construct to reference superclass members; ATS tools do not recognize "super".



Figure 6. jampack and Mixin compositions

### 5.2 Extending Constructors

A constructor is a special method and to extend it requires a special declaration in Jak files. Consider the following file that declares a constructor:

```
class test {
    int y;
    test() { y = -1; }
}
```

An extension of test and its constructor is:

```
refines class test {
    int x;
    refines test() { x = 2; }
}
```

where "refines <constructor>" is the Jak statement that extends a particular constructor. The jampack composition of these files is shown in Figure 7a. That is, the actions of the original constructor are grouped into a block and are performed first, then the actions of the constructor extension are grouped into a block and performed next. The semantically equivalent mixin composition is shown in Figure 7b.



Figure 7. Another jampack and Mixin composition

#### 5.3 Local Identifiers

Variables that are local to a feature are common. Such variables are used only by the feature itself, and are not to be exported or referenced by other features.

Suppose a class **bar** declares a local variable **x**, and an extension of **bar** declares a local variable, also named **x**:



jampack is smart enough to alert you that multiple definitions of x are present; mixin isn't that smart — and you will discover the error when you compile the translated Java files and see there are multiple definitions of x.

The problem we just outlined isn't specific to AHEAD. In fact, it is an example of a classic problem in metaprogramming, and in particular, macro expansion. The problem is called *inadvertent capture* — i.e., multiple distinct variables are given the same names as identifiers. A general solution is to make sure that distinct variables are given unique names [16].

The way this is done in AHEAD is by using a Local\_Id declaration. This declaration lists the set of identifiers (i.e., variable names and method names) that are *local* to a feature; ATS tools will mangle their names so that they will always be unique. So a better way to define the above is:

The jampack and mixin composition of the above two files are:

{

(b)



where local names are replaced with their mangled counterparts so that their names no longer conflict.

# **6** A More Complex Example

Consider model L, which defines a set of programs that implement linked lists:

L = { sgl, dbl, sgldel, dbldel }

The lone value is **sg1** which contains a pair of classes, **list** and **node**, that implement a bare-bones singly-linked list (Figure 8a-b).



Figure 8. The **sgl** and **dbl** Layers

An extension of sgl is dbl, which converts the program of sgl into a doubly-linked list. dbl is a crosscut that augments the node class with a prior pointer, adds a last pointer to the list class, and extends the insert method so that the values assigned to the last and prior pointers are consistent (Figure 8c-d).

The composition **both** = dbl•sgl yields the doubly-linked list program of Figure 9. The code underlined originates from the dbl extension.



Figure 9. Composition dbl•sgl

Now suppose we want to enhance the design of our list programs by adding a delete method. sgldel does exactly this for singly-linked lists: it adds a delete method to the list class (Figure 10a). We can use sgldel in a composition slist that defines a singly-linked list with both insert and delete methods:

slist = sgldel • sgl

To create a doubly-linked list that has both insert and delete methods requires an extension dbldel (Figure 10b). dbldel converts the singly-linked list deletion algorithm of sgldel to a doubly-linked list deletion algorithm by replacing (or overriding) the findAndDelete method.

The following equations yield identical programs for inserting and deleting elements from a doubly-linked list. The reason why they are equivalent is that the extensions **dbl** and **sgldel** are independent of each other, and thus can be composed in any order.



(a) L/sgldel/list.jak

Figure 10. The **sgldel** and **dbldel** Layers

### **Model Exercises**

- [10] Suppose other operations for traversing the list are added. How would this impact model L? What about the operation reverse(), which reverses the order in which nodes are listed?
- [11] Suppose an "ordering" feature is added to a list, meaning that nodes have keys and are maintained in ascending key order. How would this feature impact L?
- [12] Consider a "monitor" feature, which precludes more than one thread to access a list at a time. How would this feature impact L? How would it be defined?

#### **Tool Exercises**

The directory structure for L is:

```
L/sgl/list.jak// see Figure 8aL/sgl/node.jak// see Figure 8bL/dbl/list.jak// see Figure 8cL/dbl/node.jak// see Figure 8dL/sgldel/list.jak// see Figure 10aL/dbldel/list.jak// see Figure 10b
```

The files of Figure 9 are the result of evaluating the equation **both** = dlb•sgl using the composer tool:

```
> cd L
> composer --target=both sgl dbl
```

The generated directory structure is:

L/both/list.jak	11	see	Figure	9a
L/both/node.jak	//	see	Figure	9b

[13] What is a guids1 model of L?

#### 6.1 Multi-Dimensional Models and Origami

There remains a fundamental relationship among the features of **L** that we have not yet captured. Consider the following incorrect compositions:

```
error1 = dbl•sgldel•sgl
error2 = dbldel•sgldel•sgl
```

Both define programs that are partially and thus incorrectly implemented. error1 is a program whose insert method works on a doubly-linked list, but whose delete method works only on a singly-linked list. error2 is a program whose insert method works on a singly-linked list, but whose delete method works for a doubly-linked list.

The problem is that if a data structure is extended (i.e., a singly-linked list becomes doubly-linked), then *all* of its operations should be updated to maintain the consistency of this extension, and not just some. That is, if a singly-linked list has both **insert** and **delete** operations, when the structure becomes doubly-linked, both operations must

be updated to work on doubly-linked lists. Equivalently, if a feature adds a new method to a data structure, then that method must work for that data structure and not some other structure.

Although this is an elementary example, it is representative of a large class of problems in FOP, namely that a model defines a group of features that are not truly independent and this group must be applied in lock-step — all or nothing — manner. Whenever you notice this phenomena, realize that these groups represent "higherlevel" features.

Here's a technique for understanding this problem. Create a matrix, called an *Origami* matrix, where rows represent operations (insert, delete), and columns represent structure variants (singleLink, doubleLink). Entries of this matrix are the features of L (see Table 1). This matrix can be extended to handle other operations (sort, find) and other structure variants (ordered-lists, monitors, etc.).

Note: what we have done is to identify the orthogonal "higher-level" features as 'data structure operations' and 'data structure variants'.

	doubleLink	singleLink
insert	dbl	sgl
delete	dbldel	sgldel

Table 1	Origami Matrix fo	r L
---------	-------------------	-----

Suppose the rows of this matrix are composed (or *folded* — hence the name "Origami"), where the corresponding entries in each column are composed (Table 2):

	doubleLink	singleLink
delete●insert	dbldel●dbl	sgldel●sgl

Table 2	Row-Composed	Origami Matrix
---------	--------------	----------------

Study the entries of Table 2. Consider the entry in the singleLink column: sgldel•sgl defines a singly-linked program s that has both an insert and delete method. The entry in the doubleLink column, dbldel•dbl, defines an extension of s that converts its insert and delete methods to work on a doubly-linked list. Thus by composing the delete row with the insert row of Table 1, we synthesize a data structure that has multiple methods, and an extension of that data structure that consistently updates these methods. This interpretation holds if more rows (operations) or more list features (columns) are added.

The columns of Table 2 can be composed to yield a  $1 \times 1$  matrix whose entry is an expression that defines a doubly-linked list with insert and delete methods (Table 3). This expression is identical to equation (8).

	doubleLink●singleLink
delete●insert	dbldel●dbl●sgldel●sgl

 Table 3 A Completely Folded Matrix

Now instead of composing rows of Table 1, let's compose the columns, where corresponding entries in each row are composed (Table 4):

	doubleLink●singleLink
insert	dbl●sgl
delete	dbldel•sgldel

Table 4 Column Composed Origami Matrix

The entry in the insert row, dbl•sgl, defines program D that implements a doublylinked list with an insert method. The entry in the delete row, dbldel•sgldel, defines an extension of D that adds a delete method. By composing the columns of Table 1, we have synthesized a data structure with a single (insert) method, and an extension that adds a delete method to this structure. Again, this interpretation holds if we add more rows (methods) or more columns (features) to Table 1. By folding the rows of Table 4, a 1×1 matrix is produced whose lone entry is equation (9). As a general rule, as long as the order in which rows and columns (that is, 'data structure operation' features or 'data structure variant' features) are composed is legal, the resulting equations in a fully-folded matrix should be equivalent. (If they are not, then a dimension is missing in the design).

Origami matrices capture fundamental relationships among groups of features: to build consistent and correct programs, it is often necessary to apply an entire group of features at once [6]. A matrix representation of these relationships works because the set of features along one dimension are *orthogonal* to those of another. In our example, the set of methods that can be used with a data structure is orthogonal to the set of data structure variants.

Although this is a simple example, Origami applies at much greater levels of granularity. For example, ATS has five tools — including jampack, mixin, and unmixin each having over 30K LOC, and totalling over 150K LOC. These tools are synthesized by folding a 3-dimensional (8×6×8) Origami matrix.

### 6.2 The Meaning of Origami

Why is Origami significant? There are several reasons, all of which capture important generalizations of equational program specifications.

In earlier sections, we defined a program by a single equation. Origami generalizes this idea, so that a program is defined by a set of k equations, one per dimension. This has a significant impact on reducing the complexity of a program specification. Suppose each of the k equations has n terms. Thus, a program specification in Origami is of length O(nk). Yet, the matrix that is folded into a single expression would have  $O(n^k)$  terms! That is, *Origami exponentially shortens specifications of product-line programs* [6]. Or stated another way, Origami enables very simple specifications for very complex programs.

Here's another interesting question: what is the algebraic meaning of matrix folding? The answer is evident when we interpret the composition operator  $(\bullet)$  as addition [12].

Composition in AHEAD is similar to summation. Suppose to build program  $\mathbf{P}$ , we start with a base feature  $\mathbf{F}_0$  and progressively add on features  $\mathbf{F}_1$ ,  $\mathbf{F}_3$ , and  $\mathbf{F}_7$ . Instead of using •, we will use + to denote composition:

 $P = F_7 + F_3 + F_1 + F_0$ (10)

Here's another way to represent P. Suppose F is the model that contains features  $F_0$ ,  $F_1$ ,  $F_3$ , and  $F_7$ . In general  $F_i$  is the *i*th feature of model F. Let E be the sequence of subscripts whose features we are to sum. For equation (10), E = (0,1,3,7). We could equivalently write (10) as a summation:

$$P = \sum_{i \in E} F_i$$

Now suppose our model is two dimensional. Let  $\mathbf{M}$  denote a two-dimensional Origami matrix, where  $\mathbf{M}_{ij}$  is the element in the *i*th row and *j*th column. When the matrix is folded first by rows then by columns, this corresponds to summing the matrix by columns then by rows. When the matrix is folded by columns and then by rows, this corresponds to summing by rows and then columns. Let  $\mathbf{R}$  be the sequence of subscripts in which rows are folded; let  $\mathbf{c}$  be the sequence of subscripts in which columns are folded. Origami expresses the equivalence of the summation of elements of a matrix in different orders:

$$\mathbf{P} = \sum_{i \in \mathbf{R}} \sum_{j \in \mathbf{C}} \mathbf{M}_{i,j} = \sum_{j \in \mathbf{C}} \sum_{i \in \mathbf{R}} \mathbf{M}_{i,j}$$

That is, an Origami matrix is a *k*-dimensional "cube", which when summed across different dimensions yields a program in a product-line. Summation of matrix entries and permuting the order in which entities are added, are familiar ideas in mathematics. The name "Origami" is really a visual interpretation of matrix summation.

Finally, it is worth noting that Origami and multi-dimensional models are historically related to a fundamental problem in program design called the "expression problem". It has been widely studied within the context of programming language design, where the focus is achieving data type and operation extensibility in a type-safe manner. The FOP contribution to this is to show how the idea scales to the synthesis of large programs [6][18].

#### 6.3 Metamodels and Model Synthesis

How are Origami matrices represented in AHEAD? Before we can answer this question, we need to introduce an important concept in modeling called metamodels. A *metamodel* is a model whose instances are themselves models. Consider model M, which has units a, b, and c:

 $M = \{ a, b, c \}$ 

Now consider metamodel  $\mathbf{MM}$ , which also has three units, each being a set with a single unit:

A model can be synthesized by composing metamodel units. The MM equation for model  $\mathbf{M}$  is:

```
M = AAA \bullet BBB \bullet CCC
```

In this particular case, because there are no units in common with AAA—ccc, composition reduces to set-union. The interesting thing about metamodels is that they are identical to models. That is, a model or metamodel is a set of units, where each unit may be a set. Further, the composition operator for units of metamodels (•) is the same operator for units of models (•).

An Origami matrix is a metamodel. Our example is a 2-dimensional (and in general, a *k*-dimensional) array of units. A set is a hierarchy. So to represent matrices in AHEAD, we need to encode a matrix as a tree. A 2-dimensional matrix can be decomposed first into rows, and then each row into columns. Another way is to organize by columns first, and then rows. Figure 11 shows these embeddings for an  $n \times m$  matrix o where  $o_{ij}$  denotes the row *i* column *j* element of o.



Figure 11. Matrix Embeddings in Trees

#### 6.4 Representing Origami Matrices

Now lets consider how to represent Origami matrices. Consider a row-dominant decomposition. Figure 12a shows our example matrix, where entries are equation files that have the same name (eqn.equation). Entry subscripts denote (to us) their true identity. Figure 12b is the corresponding row-oriented metamodel; Figure 12c is its AHEAD directory structure. Figure 12d-g are the contents of the equation files.



Figure 12. Row-Dominant Embedding of a Matrix

Why do we use this particular representation of a matrix? Why use equation files, rather than embedding the actual feature directories themselves? The answer: convenience. Try to create such a hierarchical directory yourself, where instead of equation files, you have feature directories. It's hard to navigate such a directory structure, let alone maintain it. The simpler the representation the better. So it is common that we have a flat model directory (where features are immediate subdirectories), and a separate Origami directory which defines the multi-dimensional relationship among features using equation files.

### **Model Exercises**

[14] Expand the Origami matrix to handle more data structure operations and variants.

#### **Tool Exercises**

To fold a 2-dimensional matrix, you need to invoke **composer** twice: once to compose rows and a second time for columns. (For a *k*-dimensional matrix, we would invoke **composer** *k* times). So to produce the AHEAD equivalent of Table 2, we compose the rows of the **origami** model to produce model **Table2** = **delete**•insert:

```
> cd Origami
> composer --target=Table2 insert delete
```

The resulting model **Table2** is depicted in Figure 13a, and its synthesized AHEAD directory structure in Figure 13b, and the contents of the equation files in Figure 13c-d.

To produce the  $1 \times 1$  matrix of Table 3 or equation (8), we compose the columns (named single and double) using the following command:

```
(a) Table2 = { single, double }
single = { eqn<sub>sgldel</sub>•eqn<sub>sgl</sub> }
double = { eqn<sub>dbldel</sub>•eqn<sub>dbl</sub> }
(b) Origami/Table2/single/eqn.equation // Figure 13c
Origami/Table2/double/eqn.equation // Figure 13d
(c) sgl (d) super
db1
db1del
Figure 13. AHEAD Origami Metamodel
```

```
> cd Table2
> composer --target=both single double
> cd both
> jak2java *.jak
```

[15] Represent the matrix of Figure 12a by columns, and repeat the above folding.

# **Model Exercises**

- [16] Create two different GUIs for a calculator: one uses the standard 2D keypad, a second uses text fields to enter values and operations. A calculator will use one (but not both) of these GUIs. Operations on both GUIs are buttons. So when a calculator is extended by a new operation, its GUI will be extended also. Express this relationship between operations and GUIs as an Origami matrix.
- [17] Generalize the model in [16] that permits multiple GUIs per calculator. One idea would use tabs, one tab per different GUI. Implement your model.

# 7 What's Next?

There are many interesting topics and capabilities that we have yet to explore (or develop) for AHEAD. Here are just a few. If you are interested in learning more about these topics, see [1][5].

### 7.1 Extensible Languages

There are all sorts of non-Java extensions to the Jak language that we haven't talked about, including:

- metaprogramming the ability to assign code fragments to variables, the ability to compose code fragments via escape substitutions, hygienic macros.
- *state machines an embedded DSL for supporting the definition and extension of state machines.*

#### 7.2 Compiler-Compiler Tools

ATS has a sophisticated set of compiler-compiler tools that are used to (a) define base grammars, (b) define grammar extensions, and (c) to synthesize grammars by compos-

ing base grammars with extensions. Grammars are yet another representation of a program, in this case, a compiler, and ATS has tools for defining and composing grammars and generating Java files from them.

### 7.3 Generating and Optimizing MakeFiles

The idea of modules as hierarchical collections of related artifacts is powerful. A paradigm of AHEAD that we have explored so far is that of *composition*: that artifacts of a program can be composed from previously defined artifacts. But there is another way in which program artifacts can be produced: by *derivation*. For example, Java files can be produced from Jak files by the jak2java tool; class files can be produced from Java files by the javac compiler, and so on. A general paradigm is depicted in Figure 14: an artifact can be produced by first composing it from more elementary artifacts, followed by a derivation. Or equivalently, it can be produced by deriving a set of artifacts from more elementary artifacts, and then composing the derived representations<sup>6</sup>. This leads to the following fundamental distributive algebraic relationship (11).

derive( 
$$\operatorname{artifact}_i \bullet \operatorname{artifact}_j$$
) =  
derive(  $\operatorname{artifact}_i$ ) • derive(  $\operatorname{artifact}_i$ ) (11)

Ultimately, we want to specify an entire program — all of its composed and derived representations — as a set of equations. Although ATS does not yet have such a tool, one can imagine a specification like:

where the using clause tells this tool that sgldel and sgl are units in model L, and by inference, composer should be used to compose them. The resulting module will have .jak, .java, .class and .html files. The jak2java tool, when applied to the module of sgldel(sgl), translates all Jak files to Java files and adds them to the module. Similarly, the javac operation compiles all Java files and adds their .class files to the module. The javadoc operation will generate JavaDoc .html files from the generated



6. Figure 14 can be generalized further, so that multiple output artifacts can be derived from a single input artifact, and vice versa.

Java files, and so on, progressively enlarging the contents of that module/directory. In effect, (12) is really an equational representation of a makefile! More on this shortly.

The lesson that we learned from relational query optimizers is that an expression represents a program design and expressions (and hence designs) can be optimized. In this particular example, there really isn't anything to optimize. There is, though, a particular sequencing of the application of the javadoc, javac, and jak2java operations that must be imposed. (In fact, this really is the only legal ordering of these operations for this equation). So notions of design rules also apply to tool operations. But as equations become more complicated, there is the possibility of optimization. In some of our larger examples using Origami, generating common subexpressions among different sets of tools arises. Evaluating common subexpressions once, and not many times, is an important optimization that a tool should be able achieve automatically [14].

The big picture is depicted below. Given an equational representation of a program that specifies both the artifacts that are to be composed and those that are to be derived, a tool will expand the equations and perform optimizations to synthesize the resulting program in an efficient manner. The tool will then produce an optimized set of equations, and a generator will translate these equations into a *makefile* — a functional-like language that efficiently executes equational specifications [14].



Figure 15. Generation and Optimization of MakeFiles

### 7.4 Type Systems

As mentioned earlier, extensions are functions that appear untyped. In fact, function inputs and outputs have definite constraints. Our tools assume that the correct types are both being input and output. In general, this is bad assumption.

Question: how does one type a program? Should Java interfaces be used? How does typing generalize to, say, grammar files or equation files? What is a general mechanism for typing arbitrary artifacts and their extensions? We have the outlines of a solution for AHEAD, but at this time, AHEAD has no tool support.

### 7.5 Aspect-Oriented Programming

Aspect-Oriented Programming (AOP) is closely related to FOP. Both deal with modules that encapsulate crosscuts of classes, and both express program extensions. FOP uses a subset of the "advising" capabilities of AOP, namely those that use execution pointcuts. However, the primary difference between AOP and FOP is their composition models. FOP treats aspects as functions that map programs, and uses function composition as the means to compose aspects. This leads to algebraic representations of programs and a simple means to perform program reasoning with aspects. In contrast, AOP uses a complex model of aspect composition (e.g., precedence rules) that complicates program reasoning using aspects and makes step-wise development difficult [19]. AOP and FOP are thus not directly comparable, but are instances of a more general paradigm of automated software development — one that composes aspects by FOP function composition and uses the full power of AOP pointcuts.

# 8 Conclusions

Just as the structure of matter is fundamental to chemistry and physics, so too must the structure of software be fundamental to computer science. Unfortunately, our understanding of software structure is in its infancy. Today, software design is an art. As long as it remains so, our ability to automate rote tasks of program design and synthesis will be limited. And software engineering will be more of a craft than a discipline.

Software designs can be given mathematical precision when expressed as a composition of features. We have presented a simple and elegant theory of program design, backed by years of implementation and experimentation, that brings together key elements in the future of software development: generative programming, domain-specific languages, automatic programming, and step-wise development. Generative programming gives our theory its mathematical backbone: functions can map programs. Domain-specific languages give programming artifacts their form: these are the artifacts that functions transform. Automatic programming underscores AHEAD as a simple model that relates automated reasoning, compositional programming, and design optimization by algebraic reasoning. And step-wise development is a practical way of controlling complexity. AHEAD provides an algebraic foundation for understanding program development on a larger scale.

This paper has explored basic concepts of FOP and a (small) subset of the tools of the AHEAD tool suite. For the most recent results, see our web site [17] and consult the AHEAD documentation [1].

### 9 Suggested Reading

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