

**TRANSCRIPTS FOR THE PROOF OF THE  
ALTERNATING BIT PROTOCOL**

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Technical Report #22@June 1981

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The sole purpose of this report is to bring together the many pages of verifier transcripts that were generated in our proof of the Alternating Bit Protocol. A summary of this work is contained in a companion report [DiVito 81]. Refer to that report for a description of the problem and a basic outline of the approach. The present report is not self-contained; it is primarily a raw collection of transcripts and is not intended to contain explanatory material.

As mentioned in the summary report, the proof was a fully mechanical verification effort. In addition, there were two separate verification systems used in this work: the Gypsy system and the Affirm system. We present complete transcripts showing the work done on both systems. It is divided into the following four parts:

1. Text of the Gypsy model of the protocol and the intermediate specifications. Includes the supporting lemmas used in the Gypsy part of the proof. Followed by the output of the verification condition (VC) generation.

2. Prover transcripts for the proofs of the VCs. These were done with the Gypsy prover.

3. Prover transcripts for the proofs of those supporting lemmas which were proved with the Gypsy prover.

4. Transcripts from the Affirm system. Includes a listing of the type specifications expressed in Affirm. Followed by sessions with the Affirm prover in which the remaining lemmas were proved.

Documentation on the use of both verification systems can be found in the various manuals cited in the references.

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## References

[DiVito 81] B. L. DiVito. "A Mechanical Verification of the Alternating Bit Protocol," Technical Report ICSCA-CMP-21, University of Texas at Austin, June 1981.

[Good 78] D. I. Good, et al. "Report on the Language Gypsy Version 2.0," ICSCA-CMP-10, University of Texas at Austin, September 1978.

[CMP 80] Certifiable Minicomputer Project. "Gypsy 2.0 Verification Environment 6.0 Users Manual," ICSCA, University of Texas at Austin, February 1980.

[Thompson 81] D. H. Thompson, et al. "The Affirm Reference

Library," USC-ISI, 1981. (Five volume set.)

[PHOTO: Recording initiated Tue 5-May-81 9:05AM]

LINK FROM CMP.DIVITO, TTY 20

TOPS-20 Command processor 4(560)

[PHOTO: Logging disabled Tue 5-May-81 9:05AM]

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44444 The following is a transcript of the modeling and verification of  
4 the Alternating Bit Protocol in Gypsy. We begin by displaying the  
4 Gypsy text and the generation of verification conditions. This is  
4 followed by the various proof transcripts. Most of the proofs are  
4 carried out with the Gypsy prover. However, some are performed  
4 with the help of the Affirm system. These are documented in a  
4 separate set of transcripts.

44444@ty abp.gyp,abp.lem

Abp.Gyp.2

scope alt\_bit\_protocol =

begin

type bit = (zero, one);

type message = sequence of character;

type packet = record (mssg : message;

seqno : bit);

type pkt\_buf = buffer of packet;

type clk\_buf = buffer of boolean;

type msg\_buf = buffer of message;

type msg\_seq = sequence of message;

type pkt\_seq = sequence of packet;

type bit\_seq = sequence of bit;

procedure ab\_protocol (var source : msg\_buf<input>;

var sink : msg\_buf<output>) =

begin

block msg\_lag (outto (sink, myid), infrom (source, myid), 1);

exit false;

var pkt\_send, pkt\_recv, ack\_send, ack\_recv : pkt\_buf;

var clock\_in, clock\_out : clk\_buf;

cobegin

sender (source, pkt\_send, ack\_send, clock\_in, clock\_out);

medium (pkt\_send, pkt\_recv);

medium (ack\_recv, ack\_send);

receiver (sink, pkt\_recv, ack\_recv);

timer (clock\_in, clock\_out)

end

end;

```

procedure sender (var source : msg_buf<input>;
var pkt_send : pkt_buf<output>;
var ack_send : pkt_buf<input>;
var start : clk_buf<output>;
var tick : clk_buf<input>) =
begin
block proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1);
exit false;
var pack, ack : packet;
var b : boolean;
var next : bit := one;
loop
assert proper_transmission (infrom (source, myid),
outto (pkt_send, myid),
infrom (ack_send, myid), 0)
& next = next_seqnum (outto (pkt_send, myid))
& next = next_seqnum (infrom (ack_send, myid));
receive pack.mssg from source;
pack.seqno := next;
send pack to pkt_send;
send true to start;
loop
assert proper_transmission (infrom (source, myid),
outto (pkt_send, myid),
infrom (ack_send, myid), 1)
& infrom (source, myid)
= unique_msg (outto (pkt_send, myid))
& size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
& outto (pkt_send, myid) ne null (pkt_seq)
& pack = last (outto (pkt_send, myid))
& next = next_seqnum (infrom (ack_send, myid))
& pack.seqno = next;
await
on receive ack from ack_send
then if ack.seqno = next
then leave
end
on receive b from tick
then send pack to pkt_send;
send true to start

```

```

end
end;
next := comp (next)
end
end;
procedure medium (var pkt_in : pkt_buf <input>;
var pkt_out : pkt_buf <output>) =
begin
block outto (pkt_out, myid) sub infrom (pkt_in, myid);
exit false;
pending
end;
procedure receiver (var sink : msg_buf<output>;
var pkt_rcv : pkt_buf<input>;
var ack_rcv : pkt_buf<output>) =
begin
block proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 1);
exit false;
var pack : packet;
var exp : bit := one;
loop
assert proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
& exp = next_seqnum (infrom (pkt_rcv, myid))
& exp = next_seqnum (outto (ack_rcv, myid));
receive pack from pkt_rcv;
if exp = pack.seqno
then send pack.mssg to sink;
exp := comp (exp)
end;
send pack to ack_rcv
end
end;
procedure timer (var clock_in : clk_buf<input>;
var clock_out : clk_buf<output>) =
begin
block true;
exit false;
pending
end;
function comp (b : bit) : bit =

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```

begin
exit result = if b = zero then one else zero fi;
result := if b = zero then one else zero fi;
end;
name proper_transmission, proper_reception, next_seqnum, msg_lag,
seqnums, last_bit from alt_bit_specs;
name nchanges, unique_msg, repeats, initial_subseq from alt_bit_specs;
end;
scope alt_bit_specs =
begin
name bit, message, packet, pkt_buf, msg_buf, clk_buf, pkt_seq,
msg_seq, bit_seq, comp from alt_bit_protocol;
function msg_lag (s, t : msg_seq; n : integer) : boolean =
begin
exit (assume result
iff initial_subseq (s, t)
& size (t) - size (s) in [0..n]);
end;
function initial_subseq (u, v : msg_seq) : boolean = pending;
{begin
exit (assume result iff some s : msg_seq, u s = v);
end;}
function proper_transmission (source : msg_seq;
pkt_send, ack_send : pkt_seq; n : integer)
: boolean =
begin
exit (assume result
iff msg_lag (unique_msg (pkt_send), source, n)
& size (unique_msg (pkt_send))
- size (unique_msg (ack_send))
in [0..n]
& size (source) - size (unique_msg (ack_send))
in [0..n] & repeats (pkt_send));
end;
function proper_reception (sink : msg_seq;
pkt_rcv, ack_rcv : pkt_seq; n : integer) : boolean =
begin
exit (assume result
iff msg_lag (sink, unique_msg (pkt_rcv), n)
& ack_rcv sub pkt_rcv
& size (sink) - size (unique_msg (ack_rcv))
in [0..n]);

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end;
function next_seqnum (ps : pkt_seq) : bit =
begin
exit (assume result = comp (last_bit (seqnums (ps))));
end;
function last_bit (bs : bit_seq) : bit =
begin
exit (assume result = if bs = null (bit_seq) then zero else last (bs) fi);
end;
function seqnums (ps : pkt_seq) : bit_seq =
begin
exit (assume result
= if ps = null (pkt_seq)
then null (bit_seq)
else seqnums (nonlast (ps)) <: last (ps).seqno
fi);
end;
function nchanges (bs : bit_seq) : integer =
begin
exit (assume result
= if bs = null (bit_seq)
then 0
else if last (bs) = last_bit (nonlast (bs))
then nchanges (nonlast (bs))
else nchanges (nonlast (bs)) + 1
fi
fi);
end;
function unique_msg (ps : pkt_seq) : msg_seq =
begin
exit (assume result
= if ps = null (pkt_seq)
then null (msg_seq)
else if last (ps).seqno
= next_seqnum (nonlast (ps))
then unique_msg (nonlast (ps)) <: last (ps).mssg
else unique_msg (nonlast (ps))
fi
fi);
end;
function repeats (ps : pkt_seq) : boolean =
begin

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exit (assume result
iff if ps = null (pkt_seq) or nonlast (ps) = null (pkt_seq)
then true
else repeats (nonlast (ps))
& [ last (ps).seqno
ne next_seqnum (nonlast (ps))
-> last (ps) = last (nonlast (ps)) ]
fi);
end;
end;
Abp.Lem.5
scope lemmas =
begin
lemma prop_trans_1 (u: msg_seq; x, y: pkt_seq; p:packet; m: message) =
p.seqno = next_seqnum (x) & p.mssg = m
& proper_transmission (u, x, y, 0)
-> u <: m = unique_msg (x <: p);
lemma prop_trans_2 (u: msg_seq; x, y: pkt_seq; p:packet; m: message) =
p.seqno = next_seqnum (x) & p.mssg = m
& proper_transmission (u, x, y, 0)
-> proper_transmission (u <: m, x <: p, y, 1);
lemma prop_trans_3 (u: msg_seq; x, y: pkt_seq; p: packet) =
proper_transmission (u, x, y, 1)
& x ne null (pkt_seq) & p = last(x)
-> proper_transmission (u, x <: p, y, 1);
lemma prop_trans_4 (u: msg_seq; x, y: pkt_seq; p:packet) =
p.seqno ne next_seqnum (y)
& proper_transmission (u, x, y, 1)
-> proper_transmission (u, x, y <: p, 1);
lemma prop_trans_5 (u: msg_seq; x, y: pkt_seq; m: message) =
proper_transmission (u, x, y, 0)
-> proper_transmission (u <: m, x, y, 1);
lemma prop_trans_6 (u: msg_seq; x, y: pkt_seq) =
proper_transmission (u, x, y, 0)
-> proper_transmission (u, x, y, 1);
lemma prop_trans_7 (u: msg_seq; x, y: pkt_seq; p: packet) =
unique_msg (x) = u
& size (unique_msg (x)) = size (unique_msg (y)) + 1
& p.seqno = next_seqnum (y)
& proper_transmission (u, x, y, 1)
-> proper_transmission (u, x, y <: p, 0);
lemma prop_rec_1 (u: msg_seq; x, y: pkt_seq; p: packet; m: message) =

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p.seqno = next_seqnum (x) & p.mssg = m
& proper_reception (u, x, y, 0)
-> proper_reception (u <: m, x <: p, y, 1);
lemma prop_rec_2 (u: msg_seq; x, y: pkt_seq; p: packet) =
proper_reception (u, x, y, 0)
-> proper_reception (u, x <: p, y, 1);
lemma prop_rec_3 (u: msg_seq; x, y: pkt_seq) =
proper_reception (u, x, y, 0) -> proper_reception (u, x, y, 1);
lemma prop_rec_4 (u: msg_seq; x, y: pkt_seq; p: packet; m: message) =
p.seqno = next_seqnum (x) & p.seqno = next_seqnum (y)
& proper_reception (u, x, y, 0) & p.mssg = m
-> proper_reception (u <: m, x <: p, y <: p, 0);
lemma prop_rec_5 (u: msg_seq; x, y: pkt_seq; p: packet) =
p.seqno ne next_seqnum (x) & p.seqno ne next_seqnum (y)
& proper_reception (u, x, y, 0)
-> proper_reception (u, x <: p, y <: p, 0);
lemma abp_1 (u, v: msg_seq; w, x, y, z: pkt_seq) =
proper_transmission (u, w, z, 1)
& proper_reception (v, x, y, 1)
& x sub w & z sub y
-> msg_lag (v, u, 1);
lemma main_lemma (s: bit_seq; x, y: pkt_seq) =
s sub seqnums (x) & x sub y & repeats (y)
& nchanges (seqnums (y)) - nchanges (s) in [0..1]
-> msg_lag (unique_msg (x), unique_msg (y), 1);
lemma interpolate (s: bit_seq; x, y: pkt_seq) =
s sub seqnums (x) & x sub y & repeats (y)
& nchanges (seqnums (y)) - nchanges (s) in [0..1]
-> nchanges (seqnums (y)) - nchanges (seqnums (x)) in [0..1] ;
lemma next_comp (x: pkt_seq; p: packet) =
next_seqnum (x <: p) = comp (p.seqno);
lemma ne_next (x: pkt_seq; p: packet) =
p.seqno ne next_seqnum (x)
-> next_seqnum (x <: p) = next_seqnum (x);
lemma last_next (x: pkt_seq; p: packet) =
x ne null (pkt_seq) & p = last (x)
-> p.seqno ne next_seqnum (x);
lemma last_unique (x: pkt_seq; p: packet) =
x ne null (pkt_seq) & p = last(x)
-> unique_msg (x <: p) = unique_msg (x);
lemma last_repeats (x: pkt_seq; p: packet) =
x ne null (pkt_seq) & p = last (x) & repeats (x)

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```

-> repeats (x <: p);

lemma eq_iss (u, v: msg_seq) =
u = v -> initial_subseq (u, v);

lemma eq_iss_app (u, v: msg_seq; m: message) =
u = v -> initial_subseq (u <: m, v <: m);

lemma iss_app (u, v: msg_seq; m: message) =
initial_subseq (u, v) -> initial_subseq (u, v <: m);

lemma iss_trans (u, v, w: msg_seq) =
initial_subseq (u, v) & initial_subseq (v, w)
-> initial_subseq (u, w);

lemma msg_lag_eq (u, v: msg_seq) =
msg_lag (u, v, 0) iff u = v;

lemma comp_ne (b1, b2: bit) = b1 ne b2 iff comp (b1) = b2;

lemma bit_cases (b: bit) = b = zero or b = one;

lemma hist_sub (x, y: pkt_buf) =
allfrom (x) sub allfrom (y) -> allfrom (x) sub alto (y);

lemma app_pkt_nonnull (x: pkt_seq; p: packet) =
[(x <: p) = null (pkt_seq)] = false;

lemma app_msg_nonnull (u: msg_seq; m: message) =
[(u <: m) = null (msg_seq)] = false;

lemma app_bit_nonnull (s: bit_seq; b: bit) =
[(s <: b) = null (bit_seq)] = false;

lemma sub_app (x, y: pkt_seq; p: packet) =
(assume x sub y -> x <: p sub y <: p);

lemma size_null (u: msg_seq) =
(assume size (u) = 0 iff u = null (msg_seq));

lemma sub_seqnum (x, y: pkt_seq) =
(assume x sub y -> seqnums (x) sub seqnums (y));

lemma sub_nchanges (s, t: bit_seq) =
(assume s sub t -> nchanges (s) le nchanges (t));

lemma nchanges_unique (x: pkt_seq) =
(assume size (unique_msg (x)) = nchanges (seqnums (x)) );

lemma sub_to_lag (x, y: pkt_seq) =
(assume x sub y & repeats (y)
& nchanges (seqnums (y)) - nchanges (seqnums (x)) in [0..1]
-> initial_subseq (unique_msg (x), unique_msg (y)) );

name proper_transmission, proper_reception, next_seqnum, last_bit, seqnums,
nchanges, unique_msg, repeats, initial_subseq, msg_lag
from alt_bit_specs;

name bit, message, packet, pkt_seq, msg_seq, bit_seq, comp, pkt_buf
from alt_bit_protocol;

end;

```

4444@vsysxxx

[Continuing]

translate abp.gyp

No syntax errors detected

No semantic errors detected

Exec-> translate abp.lem

No syntax errors detected

No semantic errors detected

Exec-> show status all

The current design and verification status is:

SCOPE ALT\_BIT\_PROTOCOL

Waiting for VC generation: AB\_PROTOCOL, COMP, RECEIVER, SENDER

Waiting for pending body to be filled in: MEDIUM, TIMER

Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET,  
PKT\_BUF, PKT\_SEQ

SCOPE ALT\_BIT\_SPECS

Waiting for pending body to be filled in: INITIAL\_SUBSEQ

For specifications only: LAST\_BIT, MSG\_LAG, NCHANGES, NEXT\_SEQNUM,  
PROPER\_RECEPTION, PROPER\_TRANSMISSION, REPEATS, SEQNUMS, UNIQUE\_MSG  
SCOPE LEMMAS

Waiting for VC generation: APP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL,  
APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB,  
ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE,  
LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4,  
PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4,  
PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL,  
SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES

Exec-> set scope alt\_bit\_protocol

Exec-> vcs sender

Generating VCs for procedure sender

Found 1st path

Found 2nd path

Found 3rd path

Found 4th path

Found 5th path

Note: loop has no exit paths

Found 6th path

---

Beginning new path...

Assume (unit entry specification)

true

initializing local variables  
entering loop...  
Evaluating next\_seqnum (infrom (ack\_send, myid))  
Continuing in path...  
Evaluating next\_seqnum (outto (pkt\_send, myid))  
Continuing in path...  
Evaluating proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
Continuing in path...  
Assert proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
& next = next\_seqnum (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid))

-----

Must verify Assert condition

Verification condition sender#4

1: next\_seqnum (null (#seqtype#)) = one  
2: proper\_transmission (null (#seqtype#), null (#seqtype#), null (#seqtype#),  
0)

-----

End of path

-----

-----

Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
& next = next\_seqnum (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid))

Receive pack.mssg from source

-----

Must verify (Receive blocked) condition

Verification condition sender#5

H1: empty (source#1)  
H2: next\_seqnum (infrom (ack\_send, myid)) = next  
H3: next\_seqnum (outto (pkt\_send, myid)) = next  
H4: infrom (source, myid) = infrom (source#1, myid)  
H5: outto (source, myid) = outto (source#1, myid)  
H6: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

-->

C1: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

-----

Continuing in path...

binding due to receive..

pack := pack with (.mssg:=pack#1.mssg)

pack := pack with (.seqno:=next)

Send pack to pkt\_send

-----

Must verify (Send blocked) condition

Verification condition sender#6

H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)

H2: next\_seqnum (infrom (ack\_send, myid)) = next

H3: next\_seqnum (outto (pkt\_send, myid)) = next

H4: infrom (pkt\_send, myid) = infrom (pkt\_send#1, myid)

H5: outto (pkt\_send, myid) = outto (pkt\_send#1, myid)

H6: outto (source, myid) = outto (source#2, myid)

H7: full (pkt\_send#1)

H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

-->

C1: proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
outto (pkt\_send, myid), infrom (ack\_send, myid), 1)

-----

Continuing in path...

Send true to start

-----

Must verify (Send blocked) condition

Verification condition sender#7

H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)

H2: outto (pkt\_send, myid)

[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)]

= outto (pkt\_send#2, myid)

H3: next\_seqnum (infrom (ack\_send, myid)) = next

H4: next\_seqnum (outto (pkt\_send, myid)) = next

H5: infrom (pkt\_send, myid) = infrom (pkt\_send#2, myid)

H6: infrom (start, myid) = infrom (start#1, myid)

H7: outto (source, myid) = outto (source#2, myid)

H8: outto (start, myid) = outto (start#1, myid)

H9: full (start#1)

H10: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

```
-->
C1: proper_transmission (infrom (source, myid) [seq: pack#1.mssg],
outto (pkt_send, myid)
[seq: pack with (.mssg:=pack#1.mssg;
.seqno:=next)],
infrom (ack_send, myid), 1)
-----
Continuing in path...
entering loop...
Evaluating next_seqnum (infrom (ack_send, myid))
Continuing in path...
Evaluating unique_msg (infrom (ack_send, myid))
Continuing in path...
Evaluating unique_msg (outto (pkt_send, myid))
Continuing in path...
Evaluating unique_msg (outto (pkt_send, myid))
Continuing in path...
Evaluating proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
Continuing in path...
Assert proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
& infrom (source, myid) = unique_msg (outto (pkt_send, myid))
& size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
& outto (pkt_send, myid) ne null (pkt_seq)
& pack = last (outto (pkt_send, myid))
& next = next_seqnum (infrom (ack_send, myid)) & pack.seqno = next
-----
Must verify Assert condition
Verification condition sender#13
H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)
H2: outto (pkt_send, myid)
[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)]
= outto (pkt_send#2, myid)
H3: next_seqnum (infrom (ack_send, myid)) = next
H4: next_seqnum (outto (pkt_send, myid)) = next
H5: infrom (pkt_send, myid) = infrom (pkt_send#2, myid)
H6: outto (source, myid) = outto (source#2, myid)
H7: proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 0)
-->
```

C1: infrom (source, myid) [seq: pack#1.mssg]  
= unique\_msg ( outto (pkt\_send, myid)  
[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])  
C2: size (unique\_msg ( outto (pkt\_send, myid)  
[seq: pack with (.mssg:=pack#1.mssg;  
.seqno:=next)]))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
C3: proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
outto (pkt\_send, myid)  
[seq: pack with (.mssg:=pack#1.mssg;  
.seqno:=next)],  
infrom (ack\_send, myid), 1)

---

End of path

---



---

Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
& infrom (source, myid) = unique\_msg (outto (pkt\_send, myid))  
& size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
& outto (pkt\_send, myid) ne null (pkt\_seq)  
& pack = last (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid)) & pack.seqno = next

Assume (Await blocked)

empty (tick) & empty (ack\_send)

Blockage Assertion is

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

End of path

---



---

Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
& infrom (source, myid) = unique\_msg (outto (pkt\_send, myid))  
& size (unique\_msg (outto (pkt\_send, myid)))

```

= size (unique_msg (infrom (ack_send, myid))) + 1
& outto (pkt_send, myid) ne null (pkt_seq)
& pack = last (outto (pkt_send, myid))
& next = next_seqnum (infrom (ack_send, myid)) & pack.seqno = next
Receive ack from ack_send
binding due to receive..
ack := ack#1
Assume (If test failed)
not ack.seqno = next
entering next iteration of loop...
Evaluating next_seqnum (infrom (ack_send, myid))
Continuing in path...
Evaluating unique_msg (infrom (ack_send, myid))
Continuing in path...
Evaluating unique_msg (outto (pkt_send, myid))
Continuing in path...
Evaluating unique_msg (outto (pkt_send, myid))
Continuing in path...
Evaluating proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
Continuing in path...
Assert proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
& infrom (source, myid) = unique_msg (outto (pkt_send, myid))
& size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
& outto (pkt_send, myid) ne null (pkt_seq)
& pack = last (outto (pkt_send, myid))
& next = next_seqnum (infrom (ack_send, myid)) & pack.seqno = next
-----
```

Must verify Assert condition

Verification condition sender#20

```

H1: infrom (ack_send, myid) [seq: ack#1] = infrom (ack_send#3, myid)
H2: pack.seqno = next
H3: next_seqnum (infrom (ack_send, myid)) = next
H4: unique_msg (outto (pkt_send, myid)) = infrom (source, myid)
H5: outto (ack_send, myid) = outto (ack_send#3, myid)
H6: outto (pkt_send, myid)[size (outto (pkt_send, myid))] = pack
H7: size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
H8: proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
```

H9: ack#1.seqno ne next  
H10: null (pkt\_seq) ne outto (pkt\_send, myid)  
-->  
C1: next\_seqnum (infrom (ack\_send, myid) [seq: ack#1]) = next  
C2: size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid) [seq: ack#1])) + 1  
C3: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid) [seq: ack#1], 1)

---

End of path

---

---

Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
& infrom (source, myid) = unique\_msg (outto (pkt\_send, myid))  
& size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
& outto (pkt\_send, myid) ne null (pkt\_seq)  
& pack = last (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid)) & pack.seqno = next

Receive b from tick

binding due to receive..

b := b#1

Send pack to pkt\_send

Continuing in path...

Send true to start

---

Must verify (Send blocked) condition

Verification condition sender#22

H1: outto (pkt\_send, myid) [seq: pack] = outto (pkt\_send#4, myid)

H2: pack.seqno = next

H3: next\_seqnum (infrom (ack\_send, myid)) = next

H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H5: infrom (pkt\_send, myid) = infrom (pkt\_send#4, myid)

H6: infrom (start, myid) = infrom (start#3, myid)

H7: outto (start, myid) = outto (start#3, myid)

H8: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H9: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H10: full (start#3)

H11: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H12: null (pkt\_seq) ne outto (pkt\_send, myid)

-->

C1: proper\_transmission (infrom (source, myid),  
outto (pkt\_send, myid) [seq: pack],  
infrom (ack\_send, myid), 1)

-----  
Continuing in path...

entering next iteration of loop...

Evaluating next\_seqnum (infrom (ack\_send, myid))

Continuing in path...

Evaluating unique\_msg (infrom (ack\_send, myid))

Continuing in path...

Evaluating unique\_msg (outto (pkt\_send, myid))

Continuing in path...

Evaluating unique\_msg (outto (pkt\_send, myid))

Continuing in path...

Evaluating proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

Continuing in path...

Assert proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

& infrom (source, myid) = unique\_msg (outto (pkt\_send, myid))

& size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

& outto (pkt\_send, myid) ne null (pkt\_seq)

& pack = last (outto (pkt\_send, myid))

& next = next\_seqnum (infrom (ack\_send, myid)) & pack.seqno = next

-----  
Must verify Assert condition

Verification condition sender#28

H1: outto (pkt\_send, myid) [seq: pack] = outto (pkt\_send#4, myid)

H2: pack.seqno = next

H3: next\_seqnum (infrom (ack\_send, myid)) = next

H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H5: infrom (pkt\_send, myid) = infrom (pkt\_send#4, myid)

H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H7: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)  
H9: null (pkt\_seq) ne outto (pkt\_send, myid)  
-->  
C1: unique\_msg (outto (pkt\_send, myid) [seq: pack])  
= infrom (source, myid)  
C2: size (unique\_msg (outto (pkt\_send, myid) [seq: pack]))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
C3: proper\_transmission (infrom (source, myid),  
outto (pkt\_send, myid) [seq: pack],  
infrom (ack\_send, myid), 1)

-----

End of path

-----

-----

Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
& infrom (source, myid) = unique\_msg (outto (pkt\_send, myid))  
& size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
& outto (pkt\_send, myid) ne null (pkt\_seq)  
& pack = last (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid)) & pack.seqno = next

Receive ack from ack\_send

binding due to receive..

ack := ack#1

Assume (If test succeeded)

ack.seqno = next

Leaving loop...

Evaluating comp (next)

Continuing in path...

next := comp (next)

entering next iteration of loop...

Evaluating next\_seqnum (infrom (ack\_send, myid))

Continuing in path...

Evaluating next\_seqnum (outto (pkt\_send, myid))

Continuing in path...

Evaluating proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

Continuing in path...

Assert proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
& next = next\_seqnum (outto (pkt\_send, myid))  
& next = next\_seqnum (infrom (ack\_send, myid))

---

Must verify Assert condition

Verification condition sender#33

H1: infrom (ack\_send, myid) [seq: ack#1] = infrom (ack\_send#3, myid)

H2: ack#1.seqno = next

H3: pack.seqno = next

H4: next\_seqnum (infrom (ack\_send, myid)) = next

H5: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H6: outto (ack\_send, myid) = outto (ack\_send#3, myid)

H7: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H8: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H9: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H10: null (pkt\_seq) ne outto (pkt\_send, myid)

-->

C1: comp (next)

= next\_seqnum (infrom (ack\_send, myid) [seq: ack#1])

C2: comp (next) = next\_seqnum (outto (pkt\_send, myid))

C3: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid) [seq: ack#1], 0)

---

End of path

---

Exec-> vcs receiver

Generating VCs for procedure receiver

Found 1st path

Note: loop has no exit paths

Found 2nd path

Found 3rd path

---

Beginning new path...

Assume (unit entry specification)

true

initializing local variables

entering loop...

Evaluating next\_seqnum (outto (ack\_rcv, myid))

Continuing in path...

Evaluating next\_seqnum (infrom (pkt\_rcv, myid))  
Continuing in path...  
Evaluating proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
Continuing in path...  
Assert proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
& exp = next\_seqnum (infrom (pkt\_rcv, myid))  
& exp = next\_seqnum (outto (ack\_rcv, myid))

-----

Must verify Assert condition

Verification condition receiver#4

1: next\_seqnum (null (#seqtype#)) = one  
2: proper\_reception (null (#seqtype#), null (#seqtype#), null (#seqtype#),  
0)

-----

End of path

-----  
-----

Beginning new path...

continuing in loop ...

Assume (from last assertion)

proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
& exp = next\_seqnum (infrom (pkt\_rcv, myid))  
& exp = next\_seqnum (outto (ack\_rcv, myid))

Receive pack from pkt\_rcv

-----

Must verify (Receive blocked) condition

Verification condition receiver#5

H1: empty (pkt\_rcv#1)  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: infrom (pkt\_rcv, myid) = infrom (pkt\_rcv#1, myid)  
H5: outto (pkt\_rcv, myid) = outto (pkt\_rcv#1, myid)  
H6: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

-->

C1: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 1)

-----

Continuing in path...

binding due to receive..

pack := pack#1

Assume (If test succeeded)

exp = pack.seqno

Send pack.mssg to sink

-----  
Must verify (Send blocked) condition

Verification condition receiver#6

H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)

H2: pack#1.seqno = exp

H3: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H4: next\_seqnum (outto (ack\_rcv, myid)) = exp

H5: infrom (sink, myid) = infrom (sink#1, myid)

H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)

H7: outto (sink, myid) = outto (sink#1, myid)

H8: full (sink#1)

H9: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

-->

C1: proper\_reception (outto (sink, myid),  
infrom (pkt\_rcv, myid) [seq: pack#1],  
outto (ack\_rcv, myid), 1)

-----  
Continuing in path...

Evaluating comp (exp)

Continuing in path...

exp := comp (exp)

Send pack to ack\_rcv

-----  
Must verify (Send blocked) condition

Verification condition receiver#8

H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)

H2: outto (sink, myid) [seq: pack#1.mssg] = outto (sink#2, myid)

H3: pack#1.seqno = exp

H4: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H5: next\_seqnum (outto (ack\_rcv, myid)) = exp

H6: infrom (ack\_rcv, myid) = infrom (ack\_rcv#1, myid)

H7: infrom (sink, myid) = infrom (sink#2, myid)

H8: outto (ack\_rcv, myid) = outto (ack\_rcv#1, myid)

H9: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)

H10: full (ack\_rcv#1)

H11: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),

```

outto (ack_rcv, myid), 0
-->
C1: proper_reception (outto (sink, myid) [seq: pack#1.mssg],
infrom (pkt_rcv, myid) [seq: pack#1],
outto (ack_rcv, myid), 1)
-----
Continuing in path...
entering next iteration of loop...
Evaluating next_seqnum (outto (ack_rcv, myid))
Continuing in path...
Evaluating next_seqnum (infrom (pkt_rcv, myid))
Continuing in path...
Evaluating proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
Continuing in path...
Assert proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
& exp = next_seqnum (infrom (pkt_rcv, myid))
& exp = next_seqnum (outto (ack_rcv, myid))
-----
Must verify Assert condition
Verification condition receiver#12
H1: infrom (pkt_rcv, myid) [seq: pack#1] = infrom (pkt_rcv#2, myid)
H2: outto (ack_rcv, myid) [seq: pack#1] = outto (ack_rcv#2, myid)
H3: outto (sink, myid) [seq: pack#1.mssg] = outto (sink#2, myid)
H4: pack#1.seqno = exp
H5: next_seqnum (infrom (pkt_rcv, myid)) = exp
H6: next_seqnum (outto (ack_rcv, myid)) = exp
H7: infrom (ack_rcv, myid) = infrom (ack_rcv#2, myid)
H8: infrom (sink, myid) = infrom (sink#2, myid)
H9: outto (pkt_rcv, myid) = outto (pkt_rcv#2, myid)
H10: proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
-->
C1: comp (exp)
= next_seqnum (infrom (pkt_rcv, myid) [seq: pack#1])
C2: comp (exp) = next_seqnum (outto (ack_rcv, myid) [seq: pack#1])
C3: proper_reception (outto (sink, myid) [seq: pack#1.mssg],
infrom (pkt_rcv, myid) [seq: pack#1],
outto (ack_rcv, myid) [seq: pack#1], 0)
-----
End of path

```

-----  
-----  
Beginning new path...  
continuing in loop ...  
Assume (from last assertion)  
proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
& exp = next\_seqnum (infrom (pkt\_rcv, myid))  
& exp = next\_seqnum (outto (ack\_rcv, myid))  
Receive pack from pkt\_rcv

-----

Must verify (Receive blocked) condition  
Verification condition receiver#13  
H1: empty (pkt\_rcv#1)  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: infrom (pkt\_rcv, myid) = infrom (pkt\_rcv#1, myid)  
H5: outto (pkt\_rcv, myid) = outto (pkt\_rcv#1, myid)  
H6: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
-->  
C1: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 1)

-----

Continuing in path...  
binding due to receive..  
pack := pack#1  
Assume (If test failed)  
not exp = pack.seqno  
Send pack to ack\_rcv

-----

Must verify (Send blocked) condition  
Verification condition receiver#14  
H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: infrom (ack\_rcv, myid) = infrom (ack\_rcv#3, myid)  
H5: outto (ack\_rcv, myid) = outto (ack\_rcv#3, myid)  
H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)  
H7: full (ack\_rcv#3)  
H8: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

H9: pack#1.seqno ne exp  
-->  
C1: proper\_reception (outto (sink, myid),  
infrom (pkt\_rcv, myid) [seq: pack#1],  
outto (ack\_rcv, myid), 1)  
-----  
Continuing in path...  
entering next iteration of loop...  
Evaluating next\_seqnum (outto (ack\_rcv, myid))  
Continuing in path...  
Evaluating next\_seqnum (infrom (pkt\_rcv, myid))  
Continuing in path...  
Evaluating proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
Continuing in path...  
Assert proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
& exp = next\_seqnum (infrom (pkt\_rcv, myid))  
& exp = next\_seqnum (outto (ack\_rcv, myid))

-----  
Must verify Assert condition  
Verification condition receiver#18  
H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)  
H2: outto (ack\_rcv, myid) [seq: pack#1] = outto (ack\_rcv#4, myid)  
H3: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H4: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H5: infrom (ack\_rcv, myid) = infrom (ack\_rcv#4, myid)  
H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)  
H7: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
H8: pack#1.seqno ne exp

-->  
C1: next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp  
C2: next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1]) = exp  
C3: proper\_reception (outto (sink, myid),  
infrom (pkt\_rcv, myid) [seq: pack#1],  
outto (ack\_rcv, myid) [seq: pack#1], 0)

-----  
End of path

-----  
Exec-> vcs ab\_protocol  
Generating VCs for procedure ab\_protocol

Found 1st path

Found 2nd path

---

Beginning new path...

Assume (unit entry specification)

true

initializing local variables

entering cobegin...

timer (clock\_in, clock\_out)

receiver (sink, pkt\_rcv, ack\_rcv)

medium (ack\_rcv, ack\_send)

medium (pkt\_send, pkt\_rcv)

sender (source, pkt\_send, ack\_send, clock\_in, clock\_out)

Continuing in path...

assume cobegin blocks.

Assume (blockage specification for subprocess sender#1)

if isblocked (sender#1)

then proper\_transmission (infrom (source#1, sender#1),

outto (pkt\_send#1, sender#1),

infrom (ack\_send#1, sender#1), 1)

else false

fi

Assume (blockage specification for subprocess medium#1)

if isblocked (medium#1)

then outto (pkt\_rcv#1, medium#1) sub infrom (pkt\_send#1, medium#1)

else false

fi

Assume (blockage specification for subprocess medium#2)

if isblocked (medium#2)

then outto (ack\_send#1, medium#2) sub infrom (ack\_rcv#1, medium#2)

else false

fi

Assume (blockage specification for subprocess receiver#1)

if isblocked (receiver#1)

then proper\_reception (outto (sink#1, receiver#1),

infrom (pkt\_rcv#1, receiver#1),

outto (ack\_rcv#1, receiver#1), 1)

else false

fi

Assume (blockage specification for subprocess timer#1)

if isblocked (timer#1) then true else false fi

Assume (blockage specification for unit ab\_protocol)

isblocked (sender#1) or isblocked (medium#1) or isblocked (medium#2)  
or isblocked (receiver#1) or isblocked (timer#1)

Blockage Assertion is

msg\_lag (outto (sink, myid), infrom (source, myid), 1)

-----  
Must verify (process blockage) condition

Verification condition ab\_protocol#2

H1: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_rcv#1),  
allto (ack\_rcv#1), 1)

H2: proper\_transmission (infrom (source#1, sender#1), allto (pkt\_send#1),  
allfrom (ack\_send#1), 1)

H3: isblocked (medium#1)

H4: isblocked (medium#2)

H5: isblocked (receiver#1)

H6: isblocked (sender#1)

H7: isblocked (timer#1)

H8: allto (ack\_send#1) sub allfrom (ack\_rcv#1)

H9: allto (pkt\_rcv#1) sub allfrom (pkt\_send#1)

-->

C1: msg\_lag (outto (sink#1, receiver#1), infrom (source#1, sender#1), 1)

-----  
End of path

-----  
-----  
Beginning new path...

Assume (unit entry specification)

true

initializing local variables

entering cobegin...

timer (clock\_in, clock\_out)

receiver (sink, pkt\_rcv, ack\_rcv)

medium (ack\_rcv, ack\_send)

medium (pkt\_send, pkt\_rcv)

sender (source, pkt\_send, ack\_send, clock\_in, clock\_out)

Continuing in path...

Assume Procedure Exit Specifications

false & false & false & false & false

assume all procedure activations terminate normally.

Leaving Unit ab\_protocol

Assert false

End of path

Exec-> vcs comp  
Generating VCs for function comp  
Found 1st path

---

Beginning new path...  
Assume (unit entry specification)  
true  
result := if b = zero then one else zero fi  
Leaving Unit comp  
Assert result = if b = zero then one else zero fi  
End of path

---

Exec-> show status all  
The current design and verification status is:  
SCOPE ALT\_BIT\_PROTOCOL  
Waiting for pending body to be filled in: MEDIUM, TIMER  
Proved: COMP  
Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET,  
PKT\_BUF, PKT\_SEQ  
Check VCs (not fully checked): AB\_PROTOCOL, RECEIVER, SENDER  
Check VCs (path pending): AB\_PROTOCOL, RECEIVER, SENDER  
ab\_protocol  
Waiting to be proved: AB\_PROTOCOL#2  
Proved in VC generator: AB\_PROTOCOL#1, AB\_PROTOCOL#3, AB\_PROTOCOL#4  
receiver  
Waiting to be proved: RECEIVER#4, RECEIVER#5, RECEIVER#6, RECEIVER#8,  
RECEIVER#12, RECEIVER#13, RECEIVER#14, RECEIVER#18  
Proved in VC generator: RECEIVER#1, RECEIVER#2, RECEIVER#3, RECEIVER#7,  
RECEIVER#9, RECEIVER#10, RECEIVER#11, RECEIVER#15, RECEIVER#16,  
RECEIVER#17  
sender  
Waiting to be proved: SENDER#4, SENDER#5, SENDER#6, SENDER#7, SENDER#13,  
SENDER#20, SENDER#22, SENDER#28, SENDER#33  
Proved in VC generator: SENDER#1, SENDER#2, SENDER#3, SENDER#8,  
SENDER#9, SENDER#10, SENDER#11, SENDER#12, SENDER#14, SENDER#15,  
SENDER#16, SENDER#17, SENDER#18, SENDER#19, SENDER#21, SENDER#23,  
SENDER#24, SENDER#25, SENDER#26, SENDER#27, SENDER#29, SENDER#30,  
SENDER#31, SENDER#32  
SCOPE ALT\_BIT\_SPECS  
Waiting for pending body to be filled in: INITIAL\_SUBSEQ  
For specifications only: LAST\_BIT, MSG\_LAG, NCHANGES, NEXT\_SEQNUM,  
PROPER\_RECEPTION, PROPER\_TRANSMISSION, REPEATS, SEQNUMS, UNIQUE\_MSG

## SCOPE LEMMAS

Waiting for VC generation: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL, APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB, ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE, LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP, NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4, PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4, PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES

Exec-> save abp.dmp

File ABP.DMP already exists. Rewrite it? -> y

Saving.....

.....

.....

[PHOTO: Logging disabled Tue 5-May-81 9:41AM]

[PHOTO: Recording terminated Tue 5-May-81 9:43AM]

[PHOTO: Recording initiated Thu 7-May-81 7:52AM]

LINK FROM CMP.DIVITO, TTY 20

TOPS-20 Command processor 4(560)

[PHOTO: Logging disabled Thu 7-May-81 7:52AM]

PHOTO: Logging enabled Thu 7-May-81 7:55AM]

% We are now ready to do the proofs. We will first knock off the VCs

% and then take on the various lemmas. These will go in roughly a

% top down order. The lemmas which get proved in the Affirm system

% will simply be assumed here.

show status all

The current design and verification status is:

SCOPE ALT\_BIT\_PROTOCOL

Waiting for pending body to be filled in: MEDIUM, TIMER

Proved: COMP

Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET, PKT\_BUF, PKT\_SEQ

Check VCs (not fully checked): AB\_PROTOCOL, RECEIVER, SENDER

Check VCs (path pending): AB\_PROTOCOL, RECEIVER, SENDER

ab\_protocol

Waiting to be proved: AB\_PROTOCOL#2

Proved in VC generator: AB\_PROTOCOL#1, AB\_PROTOCOL#3, AB\_PROTOCOL#4  
receiver

Waiting to be proved: RECEIVER#4, RECEIVER#5, RECEIVER#6, RECEIVER#8,  
RECEIVER#12, RECEIVER#13, RECEIVER#14, RECEIVER#18

Proved in VC generator: RECEIVER#1, RECEIVER#2, RECEIVER#3, RECEIVER#7,

RECEIVER#9, RECEIVER#10, RECEIVER#11, RECEIVER#15, RECEIVER#16,  
RECEIVER#17

sender

Waiting to be proved: SENDER#4, SENDER#5, SENDER#6, SENDER#7, SENDER#13,  
SENDER#20, SENDER#22, SENDER#28, SENDER#33

Proved in VC generator: SENDER#1, SENDER#2, SENDER#3, SENDER#8,  
SENDER#9, SENDER#10, SENDER#11, SENDER#12, SENDER#14, SENDER#15,  
SENDER#16, SENDER#17, SENDER#18, SENDER#19, SENDER#21, SENDER#23,  
SENDER#24, SENDER#25, SENDER#26, SENDER#27, SENDER#29, SENDER#30,  
SENDER#31, SENDER#32

SCOPE ALT\_BIT\_SPECS

Waiting for pending body to be filled in: INITIAL\_SUBSEQ

For specifications only: LAST\_BIT, MSG\_LAG, NCHANGES, NEXT\_SEQNUM,

PROPER\_RECEPTION, PROPER\_TRANSMISSION, REPEATS, SEQNUMS, UNIQUE\_MSG

SCOPE LEMMAS

Waiting to be proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL,  
APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB,  
ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE,  
LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4,  
PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4,  
PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL,  
SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES

Exec-> prove sender#4

Entering Prover with verification condition sender#4

C1: next\_seqnum (null (#seqtype#)) = one

C2: proper\_transmission (null (#seqtype#), null (#seqtype#),  
null (#seqtype#), 0)

Backup point

(.)

Prvr-> \$Proceeding

Backup point

(. 1 .)

Prvr-> expand next\_seqnum

Backup point

(. 1 . E .)

Prvr-> theorem

C1: comp (last\_bit (seqnums (null (#seqtype#)))) = one

Prvr-> expand last\_bit

Backup point

(. 1 . E . E .)

Prvr-> expand seqnums

Backup point  
 (. 1 . E . E . E .)  
 Prvr-> theorem  
 C1: comp (if null (bit\_seq) = null (bit\_seq)  
 then zero  
 else null (bit\_seq)[size (null (bit\_seq))]  
 fi)  
 = one  
 Prvr-> simplify theorem  
 Prvr-> expand comp  
 Backup point  
 (. 1 . E . E . E . E .)  
 Prvr-> \$Proceeding  
 (. 1 .)  
 next\_seqnum (null (#seqtype#)) = one  
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 (. 2 .)  
 Prvr-> theorem  
 C1: proper\_transmission (null (#seqtype#), null (#seqtype#),  
 null (#seqtype#), 0)  
 Prvr-> expand proper\_transmission  
 Backup point  
 (. 2 . E .)  
 Prvr->theorem  
 C1: 0 = size (unique\_msg (null (#seqtype#)))  
 C2: msg\_lag (unique\_msg (null (#seqtype#)), null (#seqtype#), 0)  
 C3: repeats (null (#seqtype#))  
 Prvr-> expand unique\_msg  
 Backup point  
 (. 2 . E . E .)  
 Prvr-> expand repeats  
 Backup point  
 (. 2 . E . E . E .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 C1: msg\_lag (null (msg\_seq), null (#seqtype#), 0)  
 Prvr-> expand msg\_lag  
 Backup point  
 (. 2 . E . E . E . E .)  
 Prvr-> theorem

C1: initial\_subseq (null (msg\_seq), null (#seqtype#))  
Prvr-> use eq\_iss  
\*\*\*\* EQ\_ISS is not known in scope ALT\_BIT\_PROTOCOL  
Illegal argument to USE  
Prvr-> use eq\_iss::lemmas  
Backup point  
(. 2 . E . E . E . U .)  
Prvr-> qed  
(. 2 . E . E . E . U . QED)  
(. 2 . E . E . E . U . QED BC)  
(. 2 . E . E . E . U . QED BC)  
null (msg\_seq) = null (#seqtype#)  
Proved  
QED  
Prvr-> \$Proceeding  
(. 2 .)  
proper\_transmission (null (#seqtype#), null (#seqtype#), null (#seqtype#),  
0)  
Proved  
Prvr-> \$Proceeding  
sender#4  
proved in theorem prover.  
Exec-> prove sender#5  
Entering Prover with verification condition sender#5  
H1: empty (source#1)  
H2: next\_seqnum (infrom (ack\_send, myid)) = next  
H3: next\_seqnum (outto (pkt\_send, myid)) = next  
H4: infrom (source, myid) = infrom (source#1, myid)  
H5: outto (source, myid) = outto (source#1, myid)  
H6: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
->  
C1: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
Backup point  
(.)  
Prvr-> retain h6  
Backup point  
(. D .)  
Prvr-> use prop\_trans\_6::lemmas  
Backup point  
(. D . U .)

Prvr-> qed  
(. D . U . QED)  
:::(. D . U . QED BC)  
(. D . U . QED BC)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
Proved  
QED  
Prvr-> \$Proceeding  
sender#5  
proved in theorem prover.  
Exec-> prove sender#6  
Entering Prover with verification condition sender#6  
H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)  
H2: next\_seqnum (infrom (ack\_send, myid)) = next  
H3: next\_seqnum (outto (pkt\_send, myid)) = next  
H4: infrom (pkt\_send, myid) = infrom (pkt\_send#1, myid)  
H5: outto (pkt\_send, myid) = outto (pkt\_send#1, myid)  
H6: outto (source, myid) = outto (source#2, myid)  
H7: full (pkt\_send#1)  
H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
->  
C1: proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
outto (pkt\_send, myid), infrom (ack\_send, myid), 1)  
Backup point  
(.)  
Prvr-> retain h8  
Backup point  
(. D .)  
Prvr-> use prop\_trans\_5::lemmas  
Backup point  
(. D . U .)  
Prvr-> qed  
(. D . U . QED)  
:::(. D . U . QED BC)  
(. D . U . QED BC)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)  
Proved  
QED  
Prvr-> \$Proceeding

sender#6  
 proved in theorem prover.  
 Exec-> prove sender#7  
 Entering Prover with verification condition sender#7  
 H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)  
 H2: outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)]  
 = outto (pkt\_send#2, myid)  
 H3: next\_seqnum (infrom (ack\_send, myid)) = next  
 H4: next\_seqnum (outto (pkt\_send, myid)) = next  
 H5: infrom (pkt\_send, myid) = infrom (pkt\_send#2, myid)  
 H6: infrom (start, myid) = infrom (start#1, myid)  
 H7: outto (source, myid) = outto (source#2, myid)  
 H8: outto (start, myid) = outto (start#1, myid)  
 H9: full (start#1)  
 H10: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 0)  
 ->  
 C1: proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
 outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg;  
 .seqno:=next)],  
 infrom (ack\_send, myid), 1)  
 Backup point  
 ()  
 Prvr-> retain h4,h10  
 Backup point  
 (. D .)  
 Prvr-> use prop\_trans\_2::lemmas  
 Backup point  
 (. D . U .)  
 Prvr-> qed  
 (. D . U . QED)  
 :::(. D . U . QED BC)  
 (. D . U . QED BC 1)  
 (. D . U . QED BC 1)  
 pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg  
 Proved  
 (. D . U . QED BC 2)  
 (. D . U . QED BC 2)  
 pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno  
 = next\_seqnum (outto (pkt\_send, myid))

Proved  
(. D . U . QED BC 3)  
(. D . U . QED BC 3)  
proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

Proved  
(. D . U . QED BC)  
pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg  
& pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno  
= next\_seqnum (outto (pkt\_send, myid))  
& proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

Proved

QED

Prvr-> \$Proceeding

sender#7

proved in theorem prover.

Exec-> save

Enter file name-> abp.dmp

File ABP.DMP already exists. Rewrite it? -> y

Saving.....

.....  
.....  
.....

Exec-> show status sender

Check VCs (not fully checked): SENDER

Check VCs (path pending): SENDER

sender

Waiting to be proved: SENDER#13, SENDER#20, SENDER#22, SENDER#28,  
SENDER#33

Proved in VC generator: SENDER#1, SENDER#2, SENDER#3, SENDER#8,  
SENDER#9, SENDER#10, SENDER#11, SENDER#12, SENDER#14, SENDER#15,  
SENDER#16, SENDER#17, SENDER#18, SENDER#19, SENDER#21, SENDER#23,  
SENDER#24, SENDER#25, SENDER#26, SENDER#27, SENDER#29, SENDER#30,  
SENDER#31, SENDER#32

Proved in theorem prover: SENDER#4, SENDER#5, SENDER#6, SENDER#7

Exec-> prove sender#13

Entering Prover with verification condition sender#13

H1: infrom (source, myid) [seq: pack#1.mssg] = infrom (source#2, myid)

H2: outto (pkt\_send, myid)

[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)]  
= outto (pkt\_send#2, myid)

H3: next\_seqnum (infrom (ack\_send, myid)) = next  
 H4: next\_seqnum (outto (pkt\_send, myid)) = next  
 H5: infrom (pkt\_send, myid) = infrom (pkt\_send#2, myid)  
 H6: outto (source, myid) = outto (source#2, myid)  
 H7: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 0)  
 ->  
 C1: infrom (source, myid) [seq: pack#1.mssg]  
 = unique\_msg ( outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])  
 C2: size (unique\_msg ( outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg;  
 .seqno:=next)])  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 C3: proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
 outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg;  
 .seqno:=next)],  
 infrom (ack\_send, myid), 1)  
 Backup point  
 (.)  
 Prvr-> retain h4,h7  
 Backup point  
 (. D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 1 .)  
 Prvr-> theorem  
 H1: next\_seqnum (outto (pkt\_send, myid)) = next  
 H2: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 0)  
 ->  
 C1: infrom (source, myid) [seq: pack#1.mssg]  
 = unique\_msg ( outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])  
 Prvr-> use prop\_trans\_1::lemmas  
 Backup point  
 (. D . 1 . U .)  
 Prvr-> qed  
 (. D . 1 . U . QED)  
 ::Conclusion simplified to:  
 infrom (source, myid) [seq: pack#1.mssg]

```

= unique_msg ( outto (pkt_send, myid)
  [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)]).( D . 1 .
U . QED BC)
( D . 1 . U . QED BC 1)
( D . 1 . U . QED BC 1)
pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg
Proved
( D . 1 . U . QED BC 2)
( D . 1 . U . QED BC 2)
pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno
= next_seqnum (outto (pkt_send, myid))
Proved
( D . 1 . U . QED BC 3)
::( D . 1 . U . QED BC 3)
proper_transmission (infrom (source, myid), outto (pkt_send, myid), y#8$, 0)
Proved
( D . 1 . U . QED BC)
pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg
& pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno
= next_seqnum (outto (pkt_send, myid))
& proper_transmission (infrom (source, myid), outto (pkt_send, myid), y#8$,
0)
Proved
QED
Prvr-> $Proceeding
( D . 1 .)
infrom (source, myid) [seq: pack#1.mssg]
= unique_msg ( outto (pkt_send, myid)
  [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])
Proved
Prvr-> $Proceeding
Backup point
( D . 2 .)
Prvr-> theorem
H1: next_seqnum (outto (pkt_send, myid)) = next
H2: proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 0)
->
C1: size (unique_msg ( outto (pkt_send, myid)
  [seq: pack with (.mssg:=pack#1.mssg;
.seqno:=next)]))
= size (unique_msg (infrom (ack_send, myid))) + 1

```

Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: unique\_msg ( outto (pkt\_send, myid)  
 [seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])  
 2: unique\_msg (infrom (ack\_send, myid))  
 Which do you want to expand? 1  
 Backup point  
 (. D . 2 . E .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: next\_seqnum (outto (pkt\_send, myid)) = next  
 H2: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 0)  
 ->  
 C1: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid)))  
 Prvr-> expand proper\_transmission  
 Backup point  
 (. D . 2 . E . E .)  
 Prvr-> simplify hypothesis  
 Prvr-> theorem  
 H1: next\_seqnum (outto (pkt\_send, myid)) = next  
 H2: size (unique\_msg (infrom (ack\_send, myid)))  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H3: size (unique\_msg (infrom (ack\_send, myid))) = size (infrom (source,  
 myid))  
 H4: msg\_lag (unique\_msg (outto (pkt\_send, myid)), infrom (source, myid), 0)  
 H5: repeats (outto (pkt\_send, myid))  
 ->  
 C1: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid)))  
 Prvr-> equality substitute h2  
 H2 can be solved for:  
 T1: size (unique\_msg (infrom (ack\_send, myid)))  
 T2: size (unique\_msg (outto (pkt\_send, myid)))  
 Which term (by label) do you want to substitute for?  
 t1  
 size (unique\_msg (infrom (ack\_send, myid))) :=  
 size (unique\_msg (outto (pkt\_send, myid)))  
 OK??  
 y

TypeList equalities

`size (infrom (source, myid)) = size (unique_msg (outto (pkt_send, myid)))`

Backup point

(. D . 2 . E . E . =S .)

Prvr-> \$Proceeding

(. D . 2 .)

`size (unique_msg ( outto (pkt_send, myid)`  
`[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)])])`  
`= size (unique_msg (infrom (ack_send, myid))) + 1`

Proved

Prvr-> \$Proceeding

Backup point

(. D . 3 .)

Prvr-> theorem

H1: `next_seqnum (outto (pkt_send, myid)) = next`

H2: `proper_transmission (infrom (source, myid), outto (pkt_send, myid),`  
`infrom (ack_send, myid), 0)`

->

C1: `proper_transmission (infrom (source, myid) [seq: pack#1.mssg],`  
`outto (pkt_send, myid)`  
`[seq: pack with (.mssg:=pack#1.mssg;`  
`.seqno:=next)],`  
`infrom (ack_send, myid), 1)`

Prvr-> use prop\_trans\_2::lemmas

Backup point

(. D . 3 . U .)

Prvr-> qed

(. D . 3 . U . QED)

:::(. D . 3 . U . QED BC)

(. D . 3 . U . QED BC 1)

(. D . 3 . U . QED BC 1)

`pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg`

Proved

(. D . 3 . U . QED BC 2)

(. D . 3 . U . QED BC 2)

`pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno`  
`= next_seqnum (outto (pkt_send, myid))`

Proved

(. D . 3 . U . QED BC 3)

(. D . 3 . U . QED BC 3)

`proper_transmission (infrom (source, myid), outto (pkt_send, myid),`  
`infrom (ack_send, myid), 0)`

Proved

(. D . 3 . U . QED BC)

pack with (.mssg:=pack#1.mssg; .seqno:=next).mssg = pack#1.mssg  
& pack with (.mssg:=pack#1.mssg; .seqno:=next).seqno  
= next\_seqnum (outto (pkt\_send, myid))  
& proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 0)

Proved

QED

Prvr-> \$Proceeding

(. D . 3 .)

proper\_transmission (infrom (source, myid) [seq: pack#1.mssg],  
outto (pkt\_send, myid)  
[seq: pack with (.mssg:=pack#1.mssg; .seqno:=next)],  
infrom (ack\_send, myid), 1)

Proved

Prvr-> \$Proceeding

sender#13

proved in theorem prover.

Exec-> prove sender#20

Entering Prover with verification condition sender#20

H1: infrom (ack\_send, myid) [seq: ack#1] = infrom (ack\_send#3, myid)

H2: pack.seqno = next

H3: next\_seqnum (infrom (ack\_send, myid)) = next

H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H5: outto (ack\_send, myid) = outto (ack\_send#3, myid)

H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H7: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H9: ack#1.seqno ne next

H10: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: next\_seqnum (infrom (ack\_send, myid) [seq: ack#1]) = next

C2: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid) [seq: ack#1])) + 1

C3: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid) [seq: ack#1], 1)

TypeList equalities

size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

Backup point  
 (. )  
 Prvr-> retain h3,h7,h8,h9  
 Typelist equalities  
 size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 Backup point  
 (. D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 1 .)  
 Prvr-> theorem  
 H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H2: next\_seqnum (infrom (ack\_send, myid)) = next  
 H3: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H4: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)  
 H5: ack#1.seqno ne next  
 ->  
 C1: next\_seqnum (infrom (ack\_send, myid) [seq: ack#1]) = next  
 Prvr-> retain h2,h5  
 Backup point  
 (. D . 1 . D .)  
 Prvr-> use ne\_next::lemmas  
 Typelist equalities  
 size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 & size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 Backup point  
 (. D . 1 . D . U .)  
 Prvr-> hypothesis  
 H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H2: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H3: p#8\$.seqno ne next\_seqnum (x#12\$)  
 -> next\_seqnum (x#12\$ [seq: p#8\$]) = next\_seqnum (x#12\$)  
 H4: next\_seqnum (infrom (ack\_send, myid)) = next  
 H5: ack#1.seqno ne next

Prvr-> reorder h4,h3,h5  
 Backup point  
 (. D . 1 . D . U . REORDER .)  
 Prvr-> qed  
 (. D . 1 . D . U . REORDER . QED)  
 :::::  
 next := next\_seqnum (infrom (ack\_send, myid))  
 (. D . 1 . D . U . REORDER . QED =S)  
 :::::  
 size (unique\_msg (infrom (ack\_send, myid))) :=  
 size (unique\_msg (outto (pkt\_send, myid))) - 1  
 (. D . 1 . D . U . REORDER . QED =S =S)  
 ::(. D . 1 . D . U . REORDER . QED =S =S BC)  
 (. D . 1 . D . U . REORDER . QED =S =S BC)  
 ack#1.seqno ne next\_seqnum (infrom (ack\_send, myid))  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 (. D . 1 .)  
 next\_seqnum (infrom (ack\_send, myid) [seq: ack#1]) = next  
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 2 .)  
 Prvr-> theorem  
 H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H2: next\_seqnum (infrom (ack\_send, myid)) = next  
 H3: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H4: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)  
 H5: ack#1.seqno ne next  
 ->  
 C1: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid) [seq: ack#1])) + 1  
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: unique\_msg (infrom (ack\_send, myid))  
 2: unique\_msg (outto (pkt\_send, myid))  
 3: unique\_msg (infrom (ack\_send, myid) [seq: ack#1])

Which do you want to expand? 3

Backup point

(. D . 2 . E .)

Prvr-> simplify theorem

Prvr->theorem

H1: next\_seqnum (infrom (ack\_send, myid)) = next

H2: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

H3: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H4: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H5: ack#1.seqno ne next

->

C1: size (unique\_msg (outto (pkt\_send, myid)))

= size (if ack#1.seqno = next\_seqnum (infrom (ack\_send, myid))

then unique\_msg (infrom (ack\_send, myid))

[seq: ack#1.mssg]

else unique\_msg (infrom (ack\_send, myid))

fi) + 1

Prvr-> equality substitute h1

H1 yields

next\_seqnum (infrom (ack\_send, myid)) := next

Backup point

(. D . 2 . E . =S .)

Prvr-> simplify theorem

Prvr->theorem

C1: true

Prvr-> \$Proceeding

(. D . 2 .)

size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid) [seq: ack#1])) + 1

Proved

Prvr-> \$Proceeding

Backup point

(. D . 3 .)

Prvr-> theorem

H1: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

H2: next\_seqnum (infrom (ack\_send, myid)) = next

H3: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H4: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H5: ack#1.seqno ne next

->

C1: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid) [seq: ack#1], 1)

Prvr-> use prop\_trans\_4::lemmas

Backup point

(. D . 3 . U .)

Prvr-> qed

(. D . 3 . U . QED)

:::::(. D . 3 . U . QED BC)

(. D . 3 . U . QED BC 1)

(. D . 3 . U . QED BC 1)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

Proved

(. D . 3 . U . QED BC 2)

:::::

size (unique\_msg (infrom (ack\_send, myid))) :=

size (unique\_msg (outto (pkt\_send, myid))) - 1

(. D . 3 . U . QED BC 2 =S)

::::

next\_seqnum (infrom (ack\_send, myid)) := next

(. D . 3 . U . QED BC 2 =S =S)

(. D . 3 . U . QED BC 2)

ack#1.seqno ne next\_seqnum (infrom (ack\_send, myid))

Proved

(. D . 3 . U . QED BC)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

& ack#1.seqno ne next\_seqnum (infrom (ack\_send, myid))

Proved

QED

Prvr-> \$Proceeding

(. D . 3 .)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid) [seq: ack#1], 1)

Proved

Prvr-> \$Proceeding

sender#20

proved in theorem prover.

Exec->  
save  
Enter file name-> abp.dmp  
File ABP.DMP already exists. Rewrite it? -> y  
Saving.....  
.....  
.....

Exec-> prove sender#22  
Entering Prover with verification condition sender#22  
H1: outto (pkt\_send, myid) [seq: pack] = outto (pkt\_send#4, myid)  
H2: pack.seqno = next  
H3: next\_seqnum (infrom (ack\_send, myid)) = next  
H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
H5: infrom (pkt\_send, myid) = infrom (pkt\_send#4, myid)  
H6: infrom (start, myid) = infrom (start#3, myid)  
H7: outto (start, myid) = outto (start#3, myid)  
H8: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
H9: size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
H10: full (start#3)  
H11: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
H12: null (pkt\_seq) ne outto (pkt\_send, myid)  
->  
C1: proper\_transmission (infrom (source, myid),  
outto (pkt\_send, myid) [seq: pack],  
infrom (ack\_send, myid), 1)  
Typelist equalities  
size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
Backup point  
(.)  
Prvr-> retain h8,h11,h12  
Backup point  
(. D .)  
Prvr-> use prop\_trans\_3::lemmas  
Typelist equalities  
size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
& size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1

Backup point

(. D . U .)

Prvr-> qed

(. D . U . QED)

::::::.

size (unique\_msg (infrom (ack\_send, myid))) :=  
 size (unique\_msg (outto (pkt\_send, myid))) - 1  
 (. D . U . QED =S)

::::.

pack := outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]  
 (. D . U . QED =S =S)  
 ::::::::::::(. D . U . QED =S =S BC)  
 (. D . U . QED =S =S BC 1)  
 (. D . U . QED =S =S BC 1)  
 outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]  
 = outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]

Proved

(. D . U . QED =S =S BC 2)  
 (. D . U . QED =S =S BC 2)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)

Proved

(. D . U . QED =S =S BC 3)  
 (. D . U . QED =S =S BC 3)

null (pkt\_seq) ne outto (pkt\_send, myid)

Proved

(. D . U . QED =S =S BC)

outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]  
 = outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]  
 & proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)  
 & null (pkt\_seq) ne outto (pkt\_send, myid)

Proved

QED

Prvr-> \$Proceeding

sender#22

proved in theorem prover.

Exec-> prove sender#28

Entering Prover with verification condition sender#28

H1: outto (pkt\_send, myid) [seq: pack] = outto (pkt\_send#4, myid)

H2: pack.seqno = next

H3: next\_seqnum (infrom (ack\_send, myid)) = next

H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
 H5: infrom (pkt\_send, myid) = infrom (pkt\_send#4, myid)  
 H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
 H7: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)  
 H9: null (pkt\_seq) ne outto (pkt\_send, myid)  
 ->  
 C1: unique\_msg (outto (pkt\_send, myid) [seq: pack])  
 = infrom (source, myid)  
 C2: size (unique\_msg (outto (pkt\_send, myid) [seq: pack]))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 C3: proper\_transmission (infrom (source, myid),  
 outto (pkt\_send, myid) [seq: pack],  
 infrom (ack\_send, myid), 1)  
 Typelist equalities  
 size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 Backup point  
 (. )  
 Prvr-> retain h4,h6,h7,h8,h9  
 Typelist equalities  
 size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 Backup point  
 (. D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 1 .)  
 Prvr-> theorem  
 H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H2: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
 H3: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
 H4: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H5: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
 infrom (ack\_send, myid), 1)  
 H6: null (pkt\_seq) ne outto (pkt\_send, myid)  
 ->  
 C1: unique\_msg (outto (pkt\_send, myid) [seq: pack])

```

= infrom (source, myid)
Prvr-> retain h2,h3,h6
Backup point
(. D . 1 . D .)
Prvr-> use last_unique::lemmas
Typelist equalities
size (unique_msg (infrom (ack_send, myid))) + 1
= size (unique_msg (outto (pkt_send, myid)))
& size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
Backup point
(. D . 1 . D . U .)
Prvr-> hypothesis
H1: size (unique_msg (infrom (ack_send, myid))) + 1
= size (unique_msg (outto (pkt_send, myid)))
H2: size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
H3: x#18$[size (x#18$)] = p#14$ & null (pkt_seq) ne x#18$
-> unique_msg (x#18$ [seq: p#14$]) = unique_msg (x#18$)
H4: unique_msg (outto (pkt_send, myid)) = infrom (source, myid)
H5: outto (pkt_send, myid)[size (outto (pkt_send, myid))] = pack
H6: null (pkt_seq) ne outto (pkt_send, myid)
Prvr-> delete h1,h2
Backup point
(. D . 1 . D . U . D .)
Prvr-> qed
(. D . 1 . D . U . D . QED)
::::.
infrom (source, myid) := unique_msg (outto (pkt_send, myid))
(. D . 1 . D . U . D . QED =S)
::::.
pack := outto (pkt_send, myid)[size (outto (pkt_send, myid))]
(. D . 1 . D . U . D . QED =S =S)
::::(. D . 1 . D . U . D . QED =S =S BC)
(. D . 1 . D . U . D . QED =S =S BC 1)
(. D . 1 . D . U . D . QED =S =S BC 1)
outto (pkt_send, myid)[size (outto (pkt_send, myid))]
= outto (pkt_send, myid)[size (outto (pkt_send, myid))]
Proved
(. D . 1 . D . U . D . QED =S =S BC 2)
(. D . 1 . D . U . D . QED =S =S BC 2)
null (pkt_seq) ne outto (pkt_send, myid)

```

Proved

(. D . 1 . D . U . D . QED =S =S BC)

outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]

= outto (pkt\_send, myid)[size (outto (pkt\_send, myid))]

& null (pkt\_seq) ne outto (pkt\_send, myid)

Proved

QED

Prvr-> \$Proceeding

(. D . 1 .)

unique\_msg (outto (pkt\_send, myid) [seq: pack]) = infrom (source, myid)

Proved

Prvr-> \$Proceeding

Backup point

(. D . 2 .)

Prvr-> theorem

H1: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

H2: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H3: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H4: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H5: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

H6: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: size (unique\_msg (outto (pkt\_send, myid) [seq: pack]))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

Prvr-> delete h4,h5

TypeList equalities

size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

Backup point

(. D . 2 . D .)

Prvr-> use last\_unique::lemmas

Backup point

(. D . 2 . D . U .)

Prvr-> hypothesis

H1: x#20\$[size (x#20\$)] = p#16\$ & null (pkt\_seq) ne x#20\$

-> unique\_msg (x#20\$ [seq: p#16\$]) = unique\_msg (x#20\$)

H2: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H3: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))  
H4: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
H5: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
H6: null (pkt\_seq) ne outto (pkt\_send, myid)

Prvr-> forwardchain h1

:::::Forward chaining gives

unique\_msg (outto (pkt\_send, myid) [seq: pack])  
= unique\_msg (outto (pkt\_send, myid))

Backup point

(. D . 2 . D . U . FC .)

Prvr-> theorem

H1: unique\_msg (outto (pkt\_send, myid) [seq: pack])  
= unique\_msg (outto (pkt\_send, myid))  
H2: x#20\$[size (x#20\$)] = p#16\$ & null (pkt\_seq) ne x#20\$  
-> unique\_msg (x#20\$ [seq: p#16\$]) = unique\_msg (x#20\$)  
H3: size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
H4: size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
H5: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
H7: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: size (unique\_msg (outto (pkt\_send, myid) [seq: pack]))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1

Prvr-> equality substitute h1

H1 yields

unique\_msg (outto (pkt\_send, myid) [seq: pack]) :=  
unique\_msg (outto (pkt\_send, myid))

Backup point

(. D . 2 . D . U . FC . =S .)

Prvr-> \$Proceeding

(. D . 2 .)

size (unique\_msg (outto (pkt\_send, myid) [seq: pack]))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1

Proved

Prvr-> \$Proceeding

Backup point

(. D . 3 .)

Prvr-> theorem

H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))

H2: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H3: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H4: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H5: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

H6: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: proper\_transmission (infrom (source, myid),

outto (pkt\_send, myid) [seq: pack],

infrom (ack\_send, myid), 1)

Prvr-> use prop\_trans\_3::lemmas

Backup point

(. D . 3 . U .)

Prvr-> qed

(. D . 3 . U . QED)

:::::::(. D . 3 . U . QED BC)

(. D . 3 . U . QED BC 1)

(. D . 3 . U . QED BC 1)

outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

Proved

(. D . 3 . U . QED BC 2)

(. D . 3 . U . QED BC 2)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

Proved

(. D . 3 . U . QED BC 3)

(. D . 3 . U . QED BC 3)

null (pkt\_seq) ne outto (pkt\_send, myid)

Proved

(. D . 3 . U . QED BC)

outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

& proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

& null (pkt\_seq) ne outto (pkt\_send, myid)

Proved

QED

Prvr-> \$Proceeding

(. D . 3 .)

proper\_transmission (infrom (source, myid),

outto (pkt\_send, myid) [seq: pack],

infrom (ack\_send, myid), 1)

Proved  
Prvr-> \$Proceeding  
sender#28

proved in theorem prover.

[PHOTO: Recording initiated Sat 9-May-81 9:55AM]

LINK FROM CMP.DIVITO, TTY 20

TOPS-20 Command processor 4(560)

[PHOTO: Logging disabled Sat 9-May-81 9:55AM]

PHOTO: Logging enabled Sat 9-May-81 10:04AM]

prove sender#33

Entering Prover with verification condition sender#33

H1: infrom (ack\_send, myid) [seq: ack#1] = infrom (ack\_send#3, myid)

H2: ack#1.seqno = next

H3: pack.seqno = next

H4: next\_seqnum (infrom (ack\_send, myid)) = next

H5: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H6: outto (ack\_send, myid) = outto (ack\_send#3, myid)

H7: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H8: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H9: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H10: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: comp (next)

= next\_seqnum (infrom (ack\_send, myid) [seq: ack#1])

C2: comp (next) = next\_seqnum (outto (pkt\_send, myid))

C3: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid) [seq: ack#1], 0)

TypeList equalities

size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

Backup point

(.)

Prvr-> delete h1,h6

Backup point

(. D .)

Prvr-> \$Proceeding

Backup point

(. D . 1 .)

Prvr-> theorem

H1: size (unique\_msg (infrom (ack\_send, myid))) + 1

```

= size (unique_msg (outto (pkt_send, myid)))
H2: ack#1.seqno = next
H3: pack.seqno = next
H4: next_seqnum (infrom (ack_send, myid)) = next
H5: unique_msg (outto (pkt_send, myid)) = infrom (source, myid)
H6: outto (pkt_send, myid)[size (outto (pkt_send, myid))] = pack
H7: size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
H8: proper_transmission (infrom (source, myid), outto (pkt_send, myid),
infrom (ack_send, myid), 1)
H9: null (pkt_seq) ne outto (pkt_send, myid)
->
C1: comp (next)
= next_seqnum (infrom (ack_send, myid) [seq: ack#1])
Prvr-> retain h2
Backup point
(. D . 1 . D .)
Prvr-> use next_comp::lemmas
Typelist equalities
size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
& size (unique_msg (infrom (ack_send, myid))) + 1
= size (unique_msg (outto (pkt_send, myid)))
Backup point
(. D . 1 . D . U .)
Prvr-> theorem
H1: size (unique_msg (outto (pkt_send, myid)))
= size (unique_msg (infrom (ack_send, myid))) + 1
H2: size (unique_msg (infrom (ack_send, myid))) + 1
= size (unique_msg (outto (pkt_send, myid)))
H3: comp (p#20$.seqno) = next_seqnum (x#24$ [seq: p#20$])
H4: ack#1.seqno = next
->
C1: comp (next)
= next_seqnum (infrom (ack_send, myid) [seq: ack#1])
Prvr-> delete h1,h2
Backup point
(. D . 1 . D . U . D .)
Prvr-> qed
(. D . 1 . D . U . D . QED)
:::
next := ack#1.seqno

```

(. D . 1 . D . U . D . QED =S)  
QED  
Prvr-> \$Proceeding  
(. D . 1 .)  
comp (next) = next\_seqnum (infrom (ack\_send, myid) [seq: ack#1])  
Proved  
Prvr-> \$Proceeding  
Backup point  
(. D . 2 .)  
Prvr-> theorem  
H1: size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
H2: ack#1.seqno = next  
H3: pack.seqno = next  
H4: next\_seqnum (infrom (ack\_send, myid)) = next  
H5: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)  
H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
H7: size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)  
H9: null (pkt\_seq) ne outto (pkt\_send, myid)  
->  
C1: comp (next) = next\_seqnum (outto (pkt\_send, myid))  
Prvr-> retain h3,h6,h9  
Backup point  
(. D . 2 . D .)  
Prvr-> use last\_next::lemmas  
Typelist equalities  
size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
& size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
Backup point  
(. D . 2 . D . U .)  
Prvr-> theorem  
H1: size (unique\_msg (outto (pkt\_send, myid)))  
= size (unique\_msg (infrom (ack\_send, myid))) + 1  
H2: size (unique\_msg (infrom (ack\_send, myid))) + 1  
= size (unique\_msg (outto (pkt\_send, myid)))  
H3: x#26\$[size (x#26\$)] = p#22\$ & null (pkt\_seq) ne x#26\$  
-> p#22\$.seqno ne next\_seqnum (x#26\$)

H4: pack.seqno = next  
 H5: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
 H6: null (pkt\_seq) ne outto (pkt\_send, myid)  
 ->  
 C1: comp (next) = next\_seqnum (outto (pkt\_send, myid))  
 Prvr-> forwardchain h3  
 ::::Forward chaining gives  
 pack.seqno ne next\_seqnum (outto (pkt\_send, myid))  
 Backup point  
 (. D . 2 . D . U . FC .)  
 Prvr-> hypothesis  
 H1: pack.seqno ne next\_seqnum (outto (pkt\_send, myid))  
 H2: size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 H3: size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))  
 H4: x#26\$[size (x#26\$)] = p#22\$ & null (pkt\_seq) ne x#26\$  
 -> p#22\$.seqno ne next\_seqnum (x#26\$)  
 H5: pack.seqno = next  
 H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack  
 H7: null (pkt\_seq) ne outto (pkt\_send, myid)  
 Prvr-> retain h1,h5  
 Backup point  
 (. D . 2 . D . U . FC . D .)  
 Prvr-> hypothesis  
 H1: pack.seqno ne next\_seqnum (outto (pkt\_send, myid))  
 H2: pack.seqno = next  
 Prvr-> equality substitute h2  
 H2 yields  
 next := pack.seqno  
 Backup point  
 (. D . 2 . D . U . FC . D . =S .)  
 Prvr-> theorem  
 H1: pack.seqno ne next\_seqnum (outto (pkt\_send, myid))  
 ->  
 C1: comp (pack.seqno) = next\_seqnum (outto (pkt\_send, myid))  
 Prvr-> use comp\_ne::lemmas  
 Typelist equalities  
 size (unique\_msg (outto (pkt\_send, myid)))  
 = size (unique\_msg (infrom (ack\_send, myid))) + 1  
 & size (unique\_msg (infrom (ack\_send, myid))) + 1  
 = size (unique\_msg (outto (pkt\_send, myid)))

Backup point

(. D . 2 . D . U . FC . D . =S . U .)

Prvr-> theorem

H1: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H2: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

H3: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$

H4: pack.seqno ne next\_seqnum (outto (pkt\_send, myid))

->

C1: comp (pack.seqno) = next\_seqnum (outto (pkt\_send, myid))

Prvr-> forwardchain h3

Which way? (left or right)

left

:::Forward chaining gives

comp (pack.seqno) = next\_seqnum (outto (pkt\_send, myid))

Backup point

(. D . 2 . D . U . FC . D . =S . U . FC .)

Prvr-> \$Proceeding

(. D . 2 .)

comp (next) = next\_seqnum (outto (pkt\_send, myid))

Proved

Prvr-> \$Proceeding

Backup point

(. D . 3 .)

Prvr-> theorem

H1: size (unique\_msg (infrom (ack\_send, myid))) + 1

= size (unique\_msg (outto (pkt\_send, myid)))

H2: ack#1.seqno = next

H3: pack.seqno = next

H4: next\_seqnum (infrom (ack\_send, myid)) = next

H5: unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

H6: outto (pkt\_send, myid)[size (outto (pkt\_send, myid))] = pack

H7: size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

H8: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid), 1)

H9: null (pkt\_seq) ne outto (pkt\_send, myid)

->

C1: proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),  
infrom (ack\_send, myid) [seq: ack#1], 0)

Prvr-> use prop\_trans\_7::lemmas

Backup point

(. D . 3 . U .)

Prvr-> qed

(. D . 3 . U . QED)

::::::::::(. D . 3 . U . QED BC)

(. D . 3 . U . QED BC 1)

::::::::::::

size (unique\_msg (infrom (ack\_send, myid))) :=

size (unique\_msg (outto (pkt\_send, myid))) - 1

(. D . 3 . U . QED BC 1 =S)

::::::::::::

ack#1.seqno := next

(. D . 3 . U . QED BC 1 =S =S)

(. D . 3 . U . QED BC 1)

ack#1.seqno = next\_seqnum (infrom (ack\_send, myid))

Proved

(. D . 3 . U . QED BC 2)

(. D . 3 . U . QED BC 2)

unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

Proved

(. D . 3 . U . QED BC 3)

(. D . 3 . U . QED BC 3)

size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

Proved

(. D . 3 . U . QED BC 4)

(. D . 3 . U . QED BC 4)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

Proved

(. D . 3 . U . QED BC)

ack#1.seqno = next\_seqnum (infrom (ack\_send, myid))

& unique\_msg (outto (pkt\_send, myid)) = infrom (source, myid)

& size (unique\_msg (outto (pkt\_send, myid)))

= size (unique\_msg (infrom (ack\_send, myid))) + 1

& proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid), 1)

Proved

QED

Prvr-> \$Proceeding

(. D . 3 .)

proper\_transmission (infrom (source, myid), outto (pkt\_send, myid),

infrom (ack\_send, myid) [seq: ack#1], 0)  
Proved  
Prvr-> \$Proceeding  
sender#33  
proved in theorem prover.  
Exec-> show status sender  
Proved: SENDER  
sender#1 . . . sender#33 proved.  
Exec-> show status receiver  
receiver  
Waiting to be proved: RECEIVER#4, RECEIVER#5, RECEIVER#6, RECEIVER#8,  
RECEIVER#12, RECEIVER#13, RECEIVER#14, RECEIVER#18  
Proved in VC generator: RECEIVER#1, RECEIVER#2, RECEIVER#3, RECEIVER#7,  
RECEIVER#9, RECEIVER#10, RECEIVER#11, RECEIVER#15, RECEIVER#16,  
RECEIVER#17  
Exec-> prove receiver#4  
Entering Prover with verification condition receiver#4  
C1: next\_seqnum (null (#seqtype#)) = one  
C2: proper\_reception (null (#seqtype#), null (#seqtype#), null (#seqtype#),  
0)  
Backup point  
(.)  
Prvr-> \$Proceeding  
Backup point  
(. 1 .)  
Prvr-> expand next\_seqnum  
Backup point  
(. 1 . E .)  
Prvr-> theorem  
C1: comp (last\_bit (seqnums (null (#seqtype#)))) = one  
Prvr-> expand seqnums  
Backup point  
(. 1 . E . E .)  
Prvr->expand last\_bit  
Backup point  
(. 1 . E . E . E .)  
Prvr-> expand comp  
Backup point  
(. 1 . E . E . E . E .)  
Prvr-> simplify theorem  
Prvr-> \$Proceeding  
(. 1 .)

```

next_seqnum (null (#seqtype#)) = one
Proved
Prvr-> $Proceeding
Backup point
(. 2 .)
Prvr-> theorem
C1: proper_reception (null (#seqtype#), null (#seqtype#), null (#seqtype#),
0)
Prvr-> expand proper_reception
Backup point
(. 2 . E .)
Prvr-> theorem
C1: 0 = size (unique_msg (null (#seqtype#)))
C2: msg_lag (null (#seqtype#), unique_msg (null (#seqtype#)), 0)
Prvr-> expand unique_msg
Backup point
(. 2 . E . E .)
Prvr->expand msg_lag
Backup point
(. 2 . E . E . E .)
Prvr-> theorem
C1: 0 = size (null (msg_seq))
C2: initial_subseq (null (#seqtype#), null (msg_seq))
Prvr-> simplify theorem
Prvr-> use eq_iss::lemmas
Backup point
(. 2 . E . E . E . U .)
Prvr-> qed
(. 2 . E . E . E . U . QED)
(. 2 . E . E . E . U . QED BC)
(. 2 . E . E . E . U . QED BC)
null (#seqtype#) = null (msg_seq)
Proved
QED
Prvr-> $Proceeding
(. 2 .)
proper_reception (null (#seqtype#), null (#seqtype#), null (#seqtype#), 0)
Proved
Prvr-> $Proceeding
receiver#4
proved in theorem prover.
Exec-> prove receiver#5

```

Entering Prover with verification condition receiver#5

H1: empty (pkt\_rcv#1)

H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H3: next\_seqnum (outto (ack\_rcv, myid)) = exp

H4: infrom (pkt\_rcv, myid) = infrom (pkt\_rcv#1, myid)

H5: outto (pkt\_rcv, myid) = outto (pkt\_rcv#1, myid)

H6: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

->

C1: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 1)

Backup point

(.)

Prvr-> retain h6

Backup point

(. D .)

Prvr-> use prop\_rec\_3::lemmas

Backup point

(. D . U .)

Prvr-> qed

(. D . U . QED)

::(. D . U . QED BC)

(. D . U . QED BC)

proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

Proved

QED

Prvr-> \$Proceeding

receiver#5

proved in theorem prover.

Exec-> prove receiver#6

Entering Prover with verification condition receiver#6

H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)

H2: pack#1.seqno = exp

H3: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H4: next\_seqnum (outto (ack\_rcv, myid)) = exp

H5: infrom (sink, myid) = infrom (sink#1, myid)

H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)

H7: outto (sink, myid) = outto (sink#1, myid)

H8: full (sink#1)

H9: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

->

C1: proper\_reception (outto (sink, myid),  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid), 1)

Backup point

(.)

Prvr-> retain h9

Backup point

(. D .)

Prvr-> use prop\_rec\_2::lemmas

Backup point

(. D . U .)

Prvr-> qed

(. D . U . QED)

::(. D . U . QED BC)

(. D . U . QED BC)

proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)

Proved

QED

Prvr-> \$Proceeding

receiver#6

proved in theorem prover.

Exec-> prove receiver#8

Entering Prover with verification condition receiver#8

H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)

H2: outto (sink, myid) [seq: pack#1.mssg] = outto (sink#2, myid)

H3: pack#1.seqno = exp

H4: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H5: next\_seqnum (outto (ack\_rcv, myid)) = exp

H6: infrom (ack\_rcv, myid) = infrom (ack\_rcv#1, myid)

H7: infrom (sink, myid) = infrom (sink#2, myid)

H8: outto (ack\_rcv, myid) = outto (ack\_rcv#1, myid)

H9: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)

H10: full (ack\_rcv#1)

H11: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)

->

C1: proper\_reception (outto (sink, myid) [seq: pack#1.mssg],  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid), 1)

Backup point

(.)  
Prvr-> retain h3,h4,h11  
Backup point  
(. D .)  
Prvr-> use prop\_rec\_1::lemmas  
Backup point  
(. D . U .)  
Prvr-> qed  
(. D . U . QED)  
::::(. D . U . QED BC)  
(. D . U . QED BC 1)  
(. D . U . QED BC 1)  
pack#1.mssg = pack#1.mssg  
Proved  
(. D . U . QED BC 2)  
::::.  
pack#1.seqno := exp  
(. D . U . QED BC 2 =S)  
(. D . U . QED BC 2)  
pack#1.seqno = next\_seqnum (infrom (pkt\_rcv, myid))  
Proved  
(. D . U . QED BC 3)  
(. D . U . QED BC 3)  
proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
Proved  
(. D . U . QED BC)  
pack#1.mssg = pack#1.mssg  
& pack#1.seqno = next\_seqnum (infrom (pkt\_rcv, myid))  
& proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
Proved  
QED  
Prvr-> \$Proceeding  
receiver#8  
proved in theorem prover.  
Exec-> prove receiver#13  
Entering Prover with verification condition receiver#13  
H1: empty (pkt\_rcv#1)  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: infrom (pkt\_rcv, myid) = infrom (pkt\_rcv#1, myid)

H5: outto (pkt\_rcv, myid) = outto (pkt\_rcv#1, myid)  
 H6: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 ->  
 C1: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 1)  
 Backup point  
 (. )  
 Prvr-> retain h6  
 Backup point  
 (. D .)  
 Prvr-> use prop\_rec\_3::lemmas  
 Backup point  
 (. D . U .)  
 Prvr-> qed  
 (. D . U . QED)  
 ::(. D . U . QED BC)  
 (. D . U . QED BC)  
 proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 receiver#13  
 proved in theorem prover.  
 Exec-> prove receiver#14  
 Entering Prover with verification condition receiver#14  
 H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)  
 H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
 H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
 H4: infrom (ack\_rcv, myid) = infrom (ack\_rcv#3, myid)  
 H5: outto (ack\_rcv, myid) = outto (ack\_rcv#3, myid)  
 H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)  
 H7: full (ack\_rcv#3)  
 H8: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 H9: pack#1.seqno ne exp  
 ->  
 C1: proper\_reception (outto (sink, myid),  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid), 1)  
 Backup point

(.)  
Prvr-> retain h8  
Backup point  
(. D .)  
Prvr-> use prop\_rec\_2::lemmas  
Backup point  
(. D . U .)  
Prvr-> qed  
(. D . U . QED)  
:::(. D . U . QED BC)  
(. D . U . QED BC)  
proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
Proved  
QED  
Prvr-> \$Proceeding  
receiver#14  
proved in theorem prover.  
Exec-> save abp.dmp  
File ABP.DMP already exists. Rewrite it? -> y  
Saving.....  
.....  
.....  
Exec-> show status receiver  
receiver  
Waiting to be proved: RECEIVER#12, RECEIVER#18  
Proved in VC generator: RECEIVER#1, RECEIVER#2, RECEIVER#3, RECEIVER#7,  
RECEIVER#9, RECEIVER#10, RECEIVER#11, RECEIVER#15, RECEIVER#16,  
RECEIVER#17  
Proved in theorem prover: RECEIVER#4, RECEIVER#5, RECEIVER#6,  
RECEIVER#8, RECEIVER#13, RECEIVER#14  
Exec-> prove receiver#12  
Entering Prover with verification condition receiver#12  
H1: infrom (pkt\_rcv, myid) [seq: pack#1] = infrom (pkt\_rcv#2, myid)  
H2: outto (ack\_rcv, myid) [seq: pack#1] = outto (ack\_rcv#2, myid)  
H3: outto (sink, myid) [seq: pack#1.mssg] = outto (sink#2, myid)  
H4: pack#1.seqno = exp  
H5: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H6: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H7: infrom (ack\_rcv, myid) = infrom (ack\_rcv#2, myid)  
H8: infrom (sink, myid) = infrom (sink#2, myid)

H9: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)  
 H10: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 ->  
 C1: comp (exp)  
 = next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1])  
 C2: comp (exp) = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])  
 C3: proper\_reception (outto (sink, myid) [seq: pack#1.mssg],  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid) [seq: pack#1], 0)  
 Backup point  
 (. )  
 Prvr-> retain h4,h5,h6,h10  
 Backup point  
 (. D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 1 .)  
 Prvr-> use next\_comp::lemmas  
 Backup point  
 (. D . 1 . U .)  
 Prvr-> theorem  
 H1: comp (p#8\$.seqno) = next\_seqnum (x#12\$ [seq: p#8\$])  
 H2: pack#1.seqno = exp  
 H3: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
 H4: next\_seqnum (outto (ack\_rcv, myid)) = exp  
 H5: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 ->  
 C1: comp (exp)  
 = next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1])  
 Prvr-> put  
 For what?\* p#8\$;  
 Put what?\* pack#1;  
 For what?\* \$done  
 Backup point  
 (. D . 1 . U . PUT .)  
 Prvr-> equality substitute h3  
 H3 yields  
 exp := next\_seqnum (infrom (pkt\_rcv, myid))  
 Backup point  
 (. D . 1 . U . PUT . =S .)

Prvr-> theorem

H1: pack#1.seqno = next\_seqnum (infrom (pkt\_rcv, myid))  
H2: comp (pack#1.seqno) = next\_seqnum (x#12\$ [seq: pack#1])  
H3: next\_seqnum (infrom (pkt\_rcv, myid))  
= next\_seqnum (outto (ack\_rcv, myid))  
H4: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

->

C1: comp (next\_seqnum (infrom (pkt\_rcv, myid)))  
= next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1])

Prvr-> equality substitute h1

H1 yields

next\_seqnum (infrom (pkt\_rcv, myid)) := pack#1.seqno

Backup point

(. D . 1 . U . PUT . =S . =S .)

Prvr-> \$Proceeding

::( D . 1 .)

comp (exp) = next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1])

Proved

Prvr-> \$Proceeding

Backup point

(. D . 2 .)

Prvr-> \$Proceeding

:.....Ran out of tricks

Prvr-> theorem

H1: pack#1.seqno = exp  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

->

C1: comp (exp) = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])

Prvr-> equality substitute h1

H1 yields

exp := pack#1.seqno

Backup point

(. D . 2 . =S .)

Prvr-> theorem

H1: pack#1.seqno = next\_seqnum (infrom (pkt\_rcv, myid))  
H2: pack#1.seqno = next\_seqnum (outto (ack\_rcv, myid))  
H3: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

->

C1: comp (pack#1.seqno) = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])  
Prvr-> retain h2  
Backup point  
(. D . 2 . =S . D .)  
Prvr-> use next\_comp::lemmas  
Backup point  
(. D . 2 . =S . D . U .)  
Prvr-> theorem  
H1: comp (p#10\$.seqno) = next\_seqnum (x#14\$ [seq: p#10\$])  
H2: pack#1.seqno = next\_seqnum (outto (ack\_rcv, myid))  
->  
C1: comp (pack#1.seqno) = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])  
Prvr-> \$Proceeding  
:(. D . 2 .)  
comp (exp) = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])  
Proved  
Prvr-> \$Proceeding  
Backup point  
(. D . 3 .)  
Prvr-> theorem  
H1: pack#1.seqno = exp  
H2: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
H3: next\_seqnum (outto (ack\_rcv, myid)) = exp  
H4: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)  
->  
C1: proper\_reception (outto (sink, myid) [seq: pack#1.mssg],  
infrom (pkt\_rcv, myid) [seq: pack#1],  
outto (ack\_rcv, myid) [seq: pack#1], 0)  
Prvr-> use prop\_rec\_4::lemmas  
Backup point  
(. D . 3 . U .)  
Prvr-> qed  
(. D . 3 . U . QED)  
:::::(. D . 3 . U . QED BC)  
(. D . 3 . U . QED BC 1)  
(. D . 3 . U . QED BC 1)  
pack#1.mssg = pack#1.mssg  
Proved

```

(. D . 3 . U . QED BC 2)
::::.
pack#1.seqno := exp
(. D . 3 . U . QED BC 2 =S)
(. D . 3 . U . QED BC 2)
pack#1.seqno = next_seqnum (infrom (pkt_rcv, myid))
Proved
(. D . 3 . U . QED BC 3)
::::.
pack#1.seqno := exp
(. D . 3 . U . QED BC 3 =S)
(. D . 3 . U . QED BC 3)
pack#1.seqno = next_seqnum (outto (ack_rcv, myid))
Proved
(. D . 3 . U . QED BC 4)
(. D . 3 . U . QED BC 4)
proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
Proved
(. D . 3 . U . QED BC)
pack#1.mssg = pack#1.mssg
& pack#1.seqno = next_seqnum (infrom (pkt_rcv, myid))
& pack#1.seqno = next_seqnum (outto (ack_rcv, myid))
& proper_reception (outto (sink, myid), infrom (pkt_rcv, myid),
outto (ack_rcv, myid), 0)
Proved
QED
Prvr-> $Proceeding
(. D . 3 .)
proper_reception (outto (sink, myid) [seq: pack#1.mssg],
infrom (pkt_rcv, myid) [seq: pack#1],
outto (ack_rcv, myid) [seq: pack#1], 0)
Proved
Prvr-> $Proceeding
receiver#12
proved in theorem prover.
Exec-> prove receiver#18
Entering Prover with verification condition receiver#18
H1: infrom (pkt_rcv, myid) [seq: pack#1] = infrom (pkt_rcv#2, myid)
H2: outto (ack_rcv, myid) [seq: pack#1] = outto (ack_rcv#4, myid)
H3: next_seqnum (infrom (pkt_rcv, myid)) = exp
H4: next_seqnum (outto (ack_rcv, myid)) = exp

```

H5: infrom (ack\_rcv, myid) = infrom (ack\_rcv#4, myid)  
 H6: outto (pkt\_rcv, myid) = outto (pkt\_rcv#2, myid)  
 H7: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 H8: pack#1.seqno ne exp  
 ->  
 C1: next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp  
 C2: next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1]) = exp  
 C3: proper\_reception (outto (sink, myid),  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid) [seq: pack#1], 0)  
 Backup point  
 (. )  
 Prvr-> retain h3,h4,h7,h8  
 Backup point  
 (. D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 1 .)  
 Prvr-> theorem  
 H1: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
 H2: next\_seqnum (outto (ack\_rcv, myid)) = exp  
 H3: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 H4: pack#1.seqno ne exp  
 ->  
 C1: next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp  
 Prvr-> retain h1,h4  
 Backup point  
 (. D . 1 . D .)  
 Prvr-> use next\_comp::lemmas  
 Backup point  
 (. D . 1 . D . U .)  
 Prvr-> use comp\_ne::lemmas  
 Backup point  
 (. D . 1 . D . U . U .)  
 Prvr-> theorem  
 H1: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$  
 H2: comp (p#14\$.seqno) = next\_seqnum (x#18\$ [seq: p#14\$])  
 H3: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
 H4: pack#1.seqno ne exp  
 ->

C1: next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp

Prvr-> forwardchain h1

Which way? (left or right)

left

:::Forward chaining gives

comp (pack#1.seqno) = exp

Backup point

(. D . 1 . D . U . U . FC .)

Prvr-> theorem

H1: comp (pack#1.seqno) = exp

H2: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$

H3: comp (p#14\$.seqno) = next\_seqnum (x#18\$ [seq: p#14\$])

H4: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H5: pack#1.seqno ne exp

->

C1: next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp

Prvr-> equality substitute h1

H1 yields

exp := comp (pack#1.seqno)

Backup point

(. D . 1 . D . U . U . FC . =S .)

Prvr-> theorem

H1: comp (p#14\$.seqno) = next\_seqnum (x#18\$ [seq: p#14\$])

H2: comp (pack#1.seqno) = next\_seqnum (infrom (pkt\_rcv, myid))

H3: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$

H4: pack#1.seqno ne comp (pack#1.seqno)

->

C1: comp (pack#1.seqno)

= next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1])

Prvr-> retain h1,h2

Backup point

(. D . 1 . D . U . U . FC . =S . D .)

Prvr-> \$Proceeding

:(. D . 1 .)

next\_seqnum (infrom (pkt\_rcv, myid) [seq: pack#1]) = exp

Proved

Prvr-> \$Proceeding

Backup point

(. D . 2 .)

Prvr-> theorem

H1: next\_seqnum (infrom (pkt\_rcv, myid)) = exp

H2: next\_seqnum (outto (ack\_rcv, myid)) = exp

H3: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
outto (ack\_rcv, myid), 0)

H4: pack#1.seqno ne exp

->

C1: next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1]) = exp

Prvr-> retain h2,h4

Backup point

(. D . 2 . D .)

Prvr-> use next\_comp::lemmas

Backup point

(. D . 2 . D . U .)

Prvr-> use comp\_ne::lemmas

Backup point

(. D . 2 . D . U . U .)

Prvr-> theorem

H1: comp (b1#4\$) = b2#4\$ iff b1#4\$ ne b2#4\$

H2: comp (p#16\$.seqno) = next\_seqnum (x#20\$ [seq: p#16\$])

H3: next\_seqnum (outto (ack\_rcv, myid)) = exp

H4: pack#1.seqno ne exp

->

C1: next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1]) = exp

Prvr-> forwardchain h1

Which way? (left or right)

left

:::Forward chaining gives

comp (pack#1.seqno) = exp

Backup point

(. D . 2 . D . U . U . FC .)

Prvr-> hypothesis

H1: comp (pack#1.seqno) = exp

H2: comp (b1#4\$) = b2#4\$ iff b1#4\$ ne b2#4\$

H3: comp (p#16\$.seqno) = next\_seqnum (x#20\$ [seq: p#16\$])

H4: next\_seqnum (outto (ack\_rcv, myid)) = exp

H5: pack#1.seqno ne exp

Prvr-> equality substitute h1

H1 yields

exp := comp (pack#1.seqno)

Backup point

(. D . 2 . D . U . U . FC . =S .)

Prvr-> theorem

H1: comp (p#16\$.seqno) = next\_seqnum (x#20\$ [seq: p#16\$])

H2: comp (pack#1.seqno) = next\_seqnum (outto (ack\_rcv, myid))

H3: comp (b1#4\$) = b2#4\$ iff b1#4\$ ne b2#4\$  
 H4: pack#1.seqno ne comp (pack#1.seqno)  
 ->  
 C1: comp (pack#1.seqno)  
 = next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1])  
 Prvr-> retain h1,h2  
 Backup point  
 (. D . 2 . D . U . U . FC . =S . D .)  
 Prvr-> \$Proceeding  
 :(. D . 2 .)  
 next\_seqnum (outto (ack\_rcv, myid) [seq: pack#1]) = exp  
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 (. D . 3 .)  
 Prvr-> theorem  
 H1: next\_seqnum (infrom (pkt\_rcv, myid)) = exp  
 H2: next\_seqnum (outto (ack\_rcv, myid)) = exp  
 H3: proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 H4: pack#1.seqno ne exp  
 ->  
 C1: proper\_reception (outto (sink, myid),  
 infrom (pkt\_rcv, myid) [seq: pack#1],  
 outto (ack\_rcv, myid) [seq: pack#1], 0)  
 Prvr-> use prop\_rec\_5::lemmas  
 Backup point  
 (. D . 3 . U .)  
 Prvr-> qed  
 (. D . 3 . U . QED)  
 :::::(. D . 3 . U . QED BC)  
 (. D . 3 . U . QED BC 1)  
 (. D . 3 . U . QED BC 1)  
 proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 Proved  
 (. D . 3 . U . QED BC 2)  
 :::::  
 next\_seqnum (infrom (pkt\_rcv, myid)) := exp  
 (. D . 3 . U . QED BC 2 =S)  
 (. D . 3 . U . QED BC 2)  
 pack#1.seqno ne next\_seqnum (infrom (pkt\_rcv, myid))

Proved  
 (. D . 3 . U . QED BC 3)  
 :::::  
 next\_seqnum (outto (ack\_rcv, myid)) := exp  
 (. D . 3 . U . QED BC 3 =S)  
 (. D . 3 . U . QED BC 3)  
 pack#1.seqno ne next\_seqnum (outto (ack\_rcv, myid))  
 Proved  
 (. D . 3 . U . QED BC)  
 proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid),  
 outto (ack\_rcv, myid), 0)  
 & pack#1.seqno ne next\_seqnum (infrom (pkt\_rcv, myid))  
 & pack#1.seqno ne next\_seqnum (outto (ack\_rcv, myid))  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 (. D . 3 .)  
 proper\_reception (outto (sink, myid), infrom (pkt\_rcv, myid)  
 [seq: pack#1],  
 outto (ack\_rcv, myid) [seq: pack#1], 0)  
 Proved  
 Prvr-> \$Proceeding  
 receiver#18  
 proved in theorem prover.  
 Exec-> show status receiver  
 Proved: RECEIVER  
 receiver#1 . . . receiver#18 proved.  
 Exec-> prove ab\_protocol  
 ab\_protocol#1  
 proved in VC generator.  
 Used in proof: TIMER, RECEIVER, MEDIUM, SENDER  
 Entering Prover with verification condition ab\_protocol#2  
 H1: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_rcv#1),  
 allo (ack\_rcv#1), 1)  
 H2: proper\_transmission (infrom (source#1, sender#1), allo (pkt\_send#1),  
 allfrom (ack\_send#1), 1)  
 H3: isblocked (medium#1)  
 H4: isblocked (medium#2)  
 H5: isblocked (receiver#1)  
 H6: isblocked (sender#1)  
 H7: isblocked (timer#1)  
 H8: allo (ack\_send#1) sub allfrom (ack\_rcv#1)

H9: allto (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: msg\_lag (outto (sink#1, receiver#1), infrom (source#1, sender#1), 1)  
 Backup point  
 (. )  
 Prvr-> retain h1,h2,h8,h9  
 Backup point  
 (. D .)  
 Prvr-> use abp\_1::lemmas  
 Backup point  
 (. D . U .)  
 Prvr-> theorem  
 H1: proper\_reception (v#2\$, x#2\$, y#2\$, 1)  
 & proper\_transmission (u#2\$, w#2\$, z#2\$, 1) & x#2\$ sub w#2\$  
 & z#2\$ sub y#2\$  
 -> msg\_lag (v#2\$, u#2\$, 1)  
 H2: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_rcv#1),  
 allto (ack\_rcv#1), 1)  
 H3: proper\_transmission (infrom (source#1, sender#1), allto (pkt\_send#1),  
 allfrom (ack\_send#1), 1)  
 H4: allto (ack\_send#1) sub allfrom (ack\_rcv#1)  
 H5: allto (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: msg\_lag (outto (sink#1, receiver#1), infrom (source#1, sender#1), 1)  
 Prvr-> qed  
 (. D . U . QED)  
 :::::(. D . U . QED BC)  
 (. D . U . QED BC 1)  
 :(.( D . U . QED BC 1)  
 proper\_reception (outto (sink#1, receiver#1), x#2\$, y#2\$, 1)  
 Proved  
 (. D . U . QED BC 2)  
 :::(. D . U . QED BC 2)  
 proper\_transmission (infrom (source#1, sender#1), w#2\$, z#2\$, 1)  
 Proved  
 (. D . U . QED BC 3)  
 :::::::::::::::Ran out of tricks  
 Prvr-> theorem  
 H1: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_rcv#1),  
 allto (ack\_rcv#1), 1)  
 H2: proper\_transmission (infrom (source#1, sender#1), allto (pkt\_send#1),  
 allfrom (ack\_send#1), 1)

H3: allto (ack\_send#1) sub allfrom (ack\_recv#1)  
 H4: allto (pkt\_recv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: allfrom (pkt\_recv#1) sub allto (pkt\_send#1)  
 Prvr-> label  
 (. D . U . QED BC 3)  
 Prvr-> back up 3  
 Restored  
 Backup point  
 (. D . U . QED .)  
 Prvr-> back up2  
 \*\*\* Illegal command - UP2  
 Back UP or establish a back up POINT to return to? up  
 How many levels would you like to back up? 2  
 Restored  
 Backup point  
 (. D . U .)  
 Prvr-> theorem  
 H1: proper\_reception (v#2\$, x#2\$, y#2\$, 1)  
 & proper\_transmission (u#2\$, w#2\$, z#2\$, 1) & x#2\$ sub w#2\$  
 & z#2\$ sub y#2\$  
 -> msg\_lag (v#2\$, u#2\$, 1)  
 H2: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_recv#1),  
 allto (ack\_recv#1), 1)  
 H3: proper\_transmission (infrom (source#1, sender#1), allto (pkt\_send#1),  
 allfrom (ack\_send#1), 1)  
 H4: allto (ack\_send#1) sub allfrom (ack\_recv#1)  
 H5: allto (pkt\_recv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: msg\_lag (outto (sink#1, receiver#1), infrom (source#1, sender#1), 1)  
 Prvr-> claim  
 Newgoal:  
 \* allfrom(ack\_send#1) sub allto(ack\_recv#1)  
 \* & allfrom(pkt\_recv#1) sub allto(pkt\_send#1);  
 Defer proof of claim? y  
 Backup point  
 (. D . U . .)  
 Prvr-> theorem  
 H1: allfrom (ack\_send#1) sub allto (ack\_recv#1)  
 H2: allfrom (pkt\_recv#1) sub allto (pkt\_send#1)  
 H3: proper\_reception (v#2\$, x#2\$, y#2\$, 1)  
 & proper\_transmission (u#2\$, w#2\$, z#2\$, 1) & x#2\$ sub w#2\$

```

& z#2$ sub y#2$
-> msg_lag (v#2$, u#2$, 1)
H4: proper_reception (outto (sink#1, receiver#1), allfrom (pkt_rcv#1),
allto (ack_rcv#1), 1)
H5: proper_transmission (infrom (source#1, sender#1), allto (pkt_send#1),
allfrom (ack_send#1), 1)
H6: allto (ack_send#1) sub allfrom (ack_rcv#1)
H7: allto (pkt_rcv#1) sub allfrom (pkt_send#1)
->
C1: msg_lag (outto (sink#1, receiver#1), infrom (source#1, sender#1), 1)
Prvr-> qed
(. D . U .. QED)
:::::::(. D . U .. QED BC)
(. D . U .. QED BC 1)
:::(. D . U .. QED BC 1)
proper_reception (outto (sink#1, receiver#1), x#2$, y#2$, 1)
Proved
(. D . U .. QED BC 2)
::::(. D . U .. QED BC 2)
proper_transmission (infrom (source#1, sender#1), w#2$, z#2$, 1)
Proved
(. D . U .. QED BC 3)
(. D . U .. QED BC 3)
allfrom (pkt_rcv#1) sub allto (pkt_send#1)
Proved
(. D . U .. QED BC 4)
(. D . U .. QED BC 4)
allfrom (ack_send#1) sub allto (ack_rcv#1)
Proved
(. D . U .. QED BC)
proper_reception (outto (sink#1, receiver#1), x#2$, y#2$, 1)
& proper_transmission (infrom (source#1, sender#1), w#2$, z#2$, 1)
& x#2$ sub w#2$ & z#2$ sub y#2$
Proved
QED
Prvr-> $Proceeding
Proved using CLAIM. Now prove the claim.
Backup point
(CLAIM .)
Prvr-> theorem
H1: proper_reception (v#2$, x#2$, y#2$, 1)
& proper_transmission (u#2$, w#2$, z#2$, 1) & x#2$ sub w#2$

```

& z#2\$ sub y#2\$  
 -> msg\_lag (v#2\$, u#2\$, 1)  
 H2: proper\_reception (outto (sink#1, receiver#1), allfrom (pkt\_rcv#1),  
 allo (ack\_rcv#1), 1)  
 H3: proper\_transmission (infrom (source#1, sender#1), allo (pkt\_send#1),  
 allfrom (ack\_send#1), 1)  
 H4: allo (ack\_send#1) sub allfrom (ack\_rcv#1)  
 H5: allo (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: allfrom (ack\_send#1) sub allo (ack\_rcv#1)  
 C2: allfrom (pkt\_rcv#1) sub allo (pkt\_send#1)  
 Prvr-> retain h4,h5  
 Backup point  
 (CLAIM . D .)  
 Prvr-> \$Proceeding  
 Backup point  
 (CLAIM . D . 1 .)  
 Prvr-> theorem  
 H1: allo (ack\_send#1) sub allfrom (ack\_rcv#1)  
 H2: allo (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
 ->  
 C1: allfrom (ack\_send#1) sub allo (ack\_rcv#1)  
 Prvr-> delete h2  
 Backup point  
 (CLAIM . D . 1 . D .)  
 Prvr-> \$Proceeding  
 Ran out of tricks  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: allo (ack\_send#1) sub allfrom (ack\_rcv#1)  
 ->  
 C1: allfrom (ack\_send#1) sub allo (ack\_rcv#1)  
 Prvr-> use hist\_sub::lemmas  
 Backup point  
 (CLAIM . D . 1 . D . U .)  
 Prvr-> qed  
 (CLAIM . D . 1 . D . U . QED)  
 ::(CLAIM . D . 1 . D . U . QED BC)  
 (CLAIM . D . 1 . D . U . QED BC)  
 allfrom (ack\_send#1) sub allfrom (ack\_rcv#1)  
 Proved  
 QED

Prvr-> \$Proceeding  
(CLAIM . D . 1 .)  
allfrom (ack\_send#1) sub allto (ack\_rcv#1)  
Proved  
Prvr-> \$Proceeding  
Backup point  
(CLAIM . D . 2 .)  
Prvr-> theorem  
H1: allto (ack\_send#1) sub allfrom (ack\_rcv#1)  
H2: allto (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
->  
C1: allfrom (pkt\_rcv#1) sub allto (pkt\_send#1)  
Prvr-> delete h1  
Backup point  
(CLAIM . D . 2 . D .)  
Prvr-> use hist\_sub::lemmas  
Backup point  
(CLAIM . D . 2 . D . U .)  
Prvr-> qed  
(CLAIM . D . 2 . D . U . QED)  
::(CLAIM . D . 2 . D . U . QED BC)  
(CLAIM . D . 2 . D . U . QED BC)  
allfrom (pkt\_rcv#1) sub allfrom (pkt\_send#1)  
Proved  
QED  
Prvr-> \$Proceeding  
(CLAIM . D . 2 .)  
allfrom (pkt\_rcv#1) sub allto (pkt\_send#1)  
Proved  
Prvr-> \$Proceeding  
(CLAIM .)  
allfrom (ack\_send#1) sub allto (ack\_rcv#1)  
& allfrom (pkt\_rcv#1) sub allto (pkt\_send#1)  
Established claim  
ab\_protocol#2  
proved in theorem prover.  
Used in proof: TIMER, RECEIVER, MEDIUM, SENDER  
ab\_protocol#3  
proved in VC generator.  
Used in proof: TIMER, RECEIVER, MEDIUM, SENDER  
ab\_protocol#4  
proved in VC generator.

Used in proof: TIMER, RECEIVER, MEDIUM, SENDER

Exec-> show status scope \$

SCOPE ALT\_BIT\_PROTOCOL

Waiting for pending body to be filled in: MEDIUM, TIMER

Proved: AB\_PROTOCOL, COMP, RECEIVER, SENDER

Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET, PKT\_BUF, PKT\_SEQ

Exec-> show status scope lemmas

SCOPE LEMMAS

Waiting to be proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL, APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB, ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE, LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP, NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4, PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4, PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES

Exec-> save abp.dmp

File ABP.DMP already exists. Rewrite it? -> y

Saving.....

.....

.....

Exec-> exit no

4@pop

@pop

[PHOTO: Recording terminated Sat 9-May-81 10:44AM]

[PHOTO: Recording initiated Sat 9-May-81 10:54AM]

LINK FROM CMP.DIVITO, TTY 20

TOPS-20 Command processor 4(560)

[PHOTO: Logging disabled Sat 9-May-81 10:54AM]

PHOTO: Logging enabled Sat 9-May-81 10:57AM]

% It is now time to prove the lemmas. We will start with the

% higher level ones and move down to the lower level ones.

show status all

The current design and verification status is:

SCOPE ALT\_BIT\_PROTOCOL

Waiting for pending body to be filled in: MEDIUM, TIMER

Proved: AB\_PROTOCOL, COMP, RECEIVER, SENDER

Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET, PKT\_BUF, PKT\_SEQ

SCOPE ALT\_BIT\_SPECS

Waiting for pending body to be filled in: INITIAL\_SUBSEQ

For specifications only: LAST\_BIT, MSG\_LAG, NCHANGES, NEXT\_SEQNUM,  
PROPER\_RECEPTION, PROPER\_TRANSMISSION, REPEATS, SEQNUMS, UNIQUE\_MSG  
SCOPE LEMMAS

Waiting to be proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL,  
APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB,  
ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE,  
LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4,  
PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4,  
PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL,  
SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES

Exec-> set scope lemmas

Exec-> prove prop\_trans\_1

Entering Prover with lemma prop\_trans\_1

all u : msg\_seq,

all x, y : pkt\_seq,

all p : packet,

all m : message,

p.mssg = m & p.seqno = next\_seqnum (x)

& proper\_transmission (u, x, y, 0)

-> u [seq: m] = unique\_msg (x [seq: p])

H1: p.mssg = m

H2: p.seqno = next\_seqnum (x)

H3: proper\_transmission (u, x, y, 0)

->

C1: u [seq: m] = unique\_msg (x [seq: p])

Backup point

(.)

Prvr-> expand proper\_transmission

Backup point

(. E .)

Prvr-> simplify theorem

Prvr->theorem

H1: p.mssg = m

H2: p.seqno = next\_seqnum (x)

H3: size (unique\_msg (y)) = size (unique\_msg (x))

H4: size (unique\_msg (y)) = size (u)

H5: msg\_lag (unique\_msg (x), u, 0)

H6: repeats (x)

->

C1: u [seq: m] = unique\_msg (x [seq: p])

Prvr-> retain h1,h2,h5  
 Backup point  
 (. E . D .)  
 Prvr-> use msg\_lag\_eq  
 Backup point  
 (. E . D . U .)  
 Prvr-> hypothesis  
 H1:  $u \#2\$ = v \#2\$$  iff  $\text{msg\_lag}(u \#2\$, v \#2\$, 0)$   
 H2:  $p.\text{mssg} = m$   
 H3:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H4:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 0)$   
 Prvr-> forwardchain h1  
 Which way? (left or right)  
 left  
 ::::Forward chaining gives  
 $\text{unique\_msg}(x) = u$   
 Backup point  
 (. E . D . U . FC .)  
 Prvr-> theorem  
 H1:  $\text{unique\_msg}(x) = u$   
 H2:  $u \#2\$ = v \#2\$$  iff  $\text{msg\_lag}(u \#2\$, v \#2\$, 0)$   
 H3:  $p.\text{mssg} = m$   
 H4:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H5:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 0)$   
 ->  
 C1:  $u [\text{seq: } m] = \text{unique\_msg}(x [\text{seq: } p])$   
 Prvr-> equality substitute htheorem  
 HTHEOREM not in last output  
 \*\*\*\* Command Aborted  
 Prvr-> equality substitute h1  
 H1 yields  
 $u := \text{unique\_msg}(x)$   
 Backup point  
 (. E . D . U . FC . =S .)  
 Prvr-> theorem  
 H1:  $p.\text{mssg} = m$   
 H2:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H3:  $u \#2\$ = v \#2\$$  iff  $\text{msg\_lag}(u \#2\$, v \#2\$, 0)$   
 H4:  $\text{msg\_lag}(\text{unique\_msg}(x), \text{unique\_msg}(x), 0)$   
 ->  
 C1:  $\text{unique\_msg}(x) [\text{seq: } m] = \text{unique\_msg}(x [\text{seq: } p])$   
 Prvr-> delete h3,h4

Backup point  
 $(. E . D . U . FC . =S . D .)$   
 Prvr-> equality substitute h1  
 H1 yields  
 $m := p.mssg$   
 Backup point  
 $(. E . D . U . FC . =S . D . =S .)$   
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: unique\_msg (x)  
 2: unique\_msg (x [seq: p])  
 Which do you want to expand? 2  
 Backup point  
 $(. E . D . U . FC . =S . D . =S . E .)$   
 Prvr-> conclusion  
 C1: unique\_msg (x) [seq: p.mssg]  
 $= \text{if } p.seqno = \text{next\_seqnum} (x)$   
 $\text{then unique\_msg} (x) [\text{seq: } p.mssg]$   
 $\text{else unique\_msg} (x)$   
 fi  
 Prvr-> simplify theorem  
 Prvr->theorem  
 C1: true  
 Prvr-> \$Proceeding  
 prop\_trans\_1 proved in theorem prover.  
 Exec-> prove prop\_trans\_2  
 Entering Prover with lemma prop\_trans\_2  
 all u : msg\_seq,  
 all x, y : pkt\_seq,  
 all p : packet,  
 all m : message,  
 $p.mssg = m \ \& \ p.seqno = \text{next\_seqnum} (x)$   
 $\& \ \text{proper\_transmission} (u, x, y, 0)$   
 $\rightarrow \text{proper\_transmission} (u [\text{seq: } m], x [\text{seq: } p], y, 1)$   
 H1:  $p.mssg = m$   
 H2:  $p.seqno = \text{next\_seqnum} (x)$   
 H3:  $\text{proper\_transmission} (u, x, y, 0)$   
 $\rightarrow$   
 C1:  $\text{proper\_transmission} (u [\text{seq: } m], x [\text{seq: } p], y, 1)$   
 Backup point  
 $(.)$

Prvr-> expand proper\_transmission  
 More than one to expand.  
 Which do you want to expand? all  
 Backup point  
 (. E .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: p.mssg = m  
 H2: p.seqno = next\_seqnum (x)  
 H3: size (unique\_msg (y)) = size (unique\_msg (x))  
 H4: size (unique\_msg (y)) = size (u)  
 H5: msg\_lag (unique\_msg (x), u, 0)  
 H6: repeats (x)  
 ->  
 C1: msg\_lag (unique\_msg (x [seq: p]), u [seq: m], 1)  
 C2: repeats (x [seq: p])  
 C3: size (unique\_msg (x [seq: p])) - size (unique\_msg (y))  
 in [0..1]  
 C4: (size (u) - size (unique\_msg (y))) + 1 in [0..1]  
 Prvr-> equality substitute h4  
 H4 can be solved for:  
 T1: size (unique\_msg (y))  
 T2: size (u)  
 Which term (by label) do you want to substitute for?  
 t1  
 size (unique\_msg (y)) := size (u)  
 OK??  
 y  
 Backup point  
 (. E . =S .)  
 Prvr-> use msg\_lag\_eq  
 Backup point  
 (. E . =S . U .)  
 Prvr-> hypothesis  
 H1: u#2\$ = v#2\$ iff msg\_lag (u#2\$, v#2\$, 0)  
 H2: p.mssg = m  
 H3: p.seqno = next\_seqnum (x)  
 H4: size (u) = size (unique\_msg (x))  
 H5: msg\_lag (unique\_msg (x), u, 0)  
 H6: repeats (x)  
 Prvr-> forwardchain h1  
 Which way? (left or right)

left  
 ::::Forward chaining gives  
 $\text{unique\_msg}(x) = u$   
 Backup point  
 $(. \text{ E } . = S . U . \text{ FC } .)$   
 Prvr-> theorem  
 H1:  $\text{unique\_msg}(x) = u$   
 H2:  $u \# 2\$ = v \# 2\$$  iff  $\text{msg\_lag}(u \# 2\$, v \# 2\$, 0)$   
 H3:  $p.\text{mssg} = m$   
 H4:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H5:  $\text{size}(u) = \text{size}(\text{unique\_msg}(x))$   
 H6:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 0)$   
 H7: repeats( $x$ )  
 $\rightarrow$   
 C1:  $\text{msg\_lag}(\text{unique\_msg}(x \text{ [seq: } p]), u \text{ [seq: } m], 1)$   
 C2: repeats( $x \text{ [seq: } p]$ )  
 C3:  $\text{size}(\text{unique\_msg}(x \text{ [seq: } p])) - \text{size}(u)$  in  $[0..1]$   
 Prvr-> equality substitute h1,h3  
 H1 yields  
 $u := \text{unique\_msg}(x)$   
 H3 yields  
 $m := p.\text{mssg}$   
 Backup point  
 $(. \text{ E } . = S . U . \text{ FC } . = S .)$   
 Prvr-> theorem  
 H1:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H2:  $u \# 2\$ = v \# 2\$$  iff  $\text{msg\_lag}(u \# 2\$, v \# 2\$, 0)$   
 H3:  $\text{msg\_lag}(\text{unique\_msg}(x), \text{unique\_msg}(x), 0)$   
 H4: repeats( $x$ )  
 $\rightarrow$   
 C1:  $\text{msg\_lag}(\text{unique\_msg}(x \text{ [seq: } p]), \text{unique\_msg}(x) \text{ [seq: } p.\text{mssg}], 1)$   
 C2: repeats( $x \text{ [seq: } p]$ )  
 C3:  $\text{size}(\text{unique\_msg}(x \text{ [seq: } p])) - \text{size}(\text{unique\_msg}(x))$   
 in  $[0..1]$   
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1:  $\text{unique\_msg}(x)$   
 2:  $\text{unique\_msg}(x \text{ [seq: } p])$   
 Which do you want to expand? 2  
 Backup point

(. E . =S . U . FC . =S . E .)

Prvr-> simplify theorem

Prvr->theorem

H1: p.seqno = next\_seqnum (x)

H2: u#2\$ = v#2\$ iff msg\_lag (u#2\$, v#2\$, 0)

H3: msg\_lag (unique\_msg (x), unique\_msg (x), 0)

H4: repeats (x)

->

C1: msg\_lag (unique\_msg (x) [seq: p.mssg],  
unique\_msg (x) [seq: p.mssg], 1)

C2: repeats (x [seq: p])

Prvr-> retain h1,h4

Backup point

(. E . =S . U . FC . =S . E . D .)

Prvr-> \$Proceeding

Backup point

(. E . =S . U . FC . =S . E . D . 1 .)

Prvr-> theorem

H1: p.seqno = next\_seqnum (x)

H2: repeats (x)

->

C1: msg\_lag (unique\_msg (x) [seq: p.mssg],  
unique\_msg (x) [seq: p.mssg], 1)

Prvr-> expand msg\_lag

Backup point

(. E . =S . U . FC . =S . E . D . 1 . E .)

Prvr-> use eq\_iss

TypeList equalities

size (u) = size (unique\_msg (x))

Backup point

(. E . =S . U . FC . =S . E . D . 1 . E . U .)

Prvr-> theorem

H1: size (u) = size (unique\_msg (x))

H2: u#4\$ = v#4\$ -> initial\_subseq (u#4\$, v#4\$)

H3: p.seqno = next\_seqnum (x)

H4: repeats (x)

->

C1: initial\_subseq (unique\_msg (x) [seq: p.mssg],  
unique\_msg (x) [seq: p.mssg])

Prvr-> retain h2

Backup point

(. E . =S . U . FC . =S . E . D . 1 . E . U . D .)

Prvr-> qed  
 (. E . =S . U . FC . =S . E . D . 1 . E . U . D . QED)  
 (. E . =S . U . FC . =S . E . D . 1 . E . U . D . QED BC)  
 (. E . =S . U . FC . =S . E . D . 1 . E . U . D . QED BC)  
 unique\_msg (x) [seq: p.mssg] = unique\_msg (x) [seq: p.mssg]  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 (. E . =S . U . FC . =S . E . D . 1 .)  
 msg\_lag (unique\_msg (x) [seq: p.mssg],  
 unique\_msg (x) [seq: p.mssg], 1)  
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 (. E . =S . U . FC . =S . E . D . 2 .)  
 Prvr-> theorem  
 H1: p.seqno = next\_seqnum (x)  
 H2: repeats (x)  
 ->  
 C1: repeats (x [seq: p])  
 Prvr-> expand repeats  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: repeats (x)  
 2: repeats (x [seq: p])  
 Which do you want to expand? 2  
 Typelist equalities  
 size (u) = size (unique\_msg (x))  
 Backup point  
 (. E . =S . U . FC . =S . E . D . 2 . E .)  
 Prvr-> theorem  
 H1: size (u) = size (unique\_msg (x))  
 H2: null (pkt\_seq) ne x  
 H3: p.seqno = next\_seqnum (x)  
 H4: repeats (x)  
 ->  
 C1: repeats (x)  
 C2: p.seqno ne next\_seqnum (x) -> x[size (x)] = p  
 Prvr-> back up 2  
 Restored  
 Backup point  
 (. E . =S . U . FC . =S . E . D . 2 .)

Prvr-> theorem

H1: p.seqno = next\_seqnum (x)

H2: repeats (x)

->

C1: repeats (x [seq: p])

Prvr-> use last\_repeats

TypeList equalities

size (u) = size (unique\_msg (x))

Backup point

(. E . =S . U . FC . =S . E . D . 2 . U .)

Prvr-> qed

(. E . =S . U . FC . =S . E . D . 2 . U . QED)

:::::(. E . =S . U . FC . =S . E . D . 2 . U . QED BC)

(. E . =S . U . FC . =S . E . D . 2 . U . QED BC 1)

:::::Ran out of tricks

Prvr-> back up 4

Restored

Backup point

(. E . =S . U . FC . =S . E . D . 2 . U .)

Prvr-> theorem

H1: size (u) = size (unique\_msg (x))

H2: x#2\$[size (x#2\$)] = p#2\$ & repeats (x#2\$) & null (pkt\_seq)

ne x#2\$

-> repeats (x#2\$ [seq: p#2\$])

H3: p.seqno = next\_seqnum (x)

H4: repeats (x)

->

C1: repeats (x [seq: p])

Prvr-> back up 2

Restored

Backup point

(. E . =S . U . FC . =S . E . D . 2 .)

Prvr-> theorem

H1: p.seqno = next\_seqnum (x)

H2: repeats (x)

->

C1: repeats (x [seq: p])

Prvr-> qed

(. E . =S . U . FC . =S . E . D . 2 . QED)

:::::(. E . =S . U . FC . =S . E . D . 2 . QED E)

TypeList equalities

size (u) = size (unique\_msg (x))

```

(. E .=S . U . FC .=S . E . D . 2 . QED E P->)
(. E .=S . U . FC .=S . E . D . 2 . QED E P-> 1)
(. E .=S . U . FC .=S . E . D . 2 . QED E P-> 1)
repeats (x)
Proved
(. E .=S . U . FC .=S . E . D . 2 . QED E P-> 2)
(. E .=S . U . FC .=S . E . D . 2 . QED E P-> 2 P->)
(. E .=S . U . FC .=S . E . D . 2 . QED E P-> 2)
p.seqno ne next_seqnum (x) -> x[size (x)] = p
Proved
QED
Prvr-> $Proceeding
(. E .=S . U . FC .=S . E . D . 2 .)
repeats (x [seq: p])
Proved
Prvr-> $Proceeding
prop_trans_2 proved in theorem prover.
Exec-> prove prop_trans_3
Entering Prover with lemma prop_trans_3
all u : msg_seq,
all x, y : pkt_seq,
all p : packet,
x[size (x)] = p & proper_transmission (u, x, y, 1)
& null (pkt_seq) ne x
-> proper_transmission (u, x [seq: p], y, 1)
H1: x[size (x)] = p
H2: proper_transmission (u, x, y, 1)
H3: null (pkt_seq) ne x
->
C1: proper_transmission (u, x [seq: p], y, 1)
Backup point
(.)
Prvr-> expand proper_transmission
More than one to expand.
Which do you want to expand? all
Backup point
(. E .)
Prvr-> simplify theorem
Prvr->theorem
H1: x[size (x)] = p
H2: msg_lag (unique_msg (x), u, 1)
H3: repeats (x)

```

H4: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]

H5: size (u) - size (unique\_msg (y)) in [0..1]

H6: null (pkt\_seq) ne x

->

C1: msg\_lag (unique\_msg (x [seq: p]), u, 1)

C2: repeats (x [seq: p])

C3: size (unique\_msg (x [seq: p])) - size (unique\_msg (y))  
in [0..1]

Prvr-> use last\_unique

Backup point

(. E . U .)

Prvr-> hypothesis

H1: x#[size (x#2\$)] = p#2\$ & null (pkt\_seq) ne x#2\$

-> unique\_msg (x#[size (x#2\$)]) = unique\_msg (x#2\$)

H2: x[size (x)] = p

H3: msg\_lag (unique\_msg (x), u, 1)

H4: repeats (x)

H5: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]

H6: size (u) - size (unique\_msg (y)) in [0..1]

H7: null (pkt\_seq) ne x

Prvr-> forwardchain h1

::Forward chaining gives

unique\_msg (x [seq: p]) = unique\_msg (x)

Backup point

(. E . U . FC .)

Prvr-> theorem

H1: unique\_msg (x [seq: p]) = unique\_msg (x)

H2: x#[size (x#2\$)] = p#2\$ & null (pkt\_seq) ne x#2\$

-> unique\_msg (x#[size (x#2\$)]) = unique\_msg (x#2\$)

H3: x[size (x)] = p

H4: msg\_lag (unique\_msg (x), u, 1)

H5: repeats (x)

H6: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]

H7: size (u) - size (unique\_msg (y)) in [0..1]

H8: null (pkt\_seq) ne x

->

C1: msg\_lag (unique\_msg (x [seq: p]), u, 1)

C2: repeats (x [seq: p])

C3: size (unique\_msg (x [seq: p])) - size (unique\_msg (y))  
in [0..1]

Prvr-> equality substitute h1

H1 yields

unique\_msg (x [seq: p]) := unique\_msg (x)  
 Backup point  
 $(. E . U . FC . =S .)$   
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1:  $x[\text{size}(x)] = p$   
 H2: msg\_lag (unique\_msg (x), u, 1)  
 H3: repeats (x)  
 H4:  $x[2\$\text{size}(x)] = p[2\$ \& \text{null}(\text{pkt\_seq}) \neq x[2\$]$   
 $\rightarrow \text{unique\_msg}(x[2\$ \text{seq}: p[2\$]]) = \text{unique\_msg}(x[2\$])$   
 H5: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]  
 H6: size (u) - size (unique\_msg (y)) in [0..1]  
 H7: null (pkt\_seq) ne x  
 $\rightarrow$   
 C1: repeats (x [seq: p])  
 Prvr-> retain h1,h3,h7  
 Backup point  
 $(. E . U . FC . =S . D .)$   
 Prvr-> use last\_repeats  
 Backup point  
 $(. E . U . FC . =S . D . U .)$   
 Prvr-> qed  
 $(. E . U . FC . =S . D . U . \text{QED})$   
 $:::(. E . U . FC . =S . D . U . \text{QED BC})$   
 $(. E . U . FC . =S . D . U . \text{QED BC 1})$   
 $(. E . U . FC . =S . D . U . \text{QED BC 1})$   
 $x[\text{size}(x)] = p$   
 Proved  
 $(. E . U . FC . =S . D . U . \text{QED BC 2})$   
 $(. E . U . FC . =S . D . U . \text{QED BC 2})$   
 repeats (x)  
 Proved  
 $(. E . U . FC . =S . D . U . \text{QED BC 3})$   
 $(. E . U . FC . =S . D . U . \text{QED BC 3})$   
 null (pkt\_seq) ne x  
 Proved  
 $(. E . U . FC . =S . D . U . \text{QED BC})$   
 $x[\text{size}(x)] = p \& \text{repeats}(x) \& \text{null}(\text{pkt\_seq}) \neq x$   
 Proved  
 QED  
 Prvr-> \$Proceeding  
 prop\_trans\_3 proved in theorem prover.

```

Exec-> prove prop_trans_4
Entering Prover with lemma prop_trans_4
all u : msg_seq,
all x, y : pkt_seq,
all p : packet,
proper_transmission (u, x, y, 1) & p.seqno
ne next_seqnum (y)
-> proper_transmission (u, x, y [seq: p], 1)
H1: proper_transmission (u, x, y, 1)
H2: p.seqno ne next_seqnum (y)
->
C1: proper_transmission (u, x, y [seq: p], 1)
Backup point
(.)

Prvr-> expand proper_transmission
More than one to expand.
Which do you want to expand? all
Backup point
(. E .)

Prvr-> simplify theorem
Prvr->theorem
H1: msg_lag (unique_msg (x), u, 1)
H2: repeats (x)
H3: size (unique_msg (x)) - size (unique_msg (y)) in [0..1]
H4: size (u) - size (unique_msg (y)) in [0..1]
H5: p.seqno ne next_seqnum (y)
->
C1: size (unique_msg (x)) - size (unique_msg (y [seq: p])) in [0..1]
C2: size (u) - size (unique_msg (y [seq: p])) in [0..1]
Prvr-> expand unique_msg
More than one to expand.
Which do you want to expand? show-choices
1: unique_msg (x)
2: unique_msg (y)
3: unique_msg (y [seq: p])
Which do you want to expand? 3
Backup point
(. E . E .)

Prvr-> simplify theorem
Prvr->theorem
C1: true

```

Prvr-> \$Proceeding  
 prop\_trans\_4 proved in theorem prover.  
 [Your LOG file is job11.LOG;T;P777700]  
 [Recording initiated at Sat 9-May-81 12:17:42]  
 prove prop\_trans\_5  
 Entering Prover with lemma prop\_trans\_5  
 all u : msg\_seq,  
 all x, y : pkt\_seq,  
 all m : message,  
 proper\_transmission (u, x, y, 0)  
 $\rightarrow$  proper\_transmission (u [seq: m], x, y, 1)  
 H1: proper\_transmission (u, x, y, 0)  
 $\rightarrow$   
 C1: proper\_transmission (u [seq: m], x, y, 1)  
 Backup point  
 (. )  
 Prvr-> expand proper\_transmission  
 More than one to expand.  
 Which do you want to expand?all  
 Backup point  
 (. E .)  
 Prvr->simplify theorem  
 Prvr->theorem  
 H1: size (unique\_msg (y)) = size (unique\_msg (x))  
 H2: size (unique\_msg (y)) = size (u)  
 H3: msg\_lag (unique\_msg (x), u, 0)  
 H4: repeats (x)  
 $\rightarrow$   
 C1: msg\_lag (unique\_msg (x), u [seq: m], 1)  
 C2: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]  
 C3: (size (u) - size (unique\_msg (y))) + 1 in [0..1]  
 Prvr-> equality substitute h1,h2  
 H1 can be solved for:  
 T1: size (unique\_msg (y))  
 T2: size (unique\_msg (x))  
 Which term (by label) do you want to substitute for?  
 t2  
 size (unique\_msg (x)) := size (unique\_msg (y))  
 OK??  
 y  
 H2 can be solved for:  
 T1: size (unique\_msg (y))

T2: size (u)

Which term (by label) do you want to substitute for?

t2

size (u) := size (unique\_msg (y))

OK??

y

Backup point

(. E . =S .)

Prvr-> theorem

H1: msg\_lag (unique\_msg (x), u, 0)

H2: repeats (x)

->

C1: msg\_lag (unique\_msg (x), u [seq: m], 1)

Prvr-> retain h1

Backup point

(. E . =S . D .)

Prvr-> use eq\_iss

Backup point

(. E . =S . D . U .)

Prvr-> hypothesis

H1: u#8\$ = v#8\$ -> initial\_subseq (u#8\$, v#8\$)

H2: msg\_lag (unique\_msg (x), u, 0)

Prvr-> forwardchain h1

::Forward chaining gives

initial\_subseq (v#8\$, v#8\$)

Backup point

(. E . =S . D . U . FC .)

Prvr-> back up 3

Restored

Backup point

(. E . =S . D .)

Prvr-> use msg\_lag\_eq

Backup point

(. E . =S . D . U .)

Prvr-> theorem

H1: u#10\$ = v#10\$ iff msg\_lag (u#10\$, v#10\$, 0)

H2: msg\_lag (unique\_msg (x), u, 0)

->

C1: msg\_lag (unique\_msg (x), u [seq: m], 1)

Prvr-> forwardchain h1

Which way? (left or right)

left

::Forward chaining gives

unique\_msg (x) = u

Backup point

(. E . =S . D . U . FC .)

Prvr-> equality substitute h1

H1 can be solved for:

T1: u#10\$ = v#10\$

T2: msg\_lag (u#10\$, v#10\$, 0)

Which term (by label) do you want to substitute for?

t1

u#10\$ = v#10\$ := msg\_lag (u#10\$, v#10\$, 0)

OK??

y

Backup point

(. E . =S . D . U . FC . =S .)

Prvr-> theorem

H1: unique\_msg (x) = u

H2: msg\_lag (unique\_msg (x), u, 0)

->

C1: msg\_lag (unique\_msg (x), u [seq: m], 1)

Prvr-> equality substitute h1

H1 can be solved for:

T1: unique\_msg (x)

T2: u

Which term (by label) do you want to substitute for?

t1

unique\_msg (x) := u

OK??

y

Backup point

(. E . =S . D . U . FC . =S . =S .)

Prvr-> expand msg\_lag

More than one to expand.

Which do you want to expand? 2

Backup point

(. E . =S . D . U . FC . =S . =S . E .)

Prvr-> simplify theorem

Prvr->theorem

H1: msg\_lag (u, u, 0)

->

C1: initial\_subseq (u, u [seq: m])

Prvr-> use eq\_iss

Backup point  
 (. E . =S . D . U . FC . =S . =S . E . U .)  
 Prvr-> use iss\_app  
 Backup point  
 (. E . =S . D . U . FC . =S . =S . E . U . U .)  
 Prvr->qed  
 (. E . =S . D . U . FC . =S . =S . E . U . U . QED)  
 :::(. E . =S . D . U . FC . =S . =S . E . U . U . QED BC)  
 :::(. E . =S . D . U . FC . =S . =S . E . U . U . QED BC BC)  
 (. E . =S . D . U . FC . =S . =S . E . U . U . QED BC BC)  
 u = u  
 Proved  
 (. E . =S . D . U . FC . =S . =S . E . U . U . QED BC)  
 initial\_subseq (u, u)  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 prop\_trans\_5 proved in theorem prover.  
 Exec-> prove prop\_trans\_6  
 Entering Prover with lemma prop\_trans\_6  
 all u : msg\_seq,  
 all x, y : pkt\_seq,  
 proper\_transmission (u, x, y, 0) -> proper\_transmission (u, x, y, 1)  
 H1: proper\_transmission (u, x, y, 0)  
 ->  
 C1: proper\_transmission (u, x, y, 1)  
 Backup point  
 (.)  
 Prvr-> expand proper\_transmission  
 More than one to expand.  
 Which do you want to expand?all  
 Backup point  
 (. E .)  
 Prvr->simplify theorem  
 Prvr->theorem  
 H1: size (unique\_msg (y)) = size (unique\_msg (x))  
 H2: size (unique\_msg (y)) = size (u)  
 H3: msg\_lag (unique\_msg (x), u, 0)  
 H4: repeats (x)  
 ->  
 C1: msg\_lag (unique\_msg (x), u, 1)  
 C2: size (unique\_msg (x)) - size (unique\_msg (y)) in [0..1]

C3: size (u) - size (unique\_msg (y)) in [0..1]  
Prvr-> equality substitute h1,h2  
H1 can be solved for:  
T1: size (unique\_msg (y))  
T2: size (unique\_msg (x))  
Which term (by label) do you want to substitute for?  
t2  
size (unique\_msg (x)) := size (unique\_msg (y))  
OK??  
y  
H2 can be solved for:  
T1: size (unique\_msg (y))  
T2: size (u)  
Which term (by label) do you want to substitute for?  
t2  
size (u) := size (unique\_msg (y))  
OK??  
y  
Backup point  
(. E . =S .)  
Prvr-> theorem  
H1: msg\_lag (unique\_msg (x), u, 0)  
H2: repeats (x)  
->  
C1: msg\_lag (unique\_msg (x), u, 1)  
Prvr-> retain h1  
Backup point  
(. E . =S . D .)  
Prvr-> expand msg\_lag  
More than one to expand.  
Which do you want to expand? all  
Backup point  
(. E . =S . D . E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: size (unique\_msg (x)) = size (u)  
H2: initial\_subseq (unique\_msg (x), u)  
->  
C1: size (u) - size (unique\_msg (x)) in [0..1]  
Prvr-> equality substitute h1  
H1 can be solved for:  
T1: size (unique\_msg (x))

T2: size (u)

Which term (by label) do you want to substitute for?

t1

size (unique\_msg (x)) := size (u)

OK??

y

Backup point

(. E . =S . D . E . =S .)

Prvr-> \$Proceeding

prop\_trans\_6 proved in theorem prover.

Exec-> prove prop\_trans\_7

Entering Prover with lemma prop\_trans\_7

all u : msg\_seq,

all x, y : pkt\_seq,

all p : packet,

p.seqno = next\_seqnum (y) & unique\_msg (x) = u

& size (unique\_msg (x)) = size (unique\_msg (y)) + 1

& proper\_transmission (u, x, y, 1)

-> proper\_transmission (u, x, y [seq: p], 0)

H1: p.seqno = next\_seqnum (y)

H2: unique\_msg (x) = u

H3: size (unique\_msg (x)) = size (unique\_msg (y)) + 1

H4: proper\_transmission (u, x, y, 1)

->

C1: proper\_transmission (u, x, y [seq: p], 0)

TypeList equalities

size (unique\_msg (y)) + 1 = size (unique\_msg (x))

Backup point

(.)

Prvr-> expand proper\_transmission

More than one to expand.

Which do you want to expand? all

Backup point

(. E .)

Prvr-> simplify theorem

Prvr-> theorem

H1: p.seqno = next\_seqnum (y)

H2: unique\_msg (x) = u

H3: size (unique\_msg (x)) = size (unique\_msg (y)) + 1

H4: size (unique\_msg (y)) + 1 = size (unique\_msg (x))

H5: msg\_lag (unique\_msg (x), u, 1)

H6: repeats (x)

H7:  $\text{size}(\text{unique\_msg}(x)) - \text{size}(\text{unique\_msg}(y))$  in  $[0..1]$

H8:  $\text{size}(u) - \text{size}(\text{unique\_msg}(y))$  in  $[0..1]$

->

C1:  $\text{size}(\text{unique\_msg}(y[\text{seq}: p])) = \text{size}(\text{unique\_msg}(x))$

C2:  $\text{size}(\text{unique\_msg}(y[\text{seq}: p])) = \text{size}(u)$

C3:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 0)$

Prvr-> expand unique\_msg

More than one to expand.

Which do you want to expand? show-choices

1: unique\_msg(x)

2: unique\_msg(y)

3: unique\_msg(y [seq: p])

Which do you want to expand? 3

Backup point

(. E . E .)

Prvr->simplify theorem

Prvr->theorem

H1:  $p.\text{seqno} = \text{next\_seqnum}(y)$

H2:  $\text{unique\_msg}(x) = u$

H3:  $\text{size}(\text{unique\_msg}(x)) = \text{size}(\text{unique\_msg}(y)) + 1$

H4:  $\text{size}(\text{unique\_msg}(y)) + 1 = \text{size}(\text{unique\_msg}(x))$

H5:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 1)$

H6: repeats(x)

H7:  $\text{size}(\text{unique\_msg}(x)) - \text{size}(\text{unique\_msg}(y))$  in  $[0..1]$

H8:  $\text{size}(u) - \text{size}(\text{unique\_msg}(y))$  in  $[0..1]$

->

C1:  $\text{size}(\text{unique\_msg}(y)) + 1 = \text{size}(u)$

C2:  $\text{msg\_lag}(\text{unique\_msg}(x), u, 0)$

Prvr-> equality substitute h2

H2 can be solved for:

T1: unique\_msg(x)

T2: u

Which term (by label) do you want to substitute for?

t1

unique\_msg(x) := u

OK??

y

Backup point

(. E . E . =S .)

Prvr-> theorem

H1:  $p.\text{seqno} = \text{next\_seqnum}(y)$

H2:  $\text{size}(\text{unique\_msg}(y)) + 1 = \text{size}(u)$

H3: size (u) = size (unique\_msg (y)) + 1

H4: msg\_lag (u, u, 1)

H5: repeats (x)

H6: size (u) - size (unique\_msg (y)) in [0..1]

->

C1: size (unique\_msg (y)) + 1 = size (u)

C2: msg\_lag (u, u, 0)

Prvr-> retain

What hypotheses would you like to retain? h4

Backup point

(. E . E . =S . D .)

Prvr-> simplify theorem

Prvr->theorem

H1: msg\_lag (u, u, 1)

->

C1: size (unique\_msg (y)) + 1 = size (u)

C2: msg\_lag (u, u, 0)

Prvr-> back up2

\*\*\*\* Illegal command - UP2

Back UP or establish a back up POINT to return to? up

How many levels would you like to back up? 2

Restored

Backup point

(. E . E . =S .)

Prvr-> theorem

H1: p.seqno = next\_seqnum (y)

H2: size (unique\_msg (y)) + 1 = size (u)

H3: size (u) = size (unique\_msg (y)) + 1

H4: msg\_lag (u, u, 1)

H5: repeats (x)

H6: size (u) - size (unique\_msg (y)) in [0..1]

->

C1: size (unique\_msg (y)) + 1 = size (u)

C2: msg\_lag (u, u, 0)

Prvr-> retain h2

TypeList equalities

size (u) = size (unique\_msg (y)) + 1

Backup point

(. E . E . =S . D .)

Prvr-> simplify theorem

Prvr->theorem

H1: size (unique\_msg (y)) + 1 = size (u)

H2: size (u) = size (unique\_msg (y)) + 1  
 ->  
 C1: msg\_lag (u, u, 0)  
 Prvr-> use msg\_lag\_eq  
 Backup point  
 (. E . =S . D . U .)  
 Prvr-> qed  
 (. E . =S . D . U . QED)  
 :::  
 size (unique\_msg (y)) := size (u) - 1  
 (. E . =S . D . U . QED =S)  
 (. E . =S . D . U . QED =S E)  
 Ran out of tricks  
 Prvr-> theorem  
 H1: u#4\$ = v#4\$ iff msg\_lag (u#4\$, v#4\$, 0)  
 ->  
 C1: initial\_subseq (u, u)  
 Prvr-> back up 4  
 Restored  
 Backup point  
 (. E . =S . D . U .)  
 Prvr-> theorem  
 H1: u#4\$ = v#4\$ iff msg\_lag (u#4\$, v#4\$, 0)  
 H2: size (unique\_msg (y)) + 1 = size (u)  
 H3: size (u) = size (unique\_msg (y)) + 1  
 ->  
 C1: msg\_lag (u, u, 0)  
 Prvr-> use eq\_iss  
 Backup point  
 (. E . =S . D . U . U .)  
 Prvr-> hypothesis  
 H1: u#6\$ = v#6\$ -> initial\_subseq (u#6\$, v#6\$)  
 H2: u#4\$ = v#4\$ iff msg\_lag (u#4\$, v#4\$, 0)  
 H3: size (unique\_msg (y)) + 1 = size (u)  
 H4: size (u) = size (unique\_msg (y)) + 1  
 Prvr-> retain h1  
 Backup point  
 (. E . =S . D . U . U . D .)  
 Prvr-> expand msg\_lag  
 Backup point  
 (. E . =S . D . U . U . D . E .)  
 Prvr-> qed

(. E . =S . D . U . U . D . E . QED)  
(. E . =S . D . U . U . D . E . QED BC)  
(. E . =S . D . U . U . D . E . QED BC)  
u = u  
Proved  
QED  
Prvr-> \$Proceeding  
prop\_trans\_7 proved in theorem prover.  
Exec-> show status scope \$  
SCOPE LEMMAS  
Waiting to be proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL,  
APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB,  
ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE,  
LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
NCHANGES\_UNIQUE, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4,  
PROP\_REC\_5, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG, SUB\_NCHANGES  
Proved: PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4,  
PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7  
Exec-> prove prop\_rec\_1  
Entering Prover with lemma prop\_rec\_1  
all u : msg\_seq,  
all x, y : pkt\_seq,  
all p : packet,  
all m : message,  
p.mssg = m & p.seqno = next\_seqnum (x)  
& proper\_reception (u, x, y, 0)  
-> proper\_reception (u [seq: m], x [seq: p], y, 1)  
H1: p.mssg = m  
H2: p.seqno = next\_seqnum (x)  
H3: proper\_reception (u, x, y, 0)  
->  
C1: proper\_reception (u [seq: m], x [seq: p], y, 1)  
Backup point  
(.)  
Prvr-> expand proper\_reception  
More than one to expand.  
Which do you want to expand?all  
Backup point  
(. E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: p.mssg = m

H2:  $p.seqno = \text{next\_seqnum}(x)$   
 H3:  $\text{size}(\text{unique\_msg}(y)) = \text{size}(u)$   
 H4:  $\text{msg\_lag}(u, \text{unique\_msg}(x), 0)$   
 H5:  $y \text{ sub } x$   
 $\rightarrow$   
 C1:  $\text{msg\_lag}(u \text{ [seq: } m], \text{unique\_msg}(x \text{ [seq: } p]), 1)$   
 C2:  $(\text{size}(u) - \text{size}(\text{unique\_msg}(y))) + 1 \text{ in } [0..1]$   
 Prvr-> equality substitute h3  
 H3 can be solved for:  
 T1:  $\text{size}(\text{unique\_msg}(y))$   
 T2:  $\text{size}(u)$   
 Which term (by label) do you want to substitute for?  
 t1  
 $\text{size}(\text{unique\_msg}(y)) := \text{size}(u)$   
 OK??  
 y  
 Backup point  
 $(. E . =S .)$   
 Prvr-> theorem  
 H1:  $p.mssg = m$   
 H2:  $p.seqno = \text{next\_seqnum}(x)$   
 H3:  $\text{msg\_lag}(u, \text{unique\_msg}(x), 0)$   
 H4:  $y \text{ sub } x$   
 $\rightarrow$   
 C1:  $\text{msg\_lag}(u \text{ [seq: } m], \text{unique\_msg}(x \text{ [seq: } p]), 1)$   
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? 2  
 Backup point  
 $(. E . =S . E .)$   
 Prvr-> use msg\_lag\_eq  
 Backup point  
 $(. E . =S . E . U .)$   
 Prvr-> theorem  
 H1:  $u\$ = v\$ \text{ iff } \text{msg\_lag}(u\$, v\$, 0)$   
 H2:  $p.mssg = m$   
 H3:  $p.seqno = \text{next\_seqnum}(x)$   
 H4:  $\text{msg\_lag}(u, \text{unique\_msg}(x), 0)$   
 H5:  $y \text{ sub } x$   
 $\rightarrow$   
 C1:  $\text{msg\_lag}(u \text{ [seq: } m],$   
 if  $p.seqno = \text{next\_seqnum}(x)$

```

then unique_msg (x) [seq: p.mssg]
else unique_msg (x)
fi, 1)
Prvr-> forwardchain h1
Which way? (left or right)
left
:::Forward chaining gives
u = unique_msg (x)
Backup point
(. E . =S . E . U . FC .)
Prvr-> simplify theorem
Prvr->theorem
H1: p.mssg = m
H2: p.seqno = next_seqnum (x)
H3: unique_msg (x) = u
H4: u#2$ = v#2$ iff msg_lag (u#2$, v#2$, 0)
H5: msg_lag (u, unique_msg (x), 0)
H6: y sub x
->
C1: msg_lag (u [seq: m], unique_msg (x) [seq: p.mssg], 1)
Prvr-> retain h1,h3
Backup point
(. E . =S . E . U . FC . D .)
Prvr-> hypothesis
H1: p.mssg = m
H2: unique_msg (x) = u
Prvr-> equality substitute h1,h2
H1 can be solved for:
T1: p.mssg
T2: m
Which term (by label) do you want to substitute for?
t1
p.mssg := m
OK??
y
H2 can be solved for:
T1: unique_msg (x)
T2: u
Which term (by label) do you want to substitute for?
t1
unique_msg (x) := u
OK??

```

y  
Backup point  
(. E . =S . E . U . FC . D . =S .)  
Prvr-> theorem  
H1: true  
->  
C1: msg\_lag (u [seq: m], u [seq: m], 1)  
Prvr-> expand msg\_lag  
Backup point  
(. E . =S . E . U . FC . D . =S . E .)  
Prvr->use eq\_iss  
Backup point  
(. E . =S . E . U . FC . D . =S . E . U .)  
Prvr-> qed  
(. E . =S . E . U . FC . D . =S . E . U . QED)  
(. E . =S . E . U . FC . D . =S . E . U . QED BC)  
(. E . =S . E . U . FC . D . =S . E . U . QED BC)  
u [seq: m] = u [seq: m]  
Proved  
QED  
Prvr-> \$Proceeding  
prop\_rec\_1 proved in theorem prover.  
Exec-> prove prop\_rec\_2  
Entering Prover with lemma prop\_rec\_2  
all u : msg\_seq,  
all x, y : pkt\_seq,  
all p : packet,  
proper\_reception (u, x, y, 0)  
-> proper\_reception (u, x [seq: p], y, 1)  
H1: proper\_reception (u, x, y, 0)  
->  
C1: proper\_reception (u, x [seq: p], y, 1)  
Backup point  
(.)  
Prvr-> expand proper\_reception  
More than one to expand.  
Which do you want to expand?all  
Backup point  
(. E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: size (unique\_msg (y)) = size (u)

H2: msg\_lag (u, unique\_msg (x), 0)

H3: y sub x

->

C1: msg\_lag (u, unique\_msg (x [seq: p]), 1)

C2: size (u) - size (unique\_msg (y)) in [0..1]

Prvr-> equality substitute h1

H1 can be solved for:

T1: size (unique\_msg (y))

T2: size (u)

Which term (by label) do you want to substitute for?

t1

size (unique\_msg (y)) := size (u)

OK??

y

Backup point

(. E . =S .)

Prvr-> theorem

H1: msg\_lag (u, unique\_msg (x), 0)

H2: y sub x

->

C1: msg\_lag (u, unique\_msg (x [seq: p]), 1)

Prvr-> retain h1

Backup point

(. E . =S . D .)

Prvr-> use msg\_lag\_eq

Backup point

(. E . =S . D . U .)

Prvr-> hypothesis

H1: u#2\$ = v#2\$ iff msg\_lag (u#2\$, v#2\$, 0)

H2: msg\_lag (u, unique\_msg (x), 0)

Prvr-> forwardchain h1

Which way? (left or right)

left

::Forward chaining gives

u = unique\_msg (x)

Backup point

(. E . =S . D . U . FC .)

Prvr-> hypothesis

H1: u = unique\_msg (x)

H2: u#2\$ = v#2\$ iff msg\_lag (u#2\$, v#2\$, 0)

H3: msg\_lag (u, unique\_msg (x), 0)

Prvr-> retain h1

Backup point  
 $(. E . =S . D . U . FC . D .)$   
 Prvr-> equality substitute h1  
 H1 yields  
 $u := \text{unique\_msg}(x)$   
 Backup point  
 $(. E . =S . D . U . FC . D . =S .)$   
 Prvr-> theorem  
 H1: true  
 $\rightarrow$   
 C1:  $\text{msg\_lag}(\text{unique\_msg}(x), \text{unique\_msg}(x \text{ [seq: } p]), 1)$   
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1:  $\text{unique\_msg}(x)$   
 2:  $\text{unique\_msg}(x \text{ [seq: } p])$   
 Which do you want to expand? 2  
 Backup point  
 $(. E . =S . D . U . FC . D . =S . E .)$   
 Prvr-> theorem  
 H1: true  
 $\rightarrow$   
 C1:  $\text{msg\_lag}(\text{unique\_msg}(x),$   
 if  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 then  $\text{unique\_msg}(x) \text{ [seq: } p.\text{mssg}]$   
 else  $\text{unique\_msg}(x)$   
 fi, 1)  
 Prvr-> cases  
 Case:  
 \*  $p.\text{seqno} = \text{next\_seqnum}(x);$   
 Case:  
 \* \$done  
 Attempting CASE1  
 $p.\text{seqno} = \text{next\_seqnum}(x)$   
 Backup point  
 $(. E . =S . D . U . FC . D . =S . E . \text{CASE1} .)$   
 Prvr-> theorem  
 H1:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 $\rightarrow$   
 C1:  $\text{msg\_lag}(\text{unique\_msg}(x),$   
 if  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 then  $\text{unique\_msg}(x) \text{ [seq: } p.\text{mssg}]$

```

else unique_msg (x)
fi, 1)
Prvr-> simplify theorem
Prvr->theorem
H1: p.seqno = next_seqnum (x)
->
C1: msg_lag (unique_msg (x), unique_msg (x) [seq: p.mssg], 1)
Prvr-> use eq_iss
Backup point
(. E . =S . D . U . FC . D . =S . E . CASE1 . U .)
Prvr->use iss_app
Backup point
(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U .)
Prvr-> qed
(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED)
:::(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED E)
:::(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED E BC)
:::(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED E BC BC)
(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED E BC BC)
unique_msg (x) = unique_msg (x)
Proved
(. E . =S . D . U . FC . D . =S . E . CASE1 . U . U . QED E BC)
initial_subseq (unique_msg (x), unique_msg (x))
Proved
QED
Prvr-> $Proceeding
(. E . =S . D . U . FC . D . =S . E . CASE1 .)
p.seqno = next_seqnum (x)
-> msg_lag (unique_msg (x),
if p.seqno = next_seqnum (x)
then unique_msg (x) [seq: p.mssg]
else unique_msg (x)
fi, 1)
Proved
Attempting CASE2
p.seqno ne next_seqnum (x)
Backup point
(. E . =S . D . U . FC . D . =S . E . CASE2 .)
Prvr-> theorem
H1: p.seqno ne next_seqnum (x)
->
C1: msg_lag (unique_msg (x),

```

```

if p.seqno = next_seqnum (x)
then unique_msg (x) [seq: p.mssg]
else unique_msg (x)
fi, 1)
Prvr-> simplify theorem
Prvr->theorem
H1: p.seqno ne next_seqnum (x)
->
C1: msg_lag (unique_msg (x), unique_msg (x), 1)
Prvr-> use eq_iss
Backup point
(. E . =S . D . U . FC . D . =S . E . CASE2 . U .)
Prvr-> qed
(. E . =S . D . U . FC . D . =S . E . CASE2 . U . QED)
:::(. E . =S . D . U . FC . D . =S . E . CASE2 . U . QED E)
:::(. E . =S . D . U . FC . D . =S . E . CASE2 . U . QED E BC)
(. E . =S . D . U . FC . D . =S . E . CASE2 . U . QED E BC)
unique_msg (x) = unique_msg (x)
Proved
QED
Prvr-> $Proceeding
(. E . =S . D . U . FC . D . =S . E . CASE2 .)
p.seqno ne next_seqnum (x)
-> msg_lag (unique_msg (x),
if p.seqno = next_seqnum (x)
then unique_msg (x) [seq: p.mssg]
else unique_msg (x)
fi, 1)
Proved
Done with cases
prop_rec_2 proved in theorem prover.
Exec->$
**** Illegal command - <ESCAPE>
Exec-> prove prop_rec_3
Entering Prover with lemma prop_rec_3
all u : msg_seq,
all x, y : pkt_seq,
proper_reception (u, x, y, 0) -> proper_reception (u, x, y, 1)
H1: proper_reception (u, x, y, 0)
->
C1: proper_reception (u, x, y, 1)
Backup point

```

(.)  
Prvr-> expand proper\_reception  
More than one to expand.  
Which do you want to expand? all  
Backup point  
(. E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: size (unique\_msg (y)) = size (u)  
H2: msg\_lag (u, unique\_msg (x), 0)  
H3: y sub x  
->  
C1: msg\_lag (u, unique\_msg (x), 1)  
C2: size (u) - size (unique\_msg (y)) in [0..1]  
Prvr-> equality substitute h1  
H1 can be solved for:  
T1: size (unique\_msg (y))  
T2: size (u)  
Which term (by label) do you want to substitute for?  
t1  
size (unique\_msg (y)) := size (u)  
OK??  
y  
Backup point  
(. E . =S .)  
Prvr-> theorem  
H1: msg\_lag (u, unique\_msg (x), 0)  
H2: y sub x  
->  
C1: msg\_lag (u, unique\_msg (x), 1)  
Prvr-> expand msg\_lag  
More than one to expand.  
Which do you want to expand? all  
Backup point  
(. E . =S . E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: size (u) = size (unique\_msg (x))  
H2: initial\_subseq (u, unique\_msg (x))  
H3: y sub x  
->  
C1: size (unique\_msg (x)) - size (u) in [0..1]

Prvr-> equality substitute h1  
 H1 can be solved for:  
 T1: size (u)  
 T2: size (unique\_msg (x))  
 Which term (by label) do you want to substitute for?  
 t1  
 size (u) := size (unique\_msg (x))  
 OK??  
 y  
 Backup point  
 (. E . =S . E . =S .)  
 Prvr-> \$Proceeding  
 prop\_rec\_3 proved in theorem prover.  
 Exec->\$  
 \*\*\*\* Illegal command - <ESCAPE>  
 Exec-> prove prop\_rec\_4  
 Entering Prover with lemma prop\_rec\_4  
 all u : msg\_seq,  
 all x, y : pkt\_seq,  
 all p : packet,  
 all m : message,  
 p.mssg = m & p.seqno = next\_seqnum (x)  
 & p.seqno = next\_seqnum (y) & proper\_reception (u, x, y, 0)  
 -> proper\_reception (u [seq: m], x [seq: p], y [seq: p], 0)  
 H1: p.mssg = m  
 H2: p.seqno = next\_seqnum (x)  
 H3: p.seqno = next\_seqnum (y)  
 H4: proper\_reception (u, x, y, 0)  
 ->  
 C1: proper\_reception (u [seq: m], x [seq: p], y [seq: p], 0)  
 Backup point  
 (. )  
 Prvr-> expand proper\_reception  
 More than one to expand.  
 Which do you want to expand?all  
 Backup point  
 (. E .)  
 Prvr->simplify theorem  
 Prvr->theorem  
 H1: p.mssg = m  
 H2: p.seqno = next\_seqnum (x)  
 H3: p.seqno = next\_seqnum (y)

H4: size (unique\_msg (y)) = size (u)  
 H5: msg\_lag (u, unique\_msg (x), 0)  
 H6: y sub x  
 ->  
 C1: size (unique\_msg (y [seq: p])) = size (u) + 1  
 C2: msg\_lag (u [seq: m], unique\_msg (x [seq: p]), 0)  
 C3: y [seq: p] sub x [seq: p]  
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: unique\_msg (y)  
 2: unique\_msg (x)  
 3: unique\_msg (y [seq: p])  
 4: unique\_msg (x [seq: p])  
 Which do you want to expand? 3,4  
 Backup point  
 (. E . E .)  
 Prvr-> simplify theorem  
 Prvr-> theorem  
 H1: p.mssg = m  
 H2: p.seqno = next\_seqnum (x)  
 H3: p.seqno = next\_seqnum (y)  
 H4: size (unique\_msg (y)) = size (u)  
 H5: msg\_lag (u, unique\_msg (x), 0)  
 H6: y sub x  
 ->  
 C1: msg\_lag (u [seq: m], unique\_msg (x) [seq: p.mssg], 0)  
 C2: y [seq: p] sub x [seq: p]  
 Prvr-> use eq\_iss  
 Backup point  
 (. E . E . U .)  
 Prvr-> hypothesis  
 H1: u#2\$ = v#2\$ -> initial\_subseq (u#2\$, v#2\$)  
 H2: p.mssg = m  
 H3: p.seqno = next\_seqnum (x)  
 H4: p.seqno = next\_seqnum (y)  
 H5: size (unique\_msg (y)) = size (u)  
 H6: msg\_lag (u, unique\_msg (x), 0)  
 H7: y sub x  
 Prvr-> forwardchain h1  
 ::Forward chaining gives  
 initial\_subseq (p.seqno, next\_seqnum (x))

Backup point  
 (. E . E . U . FC .)  
 Prvr-> back up 2  
 Restored  
 Backup point  
 (. E . E . U .)  
 Prvr-> back up 2  
 Restored  
 Backup point  
 (. E . E .)  
 Prvr-> use msg\_lag\_eq  
 Backup point  
 (. E . E . U .)  
 Prvr-> hypothesis  
 H1:  $u \#4\$ = v \#4\$$  iff  $\text{msg\_lag}(u \#4\$, v \#4\$, 0)$   
 H2:  $p.\text{mssg} = m$   
 H3:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H4:  $p.\text{seqno} = \text{next\_seqnum}(y)$   
 H5:  $\text{size}(\text{unique\_msg}(y)) = \text{size}(u)$   
 H6:  $\text{msg\_lag}(u, \text{unique\_msg}(x), 0)$   
 H7:  $y \text{ sub } x$   
 Prvr->forwardchain h1  
 Which way? (left or right)  
 left  
 ::::::Forward chaining gives  
 $u = \text{unique\_msg}(x)$   
 Backup point  
 (. E . E . U . FC .)  
 Prvr-> hypothesis  
 H1:  $u = \text{unique\_msg}(x)$   
 H2:  $u \#4\$ = v \#4\$$  iff  $\text{msg\_lag}(u \#4\$, v \#4\$, 0)$   
 H3:  $p.\text{mssg} = m$   
 H4:  $p.\text{seqno} = \text{next\_seqnum}(x)$   
 H5:  $p.\text{seqno} = \text{next\_seqnum}(y)$   
 H6:  $\text{size}(\text{unique\_msg}(y)) = \text{size}(u)$   
 H7:  $\text{msg\_lag}(u, \text{unique\_msg}(x), 0)$   
 H8:  $y \text{ sub } x$   
 Prvr-> equality substitute h1  
 H1 can be solved for:  
 T1:  $u$   
 T2:  $\text{unique\_msg}(x)$   
 Which term (by label) do you want to substitute for?

```

t2
unique_msg (x) := u
OK??
y
Typelist equalities
size (u) = size (unique_msg (y))
Backup point
(. E . U . FC . =S .)
Prvr->theorem
H1: size (u) = size (unique_msg (y))
H2: p.mssg = m
H3: p.seqno = next_seqnum (x)
H4: p.seqno = next_seqnum (y)
H5: size (unique_msg (y)) = size (u)
H6: u#4$ = v#4$ iff msg_lag (u#4$, v#4$, 0)
H7: msg_lag (u, u, 0)
H8: y sub x
->
C1: size (if p.seqno = next_seqnum (y)
then unique_msg (y) [seq: p.mssg]
else unique_msg (y)
fi)
= size (u) + 1
C2: msg_lag (u [seq: m],
if p.seqno = next_seqnum (x)
then u [seq: p.mssg]
else u
fi, 0)
C3: y [seq: p] sub x [seq: p]
Prvr-> simplify theorem
Prvr->theorem
H1: p.mssg = m
H2: p.seqno = next_seqnum (x)
H3: p.seqno = next_seqnum (y)
H4: size (unique_msg (y)) = size (u)
H5: size (u) = size (unique_msg (y))
H6: u#4$ = v#4$ iff msg_lag (u#4$, v#4$, 0)
H7: msg_lag (u, u, 0)
H8: y sub x
->
C1: msg_lag (u [seq: m], u [seq: p.mssg], 0)
C2: y [seq: p] sub x [seq: p]

```

Prvr-> equality substitute h1

H1 can be solved for:

T1: p.mssg

T2: m

Which term (by label) do you want to substitute for?

t1

p.mssg := m

OK??

y

Backup point

(. E . E . U . FC . =S . =S .)

Prvr->hypothesis

H1: p.seqno = next\_seqnum (x)

H2: p.seqno = next\_seqnum (y)

H3: size (unique\_msg (y)) = size (u)

H4: size (u) = size (unique\_msg (y))

H5: u#4\$ = v#4\$ iff msg\_lag (u#4\$, v#4\$, 0)

H6: msg\_lag (u, u, 0)

H7: y sub x

Prvr-> retain h6,h7

Backup point

(. E . E . U . FC . =S . =S . D .)

Prvr-> \$Proceeding

Backup point

(. E . E . U . FC . =S . =S . D . 1 .)

Prvr-> theorem

H1: msg\_lag (u, u, 0)

H2: y sub x

->

C1: msg\_lag (u [seq: m], u [seq: m], 0)

Prvr-> use eq\_iss\_app

TypeList equalities

size (u) = size (unique\_msg (y))

Backup point

(. E . E . U . FC . =S . =S . D . 1 . U .)

Prvr->expand msg\_lag

More than one to expand.

Which do you want to expand? all

Backup point

(. E . E . U . FC . =S . =S . D . 1 . U . E .)

Prvr->qed

(. E . E . U . FC . =S . =S . D . 1 . U . E . QED)

:::(. E . E . U . FC . =S . =S . D . 1 . U . E . QED BC)  
(. E . E . U . FC . =S . =S . D . 1 . U . E . QED BC)  
u = u  
Proved  
QED  
Prvr-> \$Proceeding  
(. E . E . U . FC . =S . =S . D . 1 .)  
msg\_lag (u [seq: m], u [seq: m], 0)  
Proved  
Prvr-> \$Proceeding  
Backup point  
(. E . E . U . FC . =S . =S . D . 2 .)  
Prvr-> theorem  
H1: msg\_lag (u, u, 0)  
H2: y sub x  
->  
C1: y [seq: p] sub x [seq: p]  
Prvr-> retain h2  
Backup point  
(. E . E . U . FC . =S . =S . D . 2 . D .)  
Prvr-> simplify theorem  
Prvr->theorem  
H1: y sub x  
->  
C1: y [seq: p] sub x [seq: p]  
Prvr-> use sub\_app  
Typelist equalities  
size (u) = size (unique\_msg (y))  
Backup point  
(. E . E . U . FC . =S . =S . D . 2 . D . U .)  
Prvr->qed  
(. E . E . U . FC . =S . =S . D . 2 . D . U . QED)  
:::(. E . E . U . FC . =S . =S . D . 2 . D . U . QED BC)  
(. E . E . U . FC . =S . =S . D . 2 . D . U . QED BC)  
y sub x  
Proved  
QED  
Prvr-> \$Proceeding  
(. E . E . U . FC . =S . =S . D . 2 .)  
y [seq: p] sub x [seq: p]  
Proved  
Prvr-> \$Proceeding

prop\_rec\_4 proved in theorem prover.  
 Exec-> prove prop\_rec\_5  
 Entering Prover with lemma prop\_rec\_5  
 all u : msg\_seq,  
 all x, y : pkt\_seq,  
 all p : packet,  
 proper\_reception (u, x, y, 0) & p.seqno ne next\_seqnum (x)  
 & p.seqno ne next\_seqnum (y)  
 -> proper\_reception (u, x [seq: p], y [seq: p], 0)  
 H1: proper\_reception (u, x, y, 0)  
 H2: p.seqno ne next\_seqnum (x)  
 H3: p.seqno ne next\_seqnum (y)  
 ->  
 C1: proper\_reception (u, x [seq: p], y [seq: p], 0)  
 Backup point  
 (. )  
 Prvr-> expand proper\_reception  
 More than one to expand.  
 Which do you want to expand?all  
 Backup point  
 (. E .)  
 Prvr->simplify theorem  
 Prvr->theorem  
 H1: size (unique\_msg (y)) = size (u)  
 H2: msg\_lag (u, unique\_msg (x), 0)  
 H3: p.seqno ne next\_seqnum (x)  
 H4: p.seqno ne next\_seqnum (y)  
 H5: y sub x  
 ->  
 C1: size (unique\_msg (y [seq: p])) = size (u)  
 C2: msg\_lag (u, unique\_msg (x [seq: p]), 0)  
 C3: y [seq: p] sub x [seq: p]  
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand?show-choices  
 1: unique\_msg (y)  
 2: unique\_msg (x)  
 3: unique\_msg (y [seq: p])  
 4: unique\_msg (x [seq: p])  
 Which do you want to expand? 3,4  
 Backup point  
 (. E . E .)

Prvr->simplify theorem

Prvr->theorem

H1: size (unique\_msg (y)) = size (u)

H2: msg\_lag (u, unique\_msg (x), 0)

H3: p.seqno ne next\_seqnum (x)

H4: p.seqno ne next\_seqnum (y)

H5: y sub x

->

C1: y [seq: p] sub x [seq: p]

Prvr-> retain h5

Backup point

(. E . E . D .)

Prvr-> use sub\_app

Backup point

(. E . E . D . U .)

Prvr->qed

(. E . E . D . U . QED)

::(. E . E . D . U . QED BC)

(. E . E . D . U . QED BC)

y sub x

Proved

QED

Prvr-> \$Proceeding

prop\_rec\_5 proved in theorem prover.

Exec-> show status scope \$

SCOPE LEMMAS

Waiting to be proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL,  
APP\_PKT\_NONNULL, BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB,  
ISS\_APP, ISS\_TRANS, INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE,  
LAST\_REPEATS, MAIN\_LEMMA, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
NCHANGES\_UNIQUE, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG,  
SUB\_NCHANGES

Proved: PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4, PROP\_REC\_5,  
PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4, PROP\_TRANS\_5,  
PROP\_TRANS\_6, PROP\_TRANS\_7

Exec-> save abp.dmp

File ABP.DMP already exists. Rewrite it? -> y

Saving.....

.....

.....

Exec->

```

prove abp_1
Entering Prover with lemma abp_1
all u, v : msg_seq,
all w, x, y, z : pkt_seq,
proper_reception (v, x, y, 1) & proper_transmission (u, w, z, 1)
& x sub w & z sub y
-> msg_lag (v, u, 1)
H1: proper_reception (v, x, y, 1)
H2: proper_transmission (u, w, z, 1)
H3: x sub w
H4: z sub y
->
C1: msg_lag (v, u, 1)
Backup point
(.)
Prvr-> expand proper_reception
Backup point
(. E .)
Prvr-> expand proper_transmission
Backup point
(. E . E .)
Prvr-> simplify theorem
Prvr->theorem
H1: msg_lag (unique_msg (w), u, 1)
H2: msg_lag (v, unique_msg (x), 1)
H3: repeats (w)
H4: size (v) - size (unique_msg (y)) in [0..1]
H5: size (unique_msg (w)) - size (unique_msg (z)) in [0..1]
H6: size (u) - size (unique_msg (z)) in [0..1]
H7: x sub w
H8: y sub x
H9: z sub y
->
C1: msg_lag (v, u, 1)
Prvr-> use nchanges_unique
Backup point
(. E . E . U .)
Prvr->use nchanges_unique
Backup point
(. E . E . U . U .)
Prvr-> hypothesis
H1: size (unique_msg (x#4$)) = nchanges (seqnums (x#4$))

```

H2: size (unique\_msg (x#2\$)) = nchanges (seqnums (x#2\$))  
 H3: msg\_lag (unique\_msg (w), u, 1)  
 H4: msg\_lag (v, unique\_msg (x), 1)  
 H5: repeats (w)  
 H6: size (v) - size (unique\_msg (y)) in [0..1]  
 H7: size (unique\_msg (w)) - size (unique\_msg (z)) in [0..1]  
 H8: size (u) - size (unique\_msg (z)) in [0..1]  
 H9: x sub w  
 H10: y sub x  
 H11: z sub y  
 Prvr-> put  
 For what?\* x#4\$;  
 Put what?\* w;  
 For what?\* x#2\$;  
 Put what?\* z;  
 For what?\* \$done  
 Backup point  
 (. E . E . U . U . PUT .)  
 Prvr-> hypothesis  
 H1: size (unique\_msg (z)) = nchanges (seqnums (z))  
 H2: size (unique\_msg (w)) = nchanges (seqnums (w))  
 H3: z sub y  
 H4: y sub x  
 H5: x sub w  
 H6: size (u) - size (unique\_msg (z)) in [0..1]  
 H7: size (unique\_msg (w)) - size (unique\_msg (z)) in [0..1]  
 H8: size (v) - size (unique\_msg (y)) in [0..1]  
 H9: repeats (w)  
 H10: msg\_lag (v, unique\_msg (x), 1)  
 H11: msg\_lag (unique\_msg (w), u, 1)  
 Prvr-> equality substitute h1,h2  
 H1 yields  
 size (unique\_msg (z)) := nchanges (seqnums (z))  
 H2 yields  
 size (unique\_msg (w)) := nchanges (seqnums (w))  
 Backup point  
 (. E . E . U . U . PUT . =S .)  
 Prvr-> theorem  
 H1: msg\_lag (unique\_msg (w), u, 1)  
 H2: msg\_lag (v, unique\_msg (x), 1)  
 H3: repeats (w)  
 H4: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]  
 H5: size (u) - nchanges (seqnums (z)) in [0..1]  
 H6: size (v) - size (unique\_msg (y)) in [0..1]  
 H7: x sub w  
 H8: y sub x  
 H9: z sub y  
 ->  
 C1: msg\_lag (v, u, 1)  
 Prvr-> claim  
 Newgoal:  
 \* z sub x;  
 Defer proof of claim? y  
 Backup point  
 (. E . E . U . U . PUT . =S . .)  
 Prvr-> use sub\_seqnum  
 Backup point  
 (. E . E . U . U . PUT . =S . . U .)  
 Prvr-> hypothesis  
 H1: x#6\$ sub y#2\$ -> seqnums (x#6\$) sub seqnums (y#2\$)  
 H2: z sub x  
 H3: msg\_lag (unique\_msg (w), u, 1)  
 H4: msg\_lag (v, unique\_msg (x), 1)  
 H5: repeats (w)  
 H6: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H7: size (u) - nchanges (seqnums (z)) in [0..1]  
 H8: size (v) - size (unique\_msg (y)) in [0..1]  
 H9: x sub w  
 H10: y sub x  
 H11: z sub y  
 Prvr-> forwardchain h1  
 ::Forward chaining gives  
 seqnums (z) sub seqnums (x)  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC .)  
 Prvr-> use main\_lemma  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U .)  
 Prvr-> theorem  
 H1: repeats (y#4\$)  
 & nchanges (seqnums (y#4\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#8\$) & x#8\$ sub y#4\$

-> msg\_lag (unique\_msg (x#8\$), unique\_msg (y#4\$), 1)  
 H2: seqnums (z) sub seqnums (x)  
 H3: x#6\$ sub y#2\$ -> seqnums (x#6\$) sub seqnums (y#2\$)  
 H4: z sub x  
 H5: msg\_lag (unique\_msg (w), u, 1)  
 H6: msg\_lag (v, unique\_msg (x), 1)  
 H7: repeats (w)  
 H8: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H9: size (u) - nchanges (seqnums (z)) in [0..1]  
 H10: size (v) - size (unique\_msg (y)) in [0..1]  
 H11: x sub w  
 H12: y sub x  
 H13: z sub y  
 ->  
 C1: msg\_lag (v, u, 1)  
 Prvr-> forwardchain h1  
 ::::::::::::::Forward chaining gives  
 msg\_lag (unique\_msg (x), unique\_msg (w), 1)  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC .)  
 Prvr-> expand msg\_lag  
 More than one to expand.  
 Which do you want to expand? all  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E .)  
 Prvr->theorem  
 H1: initial\_subseq (unique\_msg (x), unique\_msg (w))  
 & size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H2: repeats (y#4\$)  
 & nchanges (seqnums (y#4\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#8\$) & x#8\$ sub y#4\$  
 -> initial\_subseq (unique\_msg (x#8\$), unique\_msg (y#4\$))  
 & size (unique\_msg (y#4\$)) - size (unique\_msg (x#8\$))  
 in [0..1]  
 H3: seqnums (z) sub seqnums (x)  
 H4: x#6\$ sub y#2\$ -> seqnums (x#6\$) sub seqnums (y#2\$)  
 H5: z sub x  
 H6: initial\_subseq (unique\_msg (w), u)  
 & size (u) - size (unique\_msg (w)) in [0..1]  
 H7: initial\_subseq (v, unique\_msg (x))  
 & size (unique\_msg (x)) - size (v) in [0..1]

H8: repeats (w)  
 H9: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H10: size (u) - nchanges (seqnums (z)) in [0..1]  
 H11: size (v) - size (unique\_msg (y)) in [0..1]  
 H12: x sub w  
 H13: y sub x  
 H14: z sub y  
 ->  
 C1: initial\_subseq (v, u)  
 C2: size (u) - size (v) in [0..1]  
 Prvr-> delete h2,h8  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: initial\_subseq (unique\_msg (w), u)  
 H2: initial\_subseq (unique\_msg (x), unique\_msg (w))  
 H3: initial\_subseq (v, unique\_msg (x))  
 H4: x#6\$ sub y#2\$ -> seqnums (x#6\$) sub seqnums (y#2\$)  
 H5: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H6: size (u) - nchanges (seqnums (z)) in [0..1]  
 H7: size (u) - size (unique\_msg (w)) in [0..1]  
 H8: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H9: size (v) - size (unique\_msg (y)) in [0..1]  
 H10: size (unique\_msg (x)) - size (v) in [0..1]  
 H11: seqnums (z) sub seqnums (x)  
 H12: x sub w  
 H13: y sub x  
 H14: z sub x  
 H15: z sub y  
 ->  
 C1: initial\_subseq (v, u)  
 C2: size (u) - size (v) in [0..1]  
 Prvr-> \$Proceeding  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 1 .)  
 Prvr-> retain h1,h2,h3  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 1 . D .)  
 Prvr-> use iss\_trans

Backup point  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U .)  
 Prvr-> use iss\_trans  
 Backup point  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U .)  
 Prvr->theorem  
 H1: initial\_subseq (u#4\$, v#4\$) & initial\_subseq (v#4\$, w#4\$)  
 -> initial\_subseq (u#4\$, w#4\$)  
 H2: initial\_subseq (u#2\$, v#2\$) & initial\_subseq (v#2\$, w#2\$)  
 -> initial\_subseq (u#2\$, w#2\$)  
 H3: initial\_subseq (unique\_msg (w), u)  
 H4: initial\_subseq (unique\_msg (x), unique\_msg (w))  
 H5: initial\_subseq (v, unique\_msg (x))  
 ->  
 C1: initial\_subseq (v, u)  
 Prvr-> qed  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U .  
 QED)  
 :::(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U .  
 QED BC)  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
 C 1)  
 :::(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . Q  
 ED BC 1)  
 initial\_subseq (v, v#4\$)  
 Proved  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
 C 2)  
 :::(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U .  
 QED BC 2 BC)  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
 C 2 BC 1)  
 ::(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED  
 BC 2 BC 1)  
 initial\_subseq (unique\_msg (x), v#2\$)  
 Proved  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
 C 2 BC 2)  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
 C 2 BC 2)  
 initial\_subseq (unique\_msg (w), u)  
 Proved

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
C 2 BC)

initial\_subseq (unique\_msg (x), v#2\$) & initial\_subseq (v#2\$, u)

Proved

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
C 2)

initial\_subseq (unique\_msg (x), u)

Proved

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 . D . U . U . QED B  
C)

initial\_subseq (v, v#4\$) & initial\_subseq (v#4\$, u)

Proved

QED

Prvr-> \$Proceeding

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 1 .)

initial\_subseq (v, u)

Proved

Prvr-> \$Proceeding

Backup point

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 .)

Prvr-> theorem

H1: initial\_subseq (unique\_msg (w), u)

H2: initial\_subseq (unique\_msg (x), unique\_msg (w))

H3: initial\_subseq (v, unique\_msg (x))

H4: x#6\$ sub y#2\$ -> seqnums (x#6\$) sub seqnums (y#2\$)

H5: nchanges (seqnums (w)) - nchanges (seqnums (z))  
in [0..1]

H6: size (u) - nchanges (seqnums (z)) in [0..1]

H7: size (u) - size (unique\_msg (w)) in [0..1]

H8: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]

H9: size (v) - size (unique\_msg (y)) in [0..1]

H10: size (unique\_msg (x)) - size (v) in [0..1]

H11: seqnums (z) sub seqnums (x)

H12: x sub w

H13: y sub x

H14: z sub x

H15: z sub y

->

C1: size (u) - size (v) in [0..1]

Prvr-> delete h1,h2,h3,h4,h11,h12,h13,h14

Backup point

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D .)

Prvr-> theorem

H1: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

H2: size (u) - nchanges (seqnums (z)) in [0..1]

H3: size (u) - size (unique\_msg (w)) in [0..1]

H4: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]

H5: size (v) - size (unique\_msg (y)) in [0..1]

H6: size (unique\_msg (x)) - size (v) in [0..1]

H7: z sub y

->

C1: size (u) - size (v) in [0..1]

Prvr-> use sub\_seqnum

Backup point

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D . U . )

Prvr-> use sub\_nchanges

Backup point

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D . U . U . )

Prvr-> hypothesis

H1: s#4\$ sub t#2\$ -> nchanges (s#4\$) le nchanges (t#2\$)

H2: x#10\$ sub y#6\$ -> seqnums (x#10\$) sub seqnums (y#6\$)

H3: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

H4: size (u) - nchanges (seqnums (z)) in [0..1]

H5: size (u) - size (unique\_msg (w)) in [0..1]

H6: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]

H7: size (v) - size (unique\_msg (y)) in [0..1]

H8: size (unique\_msg (x)) - size (v) in [0..1]

H9: z sub y

Prvr-> forwardchain h2

:::::::Forward chaining gives

seqnums (z) sub seqnums (y)

Backup point

(. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D . U . U . FC . )

Prvr->hypothesis

H1: seqnums (z) sub seqnums (y)

H2: s#4\$ sub t#2\$ -> nchanges (s#4\$) le nchanges (t#2\$)

H3: x#10\$ sub y#6\$ -> seqnums (x#10\$) sub seqnums (y#6\$)

H4: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

H5: size (u) - nchanges (seqnums (z)) in [0..1]

H6: size (u) - size (unique\_msg (w)) in [0..1]

H7: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]

H8: size (v) - size (unique\_msg (y)) in [0..1]  
 H9: size (unique\_msg (x)) - size (v) in [0..1]  
 H10: z sub y  
 Prvr->hypothesis  
 H1: seqnums (z) sub seqnums (y)  
 H2: s#4\$ sub t#2\$ -> nchanges (s#4\$) le nchanges (t#2\$)  
 H3: x#10\$ sub y#6\$ -> seqnums (x#10\$) sub seqnums (y#6\$)  
 H4: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H5: size (u) - nchanges (seqnums (z)) in [0..1]  
 H6: size (u) - size (unique\_msg (w)) in [0..1]  
 H7: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H8: size (v) - size (unique\_msg (y)) in [0..1]  
 H9: size (unique\_msg (x)) - size (v) in [0..1]  
 H10: z sub y  
 Prvr-> forwardchain h2  
 :Forward chaining gives  
 nchanges (seqnums (z)) le nchanges (seqnums (y))  
 Backup point  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D . U . U . FC .  
 FC .)  
 Prvr-> hypothesis  
 H1: nchanges (seqnums (z)) le nchanges (seqnums (y))  
 H2: seqnums (z) sub seqnums (y)  
 H3: s#4\$ sub t#2\$ -> nchanges (s#4\$) le nchanges (t#2\$)  
 H4: x#10\$ sub y#6\$ -> seqnums (x#10\$) sub seqnums (y#6\$)  
 H5: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H6: size (u) - nchanges (seqnums (z)) in [0..1]  
 H7: size (u) - size (unique\_msg (w)) in [0..1]  
 H8: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H9: size (v) - size (unique\_msg (y)) in [0..1]  
 H10: size (unique\_msg (x)) - size (v) in [0..1]  
 H11: z sub y  
 Prvr-> delete h2,h3,h4,h11  
 Backup point  
 (. E . E . U . U . PUT . =S .. U . FC . U . FC . E . D . 2 . D . U . U . FC .  
 FC . D .)  
 Prvr->simplify theorem  
 Prvr->theorem  
 H1: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]

H2: size (u) - nchanges (seqnums (z)) in [0..1]  
 H3: size (u) - size (unique\_msg (w)) in [0..1]  
 H4: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H5: size (v) - size (unique\_msg (y)) in [0..1]  
 H6: size (unique\_msg (x)) - size (v) in [0..1]  
 H7: nchanges (seqnums (z)) le nchanges (seqnums (y))  
 ->  
 C1: size (u) - size (v) in [0..1]  
 Prvr-> use nchanges\_unique  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 2 . D . U . U . FC .  
 FC . D . U .)  
 Prvr->put  
 For what?\* \$done  
 Prvr-> hypothesis  
 H1: size (unique\_msg (x#12\$)) = nchanges (seqnums (x#12\$))  
 H2: nchanges (seqnums (w)) - nchanges (seqnums (z))  
 in [0..1]  
 H3: size (u) - nchanges (seqnums (z)) in [0..1]  
 H4: size (u) - size (unique\_msg (w)) in [0..1]  
 H5: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H6: size (v) - size (unique\_msg (y)) in [0..1]  
 H7: size (unique\_msg (x)) - size (v) in [0..1]  
 H8: nchanges (seqnums (z)) le nchanges (seqnums (y))  
 Prvr-> put  
 For what?\* x#12\$;  
 Put what?\* y;  
 For what?\* \$done  
 Backup point  
 (. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 2 . D . U . U . FC .  
 FC . D . U . PUT .)  
 Prvr->equality substitute h1  
 H1 no longer part of current HYPOTHESES.  
 \*\*\*\* Command Aborted  
 Prvr-> hypothesis  
 H1: size (unique\_msg (y)) = nchanges (seqnums (y))  
 H2: nchanges (seqnums (z)) le nchanges (seqnums (y))  
 H3: size (unique\_msg (x)) - size (v) in [0..1]  
 H4: size (v) - size (unique\_msg (y)) in [0..1]  
 H5: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]  
 H6: size (u) - size (unique\_msg (w)) in [0..1]  
 H7: size (u) - nchanges (seqnums (z)) in [0..1]

H8: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

Prvr-> equality substitute h1

H1 can be solved for:

T1: nchanges (seqnums (y))

T2: size (unique\_msg (y))

Which term (by label) do you want to substitute for?

t1

nchanges (seqnums (y)) := size (unique\_msg (y))

OK??

y

Backup point

(. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 2 . D . U . U . FC .

FC . D . U . PUT . =S .)

Prvr->theorem

H1: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

H2: size (u) - nchanges (seqnums (z)) in [0..1]

H3: size (u) - size (unique\_msg (w)) in [0..1]

H4: size (unique\_msg (w)) - size (unique\_msg (x)) in [0..1]

H5: size (v) - size (unique\_msg (y)) in [0..1]

H6: size (unique\_msg (x)) - size (v) in [0..1]

H7: nchanges (seqnums (z)) le size (unique\_msg (y))

->

C1: size (u) - size (v) in [0..1]

Prvr-> \$Proceeding

::::::(. E . E . U . U . PUT . =S . . U . FC . U . FC . E . D . 2 .)

size (u) - size (v) in [0..1]

Proved

Prvr-> \$Proceeding

Proved using CLAIM. Now prove the claim.

Backup point

(CLAIM .)

Prvr-> theorem

H1: msg\_lag (unique\_msg (w), u, 1)

H2: msg\_lag (v, unique\_msg (x), 1)

H3: repeats (w)

H4: nchanges (seqnums (w)) - nchanges (seqnums (z))

in [0..1]

H5: size (u) - nchanges (seqnums (z)) in [0..1]

H6: size (v) - size (unique\_msg (y)) in [0..1]

H7: x sub w

H8: y sub x  
 H9: z sub y  
 ->  
 C1: z sub x  
 Prvr-> retain h8,h9  
 Backup point  
 (CLAIM . D .)  
 Prvr-> \$Proceeding  
 (CLAIM .)  
 z sub x  
 Established claim  
 abp\_1 proved in theorem prover.  
 Exec-> prove main\_lemma  
 Entering Prover with lemma main\_lemma  
 all s : bit\_seq,  
 all x, y : pkt\_seq,  
 repeats (y)  
 & nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 & s sub seqnums (x) & x sub y  
 -> msg\_lag (unique\_msg (x), unique\_msg (y), 1)  
 H1: repeats (y)  
 H2: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H3: s sub seqnums (x)  
 H4: x sub y  
 ->  
 C1: msg\_lag (unique\_msg (x), unique\_msg (y), 1)  
 Backup point  
 (.)  
 Prvr-> use interpolate  
 Backup point  
 (. U .)  
 Prvr-> hypothesis  
 H1: repeats (y#2\$)  
 & nchanges (seqnums (y#2\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#2\$) & x#2\$ sub y#2\$  
 -> nchanges (seqnums (y#2\$))  
 - nchanges (seqnums (x#2\$))  
 in [0..1]  
 H2: repeats (y)  
 H3: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H4: s sub seqnums (x)  
 H5: x sub y

Prvr-> forwardchain h1  
 :::::::Forward chaining gives  
 nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 Backup point  
 (. U . FC .)  
 Prvr-> expand msg\_lag  
 Backup point  
 (. U . FC . E .)  
 Prvr-> theorem  
 H1: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 H2: repeats (y#2\$)  
 & nchanges (seqnums (y#2\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#2\$) & x#2\$ sub y#2\$  
 -> nchanges (seqnums (y#2\$))  
 - nchanges (seqnums (x#2\$))  
 in [0..1]  
 H3: repeats (y)  
 H4: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H5: s sub seqnums (x)  
 H6: x sub y  
 ->  
 C1: initial\_subseq (unique\_msg (x), unique\_msg (y))  
 C2: size (unique\_msg (y)) - size (unique\_msg (x)) in [0..1]  
 Prvr-> \$Proceeding  
 Backup point  
 (. U . FC . E . 1 .)  
 Prvr-> use sub\_to\_lag  
 Backup point  
 (. U . FC . E . 1 . U .)  
 Prvr-> theorem  
 H1: repeats (y#4\$)  
 & nchanges (seqnums (y#4\$))  
 - nchanges (seqnums (x#4\$))  
 in [0..1] & x#4\$ sub y#4\$  
 -> initial\_subseq (unique\_msg (x#4\$), unique\_msg (y#4\$))  
 H2: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 H3: repeats (y#2\$)  
 & nchanges (seqnums (y#2\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#2\$) & x#2\$ sub y#2\$

-> nchanges (seqnums (y#2\$))  
 - nchanges (seqnums (x#2\$))  
 in [0..1]  
 H4: repeats (y)  
 H5: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H6: s sub seqnums (x)  
 H7: x sub y  
 ->  
 C1: initial\_subseq (unique\_msg (x), unique\_msg (y))  
 Prvr-> qed  
 (. U . FC . E . 1 . U . QED)  
 :::::::(. U . FC . E . 1 . U . QED BC)  
 (. U . FC . E . 1 . U . QED BC 1)  
 (. U . FC . E . 1 . U . QED BC 1)  
 repeats (y)  
 Proved  
 (. U . FC . E . 1 . U . QED BC 2)  
 (. U . FC . E . 1 . U . QED BC 2)  
 nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 Proved  
 (. U . FC . E . 1 . U . QED BC 3)  
 (. U . FC . E . 1 . U . QED BC 3)  
 x sub y  
 Proved  
 (. U . FC . E . 1 . U . QED BC)  
 repeats (y)  
 & nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1] & x sub y  
 Proved  
 QED  
 Prvr-> \$Proceeding  
 (. U . FC . E . 1 .)  
 initial\_subseq (unique\_msg (x), unique\_msg (y))  
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 (. U . FC . E . 2 .)  
 Prvr-> theorem  
 H1: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 H2: repeats (y#2\$)

& nchanges (seqnums (y#2\$)) - nchanges (s#2\$)  
 in [0..1] & s#2\$ sub seqnums (x#2\$) & x#2\$ sub y#2\$  
 -> nchanges (seqnums (y#2\$))  
 - nchanges (seqnums (x#2\$))  
 in [0..1]  
 H3: repeats (y)  
 H4: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H5: s sub seqnums (x)  
 H6: x sub y  
 ->  
 C1: size (unique\_msg (y)) - size (unique\_msg (x)) in [0..1]  
 Prvr-> retain h1  
 Backup point  
 (. U . FC . E . 2 . D .)  
 Prvr-> use nchanges\_unique  
 Backup point  
 (. U . FC . E . 2 . D . U .)  
 Prvr->use nchanges\_unique  
 Backup point  
 (. U . FC . E . 2 . D . U . U .)  
 Prvr->hypothesis  
 H1: size (unique\_msg (x#8\$)) = nchanges (seqnums (x#8\$))  
 H2: size (unique\_msg (x#6\$)) = nchanges (seqnums (x#6\$))  
 H3: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 Prvr-> put  
 For what?\* x#8\$;  
 Put what?\* y;  
 For what?\* x#6\$;  
 Put what?\* x;  
 For what?\* \$done  
 Backup point  
 (. U . FC . E . 2 . D . U . U . PUT .)  
 Prvr->hypothesis  
 H1: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 H2: size (unique\_msg (x)) = nchanges (seqnums (x))  
 H3: size (unique\_msg (y)) = nchanges (seqnums (y))  
 Prvr-> equality substitute h2,h3  
 H2 yields  
 size (unique\_msg (x)) := nchanges (seqnums (x))  
 H3 yields

```

size (unique_msg (y)) := nchanges (seqnums (y))
Backup point
(. U . FC . E . 2 . D . U . U . PUT . =S .)
Prvr-> $Proceeding
(. U . FC . E . 2 .)
size (unique_msg (y)) - size (unique_msg (x)) in [0..1]
Proved
Prvr-> $Proceeding
main_lemma proved in theorem prover.
Exec-> prove interpolate
Entering Prover with lemma interpolate
all s : bit_seq,
all x, y : pkt_seq,
repeats (y)
& nchanges (seqnums (y)) - nchanges (s) in [0..1]
& s sub seqnums (x) & x sub y
-> nchanges (seqnums (y)) - nchanges (seqnums (x))
in [0..1]
H1: repeats (y)
H2: nchanges (seqnums (y)) - nchanges (s) in [0..1]
H3: s sub seqnums (x)
H4: x sub y
->
C1: nchanges (seqnums (y)) - nchanges (seqnums (x))
in [0..1]
Backup point
(.)
Prvr-> use sub_seqnum
Backup point
(. U .)
Prvr->use sub_nchanges
Backup point
(. U . U .)
Prvr-> hypothesis
H1: s#2$ sub t#2$ -> nchanges (s#2$) le nchanges (t#2$)
H2: x#2$ sub y#2$ -> seqnums (x#2$) sub seqnums (y#2$)
H3: repeats (y)
H4: nchanges (seqnums (y)) - nchanges (s) in [0..1]
H5: s sub seqnums (x)
H6: x sub y
Prvr-> forwardchain h2
:::::Forward chaining gives

```

seqnums (x) sub seqnums (y)  
 Backup point  
 (. U . U . FC .)  
 Prvr-> hypothesis  
 H1: seqnums (x) sub seqnums (y)  
 H2: s#2\$ sub t#2\$ -> nchanges (s#2\$) le nchanges (t#2\$)  
 H3: x#2\$ sub y#2\$ -> seqnums (x#2\$) sub seqnums (y#2\$)  
 H4: repeats (y)  
 H5: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H6: s sub seqnums (x)  
 H7: x sub y  
 Prvr-> forwardchain h2  
 :Forward chaining gives  
 nchanges (seqnums (x)) le nchanges (seqnums (y))  
 Backup point  
 (. U . U . FC . FC .)  
 Prvr-> reorder h6  
 Backup point  
 (. U . U . FC . FC . REORDER .)  
 Prvr-> use sub\_nchanges  
 Backup point  
 (. U . U . FC . FC . REORDER . U .)  
 Prvr->hypothesis  
 H1: s#4\$ sub t#4\$ -> nchanges (s#4\$) le nchanges (t#4\$)  
 H2: s sub seqnums (x)  
 H3: nchanges (seqnums (x)) le nchanges (seqnums (y))  
 H4: seqnums (x) sub seqnums (y)  
 H5: s#2\$ sub t#2\$ -> nchanges (s#2\$) le nchanges (t#2\$)  
 H6: x#2\$ sub y#2\$ -> seqnums (x#2\$) sub seqnums (y#2\$)  
 H7: repeats (y)  
 H8: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H9: x sub y  
 Prvr-> forwardchain h1  
 :Forward chaining gives  
 nchanges (s) le nchanges (seqnums (x))  
 Backup point  
 (. U . U . FC . FC . REORDER . U . FC .)  
 Prvr->theorem  
 H1: nchanges (s) le nchanges (seqnums (x))  
 H2: s#4\$ sub t#4\$ -> nchanges (s#4\$) le nchanges (t#4\$)  
 H3: s sub seqnums (x)  
 H4: nchanges (seqnums (x)) le nchanges (seqnums (y))

H5: seqnums (x) sub seqnums (y)  
 H6: s#2\$ sub t#2\$ -> nchanges (s#2\$) le nchanges (t#2\$)  
 H7: x#2\$ sub y#2\$ -> seqnums (x#2\$) sub seqnums (y#2\$)  
 H8: repeats (y)  
 H9: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 H10: x sub y  
 ->  
 C1: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 Prvr-> retain h1,h4,h9  
 Backup point  
 (. U . FC . FC . REORDER . U . FC . D .)  
 Prvr->theorem  
 H1: nchanges (s) le nchanges (seqnums (x))  
 H2: nchanges (seqnums (x)) le nchanges (seqnums (y))  
 H3: nchanges (seqnums (y)) - nchanges (s) in [0..1]  
 ->  
 C1: nchanges (seqnums (y)) - nchanges (seqnums (x))  
 in [0..1]  
 Prvr-> \$Proceeding  
 :::interpolate proved in theorem prover.  
 Exec-> show status scope \$  
 SCOPE LEMMAS  
 Waiting to be proved: APP\_BIT\_NONNULL, APP\_MSG\_NONNULL, APP\_PKT\_NONNULL,  
 BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB, ISS\_APP, ISS\_TRANS,  
 LAST\_NEXT, LAST\_UNIQUE, LAST\_REPEATS, MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP,  
 NCHANGES\_UNIQUE, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG,  
 SUB\_NCHANGES  
 Proved: ABP\_1, INTERPOLATE, MAIN\_LEMMA, PROP\_REC\_1, PROP\_REC\_2, PROP\_REC\_3,  
 PROP\_REC\_4, PROP\_REC\_5, PROP\_TRANS\_1, PROP\_TRANS\_2, PROP\_TRANS\_3,  
 PROP\_TRANS\_4, PROP\_TRANS\_5, PROP\_TRANS\_6, PROP\_TRANS\_7  
 Exec-> save abp.dmp  
 File ABP.DMP already exists. Rewrite it? -> y  
 Saving.....  
 .....  
 .....  
 Exec-> prove next\_comp  
 Entering Prover with lemma next\_comp  
 all x : pkt\_seq,  
 all p : packet, comp (p.seqno) = next\_seqnum (x [seq: p])  
 C1: comp (p.seqno) = next\_seqnum (x [seq: p])

Backup point  
(.)  
Prvr-> qed  
(. QED)  
Ran out of tricks  
Prvr-> expand next\_seqnum  
Backup point  
(. QED E .)  
Prvr->theorem  
C1: comp (p.seqno)  
= comp (last\_bit (seqnums (x [seq: p])))  
Prvr-> qed  
(. QED E . QED)  
Ran out of tricks  
Prvr-> expand seqnums  
Backup point  
(. QED E . QED E .)  
Prvr-> expand last\_bit  
Backup point  
(. QED E . QED E . E .)  
Prvr-> simplify theorem  
Prvr->theorem  
C1: true  
Prvr-> \$Proceeding  
QED  
Prvr-> \$Proceeding  
QED  
Prvr-> \$Proceeding  
next\_comp proved in theorem prover.  
Exec-> prove ne\_next  
Entering Prover with lemma ne\_next  
all x : pkt\_seq,  
all p : packet,  
p.seqno ne next\_seqnum (x)  
-> next\_seqnum (x [seq: p]) = next\_seqnum (x)  
H1: p.seqno ne next\_seqnum (x)  
->  
C1: next\_seqnum (x [seq: p]) = next\_seqnum (x)  
Backup point  
(.)  
Prvr-> expand next\_seqnum  
More than one to expand.

Which do you want to expand?show-choices

1: next\_seqnum (x)

2: next\_seqnum (x [seq: p])

Which do you want to expand? 2

Backup point

(. E .)

Prvr-> theorem

H1: p.seqno ne next\_seqnum (x)

->

C1: comp (last\_bit (seqnums (x [seq: p])))

= next\_seqnum (x)

Prvr-> expand seqnums

Backup point

(. E . E .)

Prvr->expand last\_bit

Backup point

(. E . E . E .)

Prvr-> simplify theorem

Prvr->theorem

H1: p.seqno ne next\_seqnum (x)

->

C1: comp (p.seqno) = next\_seqnum (x)

Prvr-> use comp\_ne

Backup point

(. E . E . E . U .)

Prvr-> hypothesis

H1: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$

H2: p.seqno ne next\_seqnum (x)

Prvr-> forwardchain h1

Which way? (left or right)

left

::Forward chaining gives

comp (p.seqno) = next\_seqnum (x)

Backup point

(. E . E . E . U . FC .)

Prvr-> \$Proceeding

ne\_next proved in theorem prover.

Exec-> prove last\_next

Entering Prover with lemma last\_next

all x : pkt\_seq,

all p : packet,

x[size (x)] = p & null (pkt\_seq) ne x

-> p.seqno ne next\_seqnum (x)  
 H1: x[size (x)] = p  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: p.seqno ne next\_seqnum (x)  
 Backup point  
 (. )  
 Prvr-> expand next\_seqnum  
 Backup point  
 (. E . )  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: x[size (x)] = p  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: p.seqno ne comp (last\_bit (seqnums (x)))  
 Prvr-> expand seqnums  
 Backup point  
 (. E . E . )  
 Prvr->expand last\_bit  
 Backup point  
 (. E . E . E . )  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: x[size (x)] = p  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: p.seqno ne comp (x[size (x)].seqno)  
 Prvr-> equality substitute h1  
 H1 can be solved for:  
 T1: x[size (x)]  
 T2: p  
 Which term (by label) do you want to substitute for?  
 t1  
 x[size (x)] := p  
 OK??  
 y  
 Backup point  
 (. E . E . E . =S . )  
 Prvr-> theorem  
 H1: null (pkt\_seq) ne x  
 ->

C1: p.seqno ne comp (p.seqno)  
 Prvr-> use comp\_ne  
 Backup point  
 (. E . E . =S . U .)  
 Prvr-> theorem  
 H1: comp (b1#2\$) = b2#2\$ iff b1#2\$ ne b2#2\$  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: p.seqno ne comp (p.seqno)  
 Prvr-> put  
 For what?\* b1#2\$;  
 Put what?\* p.seqno;  
 For what?\* b2#2\$;  
 Put what?\* p.seqno;  
 For what?\* \$done  
 Backup point  
 (. E . E . =S . U . PUT .)  
 Prvr-> theorem  
 H1: comp (p.seqno) = p.seqno iff p.seqno ne p.seqno  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: p.seqno ne comp (p.seqno)  
 Prvr-> \$Proceeding  
 last\_next proved in theorem prover.  
 Exec-> prove last\_unique  
 Entering Prover with lemma last\_unique  
 all x : pkt\_seq,  
 all p : packet,  
 x[size(x)] = p & null (pkt\_seq) ne x  
 -> unique\_msg (x [seq: p]) = unique\_msg (x)  
 H1: x[size(x)] = p  
 H2: null (pkt\_seq) ne x  
 ->  
 C1: unique\_msg (x [seq: p]) = unique\_msg (x)  
 Backup point  
 (.)  
 Prvr-> expand unique\_msg  
 More than one to expand.  
 Which do you want to expand? show-choices  
 1: unique\_msg (x [seq: p])  
 2: unique\_msg (x)  
 Which do you want to expand? 1

Backup point  
 (. E .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1:  $x[\text{size}(x)] = p$   
 H2:  $\text{null}(\text{pkt\_seq}) \neq x$   
 ->  
 C1:  $\text{unique\_msg}(x)$   
 $= \text{if } p.\text{seqno} = \text{next\_seqnum}(x)$   
 $\text{then } \text{unique\_msg}(x) \text{ [seq: } p.\text{mssg}]$   
 $\text{else } \text{unique\_msg}(x)$   
 fi  
 Prvr-> use last\_next  
 Backup point  
 (. E . U .)  
 Prvr-> hypothesis  
 H1:  $x[\text{size}(x)] = p \& \text{null}(\text{pkt\_seq}) \neq x$   
 $\rightarrow p.\text{seqno} \neq \text{next\_seqnum}(x)$   
 H2:  $x[\text{size}(x)] = p$   
 H3:  $\text{null}(\text{pkt\_seq}) \neq x$   
 Prvr-> forwardchain h1  
 ::Forward chaining gives  
 $p.\text{seqno} \neq \text{next\_seqnum}(x)$   
 Backup point  
 (. E . U . FC .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 C1: true  
 Prvr-> \$Proceeding  
 last\_unique proved in theorem prover.  
 Exec-> prove last\_repeats  
 Entering Prover with lemma last\_repeats  
 all  $x : \text{pkt\_seq}$ ,  
 all  $p : \text{packet}$ ,  
 $x[\text{size}(x)] = p \& \text{repeats}(x) \& \text{null}(\text{pkt\_seq}) \neq x$   
 $\rightarrow \text{repeats}(x \text{ [seq: } p])$   
 H1:  $x[\text{size}(x)] = p$   
 H2:  $\text{repeats}(x)$   
 H3:  $\text{null}(\text{pkt\_seq}) \neq x$   
 ->  
 C1:  $\text{repeats}(x \text{ [seq: } p])$   
 Backup point

(.)  
Prvr-> expand repeats  
More than one to expand.  
Which do you want to expand? show-choices  
1: repeats (x)  
2: repeats (x [seq: p])  
Which do you want to expand? 2  
Backup point  
(. E .)  
Prvr-> simplify theorem  
Prvr->theorem  
C1: true  
Prvr-> \$Proceeding  
last\_repeats proved in theorem prover.  
Exec->  
% Now we need to stop and fill in one last specification function.  
% The definition of "initial\_subseq" was deliberately left pending  
% to avoid certain unstable prover behavior when it was expanded.  
% We now give it a definition in order to prove the lemmas which  
% use it.  
translate tty:  
Gypsy Text: (terminate with ^Z)  
\$extending scope alt\_bit\_specs =  
begin  
function initial\_subseq (u, v: msg\_seq) : boolean =  
begin  
exit (assume result iff some s: msg\_seq, u s = v);  
end;  
end;  
^Z  
No syntax errors detected  
No semantic errors detected  
Exec-> set scope lemmas  
Exec-> prove eq\_iss  
Entering Prover with lemma eq\_iss  
all u, v : msg\_seq, u = v -> initial\_subseq (u, v)  
H1: u = v  
->  
C1: initial\_subseq (u, v)  
Backup point  
(.)  
Prvr-> expand initial\_subseq

Backup point  
(. E .)  
Prvr-> theorem  
H1:  $u = v$   
->  
C1:  $u \ s\#4\$ = v$   
Prvr-> \$Proceeding  
Ran out of tricks  
Prvr-> put  
For what?\*  $s\#4\$;$   
Put what?\* null(msg\_seq);  
For what?\* \$done  
Backup point  
(. E . PUT .)  
Prvr-> \$Proceeding  
eq\_iss proved in theorem prover.  
Exec-> prove eq\_iss\_app  
Entering Prover with lemma eq\_iss\_app  
all  $u, v : msg\_seq$ ,  
all  $m : message$ ,  
 $u = v \rightarrow initial\_subseq(u [seq: m], v [seq: m])$   
H1:  $u = v$   
->  
C1:  $initial\_subseq(u [seq: m], v [seq: m])$   
Backup point  
(.)  
Prvr-> expand initial\_subseq  
Backup point  
(. E .)  
Prvr->theorem  
H1:  $u = v$   
->  
C1:  $u [seq: m] \ s\#4\$ = v [seq: m]$   
Prvr-> put  
For what?\*  $s\#4\$;$   
Put what?\* null(msg\_seq);  
For what?\* \$done  
Backup point  
(. E . PUT .)  
Prvr-> \$Proceeding  
Conclusion simplified to:  
 $u [seq: m] = v [seq: m]$ Ran out of tricks

Prvr-> theorem

H1:  $u = v$

->

C1:  $u \text{ [seq: m]} \text{ null (msg_seq)} = v \text{ [seq: m]}$

Prvr-> equality substitute h1

H1 can be solved for:

T1:  $u$

T2:  $v$

Which term (by label) do you want to substitute for?

t1

$u := v$

OK??

y

Backup point

(. E . PUT . =S .)

Prvr-> \$Proceeding

eq\_iss\_app proved in theorem prover.

Exec-> prove iss\_app

Entering Prover with lemma iss\_app

all  $u, v : \text{msg\_seq}$ ,

all  $m : \text{message}$ ,

initial\_subseq ( $u, v$ ) -> initial\_subseq ( $u, v \text{ [seq: m]}$ )

H1: initial\_subseq ( $u, v$ )

->

C1: initial\_subseq ( $u, v \text{ [seq: m]}$ )

Backup point

(.)

Prvr-> expand initial\_subseq

More than one to expand.

Which do you want to expand? all

Backup point

(. E .)

Prvr->theorem

H1:  $u \text{ s\#2} = v$

->

C1:  $u \text{ s\#7\$} = v \text{ [seq: m]}$

Prvr-> simplify theorem

Prvr->theorem

H1:  $u \text{ s\#2} = v$

->

C1:  $u \text{ s\#7\$} = v \text{ [seq: m]}$

Prvr-> equality substitute h1

H1 yields  
v := u s#2  
Backup point  
(. E . =S .)  
Prvr->theorem  
H1: true  
->  
C1: u s#2 [seq: m] = u s#7\$  
Prvr-> \$Proceeding  
iss\_app proved in theorem prover.  
Exec-> prove iss\_trans  
Entering Prover with lemma iss\_trans  
all u, v, w : msg\_seq,  
initial\_subseq (u, v) & initial\_subseq (v, w)  
-> initial\_subseq (u, w)  
H1: initial\_subseq (u, v)  
H2: initial\_subseq (v, w)  
->  
C1: initial\_subseq (u, w)  
Backup point  
(.)  
Prvr-> expand initial\_subseq  
More than one to expand.  
Which do you want to expand? all  
Backup point  
(. E .)  
Prvr->simplify theorem  
Prvr->theorem  
H1: u s#2 = v  
H2: v s#3 = w  
->  
C1: u s#10\$ = w  
Prvr-> \$Proceeding  
:::Ran out of tricks  
Prvr-> equality substitute h1  
H1 yields  
v := u s#2  
Backup point  
(. E . =S .)  
Prvr-> theorem  
H1: u s#2 s#3 = w  
->

```

C1: u s#10$ = w
Prvr-> equality substitute h1
H1 yields
w := u s#2 s#3
Backup point
(. E . =S . =S .)
Prvr-> theorem
H1: true
->
C1: u s#2 s#3 = u s#10$
Prvr-> $Proceeding
iss_trans proved in theorem prover.
Exec-> prove msg_lag_eq
Entering Prover with lemma msg_lag_eq
all u, v : msg_seq, u = v iff msg_lag (u, v, 0)
C1: u = v iff msg_lag (u, v, 0)
Backup point
(.)
Prvr-> expand msg_lag
Backup point
(. E .)
Prvr-> simplify theorem
Prvr->theorem
C1: size (u) = size (v) & initial_subseq (u, v) iff u = v
Prvr-> $Proceeding
Backup point
(. E . IFFC .)
Prvr-> theorem
C1: size (u) = size (v) & initial_subseq (u, v) -> u = v
C2: u = v -> size (u) = size (v) & initial_subseq (u, v)
Prvr-> $Proceeding
Backup point
(. E . IFFC . 1 .)
Prvr-> theorem
C1: size (u) = size (v) & initial_subseq (u, v) -> u = v
Prvr-> $Proceeding
Typelist equalities
size (v) = size (u)
Backup point
(. E . IFFC . 1 . P-> .)
Prvr-> theorem
H1: size (v) = size (u)

```

H2: size (u) = size (v)  
 H3: initial\_subseq (u, v)  
 ->  
 C1: u = v  
 Prvr-> expand initial\_subseq  
 Backup point  
 (. E . IFFC . 1 . P-> . E .)  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: u s#2 = v  
 H2: size (u) = size (v)  
 H3: size (v) = size (u)  
 ->  
 C1: u = v  
 Prvr-> use size\_null  
 Backup point  
 (. E . IFFC . 1 . P-> . E . U .)  
 Prvr-> theorem  
 H1: null (msg\_seq) = u#2\$ iff 0 = size (u#2\$)  
 H2: u s#2 = v  
 H3: size (u) = size (v)  
 H4: size (v) = size (u)  
 ->  
 C1: u = v  
 Prvr-> \$Proceeding  
 .....Ran out of tricks  
 Prvr-> put  
 For what?\* u#2\$;  
 Put what?\* s#2;  
 For what?\* \$done  
 Backup point  
 (. E . IFFC . 1 . P-> . E . U . PUT .)  
 Prvr-> theorem  
 H1: null (msg\_seq) = s#2 iff 0 = size (s#2)  
 H2: size (v) = size (u)  
 H3: size (u) = size (v)  
 H4: u s#2 = v  
 ->  
 C1: u = v  
 Prvr-> simplify theorem  
 Prvr->theorem  
 H1: u s#2 = v

H2:  $\text{size}(u) = \text{size}(v)$   
 H3:  $\text{size}(v) = \text{size}(u)$   
 H4:  $\text{null}(\text{msg\_seq}) = s\#2$  iff  $0 = \text{size}(s\#2)$   
 ->  
 C1:  $u = v$   
 Prvr-> equality substitute h1  
 H1 yields  
 $v := u$   $s\#2$   
 Backup point  
 $(. E . \text{IFFC} . 1 . P-> . E . U . \text{PUT} . =S .)$   
 Prvr-> theorem  
 H1:  $\text{null}(\text{msg\_seq}) = s\#2$   
 H2:  $0 = \text{size}(s\#2)$   
 ->  
 C1:  $u$   $s\#2 = u$   
 Prvr-> simplify theorem  
 Prvr->theorem  
 C1: true  
 Prvr-> \$Proceeding  
 $(. E . \text{IFFC} . 1 .)$   
 $\text{size}(u) = \text{size}(v) \ \& \ \text{initial\_subseq}(u, v) \rightarrow u = v$   
 Proved  
 Prvr-> \$Proceeding  
 Backup point  
 $(. E . \text{IFFC} . 2 .)$   
 Prvr-> theorem  
 C1:  $u = v \rightarrow \text{size}(u) = \text{size}(v) \ \& \ \text{initial\_subseq}(u, v)$   
 Prvr-> \$Proceeding  
 Backup point  
 $(. E . \text{IFFC} . 2 . P-> .)$   
 Prvr-> theorem  
 H1:  $u = v$   
 ->  
 C1:  $\text{size}(u) = \text{size}(v)$   
 C2:  $\text{initial\_subseq}(u, v)$   
 Prvr-> equality substitute h1  
 H1 can be solved for:  
 T1:  $u$   
 T2:  $v$   
 Which term (by label) do you want to substitute for?  
 t1  
 $u := v$

OK??  
y  
Backup point  
(. E . IFFC . 2 . P-> . =S .)  
Prvr-> \$Proceeding  
Ran out of tricks  
Prvr-> theorem  
H1: true  
->  
C1: initial\_subseq (v, v)  
Prvr-> use eq\_iss  
Backup point  
(. E . IFFC . 2 . P-> . =S . U .)  
Prvr-> qed  
(. E . IFFC . 2 . P-> . =S . U . QED)  
(. E . IFFC . 2 . P-> . =S . U . QED BC)  
(. E . IFFC . 2 . P-> . =S . U . QED BC)  
v = v  
Proved  
QED  
Prvr-> \$Proceeding  
(. E . IFFC . 2 .)  
u = v -> size (u) = size (v) & initial\_subseq (u, v)  
Proved  
Prvr-> \$Proceeding  
msg\_lag\_eq proved in theorem prover.  
Exec-> prove comp\_ne  
Entering Prover with lemma comp\_ne  
all b1, b2 : bit, comp (b1) = b2 iff b1 ne b2  
C1: comp (b1) = b2 iff b1 ne b2  
Backup point  
(.)  
Prvr-> \$Proceeding  
Backup point  
(. IFFC .)  
Prvr-> \$Proceeding  
Backup point  
(. IFFC . 1 .)  
Prvr-> theorem  
C1: comp (b1) = b2 -> b1 ne b2  
Prvr-> \$Proceeding  
Backup point

```

(. IFFC . 1 . P->.)
Prvr-> theorem
H1: comp (b1) = b2
->
C1: b1 ne b2
Prvr-> use bit_cases
Backup point
(. IFFC . 1 . P-> . U .)
Prvr-> theorem
H1: b#2$ = one or b#2$ = zero
H2: comp (b1) = b2
->
C1: b1 ne b2
Prvr-> expand comp
Backup point
(. IFFC . 1 . P-> . U . E .)
Prvr-> simplify theorem
Prvr->theorem
H1: if b1 = zero then one else zero fi = b2
H2: b#2$ = one or b#2$ = zero
->
C1: b1 ne b2
Prvr-> put
For what?* b#2$;
Put what?* b1
* ;
For what?* $done
Backup point
(. IFFC . 1 . P-> . U . E . PUT .)
Prvr-> simplify theorem
Prvr->theorem
H1: if b1 = zero then one else zero fi = b2
H2: b1 = one or b1 = zero
->
C1: b1 ne b2
Prvr-> qed
(. IFFC . 1 . P-> . U . E . PUT . QED)
;;
b2 := if b1 = zero then one else zero fi
(. IFFC . 1 . P-> . U . E . PUT . QED =S)
Attempting CASE1
b1 = one

```

(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE1)

Ran out of tricks

Prvr-> theorem

H1: b1 = one

->

C1: if b1 = zero then one else zero fi ne b1

Prvr-> simplify theorem

Prvr->theorem

H1: b1 = one

->

C1: if b1 = zero then one else zero fi ne b1

Prvr-> equality substitute h1

H1 can be solved for:

T1: b1

T2: one

Which term (by label) do you want to substitute for?

t1

b1 := one

OK??

y

Backup point

(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE1 =S .)

Prvr-> \$Proceeding

(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE1 .)

b1 = one -> if b1 = zero then one else zero fi ne b1

Proved

Attempting CASE2

b1 = zero

Backup point

(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE2 .)

Prvr-> theorem

H1: b1 = zero

->

C1: if b1 = zero then one else zero fi ne b1

Prvr-> equality substitute h1

H1 can be solved for:

T1: b1

T2: zero

Which term (by label) do you want to substitute for?

t1

b1 := zero

OK??

y  
Backup point  
(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE2 . =S .)  
Prvr-> \$Proceeding  
(. IFFC . 1 . P-> . U . E . PUT . QED =S CASE2 .)  
b1 = zero -> if b1 = zero then one else zero fi ne b1  
Proved  
Done with cases  
QED  
Prvr-> \$Proceeding  
(. IFFC . 1 .)  
comp (b1) = b2 -> b1 ne b2  
Proved  
Prvr-> \$Proceeding  
Backup point  
(. IFFC . 2 .)  
Prvr-> theorem  
C1: b1 ne b2 -> comp (b1) = b2  
Prvr-> \$Proceeding  
Backup point  
(. IFFC . 2 . P-> .)  
Prvr-> theorem  
H1: b1 ne b2  
->  
C1: comp (b1) = b2  
Prvr-> expand comp  
Backup point  
(. IFFC . 2 . P-> . E .)  
Prvr-> simplify theorem  
Prvr->theorem  
H1: b1 ne b2  
->  
C1: if b1 = zero then one else zero fi = b2  
Prvr-> use bit\_cases  
Backup point  
(. IFFC . 2 . P-> . E . U .)  
Prvr-> hypothesis  
H1: b#4\$ = one or b#4\$ = zero  
H2: b1 ne b2  
Prvr-> put  
For what?\* b#4\$;  
Put what?\* b1;

For what?\* \$done  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT .)  
Prvr-> theorem  
H1: b1 = one or b1 = zero  
H2: b1 ne b2  
->  
C1: if b1 = zero then one else zero fi = b2  
Prvr-> qed  
(. IFFC . 2 . P-> . E . U . PUT . QED)  
:::Attempting CASE1  
b1 = one  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1)  
:::Ran out of tricks  
Prvr-> theorem  
H1: b1 = one  
H2: b1 ne b2  
->  
C1: if b1 = zero then one else zero fi = b2  
Prvr-> equality substitute h1  
H1 yields  
b1 := one  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S .)  
Prvr-> \$Proceeding  
Ran out of tricks  
Prvr-> theorem  
H1: b2 ne one  
->  
C1: b2 = zero  
Prvr-> use bit\_cases  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U .)  
Prvr-> theorem  
H1: b#6\$ = one or b#6\$ = zero  
H2: b2 ne one  
->  
C1: b2 = zero  
Prvr-> put  
For what?\* b#6\$;  
Put what?\* b2;  
For what?\* \$done

Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U . PUT .)  
Prvr-> \$Proceeding  
:::Attempting CASE1  
b2 = one  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U . PUT . CASE1 .)  
Prvr-> \$Proceeding  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U . PUT . CASE1 .)  
b2 = one -> b2 = zero  
Proved  
Attempting CASE2  
b2 = zero  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U . PUT . CASE2 .)  
Prvr-> \$Proceeding  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 =S . U . PUT . CASE2 .)  
b2 = zero -> b2 = zero  
Proved  
Done with cases  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE1 .)  
b1 = one -> if b1 = zero then one else zero fi = b2  
Proved  
Attempting CASE2  
b1 = zero  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 .)  
Prvr-> \$Proceeding  
:::Ran out of tricks  
Prvr-> theorem  
H1: b1 = zero  
H2: b1 ne b2  
->  
C1: if b1 = zero then one else zero fi = b2  
Prvr-> equality substitute h1  
H1 yields  
b1 := zero  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S .)  
Prvr-> \$Proceeding  
Ran out of tricks  
Prvr-> theorem

H1: b2 ne zero  
->  
C1: b2 = one  
Prvr-> use bit\_cases  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U .)  
Prvr-> hypothesis  
H1: b#8\$ = one or b#8\$ = zero  
H2: b2 ne zero  
Prvr-> put  
For what?\* b#8\$;  
Put what?\* b2;  
For what?\* \$done  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U . PUT .)  
Prvr-> \$Proceeding  
::Attempting CASE1  
b2 = one  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U . PUT . CASE1 .)  
Prvr-> \$Proceeding  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U . PUT . CASE1 .)  
b2 = one -> b2 = one  
Proved  
Attempting CASE2  
b2 = zero  
Backup point  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U . PUT . CASE2 .)  
Prvr-> \$Proceeding  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 . =S . U . PUT . CASE2 .)  
b2 = zero -> b2 = one  
Proved  
Done with cases  
(. IFFC . 2 . P-> . E . U . PUT . QED CASE2 .)  
b1 = zero -> if b1 = zero then one else zero fi = b2  
Proved  
Done with cases  
QED  
Prvr-> \$Proceeding  
(. IFFC . 2 .)  
b1 ne b2 -> comp (b1) = b2  
Proved

Prvr-> \$Proceeding  
comp\_ne proved in theorem prover.  
Exec-> prove hist\_sub  
Entering Prover with lemma hist\_sub  
all x, y : pkt\_buf,  
allfrom (x) sub allfrom (y) -> allfrom (x) sub allo (y)  
C1: true  
Backup point  
(.)  
Prvr-> \$Proceeding  
hist\_sub proved in theorem prover.  
Exec->  
% The following lemma constitutes the entire basis for the proof.  
prove bit\_cases  
Entering Prover with lemma bit\_cases  
all b : bit, b = one or b = zero  
C1: b = one or b = zero  
Backup point  
(.)  
Prvr-> simplify theorem  
Prvr->theorem  
C1: b = one or b = zero  
Prvr->  
% This lemma must be assumed since the prover does not have the  
% information needed about the enumeration type "bit".  
assume  
Select assumed subgoal name bit\_cases  
Enter justification (terminate with ESCape)  
see above.  
\$bit\_cases proved in theorem prover.  
Exec->  
% The following lemmas were once needed but no longer are  
% due to improvements in the simplifier.  
prove app\_pkt\_nonnull  
Entering Prover with lemma app\_pkt\_nonnull  
true  
C1: true  
Backup point  
(.)  
Prvr-> \$Proceeding  
app\_pkt\_nonnull proved in theorem prover.  
Exec-> prove app\_msg\_nonnull

```
Entering Prover with lemma app_msg_nonnull
true
C1: true
Backup point
(.)
Prvr-> $Proceeding
app_msg_nonnull proved in theorem prover.
Exec-> prove app_bit_nonnull
Entering Prover with lemma app_bit_nonnull
true
C1: true
Backup point
(.)
Prvr-> $Proceeding
app_bit_nonnull proved in theorem prover.
Exec->
% Finally, we come to the remaining set of lemmas which are those
% proved under the Affirm system. Their definitions have noted
% that they are to be assumed so they will just fall through the
% prover here.
prove sub_app
Entering Prover with lemma sub_app
true
C1: true
Backup point
(.)
Prvr-> $Proceeding
sub_app proved in theorem prover.
Exec-> prove size_null
Entering Prover with lemma size_null
true
C1: true
Backup point
(.)
Prvr-> $Proceeding
size_null proved in theorem prover.
Exec-> prove sub_seqnum
Entering Prover with lemma sub_seqnum
true
C1: true
Backup point
(.)
```

Prvr->\$Proceeding  
sub\_seqnum proved in theorem prover.  
Exec-> prove sub\_seqnum  
Entering Prover with lemma sub\_seqnum  
true  
C1: true  
Backup point  
(.)  
Prvr-> \$Proceeding  
sub\_seqnum proved in theorem prover.  
Exec-> prove sub\_nchanges  
Entering Prover with lemma sub\_nchanges  
true  
C1: true  
Backup point  
(.)  
Prvr->\$Proceeding  
sub\_nchanges proved in theorem prover.  
Exec-> prove nchanges\_unique  
Entering Prover with lemma nchanges\_unique  
true  
C1: true  
Backup point  
(.)  
Prvr->\$Proceeding  
nchanges\_unique proved in theorem prover.  
Exec-> prove sub\_to\_lag  
Entering Prover with lemma sub\_to\_lag  
true  
C1: true  
Backup point  
(.)  
Prvr-> \$Proceeding  
sub\_to\_lag proved in theorem prover.  
Exec-> show status all  
The current design and verification status is:  
SCOPE ALT\_BIT\_PROTOCOL  
Waiting for pending body to be filled in: MEDIUM, TIMER  
Proved: AB\_PROTOCOL, COMP, RECEIVER, SENDER  
Types, constants: BIT, BIT\_SEQ, CLK\_BUF, MESSAGE, MSG\_BUF, MSG\_SEQ, PACKET,  
PKT\_BUF, PKT\_SEQ  
SCOPE LEMMAS

Proved: ABP\_1, APP\_BIT\_NONNULL, APP\_MSG\_NONNULL, APP\_PKT\_NONNULL,  
BIT\_CASES, COMP\_NE, EQ\_ISS, EQ\_ISS\_APP, HIST\_SUB, ISS\_APP, ISS\_TRANS,  
INTERPOLATE, LAST\_NEXT, LAST\_UNIQUE, LAST\_REPEATS, MAIN\_LEMMA,  
MSG\_LAG\_EQ, NE\_NEXT, NEXT\_COMP, NCHANGES\_UNIQUE, PROP\_REC\_1,  
PROP\_REC\_2, PROP\_REC\_3, PROP\_REC\_4, PROP\_REC\_5, PROP\_TRANS\_1,  
PROP\_TRANS\_2, PROP\_TRANS\_3, PROP\_TRANS\_4, PROP\_TRANS\_5, PROP\_TRANS\_6,  
PROP\_TRANS\_7, SUB\_APP, SIZE\_NULL, SUB\_SEQNUM, SUB\_TO\_LAG,  
SUB\_NCHANGES

SCOPE ALT\_BIT\_SPECS

For specifications only: INITIAL\_SUBSEQ, LAST\_BIT, MSG\_LAG, NCHANGES,  
NEXT\_SEQNUM, PROPER\_RECEPTION, PROPER\_TRANSMISSION, REPEATS, SEQNUMS,  
UNIQUE\_MSG

Exec-> save abv.dmp

File ABP.DMP already exists. Rewrite it? -> y

Saving.....

.....  
.....  
.....

Exec->

% This ends the Gypsy part of our proof of the Alternating Bit Protocol.

% Be sure to tune in next time when we try to prove bigger and better

% protocols.

[HDCOPY terminated at Sat 9-May-81 14:38:34]

Transcript file <DIVITO>AFFIRMTRANSCRIPT.8-FEB-81.1

is open in the AFFIRM system <AFFIRM>AFFIRM.EXE.120

1 U: load abpcontext;

file created for AFFIRM on 31-Jan-81 15:27:15

ABPCONTEXTCOMS

file created for AFFIRM on 4-Feb-81 21:48:05

BITCOMS

<DIVITO>BIT..2

file created for AFFIRM on 8-Jan-81 22:00:35

PACKETCOMS

compiled for AFFIRM on 20-Dec-80 15:42:13

file created for AFFIRM on 20-Dec-80 15:42:10

ELEMTYPECOMS

(File created under Affirm 121)

<PVLIBRARY>ELEMTYPE.COM.4<DIVITO>PACKET..2

file created for AFFIRM on 31-Jan-81 15:26:55

SEQUENCEOFELEMTYPECOMS

<DIVITO>SEQUENCEOFELEMTYPE..5

```

file created for AFFIRM on 31-Jan-81 15:25:36
SEQUENCEOFBITCOMS
<DIVITO>SEQUENCEOFBIT..5
file created for AFFIRM on 7-Feb-81 06:44:08
SEQUENCEOFPACKETCOMS
<DIVITO>SEQUENCEOFPACKET..7<DIVITO>ABPCONTEXT..3
2 U: print type elemtype;
(elemtype => ElemType)
type ElemType;
declare dummy: ElemType;
axiom dummy=dummy == TRUE;
end {ElemType} ;
3 U: print type bit;
(bit => Bit)
type Bit;
declare dummy, b: Bit;
interfaces zero, one, comp(b): Bit;
interface NormalForm(b): Boolean;
axioms dummy=dummy == TRUE,
zero = one == FALSE,
one = zero == FALSE;
axioms comp(zero) == one,
comp(one) == zero;
schema NormalForm(b) == cases(Prop(zero), Prop(one));
end {Bit} ;
4 U: print type packet;
(packet => Packet)
type Packet;
needs types Bit, ElemType;
declare dummy, p: Packet;
interface mssg(p): ElemType;
interface seqno(p): Bit;
axiom dummy=dummy == TRUE;
end {Packet} ;
5 U: print type sequenceofelemtype;
(sequenceofelemtype => SequenceOfElemType)
type SequenceOfElemType;
needs types Integer, ElemType;
declare dummy, ss, s, s1, s2, s3, s4, s5: SequenceOfElemType;
declare k, k1, k2: Integer;
declare ii, i, i1, i2, j: ElemType;
interfaces NewSequenceOfElemType, s apr i, i apl s, seq(i),

```

```

s1 join s2, LessFirst(s), LessLast(s): SequenceOfElemType;
infix join, apl, apr;
interfaces isNewSequenceOfElemType(s), s1 subseq s2, FirstInduction(s),
Induction(s), NormalForm(s), i in s, s1 iss s2: Boolean;
infix in, subseq, iss;
interface Length(s): Integer;
interfaces First(s), Last(s): ElemType;
axioms dummy=dummy == TRUE,
NewSequenceOfElemType = s apr i == FALSE,
s apr i = NewSequenceOfElemType == FALSE,
s apr i = s1 apr i1 == ((s=s1) and (i=i1));
axioms i apl NewSequenceOfElemType == NewSequenceOfElemType apr i,
i apl (s apr i1) == (i apl s) apr i1;
axiom seq(i) == NewSequenceOfElemType apr i;
axioms NewSequenceOfElemType join s == s,
(s apr i) join s1 == s join (i apl s1);
axiom LessFirst(s apr i)
== if s = NewSequenceOfElemType
then NewSequenceOfElemType
else LessFirst(s) apr i;
axiom LessLast(s apr i) == s;
axiom isNewSequenceOfElemType(s) == (s = NewSequenceOfElemType);
axioms s1 subseq (s apr i)
== ( (s1 = NewSequenceOfElemType) or s1 subseq s
or LessLast(s1) subseq s and (Last(s1) = i)),
s subseq NewSequenceOfElemType == (s = NewSequenceOfElemType);
axioms i in NewSequenceOfElemType == FALSE,
i in (s apr i1) == (i in s or (i=i1));
axioms s iss NewSequenceOfElemType == (s = NewSequenceOfElemType),
s1 iss (s2 apr i)
== ( (s1 = NewSequenceOfElemType) or s1 iss s2
or (LessLast(s1) = s2) and (Last(s1) = i));
axioms Length(NewSequenceOfElemType) == 0,
Length(s apr i) == Length(s) + 1;
axiom First(s apr i) == if s = NewSequenceOfElemType
then i
else First(s);
axiom Last(s apr i) == i;
rulemmas NewSequenceOfElemType = i apl s == FALSE,
i apl s = NewSequenceOfElemType == FALSE;
rulemmas s join (s1 apr i) == (s join s1) apr i,
s join NewSequenceOfElemType == s,

```

```

(i apl s1) join s2 == i apl (s1 join s2),
(s join (i apl s1)) join s2
== s join (i apl (s1 join s2)),
s join (s1 join s2) == (s join s1) join s2;
rulelemma LessFirst(i apl s) == s;
rulelemma LessLast(i apl s)
== if s = NewSequenceOfElemType
then NewSequenceOfElemType
else i apl LessLast(s);
rulelemmas NewSequenceOfElemType subseq s == TRUE,
s subseq s == TRUE;
rulelemma i in (i1 apl s) == (i in s or (i=i1));
rulelemmas NewSequenceOfElemType iss s == TRUE,
s iss s == TRUE;
rulelemma First(i apl s) == i;
rulelemma Last(i apl s) == if s = NewSequenceOfElemType
then i
else Last(s);
schemas FirstInduction(s)
== cases(Prop(NewSequenceOfElemType), all ss, ii
(IH(ss)
imp Prop(ii
apl ss))),
Induction(s)
== cases(Prop(NewSequenceOfElemType), all ss, ii
(IH(ss)
imp Prop(ss
apr ii))),
NormalForm(s)
== cases(Prop(NewSequenceOfElemType), all ss, ii (Prop(ss
apr ii)))
;
end {SequenceOfElemType} ;
6 U: print type sequenceofbit;
(sequenceofbit => SequenceOfBit)
type SequenceOfBit;
needs type Bit;
declare dummy, ss, s, s1, s2, s3, s4, s5: SequenceOfBit;
declare k, k1, k2: Integer;
declare ii, i, i1, i2, j: Bit;
interfaces NewSequenceOfBit, s apr i, i apl s, seq(i), s1 join s2,
LessFirst(s), LessLast(s): SequenceOfBit;

```

```

infix join, apl, apr;
interfaces isNewSequenceOfBit(s), s1 subseq s2, FirstInduction(s),
Induction(s), NormalForm(s), i in s, s1 iss s2: Boolean;
infix in, subseq, iss;
interfaces Nchanges(s), Length(s): Integer;
interfaces First(s), Last(s), LastBit(s): Bit;
axioms dummy=dummy == TRUE,
NewSequenceOfBit = s apr i == FALSE,
s apr i = NewSequenceOfBit == FALSE,
s apr i = s1 apr i1 == ((s=s1) and (i=i1));
axioms i apl NewSequenceOfBit == NewSequenceOfBit apr i,
i apl (s apr i1) == (i apl s) apr i1;
axiom seq(i) == NewSequenceOfBit apr i;
axioms NewSequenceOfBit join s == s,
(s apr i) join s1 == s join (i apl s1);
axiom LessFirst(s apr i)
== if s = NewSequenceOfBit
then NewSequenceOfBit
else LessFirst(s) apr i;
axiom LessLast(s apr i) == s;
axiom isNewSequenceOfBit(s) == (s = NewSequenceOfBit);
axioms s1 subseq (s apr i)
== ( (s1 = NewSequenceOfBit) or s1 subseq s
or LessLast(s1) subseq s and (Last(s1) = i)),
s subseq NewSequenceOfBit == (s = NewSequenceOfBit);
axioms i in NewSequenceOfBit == FALSE,
i in (s apr i1) == (i in s or (i=i1));
axioms s iss NewSequenceOfBit == (s = NewSequenceOfBit),
s1 iss (s2 apr i)
== ( (s1 = NewSequenceOfBit) or s1 iss s2
or (LessLast(s1) = s2) and (Last(s1) = i));
axioms Nchanges(NewSequenceOfBit) == 0,
Nchanges(s apr i)
== if LastBit(s) = i
then Nchanges(s)
else Nchanges(s) + 1;
axioms Length(NewSequenceOfBit) == 0,
Length(s apr i) == Length(s) + 1;
axiom First(s apr i) == if s = NewSequenceOfBit
then i
else First(s);
axiom Last(s apr i) == i;

```

```

axioms LastBit(NewSequenceOfBit) == zero,
LastBit(s apr i) == i;
rulelemmas NewSequenceOfBit = i apl s == FALSE,
i apl s = NewSequenceOfBit == FALSE;
rulelemmas s join (s1 apr i) == (s join s1) apr i,
s join NewSequenceOfBit == s,
(i apl s1) join s2 == i apl (s1 join s2),
(s join (i apl s1)) join s2
== s join (i apl (s1 join s2)),
s join (s1 join s2) == (s join s1) join s2;
rulelemma LessFirst(i apl s) == s;
rulelemma LessLast(i apl s)
== if s = NewSequenceOfBit
then NewSequenceOfBit
else i apl LessLast(s);
rulelemmas NewSequenceOfBit subseq s == TRUE,
s subseq s == TRUE;
rulelemma i in (i1 apl s) == (i in s or (i=i1));
rulelemmas NewSequenceOfBit iss s == TRUE,
s iss s == TRUE;
rulelemma First(i apl s) == i;
rulelemma Last(i apl s) == if s = NewSequenceOfBit
then i
else Last(s);
schemas FirstInduction(s)
== cases(Prop(NewSequenceOfBit), all ss, ii
(IH(ss)
imp Prop(ii apl ss))),
Induction(s)
== cases(Prop(NewSequenceOfBit), all ss, ii
(IH(ss)
imp Prop(ss apr ii))),
NormalForm(s)
== cases(Prop(NewSequenceOfBit), all ss, ii (Prop(ss apr ii)));
end {SequenceOfBit} ;
7 U: print type sequenceofpacket;
(sequenceofpacket => SequenceOfPacket)
type SequenceOfPacket;
needs types Integer, Packet, SequenceOfBit, SequenceOfElemType;
declare dummy, ss, s, s1, s2, s3, s4, s5: SequenceOfPacket;
declare k, k1, k2: Integer;
declare ii, i, i1, i2, j: Packet;

```

```

interfaces NewSequenceOfPacket, s apr i, i apl s, seq(i), s1 join s2,
LessFirst(s), LessLast(s): SequenceOfPacket;
infix join, apl, apr;
interfaces isNewSequenceOfPacket(s), s1 subseq s2, FirstInduction(s),
Induction(s), NormalForm(s), i in s, s1 iss s2, Repeats(s): Boolean;
infix in, subseq, iss;
interface Seqnums(s): SequenceOfBit;
interface UniqueMsg(s): SequenceOfElemType;
interface Length(s): Integer;
interfaces First(s), Last(s): Packet;
axioms dummy=dummy == TRUE,
NewSequenceOfPacket = s apr i == FALSE,
s apr i = NewSequenceOfPacket == FALSE,
s apr i = s1 apr i1 == ((s=s1) and (i=i1));
axioms i apl NewSequenceOfPacket == NewSequenceOfPacket apr i,
i apl (s apr i1) == (i apl s) apr i1;
axiom seq(i) == NewSequenceOfPacket apr i;
axioms NewSequenceOfPacket join s == s,
(s apr i) join s1 == s join (i apl s1);
axiom LessFirst(s apr i)
== if s = NewSequenceOfPacket
then NewSequenceOfPacket
else LessFirst(s) apr i;
axiom LessLast(s apr i) == s;
axiom isNewSequenceOfPacket(s) == (s = NewSequenceOfPacket);
axioms s1 subseq (s apr i)
== ( (s1 = NewSequenceOfPacket) or s1 subseq s
or LessLast(s1) subseq s and (Last(s1) = i)),
s subseq NewSequenceOfPacket == (s = NewSequenceOfPacket);
axioms i in NewSequenceOfPacket == FALSE,
i in (s apr i1) == (i in s or (i=i1));
axioms s iss NewSequenceOfPacket == (s = NewSequenceOfPacket),
s1 iss (s2 apr i)
== ( (s1 = NewSequenceOfPacket) or s1 iss s2
or (LessLast(s1) = s2) and (Last(s1) = i));
axioms Repeats(NewSequenceOfPacket) == TRUE,
Repeats(s apr i)
== ( Repeats(s)
and s ~= NewSequenceOfPacket
and seqno(i) = seqno(Last(s))
imp i = Last(s));
axioms Seqnums(NewSequenceOfPacket) == NewSequenceOfBit,

```

```

Seqnums(s apr i) == Seqnums(s) apr seqno(i);
axioms UniqueMsg(NewSequenceOfPacket) == NewSequenceOfElemType,
UniqueMsg(s apr i)
== if seqno(i) = LastBit(Seqnums(s))
then UniqueMsg(s)
else UniqueMsg(s) apr mssg(i);
axioms Length(NewSequenceOfPacket) == 0,
Length(s apr i) == Length(s) + 1;
axiom First(s apr i) == if s = NewSequenceOfPacket
then i
else First(s);
axiom Last(s apr i) == i;
rulemmas NewSequenceOfPacket = i apl s == FALSE,
i apl s = NewSequenceOfPacket == FALSE;
rulemmas s join (s1 apr i) == (s join s1) apr i,
s join NewSequenceOfPacket == s,
(i apl s1) join s2 == i apl (s1 join s2),
(s join (i apl s1)) join s2
== s join (i apl (s1 join s2)),
s join (s1 join s2) == (s join s1) join s2;
rulemma LessFirst(i apl s) == s;
rulemma LessLast(i apl s)
== if s = NewSequenceOfPacket
then NewSequenceOfPacket
else i apl LessLast(s);
rulemmas NewSequenceOfPacket subseq s == TRUE,
s subseq s == TRUE;
rulemma i in (i1 apl s) == (i in s or (i=i1));
rulemmas NewSequenceOfPacket iss s == TRUE,
s iss s == TRUE;
rulemma First(i apl s) == i;
rulemma Last(i apl s) == if s = NewSequenceOfPacket
then i
else Last(s);
schemas FirstInduction(s)
== cases(Prop(NewSequenceOfPacket), all ss, ii
(IH(ss)
imp Prop(ii apl ss))),
Induction(s)
== cases(Prop(NewSequenceOfPacket), all ss, ii
(IH(ss)
imp Prop(ss apr ii))),

```

```

NormalForm(s)
== cases(Prop(NewSequenceOfPacket), all ss, ii (Prop( ss
apr ii)));
end {SequenceOfPacket} ;
8 U: print type abpcontext;
(abpcontext => AbpContext)
type AbpContext;
needs types Bit, Integer, Packet, SequenceOfElemType, SequenceOfBit,
SequenceOfPacket, ElemType;
declare dummy: AbpContext;
declare b, b1, b2: Bit;
declare i, i1, i2, j, k, k1, k2: Integer;
declare p, p1, p2, i$: Packet;
declare m, m1, m2: SequenceOfElemType;
declare n, n1, n2: SequenceOfBit;
declare s, s1, s2: SequenceOfPacket;
declare e, e1, e2: ElemType;
interfaces Bounded(k1, k2, j), MsgLag(m1, m2, j): Boolean;
axiom dummy=dummy == TRUE;
rulemmas Bounded(k, k, 1) == TRUE,
Bounded(k, k+1, 1) == TRUE,
Bounded(k+1, k, 1) == FALSE,
Bounded(k1+1, k2+1, 1) == Bounded(k1, k2, 1);
rulemmas MsgLag(m, m, 1) == TRUE,
MsgLag(m, m apr e, 1) == TRUE,
MsgLag(m apr e, m, 1) == FALSE;
define Bounded(k1, k2, j)
== ((k1 <= k2) and (k2 <= j+k1)),
MsgLag(m1, m2, j)
== (m1 iss m2 and Bounded(Length(m1), Length(m2), j));
end {AbpContext} ;
9 U: read abpcontext.theorems;
(Reading AFFIRM commands from <DIVITO>ABPCONTEXT.THEOREMS.13)
New environment:
dummy: AbpContext
b, b1, b2: Bit
i, i1, i2, j, k, k1, k2: Integer
p, p1, p2, i$: Packet
m, m1, m2: SequenceOfElemType
n, n1, n2: SequenceOfBit
s, s1, s2: SequenceOfPacket
e, e1, e2: ElemType

```

theorem SubToLag, s1 subseq s2  
 and Repeats(s2)  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(s2);  
 theorem PktSubBound, s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)) + 1, 1)  
 imp Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2));  
 theorem BitSubBound, n1 subseq n2  
 and Bounded(Nchanges(n1),  
 Nchanges(n2) + 1, 1)  
 imp Bounded(Nchanges(n1), Nchanges(n2), 1)  
 and Nchanges(n1) = Nchanges(n2);  
 theorem UniqueEq, UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)), 1)  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2);  
 theorem LastEq, n1 subseq n2  
 and Bounded(Nchanges(n1), Nchanges(n2), 1)  
 imp LastBit(n1) = LastBit(n2) eqv Nchanges(n1) = Nchanges(n2);  
 theorem SubLess, n1 subseq n2 imp Nchanges(n1) <= Nchanges(n2);  
 theorem SameLastBit, n1 subseq n2  
 and b = LastBit(n2)  
 and ~((n1 apr b) subseq n2)  
 imp LastBit(n1) = LastBit(n2);  
 theorem SameLastBit2, s1 subseq s2  
 and p = Last(s2)  
 and ~((s1 apr p) subseq s2)  
 imp LastBit(Seqnums(s1)) = LastBit(Seqnums(s2));  
 theorem SubSeqnum, s1 subseq s2 imp Seqnums(s1) subseq Seqnums(s2);  
 theorem NcUnique, Nchanges(Seqnums(s)) = Length(UniqueMsg(s));  
 theorem LastSeq, s ~ NewSequenceOfPacket  
 imp seqno(Last(s)) = LastBit(Seqnums(s));  
 theorem NcNonneg, Nchanges(n) >= 0;  
 theorem BoundedBy1, Bounded(k1, k2, 1)  
 eqv (k1=k2) or (k1+1 = k2);  
 theorem IssLenEq, m1 iss m2 and (Length(m1) = Length(m2))

```

eqv m1=m2;
theorem IssLenLe, m1 iss m2 imp Length(m1) <= Length(m2);
theorem BiValued, (b ~=~ b1) and (b ~=~ b2)
imp b1=b2;
10 U: print status;
The untried theorems are BitSubBound, BiValued, BoundedBy1, IssLenEq, IssLenLe
, LastEq, LastSeq, NcNonneg, NcUnique, PktSubBound, SameLastBit, SameLastBit2,
SubLess, SubSeqnum, SubToLag, and UniqueEq.
No theorems are tried.
No theorems are assumed.
No theorems are awaiting lemma proof.
No theorems are proved.
11 U: try SubToLag;
SubToLag is untried.
all s1, s2
( s1 subseq s2 and Repeats(s2)
and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)
imp UniqueMsg(s1) iss UniqueMsg(s2))
12 U: employ Induction(s2);
Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) remains to be shown.
Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.
(NewSequenceOfPacket:)
all s1
( (s1 = NewSequenceOfPacket) and Bounded(Nchanges(Seqnums(s1)),
0, 1)
imp UniqueMsg(s1) = NewSequenceOfElemType)
13 U: replace;
TRUE
Going to leaf apr:.
all ss', ii', s1
( IH(ss', 1 {SubToLag})
and (s1 = NewSequenceOfPacket) or s1 subseq ss'
or LessLast(s1) subseq ss' and (Last(s1) = ii')
and Repeats(ss')
and (ss' ~=~ NewSequenceOfPacket) and seqno(ii')
= seqno(Last(ss'))
imp ii' = Last(ss')
imp if LastBit(Seqnums(ss')) = seqno(ii')
then Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)
imp UniqueMsg(s1) iss UniqueMsg(ss')
else Bounded(Nchanges(Seqnums(s1)),
Nchanges(Seqnums(ss')) + 1, 1)

```

imp UniqueMsg(s1) = NewSequenceOfElemType  
 or UniqueMsg(s1) iss UniqueMsg(ss')  
 or LessLast(UniqueMsg(s1)) = UniqueMsg(ss')  
 and Last(UniqueMsg(s1)) = mssg(ii'))  
 14 U: split;  
 (first:)  
 all ss', ii', s1  
 ( IH(ss', 1 {SubToLag}) and (s1 = NewSequenceOfPacket) and Repeats(  
 ss')  
 and (ss' ~= NewSequenceOfPacket) and seqno(ii')  
 = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 imp if LastBit(Seqnums(ss')) = seqno(ii')  
 then Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(ss')  
 else Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(ss')) + 1, 1)  
 imp UniqueMsg(s1) = NewSequenceOfElemType  
 or UniqueMsg(s1) iss UniqueMsg(ss')  
 or LessLast(UniqueMsg(s1)) = UniqueMsg(ss')  
 and Last(UniqueMsg(s1)) = mssg(ii'))  
 15 U: replace;  
 TRUE  
 Going to leaf second:  
 all ss', ii', s1  
 ( IH(ss', 1 {SubToLag}) and (s1 ~= NewSequenceOfPacket)  
 and s1 subseq ss' or LessLast(s1) subseq ss' and (Last(s1) = ii')  
 and Repeats(ss')  
 and (ss' ~= NewSequenceOfPacket) and seqno(ii')  
 = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 imp if LastBit(Seqnums(ss')) = seqno(ii')  
 then Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(ss')  
 else Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(ss')) + 1, 1)  
 imp UniqueMsg(s1) = NewSequenceOfElemType  
 or UniqueMsg(s1) iss UniqueMsg(ss')  
 or LessLast(UniqueMsg(s1)) = UniqueMsg(ss')  
 and Last(UniqueMsg(s1)) = mssg(ii'))  
 16 U: suppose LastBit(Seqnums(ss')) = seqno(ii');  
 (yes:)

all ss', ii', s1  
 ( LastBit(Seqnums(ss')) = seqno(ii')  
 and IH(ss', 1 {SubToLag})  
 and s1 ~ NewSequenceOfPacket  
 and s1 subseq ss'  
 or LessLast(s1) subseq ss'  
 and Last(s1) = ii'  
 and Repeats(ss')  
 and ss' ~ NewSequenceOfPacket  
 and seqno(ii') = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(ss')  
 17 U: spllit;  
 (spllit => split)  
 (first:  
 all ss', ii', s1  
 ( LastBit(Seqnums(ss')) = seqno(ii')  
 and IH(ss', 1 {SubToLag})  
 and s1 ~ NewSequenceOfPacket  
 and s1 subseq ss'  
 and Repeats(ss')  
 and ss' ~ NewSequenceOfPacket  
 and seqno(ii') = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(ss')  
 18 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/1: s1' = s1  
 Proved by chaining and narrowing  
 using the substitution  
 s1' = s1  
 TRUE  
 Going to leaf second:  
 all ss', ii', s1  
 ( LastBit(Seqnums(ss')) = seqno(ii')  
 and IH(ss', 1 {SubToLag})  
 and s1 ~ NewSequenceOfPacket  
 and ~(s1 subseq ss')  
 and LessLast(s1) subseq ss'  
 and Last(s1) = ii'

and Repeats(ss')  
 and ss' ~ NewSequenceOfPacket  
 and seqno(ii') = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(ss'))  
 19 U: employ NormalForm(s1);  
 Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (apr:)  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 imp if LastBit(Seqnums(ss')) = seqno(ii')  
 then Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)),  
 1)  
 imp UniqueMsg(ss') iss UniqueMsg(ss)  
 else Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii')) iss UniqueMsg(ss))  
 20 U: suppose;  
 (first:)  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss = NewSequenceOfPacket  
 imp if LastBit(Seqnums(ss')) = seqno(ii')  
 then Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)),  
 1)  
 imp UniqueMsg(ss') iss UniqueMsg(ss)  
 else Bounded(Nchanges(Seqnums(ss')) + 1,

Nchanges(Seqnums(ss)), 1  
 imp (UniqueMsg(ss') apr mssg(ii')) iss UniqueMsg(ss))  
 21 U: undo;  
 suppose undone.  
 22 U: suppose LastBit(Seqnums(ss')) = seqno(ii');  
 (yes:)  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) = seqno(ii')  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)), 1)  
 imp UniqueMsg(ss') iss UniqueMsg(ss))  
 23 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/2: s1 = ss' apr ii'  
 2/2: s1 = ss'  
 Proved by chaining and narrowing  
 using the substitution  
 s1 = ss'  
 TRUE  
 Going to leaf no.:.  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) ~= seqno(ii')  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii')) iss UniqueMsg(ss))

24 U: replace ii';  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) ~ seqno(ii)  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss))  
 25 U: apply LastSeq;  
 some s ((s = NewSequenceOfPacket) or (seqno(Last(s)) = LastBit(Seqnums(s))))  
 Automatically search for instantiation? no [confirm]  
 26 U: put s=ss;  
 all ss', ii', ss, ii  
 (if ss = NewSequenceOfPacket  
 then LastBit(Seqnums(ss')) ~ seqno(ii)  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss)  
 else seqno(Last(ss)) = LastBit(Seqnums(ss))  
 and LastBit(Seqnums(ss')) ~ seqno(ii)  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,

Nchanges(Seqnums(ss)), 1  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss))  
 27 U: suppose;  
 (first:)  
 all ss', ii', ss, ii  
 ( ss = NewSequenceOfPacket  
 and LastBit(Seqnums(ss')) ~eq seqno(ii)  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss))  
 28 U: replace ss;  
 all ss', ii', ss, ii  
 ( ss = NewSequenceOfPacket  
 and LastBit(Seqnums(ss')) ~eq seqno(ii)  
 and zero = seqno(ii)  
 and IH(NewSequenceOfPacket, 1 {SubToLag})  
 and ss' = NewSequenceOfPacket  
 and ii' = ii  
 imp ~Bounded(Nchanges(Seqnums(ss')) + 1, 0, 1))  
 29 U: replace ss';  
 TRUE  
 Going to leaf second:  
 all ss', ii', ss, ii  
 ( ss ~eq NewSequenceOfPacket  
 and seqno(Last(ss)) = LastBit(Seqnums(ss))  
 and LastBit(Seqnums(ss')) ~eq seqno(ii)  
 and LastBit(Seqnums(ss)) = seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')) + 1,  
 Nchanges(Seqnums(ss)), 1)

```

imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss))
30 U: replace seqno(ii);
all ss', ii', ss, ii
( ss ~ NewSequenceOfPacket
and seqno(Last(ss)) = LastBit(Seqnums(ss))
and LastBit(Seqnums(ss')) ~ LastBit(Seqnums(ss))
and LastBit(Seqnums(ss)) = seqno(ii)
and IH(ss, 1 {SubToLag})
and ~((ss' apr ii) subseq ss)
and ss' subseq ss
and ii' = ii
and Repeats(ss)
and ii = Last(ss)
and Bounded(Nchanges(Seqnums(ss')) + 1,
Nchanges(Seqnums(ss)), 1)
imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss))
31 U: apply SameLastBit2;
some s1, s2, p
( s1 subseq s2 and (p = Last(s2))
imp (s1 apr p) subseq s2 or (LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))))
Automatically search for instantiation? yes [confirm]
1/4: (s2 = ss) and (s1 = ss' apr ii)
2/4: (s2 = ss) and (s1 = ss')
1/1: p = ii
Proved by chaining and narrowing
using the substitution
(s2 = ss) and (s1 = ss') and (p = ii)
TRUE
32 U: nxt;
(nxt => next)
Going to leaf no:.
all ss', ii', s1
( LastBit(Seqnums(ss')) ~ seqno(ii')
and IH(ss', 1 {SubToLag})
and s1 ~ NewSequenceOfPacket
and s1 subseq ss'
or LessLast(s1) subseq ss'
and Last(s1) = ii'
and Repeats(ss')
and ss' ~ NewSequenceOfPacket
and seqno(ii') = seqno(Last(ss'))
imp ii' = Last(ss')

```

and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(ss')) + 1, 1)  
 imp UniqueMsg(s1) = NewSequenceOfElemType  
 or UniqueMsg(s1) iss UniqueMsg(ss')  
 or LessLast(UniqueMsg(s1)) = UniqueMsg(ss')  
 and Last(UniqueMsg(s1)) = mssg(ii'))  
 33 U: split;  
 (first:)  
 all ss', ii', s1  
 ( LastBit(Seqnums(ss')) ~ seqno(ii') )  
 and IH(ss', 1 {SubToLag})  
 and s1 ~ NewSequenceOfPacket  
 and s1 subseq ss'  
 and Repeats(ss')  
 and ss' ~ NewSequenceOfPacket  
 and seqno(ii') = seqno(Last(ss'))  
 imp ii' = Last(ss')  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(ss')) + 1, 1)  
 imp UniqueMsg(s1) = NewSequenceOfElemType  
 or UniqueMsg(s1) iss UniqueMsg(ss')  
 or LessLast(UniqueMsg(s1)) = UniqueMsg(ss')  
 and Last(UniqueMsg(s1)) = mssg(ii'))  
 34 U: apply PktSubBound;  
 some s1', s2  
 ( s1' subseq s2  
 and Bounded(Nchanges(Seqnums(s1')), Nchanges(Seqnums(s2)) + 1,  
 1)  
 imp Bounded(Nchanges(Seqnums(s1')), Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1')) = Nchanges(Seqnums(s2)))  
 Automatically search for instantiation? no [confirm]  
 35 U: put s1'=s1, s2=ss';  
 all ss', ii', s1  
 ( s1 subseq ss'  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(ss')) + 1, 1)  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(ss')), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(ss'))  
 and LastBit(Seqnums(ss')) ~ seqno(ii')  
 and IH(ss', 1 {SubToLag})  
 and s1 ~ NewSequenceOfPacket  
 and Repeats(ss')

and  $ss' \sim= \text{NewSequenceOfPacket}$   
and  $\text{seqno}(ii') = \text{seqno}(\text{Last}(ss'))$   
imp  $ii' = \text{Last}(ss')$   
imp  $\text{UniqueMsg}(s1) = \text{NewSequenceOfElemType}$   
or  $\text{UniqueMsg}(s1) \text{ iss UniqueMsg}(ss')$   
or  $\text{LessLast}(\text{UniqueMsg}(s1)) = \text{UniqueMsg}(ss')$   
and  $\text{Last}(\text{UniqueMsg}(s1)) = \text{mssg}(ii')$

36 U: invoke IH;

Automatically search for instantiation? yes [confirm]

1/1:  $s1' = s1$

Proved by chaining and narrowing

using the substitution

$s1' = s1$

TRUE

Going to leaf second::

all  $ss', ii', s1$

(  $\text{LastBit}(\text{Seqnums}(ss')) \sim= \text{seqno}(ii')$

and  $\text{IH}(ss', 1 \{\text{SubToLag}\})$

and  $s1 \sim= \text{NewSequenceOfPacket}$

and  $\sim(s1 \text{ subseq } ss')$

and  $\text{LessLast}(s1) \text{ subseq } ss'$

and  $\text{Last}(s1) = ii'$

and  $\text{Repeats}(ss')$

and  $ss' \sim= \text{NewSequenceOfPacket}$

and  $\text{seqno}(ii') = \text{seqno}(\text{Last}(ss'))$

imp  $ii' = \text{Last}(ss')$

and  $\text{Bounded}(\text{Nchanges}(\text{Seqnums}(s1)),$

$\text{Nchanges}(\text{Seqnums}(ss')) + 1, 1$

imp  $\text{UniqueMsg}(s1) = \text{NewSequenceOfElemType}$

or  $\text{UniqueMsg}(s1) \text{ iss UniqueMsg}(ss')$

or  $\text{LessLast}(\text{UniqueMsg}(s1)) = \text{UniqueMsg}(ss')$

and  $\text{Last}(\text{UniqueMsg}(s1)) = \text{mssg}(ii')$

37 U: employ NormalForm(s1);

Case  $\text{NewSequenceOfPacket}$ :  $\text{Prop}(\text{NewSequenceOfPacket})$  proven.

Case apr: all  $ss, ii$  ( $\text{Prop}(ss \text{ apr } ii)$ ) remains to be shown.

(apr:)

all  $ss', ii', ss, ii$

(  $\text{LastBit}(\text{Seqnums}(ss)) \sim= \text{seqno}(ii)$

and  $\text{IH}(ss, 1 \{\text{SubToLag}\})$

and  $\sim((ss' \text{ apr } ii') \text{ subseq } ss)$

and  $ss' \text{ subseq } ss$

and  $ii' = ii$

and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 imp if LastBit(Seqnums(ss')) = seqno(ii')  
 then Bounded(Nchanges(Seqnums(ss'))),  
 Nchanges(Seqnums(ss)) + 1, 1  
 imp UniqueMsg(ss') = NewSequenceOfElemType  
 or UniqueMsg(ss') iss UniqueMsg(ss)  
 or LessLast(UniqueMsg(ss')) = UniqueMsg(ss)  
 and Last(UniqueMsg(ss')) = mssg(ii)  
 else Bounded(Nchanges(Seqnums(ss'))), Nchanges(Seqnums(ss)),  
 1)  
 imp (UniqueMsg(ss') apr mssg(ii')) iss UniqueMsg(ss)  
 or UniqueMsg(ss') = UniqueMsg(ss)  
 and mssg(ii') = mssg(ii))  
 38 U: suppose LastBit(Seqnums(ss')) = seqno(ii');  
 (yes:  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) = seqno(ii')  
 and LastBit(Seqnums(ss)) ~ seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss'))),  
 Nchanges(Seqnums(ss)) + 1, 1  
 imp UniqueMsg(ss') = NewSequenceOfElemType  
 or UniqueMsg(ss') iss UniqueMsg(ss)  
 or LessLast(UniqueMsg(ss')) = UniqueMsg(ss)  
 and Last(UniqueMsg(ss')) = mssg(ii))  
 39 U: apply PktSubBound;  
 some s1, s2  
 ( s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)) + 1, 1)  
 imp Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2)))  
 Automatically search for instantiation? no [confirm]

40 U: put s1=ss', s2=ss;  
 all ss', ii', ss, ii  
 ( ss' subseq ss  
 and Bounded(Nchanges(Seqnums(ss'))),  
 Nchanges(Seqnums(ss)) + 1, 1)  
 and Bounded(Nchanges(Seqnums(ss'))), Nchanges(Seqnums(ss)), 1  
 and Nchanges(Seqnums(ss')) = Nchanges(Seqnums(ss))  
 and LastBit(Seqnums(ss')) = seqno(ii')  
 and LastBit(Seqnums(ss)) ~ seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 imp UniqueMsg(ss') = NewSequenceOfElemType  
 or UniqueMsg(ss') iss UniqueMsg(ss)  
 or LessLast(UniqueMsg(ss')) = UniqueMsg(ss)  
 and Last(UniqueMsg(ss')) = mssg(ii))  
 41 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/2: s1 = ss'  
 Proved by chaining and narrowing  
 using the substitution  
 s1 = ss'  
 TRUE  
 Going to leaf no:..  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) ~ seqno(ii')  
 and LastBit(Seqnums(ss)) ~ seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii') subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~ NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss'))), Nchanges(Seqnums(ss)), 1  
 imp (UniqueMsg(ss') apr mssg(ii')) iss UniqueMsg(ss)  
 or UniqueMsg(ss') = UniqueMsg(ss)

and mssg(ii') = mssg(ii)  
 42 U: repalce;  
 (repalce => replace)  
 all ss', ii', ss, ii  
 ( LastBit(Seqnums(ss')) ~= seqno(ii)  
 and LastBit(Seqnums(ss)) ~= seqno(ii)  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~= NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss)  
 or UniqueMsg(ss') = UniqueMsg(ss))  
 43 U: apply bivalued;  
 (bivalued => BiValued)  
 some b, b1, b2 ((b=b1) or (b=b2) or (b1=b2))  
 Automatically search for instantiation? no [confirm]  
 44 U: put b=seqno(ii), b1=LastBit(Seqnums(ss')), b2=LastBit(Seqnums(ss));  
 all ss', ii', ss, ii  
 ( seqno(ii) ~= LastBit(Seqnums(ss'))  
 and seqno(ii) ~= LastBit(Seqnums(ss))  
 and LastBit(Seqnums(ss')) = LastBit(Seqnums(ss))  
 and IH(ss, 1 {SubToLag})  
 and ~((ss' apr ii) subseq ss)  
 and ss' subseq ss  
 and ii' = ii  
 and Repeats(ss)  
 and ss ~= NewSequenceOfPacket  
 and seqno(ii) = seqno(Last(ss))  
 imp ii = Last(ss)  
 and Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)), 1)  
 imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss)  
 or UniqueMsg(ss') = UniqueMsg(ss))  
 45 U: apply UniqueEq;  
 some s1, s2  
 ( UniqueMsg(s1) iss UniqueMsg(s2) and s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))

```

imp UniqueMsg(s1) = UniqueMsg(s2)
Automatically search for instantiation? no [confirm]
46 U: put s1=ss', s2=ss;
all ss', ii', ss, ii
( ~(UniqueMsg(ss') iss UniqueMsg(ss))
and seqno(ii) ~= LastBit(Seqnums(ss'))
and seqno(ii) ~= LastBit(Seqnums(ss))
and LastBit(Seqnums(ss')) = LastBit(Seqnums(ss))
and IH(ss, 1 {SubToLag})
and ~((ss' apr ii) subseq ss)
and ss' subseq ss
and ii' = ii
and Repeats(ss)
and ss ~= NewSequenceOfPacket
and seqno(ii) = seqno(Last(ss))
imp ii = Last(ss)
and Bounded(Nchanges(Seqnums(ss')), Nchanges(Seqnums(ss)), 1)
imp (UniqueMsg(ss') apr mssg(ii)) iss UniqueMsg(ss)
or UniqueMsg(ss') = UniqueMsg(ss))
47 U: invoke IH;
Automatically search for instantiation? yes [confirm]
1/2: s1 = ss'
Proved by chaining and narrowing
using the substitution
s1 = ss'
TRUE
SubToLag is awaiting the proof of lemmas LastSeq, SameLastBit2, PktSubBound,
BiValued, and UniqueEq.
Going to lemma PktSubBound.
PktSubBound is untried.
all s1, s2
( s1 subseq s2
and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)) + 1, 1)
imp Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)
and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2)))
48 U: note The hump has been passed but there still are
a few nontrivial lemmas left. ;
49 U: freeze abp.frz;
Writing file ... <DIVITO>ABP.FRZ.1
50 U: quit;
Automatically summarize the proof attempts? no [confirm]
Type CONTINUE to return to AFFIRM.

```

Transcript file <DIVITO>AFFLOG.12-FEB-81.1  
 is open in the AFFIRM system <AFFIRM>AFFIRM.EXE.120  
 (<DIVITO>ABP.FRZ.1 . <AFFIRM>AFFIRM.EXE.120)  
 50 U: print status;  
 The untried theorems are BitSubBound, BiValued, BoundedBy1, IssLenEq, IssLenLe,  
 , LastEq, LastSeq, NcNonneg, NcUnique, PktSubBound, SameLastBit, SameLastBit2,  
 SubLess, SubSeqnum, and UniqueEq.  
 No theorems are tried.  
 No theorems are assumed.  
 The awaiting lemma proof theorem is SubToLag.  
 No theorems are proved.  
 51 U: print result;  
 all s1, s2  
 ( s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)) + 1, 1)  
 imp Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2)))  
 52 U: apply SubSeqnum;  
 some s1', s2' (s1' subseq s2' imp Seqnums(s1') subseq Seqnums(s2'))  
 Automatically search for instantiation? no [confirm]  
 53 U: put s1'=s1, s2'=s2;  
 all s1, s2  
 ( s1 subseq s2 and Seqnums(s1) subseq Seqnums(s2)  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)) + 1, 1)  
 imp Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2)))  
 54 U: invoke Bounded |all|;  
 all s1, s2  
 ( s1 subseq s2 and Seqnums(s1) subseq Seqnums(s2)  
 and Nchanges(Seqnums(s1)) <= Nchanges(Seqnums(s2)) + 1  
 and Nchanges(Seqnums(s2)) <= Nchanges(Seqnums(s1))  
 imp Nchanges(Seqnums(s1)) <= Nchanges(Seqnums(s2)))  
 55 U: apply SubLess;  
 some n1, n2 (n1 subseq n2 imp Nchanges(n1) <= Nchanges(n2))  
 Automatically search for instantiation? yes [confirm]  
 1/2: (n2 = Seqnums(s2)) and (n1 = Seqnums(s1))  
 Proved by chaining and narrowing  
 using the substitution  
 (n2 = Seqnums(s2)) and (n1 = Seqnums(s1))  
 TRUE  
 PktSubBound is awaiting the proof of lemmas SubSeqnum and SubLess.

56 U: next;  
Going to lemma SubLess.  
SubLess is untried.  
all n1, n2 (n1 subseq n2 imp Nchanges(n1) <= Nchanges(n2))

57 U: employ Induction(n2);

Case NewSequenceOfBit: Prop(NewSequenceOfBit) remains to be shown.

Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.

(NewSequenceOfBit:)

all n1 (n1 = NewSequenceOfBit imp Nchanges(n1) <= 0)

58 U: replace;

TRUE

Going to leaf apr:..

all ss\$, ii\$, n1

( IH(ss\$, 6 {SubLess})

and (n1 = NewSequenceOfBit) or n1 subseq ss\$

or LessLast(n1) subseq ss\$ and (Last(n1) = ii\$)

imp if LastBit(ss\$) = ii\$

then Nchanges(n1) <= Nchanges(ss\$)

else Nchanges(n1) <= Nchanges(ss\$) + 1)

59 U: split;

(first:)

all ss\$, ii\$, n1

( IH(ss\$, 6 {SubLess}) and (n1 = NewSequenceOfBit)

imp if LastBit(ss\$) = ii\$

then Nchanges(n1) <= Nchanges(ss\$)

else Nchanges(n1) <= Nchanges(ss\$) + 1)

60 U: apply NcNonneg;

some n (0 <= Nchanges(n))

Automatically search for instantiation? no [confirm]

61 U: put n=ss\$;

all ss\$, ii\$, n1

( (0 <= Nchanges(ss\$)) and IH(ss\$, 6 {SubLess})

and n1 = NewSequenceOfBit

imp if LastBit(ss\$) = ii\$

then Nchanges(n1) <= Nchanges(ss\$)

else Nchanges(n1) <= Nchanges(ss\$) + 1)

62 U: replace;

TRUE

Going to leaf second:..

all ss\$, ii\$, n1

( IH(ss\$, 6 {SubLess}) and (n1 ~= NewSequenceOfBit)

and n1 subseq ss\$ or LessLast(n1) subseq ss\$ and (Last(n1) = ii\$)

imp if LastBit(ss\$) = ii\$  
 then Nchanges(n1) <= Nchanges(ss\$)  
 else Nchanges(n1) <= Nchanges(ss\$) + 1  
 63 U: split;  
 (first:)  
 all ss\$, ii\$, n1  
 ( IH(ss\$, 6 {SubLess}) and (n1 ~= NewSequenceOfBit) and n1 subseq ss\$  
 imp if LastBit(ss\$) = ii\$  
 then Nchanges(n1) <= Nchanges(ss\$)  
 else Nchanges(n1) <= Nchanges(ss\$) + 1  
 64 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/1: n1' = n1  
 Unsuccessful.  
 all ss\$, ii\$, n1 (some n1'  
 ( n1' subseq ss\$ imp Nchanges(n1') <= Nchanges(ss\$)  
 and n1 ~= NewSequenceOfBit  
 and n1 subseq ss\$  
 imp if LastBit(ss\$) = ii\$  
 then Nchanges(n1) <= Nchanges(ss\$)  
 else Nchanges(n1) <= Nchanges(ss\$) + 1))  
 65 U: put n1'=n1;  
 TRUE  
 Going to leaf second:  
 all ss\$, ii\$, n1  
 ( IH(ss\$, 6 {SubLess}) and (n1 ~= NewSequenceOfBit)  
 and ~(n1 subseq ss\$)  
 and LessLast(n1) subseq ss\$  
 and Last(n1) = ii\$  
 imp if LastBit(ss\$) = ii\$  
 then Nchanges(n1) <= Nchanges(ss\$)  
 else Nchanges(n1) <= Nchanges(ss\$) + 1  
 66 U: employ NormalForm(n1);  
 Case NewSequenceOfBit: Prop(NewSequenceOfBit) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (apr:)  
 all ss\$, ii\$, ss\$', ii'\$  
 ( IH(ss\$', 6 {SubLess}) and ~((ss\$ apr ii\$) subseq ss\$'))  
 and ss\$ subseq ss\$'  
 and ii\$=ii\$'  
 imp if LastBit(ss\$') = ii\$'  
 then if LastBit(ss\$) = ii\$

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then Nchanges(ss$) <= Nchanges(ss$')
else Nchanges(ss$) < Nchanges(ss$')
else if LastBit(ss$) = ii$
then Nchanges(ss$) <= Nchanges(ss$') + 1
else Nchanges(ss$) <= Nchanges(ss$'))
67 U: invoke IH;
Automatically search for instantiation? no [confirm]
all ss$, ii$, ss$', ii$' (some n1
( n1 subseq ss$' imp Nchanges(n1) <= Nchanges(ss$')
and ~((ss$ apr ii$) subseq ss$')
and ss$ subseq ss$'
and ii$=ii$'
imp if LastBit(ss$') = ii$'
then if LastBit(ss$) = ii$
then Nchanges(ss$) <= Nchanges(ss$')
else Nchanges(ss$) < Nchanges(ss$')
else if LastBit(ss$) = ii$
then Nchanges(ss$) <= Nchanges(ss$') + 1
else Nchanges(ss$) <= Nchanges(ss$'))))
68 U: put n1=ss$;
all ss$, ii$, ss$', ii$'
( ss$ subseq ss$' and (Nchanges(ss$) <= Nchanges(ss$'))
and ~((ss$ apr ii$) subseq ss$')
and ii$ = ii$'
and LastBit(ss$') = ii$'
imp (LastBit(ss$) = ii$) or (Nchanges(ss$) < Nchanges(ss$'))))
69 U: replace;
all ss$, ii$, ss$', ii$'
( ss$ subseq ss$' and (Nchanges(ss$) <= Nchanges(ss$'))
and ~((ss$ apr ii$') subseq ss$')
and ii$ = ii$'
and LastBit(ss$') = ii$'
imp (LastBit(ss$) = ii$') or (Nchanges(ss$) < Nchanges(ss$'))))
70 U: apply SameLastBit;
some n1, n2, b
( n1 subseq n2 and (b = LastBit(n2))
imp (n1 apr b) subseq n2 or (LastBit(n1) = LastBit(n2)))
Automatically search for instantiation? yes [confirm]
1/4: (n2 = ss$') and (n1 = ss$)
1/2: b = LastBit(ss$)
2/2: b = ii$'
2/4: (n2 = ss$') and (n1 = ss$ apr ii$')

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3/4:  $b = \text{LastBit}(n1)$   
 4/4:  $(n2 = ss\$')$  and  $(b = ii\$')$  and  $(n1 = ss\$)$   
 Unsuccessful.  
 71 U: choose 4;  
 4/4:  $(n2 = ss\$')$  and  $(b = ii\$')$  and  $(n1 = ss\$)$   
 all  $ss\$, ii\$, ss\$', ii\$'$   
 $(ss\$ \text{ subseq } ss\$' \text{ and } (ii\$' = \text{LastBit}(ss\$'))$   
 and  $\sim((ss\$ \text{ apr } ii\$') \text{ subseq } ss\$')$   
 and  $\text{LastBit}(ss\$) = \text{LastBit}(ss\$')$   
 and  $\text{Nchanges}(ss\$) \leq \text{Nchanges}(ss\$')$   
 and  $ii\$ = ii\$'$   
 imp  $(\text{LastBit}(ss\$) = ii\$') \text{ or } (\text{Nchanges}(ss\$) < \text{Nchanges}(ss\$'))$   
 72 U: replce;  
 (replce => replace)

SubLess is awaiting the proof of lemmas NcNonneg and SameLastBit.

TRUE

Going to lemma SameLastBit.

SameLastBit is untried.

all  $n1, n2, b$

$(n1 \text{ subseq } n2 \text{ and } (b = \text{LastBit}(n2)))$   
 imp  $(n1 \text{ apr } b) \text{ subseq } n2 \text{ or } (\text{LastBit}(n1) = \text{LastBit}(n2))$

73 U: employ NormalForm(n2);

Case NewSequenceOfBit: Prop(NewSequenceOfBit) remains to be shown.

Case apr: all  $ss, ii$  (Prop(ss apr ii)) remains to be shown.

(NewSequenceOfBit:)

all  $n1, b$  ( $(n1 = \text{NewSequenceOfBit}) \text{ and } (b = \text{zero})$ )  
 imp  $\text{LastBit}(n1) = \text{zero}$

74 U: replace;

TRUE

Going to leaf apr::

all  $ss\$, ii\$, n1, b$

(if  $n1 = \text{NewSequenceOfBit}$   
 then  $b=ii\$$   
 imp  $(n1 \text{ apr } b) \text{ subseq } ss\$ \text{ or } n1 \text{ subseq } ss\$$   
 or  $\text{LastBit}(n1) = ii\$$   
 else  $\sim(n1 \text{ subseq } ss\$)$  and  $\text{LessLast}(n1) \text{ subseq } ss\$$   
 and  $\text{Last}(n1) = ii\$$   
 and  $b=ii\$$   
 imp  $(n1 \text{ apr } b) \text{ subseq } ss\$ \text{ or } (\text{LastBit}(n1) = ii\$))$

75 U: employ NormalForm(n1);

Case NewSequenceOfBit: Prop(NewSequenceOfBit) proven.

Case apr: all  $ss, ii$  (Prop(ss apr ii)) proven.

SameLastBit proved.

TRUE

Going to unproven ancestor NcNonneg.

NcNonneg is untried.

all n (0 <= Nchanges(n))

76 U: employ Induction(n);

Case NewSequenceOfBit: Prop(NewSequenceOfBit) proven.

Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.

(apr:)

all ss\$, ii\$

( IH(ss\$, 12 {NcNonneg})

imp if LastBit(ss\$) = ii\$

then 0 <= Nchanges(ss\$)

else 0 <= Nchanges(ss\$) + 1)

77 U: invoke IH;

NcNonneg proved.

SubLess proved.

TRUE

Going to unproven ancestor SubSeqnum.

SubSeqnum is untried.

all s1, s2 (s1 subseq s2 imp Seqnums(s1) subseq Seqnums(s2))

78 U: employ Induction(s2);

Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) remains to be shown.

Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.

(NewSequenceOfPacket:)

all s1 (s1 = NewSequenceOfPacket imp Seqnums(s1) = NewSequenceOfBit)

79 U: repalce;

(repalce => replace)

TRUE

Going to leaf apr:.

all ss', ii', s1

( IH(ss', 9 {SubSeqnum})

and (s1 = NewSequenceOfPacket) or s1 subseq ss'

or LessLast(s1) subseq ss' and (Last(s1) = ii')

imp (Seqnums(s1) = NewSequenceOfBit) or Seqnums(s1) subseq Seqnums(ss')

or LessLast(Seqnums(s1)) subseq Seqnums(ss') and Last(Seqnums(s1))

= seqno(ii'))

80 U: split;

(first:)

all ss', ii', s1

( IH(ss', 9 {SubSeqnum}) and (s1 = NewSequenceOfPacket)

imp (Seqnums(s1) = NewSequenceOfBit) or Seqnums(s1) subseq Seqnums(ss')

or LessLast(Seqnums(s1)) subseq Seqnums(ss') and Last(Seqnums(s1))  
 $= \text{seqno(ii')})$   
 81 U: replace;  
 TRUE  
 Going to leaf second:  
 all ss', ii', s1  
 $(\text{IH}(ss', 9 \{\text{SubSeqnum}\}) \text{ and } (s1 \sim= \text{NewSequenceOfPacket}))$   
 and  $s1 \text{ subseq } ss'$  or  $\text{LessLast}(s1) \text{ subseq } ss'$  and  $(\text{Last}(s1) = ii')$   
 $\text{imp } (\text{Seqnums}(s1) = \text{NewSequenceOfBit}) \text{ or } \text{Seqnums}(s1) \text{ subseq Seqnums}(ss')$   
 or  $\text{LessLast}(\text{Seqnums}(s1)) \text{ subseq Seqnums}(ss')$  and  $\text{Last}(\text{Seqnums}(s1))$   
 $= \text{seqno(ii')})$   
 82 U: split;  
 (first:)  
 all ss', ii', s1  
 $(\text{IH}(ss', 9 \{\text{SubSeqnum}\}) \text{ and } (s1 \sim= \text{NewSequenceOfPacket}) \text{ and } s1$   
 $\text{subseq } ss')$   
 $\text{imp } (\text{Seqnums}(s1) = \text{NewSequenceOfBit}) \text{ or } \text{Seqnums}(s1) \text{ subseq Seqnums}(ss')$   
 or  $\text{LessLast}(\text{Seqnums}(s1)) \text{ subseq Seqnums}(ss')$  and  $\text{Last}(\text{Seqnums}(s1))$   
 $= \text{seqno(ii')})$   
 83 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/1:  $s1' = s1$   
 Proved by chaining and narrowing  
 using the substitution  
 $s1' = s1$   
 TRUE  
 Going to leaf second:  
 all ss', ii', s1  
 $(\text{IH}(ss', 9 \{\text{SubSeqnum}\}) \text{ and } (s1 \sim= \text{NewSequenceOfPacket}))$   
 and  $\sim(s1 \text{ subseq } ss')$   
 and  $\text{LessLast}(s1) \text{ subseq } ss'$   
 and  $\text{Last}(s1) = ii'$   
 $\text{imp } (\text{Seqnums}(s1) = \text{NewSequenceOfBit}) \text{ or } \text{Seqnums}(s1) \text{ subseq Seqnums}(ss')$   
 or  $\text{LessLast}(\text{Seqnums}(s1)) \text{ subseq Seqnums}(ss')$  and  $\text{Last}(\text{Seqnums}(s1))$   
 $= \text{seqno(ii')})$   
 84 U: employ NormalForm(s1);  
 Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (apr:)  
 all ss', ii', ss, ii  
 $(\text{IH}(ss, 9 \{\text{SubSeqnum}\}) \text{ and } \sim((ss' \text{ apr } ii') \text{ subseq } ss))$   
 and  $ss' \text{ subseq } ss$

and  $ii' = ii$   
 $\text{imp } (\text{Seqnums}(ss') \text{ apr seqno}(ii')) \text{ subseq Seqnums}(ss)$   
 or  $\text{Seqnums}(ss') \text{ subseq Seqnums}(ss) \text{ and } (\text{seqno}(ii') = \text{seqno}(ii))$   
 85 U: replace  
 ;  
 all  $ss', ii', ss, ii$   
 $(\text{IH}(ss, 9 \{\text{SubSeqnum}\}))$   
 and  $\sim((ss' \text{ apr } ii) \text{ subseq } ss)$   
 and  $ss' \text{ subseq } ss$   
 and  $ii' = ii$   
 $\text{imp } (\text{Seqnums}(ss') \text{ apr seqno}(ii)) \text{ subseq Seqnums}(ss)$   
 or  $\text{Seqnums}(ss') \text{ subseq Seqnums}(ss))$   
 86 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/2:  $s1 = ss' \text{ apr } ii$   
 2/2:  $s1 = ss'$   
 Proved by chaining and narrowing  
 using the substitution  
 $s1 = ss'$   
 TRUE  
 SubSeqnum proved.  
 PktSubBound proved.  
 There's more than one unproven ancestor. You may pick one of UniqueEq,  
 SameLastBit2, LastSeq, or BiValued.  
 87 U: note The toughest lemmas remain in the path which  
 begins with UniqueEq. ;  
 88 U: try uniqueeq;  
 $(\text{uniqueeq} \Rightarrow \text{UniqueEq})$   
 UniqueEq is untried.  
 all  $s1, s2$   
 $(\text{UniqueMsg}(s1) \text{ iss UniqueMsg}(s2) \text{ and } s1 \text{ subseq } s2)$   
 and  $\text{Bounded}(\text{Nchanges}(\text{Seqnums}(s1)), \text{Nchanges}(\text{Seqnums}(s2)), 1)$   
 and  $\text{LastBit}(\text{Seqnums}(s1)) = \text{LastBit}(\text{Seqnums}(s2))$   
 $\text{imp UniqueMsg}(s1) = \text{UniqueMsg}(s2))$   
 89 U: apply BoundedBy1;  
 some  $k1, k2$   
 $(\text{Bounded}(k1, k2, 1))$   
 $\text{eqv } (k1 = k2) \text{ or } (k1 + 1 = k2))$   
 Automatically search for instantiation? yes [confirm]  
 1/1:  $(k2 = \text{Nchanges}(\text{Seqnums}(s2))) \text{ and } (k1 = \text{Nchanges}(\text{Seqnums}(s1)))$   
 Unsuccessful.  
 90 U: choose 1;

1/1: (k2 = Nchanges(Seqnums(s2))) and (k1 = Nchanges(Seqnums(s1)))

all s1, s2

( Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2))  
 or Nchanges(Seqnums(s1)) < Nchanges(Seqnums(s2))  
 and Nchanges(Seqnums(s1)) + 1 = Nchanges(Seqnums(s2))  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))

91 U: split;  
 (first:)

all s1, s2

( Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2))  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))

92 U: apply ncunique;  
 (ncunique => NcUnique)

some s (Nchanges(Seqnums(s)) = Length(UniqueMsg(s)))

Automatically search for instantiation? no [confirm]

93 U: apply ncunique;  
 (ncunique => NcUnique)

some s' (Nchanges(Seqnums(s')) = Length(UniqueMsg(s')))  
 Automatically search for instantiation? no [confirm]

94 U: put s=s1, s'=s2;

all s1, s2

( Nchanges(Seqnums(s2)) = Length(UniqueMsg(s2))  
 and Nchanges(Seqnums(s1)) = Length(UniqueMsg(s1))  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2))  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))

95 U: replace;

all s1, s2

( Nchanges(Seqnums(s2)) = Length(UniqueMsg(s2))  
 and Nchanges(Seqnums(s1)) = Length(UniqueMsg(s2))  
 and Length(UniqueMsg(s1)) = Length(UniqueMsg(s2))

and UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))  
 96 U: apply IssLenEq;  
 some m1, m2 (m1 iss m2 and (Length(m1) = Length(m2)) eqv m1=m2)  
 Automatically search for instantiation? yes [confirm]  
 1/1: (m2 = UniqueMsg(s2)) and (m1 = UniqueMsg(s1))  
 Proved by chaining and narrowing  
 using the substitution  
 (m2 = UniqueMsg(s2)) and (m1 = UniqueMsg(s1))  
 TRUE  
 97 U: next;  
 Going to leaf second:  
 all s1, s2  
 ( Nchanges(Seqnums(s1)) ~= Nchanges(Seqnums(s2))  
 and Nchanges(Seqnums(s1)) < Nchanges(Seqnums(s2))  
 and Nchanges(Seqnums(s1)) + 1 = Nchanges(Seqnums(s2))  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and UniqueMsg(s1) iss UniqueMsg(s2)  
 and s1 subseq s2  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))  
 98 U: apply SubSeqnum;  
 some s1', s2' (s1' subseq s2' imp Seqnums(s1') subseq Seqnums(s2'))  
 Automatically search for instantiation? no [confirm]  
 99 U: put s1'=s1, s2'=s2;  
 all s1, s2  
 ( s1 subseq s2 and Seqnums(s1) subseq Seqnums(s2)  
 and Nchanges(Seqnums(s1)) ~= Nchanges(Seqnums(s2))  
 and Nchanges(Seqnums(s1)) < Nchanges(Seqnums(s2))  
 and Nchanges(Seqnums(s1)) + 1 = Nchanges(Seqnums(s2))  
 and Bounded(Nchanges(Seqnums(s1)), Nchanges(Seqnums(s2)), 1)  
 and UniqueMsg(s1) iss UniqueMsg(s2)  
 and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
 imp UniqueMsg(s1) = UniqueMsg(s2))  
 100 U: apply LastEq;  
 some n1, n2  
 ( n1 subseq n2 and Bounded(Nchanges(n1), Nchanges(n2), 1)  
 imp LastBit(n1) = LastBit(n2) eqv Nchanges(n1) = Nchanges(n2))  
 Automatically search for instantiation? yes [confirm]  
 1/1: (n2 = Seqnums(s2)) and (n1 = Seqnums(s1))

Proved by chaining and narrowing

using the substitution

(n2 = Seqnums(s2)) and (n1 = Seqnums(s1))

TRUE

UniqueEq is awaiting the proof of lemmas BoundedBy1, NcUnique, IssLenEq

, and LastEq.

101 U: note LastEq continues the "hard line" of lemmas. ;

102 U: tyr LastEq;

what? Please correct tyr using the list: try or type.

Please correct tyr: try [confirm]

LastEq;

LastEq is untried.

all n1, n2

( n1 subseq n2 and Bounded(Nchanges(n1), Nchanges(n2), 1)

imp LastBit(n1) = LastBit(n2) eqv Nchanges(n1) = Nchanges(n2))

103 U: annotate Stating the right form of this lemma was one of  
the most crucial parts of the overall proof.;

104 U: employ Induction(n2);

Case NewSequenceOfBit: Prop(NewSequenceOfBit) remains to be shown.

Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.

(NewSequenceOfBit:)

all n1

( (n1 = NewSequenceOfBit) and Bounded(Nchanges(n1), 0, 1)

imp LastBit(n1) = zero eqv Nchanges(n1) = 0)

105 U: replace;

TRUE

Going to leaf apr.:

all ss\$, ii\$, n1

( IH(ss\$, 5 {LastEq})

and (n1 = NewSequenceOfBit) or n1 subseq ss\$

or LessLast(n1) subseq ss\$ and (Last(n1) = ii\$)

imp if LastBit(ss\$) = ii\$

then Bounded(Nchanges(n1), Nchanges(ss\$), 1)

imp LastBit(n1) = ii\$ eqv Nchanges(n1) = Nchanges(ss\$)

else Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)

imp LastBit(n1) = ii\$

eqv Nchanges(n1) = Nchanges(ss\$) + 1)

106 U: suppose LastBit(ss\$) = ii\$;

(yes:)

all ss\$, ii\$, n1

( (LastBit(ss\$) = ii\$) and IH(ss\$, 5 {LastEq})

and (n1 = NewSequenceOfBit) or n1 subseq ss\$

or LessLast(n1) subseq ss\$  
 and Last(n1) = ii\$  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 imp LastBit(n1) = ii\$ eqv Nchanges(n1) = Nchanges(ss\$))  
 107 U: replace ii\$;  
 all ss\$, ii\$, n1  
 ( (LastBit(ss\$) = ii\$) and IH(ss\$, 5 {LastEq})  
 and (n1 = NewSequenceOfBit) or n1 subseq ss\$  
 or LessLast(n1) subseq ss\$  
 and Last(n1) = LastBit(ss\$)  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 imp LastBit(n1) = LastBit(ss\$)  
 eqv Nchanges(n1) = Nchanges(ss\$))  
 108 U: suppose n1=NewSequenceOfBit or n1 subseq ss\$;  
 (yes:)  
 all ss\$, ii\$, n1  
 ( (n1 = NewSequenceOfBit) or n1 subseq ss\$  
 and LastBit(ss\$) = ii\$  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 imp LastBit(n1) = LastBit(ss\$)  
 eqv Nchanges(n1) = Nchanges(ss\$))  
 109 U: augment n1 subseq ss\$;  
 (main:)  
 all ss\$, ii\$, n1  
 ( n1 subseq ss\$ and (LastBit(ss\$) = ii\$)  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 imp LastBit(n1) = LastBit(ss\$)  
 eqv Nchanges(n1) = Nchanges(ss\$))  
 110 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/1: n1' = n1  
 Proved by chaining and narrowing  
 using the substitution  
 n1' = n1  
 TRUE  
 Going to leaf thesis:  
 all ss\$, ii\$, n1  
 ( (n1 = NewSequenceOfBit) and (LastBit(ss\$) = ii\$)  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)

```

imp n1 subseq ss$)
111 U: replace n1;
TRUE
Going to leaf no:.
all ss$, ii$, n1
( (n1 ~= NewSequenceOfBit) and ~(n1 subseq ss$)
and LastBit(ss$) = ii$
and IH(ss$, 5 {LastEq})
and LessLast(n1) subseq ss$
and Last(n1) = LastBit(ss$)
and Bounded(Nchanges(n1), Nchanges(ss$), 1)
imp LastBit(n1) = LastBit(ss$)
eqv Nchanges(n1) = Nchanges(ss$))
112 U: employ NormalForm(n1);
Case NewSequenceOfBit: Prop(NewSequenceOfBit) proven.
Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.
(apr:)
all ss$, ii$, ss$', ii$'
( ~((ss$ apr ii$) subseq ss$'))
and LastBit(ss$') = ii$'
and IH(ss$', 5 {LastEq})
and ss$ subseq ss$'
and ii$ = LastBit(ss$')
imp if LastBit(ss$) = ii$
then Bounded(Nchanges(ss$), Nchanges(ss$'), 1)
imp Nchanges(ss$) = Nchanges(ss$')
else Bounded(Nchanges(ss$) + 1, Nchanges(ss$'), 1)
imp Nchanges(ss$) + 1 = Nchanges(ss$'))
113 U: suppose;
(first:)
all ss$, ii$, ss$', ii$'
( ~((ss$ apr ii$) subseq ss$'))
and LastBit(ss$') = ii$'
and IH(ss$', 5 {LastEq})
and ss$ subseq ss$'
and ii$ = LastBit(ss$')
and LastBit(ss$) = ii$
and Bounded(Nchanges(ss$), Nchanges(ss$'), 1)
imp Nchanges(ss$) = Nchanges(ss$'))
114 U: replace;
all ss$, ii$, ss$', ii$'
( ~((ss$ apr ii$') subseq ss$'))

```

and  $\text{LastBit}(ss\$') = ii\$'$   
 and  $\text{IH}(ss\$, 5 \{\text{LastEq}\})$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = ii\$'$   
 and  $\text{LastBit}(ss\$) = ii\$'$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$), \text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) = \text{Nchanges}(ss\$')$   
 115 U: undo;  
 replace undone.  
 116 U: replace  $ii\$$ ;  
 all  $ss\$, ii\$, ss\$, ii\$'$   
 $(~((ss\$ \text{ apr } \text{LastBit}(ss\$')) \text{ subseq } ss\$'))$   
 and  $\text{LastBit}(ss\$') = ii\$'$   
 and  $\text{IH}(ss\$, 5 \{\text{LastEq}\})$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = \text{LastBit}(ss\$')$   
 and  $\text{LastBit}(ss\$) = \text{LastBit}(ss\$')$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$), \text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) = \text{Nchanges}(ss\$')$   
 117 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/2:  $n1 = ss\$ \text{ apr } \text{LastBit}(ss\$')$   
 2/2:  $n1 = ss\$$   
 Proved by chaining and narrowing  
 using the substitution  
 $n1 = ss\$$   
 TRUE  
 Going to leaf second:  
 all  $ss\$, ii\$, ss\$, ii\$'$   
 $(~((ss\$ \text{ apr } ii\$) \text{ subseq } ss\$'))$   
 and  $\text{LastBit}(ss\$') = ii\$'$   
 and  $\text{IH}(ss\$, 5 \{\text{LastEq}\})$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = \text{LastBit}(ss\$')$   
 and  $\text{LastBit}(ss\$) \sim= ii\$$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$) + 1, \text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) + 1 = \text{Nchanges}(ss\$')$   
 118 U: replace  $ii\$$ ;  
 all  $ss\$, ii\$, ss\$, ii\$'$   
 $(~((ss\$ \text{ apr } \text{LastBit}(ss\$')) \text{ subseq } ss\$'))$   
 and  $\text{LastBit}(ss\$') = ii\$'$   
 and  $\text{IH}(ss\$, 5 \{\text{LastEq}\})$

and ss\$ subseq ss\$'  
 and ii\$ = LastBit(ss\$')  
 and LastBit(ss\$) ~ = LastBit(ss\$')  
 and Bounded(Nchanges(ss\$) + 1, Nchanges(ss\$'), 1)  
 imp Nchanges(ss\$) + 1 = Nchanges(ss\$'))  
 119 U: apply SameLastBit;  
 some n1, n2, b  
 ( n1 subseq n2 and (b = LastBit(n2))  
 imp (n1 apr b) subseq n2 or (LastBit(n1) = LastBit(n2)))  
 Automatically search for instantiation? yes [confirm]  
 1/6: (n2 = ss\$') and (n1 = ss\$ apr LastBit(ss\$'))  
 2/6: (n2 = ss\$') and (n1 = ss\$)  
 1/3: b = ii\$  
 2/3: b = LastBit(ss\$)  
 3/3: b = LastBit(ss\$')  
 Proved by chaining and narrowing  
 using the substitution  
 (n2 = ss\$') and (n1 = ss\$) and (b = LastBit(ss\$'))  
 TRUE  
 120 U: next;  
 Going to leaf no.:  
 all ss\$, ii\$, n1  
 ( (LastBit(ss\$) ~ = ii\$) and IH(ss\$, 5 {LastEq})  
 and (n1 = NewSequenceOfBit) or n1 subseq ss\$  
 or LessLast(n1) subseq ss\$  
 and Last(n1) = ii\$  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 imp LastBit(n1) = ii\$  
 eqv Nchanges(n1) = Nchanges(ss\$) + 1  
 121 U: suppose n1=NewSequenceOfBit or n1 subseq ss4;  
 (... suppose aborted: effects undone)  
 122 U: suppose n1=NewSequenceOfBit or n1 subseq ss\$;  
 (yes:)  
 all ss\$, ii\$, n1  
 ( (n1 = NewSequenceOfBit) or n1 subseq ss\$  
 and LastBit(ss\$) ~ = ii\$  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 imp LastBit(n1) = ii\$  
 eqv Nchanges(n1) = Nchanges(ss\$) + 1  
 123 U: augment n1 subseq ss\$;  
 (main:)

all ss\$, ii\$, n1  
 ( n1 subseq ss\$ and (LastBit(ss\$) ~ $\equiv$  ii\$)  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 imp LastBit(n1) = ii\$  
 eqv Nchanges(n1) = Nchanges(ss\$) + 1  
 124 U: apply BitSubBound;  
 some n1', n2  
 ( n1' subseq n2 and Bounded(Nchanges(n1'), Nchanges(n2) + 1, 1)  
 imp Bounded(Nchanges(n1'), Nchanges(n2), 1) and (Nchanges(n1') = Nchanges(n2)))  
 Automatically search for instantiation? no [confirm]  
 125 U: put n1'=n1, n2=ss\$;  
 all ss\$, ii\$, n1  
 ( n1 subseq ss\$  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 and Nchanges(n1) = Nchanges(ss\$)  
 and LastBit(ss\$) ~ $\equiv$  ii\$  
 and IH(ss\$, 5 {LastEq})  
 imp LastBit(n1) ~ $\equiv$  ii\$  
 126 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/1: n1' = n1  
 Unsuccessful.  
 all ss\$, ii\$, n1 (some n1'  
 ( n1 subseq ss\$  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 and Nchanges(n1) = Nchanges(ss\$)  
 imp LastBit(ss\$) = ii\$  
 or if n1' subseq ss\$  
 and Bounded(Nchanges(n1'), Nchanges(ss\$), 1)  
 then if Nchanges(n1') = Nchanges(ss\$)  
 then LastBit(n1') = LastBit(ss\$)  
 imp LastBit(n1) ~ $\equiv$  ii\$  
 else LastBit(n1') = LastBit(ss\$)  
 or LastBit(n1) ~ $\equiv$  ii\$  
 else LastBit(n1) ~ $\equiv$  ii\$))  
 127 U: put n1'=n1;  
 all ss\$, ii\$, n1  
 ( n1 subseq ss\$

and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 and Bounded(Nchanges(n1), Nchanges(ss\$), 1)  
 and Nchanges(n1) = Nchanges(ss\$)  
 and LastBit(ss\$) ~= ii\$  
 and LastBit(n1) = LastBit(ss\$)  
 imp LastBit(n1) ~= ii\$  
 128 U: replace;  
 TRUE  
 Going to leaf thesis::  
 all ss\$, ii\$, n1  
 ( (n1 = NewSequenceOfBit) and (LastBit(ss\$) ~= ii\$)  
 and IH(ss\$, 5 {LastEq})  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 imp n1 subseq ss\$)  
 129 U: replace n1;  
 TRUE  
 Going to leaf no::  
 all ss\$, ii\$, n1  
 ( (n1 ~= NewSequenceOfBit) and ~(n1 subseq ss\$)  
 and LastBit(ss\$) ~= ii\$  
 and IH(ss\$, 5 {LastEq})  
 and LessLast(n1) subseq ss\$  
 and Last(n1) = ii\$  
 and Bounded(Nchanges(n1), Nchanges(ss\$) + 1, 1)  
 imp LastBit(n1) = ii\$  
 eqv Nchanges(n1) = Nchanges(ss\$) + 1  
 130 U: employ NormalForm(n1);  
 Case NewSequenceOfBit: Prop(NewSequenceOfBit) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (apr:  
 all ss\$, ii\$, ss\$', ii'\$  
 ( ~((ss\$ apr ii\$) subseq ss\$')  
 and LastBit(ss\$') ~= ii'\$  
 and IH(ss\$', 5 {LastEq})  
 and ss\$ subseq ss\$'  
 and ii\$ = ii'\$  
 imp if LastBit(ss\$) = ii\$  
 then Bounded(Nchanges(ss\$), Nchanges(ss\$') + 1, 1)  
 imp Nchanges(ss\$) = Nchanges(ss\$') + 1  
 else Bounded(Nchanges(ss\$), Nchanges(ss\$'), 1)  
 imp Nchanges(ss\$) + 1 = Nchanges(ss\$') + 1  
 131 U: replace ii\$';

all ss\$, ii\$, ss\$', ii\$'  
 ( ~((ss\$ apr ii\$) subseq ss\$')  
 and LastBit(ss\$') ~= ii\$  
 and IH(ss\$', 5 {LastEq})  
 and ss\$ subseq ss\$'  
 and ii\$ = ii\$'  
 imp if LastBit(ss\$) = ii\$  
 then Bounded(Nchanges(ss\$),  
 Nchanges(ss\$') + 1, 1)  
 imp Nchanges(ss\$) = Nchanges(ss\$') + 1  
 else Bounded(Nchanges(ss\$), Nchanges(ss\$'), 1)  
 imp Nchanges(ss\$) + 1 = Nchanges(ss\$') + 1)  
 132 U: suppose;  
 (first:)  
 all ss\$, ii\$, ss\$', ii\$'  
 ( ~((ss\$ apr ii\$) subseq ss\$')  
 and LastBit(ss\$') ~= ii\$  
 and IH(ss\$', 5 {LastEq})  
 and ss\$ subseq ss\$'  
 and ii\$ = ii\$'  
 and LastBit(ss\$) = ii\$  
 and Bounded(Nchanges(ss\$), Nchanges(ss\$') + 1, 1)  
 imp Nchanges(ss\$) = Nchanges(ss\$') + 1)  
 133 U: swap |all|;  
 all ss\$, ii\$, ss\$', ii\$'  
 ( ~((ss\$ apr ii\$) subseq ss\$')  
 and ii\$ ~= LastBit(ss\$')  
 and IH(ss\$', 5 {LastEq})  
 and ss\$ subseq ss\$'  
 and ii\$' = ii\$  
 and ii\$ = LastBit(ss\$)  
 and Bounded(Nchanges(ss\$), Nchanges(ss\$') + 1, 1)  
 imp Nchanges(ss\$') + 1 = Nchanges(ss\$))  
 134 U: replace;  
 all ss\$, ii\$, ss\$', ii\$'  
 ( ~((ss\$ apr LastBit(ss\$)) subseq ss\$')  
 and LastBit(ss\$) ~= LastBit(ss\$')  
 and IH(ss\$', 5 {LastEq})  
 and ss\$ subseq ss\$'  
 and ii\$' = LastBit(ss\$)  
 and ii\$ = LastBit(ss\$)  
 and Bounded(Nchanges(ss\$), Nchanges(ss\$') + 1, 1)

```

imp Nchanges(ss$') + 1 = Nchanges(ss$))
135 U: apply BitSubBound;
some n1, n2
( n1 subseq n2 and Bounded(Nchanges(n1), Nchanges(n2) + 1, 1)
imp Bounded(Nchanges(n1), Nchanges(n2), 1) and (Nchanges(n1) = Nchanges(n2)
))

Automatically search for instantiation? no [confirm]
136 U: put n1=ss$, n2=ss$';
all ss$, ii$, ss$', ii$'
( ss$ subseq ss$'
and Bounded(Nchanges(ss$), Nchanges(ss$') + 1, 1)
and Bounded(Nchanges(ss$), Nchanges(ss$'), 1)
and Nchanges(ss$) = Nchanges(ss$')
and ~((ss$ apr LastBit(ss$)) subseq ss$')
and LastBit(ss$) ~= LastBit(ss$')
and IH(ss$', 5 {LastEq}) 
and ii$' = LastBit(ss$)
imp ii$ ~= LastBit(ss$))

137 U: invoke IH;
Automatically search for instantiation? yes [confirm]
1/2: n1 = ss$

Proved by chaining and narrowing
using the substitution
n1 = ss$
TRUE

Going to leaf second:
all ss$, ii$, ss$', ii$'
( ~((ss$ apr ii$) subseq ss$')
and LastBit(ss$') ~= ii$ 
and IH(ss$', 5 {LastEq})
and ss$ subseq ss$'
and ii$ = ii$'
and LastBit(ss$) ~= ii$ 
and Bounded(Nchanges(ss$), Nchanges(ss$'), 1)
imp Nchanges(ss$) + 1 = Nchanges(ss$') + 1)

138 U: apply bivallued;
(bivallued => BiValued)
some b, b1, b2 ((b=b1) or (b=b2) or (b1=b2))
Automatically search for instantiation? no [confirm]
139 U: put b=ii$, b1=LastBit(ss$), b2=LastBit(ss$');
all ss$, ii$, ss$', ii$'
( ii$ ~= LastBit(ss$)

```

and  $ii\$ \sim= \text{LastBit}(ss\$')$   
 and  $\text{LastBit}(ss\$) = \text{LastBit}(ss\$')$   
 and  $\sim((ss\$ \text{ apr } ii\$) \text{ subseq } ss\$')$   
 and  $\text{IH}(ss\$', 5 \{\text{LastEq}\})$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = ii\$'$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$), \text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) + 1 = \text{Nchanges}(ss\$') + 1$   
 140 U: invoke IH;  
 Automatically search for instantiation? yes [confirm]  
 1/2:  $n1 = ss\$$   
 2/2:  $n1 = ss\$ \text{ apr } ii\$$   
 Unsuccessful.  
 all  $ss\$, ii\$, ss\$', ii\$'$  (some  $n1$   
 $(ii\$ \sim= \text{LastBit}(ss\$)$   
 and  $ii\$ \sim= \text{LastBit}(ss\$')$   
 and  $\text{LastBit}(ss\$) = \text{LastBit}(ss\$')$   
 imp  $(ss\$ \text{ apr } ii\$) \text{ subseq } ss\$'$   
 or if  $n1 \text{ subseq } ss\$'$   
 and  $\text{Bounded}(\text{Nchanges}(n1), \text{Nchanges}(ss\$'), 1)$   
 then if  $\text{Nchanges}(n1) = \text{Nchanges}(ss\$')$   
 then  $\text{LastBit}(n1) = \text{LastBit}(ss\$')$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = ii\$'$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$),$   
 $\text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) + 1$   
 $= \text{Nchanges}(ss\$') + 1$   
 else  $\text{LastBit}(n1) \sim= \text{LastBit}(ss\$')$   
 and  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = ii\$'$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$),$   
 $\text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) + 1$   
 $= \text{Nchanges}(ss\$') + 1$   
 else  $ss\$ \text{ subseq } ss\$'$   
 and  $ii\$ = ii\$'$   
 and  $\text{Bounded}(\text{Nchanges}(ss\$),$   
 $\text{Nchanges}(ss\$'), 1)$   
 imp  $\text{Nchanges}(ss\$) + 1$   
 $= \text{Nchanges}(ss\$') + 1))$   
 141 U: choose 1;

1/2: n1 = ss\$

LastEq is awaiting the proof of lemmas BitSubBound and BiValued.

TRUE

Going to lemma BitSubBound.

BitSubBound is untried.

all n1, n2

( n1 subseq n2 and Bounded(Nchanges(n1), Nchanges(n2) + 1, 1)

imp Bounded(Nchanges(n1), Nchanges(n2), 1) and (Nchanges(n1) = Nchanges(n2)

)

142 U: note The hump has been passed and the rest should

be clear sailing. ;

143 U: apply SubLess;

some n1', n2' (n1' subseq n2' imp Nchanges(n1') <= Nchanges(n2'))

Automatically search for instantiation? no [confirm]

144 U: put n1'=n1, n2'=n2;

all n1, n2

( n1 subseq n2 and (Nchanges(n1) <= Nchanges(n2))

and Bounded(Nchanges(n1), Nchanges(n2) + 1, 1)

imp Bounded(Nchanges(n1), Nchanges(n2), 1)

and Nchanges(n1) = Nchanges(n2))

145 U: invoke Bounded |all|;

BitSubBound proved.

TRUE

Going to unproven ancestor BiValued.

BiValued is untried.

all b, b1, b2 ((b=b1) or (b=b2) or (b1=b2))

146 U: employ NormalForm(b);

Case zero: Prop(zero) remains to be shown.

Case one: Prop(one) remains to be shown.

(zero:)

all b1, b2 ((zero = b1) or (zero = b2) or (b1=b2))

147 U: employ NormalForm(b1);

Case zero: Prop(zero) proven.

Case one: Prop(one) remains to be shown.

(one:)

all b2 ((zero = b2) or (one = b2))

148 U: employ NormalForm(b2);

Case zero: Prop(zero) proven.

Case one: Prop(one) proven.

TRUE

Going to leaf one:..

all b1, b2 ((one = b1) or (one = b2) or (b1=b2))

149 U: employ NormalForm(b1);  
 Case zero: Prop(zero) remains to be shown.  
 Case one: Prop(one) proven.  
 (zero:  
 all b2 ((one = b2) or (zero = b2))  
 150 U: employ NormalForm(b2);  
 Case zero: Prop(zero) proven.  
 Case one: Prop(one) proven.  
 BiValued proved.  
 LastEq proved.  
 TRUE  
 There's more than one unproven ancestor. You may pick one of NcUnique,  
 BoundedBy1, IssLenEq, SameLastBit2, or LastSeq.  
 151 U: try IssLenEq;  
 IssLenEq is untried.  
 all m1, m2 (m1 iss m2 and (Length(m1) = Length(m2)) eqv m1=m2)  
 152 U: employ Induction(m2);  
 Case NewSequenceOfElemType: Prop(NewSequenceOfElemType) remains to be shown.  
 Case apr: all ss, ii (IH(ss) imp Prop(ss apr ii)) remains to be shown.  
 (NewSequenceOfElemType:  
 all m1 (m1 = NewSequenceOfElemType imp Length(m1) = 0)  
 153 U: replace;  
 TRUE  
 Going to leaf apr.:  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq})  
 imp (m1 = NewSequenceOfElemType) or m1 iss ss\$\$  
 or (LessLast(m1) = ss\$\$) and (Last(m1) = ii\$\$)  
 and Length(m1) = Length(ss\$\$) + 1  
 eqv m1 = ss\$\$ apr ii\$\$)  
 154 U: replace;  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq})  
 and m1 ~= ss\$\$ apr ii\$\$  
 and (m1 = NewSequenceOfElemType) or m1 iss ss\$\$  
 or LessLast(m1) = ss\$\$  
 and Last(m1) = ii\$\$  
 imp Length(m1) ~= Length(ss\$\$) + 1)  
 155 U: split;  
 (first:  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq})

and m1 ~ ss\$\$ apr ii\$\$  
 and m1 = NewSequenceOfElemType  
 imp Length(m1) ~ Length(ss\$\$) + 1  
 156 U: replace;  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq}) and (m1 = NewSequenceOfElemType)  
 imp 0 ~ Length(ss\$\$) + 1  
 157 U: apply LenNonneg, Length(m) >= 0;  
 some m (0 <= Length(m))  
 Automatically search for instantiation? yes [confirm]  
 Unsuccessful.  
 158 U: put m=ss\$\$;  
 TRUE  
 Going to leaf second:  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq})  
 and m1 ~ ss\$\$ apr ii\$\$  
 and m1 ~ NewSequenceOfElemType  
 and m1 iss ss\$\$  
 or LessLast(m1) = ss\$\$  
 and Last(m1) = ii\$\$  
 imp Length(m1) ~ Length(ss\$\$) + 1  
 159 U: split;  
 (first:  
 all ss\$\$, ii\$\$, m1  
 ( IH(ss\$\$, 14 {IssLenEq})  
 and m1 ~ ss\$\$ apr ii\$\$  
 and m1 ~ NewSequenceOfElemType  
 and m1 iss ss\$\$  
 imp Length(m1) ~ Length(ss\$\$) + 1  
 160 U: apply IssLenLe;  
 some m1', m2 (m1' iss m2 imp Length(m1') <= Length(m2))  
 Automatically search for instantiation? no [confirm]  
 161 U: put m1'=m1, m2=ss\$\$;  
 all ss\$\$, ii\$\$, m1  
 ( m1 iss ss\$\$ and (Length(m1) <= Length(ss\$\$))  
 and IH(ss\$\$, 14 {IssLenEq})  
 imp m1 = ss\$\$ apr ii\$\$  
 or m1 = NewSequenceOfElemType  
 or Length(m1) ~ Length(ss\$\$) + 1  
 162 U: apply IntFact1, k1 <= k2 imp k1 ~ k2 + 1;  
 some k1, k2 (k1 <= k2 imp k1 ~ k2+1)

Automatically search for instantiation? yes [confirm]

1/1: ( $k_2 = \text{Length}(ss\$\$)$ ) and ( $k_1 = \text{Length}(m_1)$ )

Proved by chaining and narrowing

using the substitution

( $k_2 = \text{Length}(ss\$\$)$ ) and ( $k_1 = \text{Length}(m_1)$ )

TRUE

163 U: next;

Going to leaf second::

all  $ss\$\$, ii\$\$, m_1$

(  $\text{IH}(ss\$\$, 14 \{\text{IssLenEq}\})$  )

and  $m_1 \sim= ss\$\$ \text{ apr } ii\$\$$

and  $m_1 \sim= \text{NewSequenceOfElemType}$

and  $\sim(m_1 \text{ iss } ss\$\$)$

and  $\text{LessLast}(m_1) = ss\$\$$

and  $\text{Last}(m_1) = ii\$\$$

imp  $\text{Length}(m_1) \sim= \text{Length}(ss\$\$) + 1$

164 U: employ NormalForm( $m_1$ );

Case  $\text{NewSequenceOfElemType}$ :  $\text{Prop}(\text{NewSequenceOfElemType})$  proven.

Case  $\text{apr}$ : all  $ss, ii$  ( $\text{Prop}(ss \text{ apr } ii)$ ) proven.

$\text{IssLenEq}$  is awaiting the proof of lemmas  $\text{LenNonneg}$ ,  $\text{IssLenLe}$ , and  $\text{IntFact1}$ .

TRUE

Going to lemma  $\text{IssLenLe}$ .

$\text{IssLenLe}$  is untried.

all  $m_1, m_2$  ( $m_1 \text{ iss } m_2 \text{ imp } \text{Length}(m_1) \leq \text{Length}(m_2)$ )

165 U: employ Induction( $m_2$ );

Case  $\text{NewSequenceOfElemType}$ :  $\text{Prop}(\text{NewSequenceOfElemType})$  remains to be shown.

Case  $\text{apr}$ : all  $ss, ii$  ( $\text{IH}(ss) \text{ imp } \text{Prop}(ss \text{ apr } ii)$ ) remains to be shown.

( $\text{NewSequenceOfElemType}$ :

all  $m_1$  ( $m_1 = \text{NewSequenceOfElemType} \text{ imp } \text{Length}(m_1) \leq 0$ )

166 U: replace;

TRUE

Going to leaf  $\text{apr}::$

all  $ss\$\$, ii\$\$, m_1$

(  $\text{IH}(ss\$\$, 15 \{\text{IssLenLe}\})$  )

and ( $m_1 = \text{NewSequenceOfElemType}$ ) or  $m_1 \text{ iss } ss\$\$$

or ( $\text{LessLast}(m_1) = ss\$\$$ ) and ( $\text{Last}(m_1) = ii\$\$$ )

imp  $\text{Length}(m_1) \leq \text{Length}(ss\$\$) + 1$

167 U: suppose  $m_1 = \text{NewSequenceOfElemType}$  or  $m_1 \text{ iss } ss\$\$$ ;

(yes:)

all  $ss\$\$, ii\$\$, m_1$

( ( $m_1 = \text{NewSequenceOfElemType}$ ) or  $m_1 \text{ iss } ss\$\$$  )

and  $\text{IH}(ss\$\$, 15 \{\text{IssLenLe}\})$

```

imp Length(m1) <= Length(ss$$) + 1
168 U: augment m1 iss ss$$;
(main:)
all ss$$, ii$$, m1
( m1 iss ss$$ and IH(ss$$, 15 {IssLenLe})
imp Length(m1) <= Length(ss$$) + 1
169 U: invoke IH;
Automatically search for instantiation? yes [confirm]
1/1: m1' = m1
Unsuccessful.
all ss$$, ii$$, m1 (some m1'
( m1 iss ss$$
and m1' iss ss$$ imp Length(m1') <= Length(ss$$)
imp Length(m1) <= Length(ss$$) + 1))
170 U: put m1'=m1;
all ss$$, ii$$, m1
( m1 iss ss$$ and (Length(m1) <= Length(ss$$))
imp Length(m1) <= Length(ss$$) + 1)
171 U: apply IntFact2, k1 <= k2 imp k1 <= k2 + 1;
some k1, k2 (k1 <= k2 imp k1 <= k2+1)
Automatically search for instantiation? yes [confirm]
1/2: (k2 = Length(ss$$)) and (k1 = Length(m1))
Proved by chaining and narrowing
using the substitution
(k2 = Length(ss$$)) and (k1 = Length(m1))
TRUE
172 U: next;
Going to leaf thesis:.
all ss$$, ii$$, m1
( (m1 = NewSequenceOfElemType) and IH(ss$$, 15 {IssLenLe})
imp m1 iss ss$$)
173 U: replace;
TRUE
Going to leaf no:.
all ss$$, ii$$, m1
( (m1 ~= NewSequenceOfElemType) and ~(m1 iss ss$$)
and IH(ss$$, 15 {IssLenLe}))
and LessLast(m1) = ss$$
and Last(m1) = ii$$
imp Length(m1) <= Length(ss$$) + 1
174 U: employ NormalForm(m1);
Case NewSequenceOfElemType: Prop(NewSequenceOfElemType) proven.

```

Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.

(apr:)

all ss\$\$, ii\$\$, ss\$\$', ii\$\$'  
 $(\sim((ss\$ apr ii\$) iss ss\$'))$  and  $IH(ss\$', 15 \{IssLenLe\})$

and  $ss\$ = ss\$'$   
 and  $ii\$ = ii\$'$   
 $\text{imp Length}(ss\$) \leq \text{Length}(ss\$')$

175 U: repace;

what? Please correct repace using the list: readp or replace.  
 Please correct repace: replace [confirm]

;

$\text{IssLenLe}$  is awaiting the proof of lemma IntFact2.

TRUE

Going to lemma IntFact2.

IntFact2 is untried.

IntFact2 proved.

$\text{IssLenLe}$  proved.

TRUE

There's more than one unproven ancestor. You may pick one of LenNonneg or IntFact1.

176 U: try IntFact1;

IntFact1 is untried.

IntFact1 proved.

TRUE

Going to unproven ancestor LenNonneg.

LenNonneg is untried.

all m ( $0 \leq \text{Length}(m)$ )

177 U: annotate Proved in Affirm type library. ;

178 U: assume LenNonneg;

$\text{IssLenEq}$  proved.

179 U: next;

There's more than one unproven ancestor. You may pick one of NcUnique or BoundedBy1.

180 U: try ncunique;  
 $(ncunique \Rightarrow NcUnique)$

NcUnique is untried.

all s ( $\text{Nchanges}(\text{Seqnums}(s)) = \text{Length}(\text{UniqueMsg}(s))$ )

181 U: employ Induction(s);

Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) proven.

Case apr: all ss, ii ( $IH(ss)$  imp Prop(ss apr ii)) remains to be shown.

(apr:)

all ss', ii'

$(IH(ss', 10 \{NcUnique\}))$   
 imp if  $\text{LastBit}(\text{Seqnums}(ss')) = \text{seqno}(ii')$   
 then  $\text{Nchanges}(\text{Seqnums}(ss')) = \text{Length}(\text{UniqueMsg}(ss'))$   
 else  $\text{Nchanges}(\text{Seqnums}(ss')) + 1 = \text{Length}(\text{UniqueMsg}(ss')) + 1$   
 182 U: invoke IH;  
 NcUnique proved.  
 TRUE  
 Going to unproven ancestor BoundedBy1.  
 BoundedBy1 is untried.  
 all k1, k2  
 $(\text{Bounded}(k1, k2, 1))$   
 $\text{eqv } (k1=k2) \text{ or } (k1 < k2) \text{ and } (k1+1 = k2)$   
 183 U: invoke Bounded;  
 BoundedBy1 proved.  
 UniqueEq proved.  
 TRUE  
 There's more than one unproven ancestor. You may pick one of SameLastBit2  
 or LastSeq.  
 184 U: try SameLastBit2;  
 SameLastBit2 is untried.  
 all s1, s2, p  
 $(s1 \text{ subseq } s2 \text{ and } (p = \text{Last}(s2)))$   
 imp  $(s1 \text{ apr } p) \text{ subseq } s2 \text{ or } (\text{LastBit}(\text{Seqnums}(s1)) = \text{LastBit}(\text{Seqnums}(s2)))$   
 185 U: employ NormalForm(s2);  
 Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) remains to be shown.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (NewSequenceOfPacket:)  
 all s1, p  
 $((s1 = \text{NewSequenceOfPacket}) \text{ and } (p = \text{Last}(\text{NewSequenceOfPacket})))$   
 imp  $\text{LastBit}(\text{Seqnums}(s1)) = \text{zero}$   
 186 U: replace;  
 TRUE  
 Going to leaf apr:.  
 all ss', ii', s1, p  
 (if  $s1 = \text{NewSequenceOfPacket}$   
 then  $p=ii'$   
 imp  $(s1 \text{ apr } p) \text{ subseq } ss' \text{ or } s1 \text{ subseq } ss'$   
 or  $\text{LastBit}(\text{Seqnums}(s1)) = \text{seqno}(ii')$   
 else  $\sim(s1 \text{ subseq } ss') \text{ and } \text{LessLast}(s1) \text{ subseq } ss'$   
 and  $\text{Last}(s1) = ii'$   
 and  $p=ii'$   
 imp  $(s1 \text{ apr } p) \text{ subseq } ss' \text{ or } (\text{LastBit}(\text{Seqnums}(s1)) = \text{seqno}(ii'))$

187 U: employ NormalForm(s1);  
 Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) remains to be shown.  
 (apr:  
 all ss', ii', ss, ii, p  
 ( ~((ss' apr ii') subseq ss) and ss' subseq ss  
 and ii'=ii  
 and p=ii  
 imp ((ss' apr ii') apr p) subseq ss or (seqno(ii') = seqno(ii)))  
 188 U: replace;  
 SameLastBit2 proved.  
 TRUE  
 Going to unproven ancestor LastSeq.  
 LastSeq is untried.  
 all s ((s = NewSequenceOfPacket) or (seqno(Last(s)) = LastBit(Seqnums(s))))  
 189 U: employ NormalForm(s);  
 (employ => employ)  
 Case NewSequenceOfPacket: Prop(NewSequenceOfPacket) proven.  
 Case apr: all ss, ii (Prop(ss apr ii)) proven.  
 LastSeq proved.  
 SubToLag proved.  
 TRUE  
 The proof of this part is finished.  
 190 U: print status;  
 No theorems are untried.  
 No theorems are tried.  
 The assumed theorem is LenNonneg.  
 No theorems are awaiting lemma proof.  
 The proved theorems are BitSubBound, BiValued, BoundedBy1, IntFact1, IntFact2,  
 IssLenEq, IssLenLe, LastEq, LastSeq, NcNonneg, NcUnique, PktSubBound,  
 SameLastBit, SameLastBit2, SubLess, SubSeqnum, SubToLag, and UniqueEq.  
 191 U: quit;  
 Automatically summarize the proof attempts? yes [confirm]  
 theorem LastSeq, s ~ NewSequenceOfPacket  
 imp seqno(Last(s)) = LastBit(Seqnums(s));  
 proof tree:  
 189:! LastSeq  
 employ NormalForm(s) {proved by Divito using AFFIRM 120 on  
 12-Feb-81 in transcript  
 <DIVITO>AFFLOG.12-FEB-81.1}  
 -> NewSequenceOfPacket:  
 Immediate

-> apr:

Immediate

theorem SameLastBit2, s1 subseq s2  
and p = Last(s2)  
and ~((s1 apr p) subseq s2)  
imp LastBit(Seqnums(s1)) = LastBit(Seqnums(s2));  
proof tree:  
185:! SameLastBit2  
employ NormalForm(s2) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}  
186: NewSequenceOfPacket:  
209 replace  
-> (proven!)  
187: apr:  
210 employ NormalForm(s1)  
-> NewSequenceOfPacket:  
Immediate  
188: apr:  
211 replace  
-> (proven!)  
theorem BoundedBy1, Bounded(k1, k2, 1)  
eqv (k1=k2) or (k1+1 = k2);  
proof tree:  
182:! BoundedBy1  
normint {proved by Divito using AFFIRM 120 on 12-Feb-81 in  
transcript <DIVITO>AFFLOG.12-FEB-81.1}  
183: 207 invoke Bounded  
183: 208 normint  
-> (proven!)  
theorem NcUnique, Nchanges(Seqnums(s)) = Length(UniqueMsg(s));  
proof tree:  
181:! NcUnique  
employ Induction(s) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}  
-> NewSequenceOfPacket:  
Immediate  
181: apr:  
204 cases  
182: 205 invoke IH  
182: 206 normint

-> (proven!)

theorem LenNonneg, Length(m) >= 0;

theorem IntFact1, k1 <= k2 imp k1 ~ k2+1;

proof tree:

176:! IntFact1

normint {proved by Divito using AFFIRM 120 on 12-Feb-81 in transcript <DIVITO>AFFLOG.12-FEB-81.1}

-> (proven!)

theorem IntFact2, k1 <= k2 imp k1 <= k2+1;

proof tree:

175:! IntFact2

normint {proved by Divito using AFFIRM 120 on 12-Feb-81 in transcript <DIVITO>AFFLOG.12-FEB-81.1}

-> (proven!)

theorem IssLenLe, m1 iss m2 imp Length(m1) <= Length(m2);  
 IssLenLe uses IntFact2!.

proof tree:

165:! IssLenLe

employ Induction(m2) {proved by Divito using AFFIRM 120 on 12-Feb-81 in transcript <DIVITO>AFFLOG.12-FEB-81.1}

166: NewSequenceOfElemType:

192 replace

-> (proven!)

167: apr:

193 suppose m1 = NewSequenceOfElemType  
 or m1 iss ss\$\$

168: yes:

194 augment m1 iss ss\$\$

169: main:

196 invoke IH

170: 198 put m1'=m1

171: 199 apply IntFact2

171: 201 put k2 = Length(ss\$\$)  
 and k1 = Length(m1) {search}

171: (proven!)

173: thesis:{IssLenLe, apr:, yes:}

197 replace

-> (proven!)

174: no:{IssLenLe, apr:}

195 employ NormalForm(m1)

-> NewSequenceOfElemType:

Immediate

175: apr:

203 replace

-> (proven!)

theorem IssLenEq, m1 iss m2 and (Length(m1) = Length(m2))

eqv m1=m2;

IssLenEq uses LenNonneg%, IssLenLe!, and IntFact1!.

proof tree:

152:! IssLenEq

employ Induction(m2) {proved by Divito using AFFIRM 120 on

12-Feb-81 in transcript

<DIVITO>AFFLOG.12-FEB-81.1}

153: NewSequenceOfElemType:

176 replace

-> (proven!)

154: apr:

177 replace

155: 178 split

156: first:

179 replace

157: 181 apply LenNonneg

158: 183 put m=ss\$\$

158: 184 normint

-> (proven!)

159: second:{IssLenEq, apr:}

180 split

160: first:

185 apply IssLenLe

161: 187 put (m1'=m1) and (m2=ss\$\$)

162: 188 apply IntFact1

162: 190 put k2 = Length(ss\$\$)

and k1 = Length(m1) {search}

162: (proven!)

164: second:{IssLenEq, apr:, second:}

186 employ NormalForm(m1)

-> NewSequenceOfElemType:

Immediate

-> apr:

Immediate

theorem BiValued, (b ~ b1) and (b ~ b2)

imp b1=b2;

proof tree:

146:! BiValued  
employ NormalForm(b) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}

147: zero:  
172 employ NormalForm(b1)

-> zero:

Immediate

148: one:  
174 employ NormalForm(b2)

-> zero:

Immediate

-> one:

Immediate

149: one:{BiValued}  
173 employ NormalForm(b1)

150: zero:

175 employ NormalForm(b2)

-> zero:

Immediate

-> one:

Immediate

-> one:

Immediate

theorem BitSubBound, n1 subseq n2

and Bounded(Nchanges(n1),

Nchanges(n2) + 1, 1)

imp Bounded(Nchanges(n1), Nchanges(n2), 1)

and Nchanges(n1) = Nchanges(n2);

BitSubBound uses SubLess!.

proof tree:

143:! BitSubBound

apply SubLess {proved by Divito using AFFIRM 120 on 12-Feb-81  
in transcript <DIVITO>AFFLOG.12-FEB-81.1}

144: 169 put (n1'=n1) and (n2'=n2)

145: 170 invoke Bounded | all |

145: 171 normint

-> (proven!)

theorem LastEq, n1 subseq n2

and Bounded(Nchanges(n1), Nchanges(n2), 1)

imp LastBit(n1) = LastBit(n2) eqv Nchanges(n1) = Nchanges(n2);

LastEq uses SameLastBit!, BitSubBound!, and BiValued!.

proof tree:

104:! LastEq  
employ Induction(n2) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}

105: NewSequenceOfBit:  
122 replace  
-> (proven!)  
105: apr:  
123 cases  
106: 124 suppose LastBit(ss\$) = ii\$  
107: yes:  
125 replace ii\$  
108: 127 suppose n1 = NewSequenceOfBit  
or n1 subseq ss\$  
109: yes:  
128 augment n1 subseq ss\$  
110: main:  
130 invoke IH  
110: 132 put n1' = n1 {search}  
110: (proven!)  
111: thesis:  
131 replace n1  
-> (proven!)  
112: no:{LastEq, apr:, yes:}  
129 employ NormalForm(n1)  
-> NewSequenceOfBit:  
Immediate  
112: apr:  
134 cases  
113: 135 split  
116: first:  
136 replace ii\$  
117: 138 invoke IH  
117: 139 put n1 = ss\$ {search}  
117: (proven!)  
118: second:{LastEq, apr:, yes:, no:, apr:}  
137 replace ii\$  
119: 141 apply SameLastBit  
119: 142 put n2 = ss\$'  
and n1 = ss\$  
and b = LastBit(ss\$') {search}

119: (proven!)

122: no:{LastEq, apr:}

126 suppose n1 = NewSequenceOfBit  
or n1 subseq ss\$

123: yes:

144 augment n1 subseq ss\$

124: main:

146 apply BitSubBound

125: 148 put (n1'=n1) and (n2=ss\$)

125: 149 normint

126: 150 invoke IH

127: 151 put n1'=n1

128: 152 replace

-> (proven!)

129: thesis:{LastEq, apr:, no:, yes:}

147 replace n1

-> (proven!)

130: no:{LastEq, apr:, no:}

145 employ NormalForm(n1)

-> NewSequenceOfBit:

Immediate

130: apr:

153 cases

131: 154 replace ii\$'

132: 155 split

133: first:

156 swap | all |

134: 158 replace

135: 159 apply BitSubBound

136: 160 put (n1=ss\$) and (n2=ss\$')

136: 161 normint

137: 162 invoke IH

137: 163 put n1 = ss\$ {search}

137: (proven!)

138: second:{LastEq, apr:, no:, no:, apr:}

157 apply BiValued

139: 165 put b=ii\$  
and b1 = LastBit(ss\$)  
and b2 = LastBit(ss\$')

140: 166 invoke IH

141: 167 put n1 = ss\$ {choose}

141: 168 normint

-> (proven!)

theorem UniqueEq, UniqueMsg(s1) iss UniqueMsg(s2)  
and s1 subseq s2  
and Bounded(Nchanges(Seqnums(s1)),  
Nchanges(Seqnums(s2)), 1)  
and LastBit(Seqnums(s1)) = LastBit(Seqnums(s2))  
imp UniqueMsg(s1) = UniqueMsg(s2);  
UniqueEq uses BoundedBy1!, NcUnique!, IssLenEq!, SubSeqnum!, and LastEq!.

proof tree:

89!: UniqueEq  
apply BoundedBy1 {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}

90: 107 put k2 = Nchanges(Seqnums(s2))  
and k1 = Nchanges(Seqnums(s1)) {choose}

90: 108 normint

91: 109 split

92: first:  
110 apply NcUnique

93: 112 apply NcUnique

94: 113 put (s=s1) and (s'=s2)

95: 114 replace

96: 115 apply IssLenEq

96: 116 put (m2 = UniqueMsg(s2)) and (m1 = UniqueMsg(s1)) {search}

96: (proven!)

98: second:{UniqueEq}

111 apply SubSeqnum

99: 118 put (s1'=s1) and (s2'=s2)

100: 119 apply LastEq

100: 120 put (n2 = Seqnums(s2)) and (n1 = Seqnums(s1)) {search}

100: (proven!)

theorem SubSeqnum, s1 subseq s2 imp Seqnums(s1) subseq Seqnums(s2);

proof tree:

78!: SubSeqnum  
employ Induction(s2) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}

79: NewSequenceOfPacket:

95 replace  
-> (proven!)

80: apr:

96 split

81: first:  
97 replace  
-> (proven!)  
82: second:  
98 split  
83: first:  
99 invoke IH  
83: 101 put  $s_1' = s_1$  {search}  
83: (proven!)  
84: second:  
100 employ NormalForm( $s_1$ )  
-> NewSequenceOfPacket:  
Immediate  
85: apr:  
103 replace  
86: 104 invoke IH  
86: 105 put  $s_1 = ss'$  {search}  
86: (proven!)  
theorem NcNonneg, Nchanges(n)  $\geq 0$ ;  
proof tree:  
76!: NcNonneg  
employ Induction(n) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}  
-> NewSequenceOfBit:  
Immediate  
76: apr:  
92 cases  
77: 93 invoke IH  
77: 94 normint  
-> (proven!)  
theorem SameLastBit,  $n_1 \text{ subseq } n_2$   
and  $b = \text{LastBit}(n_2)$   
and  $\sim((n_1 \text{ apr } b) \text{ subseq } n_2)$   
imp  $\text{LastBit}(n_1) = \text{LastBit}(n_2)$ ;  
proof tree:  
73!: SameLastBit  
employ NormalForm( $n_2$ ) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}  
74: NewSequenceOfBit:  
90 replace

-> (proven!)

75: apr:

91 employ NormalForm(n1)

-> NewSequenceOfBit:

Immediate

-> apr:

Immediate

theorem SubLess, n1 subseq n2 imp Nchanges(n1) <= Nchanges(n2);  
SubLess uses NcNonneg! and SameLastBit!.

proof tree:

57!: SubLess

employ Induction(n2) {proved by Divito using AFFIRM 120 on  
12-Feb-81 in transcript  
<DIVITO>AFFLOG.12-FEB-81.1}

58: NewSequenceOfBit:

70 replace

-> (proven!)

58: apr:

71 cases

59: 72 split

60: first:

73 apply NcNonneg

61: 75 put n=ss\$

62: 76 replace

62: 77 normint

-> (proven!)

63: second:{SubLess, apr:}

74 split

64: first:

78 invoke IH

65: 80 put n1'=n1

65: 81 normint

-> (proven!)

66: second:{SubLess, apr:, second:}

79 employ NormalForm(n1)

-> NewSequenceOfBit:

Immediate

66: apr:

82 cases

67: 83 invoke IH

68: 84 put n1=ss\$

68: 85 normint

69: 86 replace  
 70: 87 apply SameLastBit  
 71: 88 put n2 = ss\$'  
 and b = ii\$'  
 and n1 = ss\$ {choose}  
 72: 89 replace  
 -> (proven!)

theorem PktSubBound, s1 subseq s2  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)) + 1, 1)  
 imp Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)), 1)  
 and Nchanges(Seqnums(s1)) = Nchanges(Seqnums(s2));  
 PktSubBound uses SubSeqnum! and SubLess!.

proof tree:

52!: PktSubBound  
 apply SubSeqnum {proved by Divito using AFFIRM 120 on 12-Feb-81  
 in transcript <DIVITO>AFFLOG.12-FEB-81.1}

53: 64 put (s1'=s1) and (s2'=s2)  
 54: 65 invoke Bounded | all |  
 54: 66 normint  
 55: 67 apply SubLess  
 55: 68 put (n2 = Seqnums(s2)) and (n1 = Seqnums(s1)) {search}  
 55: (proven!)

theorem SubToLag, s1 subseq s2  
 and Repeats(s2)  
 and Bounded(Nchanges(Seqnums(s1)),  
 Nchanges(Seqnums(s2)), 1)  
 imp UniqueMsg(s1) iss UniqueMsg(s2);  
 SubToLag uses LastSeq!, SameLastBit2!, PktSubBound!, BiValued!, and UniqueEq!.

proof tree:

12!: SubToLag  
 employ Induction(s2) {proved by Divito using AFFIRM 120 on  
 12-Feb-81 in transcript  
 <DIVITO>AFFLOG.12-FEB-81.1}

13: NewSequenceOfPacket:  
 17 replace  
 -> (proven!)

13: apr:  
 18 cases  
 14: 19 split  
 15: first:

20 replace  
 -> (proven!)  
 16: second:  
 21 suppose  $\text{LastBit}(\text{Seqnums}(ss')) = \text{seqno}(ii')$   
 17: yes:  
 22 split  
 18: first:  
 24 invoke IH  
 18: 26 put  $s1' = s1$  {search}  
 18: (proven!)  
 19: second:  
 25 employ NormalForm( $s1$ )  
 -> NewSequenceOfPacket:  
 Immediate  
 19: apr:  
 28 cases  
 22: 29 suppose  $\text{LastBit}(\text{Seqnums}(ss')) = \text{seqno}(ii')$   
 23: yes:  
 30 invoke IH  
 23: 32 put  $s1 = ss'$  {search}  
 23: (proven!)  
 24: no:31 replace  $ii'$   
 25: 34 apply LastSeq  
 26: 35 put  $s=ss$   
 27: 36 split  
 28: first:  
 37 replace  $ss$   
 29: 39 replace  $ss'$   
 -> (proven!)  
 30: second:  
 38 replace  $\text{seqno}(ii)$   
 31: 40 apply SameLastBit2  
 31: 41 put  $s2 = ss$   
 and  $s1 = ss'$   
 and  $p = ii$  {search}  
 31: (proven!)  
 33: no:{SubToLag, apr:, second:}  
 23 split  
 34: first:  
 43 apply PktSubBound  
 35: 45 put ( $s1'=s1$ ) and ( $s2=ss'$ )

36: 46 invoke IH  
 36: 47 put  $s_1' = s_1$  {search}  
 36: (proven!)  
 37: second:{SubToLag, apr:, second:, no:}  
 44 employ NormalForm( $s_1$ )  
 -> NewSequenceOfPacket:  
 Immediate  
 37: apr:  
 49 cases  
 38: 50 suppose LastBit(Seqnums( $ss'$ ))  
 = seqno(ii')  
 39: yes:  
 51 apply PktSubBound  
 40: 53 put ( $s_1=ss'$ ) and ( $s_2=ss$ )  
 41: 54 invoke IH  
 41: 55 put  $s_1 = ss'$  {search}  
 41: (proven!)  
 42: no:{SubToLag, apr:, second:, no:, second:, apr:}  
 52 replace  
 43: 57 apply BiValued  
 44: 58 put  $b = \text{seqno}(ii)$   
 and  $b_1 = \text{LastBit}(\text{Seqnums}(ss'))$   
 and  $b_2 = \text{LastBit}(\text{Seqnums}(ss))$   
 45: 59 apply UniqueEq  
 46: 60 put ( $s_1=ss'$ ) and ( $s_2=ss$ )  
 47: 61 invoke IH  
 47: 62 put  $s_1 = ss'$  {search}  
 47: (proven!)  
 Type CONTINUE to return to AFFIRM.  
 192 U: print uses;  
 Theorem Uses: Used by:  
 LastSeq, proved - SubToLag  
 SameLastBit2, proved - SubToLag  
 BoundedBy1, proved - UniqueEq  
 NcUnique, proved - UniqueEq  
 LenNonneg, assumed - IssLenEq  
 IntFact1, proved - IssLenEq  
 IntFact2, proved - IssLenLe  
 IssLenLe, proved IntFact2 IssLenEq  
 IssLenEq, proved LenNonneg UniqueEq  
 IssLenLe  
 IntFact1

BiValued, proved - LastEq  
SubToLag  
BitSubBound, proved SubLess LastEq  
LastEq, proved SameLastBit UniqueEq  
BitSubBound  
BiValued  
UniqueEq, proved BoundedBy1 SubToLag  
NcUnique  
IssLenEq  
SubSeqnum  
LastEq  
SubSeqnum, proved - UniqueEq  
PktSubBound  
NcNonneg, proved - SubLess  
SameLastBit, proved - LastEq  
SubLess  
SubLess, proved NcNonneg BitSubBound  
SameLastBit PktSubBound  
PktSubBound, proved SubSeqnum SubToLag  
SubLess  
SubToLag, proved LastSeq -  
SameLastBit2  
PktSubBound  
BiValued  
UniqueEq  
193 U: print assumptions;  
LenNonneg is used by IssLenEq.  
assume LenNonneg, Length(m) >= 0;  
194 U: quit;  
Automatically summarize the proof attempts? no [confirm]  
Type CONTINUE to return to AFFIRM.