The marriage agency

A marriage agency has in its files 25 men and 25 women and aims at acquainting the men with the women by organising dinner evenings, each one involving 12 tables, seating 2 men and 2 women. (Consequently, at each dinner evening, 1 man and 1 woman have a day off.) The question is how many of such dinner evenings the marriage agency can schedule without some man and woman sharing a table twice.

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Frans van der Sommen raised this problem at the end of the ETAC session of 8 August 1995. Rutger M. Dijkstra, who happened to attend that session, immediately showed how to schedule 12 dinner evenings: partition the men into a singleton and 12 pairs numbered [0..12], do the same with the women, and let on the nth evening the men of pair i share a table with the women of pair i (i+n)mod 12 .

The demonstration that 12 is indeed the maximum took a little bit longer. Consider a sequence of 13 dinner evenings. Then at
most 13 men have had an evening off, and therefore at least 12 (= 25 - 13) men dined all 13 evenings. Such a man enjoyed 26 (= 2 x 13) times the company of a woman; the number of women being 25, there is - pigeon-hole principle - at least one woman whose company he enjoyed at least twice.

[As said, this took a little bit longer. We first tried too a crude a counting argument in terms of man-woman combinations. Their total number is 625 (= 25 x 25), each evening 48 (= 4 x 12) combinations are getting acquainted. Since 625/48 = 13 1/48, this rules out a schedule of 14 or more evenings, but the feasibility of a schedule of 13 dinner evenings it leaves open.]

This is actually a sequel to EWD1212: feasibility is shown by means of a witness, infeasibility by a counting argument.

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