# A Composition Theorem for Layered Systems\*

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#### Abstract

We define interface, module and the meaning of M offers I, where M denotes a module and I an interface. For a module M and disjoint interfaces U and L, the meaning of M using L offers U is also defined. Let N be a module that interacts with module M across interface L. We prove the following composition theorem: If M using L offers U, and N offers L, then M interacting with N offers L. Since the composition of M and N is also a module, the theorem holds for an arbitrary number of modules organized in a linear hierarchy. This theorem provides a theoretical foundation for layered systems (e.g., computer networks) where each layer corresponds to a module in the theorem.

#### 1. Introduction

A module in our theory may be a service provider, a service consumer, or both. Interactions between a module and its environment take place at interfaces. Occurrence of an interface event involves *simultaneous* participation by both the module and its environment, and is observable from both sides of the interface. The semantics of an interface is defined by a set of allowed sequences of interface events; each such sequence defines an allowed sequence of interactions between the module and its environment. A module is specified by a state transition system (and a set of fairness requirements).

For a module M and an interface I, we define the meaning of M offers I (see Section 2). Our definition is similar to—but not quite the same as—various definitions of M satisfies S in the literature, where S is a specification of M [1,3,5,6,7,9,12,13,14]. Most definitions of M satisfies S have this informal meaning: M satisfies S if every possible observation of M is described by S. Specific definitions, however, differ in many ways: (1) in whether interface events or states are observable, (2) in whether observations are finite or infinite sequences, (3) in the particular formalism for representing these sequences, and (4) in the method of interaction at an interface.

Two modules interacting across an interface are composed to become a single module by hiding the interface between them. In this respect, the composition of two modules in our theory is defined in a manner not unlike the approaches of CSP [5] and I/O automata [14]. There are, however, some basic differences between our theory and the theories of CSP and I/O automata. First, we have an explicit notion of two-sided interfaces. Second, the interaction method between a module and its environment is different in our theory. (See below.) Third, in developing our theory, our vision of how it should be applied is different from those in [5,14]; specifically, we are more interested in decomposing the specification of a complex system (e.g., the protocols of a network) than in composition per se. An elaboration on this point follows.

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Suppose an interface I has been specified through which a system provides services. Instead of designing and implementing a monolithic module M that offers I, we would like to implement the system as a collection of smaller modules  $\{M_i\}$  such that the composition of  $\{M_i\}$  offers I. To achieve this objective, the following three-step approach may be used:

- Step 1. Derive a set of interfaces  $\{S_i\}$  from I, one for each module in the collection (decomposition step).
- Step 2. Design modules individually, and prove that  $M_i$  offers  $S_i$  assuming that the environment of  $M_i$  satisfies  $S_i$  in some manner.
- Step 3. Apply an inference rule (composition theorem) to infer from the proofs in Step 2 that the composition of  $\{M_i\}$  offers I.

The above approach has the following highly-desirable feature: given interfaces  $\{S_i\}$ , each module can be designed and implemented individually. However, the decomposition step—i.e., deriving the interfaces  $\{S_i\}$  from I—is not an easy task. Furthermore, to develop the approach into a valid method, the following problem has to be solved, namely: In general, the inference rule required in Step 3 uses circular reasoning, and may not be valid. To see this, consider modules M and N that interact across interface I. Each module guarantees some properties of I only if its environment satisfies certain properties of I. However, module M is part of the environment of module N, and module N is part of the environment of module M.

The above problem was considered by Misra and Chandy [16] for processes that communicate by CSP primitives. They gave a proof rule for assumptions and guarantees that are restricted to safety properties. Using different models, Pnueli [18] presented a proof rule and Abadi and Lamport [2] presented a composition principle, that are more general than the rule of Misra and Chandy; in particular, while the class of interface properties is still restricted, it includes progress properties.

In thinking about an interface, we depart from the usual notion that it is an external "cover" that encloses a module. Instead, we think of an interface as being two-sided, namely: there is a service provider on one side of the interface, and a user on the other, with both the user's behaviors and the service provider's behaviors constrained by the same set of interface event sequences; in this respect, an interface is symmetric. However, in our definitions of M offers I and M using L offers U (see Section 2), the user and the service provider of each interface have asymmetric obligations. By organizing modules hierarchically and having asymmetric obligations for each interface, circular reasoning is avoided.

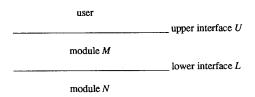


Figure 1. Module M and its environment.

For example, consider module M in Figure 1. It provides services to a user through interface U while it uses services offered by another module through interface L. We refer to U as the *upper interface* and L as the *lower interface* of module M. Note that module M is the user of interface L and the service provider of interface L. Its environment consists of both the user of L and the module that offers L.

Many practical systems have a hierarchical structure. In fact, almost all computer networks have layered protocol architectures. Each protocol layer—e.g., transport, data link—corresponds to a module in our

composition theorem. (Note that each protocol layer is composed of a set of entities [17,19,20]. We place no restriction on how these entities are composed.)

Our composition theorem provides a theoretical foundation for layered systems. With the composition theorem, we are assured that each layer in the system, say M with upper interface U and lower interface L, can be designed, implemented and modified individually. As long as the interfaces remain the same and M using L offers U is satisfied, the internals of M can change.

The balance this paper is organized as follows. In Section 2, we present our theory in a general semantic framework. In Section 3, the definitions and results are specialized to the relational notation [9], which is a specification formalism more suitable for practical application. As an example, we present in Section 4 the upper and lower interfaces of a connection management protocol. A specification of the protocol is given together with a proof that it satisfies *M using L offers U*. Section 5 has some concluding remarks. (Nontrivial applications of our theory and notation to the specification and verification of protocols for concurrency control and secure access control can be found in [8] and [11] respectively.)

# 2. Theory

We first define some notation for sequences. A sequence over E, where E is a set, means a (finite or infinite) sequence  $(e_0, e_1, \dots)$ , where  $e_i \in E$  for all i. A sequence over alternating E and F, where E and F are sets, means a sequence  $(e_0, f_0, e_1, f_1, \dots)$ , where  $e_i \in E$  and  $f_i \in F$  for all i.

# **Definition**. An interface *I* is defined by:

• Events (I), a set of events that is the union of two disjoint sets,

Inputs (I), a set of input events, and

Outputs (I), a set of output events.

AllowedEventSeqs (I), a set of sequences over Events (I), each of which is referred to as an allowed
event sequence of I.

Output events of I are under the control of the service provider of I, and input events of I are under the control of the user of I. The occurrence of an interface event can only be initiated by the side with control. (This requirement will be referred to as *unilateral control*.) Since the occurrence of an interface event requires simultaneous participation by both the service provider and user of I, it is possible that an interface event initiated by one side cannot occur because the other side refuses to participate.

For a given interface I, define

 $SafeEventSeqs(I) = \{w : w \text{ is a finite prefix of an allowed event sequence of } I\}$  which includes the empty sequence.

**Definition**. A state transition system A is defined by:

- States (A), a set of states.
- Initial (A), a subset of States (A), referred to as initial states.
- Events (A), a set of events.
- Transitions<sub>A</sub>(e), a subset of States(A)×States(A), for every  $e \in Events(A)$ . Each element of Transitions<sub>A</sub>(e) is an ordered pair of states (s,t) referred to as a transition of e.

A behavior of A is a sequence  $\sigma=(s_0, e_0, s_1, e_1, \cdots)$  over alternating States(A) and Events(A) such that  $s_0 \in Initial(A)$  and  $(s_i, s_{i+1})$  is a transition of  $e_i$  for all i. A finite sequence  $\sigma$  over alternating States(A) and Events(A) may end in a state or an event. A finite behavior, on the other hand, ends in a state by definition.

The set of behaviors of A is denoted by *Behaviors* (A). The set of finite behaviors of A is denoted by *FiniteBehaviors* (A).

For  $e \in Events(A)$ , let  $enabled_A(e) \equiv \{s : \text{ for some state } t, (s,t) \in Transitions_A(e)\}$ . An event e is said to be enabled in a state s of A iff  $s \in enabled_A(e)$ . An event e is said to be disabled in a state s of A iff  $s \notin enabled_A(e)$ .

**Notation.** For any sequence  $\sigma$  over alternating States(A) and Events(A), and for any set  $E \subseteq Events(A)$ , image  $(\sigma, E)$  denotes the sequence of events in E obtained from  $\sigma$  by deleting states and deleting events that are not in E.

**Definition.** A module M is defined by:

• Events (M), a set of events that is the union of three disjoint sets:

Inputs (M), a set of input events,

Outputs (M), a set of output events, and

Internals (M), a set of internal events.

- sts(M), a state transition system with Events (sts(M))=Events (M).
- Fairness requirements of M, a finite collection of subsets of Outputs  $(M) \cup Internals(M)$ . Each subset is referred to as a fairness requirement of M.

**Convention.** For readability, the notation sts(M) is abbreviated to M wherever such abbreviation causes no ambiguity, e.g., States(sts(M)) is abbreviated to States(M),  $enabled_{sts(M)}(e)$  is abbreviated to  $enabled_{M}(e)$ , etc.

Let F be a fairness requirement of module M. F is said to be enabled in a state s of M iff, for some  $e \in F$ , e is enabled in s. F is disabled in a state s iff F is not enabled in s. In a behavior  $\sigma = (s_0, e_0, s_1, e_1, \dots, s_j, e_j, \dots)$ , we say that F occurs in state  $s_j$  iff  $e_j \in F$ . An infinite behavior  $\sigma$  of M satisfies F iff F occurs infinitely often or is disabled infinitely often in states of  $\sigma$ .

For module M, a behavior  $\sigma$  is an allowed behavior iff for every fairness requirement F of M:  $\sigma$  is finite and F is not enabled in its last state, or  $\sigma$  is infinite and satisfies F. Let AllowedBehaviors (M) denote the set of allowed behaviors of M.

We are now in a position to formalize the notion of a module offers an interface. Consider module M and interface I. Let  $\sigma$  be a sequence over alternating states and events of module M.

**Definition.**  $\sigma$  is allowed wrt I iff image  $(\sigma, Events(I)) \in AllowedEventSeqs(I)$ .

**Definition.**  $\sigma$  is safe wrt I iff one of the following holds:

- $\sigma$  is finite and image  $(\sigma, Events(I)) \in SafeEventSeqs(I)$ .
- $\sigma$  is infinite and every finite prefix of  $\sigma$  is safe wrt I.

In what follows, we use  $last(\sigma)$  to denote the last state in finite behavior  $\sigma$ , and @ to denote concatenation.

**Definition.** Given a module M and an interface I, M offers I iff the following conditions hold:

· Naming constraints:

Inputs (M)=Inputs (I) and Outputs (M)=Outputs (I).

· Safety constraints:

For all  $\sigma \in FiniteBehaviors(M)$ , if  $\sigma$  is safe wrt I, then

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\forall e \in Outputs(M): last(\sigma) \in enabled_M(e) \Rightarrow \sigma@e \text{ is safe wrt } I, \text{ and } \forall e \in Inputs(M): \sigma@e \text{ is safe wrt } I \Rightarrow last(\sigma) \in enabled_M(e).
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· Progress constraints:

For all  $\sigma \in AllowedBehaviors(M)$ , if  $\sigma$  is safe wrt I, then  $\sigma$  is allowed wrt I.

A module M with upper interface U and lower interface L is illustrated in Figure 1. The environment of M consists of the user of U and the module that offers L. The meaning of M using L offers U is next defined. In what follows, we use " $\sigma$  is safe wrt U and L" to mean " $\sigma$  is safe wrt U and  $\sigma$  is safe wrt U."

**Definition.** Given module M and interfaces U and L, M using L offers U iff the following conditions hold:

· Naming constraints:

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Events (U) \cap Events(L) = \emptyset,

Inputs (M) = Inputs(U) \cup Outputs(L), and

Outputs (M) = Outputs(U) \cup Inputs(L).
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· Safety constraints:

For all  $\sigma \in FiniteBehaviors(M)$ , if  $\sigma$  is safe wrt U and L, then

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\forall e \in Outputs(M): last(\sigma) \in enabled_M(e) \Rightarrow \sigma@e \text{ is safe wrt } U \text{ and } L, \text{ and } U \text{ and } L \text{ and } U \text{ and } L \text{ and } U \text{ and }
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 $\forall e \in Inputs(M): \sigma@e \text{ is safe wrt } U \text{ and } L \Rightarrow last(\sigma) \in enabled_M(e).$ 

· Progress constraints:

For all  $\sigma \in AllowedBehaviors(M)$ , if  $\sigma$  is safe wrt U and L, then

 $\sigma$  is allowed wrt  $L \Rightarrow \sigma$  is allowed wrt U.

The definition of M using L offers U is similar to the definition of M offers I in most respects. We first review the key elements that are common to both definitions:

- Module M is required to satisfy its interface(s) only if the environment of M satisfies the safety requirements of its interface(s). Specifically, for any finite behavior that is not safe wrt M's interface(s), the two Safety constraints are satisfied trivially; for any allowed behavior that is not safe wrt M's interface(s), the Progress constraint is satisfied trivially. That is, as soon as the environment of M violates some safety requirement of M's interface(s), module M can behave arbitrarily and still satisfy M offers I or M using L offers U.
- Module M satisfies the safety requirements of its interface(s). Specifically, whenever an output event
  of M is enabled to occur, the event's occurrence would be safe.
- Whenever an input event of M (controlled by its environment) can occur safely, M does not block the event's occurrence.

For an input event whose occurrence would be unsafe, module M has a choice: it may block the event's occurrence or let it occur. (In this respect, our model is more general than the I/O automata model [14], which requires an I/O automaton to be always input-enabled.)

The main difference between the definitions of M offers I and M using L offers U is in the Progress constraints. For module M using interface L, it is required to satisfy the progress requirements of interface U only if the module that offers L satisfies the progress requirements of L.

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Definition. A finite set of modules \{M_j: j \in J\} are compatible iff \forall j, k \in J, j \neq k: Internals (M_i) \cap Events (M_k) = \emptyset, and Outputs (M_j) \cap Outputs (M_k) = \emptyset.
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**Notation.** For a set of modules  $\{M_j: j \in J\}$ , each state of their composition is a tuple  $s = (t_j: j \in J)$ , where  $t_i \in States(M_j)$ . We use  $image(s, M_j)$  to denote  $t_j$ .

**Definition.** The composition of a compatible set of modules  $\{M_j: j \in J\}$  is a module M defined as follows:

• Events (M) defined by:

$$Internals(M) = [\bigcup_{j \in J} Internals(M_j)] \cup [(\bigcup_{j \in J} Outputs(M_j)) \cap (\bigcup_{j \in J} Inputs(M_j))]$$

$$Outputs(M) = [\bigcup_{j \in J} Outputs(M_j)] - [\bigcup_{j \in J} Inputs(M_j)]$$

$$Inputs(M) = [\bigcup_{j \in J} Inputs(M_j)] - [\bigcup_{j \in J} Outputs(M_j)]$$

sts (M) defined by:

$$States(M) = \prod_{j \in J} States(M_j)$$

$$Initial(M) = \prod_{j \in J} Initial(M_j)$$

$$Transitions_M(e), \text{ for all } e \in Events(M), \text{ defined by: } (s, t) \in Transitions_M(e) \text{ iff, } \forall j \in J,$$

$$\text{if } e \in Events(M_j) \text{ then } (image(s, M_j), image(t, M_j)) \in Transitions_{M_j}(e), \text{ and}$$

$$\text{if } e \notin Events(M_j) \text{ then } image(s, M_j) = image(t, M_j).$$

• Fairness requirements of  $M = \bigcup_{j \in J} Fairness$  requirements of  $M_j$ .

**Theorem 1.** Let modules, M and N, and interfaces, U and L, satisfy the following:

- Internals  $(M) \cap Internals(N) = \emptyset$
- M using L offers U
- N offers L

Then, M and N are compatible and their composition offers U.

A proof of Theorem 1 can be found in [10]. It is quite long, requiring the proof of several lemmas, and is omitted due to space limitation. Theorem 1 is at the heart of our approach to compose modules hierarchically.

**Theorem 2.** Let  $M_1, I_1, M_2, I_2, \dots, M_n, I_n$  be a finite sequence over alternating modules and interfaces, such that the following hold:

- For all j, k, if  $j \neq k$  then Events  $(I_j) \cap Events(I_k) = \emptyset$  and Internals  $(M_i) \cap Internals(M_k) = \emptyset$ .
- M<sub>1</sub> offers I<sub>1</sub>.
- For  $j=2, \dots, n, M_i$  using  $I_{i-1}$  offers  $I_i$ .

Then, modules  $M_1, \dots, M_n$  are compatible and their composition offers  $I_n$ .

Using Theorem 1, a proof of Theorem 2 is straightforward and is omitted. It is also straightforward to generalize Theorem 1 to a set of modules organized as the nodes of a rooted tree; see [10].

#### 3. Relational Specifications

In this section, we give a brief introduction to the specification of state transition systems, modules and interfaces in the relational notation. Some of the definitions and results in Section 2 are recast in this notation. For a complete treatment, see [8] and also [9].

The state space of a state transition system is specified by a set of variables, called state variables. For a state transition system A, the set of variables is denoted by Variables(A). For each variable v, there is a set domain(v) of allowed values. By definition,  $States(A) = \prod_{v \in Variables(A)} domain(v)$ . Each state  $s \in States(A)$  is represented by a tuple of values,  $(d_v) : v \in Variables(A)$ , where  $d_v \in domain(v)$ .

We use state formulas to represent subsets of States(A). A state formula is a formula in Variables(A) that evaluates to true or false when Variables(A) is assigned s, for every state  $s \in States(A)$ . A state formula represents the set of states for which it evaluates to true. For state s and state formula P, s satisfies P iff P evaluates to true for s.

We use event formulas to specify the transitions of events. An event formula is a formula in  $Variables(A) \cup Variables(A)'$ , where  $Variables(A)'=\{v': v \in Variables(A)\}$  and domain(v')=domain(v). The ordered pair  $(s,t) \in States(A) \times States(A)$  is a transition specified by an event formula iff (s,t) satisfies the formula, that is, the formula evaluates to true when Variables(A) is assigned t.

**Definition.** A state transition system A is specified in the relational notation by:

- Events (A), a set of events.
- · Variables (A), a set of state variables, and their domains.
- · Initial, a state formula specifying the initial states.
- For every event  $e \in Events(A)$ , an event formula  $formula_A(e)$  specifying the transitions of e.

Note that for each event e, we have

$$enabled_A(e) = [\exists Variables(A)': formula_A(e)]$$

which is a state formula representing the set of states where e is enabled.

**Definition.** A module M is specified in the relational notation by:

- Disjoint sets of events, Inputs (M), Outputs (M), and Internals (M), with Events (M) being their union.
- sts (M), a state transition system with Events (sts (M))=Events (M), specified in the relational notation.
- Fairness requirements of M, a finite collection of subsets of Outputs  $(M) \cup Internals(M)$ .

To specify an interface in the relational notation, we use a state transition system together with invariant and progress assertions. Invariant assertions are of the form: invariant P, where P is a state formula. A finite sequence over alternating states and events satisfies invariant P iff every state in the sequence satisfies P. An infinite sequence over alternating states and events satisfies invariant P iff every finite prefix of the sequence satisfies invariant P.

We use leads-to assertions of the form:  $P \ leads-to \ Q$ , where  $P \ and \ Q$  are state formulas.<sup>2</sup> A sequence  $(s_0, e_0, s_1, e_1, \cdots)$  over alternating states and events satisfies  $P \ leads-to \ Q$  iff for all i: if  $s_i$  satisfies P then there exists j,  $j \ge i$ , such that  $s_i$  satisfies Q.

Invariant and leads-to assertions are collectively referred to as atomic assertions. In what follows, an assertion is either an atomic assertion or one constructed from atomic assertions using logical connectives and quantifiers. Let  $\sigma$  denote a sequence over alternating states and events. An assertion is true for  $\sigma$  iff  $\sigma$  satisfies

<sup>&</sup>lt;sup>1</sup> We use formula to mean a well-formed formula in the language of predicate logic.

<sup>&</sup>lt;sup>2</sup> leads-to is the only temporal connective we use.

the assertion. For a given  $\sigma$ , to evaluate the truth value of an assertion, say *Assert*, we first evaluate for  $\sigma$  the truth value of every atomic assertion within *Assert*. For example,  $\sigma$  satisfies the assertion  $X \wedge Y \Rightarrow Z$ , where X, Y and Z are atomic assertions, iff  $(\sigma$  satisfies  $X) \wedge (\sigma$  satisfies  $Y) \Rightarrow (\sigma$  satisfies Z).

A safety assertion is an assertion constructed from invariant assertions only. A state transition system satisfies a safety assertion iff every finite behavior of the state transition system satisfies the safety assertion. A progress assertion is an assertion constructed from atomic assertions that include at least one leads-to assertion. A module satisfies a progess assertion iff every allowed behavior of the module satisfies the progress assertion.

To use a state transition system, say A, for specifying an interface, we need to exercise care in defining the events of A. First, A cannot have internal events. Second, the input and output events must be defined such that they have "adequate resolution." A sufficient condition is the following:

**Definition**. A state transition system A has deterministic events iff

- Internals(A)=Ø,
- Initial (A) is a single state, and
- for all e ∈ Events (A), Transitions<sub>A</sub>(e) is a partial function, i.e., for all s ∈ States (A), there is at most one state s' such that (s, s') ∈ Transitions<sub>A</sub>(e).

This condition is easy to satisfy because events in our theory can be regarded as names or labels. (Moreover, event names can be parameterized in the relational notation [9].) The condition implies that each event sequence represents at most one behavior of A because event occurrences have deterministic effects. Behaviors of A, however, are nondeterministic because more than one event can be enabled in a state.

As an observation, note that the restriction of a single initial state may be circumvented as follows (if needed): Let  $s_0$  denote a state not in States(A), and Init(A) the desired initial states of A. Define Initial(A) to be  $\{s_0\}$  and, for all  $s \in Init(A)$ , specify a distinct event for each transition  $(s_0, s)$ .

**Notation.** For any state formula R, we use R' to denote the formula obtained from R by replacing every state variable  $\nu$  in it with  $\nu'$ .

**Definition**. An interface I is specified in the relational notation by:

- Disjoint sets of events, Inputs (1) and Outputs (1), with Events (1) being their union.
- sts (I), a state transition system with deterministic events specified in the relational notation such that
   Events (sts (I))=Events (I).
- InvAssum<sub>I</sub>, a conjunction of state formulas referred to as invariant assumptions of I, such that
   Initial(I) ⇒ InvAssum<sub>I</sub>, and

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\forall e \in Outputs(I): InvAssum_I \land formula_I(e) \Rightarrow InvAssum_I'
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InvGuar<sub>I</sub>, a conjunction of state formulas referred to as invariant guarantees of I, such that

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Initial(I) \Rightarrow InvGuar_I, and
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\forall e \in Inputs(I): InvGuar_I \land formula_I(e) \Rightarrow InvGuar_I'
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• ProgReqs<sub>I</sub>, a conjunction of progress assertions, referred to as progress requirements of I.

The invariant assumptions and guarantees of interface I are collectively referred to as invariant requirements of interface I. Define

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InvReqs_I \equiv InvAssum_I \wedge InvGuar_I.
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Given an interface I specified in the relational notation, an allowed event sequence of I is the sequence of events in a behavior of sts(I) that satisfies all invariant and progress requirements; more precisely, define

AllowedBehaviors  $(I) = \{ \sigma : \sigma \in Behaviors(I) \text{ and } \sigma \text{ satisfies } invariant InvReqs_I \text{ and } ProgReqs_I \},$ AllowedEventSeqs  $(I) = \{ image(\sigma, Events(I)) : \sigma \in AllowedBehaviors(I) \}.$ 

Lastly, for event  $e \in Events(I)$ , define

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possible_I(e) \equiv InvReqs_I \land [\exists Variables(I)': formula_I(e) \land InvReqs_I']
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which is a state formula representing the set of states in which event e can occur without violating any invariant requirement of I.

Note that we have provided two ways to specify the safety requirements of an interface: namely, a state transition system, and a set of invariant requirements. It is our experience that some safety requirements are more easily expressed by invariant requirements, while some are more easily expressed by allowed state transitions encoded in a state transition system [8]. Our approach is a flexible one.

For modules and interfaces specified in the relational notation, we provide sufficient conditions for M offers I and M using L offers U. We first introduce a refinement relation between two state transition systems A and B such that  $Variables(A) \supseteq Variables(B)$ . In this case, there is a projection mapping from States(A) to States(B) defined as follows: state  $s \in States(A)$  is mapped to state  $s \in States(B)$  where  $s \in States(B)$  in  $s \in States(B)$  can be interpreted directly over States(A) using the projection mapping. Also, event formulas in  $Variables(B) \cup Variables(B)$  can be interpreted directly over  $States(A) \cup States(A)$  using the projection mapping.

**Definition.** Given state transition systems A and B and state formula  $Inv_A$  in Variables(A), A is a refinement of B assuming  $Inv_A$  iff

- $Variables(A) \supseteq Variables(B)$  and  $Events(A) \supseteq Events(B)$
- $Initial_A \Rightarrow Initial_B$
- $\forall e \in Events(B)$ :  $Inv_A \land formula_A(e) \Rightarrow formula_B(e)$

(event refinement condition)

•  $\forall e \in Events(A) - Events(B)$ :  $Inv_A \land formula_A(e) \Rightarrow [\forall v \in Variables(B): v = v']$  (null image condition)

If A is a refinement of B assuming  $Inv_A$  and, moreover, A satisfies invariant  $Inv_A$  then A is a refinement of B as defined in [9]. In this case, for any state formula P in Variables(B), if B satisfies invariant P, then A satisfies invariant P.

Given a module M, an interface I, and some state formula  $Inv_M$  in Variables(M), the following conditions, expressed in the relational notation, are sufficient for M offers I:

- B1 Inputs (M)=Inputs (I) and Outputs (M)=Outputs (I)
- B2 sts(M) is a refinement of sts(I) assuming  $Inv_M$
- B3  $\forall e \in Inputs(I): Inv_M \land possible_I(e) \Rightarrow enabled_M(e)$
- B4  $\forall e \in Outputs(I): Inv_M \land formula_M(e) \Rightarrow InvGuar_I'$
- B5 sts(M) satisfies (invariant InvAssum<sub>I</sub>  $\Rightarrow$  invariant Inv<sub>M</sub>)
- **B6** M satisfies (invariant InvAssum<sub>I</sub>  $\Rightarrow$  ProgReqs<sub>I</sub>)

**Theorem 3.** For a module M, an interface I, and some state formula  $Inv_M$  in Variables(M), if conditions B1-B6 hold, then

- (a) M offers I, and
- (b)  $\forall \sigma \in Behaviors(M)$ :  $\sigma$  satisfies invariant  $InvAssum_I \Rightarrow \sigma$  is safe wrt I.

Given an interface I, to obtain a module M that offers I, we make use of **B1-B6** in three stages. First, the events of sts(M) are named such that **B1** is satisfied. Second, events of sts(M) are specified such that sts(M) is a refinement of sts(I) (**B2** is satisfied), each input event is enabled in states where the event's occurrence would be safe (**B3** is satisfied), and M satisfies its invariant guarantees (**B4** is satisfied). Initially,  $Inv_M$  is equal to  $InvAssum_I$ . But to prove **B2-B4**, we may have to assume that sts(M) has additional invariant properties, which are used to strengthen  $Inv_M$  and must be proved (so that **B5** is satisfied). Third, we try to prove **B5** and **B6**.

For a module M, interfaces U and L, and some state formula  $Inv_M$  in Variables(M), the following conditions, expressed in the relational notation, are sufficient for M using L offers U:

```
C1 Events (U) \cap \text{Events } (L) = \emptyset

Inputs (M) = \text{Inputs } (U) \cup \text{Outputs } (L)

Outputs (M) = \text{Outputs } (U) \cup \text{Inputs } (L)

Variables (U) \cap \text{Variables } (L) = \emptyset
```

- C2 sts(M) is a refinement of sts(U) assuming  $Inv_M$
- C3 sts(M) is a refinement of sts(L) assuming  $Inv_M$
- C4  $\forall e \in Inputs(U): Inv_M \land possible_U(e) \Rightarrow enabled_M(e)$
- C5  $\forall e \in Outputs(L): Inv_M \land possible_L(e) \Rightarrow enabled_M(e)$
- C6  $\forall e \in Inputs(L): Inv_M \land formula_M(e) \Rightarrow InvAssum_i'$
- C7  $\forall e \in Outputs(U): Inv_M \land formula_M(e) \Rightarrow InvGuar_{U'}$
- C8 sts(M) satisfies (invariant (InvAssum<sub>U</sub>  $\land$  InvGuar<sub>L</sub>)  $\Rightarrow$  invariant Inv<sub>M</sub>)
- C9 M satisfies (invariant (InvAssum<sub>U</sub>  $\land$  InvGuar<sub>L</sub>)  $\land$  ProgReqs<sub>L</sub>  $\Rightarrow$  ProgReqs<sub>U</sub>)

**Theorem 4.** For a module M, interfaces U and L, and some state formula  $Inv_M$  in Variables(M), if conditions C1-C9 hold, then

- (a) M using L offers U, and
- (b)  $\forall \sigma \in Behaviors(M)$ :  $\sigma$  satisfies invariant (InvAssum<sub>U</sub>  $\land$  InvGuar<sub>L</sub>)  $\Rightarrow \sigma$  is safe wrt U and L.

C8 indicates that we can set  $Inv_M$  equal to  $InvAssum_U \land InvGuar_L$  initially. However, to prove C2-C7 for a module M, we may have to assume that sts(M) has additional invariant properties, which are used to strengthen  $Inv_M$  and must be proved (so that C8 is satisfied).

Proofs of Theorems 3 and 4 can be found in [10].

For convenience, we employ a couple of conventions when we use the relational notation [9]. They are briefly reviewed below. Recall that an event formula defines a set of state transitions. Some examples of event definitions are shown below:

$$e_1 \equiv v_1 > 2 \land v_2' \in \{1,2,5\}$$
  
 $e_2 \equiv v_1 > v_2 \land v_1 + v_2' = 5$ 

In each definition, the event name is given on the left-hand side of " $\equiv$ " and the event formula is given on the right-hand side.

Consider a state transition system A with two state variables  $v_1$  and  $v_2$ . Let  $e_2$  above be an event of the system. Note that  $v_1$ ' does not occur free in formula  $(e_2)$ . By the following convention, it is assumed that  $v_1$  is not updated by the occurrence of  $e_2$ .

**Convention.** Given an event formula, formula(e), for every state variable v in Variables(A), if v' is not a free variable of formula(e), the conjunct v'=v is implicit in formula(e).

If a parameter occurs free in an event's formula, then there is an event defined for every allowed value of the parameter. For example, consider

$$e_3(m) \equiv v_1 > v_2 \wedge v_1 + v_2' = m$$

where m is a parameter with a specified domain of allowed values. A parameterized event is a convenient way to specify a group of related events.

Lastly, in deriving a state transition system A from a state transition system B, for A to be a refinement of B as defined above, we further require that every parameter of B be a parameter of A with the same name and same domain of allowed values.

# 4. Example—A Connection Management Protocol

We first present an interface U specifying a connection management service between two access points, named 1 and 2. Suppose there is a user entity at each access point of interface U. Connections are asymmetric in that each connection established "belongs" to the user entity that requested the connection. Call collisions are resolved in favor of the user entity at access point 1. (This example is motivated by the call setup protocol between DTE and DCE in the packet layer of X.25.)

We then present an interface L specifying a reliable message communication service between two access points, also named 1 and 2. (Note that the data link layer of X.25 provides a reliable communication service to the packet layer.)

We then specify a module M that uses L to offer U. The module consists of two protocol entities, 1 and 2, such that the events of protocol entity i match the events of U and L at access points named i, for i=1,2. We show that conditions C1-C9 are satisfied. Thus, the module satisfies M using L offers U.

# 4.1. Interface U specifying connection management

We specify the state variables, initial condition, and events of interface U. The parameter i ranges over 1 and 2. We use parameter j to range over 1 and 2 such that  $j \neq i$ .

#### State variables:

State<sub>i</sub>: {Closed, PassiveOpening, ActiveOpening, PassiveOpen, ActiveOpen}. Initially Closed.

## Input events:

 $ConnReq_i = State_i = Closed \land State_i' = ActiveOpening$ 

ConnRespi = State;=PassiveOpening \(^State\_i'=PassiveOpen\_i)

 $DiscReq_i = State_i = ActiveOpen \land State_i' = Closed$ 

# Output events:

ConnInd<sub>i</sub> = State<sub>i</sub>=Closed \ State<sub>i</sub>'=PassiveOpening

Collision 2 = State 2=ActiveOpening \(^{State} 2'=PassiveOpening\)

```
ConnConf_i = State_i = ActiveOpening \land State_i' = ActiveOpen

DiscInd_i = State_i = PassiveOpen \land State_i' = Closed
```

Note that the collision event is defined only for access point 2.

## Invariant and progress requirements:

```
InvAssum_U \equiv true

InvGuar_U \equiv InvGuar_{U,1} \land InvGuar_{U,2}, where

InvGuar_{U,i} \equiv (State_i = ActiveOpen \implies State_j = PassiveOpen)

\land (State_i = PassiveOpening \implies State_j = ActiveOpening)
```

The first conjunct of  $InvGuar_{U,i}$  can be falsified only by the event  $ConnConf_i$  (which makes the antecedent true) and the event  $DiscInd_j$  (which makes the consequent false). The second conjunct of  $InvGuar_{U,i}$  can be falsified only by the event  $ConnInd_i$  (which makes the antecedent true), the event  $ConnConf_j$  (which makes the consequent false), and the event  $Collision_2$  (which makes the consequent false for i=1, and the antecedent true for i=2). Note that all these events are output events of U. Input events of U do not falsify  $InvGuar_U$  as required by our definition of a relationally-specified interface.

```
\begin{aligned} ProgReqs_U &\equiv \\ & ((State_2 \!\!=\!\! PassiveOpening\ leads - to\ State_2 \!\!=\!\! PassiveOpen)) \\ &\Rightarrow (State_1 \!\!=\!\! ActiveOpening\ leads - to\ State_1 \!\!=\!\! ActiveOpen)) \\ &\wedge ((State_1 \!\!=\!\! PassiveOpening\ leads - to\ State_1 \!\!=\!\! PassiveOpen) \\ &\wedge (State_2 \!\!=\!\! PassiveOpening\ leads - to\ State_2 \!\!=\!\! PassiveOpen) \\ &\Rightarrow (State_2 \!\!=\!\! ActiveOpening\ leads - to\ State_2 \!\!\in\!\! \{ActiveOpen, PassiveOpen\})) \end{aligned}
```

# 4.2. Interface L specifying reliable message delivery

We specify the state variables, initial condition, and events of interface L.

#### State variables:

```
Sent<sub>i</sub>: sequence of messages. Initially the null sequence.

Received<sub>i</sub>: sequence of messages. Initially the null sequence.
```

 $Sent_i$  is the sequence of messages that have been sent at access point i since the beginning of execution.  $Received_i$  is the sequence of messages that have been received at access point i since the beginning of execution. Below, the parameter i ranges over 1 and 2.

#### Input events:

```
Send_i(m) \equiv Sent_i' = Sent_i @ (m)
```

## Output events:

```
Rec_i(m) \equiv Received_i' = Received_i@(m)
```

## Invariant and progress requirements:

```
InvAssum_L \equiv true

InvGuar_L \equiv (Received_2 \text{ prefix-of } Sent_1) \land (Received_1 \text{ prefix-of } Sent_2)
```

 $ProgReqs_L \equiv (|Sent_1| \ge k \ leads - to \ |Received_2| \ge k) \land (|Sent_2| \ge k \ leads - to \ |Received_1| \ge k)$ 

Note that input events of L do not falsify  $InvGuar_L$ .

## 4.3. Module M

The module *M* consists of two protocol entities, named 1 and 2. We specify the state variables, initial condition, and events of the protocol entities below. The protocol uses three types of messages, *conn* denoting a connect request, *disc* denoting a disconnect request, and *ack* denoting an acknowledgement to a connect request.

# State variables of protocol entity i:

```
State_i: <as defined in upper interface U>.
```

 $Sent_i$ ,  $Received_i$ : <as defined in lower interface L>.

Si: {null, connS, connR, ackS, ackR, discS, discR, disc&connS, disc&connR}. Initially null.

 $S_i$ =null indicates that protocol entity i does not have any obligation.  $S_i$ =connS indicates that protocol entity i must send a conn message.  $S_i$ =connR indicates that protocol entity i has received a conn message for which it must execute an appropriate output event. The values discS and discR (and ackS and ackR) indicate similar conditions for disc (and ack) messages. The value discS connS indicates that protocol entity i must send a disc message followed by a conn message; this can happen if protocol entity i was in the ActiveOpen state, and the local user entity issued a disconnect request followed by a connect request before protocol entity i could handle the disconnect request. The value discS connS indicates that protocol entity i has received a disc message followed by a conn message, for which it must execute appropriate output events.

## Events of protocol entity i:

We first specify module events that match events of U, and then specify module events that match events of L. For an interface event  $e_i$ , the formula of the matching module event  $e_i$  has the form  $f \cap g$  where f is the interface event formula and g is a formula that has no appearance of any primed interface variable (i.e., no change to any interface variable is specified by g). The parameter i ranges over 1 and 2. Events of protocol entity i do not access state variables of protocol entity j, where  $i \neq j$ .

```
ConnReq_1 \equiv formula_U(ConnReq_1) \land ((S_1 = discS \land S_1' = disc\&connS) \lor (S_1 \neq discS \land S_1' = connS))
ConnReq_2 \equiv formula_U(ConnReq_2) \\ \land ((S_2 = discS \land S_2' = disc\&connS) \lor (S_2 = connR \land S_2' = connR) \lor (S_2 \notin \{discS, connR\} \land S_2' = connS))
ConnResp_i \equiv formula_U(ConnResp_i) \land S_i' = ackS
DiscReq_i \equiv formula_U(DiscReq_i) \land S_i' = discS
ConnInd_i \equiv formula_U(ConnInd_i) \land S_i = connR \land S_i' = null
Collision_2 \equiv formula_U(ConlSion_2) \land S_2 = connR \land S_2' = null
ConnConf_i \equiv formula_U(ConnConf_i) \land S_i = ackR \land S_i' = null
DiscInd_i \equiv formula_U(DiscInd_i) \land ((S_i = discR \land S_i' = null) \lor (S_i = disc\&connR \land S_i' = connR))
Send_i(conn) \equiv formula_L(Send_i(conn)) \land S_i = connS \land S_i' = null
Send_i(ack) \equiv formula_L(Send_i(ack)) \land S_i = ackS \land S_i' = null
Send_i(disc) \equiv formula_L(Send_i(disc)) \land ((S_i = discS \land S_i' = null) \lor (S_i = disc\&connS \land S_i' = connS))
Rec_1(conn) \equiv formula_L(Rec_1(conn)) \land ((State_1 = Closed \land S_1' = connR) \lor (S_1 = discR \land S_1' = disc\&connR) \lor (State_1 \neq Closed \land S_1 \neq discR \land S_1' = S_1))
```

```
Rec_2(conn) \equiv formula_L(Rec_2(conn)) \land ((S_2 = discR \land S_2' = disc\&connR)) \lor (S_2 \neq discR \land S_2' = connR))
Rec_i(ack) \equiv formula_L(Rec_i(ack)) \land S_i' = ackR
Rec_i(disc) \equiv formula_L(Rec_i(disc)) \land S_i' = discR
```

Fairness requirements: For each protocol entity i of module M, there is a fairness requirement consisting of the output events of the protocol entity.

#### 4.4. Satisfaction of conditions C1-C9

It is obvious that condition C1 is satisfied. C2 and C3 are satisfied (for  $Inv_M=true$ ) because each module event has the special form  $f \land g$  described above. C4 and C5 are satisfied (for  $Inv_M=true$ ) because every input event of module M has the special form  $f \land g$  and enabled(g)=true. C6 holds since  $InvAssum_L \equiv true$ . C7 holds if we define  $Inv_M \equiv Inv_{M,1} \land Inv_{M,2}$ , where

```
Inv_{M,i} \equiv \\ (State_i = ActiveOpening \land S_i = ackR \Rightarrow State_j = PassiveOpen) \\ \land (State_i = ActiveOpen \Rightarrow State_j = PassiveOpen \land S_j \notin \{discR, disc\&connR\}) \\ \land (State_i = Closed \land S_i = connR \Rightarrow State_j = ActiveOpening) \\ \land (State_i = PassiveOpening \Rightarrow State_j = ActiveOpening \land S_j \notin \{connR, ackR\}) \\ \land (State_j = ActiveOpening \land S_j = connR \Rightarrow State_j = ActiveOpening) \end{aligned}
```

The first two conjuncts of  $Inv_{M,i}$  are sufficient (and necessary) for the output events of M to preserve the first conjunct of  $Inv_{Guar_{U,i}}$ . The last three conjuncts of  $Inv_{M,i}$  are sufficient (and necessary) for the output events of M to preserve the second conjunct of  $Inv_{Guar_{U,i}}$ .

It remains to be proved that C8 and C9 hold. (The proof is omitted due to space limitation.)

## 5. Concluding Remarks

The concept of layering was described by Dijkstra more than two decades ago [4]. Layering has been applied to the design and implementation of computer network protocols, and also operating systems (in particular security kernels). However, to reap the benefits of a layered architecture—i.e., to be able to design, implement, and modify each layer individually—we need formal definitions of the meanings of interface, M offers I, and M using L offers U, as well as a composition theorem such as the one presented in this paper.

In designing our model and theory, we were faced with two conflicting goals. On the one hand, we would like to have a model that is as general as possible so that our theory has wide applicability. On the other hand, to prove the composition theorem, the model needs to be restricted in various ways. Below, we compare our model and theory to those in [2,5,14].

Our model and the CSP model [5] are different in many ways. We mention two here. First, the semantics of a process in the CSP model is given by a set of finite traces and associated refusal sets, whereas we specify a module using a set of behaviors and a set of fairness requirements (each behavior is represented by a sequence of alternating states and events). Specifically, the concepts of internal state and fairness are essential in our theory but are absent in the theory of CSP. Second, the notion of *M satisfies S*, where *S* is a specification, in the theory of CSP is not the same as our notion of *M offers I*, where *I* is a two-sided interface between a service provider and a service consumer; in particular, there is no requirement in the CSP model that interface events are unilaterally controlled.

In the theory of I/O automata [14,15], there is no distinction between module and interface, service provider and service consumer. There is the notion of one automaton simulating another automaton, but not our notion of a two-sided interface. Furthermore, each I/O automaton is required to be input-enabled, i.e., every

input event is enabled in every state of the automaton. In this respect, our model is more general; a module in our theory is required to be input-enabled *only when* the occurrence of an input event would not violate any safety requirement of the module's interface(s). For an input event whose occurrence would be unsafe, the module has a choice: it may disable the input or let it occur. Because of the input-enabled requirement, each I/O automaton can execute independently because its outputs cannot be blocked by other automata; but the set of interface event sequences generated by the automaton is inadequate for encoding various desirable interface properties. For example, it cannot be used to specify a module with a finite buffer such that inputs causing overflow are blocked. (Blocking is useful in the specification of many communication protocols that enforce input control, flow control or congestion control.)

The model of Abadi and Lamport [2] is state-based, without interface events. It is fundamentally different from our model and those of [5,14] in how a module and its environment interact. Specifically, such an interaction is represented by a change in the observable portion of the module's state, rather than by the occurrence of an interface event involving the simultaneous participation of the module and environment.

A restriction in our model that is uniquely ours is that modules can only be composed hierarchically. We accepted this restriction because we were motivated by our interest in decomposing the specification of a complex system rather than the kind of composition problems of interest in the area of distributed algorithms.

To specify nontrivial examples, we prefer to use the relational notation [9]. We find it more convenient to work with state formulas and event formulas than individual states and transitions, and to reason with invariant and progress assertions than safe and allowed event sequences. In relational specifications, the set of allowed sequences of interface events is not represented directly. Instead, a labeled state transition system and a set of invariant and progress requirements are specified, and the set of allowed event sequences is obtained from the allowed behaviors of the state transition system. Having states represented explicitly in behaviors facilitates our proof that a module offers an interface. Specifically, we make use of a projection mapping from module states to interface states to prove that the state transition systems of the module and interface satisfy a refinement relation. By using auxiliary variables, such projection mappings [9] are as general as multi-valued possibilities mappings [14].

Conceptually, the use of a state transition system in an interface specification should not influence an implementor, because only the set of allowed event sequences, generated by the state transition system and constrained by the assertions, is of interest. In practice, however, the state transition system might bias implementors of modules that offer the interface.

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