

# Foundations of Computer Security

## Lecture 56: Cryptographic Protocols

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Consider the following scenario:

- Your friend Ivan lives in a repressive country where the police spy on everything and open all the mail.
- You need to send a valuable object to Ivan.
- You have a strongbox with a hasp big enough for several locks, but no lock to which Ivan also has a key.

How can you get the item to Ivan securely?

## A Possible Answer

You might take the following sequence of steps:

- 1 Put the item into the box, attach your lock to the hasp, and mail the box to Ivan.
- 2 Ivan adds his own lock and mails the box back to you.
- 3 You remove your lock and mail the box back to him. He now removes his lock and opens the box.

The procedure just described could be regarded as a *protocol*—a structured dialog intended to accomplish some communication-related goal.

## What's This Got to do with Computing?

**What goal:** To send some content confidentially in the context of a hostile or untrustworthy environment, when the two parties don't already share a secret/key.

You could implement the “same” protocol to send a message confidentially across the Internet. Here,

- the *valuable thing* is the contents of a secret message;
- the *locks* are applications of some cryptographic algorithm with appropriate *cryptographic keys*.

But for this to work in the computing world there's a particular feature that the ciphers have to satisfy. *Can you see what it is?*

## What is the Property?

Imagine that instead of putting another lock on the hasp, Ivan puts your lockbox inside another locked box. The protocol no longer works; you can't reach inside his box to take off your lock in step 3.

On-line, you'd have to be able to "reach inside" his encryption to undo yours. One way this would be true is if the ciphers *commute*.

$$\{\{M\}_{k_1}\}_{k_2} = \{\{M\}_{k_2}\}_{k_1}$$

Most encryption algorithms don't have this property. But one that does is: exclusive or (XOR) your message with a randomly generated string (key) of the same length.

## So Here's the Protocol

Let  $K_a$  be a random string generated by A, and  $K_b$  be a random string generated by B, both  $K_a$  and  $K_b$  of the same length as  $M$ .

- 1  $A \rightarrow B : M \oplus K_a$
- 2  $B \rightarrow A : (M \oplus K_a) \oplus K_b$
- 3  $A \rightarrow B : ((M \oplus K_a) \oplus K_b) \oplus K_a$

In step 3, the two applications of  $K_a$  "cancel out," leaving  $(M \oplus K_b)$ , which B can easily decrypt with his own key  $K_b$ .

## Whoops!

This is effectively using the one-time pad, so should be very strong. *Right?*

Even though the one-time pad is a theoretically unbreakable cipher, there's a good reason it's called "one-time." Our protocol is fundamentally flawed. *Can you see why?*

- 1  $A \rightarrow B : M \oplus K_a$
- 2  $B \rightarrow A : (M \oplus K_a) \oplus K_b$
- 3  $A \rightarrow B : ((M \oplus K_a) \oplus K_b) \oplus K_a$

An eavesdropper who stores the three messages can XOR combinations of them to extract any of  $M$ ,  $K_a$ , and  $K_b$ . *Verify this for yourself.*

## Lessons

- Cryptographic protocols accomplish security-related functions via a structured exchange of messages.
- They are very important to security on the Internet.
- They are difficult to design and easy to get wrong in subtle ways.

**Next lecture:** Cryptographic Protocols II