Performance Optimization

The following problem concerns optimizing a procedure for maximum performance on an Intel Pentium III. Recall the following performance characteristics of the functional units for this machine:

Operation	Latency	Issue Time
Integer Add	1	1
Integer Multiply	4	1
Integer Divide	36	36
Floating Point Add	3	1
Floating Point Multiply	5	2
Floating Point Divide	38	38
Load or Store (Cache Hit)	1	1

You've just joined a programming team that is trying to develop the world's fastest factorial routine. Starting with recursive factorial, they've converted the code to use iteration:

```
int fact(int n)
{
  int i;
  int result = 1;

  for (i = n; i > 0; i--)
    result = result * i;

  return result;
}
```

By doing so, they have reduced the number of cycles per element (CPE) for the function from around 63 to around 4 (really!). Still, they would like to do better.

Problem 39. (8 points):

One of the programmers heard about loop unrolling. He generated the following code:

```
int fact_u2(int n)
{
  int i;
  int result = 1;

  for (i = n; i > 0; i-=2) {
    result = (result * i) * (i-1);
  }

  return result;
}
```

Unfortunately, the team has discovered that this code returns 0 for some values of argument `n`.

A. For what values of `n` will `fact_u2` and `fact` return different values?

B. Show how to fix `fact_u2` so that its behavior is identical to `fact`. [Hint: there is a special trick for this procedure that involves modifying just a single character.]

C. Benchmarking `fact_u2` shows no improvement in performance. How would you explain that?

D. You modify the line inside the loop to read:

```
result = result * (i * (i-1));
```

To everyone's astonishment, the measured performance now has a CPE of 2.5. How do you explain this performance improvement?