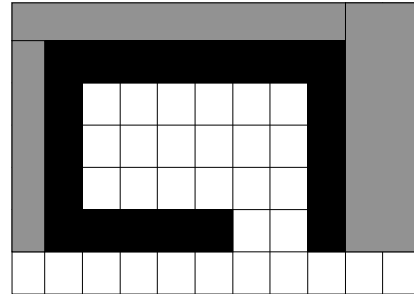


## Lecture 13: Occupancy Grids

CS 344R/393R: Robotics  
Benjamin Kuipers

### Occupancy Grid Map



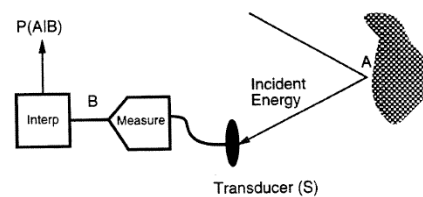
### Occupancy Grid Map

- Maps the environment as an array of cells.
  - Cell sizes range from 5 to 50 cm.
- Each cell holds a probability value
  - that the cell is occupied.
- Useful for combining different sensor scans, and even different sensor modalities.
  - Sonar, laser, IR, bump, etc.
- No assumption about type of features.
  - Static world, but with frequent updates.

### A Bit of History

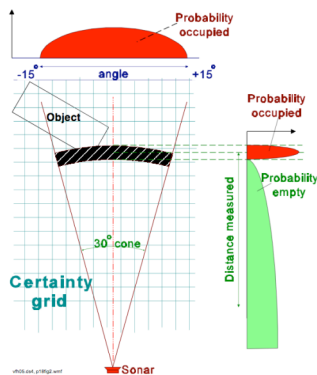
- Occupancy grids were first popularized by *Hans Moravec* and *Alberto Elfes* at CMU.
- *Kurt Konolige* at SRI made a number of valuable contributions.
  - Konolige's Erratic robot is the ancestor to the Amigobot. Konolige developed Saphira, too.
- *Hugh Durrant-Whyte* and *John Leonard* (then at Oxford) used landmarks and Kalman filters as an alternative.
- *Sebastian Thrun* (then CMU, now Stanford) has done very impressive metrical mapping work, which we will study.

### Sonar Sensors Give Evidence of Obstacles



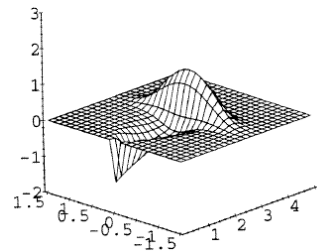
## Sonar Sweeps a Wide Cone

- Obstacle could be anywhere on the arc at distance D.
- The space closer than D is likely to be free.



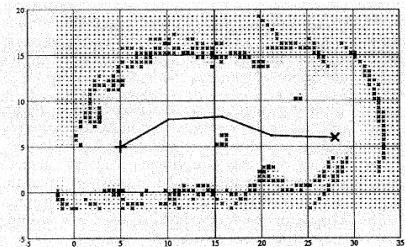
## Occupancy from Sonar Return

- One 2D Gaussian for information about occupancy.
- Another for free space.



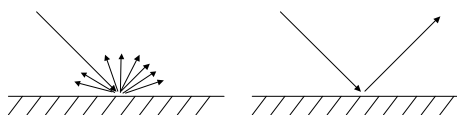
## Wide Sonar Cone Creates a Noisy Map

- From Moravec [1988]



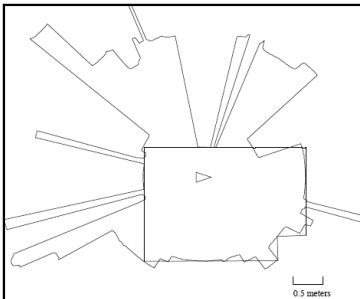
## Diffuse and Specular Reflections

- Diffuse
- Specular



## Specular Reflections in Sonar

- Specular (multi-path) reflections hallucinate free space.



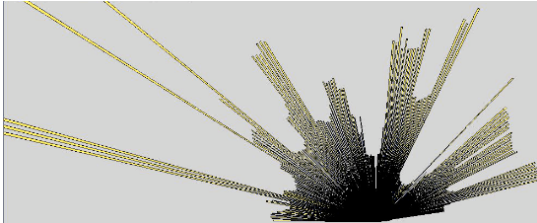
## Laser Range Finder

- 180 ranges over 180° planar field of view
- 10-12 scans/second
- 4 cm range resolution
- Max range 50-80 m.
- Problems with mirrors, glass, and matte black.
- Much better than sonar!



## Laser Rangefinder Image

- 180 narrow beams at 1° intervals.



## Occupancy Grid Cells $C_{ij}$

- The proposition  $occ(i,j)$  means:
  - The cell  $C_{ij}$  is occupied.
- **Probability:**  $p(occ(i,j))$  has range  $[0,1]$ .
- **Odds:**  $o(occ(i,j))$  has range  $[0,+\infty)$ .
 
$$o(A) = \frac{p(A)}{p(\neg A)}$$
- **Log odds:**  $\log o(occ(i,j))$  has range  $(-\infty, +\infty)$
- Each cell  $C_{ij}$  holds the value  $\log o(occ(i,j))$ 
  - $C_{ij} = 0$  corresponds to  $p(occ(i,j)) = 0.5$

## Probabilistic Occupancy Grids

- We will apply Bayes Law

$$p(A|B) = \frac{p(B|A) * p(A)}{p(B)}$$

- where  $A$  is  $occ(i,j)$
- and  $B$  is an observation  $r=D$

- We can simplify this by using the log odds representation.

## Bayes Law Using Odds

- Bayes Law:  $p(A|B) = \frac{p(B|A) * p(A)}{p(B)}$
- Likewise:  $p(\neg A|B) = \frac{p(B|\neg A) * p(\neg A)}{p(B)}$
- so:  $o(A|B) = \frac{p(A|B)}{p(\neg A|B)} = \frac{p(B|A) * p(A)}{p(B|\neg A) * p(\neg A)}$   
 $= \lambda(B|A) * o(A)$
- where:  $o(A|B) = \frac{p(A|B)}{p(\neg A|B)}$      $\lambda(B|A) = \frac{p(B|A)}{p(B|\neg A)}$

## Easy Update Using Bayes Law

- Bayes' Law can be written:

$$o(A|B) = \lambda(B|A) * o(A)$$

- Take log odds to make multiplication into addition.

$$\log o(A|B) = \log \lambda(B|A) + \log o(A)$$

- Easy update for cell contents.

## Occupancy Grid Cell Update

- Cell  $C_{ij}$  holds  $o(occ(i,j))$ .
- Evidence  $r=D$  means sensor  $r$  returns  $D$ .
- For each cell  $C_{ij}$  accumulate evidence from each sensor reading.

$$\log o(A|B) = \log \lambda(B|A) + \log o(A)$$

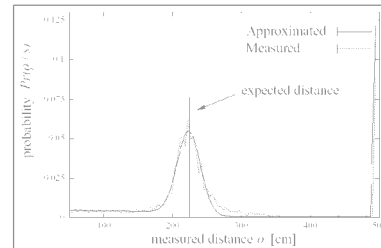
$$\log o(occ(i,j))$$

$$+ \log \lambda(r=D|occ(i,j))$$

$$= \log o(occ(i,j) | r=D)$$

## Sensor Model $p(r=D|occ(i,j))$

- Probability of range-reading given known occupancy at a known distance.

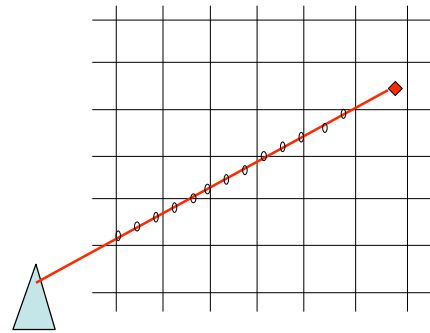


## Update Values for $\lambda$

- If the laser terminates at  $C_{ij}$  at distance  $D$ 

$$\lambda(r=D|occ(i,j)) = \frac{p(r=D|occ(i,j))}{p(r=D|\neg occ(i,j))} \approx \frac{.06}{.005} = 12$$
  - so  $\log_2 \lambda \approx +3.5$
- If the laser passes through  $C_{ij}$ .
 
$$\lambda(r>D|occ(i,j)) = \frac{p(r>D|occ(i,j))}{p(r>D|\neg occ(i,j))} \approx \frac{.45}{.90} = .5$$
  - so  $\log_2 \lambda \approx -1.0$

## Mapping One Laser Scan



## Future Attraction: SLAM

- To build an accurate map, we assume that robot pose  $(x,y,\theta)$  is known accurately.
  - This is usually not true.
- *Localization* means using sensor input to estimate the robot pose  $(x,y,\theta)$ .
- Simultaneous Localization and Mapping (SLAM) uses the existing map and current sensor input for localization.
  - Once localized, use sensors to update the map

## Mapping Assignments (4 and 5)

- We will give you laser range-sensor traces.
  - Few specular reflections; no spreading cone.
  - Off-line computation; no physical control.
- For **Assignment 4**, you will have accurate pose information  $(x,y,\theta)$ .
  - You build an accurate occupancy grid map.
- For **Assignment 5**, you will do simultaneous localization and mapping (SLAM).
  - You are given laser and odometry sensor values.

## Implementation Hints

- Use  $10 \times 10 \text{ cm}^2$  grid cells.
  - But make cell size a parameter and try others.
- To display the grid:
  - Black means occupied
  - White means free
  - Grey means unknown
- Experiment with different shade mappings.
  - Make it both useful and attractive.

## Implementation Hints

- Robot pose  $(x, y, \theta)$  and laser endpoints  $(p, q)$  are high-resolution values.
  - Grid cells correspond to extended regions.
- Put cell centers at integer coordinates so *rounding* quickly gives cell coordinates.
- Increment  $C_{ij}$  for endpoint of laser beam.
- Step regularly along free part of the beam, decrementing  $C_{ij}$  for free cells.

