

Sensor Network Security

R. Blom, "An optimal class of symmetric key generation systems," *Advances in Cryptology: Proceedings of EUROCRYPT 84*, Lecture Notes in Computer Science, Springer-Verlag, 209:335-338, 1985.

Reference on application to sensor networks

Wenliang Du, Jing Deng, Yunghsiang S. Han, and Pramod Varshney, "A Pairwise Key Pre-distribution Scheme for Wireless Sensor Networks," *Proceedings of the 10th ACM Conference on Computer and Communications Security*, Washington DC, October 2003.

Motivation

- ❑ Ad hoc networks with no trusted infrastructure support
- ❑ Sensors have limited computation, storage, and energy resources
 - use symmetric key encryption
- ❑ Standard solutions to enable key agreement between computing devices are not appropriate
 - Public key algorithms
 - Trusted server

Pre-distribution of symmetric keys

- ❑ Naïve solution - each node has the same master key
 - One node compromised => entire network compromised
- ❑ For a network of N nodes, each node is pre-installed with $N-1$ symmetric keys for all other nodes
 - Not scalable

Blom's key pre-distribution scheme

λ -secure property

- ❑ When an adversary compromises less than or equal to λ nodes, uncompromised nodes are perfectly secure.
- ❑ When an adversary compromises more than λ nodes, all pairwise keys of the entire network are compromised

Pre-deployment phase

- ❑ A trusted controller first constructs a $(\lambda+1) \times N$ matrix, G , over a finite field $GF(q)$, where
 - N is the number of nodes
 - G is public information
 - q is a prime number larger than 2^n , where n is number of bits in a key
- ❑ Then the controller
 - creates a *random* $(\lambda+1) \times (\lambda+1)$ *symmetric matrix* D over $GF(q)$
 - *Matrix D is secret* known only to the controller
 - The controller computes an $N \times (\lambda+1)$ matrix

$$A = (D.G)^T$$
 where $(D.G)^T$ is the transpose of matrix $D.G$

Pre-deployment phase (2)

□ Because D is symmetric, we have

$$\begin{aligned} A.G &= (D.G)^T.G = G^T.D^T.G = G^T.D.G \\ &= G^T.A^T = (AG)^T \end{aligned}$$

Thus, AG is a symmetric matrix to be denoted by

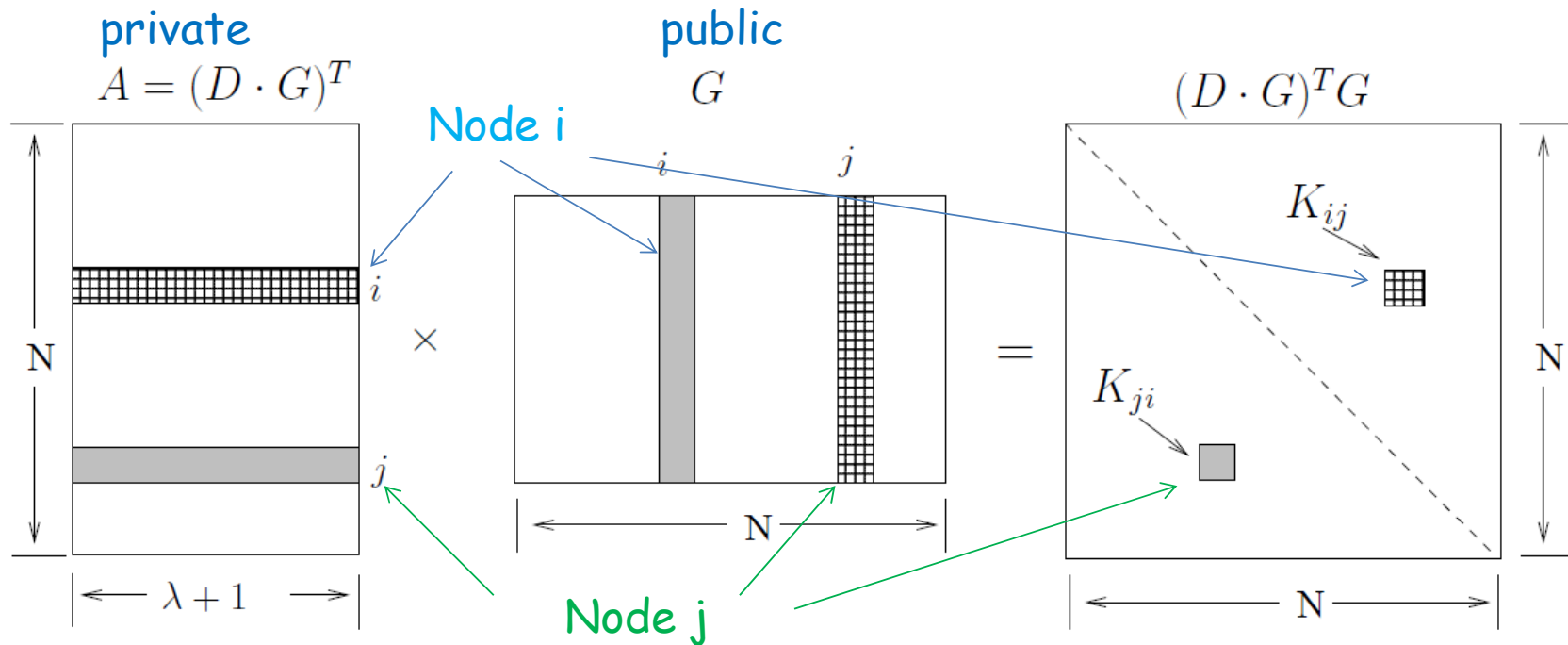
$K = AG$, where $K_{ij} = K_{ji}$, for all $1 \leq i, j \leq N$,
which can be used as the pairwise key between
nodes i and j

Comment: Since i and j share a private key, encrypted
messages between them may be relayed by other nodes

Blom's key pre-distribution

- ❑ The controller stores
 - the k th row of matrix A in node k , and
 - the k th column of matrix G at node k
- ❑ When nodes i and j need to communicate confidentially,
 - they first exchange their columns of G (which is public info) in plaintext
 - then i and j compute K_{ij} and K_{ji} , respectively, using each node's private info (row of A) and received column of G

Blom's scheme illustrated



If any $\lambda+1$ columns of G are linearly independent, then the above scheme is λ -secure

An example of matrix G

- Let each pairwise key be an element in the finite field $GF(q)$, where q is the smallest prime number larger than 2^n
 - for keys represented by n bits

- Let s be a primitive element of $GF(q)$ and $q > N$
 - each nonzero element in $GF(q)$ can be represented by some power of s
 - $s^i \neq s^j$ for $i \neq j$

An example of matrix G (cont.)

A Vandermonde matrix !

$$G = \begin{bmatrix} 1 & 1 & 1 & \dots & 1 \\ s & s^2 & s^3 & \dots & s^N \\ s^2 & (s^2)^2 & (s^3)^2 & \dots & (s^N)^2 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ s^\lambda & (s^2)^\lambda & (s^3)^\lambda & \dots & (s^N)^\lambda \end{bmatrix}$$

- s, s^2, \dots, s^N are all distinct
- any $\lambda+1$ columns of G are linearly independent
- only the seed s^k of the k th column is stored in node k

The End