CS 323E

- 1. The MATLAB command hilb(n) generates an $n \times n$ Hilbert matrix, which we denote by H_n . Try n = 3, 10, 20 in the following problems:
 - a) (4 points) Solve:

$$H_n x_n = b_n$$

for x_n , where $b_n = H_n * \text{ones}(n, 1)$. Use the MATLAB command "\" to solve the above system. (See help mldivide).

- b) (2 points) How close is x_n to the exact solution? Comment.
- c) (4 points) Explain the accuracy of x_n . Use the command cond to get the condition number of H_n .
- 2. (5 points) Does the MATLAB command "\" do pivoting? Give an example to justify your answer.
- 3. (Use pen & paper). Let

$$A = \begin{bmatrix} 10^{-16} & 10^{-17} \\ -10^{-16} & 10^{-17} \end{bmatrix}$$

- a) (2 points) Compute the determinant of A.
- b) (5 points) Compute $\kappa_1(A) = ||A||_1 \cdot ||A^{-1}||_1$.
- c) (2 points)Is A nearly singular? Comment.
- d) (1 point)Does the small magnitude of the determinant imply that A is nearly singular?
- 4. The MATLAB command pascal(n) generates an $n \times n$ Pascal matrix, which we denote by P_n . Try n = 16 in the following.
 - a) (1 point) Using MATLAB, find the determinant of P_n .
 - b) (1 point) Using MATLAB, find the condition number of P_n .
 - c) (3 points) Is P_n close to singularity? Comment.