

Problem 4. (12 points):

Consider the following 16-bit floating point representation based on the IEEE floating point format:

- There is a sign bit in the most significant bit.
- The next seven bits are the exponent. The exponent bias is 63.
- The last eight bits are the significand.

The rules are like those in the IEEE standard (normalized, denormalized, representation of 0, infinity, and NAN).

As described in Class 10, we consider the floating point format to encode numbers in a form:

$$(-1)^s \times m \times 2^E$$

where m is the *mantissa* and E is the exponent.

Fill in the table below for the following numbers, with the following instructions for each column:

Hex: The 4 hexadecimal digits describing the encoded form.

m : The fractional value of the mantissa. This should be a number of the form x or x/y , where x is an integer, and y is an integral power of 2. Examples include: 0, 67/64, and 1/256.

E : The integer value of the exponent.

Value: The numeric value represented. Use the notation x or $x \times 2^z$, where x and z are integers.

As an example, to represent the number $7/2$, we would have $s = 0$, $m = 7/4$, and $E = 1$. Our number would therefore have an exponent field of 0×40 (decimal value $63 + 1 = 64$) and a significand field $0 \times C0$ (binary 11000000_2), giving a hex representation $40C0$.

You need not fill in entries marked “—”.

Description	Hex	m	E	Value
−0				—
Smallest value > 1				
Largest Denormalized				
−∞		—	—	—
Number with hex representation 3AA0	—			