

EVENT: Start with the library "c4".

```
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;;                                %Mapping Call Parameters                ;;
;;
;;
;;
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
```

DEFINITION:

```
mg-to-p-local-values (locals)
=  if locals  $\simeq$  nil then nil
    elseif simple-mg-type-refp (cadr (car (locals)))
    then cons (mg-to-p-simple-literal (caddr (car (locals))),
              mg-to-p-local-values (cdr (locals)))
    else append (mg-to-p-simple-literal-list (caddr (car (locals))),
                mg-to-p-local-values (cdr (locals))) endif
```

THEOREM: mg-to-p-local-values-plistp
plistp (mg-to-p-local-values (*lst*))

```
;; Given a list of formals with the call site actuals, this gives the list for the new stack
;; frame. Each of the actuals is guaranteed to be an identifier and each of these is in
;; the previous frame with the address of the value in my-stack. Thus, I need only copy
;; these addresses into the current frame.
```

DEFINITION:

```
map-call-formals (formals, actuals, bindings)
=  if formals  $\simeq$  nil then nil
    else cons (cons (car (car (formals)),
                    cdr (assoc (car (actuals), bindings))),
              map-call-formals (cdr (formals), cdr (actuals), bindings)) endif
```

THEOREM: length-map-call-formals
length (map-call-formals (*formals*, *actuals*, *bindings*)) = length (*formals*)

THEOREM: map-call-formals-plistp
plistp (map-call-formals (*x*, *y*, *z*))

THEOREM: listcars-map-call-formals
listcars (map-call-formals (*formals*, *actuals*, *bindings*)) = listcars (*formals*)

```
;; Each of the local values is placed onto the temp-stk, then the indexes into
;; the stack are placed there as well. The distance of the value from the index
```

;; depends on the size of the elements between.

;; The initial value of n is (length temp-stk)

DEFINITION:

```
map-call-locals (locals, n)
=  if locals  $\simeq$  nil then nil
    elseif simple-mg-type-refp (cadr (car (locals)))
    then cons (cons (car (car (locals)), tag ('nat, n)),
                map-call-locals (cdr (locals), 1 + n))
    else cons (cons (car (car (locals)), tag ('nat, n)),
                map-call-locals (cdr (locals),
                                array-length (cadr (car (locals)))
                                + n)) endif
```

THEOREM: length-map-call-locals

length (map-call-locals (locals, n)) = length (locals)

THEOREM: map-call-locals-plistp

plistp (map-call-locals (locals, n))

THEOREM: map-call-locals-preserves-listcars

listcars (map-call-locals (locals, m)) = listcars (locals)

;; The topmost frame on the ctrl-stk at the beginning of the body of the proc-call
;; contains the p-formals which represent both the formals and locals of the mg
;; subroutine. The formals have the values of the actuals in the previous frame
;; and these are guaranteed to be addresses into the temp-stk. The locals have been
;; placed on the temp-stk as well and the address computed for this frame are those
;; locations. Thus, upon entry the following invariant is established: every local
;; (in the frame) contains an index into the temp-stk which contains the corresponding
;; value.

DEFINITION:

```
make-frame-alist (def, stmt, ctrl-stk, temp-stk)
=  append (map-call-locals (def-locals (def), length (temp-stk)),
          map-call-formals (def-formals (def),
                          call-actuals (stmt),
                          bindings (top (ctrl-stk))))
```

DEFINITION:

```
mg-actuals-to-p-actuals (mg-actuals, bindings)
=  if mg-actuals  $\simeq$  nil then nil
    else cons (cdr (assoc (car (mg-actuals), bindings)),
              mg-actuals-to-p-actuals (cdr (mg-actuals), bindings)) endif
```

THEOREM: length-mg-actuals-to-p-actuals
length (mg-actuals-to-p-actuals (*mg-actuals*, *bindings*)) = length (*mg-actuals*)

THEOREM: mg-actuals-to-p-actuals-plistp
plistp (mg-actuals-to-p-actuals (*actuals*, *bindings*))

```
;; %mapping call parameters
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;;                                     THE TRANSLATOR
;;
;;                                     ;
;;                                     ;
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
```

EVENT: Add the shell *make-cinfo*, with recognizer function symbol *cinfo* and 3 accessors: *code*, with type restriction (none-of) and default value zero; *label-alist*, with type restriction (none-of) and default value zero; *label-cnt*, with type restriction (one-of numberp) and default value zero.

DEFINITION:
nullify (*cinfo*) = make-cinfo (**nil**, label-alist (*cinfo*), label-cnt (*cinfo*))

DEFINITION:
add-code (*cinfo*, *code*)
= make-cinfo (append (code (*cinfo*), *code*),
label-alist (*cinfo*),
label-cnt (*cinfo*))

DEFINITION:
discard-label (*cinfo*)
= make-cinfo (code (*cinfo*), cdr (label-alist (*cinfo*)), label-cnt (*cinfo*))

DEFINITION:
set-label-alist (*cinfo*, *new-label-alist*)
= make-cinfo (code (*cinfo*), *new-label-alist*, label-cnt (*cinfo*))

;; Notice that I could simply use the VALUE function directly.

DEFINITION:
fetch-label (*condition*, *label-alist*) = cdr (assoc (*condition*, *label-alist*))

;; If this definition stays unchanged, I can eliminate it entirely in favor of the
;; simpler hyp on code.

DEFINITION: $\text{ok-cinfo}(cinfo) = \text{plistp}(\text{code}(cinfo))$

;; Given a list (x1 ... xn) and a label l, this generated the list
 ;; ((x1 . l) (x2 . l) ... (xn . l)). Notice that this allows that use
 ;; of the VALUE function for accessing the label.

DEFINITION:

make-label-alist (name-list, label)
 = **if** name-list \simeq **nil** **then nil**
 else cons (cons (car (name-list), label),
 make-label-alist (cdr (name-list), label)) **endif**

DEFINITION:

push-local-array-values-code (array-value)
 = **if** array-value \simeq **nil** **then nil**
 else cons (list ('push-constant,
 mg-to-p-simple-literal (car (array-value))),
 push-local-array-values-code (cdr (array-value))) **endif**

THEOREM: length-push-local-array-values-code
 $\text{length}(\text{push-local-array-values-code}(\text{array-value})) = \text{length}(\text{array-value})$

THEOREM: length-push-local-array-values-code2
 $(\text{ok-mg-local-data-decl}(\text{local}) \wedge (\neg \text{simple-mg-type-refp}(\text{cadr}(\text{local}))))$
 $\rightarrow (\text{array-length}(\text{cadr}(\text{local})) = \text{length}(\text{caddr}(\text{local})))$

EVENT: Disable length-push-local-array-values-code2.

DEFINITION:

push-locals-values-code (locals)
 = **if** locals \simeq **nil** **then nil**
 elseif simple-mg-type-refp (cadr (car (locals)))
 then cons (list ('push-constant,
 mg-to-p-simple-literal (caddr (car (locals)))),
 push-locals-values-code (cdr (locals)))
 else append (push-local-array-values-code (caddr (car (locals))),
 push-locals-values-code (cdr (locals))) **endif**

THEOREM: length-push-locals-values-code
 $\text{ok-mg-local-data-plistp}(\text{locals})$
 $\rightarrow (\text{length}(\text{push-locals-values-code}(\text{locals})) = \text{data-length}(\text{locals}))$

THEOREM: length-mg-to-p-local-values
 $\text{ok-mg-local-data-plistp}(\text{locals})$
 $\rightarrow (\text{length}(\text{mg-to-p-local-values}(\text{locals})) = \text{data-length}(\text{locals}))$

THEOREM: no-labels-in-push-local-array-values-code
 $\text{find-labelp}(n, \text{push-local-array-values-code}(value)) = \mathbf{f}$

THEOREM: no-labels-in-push-locals-values-code
 $\text{find-labelp}(n, \text{push-locals-values-code}(actuals)) = \mathbf{f}$

DEFINITION:

$\text{push-locals-addresses-code}(locals, n)$
 $=$ **if** $locals \simeq \mathbf{nil}$ **then** \mathbf{nil}
 elseif $\text{simple-mg-type-refp}(\text{cadr}(\text{car}(locals)))$
 then $\text{cons}(\text{list}('push-temp-stk-index, n),$
 $\text{push-locals-addresses-code}(\text{cdr}(locals), n))$
 else $\text{cons}(\text{list}('push-temp-stk-index, n),$
 $\text{push-locals-addresses-code}(\text{cdr}(locals),$
 $1 + (n - \text{array-length}(\text{cadr}(\text{car}(locals))))))$ **endif**

THEOREM: length-push-locals-addresses-code
 $\text{length}(\text{push-locals-addresses-code}(locals, n)) = \text{length}(locals)$

THEOREM: no-labels-in-push-locals-addresses-code
 $\text{find-labelp}(n, \text{push-locals-addresses-code}(actuals, m)) = \mathbf{f}$

DEFINITION:

$\text{push-actuals-code}(actuals)$
 $=$ **if** $actuals \simeq \mathbf{nil}$ **then** \mathbf{nil}
 else $\text{cons}(\text{list}('push-local, \text{car}(actuals)),$
 $\text{push-actuals-code}(\text{cdr}(actuals)))$ **endif**

THEOREM: no-labels-in-push-actuals-code
 $\text{find-labelp}(n, \text{push-actuals-code}(actuals)) = \mathbf{f}$

THEOREM: length-push-actuals-code
 $\text{length}(\text{push-actuals-code}(actuals)) = \text{length}(actuals)$

DEFINITION:

$\text{push-parameters-code}(locals, actuals)$
 $=$ $\text{append}(\text{push-locals-values-code}(locals),$
 $\text{append}(\text{push-locals-addresses-code}(locals,$
 $\text{data-length}(locals) - 1),$
 $\text{push-actuals-code}(actuals)))$

THEOREM: length-push-parameters-code
 $\text{ok-mg-local-data-plistp}(locals)$
 $\rightarrow (\text{length}(\text{push-parameters-code}(locals, actuals))$
 $= (\text{data-length}(locals) + \text{length}(locals) + \text{length}(actuals)))$

```
;; COMPILING THE CONDITION MAPPING
;;
;; Generate the list '(lc lc+1 lc+2 ... lc+n-1). These are the labels
;; necessary for the condition computation jumps.
```

DEFINITION:

```
cond-case-jump-label-list (lc, n)
=  if n  $\simeq$  0 then nil
    else cons (lc, cond-case-jump-label-list (1 + lc, n - 1)) endif
```

THEOREM: length-cond-case-jump-label-list
length (cond-case-jump-label-list (lc, n)) = fix (n)

DEFINITION:

```
index-cond-case-induction-hint (i, j, k)
=  if k  $\simeq$  0 then t
    else index-cond-case-induction-hint (i - 1, 1 + j, k - 1) endif
```

THEOREM: get-cond-case-jump-label-list
((i < k) \wedge (j \in \mathbf{N}))
 \rightarrow (get (i, cond-case-jump-label-list (j, k)) = (i + j))

EVENT: Disable get-cond-case-jump-label-list.

DEFINITION:

```
cond-conversion (actual-conds, lc, cond-list, label-alist)
=  if actual-conds  $\simeq$  nil then nil
    else cons (list ('dl,
                    lc,
                    nil,
                    list ('push-constant,
                        mg-cond-to-p-nat (car (actual-conds),
                                           cond-list))),
              cons ('(pop-global c-c),
                  cons (list ('jump,
                              fetch-label (car (actual-conds),
                                              label-alist)),
                        cond-conversion (cdr (actual-conds),
                                         1 + lc,
                                         cond-list,
                                         label-alist)))))) endif
```

THEOREM: length-cond-conversion
length (cond-conversion (call-conds, lc, cond-list, label-alist))
= (3 * length (call-conds))

DEFINITION:

```
label-cnt-list (lc, n)
=  if n  $\simeq$  0 then nil
   else cons (lc, label-cnt-list (lc, n - 1)) endif
```

THEOREM: length-label-cnt-list

```
length (label-cnt-list (lc, n)) = fix (n)
```

```
;; I must make sure that the condition index is in-range. I can do this by using the def-c
;; the list to index rather than the make-cond-list.
```

```
;; This was changed slightly to add two additional condition onto the front of the list. T
;; because the condition index for 'normal is not zero any longer, but is now two. Consequ
;; I'm going to use the condition index as an index into the cond-case-jump-label-list, I m
;; decrement it twice or kludge the list structure. I simply add the label for 'routineerr
;; at the beginning.
```

DEFINITION:

```
condition-map-code (actual-conds, lc, cond-list, label-alist, proc-locals-length)
=  append (list (list ('push-global, 'c-c),
                    append (cons ('jump-case,
                                   cons (lc,
                                         cons (lc,
                                                cond-case-jump-label-list (1 + lc,
                                                                              1 + length (actual-conds)))))
                                label-cnt-list (lc, proc-locals-length)),
                    list ('dl, lc, nil, ' (push-constant (nat 1))),
                    ' (pop-global c-c),
                    list ('jump, fetch-label ('routineerror, label-alist))),
            append (cond-conversion (actual-conds,
                                     1 + (1 + lc),
                                     cond-list,
                                     label-alist),
                    list (list ('dl, 1 + lc, nil, ' (no-op)))))
```

DEFINITION:

```
proc-call-code (cinfo, stmt, cond-list, locals, cond-locals-length)
=  append (push-parameters-code (locals, call-actuals (stmt)),
            cons (list ('call, call-name (stmt)),
                  condition-map-code (call-conds (stmt),
                                       label-cnt (cinfo),
                                       cond-list,
                                       label-alist (cinfo),
                                       cond-locals-length)))
```

```

;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;
;;                               %Compiling the Predefineds          ;;
;;
;;
;;
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;

```

```

;; The following functions define the sequence of statements laid
;; down for a call to a predefined procedure.

```

DEFINITION:

```

mg-simple-variable-assignment-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        '(call mg-simple-variable-assignment))

```

DEFINITION:

```

mg-simple-constant-assignment-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-constant,
              mg-to-p-simple-literal (cadr (call-actuals (stmt)))),
        '(call mg-simple-constant-assignment))

```

DEFINITION:

```

mg-simple-variable-eq-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        '(call mg-simple-variable-eq))

```

DEFINITION:

```

mg-simple-constant-eq-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-constant,
              mg-to-p-simple-literal (caddr (call-actuals (stmt)))),
        '(call mg-simple-constant-eq))

```

DEFINITION:

```

mg-integer-le-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        '(call mg-integer-le))

```


DEFINITION:

```
mg-integer-unary-minus-call-sequence (stmt, label-alist)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        '(call mg-integer-unary-minus),
        '(push-global c-c),
        '(sub1-nat),
        list ('test-nat-and-jump,
              'zero,
              fetch-label ('routineerror, label-alist)))
```

DEFINITION:

```
mg-integer-add-call-sequence (stmt, label-alist)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        '(call mg-integer-add),
        '(push-global c-c),
        '(sub1-nat),
        list ('test-nat-and-jump,
              'zero,
              fetch-label ('routineerror, label-alist)))
```

DEFINITION:

```
mg-integer-subtract-call-sequence (stmt, label-alist)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        '(call mg-integer-subtract),
        '(push-global c-c),
        '(sub1-nat),
        list ('test-nat-and-jump,
              'zero,
              fetch-label ('routineerror, label-alist)))
```

DEFINITION:

```
mg-boolean-or-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        '(call mg-boolean-or))
```

DEFINITION:

```
mg-boolean-and-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
```

```

list ('push-local, cadr (call-actuals (stmt))),
list ('push-local, caddr (call-actuals (stmt))),
'(call mg-boolean-and))

```

DEFINITION:

```

mg-boolean-not-call-sequence (stmt)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        '(call mg-boolean-not))

```

```

;; The 4th argument is a numberp supplied by the pre-processor which is
;; the size of the array. This is necessary for bounds checking.
;; >> Do I need to guarantee that it is a small-integerp?

```

DEFINITION:

```

mg-index-array-call-sequence (stmt, label-alist)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        list ('push-constant, tag ('int, caddr (call-actuals (stmt)))),
        '(call mg-index-array),
        '(push-global c-c),
        '(sub1-nat),
        list ('test-nat-and-jump,
              'zero,
              fetch-label ('routineerror, label-alist)))

```

DEFINITION:

```

mg-array-element-assignment-call-sequence (stmt, label-alist)
= list (list ('push-local, car (call-actuals (stmt))),
        list ('push-local, cadr (call-actuals (stmt))),
        list ('push-local, caddr (call-actuals (stmt))),
        list ('push-constant, tag ('int, caddr (call-actuals (stmt)))),
        '(call mg-array-element-assignment),
        '(push-global c-c),
        '(sub1-nat),
        list ('test-nat-and-jump,
              'zero,
              fetch-label ('routineerror, label-alist)))

```

DEFINITION:

```

predefined-proc-call-sequence (stmt, label-alist)
= case on call-name (stmt):
    case = mg-simple-variable-assignment

```

```

then mg-simple-variable-assignment-call-sequence (stmt)
case = mg-simple-constant-assignment
  then mg-simple-constant-assignment-call-sequence (stmt)
case = mg-simple-variable-eq
  then mg-simple-variable-eq-call-sequence (stmt)
case = mg-simple-constant-eq
  then mg-simple-constant-eq-call-sequence (stmt)
case = mg-integer-le
  then mg-integer-le-call-sequence (stmt)
case = mg-integer-unary-minus
  then mg-integer-unary-minus-call-sequence (stmt, label-alist)
case = mg-integer-add
  then mg-integer-add-call-sequence (stmt, label-alist)
case = mg-integer-subtract
  then mg-integer-subtract-call-sequence (stmt, label-alist)
case = mg-boolean-or
  then mg-boolean-or-call-sequence (stmt)
case = mg-boolean-and
  then mg-boolean-and-call-sequence (stmt)
case = mg-boolean-not
  then mg-boolean-not-call-sequence (stmt)
case = mg-index-array
  then mg-index-array-call-sequence (stmt, label-alist)
case = mg-array-element-assignment
  then mg-array-element-assignment-call-sequence (stmt, label-alist)
otherwise nil endcase

```

EVENT: Disable predefined-proc-call-sequence.

;; We now consider the bodies of the predefined routines.

DEFINITION:

MG-SIMPLE-VARIABLE-ASSIGNMENT-TRANSLATION

```

= '(mg-simple-variable-assignment
    (dest source)
    nil
    (push-local source)
    (fetch-temp-stk)
    (push-local dest)
    (deposit-temp-stk)
    (ret))

```

DEFINITION:

MG-SIMPLE-CONSTANT-ASSIGNMENT-TRANSLATION

```
= '(mg-simple-constant-assignment
  (dest source)
  nil
  (push-local source)
  (push-local dest)
  (deposit-temp-stk)
  (ret))
```

```
;; >>> Notice that deposit-temp-stk is different from my old deposit-temp
;;      in the order of args on the stack.  THESE WILL ALL HAVE TO CHANGE.
```

DEFINITION:

MG-SIMPLE-VARIABLE-EQ-TRANSLATION

```
= '(mg-simple-variable-eq
  (ans x y)
  nil
  (push-local x)
  (fetch-temp-stk)
  (push-local y)
  (fetch-temp-stk)
  (eq)
  (push-local ans)
  (deposit-temp-stk)
  (ret))
```

DEFINITION:

MG-SIMPLE-CONSTANT-EQ-TRANSLATION

```
= '(mg-simple-constant-eq
  (ans x y)
  nil
  (push-local x)
  (fetch-temp-stk)
  (push-local y)
  (eq)
  (push-local ans)
  (deposit-temp-stk)
  (ret))
```

DEFINITION:

MG-INTEGERS-LE-TRANSLATION

```
= '(mg-integer-le
  (ans x y)
  nil
```

```

(push-local y)
(fetch-temp-stk)
(push-local x)
(fetch-temp-stk)
(lt-int)
(not-bool)
(push-local ans)
(deposit-temp-stk)
(ret))

```

```

;; Since the representable positives and negatives are not
;; exactly complementary, I must check that the integer in question
;; is not that exact negative which would cause a problem.

```

DEFINITION:

MG-INTEGERS-UNARY-MINUS-TRANSLATION

```

= '(mg-integer-unary-minus
  (ans x)
  ((min-int (int -2147483648)) (temp-x (int 0)))
  (push-local x)
  (fetch-temp-stk)
  (set-local temp-x)
  (push-local min-int)
  (eq)
  (test-bool-and-jump f 0)
  (push-constant (nat 1))
  (pop-global c-c)
  (jump 1)
  (dl 0 nil (push-local temp-x))
  (neg-int)
  (push-local ans)
  (deposit-temp-stk)
  (dl 1 nil (ret)))

```

DEFINITION:

MG-INTEGERS-ADD-TRANSLATION

```

= '(mg-integer-add
  (ans y z)
  ((t1 (int 0)))
  (push-constant (bool f))
  (push-local y)
  (fetch-temp-stk)
  (push-local z)
  (fetch-temp-stk)

```

```

(add-int-with-carry)
(pop-local t1)
(test-bool-and-jump t 0)
(push-local t1)
(push-local ans)
(deposit-temp-stk)
(jump 1)
(dl 0 nil (push-constant (nat 1)))
(pop-global c-c)
(dl 1 nil (ret)))

```

DEFINITION:

MG-INTEGERS-SUBTRACT-TRANSLATION

```

= '(mg-integer-subtract
  (ans y z)
  ((t1 (int 0)))
  (push-constant (bool f))
  (push-local y)
  (fetch-temp-stk)
  (push-local z)
  (fetch-temp-stk)
  (sub-int-with-carry)
  (pop-local t1)
  (test-bool-and-jump t 0)
  (push-local t1)
  (push-local ans)
  (deposit-temp-stk)
  (jump 1)
  (dl 0 nil (push-constant (nat 1)))
  (pop-global c-c)
  (dl 1 nil (ret)))

```

DEFINITION:

MG-BOOLEAN-OR-TRANSLATION

```

= '(mg-boolean-or
  (ans b1 b2)
  nil
  (push-local b1)
  (fetch-temp-stk)
  (push-local b2)
  (fetch-temp-stk)
  (or-bool)
  (push-local ans)
  (deposit-temp-stk)
  (ret))

```

DEFINITION:

MG-BOOLEAN-AND-TRANSLATION

```
= '(mg-boolean-and
  (ans b1 b2)
  nil
  (push-local b1)
  (fetch-temp-stk)
  (push-local b2)
  (fetch-temp-stk)
  (and-bool)
  (push-local ans)
  (deposit-temp-stk)
  (ret))
```

DEFINITION:

MG-BOOLEAN-NOT-TRANSLATION

```
= '(mg-boolean-not
  (ans b1)
  nil
  (push-local b1)
  (fetch-temp-stk)
  (not-bool)
  (push-local ans)
  (deposit-temp-stk)
  (ret))
```

;; ans := A[i] of size

;; How do I know that the sub-nat to compute the index doesn't give an error?

DEFINITION:

MG-INDEX-ARRAY-TRANSLATION

```
= '(mg-index-array
  (ans a i array-size)
  ((temp-i (nat 0)))
  (push-local i)
  (fetch-temp-stk)
  (set-local temp-i)
  (test-int-and-jump neg 0)
  (push-local array-size)
  (push-local temp-i)
  (sub-int)
  (test-int-and-jump not-pos 0)
  (push-local a)
  (push-local temp-i))
```

```

(int-to-nat)
(add-nat)
(fetch-temp-stk)
(push-local ans)
(deposit-temp-stk)
(jump 1)
(dl 0 nil (push-constant (nat 1)))
(pop-global c-c)
(dl 1 nil (ret)))

;; (mg-array-element-assignment A i value size)

```

DEFINITION:

MG-ARRAY-ELEMENT-ASSIGNMENT-TRANSLATION

```

= '(mg-array-element-assignment
  (a i value array-size)
  ((temp-i (nat 0)))
  (push-local i)
  (fetch-temp-stk)
  (set-local temp-i)
  (test-int-and-jump neg 0)
  (push-local array-size)
  (push-local temp-i)
  (sub-int)
  (test-int-and-jump not-pos 0)
  (push-local value)
  (fetch-temp-stk)
  (push-local a)
  (push-local temp-i)
  (int-to-nat)
  (add-nat)
  (deposit-temp-stk)
  (jump 1)
  (dl 0 nil (push-constant (nat 1)))
  (pop-global c-c)
  (dl 1 nil (ret)))

```

```

;; The list of translations of the predefined routines is appended
;; to the list of translations of the user-defined routines and
;; becomes the program segment of the Piton program.

```

DEFINITION:

PREDEFINED-PROCEDURE-TRANSLATIONS-LIST


```
= list (MG-SIMPLE-VARIABLE-ASSIGNMENT-TRANSLATION,
        MG-SIMPLE-CONSTANT-ASSIGNMENT-TRANSLATION,
        MG-SIMPLE-VARIABLE-EQ-TRANSLATION,
        MG-SIMPLE-CONSTANT-EQ-TRANSLATION,
        MG-INTEGER-LE-TRANSLATION,
        MG-INTEGER-UNARY-MINUS-TRANSLATION,
        MG-INTEGER-ADD-TRANSLATION,
        MG-INTEGER-SUBTRACT-TRANSLATION,
        MG-BOOLEAN-OR-TRANSLATION,
        MG-BOOLEAN-AND-TRANSLATION,
        MG-BOOLEAN-NOT-TRANSLATION,
        MG-INDEX-ARRAY-TRANSLATION,
        MG-ARRAY-ELEMENT-ASSIGNMENT-TRANSLATION)
```

EVENT: Disable predefined-procedure-translations-list.

```
;; Insist that the condition on an IF statement is a variable. This means that
;; it cannot be a boolean literal. Hence the code for computing it is always.
;; (push-local b)
;; (fetch-temp-stk)
;; Otherwise, the number of statements would vary and I don't want to deal with that
;; now. This is consistent with the convention for proc-calls.
```

```
;; Condition on an IF statement is either a boolean literal or the address of a
;; boolean in the my-stack array.
```

```
;; SIGNAL
;;
;; (push-constant (nat n))          n is the index of condition in cond-list
;; (pop-global c-c)
;; (jump label)                    label is associated label of condition in lab
;;
;; PROG2
;;
;; "code for left branch"
;; "code for right branch"
;;
;;
;; LOOP
;;
;; (dl 10 nil (no-op))
;; "code for loop-body"
;; (jump L0)
;; (dl 11 nil (push-constant (nat 2)))
```

```

;;      (pop-global c-c)
;;
;; IF
;;
;;      (push-local b)
;;      (fetch-temp-stk)
;;      (test-bool-and-jump false L0)
;;      "code for true branch"
;;      (jump L1)
;;      (dl 10 nil (no-op))
;;      "code for false branch"
;;      (dl 11 nil (no-op))
;;
;; BEGIN-WHEN
;;
;;      "code for begin-body"
;;      (jump L1)
;;      (dl 10 nil (push-constant (nat 2)))
;;      (pop-global c-c)
;;      "code for when-arm-body"
;;      (dl 11 nil (no-op))
;;
;; PROC-CALL
;; For the statement
;; (PROC-CALL-MG name (act1 act2 ... actj) (cond1 cond2 ... condn))
;; we make the following code.
;;      push-locals-values-code
;;      push-locals-addresses-code
;;      push actuals-code
;;      (call name)
;;      (push-global c-c)
;;      (case-jump (L0 L1 L2 ... Ln))
;;      (push-constant (nat 1))
;;      (pop-global c-c)
;;      (jump "label-for-routineerror")
;;      (dl 11 nil (push-constant "condition-number for cond1"))
;;      (pop-global c-c)
;;      (jump "label for cond1")
;;      (dl 12 nil (push-constant "condition-number for cond2"))
;;      (pop-global c-c)
;;      (jump "label for cond2")
;;      ...
;;      (dl 1n nil (push-constant "condition-number for condn"))
;;      (pop-global c-c)

```

```
;; (jump "label for condn")
;; (dl 10 nil (no-op))
;;
;; PREDEFINED-PROC-CALL
```

DEFINITION:

```
translate (cinfo, cond-list, stmt, proc-list)
= case on car (stmt):
  case = no-op-mg
  then cinfo
  case = signal-mg
  then make-cinfo (append (code (cinfo),
                           list (list ('push-constant,
                                       mg-cond-to-p-nat (signalled-condition (stmt),
                                                           cond-list)),
                               list ('pop-global, 'c-c),
                               list ('jump,
                                       fetch-label (signalled-condition (stmt),
                                                       label-alist (cinfo))))),
                           label-alist (cinfo),
                           label-cnt (cinfo))
  case = prog2-mg
  then translate (translate (cinfo,
                           cond-list,
                           prog2-left-branch (stmt),
                           proc-list),
                 cond-list,
                 prog2-right-branch (stmt),
                 proc-list)
  case = loop-mg
  then discard-label (add-code (translate (make-cinfo (append (code (cinfo),
                                                           list (list ('dl,
                                                           label-cnt (cinfo),
                                                           nil,
                                                           ' (no-op)))))
                                       cons (cons ('leave,
                                                  1 + label-cnt (cinfo)),
                                               label-alist (cinfo)),
                                       1 + (1 + label-cnt (cinfo))),
                           cond-list,
                           loop-body (stmt),
                           proc-list),
                    list (list ('jump, label-cnt (cinfo)),
```

```

list ('d1,
      1 + label-cnt (cinfo),
      nil,
      '(push-constant
        (nat 2))),
      '(pop-global c-c))))

case = if-mg
  then add-code (translate (add-code (translate (make-cinfo (append (code (cinfo),
                                                                    list (list ('push-local,
                                                                    if-condition (stmt)),
                                                                    '(fetch-temp-stk),
                                                                    list ('test-bool-and-jump,
                                                                    'false,
                                                                    label-cnt (cinfo)))),
                                                                    label-alist (cinfo),
                                                                    1 + (1 + label-cnt (cinfo))),
                                                                    cond-list,
                                                                    if-true-branch (stmt),
                                                                    proc-list),
                                                                    list (list ('jump,
                                                                    1 + label-cnt (cinfo)),
                                                                    list ('d1,
                                                                    label-cnt (cinfo),
                                                                    nil,
                                                                    '(no-op))))),
                                                                    cond-list,
                                                                    if-false-branch (stmt),
                                                                    proc-list),
                                                                    list (list ('d1, 1 + label-cnt (cinfo), nil, '(no-op))))))

case = begin-mg
  then add-code (translate (add-code (set-label-alist (translate (make-cinfo (code (cinfo),
                                                                    append (make-label-alist (when
                                                                    label-
                                                                    label-alist (cinfo)),
                                                                    1 + (1 + label-cnt (cinfo))),
                                                                    cond-list,
                                                                    begin-body (stmt),
                                                                    proc-list),
                                                                    label-alist (cinfo))),
                                                                    list (list ('jump,
                                                                    1 + label-cnt (cinfo)),
                                                                    list ('d1,
                                                                    label-cnt (cinfo),
                                                                    nil,

```

```

                                ' (push-constant
                                  (nat 2))),
                                ' (pop-global c-c))),
                                cond-list,
                                when-handler (stmt),
                                proc-list),
                                list (list ('dl, 1 + label-cnt (cinfo), nil, ' (no-op))))
case = proc-call-mg
  then make-cinfo (append (code (cinfo),
                                proc-call-code (cinfo,
                                                  stmt,
                                                  cond-list,
                                                  def-locals (fetch-called-def (stmt,
                                                                 proc-list))),
                                length (def-cond-locals (fetch-called-def (stmt,
                                                                 proc-list))))),
                                label-alist (cinfo),
                                label-cnt (cinfo)
                                + (1 + (1 + length (call-conds (stmt)))))
case = predefined-proc-call-mg
  then add-code (cinfo,
                                predefined-proc-call-sequence (stmt, label-alist (cinfo)))
otherwise cinfo endcase

```

THEOREM: signal-translation

```

(car (stmt) = 'signal-mg)
→ (translate (cinfo, cond-list, stmt, proc-list)
    = make-cinfo (append (code (cinfo),
                                list (list ('push-constant,
                                            mg-cond-to-p-nat (signalled-condition (stmt),
                                                                cond-list)),
                                list ('pop-global, 'c-c),
                                list ('jump,
                                        fetch-label (signalled-condition (stmt),
                                                label-alist (cinfo)))))
                                label-alist (cinfo),
                                label-cnt (cinfo)))

```

THEOREM: prog2-translation

```

(car (stmt) = 'prog2-mg)
→ (translate (cinfo, cond-list, stmt, proc-list)
    = translate (translate (cinfo,
                                cond-list,
                                prog2-left-branch (stmt),

```

proc-list),
cond-list,
 prog2-right-branch (*stmt*),
proc-list)

THEOREM: loop-translation

(car (*stmt*) = 'loop-mg)
 → (translate (*cinfo*, *cond-list*, *stmt*, *proc-list*)
 = discard-label (add-code (translate (make-cinfo (append (code (*cinfo*),
 list (list ('dl,
 label-cnt (*cinfo*),
 nil,
 ' (no-op))))),
 cons (cons ('leave,
 1 + label-cnt (*cinfo*)),
 label-alist (*cinfo*)),
 1 + (1 + label-cnt (*cinfo*))),
 cond-list,
 loop-body (*stmt*),
 proc-list),
 list (list ('jump, label-cnt (*cinfo*)),
 list ('dl,
 1 + label-cnt (*cinfo*),
 nil,
 ' (push-constant
 (nat 2))),
 ' (pop-global c-c))))))

THEOREM: if-translation

(car (*stmt*) = 'if-mg)
 → (translate (*cinfo*, *cond-list*, *stmt*, *proc-list*)
 = add-code (translate (add-code (translate (make-cinfo (append (code (*cinfo*),
 list (list ('push-local,
 if-condition (*stmt*)),
 ' (fetch-temp-stk),
 list ('test-bool-and-jump,
 'false,
 label-cnt (*cinfo*))),
 label-alist (*cinfo*),
 1 + (1 + label-cnt (*cinfo*))),
 cond-list,
 if-true-branch (*stmt*),
 proc-list),
 list (list ('jump,

```

1 + label-cnt (cinfo)),
list ('dl,
    label-cnt (cinfo),
    nil,
    '(no-op))))),
cond-list,
if-false-branch (stmt),
proc-list),
list (list ('dl, 1 + label-cnt (cinfo), nil, '(no-op))))))

```

THEOREM: begin-translation

```

(car (stmt) = 'begin-mg)
→ (translate (cinfo, cond-list, stmt, proc-list)
    = add-code (translate (add-code (set-label-alist (translate (make-cinfo (code (cinfo),
                                                                    append (make-label-alist (when-
                                                                    label-c
                                                                    label-alist (cinfo)),
                                                                    1 + (1 + label-cnt (cinfo))),
                                                                    cond-list,
                                                                    begin-body (stmt),
                                                                    proc-list),
                                                                    label-alist (cinfo)),
                                                                    list (list ('jump,
                                                                    1 + label-cnt (cinfo)),
                                                                    list ('dl,
                                                                    label-cnt (cinfo),
                                                                    nil,
                                                                    '(push-constant
                                                                    (nat 2))),
                                                                    '(pop-global c-c))),
                                                                    cond-list,
                                                                    when-handler (stmt),
                                                                    proc-list),
                                                                    list (list ('dl, 1 + label-cnt (cinfo), nil, '(no-op))))))

```

THEOREM: call-translation

```

(car (stmt) = 'proc-call-mg)
→ (translate (cinfo, cond-list, stmt, proc-list)
    = make-cinfo (append (code (cinfo),
                                proc-call-code (cinfo,
                                                  stmt,
                                                  cond-list,
                                                  def-locals (fetch-called-def (stmt,
                                                                                          proc-list))),

```

$$\begin{aligned}
& \text{length}(\text{def-cond-locals}(\text{fetch-called-def}(stmt, \\
& \hspace{15em} proc-list))))), \\
& \text{label-alist}(cinfo), \\
& \text{label-cnt}(cinfo) \\
& + (1 + (1 + \text{length}(\text{call-conds}(stmt))))))
\end{aligned}$$

THEOREM: predefined-call-translation

$$\begin{aligned}
& (\text{car}(stmt) = \text{'predefined-proc-call-mg}) \\
& \rightarrow (\text{translate}(cinfo, cond-list, stmt, proc-list) \\
& \quad = \text{add-code}(cinfo, \\
& \hspace{10em} \text{predefined-proc-call-sequence}(stmt, \\
& \hspace{15em} \text{label-alist}(cinfo))))
\end{aligned}$$

EVENT: Disable translate.

THEOREM: predefined-proc-call-code-plistp

plistp(predefined-proc-call-sequence(stmt, label-alist))

THEOREM: not-find-labelp-predefined-proc-call-code

find-labelp(n, predefined-proc-call-sequence(stmt, label-alist)) = f

```

;; COMPILATION OF A PROCEDURE
;;
;; Given a procedure def of the form
;; (procedure-defn-mg name (param1 ... paramn) (cond1 ... condi) (local1 ... localj)
;;                               (local-cond1 ... local-condk) body)
;; I make the code for the body in the context of the cinfo
;;   code: nil
;;   label-alist: ((cond1 . 0) (cond2 . 0) .... (local-cond1 . 0) ...)
;;   label-cnt: 1

;; The new scheme of transforming each of the MG locals into a formal of the Piton
;; subroutine eliminates the need to convert them within the code. I hope it also
;; eliminates the need to store the stack pointer anywhere in the data-segment.

```

DEFINITION:

$$\begin{aligned}
& \text{translate-def-body}(proc-def, proc-list) \\
& = \text{add-code}(\text{translate}(\text{make-cinfo}(\text{nil}, \\
& \hspace{10em} \text{cons}(\text{cons}(\text{'routineerror}, 0), \\
& \hspace{10em} \text{make-label-alist}(\text{make-cond-list}(proc-def), \\
& \hspace{15em} 0))), \\
& \hspace{10em} 1), \\
& \hspace{10em} \text{make-cond-list}(proc-def),
\end{aligned}$$


```

      def-body (proc-def),
      proc-list),
list ('(dl 0 nil (no-op)),
      list ('pop*, data-length (def-locals (proc-def))),
      '(ret)))

```

EVENT: Disable translate-def-body.

```

;; Both the MG formals and locals become formals in the Piton world. This is a better
;; approach because it allows for structured locals just as for structured formals.

```

DEFINITION:

```

translate-def (def, proc-list)
=  append (list (def-name (def),
                append (listcars (def-locals (def)),
                        listcars (def-formals (def))),
                nil),
        code (translate-def-body (def, proc-list)))

```

DEFINITION:

```

translate-proc-list1 (proc-list1, proc-list2)
=  if proc-list1  $\simeq$  nil then nil
    else cons (translate-def (car (proc-list1), proc-list2),
              translate-proc-list1 (cdr (proc-list1), proc-list2)) endif

```

DEFINITION:

```

translate-proc-list (proc-list)
=  append (PREDEFINED-PROCEDURE-TRANSLATIONS-LIST,
          translate-proc-list1 (proc-list, proc-list))

```

EVENT: Disable translate-proc-list.

THEOREM: translate-preserves-fields

```

label-alist (translate (cinfo, cond-list, stmt, proc-list))
=  label-alist (cinfo)

```

THEOREM: code-always-plistp

```

plistp (code (cinfo))
→  plistp (code (translate (cinfo, cond-list, stmt, proc-list)))

```

THEOREM: translate-preserves-ok-cinfop

```

ok-cinfop (cinfo) → ok-cinfop (translate (cinfo, cond-list, stmt, proc-list))

```

EVENT: Disable translate-preserves-ok-cinfop.

DEFINITION:

$$\begin{aligned} & \text{nearly-equal-cinfos}(x, y) \\ &= ((\text{label-alist}(x) = \text{label-alist}(y)) \\ & \quad \wedge (\text{label-cnt}(x) = \text{label-cnt}(y))) \end{aligned}$$

THEOREM: nearly-equal-cinfos-translate

$$\begin{aligned} & (\text{cinfo}(cinfo1) \wedge \text{cinfo}(cinfo2) \wedge \text{nearly-equal-cinfos}(cinfo1, cinfo2)) \\ & \rightarrow \text{nearly-equal-cinfos}(\text{translate}(cinfo1, \text{cond-list}, \text{stmt}, \text{proc-list}), \\ & \quad \text{translate}(cinfo2, \text{cond-list}, \text{stmt}, \text{proc-list})) \end{aligned}$$

EVENT: Disable nearly-equal-cinfos-translate.

THEOREM: nullify-translate-leaves-nearly-equal

$$\begin{aligned} & \text{cinfo}(cinfo) \\ & \rightarrow \text{nearly-equal-cinfos}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list}), \\ & \quad \text{translate}(\text{nullify}(cinfo), \text{cond-list}, \text{stmt}, \text{proc-list})) \end{aligned}$$

EVENT: Disable nullify-translate-leaves-nearly-equal.

THEOREM: nullify-translate-idempotence

$$\begin{aligned} & \text{cinfo}(cinfo) \\ & \rightarrow (\text{nullify}(\text{translate}(\text{nullify}(cinfo), \text{cond-list}, \text{stmt}, \text{proc-list}))) \\ & \quad = \text{nullify}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})) \end{aligned}$$

EVENT: Disable nullify-translate-idempotence.

THEOREM: nullify-translate-idempotence2

$$\begin{aligned} & \text{cinfo}(cinfo) \\ & \rightarrow (\text{nullify}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list}))) \\ & \quad = \text{nullify}(\text{translate}(\text{nullify}(cinfo), \text{cond-list}, \text{stmt}, \text{proc-list})) \end{aligned}$$

EVENT: Disable nullify-translate-idempotence2.

THEOREM: code-doesnt-affect-other-fields

$$\begin{aligned} & \text{cinfo}(cinfo) \\ & \rightarrow ((\text{label-alist}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})) \\ & \quad = \text{label-alist}(\text{translate}(\text{nullify}(cinfo), \\ & \quad \quad \text{cond-list}, \\ & \quad \quad \text{stmt}, \\ & \quad \quad \text{proc-list}))) \\ & \quad \wedge (\text{label-cnt}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})) \\ & \quad = \text{label-cnt}(\text{translate}(\text{nullify}(cinfo), \\ & \quad \quad \text{cond-list}, \end{aligned}$$

$$stmt,$$

$$proc-list))))$$

EVENT: Disable code-doesnt-affect-other-fields.

THEOREM: add-code-doesnt-affect-other-fields
 $(\text{label-alist}(\text{add-code}(\text{info}, \text{code})) = \text{label-alist}(\text{info}))$
 $\wedge (\text{label-cnt}(\text{add-code}(\text{info}, \text{code})) = \text{label-cnt}(\text{info}))$

THEOREM: set-label-alist-doesnt-affect-other-fields

$$\begin{aligned}
& (\text{code}(\text{set-label-alist}(\text{cinfo}, \text{label-alist})) = \text{code}(\text{cinfo})) \\
& \wedge (\text{label-cnt}(\text{set-label-alist}(\text{cinfo}, \text{label-alist})) = \text{label-cnt}(\text{cinfo}))
\end{aligned}$$

THEOREM: discard-label-doesnt-affect-other-fields
 $(\text{code}(\text{discard-label}(info)) = \text{code}(info))$
 $\wedge (\text{label-cnt}(\text{discard-label}(info)) = \text{label-cnt}(info))$

THEOREM: nullify-cancels-add-code
 $\text{nullify}(\text{add-code}(\text{cinfo}, \text{code})) = \text{nullify}(\text{cinfo})$

THEOREM: code-add-code-commute
 $\text{code}(\text{add-code}(cinfo, cd)) = \text{append}(\text{code}(cinfo), cd)$

THEOREM: label-alist-set-label-alist
 label-alist (set-label-alist (*state*, *label-alist*)) = *label-alist*

THEOREM: nullify-doesnt-affect-proc-call-code

$$\text{proc-call-code}(\text{nullify}(cinfo), stmt, cond\text{-list}, locals, k) = \text{proc-call-code}(cinfo, stmt, cond\text{-list}, locals, k)$$

THEOREM: nullify-code-nil
code (nullify (*cin*fo)) = **nil**

```

DEFINITION:
nullify-induction-hint (cinfo, cond-list, stmt, proc-list)
=  case on car (stmt):
    case = no-op-mg
    then t
    case = signal-mg
        then t
    case = prog2-mg
        then nullify-induction-hint (cinfo,
                                         cond-list,
                                         prog2-left-branch (stmt),
                                         proc-list)

```

```

      ∧ nullify-induction-hint (translate (cinfo,
                                           cond-list,
                                           prog2-left-branch (stmt),
                                           proc-list),
                                cond-list,
                                prog2-right-branch (stmt),
                                proc-list)
      ∧ nullify-induction-hint (translate (nullify (cinfo),
                                           cond-list,
                                           prog2-left-branch (stmt),
                                           proc-list),
                                cond-list,
                                prog2-right-branch (stmt),
                                proc-list)
case = loop-mg
  then nullify-induction-hint (make-cinfo (append (code (cinfo),
                                                       list (list ('d1,
                                                                    label-cnt (cinfo),
                                                                    nil,
                                                                    ' (no-op) ))),
                                                       cons (cons ('leave,
                                                                    1 + label-cnt (cinfo)),
                                                                    label-alist (cinfo)),
                                                                    1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                loop-body (stmt),
                                proc-list)
      ∧ nullify-induction-hint (make-cinfo (list (list ('d1,
                                                         label-cnt (cinfo),
                                                         nil,
                                                         ' (no-op) ))),
                                         cons (cons ('leave,
                                                         1 + label-cnt (cinfo)),
                                                         label-alist (cinfo)),
                                                         1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                loop-body (stmt),
                                proc-list)
case = if-mg
  then nullify-induction-hint (make-cinfo (list (list ('push-local,
                                                         if-condition (stmt)),
                                                         ' (fetch-temp-stk),
                                                         list ('test-bool-and-jump,
                                                         'false,

```

```

label-cnt (cinfo))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list)
^ nullify-induction-hint (make-cinfo (append (code (cinfo),
list (list ('push-local,
if-condition (stmt)),
' (fetch-temp-stk),
list ('test-bool-and-jump,
'false,
label-cnt (cinfo)))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list)
^ nullify-induction-hint (add-code (translate (make-cinfo (append (code (cinfo),
list (list ('push-local,
if-condition (stmt)),
' (fetch-temp-stk),
list ('test-bool-and-jump,
'false,
label-cnt (cinfo)))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
list ('dl,
label-cnt (cinfo),
nil,
' (no-op)))),
cond-list,
if-false-branch (stmt),
proc-list)
^ nullify-induction-hint (add-code (translate (make-cinfo (list (list ('push-local,
if-condition (stmt)),
' (fetch-temp-stk),
list ('test-bool-and-jump,
'false,

```

```

label-cnt (cinfo))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
list ('dl,
label-cnt (cinfo),
nil,
'(no-op)))),
cond-list,
if-false-branch (stmt),
proc-list)
case = begin-mg
then nullify-induction-hint (add-code (set-label-alist (translate (make-cinfo (code (cinfo),
append (make-label-alist (when-labels (stmt),
label-cnt (cinfo))),
label-alist (cinfo)),
1 + (1 + label-cnt (cinfo))),
cond-list,
begin-body (stmt),
proc-list),
label-alist (cinfo)),
list (list ('jump,
1 + label-cnt (cinfo)),
list ('dl,
label-cnt (cinfo),
nil,
'(push-constant
(nat 2))),
'(pop-global c-c))),
cond-list,
when-handler (stmt),
proc-list)
^ nullify-induction-hint (make-cinfo (code (cinfo),
append (make-label-alist (when-labels (stmt),
label-cnt (cinfo)),
label-alist (cinfo)),
1 + (1 + label-cnt (cinfo))),
cond-list,
begin-body (stmt),
proc-list)

```

```

      ∧ nullify-induction-hint (add-code (set-label-alist (translate (nullify (make-cinfo (code (cinfo),
                                                                                          append (make-label-cnt
                                                                                          label-alist
                                                                                          1 + (1 + label-cnt
                                                                                          cond-list,
                                                                                          begin-body (stmt),
                                                                                          proc-list),
                                                                                          label-alist (cinfo)),
list (list ('jump,
            1 + label-cnt (cinfo)),
list ('dl,
      label-cnt (cinfo),
      nil,
      '(push-constant
        (nat 2))),
      '(pop-global
        c-c))),
cond-list,
when-handler (stmt),
proc-list)

case = proc-call-mg
then t
case = predefined-proc-call-mg
then t
otherwise f endcase

```

THEOREM: new-code-prog2-case-induction-hyps

((car (stmt) = 'prog2-mg) ∧ ok-cinfo (cinfo))

→ (ok-cinfo (translate (nullify (cinfo),

cond-list,
prog2-left-branch (stmt),
proc-list))

∧ ok-cinfo (translate (cinfo,

cond-list,
prog2-left-branch (stmt),
proc-list)))

EVENT: Disable nullify.

THEOREM: new-code-prog2-case

((car (stmt) = 'prog2-mg)

∧ ok-cinfo (cinfo)

∧ (ok-cinfo (translate (nullify (cinfo),

$$\begin{aligned}
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list})) \\
\rightarrow & \text{(append (code (translate (nullify (cinfo),} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list))),} \\
& \text{code (translate (nullify (translate (nullify (cinfo),} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list))),} \\
& \text{cond-list,} \\
& \text{prog2-right-branch (stmt),} \\
& \text{proc-list)))))) \\
= & \text{code (translate (translate (nullify (cinfo),} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list}),} \\
& \text{cond-list,} \\
& \text{prog2-right-branch (stmt),} \\
& \text{proc-list)))))) \\
\wedge & \text{(ok-cinfo (translate (cinfo,} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list}))} \\
\rightarrow & \text{(append (code (translate (cinfo,} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list))),} \\
& \text{code (translate (nullify (translate (cinfo,} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list))),} \\
& \text{cond-list,} \\
& \text{prog2-right-branch (stmt),} \\
& \text{proc-list)))))) \\
= & \text{code (translate (translate (cinfo,} \\
& \text{cond-list,} \\
& \text{prog2-left-branch (stmt),} \\
& \text{proc-list}),} \\
& \text{cond-list,} \\
& \text{prog2-right-branch (stmt),} \\
& \text{proc-list)))))) \\
\wedge & \text{(ok-cinfo (cinfo))}
\end{aligned}$$

$$\begin{aligned}
& \rightarrow (\text{append}(\text{code}(cinfo), \\
& \quad \text{code}(\text{translate}(\text{nullify}(cinfo), \\
& \quad \quad \text{cond-list}, \\
& \quad \quad \text{prog2-left-branch}(stmt), \\
& \quad \quad \text{proc-list}))) \\
& = \text{code}(\text{translate}(cinfo, \\
& \quad \text{cond-list}, \\
& \quad \text{prog2-left-branch}(stmt), \\
& \quad \text{proc-list})))) \\
& \rightarrow (\text{append}(\text{code}(cinfo), \\
& \quad \text{code}(\text{translate}(\text{nullify}(cinfo), \text{cond-list}, \text{stmt}, \text{proc-list}))) \\
& = \text{code}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})))
\end{aligned}$$

THEOREM: new-code-loop-case-induction-hyps

$$\begin{aligned}
& \text{ok-cinfop}(cinfo) \\
& \rightarrow (\text{ok-cinfop}(\text{make-cinfo}(\text{list}(\text{cons}('dl, \\
& \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad '(\text{nil } (\text{no-op}))))), \\
& \quad \text{cons}(\text{cons}('leave, 1 + \text{label-cnt}(cinfo)), \\
& \quad \quad \text{label-alist}(cinfo)), \\
& \quad 1 + (1 + \text{label-cnt}(cinfo)))) \\
& \wedge \text{ok-cinfop}(\text{make-cinfo}(\text{append}(\text{code}(cinfo), \\
& \quad \text{list}(\text{cons}('dl, \\
& \quad \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad \quad '(\text{nil } (\text{no-op}))))), \\
& \quad \quad \text{cons}(\text{cons}('leave, 1 + \text{label-cnt}(cinfo)), \\
& \quad \quad \quad \text{label-alist}(cinfo)), \\
& \quad \quad 1 + (1 + \text{label-cnt}(cinfo))))))
\end{aligned}$$

THEOREM: new-code-loop-case

$$\begin{aligned}
& ((\text{car}(stmt) = \text{'loop-mg}) \\
& \wedge \text{ok-cinfop}(cinfo) \\
& \wedge (\text{ok-cinfop}(\text{make-cinfo}(\text{list}(\text{cons}('dl, \\
& \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad '(\text{nil } (\text{no-op}))))), \\
& \quad \text{cons}(\text{cons}('leave, 1 + \text{label-cnt}(cinfo)), \\
& \quad \quad \text{label-alist}(cinfo)), \\
& \quad 1 + (1 + \text{label-cnt}(cinfo)))) \\
& \rightarrow (\text{append}(\text{code}(\text{make-cinfo}(\text{list}(\text{cons}('dl, \\
& \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad '(\text{nil } (\text{no-op}))))), \\
& \quad \text{cons}(\text{cons}('leave, \\
& \quad \quad 1 + \text{label-cnt}(cinfo)),
\end{aligned}$$

$$\begin{aligned}
& \text{label-alist}(\text{cinfo}), \\
& 1 + (1 + \text{label-cnt}(\text{cinfo}))), \\
& \text{code}(\text{translate}(\text{nullify}(\text{make-cinfo}(\text{list}(\text{cons}('dl, \\
& \hspace{15em} \text{cons}(\text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} '(\text{nil} \\
& \hspace{15em} (\text{no-op}))))), \\
& \hspace{10em} \text{cons}(\text{cons}('leave, \\
& \hspace{15em} 1 + \text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} \text{label-alist}(\text{cinfo}), \\
& \hspace{15em} 1 + (1 + \text{label-cnt}(\text{cinfo})))), \\
& \hspace{10em} \text{cond-list}, \\
& \hspace{10em} \text{loop-body}(\text{stmt}), \\
& \hspace{10em} \text{proc-list}))) \\
= & \text{code}(\text{translate}(\text{make-cinfo}(\text{list}(\text{cons}('dl, \\
& \hspace{15em} \text{cons}(\text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} '(\text{nil} \\
& \hspace{15em} (\text{no-op}))))), \\
& \hspace{10em} \text{cons}(\text{cons}('leave, \\
& \hspace{15em} 1 + \text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} \text{label-alist}(\text{cinfo}), \\
& \hspace{15em} 1 + (1 + \text{label-cnt}(\text{cinfo}))), \\
& \hspace{10em} \text{cond-list}, \\
& \hspace{10em} \text{loop-body}(\text{stmt}), \\
& \hspace{10em} \text{proc-list}))) \\
\wedge & (\text{ok-cinfo}(\text{make-cinfo}(\text{append}(\text{code}(\text{cinfo}), \\
& \hspace{15em} \text{list}(\text{cons}('dl, \\
& \hspace{15em} \text{cons}(\text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} '(\text{nil} (\text{no-op}))))), \\
& \hspace{10em} \text{cons}(\text{cons}('leave, 1 + \text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} \text{label-alist}(\text{cinfo}), \\
& \hspace{15em} 1 + (1 + \text{label-cnt}(\text{cinfo})))) \\
\rightarrow & (\text{append}(\text{code}(\text{make-cinfo}(\text{append}(\text{code}(\text{cinfo}), \\
& \hspace{15em} \text{list}(\text{cons}('dl, \\
& \hspace{15em} \text{cons}(\text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} '(\text{nil} \\
& \hspace{15em} (\text{no-op}))))), \\
& \hspace{10em} \text{cons}(\text{cons}('leave, \\
& \hspace{15em} 1 + \text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} \text{label-alist}(\text{cinfo}), \\
& \hspace{15em} 1 + (1 + \text{label-cnt}(\text{cinfo}))), \\
& \text{code}(\text{translate}(\text{nullify}(\text{make-cinfo}(\text{append}(\text{code}(\text{cinfo}), \\
& \hspace{15em} \text{list}(\text{cons}('dl, \\
& \hspace{15em} \text{cons}(\text{label-cnt}(\text{cinfo}), \\
& \hspace{15em} '(\text{nil}
\end{aligned}$$

$$\begin{aligned}
& \text{cons}(\text{cons}('leave, \\
& \quad 1 + \text{label-cnt}(cinfo)), \\
& \quad \text{label-alist}(cinfo)), \\
& \quad 1 + (1 + \text{label-cnt}(cinfo))), \\
& \quad \text{cond-list}, \\
& \quad \text{loop-body}(stmt), \\
& \quad \text{proc-list})) \\
= & \text{code}(\text{translate}(\text{make-cinfo}(\text{append}(\text{code}(cinfo), \\
& \quad \text{list}(\text{cons}('dl, \\
& \quad \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad 'nil \\
& \quad \quad (\text{no-op}))))), \\
& \quad \text{cons}(\text{cons}('leave, \\
& \quad \quad 1 + \text{label-cnt}(cinfo)), \\
& \quad \quad \text{label-alist}(cinfo)), \\
& \quad \quad 1 + (1 + \text{label-cnt}(cinfo))), \\
& \quad \text{cond-list}, \\
& \quad \text{loop-body}(stmt), \\
& \quad \text{proc-list})))))) \\
\rightarrow & (\text{append}(\text{code}(cinfo), \\
& \quad \text{code}(\text{translate}(\text{nullify}(cinfo), \text{cond-list}, \text{stmt}, \text{proc-list}))) \\
& \quad = \text{code}(\text{translate}(cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})))
\end{aligned}$$

THEOREM: new-code-if-case-induction-hyps

ok-cinfo($cinfo$)

$$\begin{aligned}
\rightarrow & (\text{ok-cinfo}(\text{add-code}(\text{translate}(\text{make-cinfo}(\text{list}(\text{list}('push-local, \\
& \quad \text{if-condition}(stmt)), \\
& \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list}('test-bool-and-jump, \\
& \quad 'false, \\
& \quad \text{label-cnt}(cinfo)), \\
& \quad \text{label-alist}(cinfo), \\
& \quad 1 + (1 + \text{label-cnt}(cinfo))), \\
& \quad \text{cond-list}, \\
& \quad \text{if-true-branch}(stmt), \\
& \quad \text{proc-list}), \\
& \quad \text{list}(\text{list}('jump, 1 + \text{label-cnt}(cinfo)), \\
& \quad \text{cons}('dl, \\
& \quad \quad \text{cons}(\text{label-cnt}(cinfo), \\
& \quad \quad '(\text{nil} (\text{no-op}))))))) \\
\wedge & \text{ok-cinfo}(\text{add-code}(\text{translate}(\text{make-cinfo}(\text{append}(\text{code}(cinfo), \\
& \quad \text{list}(\text{list}('push-local, \\
& \quad \text{if-condition}(stmt)),
\end{aligned}$$

```

                                '(fetch-temp-stk),
                                list('test-bool-and-jump,
                                      'false,
                                      label-cnt(cinfo))),
                                label-alist(cinfo),
                                1 + (1 + label-cnt(cinfo))),
                                cond-list,
                                if-true-branch(stmt),
                                proc-list,
list(list('jump, 1 + label-cnt(cinfo)),
      cons('dl,
            cons(label-cnt(cinfo),
                  '(nil (no-op))))))
^ ok-cinfop(make-cinfo(append(code(cinfo),
                                list(list('push-local,
                                              if-condition(stmt)),
                                              '(fetch-temp-stk),
                                              list('test-bool-and-jump,
                                                    'false,
                                                    label-cnt(cinfo))),
                                label-alist(cinfo),
                                1 + (1 + label-cnt(cinfo))))))
^ ok-cinfop(make-cinfo(list(list('push-local,
                                if-condition(stmt)),
                                '(fetch-temp-stk),
                                list('test-bool-and-jump,
                                      'false,
                                      label-cnt(cinfo))),
                                label-alist(cinfo),
                                1 + (1 + label-cnt(cinfo))))))

```

THEOREM: new-code-if-case

```

((car(stmt) = 'if-mg)
 ^ ok-cinfop(cinfo)
 ^ (ok-cinfop(add-code(translate(make-cinfo(list(list('push-local,
                                                        if-condition(stmt)),
                                                        '(fetch-temp-stk),
                                                        list('test-bool-and-jump,
                                                            'false,
                                                            label-cnt(cinfo))),
                                                        label-alist(cinfo),
                                                        1 + (1 + label-cnt(cinfo))),
                                cond-list,
                                if-true-branch(stmt),

```

```

      proc-list),
      list (list ('jump, 1 + label-cnt (cinfo)),
            cons ('dl,
                  cons (label-cnt (cinfo),
                        '(nil (no-op))))))
→ (append (code (add-code (translate (make-cinfo (list (list ('push-local,
                                                             if-condition (stmt)),
                                                             '(fetch-temp-stk),
                                                             list ('test-bool-and-jump,
                                                             'false,
                                                             label-cnt (cinfo))),
                                                             label-alist (cinfo),
                                                             1 + (1 + label-cnt (cinfo))),
                                                             cond-list,
                                                             if-true-branch (stmt),
                                                             proc-list),
              list (list ('jump, 1 + label-cnt (cinfo)),
                    cons ('dl,
                          cons (label-cnt (cinfo),
                                '(nil (no-op)))))),
            code (translate (nullify (add-code (translate (make-cinfo (list (list ('push-local,
                                                                                   if-condition (stmt)),
                                                                                   '(fetch-temp-stk),
                                                                                   list ('test-bool-and-jump,
                                                                                   'false,
                                                                                   label-cnt (cinfo))),
                                                                                   label-alist (cinfo),
                                                                                   1 + (1 + label-cnt (cinfo))),
                                                                                   cond-list,
                                                                                   if-true-branch (stmt),
                                                                                   proc-list),
              list (list ('jump,
                          1 + label-cnt (cinfo)),
                    cons ('dl,
                          cons (label-cnt (cinfo),
                                '(nil
                                  (no-op))))))),
            cond-list,
            if-false-branch (stmt),
            proc-list)))
= code (translate (add-code (translate (make-cinfo (list (list ('push-local,
                                                             if-condition (stmt)),
                                                             '(fetch-temp-stk),
                                                             list ('test-bool-and-jump,

```

```

                                'false,
                                label-cnt (cinfo)),
                                label-alist (cinfo),
                                1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                if-true-branch (stmt),
                                proc-list),
list (list ('jump,
            1 + label-cnt (cinfo)),
      cons ('dl,
            cons (label-cnt (cinfo),
                  '(nil
                    (no-op)))))),
                                cond-list,
                                if-false-branch (stmt),
                                proc-list))))
^  (ok-cinfo (add-code (translate (make-cinfo (append (code (cinfo),
                                                         list (list ('push-local,
                                                                    if-condition (stmt)),
                                                                    ('fetch-temp-stk),
                                                                    list ('test-bool-and-jump,
                                                                    'false,
                                                                    label-cnt (cinfo)))))
                                                         label-alist (cinfo),
                                                         1 + (1 + label-cnt (cinfo))),
                                                         cond-list,
                                                         if-true-branch (stmt),
                                                         proc-list)),
list (list ('jump, 1 + label-cnt (cinfo)),
      cons ('dl,
            cons (label-cnt (cinfo),
                  '(nil (no-op)))))))
→  (append (code (add-code (translate (make-cinfo (append (code (cinfo),
                                                         list (list ('push-local,
                                                                    if-condition (stmt)),
                                                                    ('fetch-temp-stk),
                                                                    list ('test-bool-and-jump,
                                                                    'false,
                                                                    label-cnt (cinfo)))))
                                                         label-alist (cinfo),
                                                         1 + (1 + label-cnt (cinfo))),
                                                         cond-list,
                                                         if-true-branch (stmt),
                                                         proc-list),

```

```

list (list ('jump, 1 + label-cnt (cinfo)),
      cons ('dl,
            cons (label-cnt (cinfo),
                  '(nil (no-op)))))),
code (translate (nullify (add-code (translate (make-cinfo (append (code (cinfo),
                                                                    list (list ('push-local,
                                                                    if-condition (stmt
                                                                    '(fetch-temp-stk)
                                                                    list ('test-bool-and-jump,
                                                                    'false,
                                                                    label-cnt (cinfo)
                                                                    label-alist (cinfo),
                                                                    1 + (1 + label-cnt (cinfo))),
                                                                    cond-list,
                                                                    if-true-branch (stmt),
                                                                    proc-list),
                                                                    list (list ('jump,
                                                                    1 + label-cnt (cinfo)),
                                                                    cons ('dl,
                                                                    cons (label-cnt (cinfo),
                                                                    '(nil
                                                                    (no-op))))))),
                                                                    cond-list,
                                                                    if-false-branch (stmt),
                                                                    proc-list)))
= code (translate (add-code (translate (make-cinfo (append (code (cinfo),
                                                                    list (list ('push-local,
                                                                    if-condition (stmt),
                                                                    '(fetch-temp-stk),
                                                                    list ('test-bool-and-jump,
                                                                    'false,
                                                                    label-cnt (cinfo))),
                                                                    label-alist (cinfo),
                                                                    1 + (1 + label-cnt (cinfo))),
                                                                    cond-list,
                                                                    if-true-branch (stmt),
                                                                    proc-list),
                                                                    list (list ('jump,
                                                                    1 + label-cnt (cinfo)),
                                                                    cons ('dl,
                                                                    cons (label-cnt (cinfo),
                                                                    '(nil
                                                                    (no-op))))))),
                                                                    cond-list,
                                                                    if-false-branch (stmt),
                                                                    proc-list)))

```

$$\begin{aligned}
& \text{if-false-branch} (stmt), \\
& \text{proc-list}))) \\
\wedge \quad & (\text{ok-cinfop} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo)))) \\
\rightarrow \quad & (\text{append} (\text{code} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo))))), \\
& \text{code} (\text{translate} (\text{nullify} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo))))), \\
& \text{cond-list}, \\
& \text{if-true-branch} (stmt), \\
& \text{proc-list}))) \\
= \quad & \text{code} (\text{translate} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo))))), \\
& \text{cond-list}, \\
& \text{if-true-branch} (stmt), \\
& \text{proc-list})))
\end{aligned}$$

$$\begin{aligned}
& \wedge \quad (\text{ok-cinfo} (\text{make-cinfo} (\text{list} (\text{list} ('push-local, \text{if-condition} (stmt)), \\
& \quad \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \quad \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad \quad \quad 'false, \\
& \quad \quad \quad \quad \text{label-cnt} (cinfo))), \\
& \quad \quad \quad \text{label-alist} (cinfo), \\
& \quad \quad \quad 1 + (1 + \text{label-cnt} (cinfo)))) \\
& \rightarrow \quad (\text{append} (\text{code} (\text{make-cinfo} (\text{list} (\text{list} ('push-local, \\
& \quad \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \quad \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad \quad \quad 'false, \\
& \quad \quad \quad \quad \text{label-cnt} (cinfo))), \\
& \quad \quad \quad \text{label-alist} (cinfo), \\
& \quad \quad \quad 1 + (1 + \text{label-cnt} (cinfo)))), \\
& \quad \quad \quad \text{code} (\text{translate} (\text{nullify} (\text{make-cinfo} (\text{list} (\text{list} ('push-local, \\
& \quad \quad \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \quad \quad \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad \quad \quad \quad 'false, \\
& \quad \quad \quad \quad \quad \text{label-cnt} (cinfo))), \\
& \quad \quad \quad \quad \text{label-alist} (cinfo), \\
& \quad \quad \quad \quad 1 + (1 + \text{label-cnt} (cinfo))))), \\
& \quad \quad \quad \text{cond-list}, \\
& \quad \quad \quad \text{if-true-branch} (stmt), \\
& \quad \quad \quad \text{proc-list}))) \\
& = \quad \text{code} (\text{translate} (\text{make-cinfo} (\text{list} (\text{list} ('push-local, \\
& \quad \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \quad \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad \quad \quad 'false, \\
& \quad \quad \quad \quad \text{label-cnt} (cinfo))), \\
& \quad \quad \quad \text{label-alist} (cinfo), \\
& \quad \quad \quad 1 + (1 + \text{label-cnt} (cinfo))), \\
& \quad \quad \quad \text{cond-list}, \\
& \quad \quad \quad \text{if-true-branch} (stmt), \\
& \quad \quad \quad \text{proc-list})))))) \\
& \rightarrow \quad (\text{append} (\text{code} (cinfo), \\
& \quad \quad \quad \text{code} (\text{translate} (\text{nullify} (cinfo), \text{cond-list}, \text{stmt}, \text{proc-list}))) \\
& \quad \quad \quad = \quad \text{code} (\text{translate} (cinfo, \text{cond-list}, \text{stmt}, \text{proc-list})))
\end{aligned}$$

THEOREM: new-code-begin-case-induction-hyps

ok-cinfo (*cinfo*)

\rightarrow (ok-cinfo (add-code (set-label-alist (translate (nullify (make-cinfo (code (*cinfo*),

```

                                append (make-label-alist (when-labels (stm)
                                label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                begin-body (stmt),
                                proc-list),
                                label-alist (cinfo)),
                                cons (list ('jump, 1 + label-cnt (cinfo)),
                                cons (cons ('dl,
                                cons (label-cnt (cinfo),
                                ' (nil
                                (push-constant
                                (nat 2))))),
                                ' ((pop-global c-c)))))
    ∧ ok-cinfop (make-cinfo (code (cinfo),
                                append (make-label-alist (when-labels (stm)
                                label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))))
    ∧ ok-cinfop (add-code (set-label-alist (translate (make-cinfo (code (cinfo),
                                append (make-label-alist (when-labels (stm)
                                label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                begin-body (stmt),
                                proc-list),
                                label-alist (cinfo)),
                                cons (list ('jump, 1 + label-cnt (cinfo)),
                                cons (cons ('dl,
                                cons (label-cnt (cinfo),
                                ' (nil
                                (push-constant
                                (nat 2))))),
                                ' ((pop-global c-c)))))

(prove-lemma new-code-begin-case (rewrite)
  (IMPLIES
    (AND
      (equal (car STMT) 'BEGIN-MG)
      (OK-CINFOP CINFO)

```



```

(ADD1 (ADD1 (LABEL-CNT CINFO))))
  COND-LIST
    (BEGIN-BODY STMT)
  PROC-LIST
    (LABEL-ALIST CINFO))
(CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
      (CONS (CONS 'DL
                  (CONS (LABEL-CNT CINFO)
                        '(NIL (PUSH-CONSTANT (NAT 2))))))
          '((POP-GLOBAL C-C))))))
  COND-LIST
    (WHEN-HANDLER STMT)
  PROC-LIST)))
  (CODE
(TRANSLATE
  (ADD-CODE
    (SET-LABEL-ALIST
      (TRANSLATE
        (NULLIFY (MAKE-CINFO (CODE CINFO)
                              (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
                                                            (LABEL-CNT CINFO))
                                                            (LABEL-ALIST CINFO))
                              (ADD1 (ADD1 (LABEL-CNT CINFO))))))
        COND-LIST
        (BEGIN-BODY STMT)
        PROC-LIST)
        (LABEL-ALIST CINFO))
        (CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
              (CONS (CONS 'DL
                        (CONS (LABEL-CNT CINFO)
                              '(NIL (PUSH-CONSTANT (NAT 2))))))
                  '((POP-GLOBAL C-C))))))
        COND-LIST
        (WHEN-HANDLER STMT)
        PROC-LIST))))
    (IMPLIES
      (OK-CINFOP (MAKE-CINFO (CODE CINFO)
                              (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT) (LABEL-CNT CINFO))
                                      (LABEL-ALIST CINFO))
                              (ADD1 (ADD1 (LABEL-CNT CINFO))))))
      (EQUAL
        (APPEND
          (CODE (MAKE-CINFO (CODE CINFO)
                            (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT) (LABEL-CNT CINFO))

```

```

(LABEL-ALIST CINFO))
(ADD1 (ADD1 (LABEL-CNT CINFO))))))
(CODE
  (TRANSLATE
    (NULLIFY (MAKE-CINFO (CODE CINFO)
      (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT) (LABEL-CNT CINFO))
        (LABEL-ALIST CINFO))
      (ADD1 (ADD1 (LABEL-CNT CINFO))))))
    COND-LIST (BEGIN-BODY STMT) PROC-LIST)))
  (CODE (TRANSLATE (MAKE-CINFO (CODE CINFO)
    (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT) (LABEL-CNT CINFO))
      (LABEL-ALIST CINFO))
    (ADD1 (ADD1 (LABEL-CNT CINFO))))))
    COND-LIST (BEGIN-BODY STMT) PROC-LIST))))
(IMPLIES
  (OK-CINFOP
    (ADD-CODE
      (SET-LABEL-ALIST
        (TRANSLATE (MAKE-CINFO (CODE CINFO)
          (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT) (LABEL-CNT CINFO))
            (LABEL-ALIST CINFO))
          (ADD1 (ADD1 (LABEL-CNT CINFO))))))
        COND-LIST (BEGIN-BODY STMT) PROC-LIST)
        (LABEL-ALIST CINFO))
      (CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
        (CONS (CONS 'DL (CONS (LABEL-CNT CINFO) '(NIL (PUSH-CONSTANT (NAT 2)))))
          '((POP-GLOBAL C-C)))))
      (EQUAL
        (APPEND
          (CODE
            (ADD-CODE
              (SET-LABEL-ALIST
                (TRANSLATE (MAKE-CINFO (CODE CINFO)
                  (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
                    (LABEL-CNT CINFO))
                    (LABEL-ALIST CINFO))
                  (ADD1 (ADD1 (LABEL-CNT CINFO))))))
                COND-LIST
                (BEGIN-BODY STMT)
                PROC-LIST)
                (LABEL-ALIST CINFO))
                (CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
                  (CONS (CONS 'DL
                    (CONS (LABEL-CNT CINFO)

```



```

PROC-LIST))))))
(EQUAL (APPEND (CODE CINFO)
  (CODE (TRANSLATE (NULLIFY CINFO)
    COND-LIST STMT PROC-LIST)))
  (CODE (TRANSLATE CINFO COND-LIST STMT PROC-LIST))))
((INSTRUCTIONS (disable add-code set-label-alist)
  PROMOTE (DEMOTE 3) (DIVE 1 1) (REWRITE NEW-CODE-BEGIN-CASE-INDUCTION-HYPS) UP S TOP
  (DEMOTE 3) (DIVE 1 1) (REWRITE NEW-CODE-BEGIN-CASE-INDUCTION-HYPS) UP S TOP PROMOTE
  (DEMOTE 3) (DIVE 1 1) (REWRITE NEW-CODE-BEGIN-CASE-INDUCTION-HYPS) UP S TOP PROMOTE
  (DIVE 2 1) (REWRITE BEGIN-TRANSLATION) UP (REWRITE CODE-ADD-CODE-COMMUTE) (DIVE 1) =
  UP (REWRITE ASSOCIATIVITY-OF-APPEND) (DIVE 1) (REWRITE CODE-ADD-CODE-COMMUTE) (DIVE 1) =
  (REWRITE SET-LABEL-ALIST-DOESNT-AFFECT-OTHER-FIELDS) = (DROP 4) UP
  (REWRITE ASSOCIATIVITY-OF-APPEND) UP (REWRITE ASSOCIATIVITY-OF-APPEND) TOP (REWRITE
  (DIVE 1 1) (REWRITE BEGIN-TRANSLATION) UP (REWRITE CODE-ADD-CODE-COMMUTE) (DIVE 1) (
  S TOP (DEMOTE 3) (DIVE 1 2) (S-PROP NULLIFY) S TOP PROMOTE (DIVE 1 1) = (DROP 3) TOP
  (BASH (ENABLE NULLIFY ADD-CODE TRANSLATE-PRESERVES-FIELDS APPEND-REWRITE2 SET-LABEL-
  PROMOTE (DIVE 2 1 1) (DIVE 1 3) (REWRITE CODE-DOESNT-AFFECT-OTHER-FIELDS)
  TOP (PROVE (ENABLE NULLIFY))))))

```

THEOREM: new-code-appended-to-old

```

ok-cinfo(cinfo)
→ (append (code(cinfo),
  code(translate (nullify(cinfo), cond-list, stmt, proc-list)))
  = code(translate(cinfo, cond-list, stmt, proc-list)))

```

EVENT: Disable new-code-appended-to-old.

THEOREM: new-code-appended-to-old1

```

ok-cinfo(cinfo)
→ (code(translate(cinfo, cond-list, stmt, proc-list))
  = append (code(cinfo),
    code(translate (nullify(cinfo), cond-list, stmt, proc-list))))

```

EVENT: Disable new-code-appended-to-old1.

DEFINITION:

```

collect-labels(codelist)
= if codelist ≈ nil then nil
  elseif caar(codelist) = 'd1
  then cons(cadar(codelist), collect-labels(cdr(codelist)))
  else collect-labels(cdr(codelist)) endif

```

THEOREM: collect-labels-plistp

```

plistp(collect-labels(lst))

```

THEOREM: collect-labels-distributes
 $\text{collect-labels}(\text{append}(code1, code2))$
 $= \text{append}(\text{collect-labels}(code1), \text{collect-labels}(code2))$

DEFINITION:
 $\text{all-labels-unique}(codelist) = \text{no-duplicates}(\text{collect-labels}(codelist))$

EVENT: Disable all-labels-unique.

THEOREM: all-labels-unique-append
 $\text{all-labels-unique}(\text{append}(x, y))$
 $\rightarrow (\text{all-labels-unique}(x) \wedge \text{all-labels-unique}(y))$

THEOREM: all-labels-unique-reduction
 $(\neg \text{all-labels-unique}(y)) \rightarrow (\neg \text{all-labels-unique}(\text{append}(x, y)))$

EVENT: Disable all-labels-unique-reduction.

THEOREM: all-labels-unique-reduction2
 $(\neg \text{all-labels-unique}(y)) \rightarrow (\neg \text{all-labels-unique}(\text{cons}(x, y)))$

EVENT: Disable all-labels-unique-reduction2.

THEOREM: find-labelp-rewrites-to-member
 $\text{find-labelp}(lab, code) = (lab \in \text{collect-labels}(code))$

EVENT: Disable find-labelp-rewrites-to-member.

THEOREM: all-labels-unique-reduction3
 $(\text{find-labelp}(lab, code1) \wedge \text{find-labelp}(lab, code2))$
 $\rightarrow (\neg \text{all-labels-unique}(\text{append}(code1, code2)))$

EVENT: Disable all-labels-unique-reduction3.

THEOREM: no-duplicates-append-list
 $\text{no-duplicates}(\text{append}(lst, \text{cons}(x, \text{cons}(y, lst2))))$
 $\rightarrow \text{no-duplicates}(\text{append}(lst, \text{list}(y)))$

THEOREM: no-duplicates-append-list2
 $\text{no-duplicates}(\text{append}(lst, \text{cons}(y, lst2)))$
 $\rightarrow \text{no-duplicates}(\text{append}(lst, \text{list}(y)))$

THEOREM: labels-unique-append2

all-labels-unique (append (*lst1*, cons (*x*, cons (*y*, *lst2*))))
 \rightarrow all-labels-unique (append (*lst1*, list (*y*)))

THEOREM: find-labelp-member-collect-labels

find-labelp (*x*, *code*) \rightarrow (*x* \in collect-labels (*code*))

DEFINITION:

label-hole-big-enough (*cinfo*, *cond-list*, *stmt*, *proc-list*, *y*)
 $=$ all-labels-unique (append (code (translate (*cinfo*,
cond-list,
stmt,
proc-list))),
y))

THEOREM: labels-unique-not-find-labelp

(all-labels-unique (append (*code1*, *code2*)) \wedge find-labelp (*label*, *code2*))
 \rightarrow (\neg find-labelp (*label*, *code1*))

THEOREM: labels-unique-not-find-labelp1

all-labels-unique (append (*lst*, list (list ('dl, *label*, nil, *w*))))
 \rightarrow (find-labelp (*label*, *lst*) = f)

DEFINITION:

ok-cond-list (*lst*)
 $=$ if *lst* \simeq nil then *lst* = nil
else (ok-mg-namep (car (*lst*))
 \vee (car (*lst*) \in ' (leave routineerror)))
 \wedge ok-cond-list (cdr (*lst*)) endif

THEOREM: identifier-plistp-make-cond-list-ok

identifier-plistp (*lst*) \rightarrow ok-cond-list (*lst*)

THEOREM: make-cond-list-ok

((car (*stmt*) = 'proc-call-mg)
 \wedge ok-mg-statement (*stmt*, *cond-list*, *name-alist*, *proc-list*)
 \wedge ok-mg-def-plistp (*proc-list*)
 \rightarrow ok-cond-list (make-cond-list (fetch-called-def (*stmt*, *proc-list*))))

THEOREM: cond-subsetp-preserves-ok-mg-statep

(cond-subsetp (*r-cond-list*, *t-cond-list*)
 \wedge (cc (*mg-state*) \neq 'leave)
 \wedge ok-mg-statep (*mg-state*, *r-cond-list*)
 \rightarrow ok-mg-statep (*mg-state*, *t-cond-list*))

DEFINITION:

ok-translation-parameters(*cinfo*, *cond-list*, *stmt*, *proc-list*, *y*)
 = (ok-cinfo(*cinfo*)
 \wedge ok-cond-list(*cond-list*)
 \wedge label-hole-big-enough(*cinfo*, *cond-list*, *stmt*, *proc-list*, *y*))

THEOREM: label-cnt-monotonic

label-cnt(translate(*cinfo*, *cond-list*, *stmt*, *proc-list*)) $\not\prec$ label-cnt(*cinfo*)

THEOREM: label-cnt-monotonic2

(*n* < label-cnt(*cinfo*))
 \rightarrow (*n* < label-cnt(translate(*cinfo*, *cond-list*, *stmt*, *proc-list*)))

THEOREM: label-cnt-monotonic3

(*n* < label-cnt(*cinfo*))
 \rightarrow ((*n* < label-cnt(translate(*cinfo*, *cond-list*, *stmt*, *proc-list*))) = **t**)

THEOREM: label-cnt-add1-add1-monotonic

((*n* < *lc*) \wedge (label-cnt(*cinfo*) = (1 + (1 + *lc*))))
 \rightarrow ((*n* < label-cnt(translate(*cinfo*, *cond-list*, *stmt*, *proc-list*))) = **t**)

THEOREM: label-cnt-monotonic-cond-conversion

(*n* < *lc*)
 \rightarrow (find-labelp(*n*, cond-conversion(*actual-conds*, *lc*, *cond-list*, *label-alist*))
 = **f**)

THEOREM: not-find-labelp-push-parameters-code

find-labelp(*n*, push-parameters-code(*locals*, *actuals*)) = **f**

EVENT: Disable not-find-labelp-push-parameters-code.

THEOREM: find-labelp-monotonic-lessp

((*n* < label-cnt(*cinfo*)) \wedge (\neg find-labelp(*n*, code(*cinfo*))))
 \rightarrow (find-labelp(*n*, code(translate(*cinfo*, *cond-list*, *stmt*, *proc-list*))) = **f**)

;; The following definition is used only in the proof of procedure-calls.

DEFINITION:

label-cnt-big-enough(*lc*, *code*)
 = **if** *code* \simeq **nil** **then** **t**
 elseif caar(*code*) = 'd1
 then (cadar(*code*) < *lc*) \wedge label-cnt-big-enough(*lc*, cdr(*code*))
 else label-cnt-big-enough(*lc*, cdr(*code*)) **endif**

DEFINITION:

cond-conversion-induction-hint (*lst*, *n*)
 = **if** *lst* \simeq **nil** **then** **t**
 else cond-conversion-induction-hint (cdr (*lst*), 1 + *n*) **endif**

THEOREM: label-count-big-enough-not-find-labelp
 label-cnt-big-enough (*lc*, *code*) \rightarrow (find-labelp (*lc*, *code*) = **f**)

THEOREM: greater-label-count-big-enough
 (label-cnt-big-enough (*n*, *code*) \wedge (*n* \leq *m*))
 \rightarrow label-cnt-big-enough (*m*, *code*)

THEOREM: label-cnt-big-enough-distributes
 label-cnt-big-enough (*lc*, append (*lst1*, *lst2*))
 = (label-cnt-big-enough (*lc*, *lst1*) \wedge label-cnt-big-enough (*lc*, *lst2*))

THEOREM: label-cnt-lessp1
 (*n* < label-cnt (*cinfo*))
 \rightarrow ((*n* < label-cnt (translate (*cinfo*, cond-list, stmt, proc-list))) = **t**)

THEOREM: label-cnt-big-enough-distributes2
 (label-cnt-big-enough (*n*, *lst1*) \wedge label-cnt-big-enough (*n*, *lst2*))
 \rightarrow label-cnt-big-enough (*n*, append (*lst1*, *lst2*))

THEOREM: label-cnt-big-enough-for-push-actuals-code
 label-cnt-big-enough (*n*, push-actuals-code (*actuals*))

THEOREM: label-cnt-big-enough-for-push-local-array-values-code
 label-cnt-big-enough (*n*, push-local-array-values-code (*array-value*))

THEOREM: label-cnt-big-enough-for-push-locals-values-code
 label-cnt-big-enough (*n*, push-locals-values-code (*actuals*))

THEOREM: label-cnt-big-enough-for-push-locals-addresses-code
 label-cnt-big-enough (*n*, push-locals-addresses-code (*actuals*, *m*))

THEOREM: label-cnt-big-enough-for-cond-conversion
 label-cnt-big-enough (*lc* + (1 + (1 + length (*lst*))),
 cond-conversion (*lst*, 1 + (1 + *lc*), cond-list, label-alist))

THEOREM: label-cnt-big-enough-for-proc-call-code
 label-cnt-big-enough (label-cnt (*cinfo*), code (*cinfo*))
 \rightarrow label-cnt-big-enough (label-cnt (*cinfo*)
 + (1 + (1 + length (call-conds (*stmt*)))),
 proc-call-code (*cinfo*, *stmt*, cond-list, locals, *k*))

THEOREM: label-cnt-big-enough-for-predefined-proc-call-code
 $\text{label-cnt-big-enough}(n, \text{predefined-proc-call-sequence}(\text{stmt}, \text{label-alist}))$

THEOREM: label-cnt-stays-big-enough
 $\text{label-cnt-big-enough}(\text{label-cnt}(\text{cinfo}), \text{code}(\text{cinfo}))$
 $\rightarrow \text{label-cnt-big-enough}(\text{label-cnt}(\text{translate}(\text{cinfo},$
 $\text{cond-list},$
 $\text{stmt},$
 $\text{proc-list})),$
 $\text{code}(\text{translate}(\text{cinfo}, \text{cond-list}, \text{stmt}, \text{proc-list})))$

THEOREM: label-cnt-big-enough-add1
 $\text{label-cnt-big-enough}(x, y) \rightarrow \text{label-cnt-big-enough}(1 + x, y)$

THEOREM: lesser-label-doesnt-disturb-no-duplicates
 $(\text{no-duplicates}(\text{lst}) \wedge (x \notin \text{lst})) \rightarrow \text{no-duplicates}(\text{append}(\text{lst}, \text{list}(x)))$

THEOREM: find-labelp-reduces-to-member
 $\text{find-labelp}(x, \text{lst}) = (x \in \text{collect-labels}(\text{lst}))$

THEOREM: member-labels-unique-not-find-labelp
 $(\text{all-labels-unique}(\text{append}(\text{code}, \text{code2})) \wedge \text{find-labelp}(\text{label}, \text{code2}))$
 $\rightarrow (\neg \text{find-labelp}(\text{label}, \text{code}))$

THEOREM: no-duplicates-right-cons-reduction
 $\text{no-duplicates}(\text{collect-labels}(\text{lst}))$
 $\rightarrow (\text{no-duplicates}(\text{append}(\text{collect-labels}(\text{lst}), \text{list}(x)))$
 $= (\neg \text{find-labelp}(x, \text{lst})))$

THEOREM: label-cnt-big-enough-not-find-labelp
 $\text{label-cnt-big-enough}(lc, \text{code}) \rightarrow (\text{find-labelp}(lc, \text{code}) = \mathbf{f})$

THEOREM: not-member-cond-conversion
 $(n < lc)$
 $\rightarrow ((n \in \text{collect-labels}(\text{cond-conversion}(\text{conds}, lc, \text{cond-list}, \text{label-alist})))$
 $= \mathbf{f})$

THEOREM: no-duplicates-cond-conversion
 $\text{no-duplicates}(\text{collect-labels}(\text{cond-conversion}(\text{conds}, lc, \text{cond-list}, \text{label-alist})))$

THEOREM: no-duplicates-cond-conversion-base-case
 $\text{no-duplicates}(\text{append}(\text{collect-labels}(\text{cond-conversion}(\text{conds},$
 $1 + (1 + lc),$
 $\text{cond-list},$
 $\text{label-alist})),$
 $\text{list}(1 + lc)))$

THEOREM: no-duplicates-proc-call
 (no-duplicates (collect-labels (*code*)) \wedge label-cnt-big-enough (*lc*, *code*))
 \rightarrow no-duplicates (append (collect-labels (*code*),
 cons (*lc*,
 append (collect-labels (cond-conversion (*conds*,
 1 + (1 + *lc*),
 cond-list,
 label-alist)),
 list (1 + *lc*))))))

THEOREM: collect-labels-push-actuals-code-nil
 collect-labels (push-actuals-code (*actuals*)) = **nil**

THEOREM: collect-labels-push-local-array-values-code-nil
 collect-labels (push-local-array-values-code (*array-value*)) = **nil**

THEOREM: collect-labels-push-locals-values-code-nil
 collect-labels (push-locals-values-code (*actuals*)) = **nil**

THEOREM: collect-labels-push-locals-addresses-code-nil
 collect-labels (push-locals-addresses-code (*actuals*, *m*)) = **nil**

THEOREM: collect-labels-predefined-proc-call-code-nil
 collect-labels (predefined-proc-call-sequence (*stmt*, *label-alist*)) = **nil**

THEOREM: collect-labels-strip-label
 collect-labels (cons (cons ('**dl**, cons (*label*, *x*)), *y*))
 = cons (*label*, collect-labels (*y*))

THEOREM: labels-unique-loop-case
 ((car (*stmt*) = '**loop-mg**)
 \wedge no-duplicates (collect-labels (code (*cinfo*)))
 \wedge label-cnt-big-enough (label-cnt (*cinfo*), code (*cinfo*))
 \wedge ((no-duplicates (collect-labels (code (make-cinfo (append (code (*cinfo*),
 list (cons ('**dl**,
 cons (label-cnt (*cinfo*),
 '**(nil**
 (**no-op**)))))),
 cons (cons ('**leave**,
 1 + label-cnt (*cinfo*),
 label-alist (*cinfo*),
 1 + (1 + label-cnt (*cinfo*)))))))))
 \wedge label-cnt-big-enough (label-cnt (make-cinfo (append (code (*cinfo*),
 list (cons ('**dl**,
 cons (label-cnt (*cinfo*),

```

                                '(nil
                                (no-op))))),
                                cons (cons ('leave,
                                1 + label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))),
                                code (make-cinfo (append (code (cinfo),
                                list (cons ('dl,
                                cons (label-cnt (cinfo),
                                '(nil
                                (no-op)))))),
                                cons (cons ('leave,
                                1 + label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))))))
→ no-duplicates (collect-labels (code (translate (make-cinfo (append (code (cinfo),
                                list (cons ('dl,
                                cons (label-cnt (cinfo),
                                '(nil
                                (no-op)))))),
                                cons (cons ('leave,
                                1 + label-cnt (cinfo)),
                                label-alist (cinfo)),
                                1 + (1 + label-cnt (cinfo))),
                                cond-list,
                                loop-body (stmt),
                                proc-list))))))
→ no-duplicates (collect-labels (code (translate (cinfo,
                                cond-list,
                                stmt,
                                proc-list))))

```

EVENT: Disable labels-unique-loop-case.

THEOREM: labels-unique-if-case-hyps1

```

((car (stmt) = 'if-mg)
 ∧ no-duplicates (collect-labels (code (cinfo)))
 ∧ label-cnt-big-enough (label-cnt (cinfo), code (cinfo)))
→ (no-duplicates (collect-labels (code (make-cinfo (append (code (cinfo),
                                list (list ('push-local,
                                if-condition (stmt)),
                                '(fetch-temp-stk),
                                list ('test-bool-and-jump,
                                'false,

```

$$\begin{aligned}
& \text{label-cnt} (cinfo))) , \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo)))))) \\
\wedge \quad & \text{label-cnt-big-enough} (\text{label-cnt} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo))))), \\
& \text{code} (\text{make-cinfo} (\text{append} (\text{code} (cinfo), \\
& \quad \text{list} (\text{list} ('push-local, \\
& \quad \quad \text{if-condition} (stmt)), \\
& \quad \quad '(\text{fetch-temp-stk}), \\
& \quad \text{list} ('test-bool-and-jump, \\
& \quad \quad 'false, \\
& \quad \quad \text{label-cnt} (cinfo))))), \\
& \text{label-alist} (cinfo), \\
& 1 + (1 + \text{label-cnt} (cinfo))))))
\end{aligned}$$

EVENT: Disable labels-unique-if-case-hyps1.

THEOREM: label-cnt-big-enough-not-member
 $\text{label-cnt-big-enough} (lc, code) \rightarrow (lc \notin \text{collect-labels} (code))$

THEOREM: labels-unique-if-case-hyps2
 $((\text{car} (stmt) = 'if-mg)$
 $\wedge \quad \text{no-duplicates} (\text{collect-labels} (\text{code} (cinfo)))$
 $\wedge \quad \text{label-cnt-big-enough} (\text{label-cnt} (cinfo), \text{code} (cinfo))$
 $\wedge \quad \text{no-duplicates} (\text{collect-labels} (\text{code} (\text{translate} (\text{make-cinfo} (\text{append} (\text{code} (cinfo),$
 $\quad \text{list} (\text{list} ('push-local,$
 $\quad \quad \text{if-condition} (stmt)),$
 $\quad \quad '(\text{fetch-temp-stk}),$
 $\quad \text{list} ('test-bool-and-jump,$
 $\quad \quad 'false,$
 $\quad \quad \text{label-cnt} (cinfo))))),$
 $\quad \text{label-alist} (cinfo),$
 $\quad 1 + (1 + \text{label-cnt} (cinfo))))),$
 $\quad cond-list,$
 $\quad \text{if-true-branch} (stmt),$
 $\quad proc-list))))))$
 $\rightarrow \quad (\text{no-duplicates} (\text{collect-labels} (\text{code} (\text{add-code} (\text{translate} (\text{make-cinfo} (\text{append} (\text{code} (cinfo),$

```

list (list ( 'push-local,
            if-condition (stmt)),
      ' (fetch-temp-stk),
      list ( 'test-bool-and-jump,
            'false,
            label-cnt (cinfo))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ( 'jump,
            1 + label-cnt (cinfo)),
      cons ( 'dl,
            cons (label-cnt (cinfo),
                  ' (nil
                    (no-op))))))
^ label-cnt-big-enough (label-cnt (add-code (translate (make-cinfo (append (code (cinfo),
list (list ( 'push-local,
            if-condition (stmt),
            ' (fetch-temp-stk),
            list ( 'test-bool-and-jump,
                  'false,
                  label-cnt (cinfo))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ( 'jump,
            1 + label-cnt (cinfo)),
      cons ( 'dl,
            cons (label-cnt (cinfo),
                  ' (nil
                    (no-op))))))
code (add-code (translate (make-cinfo (append (code (cinfo),
list (list ( 'push-local,
            if-condition (stmt),
            ' (fetch-temp-stk),
            list ( 'test-bool-and-jump,
                  'false,
                  label-cnt (cinfo))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),

```



```

cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
cons ('dl,
cons (label-cnt (cinfo),
'(nil
(no-op)))))))))

```

EVENT: Disable labels-unique-if-case-hyps2.

EVENT: Disable label-cnt-big-enough-not-member.

THEOREM: labels-unique-if-case

```

((car (stmt) = 'if-mg)
^ no-duplicates (collect-labels (code (cinfo)))
^ label-cnt-big-enough (label-cnt (cinfo), code (cinfo))
^ ((no-duplicates (collect-labels (code (add-code (translate (make-cinfo (append (code (cinfo),
list (list ('push-local,
if-condition (stmt)
'(fetch-temp-stk),
list ('test-bool-and-
'false,
label-cnt (cinfo))))
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
cons ('dl,
cons (label-cnt (cinfo),
'(nil
(no-op)))))))))
^ label-cnt-big-enough (label-cnt (add-code (translate (make-cinfo (append (code (cinfo),
list (list ('push-local,
if-condition (stmt)
'(fetch-temp-stk),
list ('test-bool-and-
'false,
label-cnt (cinfo))

```

```

label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
cons ('dl,
cons (label-cnt (cinfo),
' (nil
(no-op)))))),
code (add-code (translate (make-cinfo (append (code (cinfo),
list (list ('push-local,
if-condition (stmt)),
' (fetch-temp-stk),
list ('test-bool-and-jun
'false,
label-cnt (cinfo)))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))),
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
cons ('dl,
cons (label-cnt (cinfo),
' (nil
(no-op)))))))))
→ no-duplicates (collect-labels (code (translate (add-code (translate (make-cinfo (append (code (cinfo),
list (list ('pus
if-co
' (fetch
list ('tes
'fal
labe
label-alist (cinfo),
1 + (1 + label-cnt (ci
cond-list,
if-true-branch (stmt),
proc-list),
list (list ('jump,
1 + label-cnt (cinfo)),
cons ('dl,

```

```

cons (label-cnt (cinfo),
      '(nil
        (no-op))))),
cond-list,
if-false-branch (stmt),
proc-list))))
^ ((no-duplicates (collect-labels (code (make-cinfo (append (code (cinfo),
list (list ('push-local,
            if-condition (stmt)),
            '(fetch-temp-stk),
list ('test-bool-and-jump,
      'false,
      label-cnt (cinfo))))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))))))
^ label-cnt-big-enough (label-cnt (make-cinfo (append (code (cinfo),
list (list ('push-local,
            if-condition (stmt)),
            '(fetch-temp-stk),
list ('test-bool-and-jump,
      'false,
      label-cnt (cinfo))))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))))),
code (make-cinfo (append (code (cinfo),
list (list ('push-local,
            if-condition (stmt)),
            '(fetch-temp-stk),
list ('test-bool-and-jump,
      'false,
      label-cnt (cinfo))))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))))))
→ no-duplicates (collect-labels (code (translate (make-cinfo (append (code (cinfo),
list (list ('push-local,
            if-condition (stmt)),
            '(fetch-temp-stk),
list ('test-bool-and-jump,
      'false,
      label-cnt (cinfo))))),
label-alist (cinfo),
1 + (1 + label-cnt (cinfo))))),
cond-list,
if-true-branch (stmt),

```

→ no-duplicates (collect-labels (code (translate (*cinfo*,
cond-list,
stmt,
proc-list))))))

EVENT: Disable labels-unique-if-case.

THEOREM: labels-unique-begin-case-hyps

((car (*stmt*) = 'begin-mg)
 ∧ no-duplicates (collect-labels (code (*cinfo*)))
 ∧ label-cnt-big-enough (label-cnt (*cinfo*), code (*cinfo*))
 ∧ no-duplicates (collect-labels (code (translate (make-cinfo (code (*cinfo*),
 append (make-label-alist (when-labels (*stmt*),
 label-cnt (*cinfo*)),
 label-alist (*cinfo*)),
 1 + (1 + label-cnt (*cinfo*))),
cond-list,
 begin-body (*stmt*),
proc-list))))))
 → (no-duplicates (collect-labels (code (add-code (set-label-alist (translate (make-cinfo (code (*cinfo*),
 append (make-label-alist (when-labels (*stmt*),
 label-cnt (*cinfo*)),
 label-alist (*cinfo*)),
 1 + (1 + label-cnt (*cinfo*))),
cond-list,
 begin-body (*stmt*),
proc-list),
 label-alist (*cinfo*)),
 cons (list ('jump,
 1 + label-cnt (*cinfo*)),
 cons (cons ('dl,
 cons (label-cnt (*cinfo*),
 ' (nil
 (push-constant
 (nat
 2))))),
 ' ((pop-global
 c-c))))))))))
 ∧ label-cnt-big-enough (label-cnt (add-code (set-label-alist (translate (make-cinfo (code (*cinfo*),
 append (make-label-alist (when-labels (*stmt*),
 label-cnt (*cinfo*)),
 label-alist (*cinfo*)),
 1 + (1 + label-cnt (*cinfo*))),
cond-list,
 begin-body (*stmt*),
proc-list),
 label-alist (*cinfo*)),
 cons (list ('jump,
 1 + label-cnt (*cinfo*)),
 cons (cons ('dl,
 cons (label-cnt (*cinfo*),
 ' (nil
 (push-constant
 (nat
 2))))),
 ' ((pop-global
 c-c))))))))))

```

cond-list,
begin-body (stmt),
proc-list),
label-alist (cinfo)),
cons (list ('jump,
1 + label-cnt (cinfo)),
cons (cons ('dl,
cons (label-cnt (cinfo),
' (nil
(push-constant
(nat
2))))),
' ((pop-global
c-c))))),
code (add-code (set-label-alist (translate (make-cinfo (code (cinfo),
append (make-label-alist
label-alist (cinfo)
1 + (1 + label-cnt (cinfo),
cond-list,
begin-body (stmt),
proc-list),
label-alist (cinfo)),
cons (list ('jump,
1 + label-cnt (cinfo)),
cons (cons ('dl,
cons (label-cnt (cinfo),
' (nil
(push-constant
(nat
2))))),
' ((pop-global
c-c))))))))))

```

EVENT: Disable labels-unique-begin-case-hyps.

```

(prove-lemma labels-unique-begin-case (rewrite)
  (IMPLIES
    (AND (equal (car STMT) 'BEGIN-MG)
      (NO-DUPPLICATES (COLLECT-LABELS (CODE CINFO)))
      (LABEL-CNT-BIG-ENOUGH (LABEL-CNT CINFO) (CODE CINFO))
      (IMPLIES

```



```

(LABEL-ALIST CINFO))
(ADD1 (ADD1 (LABEL-CNT CINFO))))
  COND-LIST
  (BEGIN-BODY STMT)
  PROC-LIST)
(LABEL-ALIST CINFO))
(CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
  (CONS (CONS 'DL
    (CONS (LABEL-CNT CINFO)
      '(NIL (PUSH-CONSTANT (NAT 2))))))
    '((POP-GLOBAL C-C))))))
(NO-DUPPLICATES
  (COLLECT-LABELS
    (CODE
      (TRANSLATE
        (ADD-CODE
          (SET-LABEL-ALIST
            (TRANSLATE (MAKE-CINFO (CODE CINFO)
              (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
                (LABEL-CNT CINFO))
                (LABEL-ALIST CINFO))
              (ADD1 (ADD1 (LABEL-CNT CINFO))))
            COND-LIST
            (BEGIN-BODY STMT)
            PROC-LIST)
            (LABEL-ALIST CINFO))
            (CONS (LIST 'JUMP (ADD1 (LABEL-CNT CINFO)))
              (CONS (CONS 'DL
                (CONS (LABEL-CNT CINFO)
                  '(NIL (PUSH-CONSTANT (NAT 2))))))
                '((POP-GLOBAL C-C))))))
            COND-LIST
            (WHEN-HANDLER STMT)
            PROC-LIST))))))
    (IMPLIES
      (AND
        (NO-DUPPLICATES
          (COLLECT-LABELS
            (CODE (MAKE-CINFO (CODE CINFO)
              (APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
                (LABEL-CNT CINFO))
                (LABEL-ALIST CINFO))
              (ADD1 (ADD1 (LABEL-CNT CINFO))))))
          (LABEL-CNT-BIG-ENOUGH

```

```

(LABEL-CNT (MAKE-CINFO (CODE CINFO)
(APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
(LABEL-CNT CINFO))
(LABEL-ALIST CINFO))
(ADD1 (ADD1 (LABEL-CNT CINFO))))))
(CODE (MAKE-CINFO (CODE CINFO)
(APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
(LABEL-CNT CINFO))
(LABEL-ALIST CINFO))
(ADD1 (ADD1 (LABEL-CNT CINFO))))))
(NO-DUPLICATES
(COLLECT-LABELS
(CODE (TRANSLATE (MAKE-CINFO (CODE CINFO)
(APPEND (MAKE-LABEL-ALIST (WHEN-LABELS STMT)
(LABEL-CNT CINFO))
(LABEL-ALIST CINFO))
(ADD1 (ADD1 (LABEL-CNT CINFO))))))
COND-LIST
(BEGIN-BODY STMT)
PROC-LIST))))))
(NO-DUPLICATES (COLLECT-LABELS (CODE (TRANSLATE CINFO COND-LIST STMT PROC-LIST))))))
((INSTRUCTIONS PROMOTE
(DEMOTE 5)
(DIVE 1 1)
S
(REWRITE LABEL-CNT-BIG-ENOUGH-ADD1)
UP S TOP PROMOTE
(DEMOTE 4)
(DIVE 1 1 1)
(REWRITE LABELS-UNIQUE-BEGIN-CASE-HYPS)
NX
(REWRITE LABELS-UNIQUE-BEGIN-CASE-HYPS)
UP UP S TOP PROMOTE
(DIVE 1 1 1)
(REWRITE BEGIN-TRANSLATION)
UP
(REWRITE CODE-ADD-CODE-COMMUTE)
UP
(REWRITE COLLECT-LABELS-DISTRIBUTES)
(DIVE 2)
(= *
(LIST (ADD1 (LABEL-CNT CINFO)))
((ENABLE COLLECT-LABELS)))
UP UP

```



```

(REWRITE NO-DUPPLICATES-RIGHT-CONS-REDUCTION)
(DIVE 1)
(REWRITE FIND-LABELP-MONOTONIC-LESSP)
UP S
(DIVE 2)
(REWRITE ADD-CODE-DOESNT-AFFECT-OTHER-FIELDS)
(REWRITE SET-LABEL-ALIST-DOESNT-AFFECT-OTHER-FIELDS)
UP
(REWRITE LABEL-CNT-LESSP1)
PROVE
(DIVE 1 2)
(REWRITE CODE-ADD-CODE-COMMUTE)
(DIVE 1)
(REWRITE SET-LABEL-ALIST-DOESNT-AFFECT-OTHER-FIELDS)
UP UP
(REWRITE FIND-LABELP-APPEND2)
(DIVE 3)
(= F)
TOP S
(DIVE 1)
(REWRITE FIND-LABELP-MONOTONIC-LESSP)
TOP S PROVE S
(DIVE 1)
(REWRITE LABEL-CNT-BIG-ENOUGH-NOT-FIND-LABELP)
TOP S
(REWRITE LABEL-CNT-BIG-ENOUGH-ADD1)
(DEMOTE 5)
S
(REWRITE LABEL-CNT-BIG-ENOUGH-ADD1)))

```

EVENT: Disable labels-unique-begin-case.

EVENT: Disable find-labelp-rewrites-to-member.

THEOREM: translate-leaves-labels-unique
 (no-duplicates (collect-labels (code (*cinfo*)))
 \wedge label-cnt-big-enough (label-cnt (*cinfo*), code (*cinfo*)))
 \rightarrow no-duplicates (collect-labels (code (translate (*cinfo*,
 cond-list,
 stmt,
 proc-list))))))

;; Note: many of the following lemmas may never be used, particularly the ones

;; involving assoc in the hyps.

THEOREM: translate-proc-list-assoc1

$$\begin{aligned} & (\text{definedp}(\text{subr}, \text{proc-list}) \wedge \text{ok-mg-def-plistp1}(\text{proc-list}, \text{proc-list2})) \\ \rightarrow & (\text{translate-def}(\text{assoc}(\text{subr}, \text{proc-list}), \text{proc-list2}) \\ & = \text{assoc}(\text{subr}, \text{translate-proc-list1}(\text{proc-list}, \text{proc-list2}))) \end{aligned}$$

EVENT: Disable translate-proc-list-assoc1.

THEOREM: translate-proc-list-assoc

$$\begin{aligned} & (\text{user-defined-procp}(\text{subr}, \text{proc-list}) \wedge \text{ok-mg-def-plistp}(\text{proc-list})) \\ \rightarrow & (\text{translate-def}(\text{assoc}(\text{subr}, \text{proc-list}), \text{proc-list}) \\ & = \text{assoc}(\text{subr}, \text{translate-proc-list}(\text{proc-list}))) \end{aligned}$$

EVENT: Disable translate-proc-list-assoc.

THEOREM: translate-proc-list-assoc2

$$\begin{aligned} & (\text{user-defined-procp}(\text{subr}, \text{proc-list}) \wedge \text{ok-mg-def-plistp}(\text{proc-list})) \\ \rightarrow & (\text{assoc}(\text{subr}, \text{translate-proc-list}(\text{proc-list})) \\ & = \text{translate-def}(\text{assoc}(\text{subr}, \text{proc-list}), \text{proc-list})) \end{aligned}$$

EVENT: Disable translate-proc-list-assoc2.

THEOREM: translate-definedp1

$$\begin{aligned} & (\text{ok-mg-def-plistp1}(\text{lst1}, \text{lst2}) \wedge \text{definedp}(x, \text{lst1})) \\ \rightarrow & \text{definedp}(x, \text{translate-proc-list1}(\text{lst1}, \text{lst2})) \end{aligned}$$

EVENT: Disable translate-definedp1.

THEOREM: assoc-mg-simple-variable-assignment-translate-proc-list

$$\begin{aligned} & \text{assoc}(\text{'mg-simple-variable-assignment}, \text{translate-proc-list}(\text{proc-list})) \\ = & \text{MG-SIMPLE-VARIABLE-ASSIGNMENT-TRANSLATION} \end{aligned}$$

THEOREM: assoc-mg-simple-constant-assignment-translate-proc-list

$$\begin{aligned} & \text{assoc}(\text{'mg-simple-constant-assignment}, \text{translate-proc-list}(\text{proc-list})) \\ = & \text{MG-SIMPLE-CONSTANT-ASSIGNMENT-TRANSLATION} \end{aligned}$$

THEOREM: assoc-mg-simple-variable-eq-translate-proc-list

$$\begin{aligned} & \text{assoc}(\text{'mg-simple-variable-eq}, \text{translate-proc-list}(\text{proc-list})) \\ = & \text{MG-SIMPLE-VARIABLE-EQ-TRANSLATION} \end{aligned}$$

THEOREM: assoc-mg-simple-constant-eq-translate-proc-list

$$\begin{aligned} & \text{assoc}(\text{'mg-simple-constant-eq}, \text{translate-proc-list}(\text{proc-list})) \\ = & \text{MG-SIMPLE-CONSTANT-EQ-TRANSLATION} \end{aligned}$$

THEOREM: assoc-mg-integer-le-translate-proc-list
 assoc ('mg-integer-le, translate-proc-list (*proc-list*))
 = MG-INTEGER-LE-TRANSLATION

THEOREM: assoc-mg-integer-unary-minus-translate-proc-list
 assoc ('mg-integer-unary-minus, translate-proc-list (*proc-list*))
 = MG-INTEGER-UNARY-MINUS-TRANSLATION

THEOREM: assoc-mg-integer-add-translate-proc-list
 assoc ('mg-integer-add, translate-proc-list (*proc-list*))
 = MG-INTEGER-ADD-TRANSLATION

THEOREM: assoc-mg-integer-subtract-translate-proc-list
 assoc ('mg-integer-subtract, translate-proc-list (*proc-list*))
 = MG-INTEGER-SUBTRACT-TRANSLATION

THEOREM: assoc-mg-boolean-or-translate-proc-list
 assoc ('mg-boolean-or, translate-proc-list (*proc-list*))
 = MG-BOOLEAN-OR-TRANSLATION

THEOREM: assoc-mg-boolean-and-translate-proc-list
 assoc ('mg-boolean-and, translate-proc-list (*proc-list*))
 = MG-BOOLEAN-AND-TRANSLATION

THEOREM: assoc-mg-boolean-not-translate-proc-list
 assoc ('mg-boolean-not, translate-proc-list (*proc-list*))
 = MG-BOOLEAN-NOT-TRANSLATION

THEOREM: assoc-mg-index-array-translate-proc-list
 assoc ('mg-index-array, translate-proc-list (*proc-list*))
 = MG-INDEX-ARRAY-TRANSLATION

THEOREM: assoc-mg-array-element-assignment-translate-proc-list
 assoc ('mg-array-element-assignment, translate-proc-list (*proc-list*))
 = MG-ARRAY-ELEMENT-ASSIGNMENT-TRANSLATION

THEOREM: assoc-user-defined-proc2
 (\neg predefined-procp (*subr*))
 \rightarrow (assoc (*subr*, translate-proc-list (*proc-list*))
 = assoc (*subr*, translate-proc-list1 (*proc-list*, *proc-list*)))

THEOREM: translate-def-body-rewrite
 (ok-mg-def-plistp (*proc-list*)
 \wedge user-defined-procp (*subr*, *proc-list*)
 \wedge (code (translate-def-body (assoc (*subr*, *proc-list*), *proc-list*))
 = append (code (translate (*cinfo*, *t-cond-list*, *stmt*, *proc-list*)),

$$\begin{aligned} & \text{code2})) \\ \rightarrow & \text{ (cdddr (assoc (subr, translate-proc-list (proc-list)))} \\ & = \text{ append (code (translate (cinfo, t-cond-list, stmt, proc-list)),} \\ & \text{code2))} \end{aligned}$$

EVENT: Disable translate-def-body-rewrite.

THEOREM: car-definedp-defined-procp1
 (user-defined-procp (*subr*, *proc-list*)
 \wedge ok-mg-def-plistp1 (*proc-list*, *proc-list2*)
 \rightarrow definedp (*subr*, translate-proc-list1 (*proc-list*, *proc-list2*))

EVENT: Disable car-definedp-defined-procp1.

THEOREM: car-definedp-defined-procp
 (user-defined-procp (*subr*, *proc-list*) \wedge ok-mg-def-plistp (*proc-list*)
 \rightarrow definedp (*subr*, translate-proc-list (*proc-list*))

EVENT: Disable car-definedp-defined-procp.

```

;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
;;                                                                 ;;
;;                                                                 ;;
;;                                CLOCK                                ;;
;;                                                                 ;;
;;                                                                 ;;
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;

```

```

;; The time required for a call to a predefined procedure is the sum of
;; the time for the call sequence and that spent in the body. The call
;; sequence is fixed but the body may have various paths.

```

DEFINITION:
 clock-predefined-proc-call-sequence (*name*)
 = **case on** *name*:
 case = *mg-simple-variable-assignment*
 then 3
 case = *mg-simple-constant-assignment*
 then 3
 case = *mg-simple-variable-eq*
 then 4
 case = *mg-simple-constant-eq*
 then 4
 case = *mg-integer-le*

```

    then 4
case = mg-integer-unary-minus
    then 6
case = mg-integer-add
    then 7
case = mg-integer-subtract
    then 7
case = mg-boolean-or
    then 4
case = mg-boolean-and
    then 4
case = mg-boolean-not
    then 3
case = mg-index-array
    then 8
case = mg-array-element-assignment
    then 8
otherwise 0 endcase

```

EVENT: Disable clock-predefined-proc-call-sequence.

DEFINITION:

clock-predefined-proc-call-body-translation (*stmt*, *mg-state*)

```

= case on call-name (stmt):
    case = mg-simple-variable-assignment
    then 5
    case = mg-simple-constant-assignment
    then 4
    case = mg-simple-variable-eq
    then 8
    case = mg-simple-constant-eq
    then 7
    case = mg-integer-le
    then 9
    case = mg-integer-unary-minus
    then if small-integerp (inegate (untag (caddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))),
                                MG-WORD-SIZE) then 11
    else 10 endif
    case = mg-integer-add
    then if small-integerp (iplus (untag (caddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))),
                                untag (caddr (assoc (caddr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))),

```

```

                                MG-WORD-SIZE) then 13
      else 11 endif
case = mg-integer-subtract
  then if small-integerp (idifference (untag (caddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))),
                                     untag (caddr (assoc (caddr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))),
                                MG-WORD-SIZE) then 13
      else 11 endif
case = mg-boolean-or
  then 8
case = mg-boolean-and
  then 8
case = mg-boolean-not
  then 6
case = mg-index-array
  then if negativep (cadaddr (assoc (caddr (call-actuals (stmt)),
                                                                mg-alist (mg-state)))) then 7
    elseif (idifference (caddr (call-actuals (stmt)),
                                     cadaddr (assoc (caddr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))
              = 0)
      ∨ negativep (idifference (caddr (call-actuals (stmt)),
                                     cadaddr (assoc (caddr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))))
    then 11
  else 17 endif
case = mg-array-element-assignment
  then if negativep (cadaddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state)))) then 7
    elseif (idifference (caddr (call-actuals (stmt)),
                                     cadaddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))
              = 0)
      ∨ negativep (idifference (caddr (call-actuals (stmt)),
                                     cadaddr (assoc (cadr (call-actuals (stmt)),
                                                                mg-alist (mg-state))))))
    then 11
  else 17 endif
otherwise 0 endcase

```

EVENT: Disable clock-predefined-proc-call-body-translation.

DEFINITION:

```

predefined-proc-call-clock (stmt, mg-state)
= (clock-predefined-proc-call-sequence (call-name (stmt))
  + clock-predefined-proc-call-body-translation (stmt, mg-state))

```

EVENT: Disable predefined-proc-call-clock.

```
;; Removed the definition of clock-r
```

DEFINITION:

```

clock (stmt, proc-list, mg-state, n)
= if (n  $\simeq$  0)  $\vee$  ( $\neg$  normal (mg-state)) then 0
  else case on car (stmt):
    case = no-op-mg
    then 0
    case = signal-mg
    then 3
    case = prog2-mg
    then clock (prog2-left-branch (stmt),
      proc-list,
      mg-state,
      n - 1)
      + clock (prog2-right-branch (stmt),
        proc-list,
        mg-meaning (prog2-left-branch (stmt),
          proc-list,
          mg-state,
          n - 1),
          n - 1)
    case = loop-mg
    then if  $\neg$  normal (mg-meaning (loop-body (stmt),
      proc-list,
      mg-state,
      n - 1))
      then if cc (mg-meaning (loop-body (stmt),
        proc-list,
        mg-state,
        n - 1))
        = 'leave
        then 3 + clock (loop-body (stmt),
          proc-list,
          mg-state,
          n - 1)
        else 1 + clock (loop-body (stmt),

```

```

                                proc-list,
                                mg-state,
                                n - 1) endif
else 1 + ((1 + clock(loop-body(stmt),
                                proc-list,
                                mg-state,
                                n - 1))
+ clock(stmt,
        proc-list,
        mg-meaning(loop-body(stmt),
                        proc-list,
                        mg-state,
                        n - 1),
        n - 1)) endif
case = if-mg
then if mg-expression-falsep(if-condition(stmt), mg-state)
then if normal(mg-meaning(if-false-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1))
then 5 + clock(if-false-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1)
else 4 + clock(if-false-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1) endif
elseif normal(mg-meaning(if-true-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1))
then 5 + clock(if-true-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1)
else 3 + clock(if-true-branch(stmt),
                                proc-list,
                                mg-state,
                                n - 1) endif
case = begin-mg
then if cc(mg-meaning(begin-body(stmt),
                                proc-list,
                                mg-state,

```



```

       $n - 1$ ))
    ∈ when-labels ( $stmt$ )
then if normal (mg-meaning (when-handler ( $stmt$ ),
       $proc-list$ ,
      set-condition (mg-meaning (begin-body ( $stmt$ ),
         $proc-list$ ,
         $mg-state$ ,
         $n - 1$ ),
        'normal),
       $n - 1$ ))
    then clock (begin-body ( $stmt$ ),
       $proc-list$ ,
       $mg-state$ ,
       $n - 1$ )
    + (3 + clock (when-handler ( $stmt$ ),
       $proc-list$ ,
      set-condition (mg-meaning (begin-body ( $stmt$ ),
         $proc-list$ ,
         $mg-state$ ,
         $n - 1$ ),
        'normal),
       $n - 1$ ))
    else clock (begin-body ( $stmt$ ),
       $proc-list$ ,
       $mg-state$ ,
       $n - 1$ )
    + (2 + clock (when-handler ( $stmt$ ),
       $proc-list$ ,
      set-condition (mg-meaning (begin-body ( $stmt$ ),
         $proc-list$ ,
         $mg-state$ ,
         $n - 1$ ),
        'normal),
       $n - 1$ )) endif
elseif normal (mg-meaning (begin-body ( $stmt$ ),
       $proc-list$ ,
       $mg-state$ ,
       $n - 1$ ))
then 2 + clock (begin-body ( $stmt$ ),
       $proc-list$ ,
       $mg-state$ ,
       $n - 1$ )
else clock (begin-body ( $stmt$ ),
       $proc-list$ ,

```

```

                                mg-state,
                                n - 1) endif
case = proc-call-mg
  then data-length (def-locals (fetch-called-def (stmt,
                                                    proc-list)))
    + length (def-locals (fetch-called-def (stmt,
                                                    proc-list)))
    + length (call-actuals (stmt))
    + 1
    + clock (def-body (fetch-called-def (stmt,
                                          proc-list)),
              proc-list,
              make-call-environment (mg-state,
                                     stmt,
                                     fetch-called-def (stmt,
                                                         proc-list)),
              n - 1)
    + 5
    + if normal (mg-meaning (def-body (fetch-called-def (stmt,
                                                         proc-list)),
                               proc-list,
                               make-call-environment (mg-state,
                                                         stmt,
                                                         fetch-called-def (stmt,
                                                                               proc-list)),
                               n - 1)) then 1
      else 3 endif
case = predefined-proc-call-mg
  then predefined-proc-call-clock (stmt, mg-state)
  otherwise 0 endcase endif

```

THEOREM: clock-prog2

```

(car (stmt) = 'prog2-mg)
→ (clock (stmt, proc-list, mg-state, n)
   = if (n ≠ 0) ∧ normal (mg-state)
     then clock (prog2-left-branch (stmt), proc-list, mg-state, n - 1)
       + clock (prog2-right-branch (stmt),
                                     proc-list,
                                     mg-meaning (prog2-left-branch (stmt),
                                                                    proc-list,
                                                                    mg-state,
                                                                    n - 1),
                                     n - 1)
     else 0 endif)

```

THEOREM: clock-loop

```

(car (stmt) = 'loop-mg)
→ (clock (stmt, proc-list, mg-state, n)
   =  if (n ≠ 0) ∧ normal (mg-state)
      then if ¬ normal (mg-meaning (loop-body (stmt),
                                     proc-list,
                                     mg-state,
                                     n - 1))
          then if cc (mg-meaning (loop-body (stmt),
                                     proc-list,
                                     mg-state,
                                     n - 1))
              = 'leave
          then 3 + clock (loop-body (stmt),
                          proc-list,
                          mg-state,
                          n - 1)
          else 1 + clock (loop-body (stmt),
                          proc-list,
                          mg-state,
                          n - 1) endif
      else 1 + ((1 + clock (loop-body (stmt),
                              proc-list,
                              mg-state,
                              n - 1))
                + clock (stmt,
                          proc-list,
                          mg-meaning (loop-body (stmt),
                                      proc-list,
                                      mg-state,
                                      n - 1),
                          n - 1)) endif
      else 0 endif)

```

EVENT: Disable clock-loop.

THEOREM: clock-if

```

(car (stmt) = 'if-mg)
→ (clock (stmt, proc-list, mg-state, n)
   =  if (n ≠ 0) ∧ normal (mg-state)
      then if mg-expression-falsep (if-condition (stmt), mg-state)
          then if normal (mg-meaning (if-false-branch (stmt),
                                      proc-list,
                                      mg-state,

```

```

                                 $n - 1$ )
then 5 + clock (if-false-branch ( $stmt$ ),
                                 $proc-list$ ,
                                 $mg-state$ ,
                                 $n - 1$ )
else 4 + clock (if-false-branch ( $stmt$ ),
                                 $proc-list$ ,
                                 $mg-state$ ,
                                 $n - 1$ ) endif
elseif normal (mg-meaning (if-true-branch ( $stmt$ ),
                                 $proc-list$ ,
                                 $mg-state$ ,
                                 $n - 1$ ))
then 5 + clock (if-true-branch ( $stmt$ ),
                                 $proc-list$ ,
                                 $mg-state$ ,
                                 $n - 1$ )
else 3 + clock (if-true-branch ( $stmt$ ),
                                 $proc-list$ ,
                                 $mg-state$ ,
                                 $n - 1$ ) endif
else 0 endif)

```

THEOREM: clock-begin

(car ($stmt$) = 'begin-mg)

→ (clock ($stmt$, $proc-list$, $mg-state$, n)

= **if** ($n \neq 0$) \wedge normal ($mg-state$)

then if cc (mg-meaning (begin-body ($stmt$),

$proc-list$,

$mg-state$,

$n - 1$))

∈ when-labels ($stmt$)

then if normal (mg-meaning (when-handler ($stmt$),

$proc-list$,

set-condition (mg-meaning (begin-body ($stmt$),

$proc-list$,

$mg-state$,

$n - 1$),

'normal),

$n - 1$))

then clock (begin-body ($stmt$),

$proc-list$,

$mg-state$,

$n - 1$)

```

+ (3 + clock (when-handler (stmt),
                        proc-list,
                        set-condition (mg-meaning (begin-body (stmt),
                                                proc-list,
                                                mg-state,
                                                n - 1),
                                        'normal),
                        n - 1))
else clock (begin-body (stmt),
                proc-list,
                mg-state,
                n - 1)
+ (2 + clock (when-handler (stmt),
                        proc-list,
                        set-condition (mg-meaning (begin-body (stmt),
                                                proc-list,
                                                mg-state,
                                                n - 1),
                                        'normal),
                        n - 1)) endif
elseif normal (mg-meaning (begin-body (stmt),
                proc-list,
                mg-state,
                n - 1))
then 2 + clock (begin-body (stmt),
                proc-list,
                mg-state,
                n - 1)
else clock (begin-body (stmt),
                proc-list,
                mg-state,
                n - 1) endif
else 0 endif)

```

THEOREM: clock-proc-call

(car (stmt) = 'proc-call-mg)

→ (clock (stmt, proc-list, mg-state, n)

= **if** (n ≠ 0) ∧ normal (mg-state)

then data-length (def-locals (fetch-called-def (stmt, proc-list)))

+ length (def-locals (fetch-called-def (stmt, proc-list)))

+ length (call-actuals (stmt))

+ 1

+ clock (def-body (fetch-called-def (stmt, proc-list)),
proc-list,

```

                                make-call-environment (mg-state,
                                                         stmt,
                                                         fetch-called-def (stmt,
                                                         proc-list)),
                                n - 1)
+ 5
+ if normal (mg-meaning (def-body (fetch-called-def (stmt,
                                                         proc-list),
                                                         make-call-environment (mg-state,
                                                         stmt,
                                                         fetch-called-def (stmt,
                                                         proc-list)),
                                                         n - 1)) then 1
                                else 3 endif
else 0 endif)

```

THEOREM: clock-predefined-proc-call
 (car (*stmt*) = 'predefined-proc-call-mg)
 → (clock (*stmt*, *proc-list*, *mg-state*, *n*)
 = **if** (*n* ≠ 0) ∧ normal (*mg-state*)
 then predefined-proc-call-clock (*stmt*, *mg-state*)
 else 0 **endif**)

DEFINITION:
 map-down (*mg-state*, *proc-list*, *ctrl-stk*, *temp-stk*, *addr*, *cond-list*)
 = p-state (*addr*,
 ctrl-stk,
 map-down-values (mg-alist (*mg-state*),
 bindings (top (*ctrl-stk*)),
 temp-stk),
 translate-proc-list (*proc-list*),
 list (list ('c-c, mg-cond-to-p-nat (cc (*mg-state*), *cond-list*))),
 MG-MAX-CTRL-STK-SIZE,
 MG-MAX-TEMP-STK-SIZE,
 MG-WORD-SIZE,
 'run)

```

;; I need the hyp that cc is not 'leave for this theorem because cond-subsetp does not
;; preserves ok-cc unless cond is not 'leave, but I can prove that meaning never
;; returns leave anyway.

```

THEOREM: map-up-vars-inverts-map-down
 (all-cars-unique (*mg-vars*))

$$\begin{aligned}
& \wedge \text{mg-alistp}(mg\text{-vars}) \\
& \wedge \text{no-p-aliasing}(bindings, mg\text{-vars}) \\
& \wedge \text{mg-vars-list-ok-in-p-state}(mg\text{-vars}, bindings, temp\text{-stk}) \\
\rightarrow & (\text{map-up-vars-list}(bindings, \\
& \qquad \qquad \text{map-down-values}(mg\text{-vars}, bindings, temp\text{-stk}), \\
& \qquad \qquad \text{signature}(mg\text{-vars})) \\
& = mg\text{-vars})
\end{aligned}$$

THEOREM: cond-subset-preserves-ok-cc

$$\begin{aligned}
& ((cc \neq \text{'leave}) \\
& \wedge \text{cond-subsetp}(r\text{-cond-list}, t\text{-cond-list}) \\
& \wedge \text{ok-cc}(cc, r\text{-cond-list})) \\
\rightarrow & \text{ok-cc}(cc, t\text{-cond-list})
\end{aligned}$$

THEOREM: map-up-inverts-map-down

$$\begin{aligned}
& (\text{all-cars-unique}(\text{mg-alist}(mg\text{-state})) \\
& \wedge \text{ok-mg-statep}(mg\text{-state}, r\text{-cond-list}) \\
& \wedge \text{cond-subsetp}(r\text{-cond-list}, t\text{-cond-list}) \\
& \wedge \text{mg-vars-list-ok-in-p-state}(\text{mg-alist}(mg\text{-state}), \\
& \qquad \qquad \text{bindings}(\text{top}(ctrl\text{-stk})), \\
& \qquad \qquad temp\text{-stk})) \\
& \wedge \text{no-p-aliasing}(\text{bindings}(\text{top}(ctrl\text{-stk})), \text{mg-alist}(mg\text{-state})) \\
& \wedge (cc(mg\text{-state}) \neq \text{'leave}) \\
& \wedge (\neg \text{resource-errorp}(mg\text{-state}))) \\
\rightarrow & (\text{map-up}(\text{map-down}(mg\text{-state}, \\
& \qquad \qquad \text{proc-list}, \\
& \qquad \qquad ctrl\text{-stk}, \\
& \qquad \qquad temp\text{-stk}, \\
& \qquad \qquad addr, \\
& \qquad \qquad t\text{-cond-list}), \\
& \qquad \text{signature}(\text{mg-alist}(mg\text{-state})), \\
& \qquad t\text{-cond-list}) \\
& = mg\text{-state})
\end{aligned}$$

;; These are used in the proofs which follow!

THEOREM: call-exact-time-hyps1

$$\begin{aligned}
& ((\text{car}(stmt) = \text{'proc-call-mg}) \\
& \wedge \text{ok-mg-statement}(stmt, r\text{-cond-list}, name\text{-alist}, proc\text{-list}) \\
& \wedge \text{ok-mg-def-plistp}(proc\text{-list})) \\
\rightarrow & \text{ok-mg-statement}(\text{def-body}(\text{fetch-called-def}(stmt, proc\text{-list}), \\
& \qquad \text{make-cond-list}(\text{fetch-called-def}(stmt, proc\text{-list})), \\
& \qquad \text{make-name-alist}(\text{fetch-called-def}(stmt, proc\text{-list})), \\
& \qquad proc\text{-list}))
\end{aligned}$$

THEOREM: resources-adequate-temp-stk-not-max
 $(\neg \text{resources-inadequatep}(\text{stmt},$
 $\quad \text{proc-list},$
 $\quad \text{list}(\text{length}(\text{temp-stk}), \text{p-ctrl-stk-size}(\text{ctrl-stk})))$
 $\rightarrow ((\text{length}(\text{temp-stk}) < \text{MG-MAX-TEMP-STK-SIZE}) = \mathbf{t})$

THEOREM: plus-difference-cancellation
 $((x - y) \neq 0) \rightarrow (((x - y) + y) = \text{fix}(x))$

THEOREM: lessp-difference-lemma1
 $((n < (r + l)) \wedge (r < (m - l))) \rightarrow ((n < m) = \mathbf{t})$

THEOREM: resources-adequate-temp-stk-not-max2
 $((\neg \text{resources-inadequatep}(\text{stmt},$
 $\quad \text{proc-list},$
 $\quad \text{list}(\text{length}(\text{temp-stk}), \text{p-ctrl-stk-size}(\text{ctrl-stk})))$
 $\wedge (\text{car}(\text{stmt}) = \text{'predefined-proc-call-mg'})$
 $\wedge (n < (\text{predefined-proc-call-temp-stk-requirement}(\text{call-name}(\text{stmt}))$
 $\quad + \text{length}(\text{temp-stk})))$
 $\rightarrow ((n < \text{MG-MAX-TEMP-STK-SIZE}) = \mathbf{t})$

THEOREM: lessp-difference-lemma3
 $((n \leq p) \wedge (p < (m - c))) \rightarrow ((m < (n + c)) = \mathbf{f})$

EVENT: Disable lessp-difference-lemma3.

THEOREM: resources-adequate-ctrl-stk-not-max
 $((\neg \text{resources-inadequatep}(\text{stmt},$
 $\quad \text{proc-list},$
 $\quad \text{list}(\text{length}(\text{temp-stk}), \text{p-ctrl-stk-size}(\text{ctrl-stk})))$
 $\wedge (\text{car}(\text{stmt}) = \text{'predefined-proc-call-mg'})$
 $\wedge (n \leq \text{predefined-proc-call-p-frame-size}(\text{call-name}(\text{stmt})))$
 $\rightarrow ((\text{MG-MAX-CTRL-STK-SIZE} < (n + \text{p-ctrl-stk-size}(\text{ctrl-stk}))) = \mathbf{f})$

THEOREM: lessp-transitive3
 $((y < n) \wedge (n < (m - x))) \rightarrow (((x + y) < m) = \mathbf{t})$

THEOREM: lessp-difference
 $(y < (m - x)) \rightarrow (((x + y) < m) = \mathbf{t})$

THEOREM: resources-proc-call-temp-stk-ok
 $((\text{car}(\text{stmt}) = \text{'proc-call-mg'})$
 $\wedge (\neg \text{resources-inadequatep}(\text{stmt},$
 $\quad \text{proc-list},$
 $\quad \text{list}(\text{length}(\text{temp-stk}),$

$$\begin{aligned}
& \rightarrow (((\text{length}(\text{temp-stk}) \\
& \quad + \text{data-length}(\text{def-locals}(\text{fetch-called-def}(\text{stmt}, \text{proc-list}))) \\
& \quad + \text{length}(\text{def-locals}(\text{fetch-called-def}(\text{stmt}, \text{proc-list}))) \\
& \quad + \text{length}(\text{call-actuals}(\text{stmt}))) \\
& \quad < \text{MG-MAX-TEMP-STK-SIZE}) \\
& \quad = \mathbf{t})
\end{aligned}$$

EVENT: Disable resources-proc-call-temp-stk-ok.

$$\begin{aligned}
& \text{THEOREM: user-defined-def-locals-nil} \\
& (\text{ok-mg-def-plistp}(\text{proc-list}) \\
& \quad \wedge (\text{car}(\text{stmt}) = \text{'proc-call-mg}) \\
& \quad \wedge \text{ok-mg-statement}(\text{stmt}, \text{r-cond-list}, \text{name-alist}, \text{proc-list})) \\
& \rightarrow (\text{length}(\text{caddr}(\text{assoc}(\text{call-name}(\text{stmt}), \text{translate-proc-list}(\text{proc-list})))) \\
& \quad = 0)
\end{aligned}$$

EVENT: Disable user-defined-def-locals-nil.

$$\begin{aligned}
& \text{THEOREM: user-defined-def-formals-rewrite} \\
& (\text{ok-mg-def-plistp}(\text{proc-list}) \\
& \quad \wedge (\text{car}(\text{stmt}) = \text{'proc-call-mg}) \\
& \quad \wedge \text{ok-mg-statement}(\text{stmt}, \text{r-cond-list}, \text{name-alist}, \text{proc-list})) \\
& \rightarrow (\text{length}(\text{cadr}(\text{assoc}(\text{call-name}(\text{stmt}), \text{translate-proc-list}(\text{proc-list})))) \\
& \quad = (\text{length}(\text{def-locals}(\text{assoc}(\text{call-name}(\text{stmt}), \text{proc-list}))) \\
& \quad \quad + \text{length}(\text{def-formals}(\text{assoc}(\text{call-name}(\text{stmt}), \text{proc-list}))))
\end{aligned}$$

EVENT: Disable user-defined-def-formals-rewrite.

$$\begin{aligned}
& \text{THEOREM: difference-preserves-lessp2} \\
& (n < m) \rightarrow (((n - k) < m) = \mathbf{t})
\end{aligned}$$

$$\begin{aligned}
& \text{THEOREM: plus-lessp} \\
& ((n + m + x) < (m + n)) = \mathbf{f}
\end{aligned}$$

$$\begin{aligned}
& \text{THEOREM: resources-proc-call-ctrl-stk-ok} \\
& ((\text{car}(\text{stmt}) = \text{'proc-call-mg}) \\
& \quad \wedge (\neg \text{resources-inadequatep}(\text{stmt}, \\
& \quad \quad \text{proc-list}, \\
& \quad \quad \text{list}(\text{length}(\text{temp-stk}), \\
& \quad \quad \text{p-ctrl-stk-size}(\text{ctrl-stk})))) \\
& \quad \wedge \text{ok-mg-statement}(\text{stmt}, \text{r-cond-list}, \text{name-alist}, \text{proc-list}) \\
& \quad \wedge \text{ok-mg-def-plistp}(\text{proc-list})
\end{aligned}$$

$$\begin{aligned}
& \wedge \text{ user-defined-procp } (subr, proc-list)) \\
\rightarrow & ((\text{MG-MAX-CTRL-STK-SIZE} \\
& < (2 \\
& \quad + \text{ length } (\text{cadr } (\text{assoc } (\text{call-name } (stmt), \\
& \quad \quad \quad \text{translate-proc-list } (proc-list)))) \\
& \quad + \text{ length } (\text{caddr } (\text{assoc } (\text{call-name } (stmt), \\
& \quad \quad \quad \text{translate-proc-list } (proc-list)))) \\
& \quad + \text{ p-ctrl-stk-size } (ctrl-stk))) \\
& = \text{ f})
\end{aligned}$$

EVENT: Disable resources-proc-call-ctrl-stk-ok.

EVENT: Make the library "c5".

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