# A Wavelet-Based Approach to Detect Shared Congestion

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Abstract—Per-flow congestion control helps endpoints fairly and efficiently share network resources. Better utilization of network resources can be achieved, however, if congestion management algorithms can determine when two different flows share a congested link. Such knowledge can be used to implement cooperative congestion control or improve the overlay topology of a P2P system. Previous techniques to detect shared congestion either assume a common source or destination node, drop-tail queueing, or a single point of congestion. We propose in this paper a novel technique, applicable to any pair of paths on the Internet, without such limitations. Our technique employs a signal processing method, wavelet denoising, to separate queueing delay caused by network congestion from various other delay variations. Our wavelet-based technique is evaluated through both simulations and Internet experiments. We show that, when detecting shared congestion of paths with a common endpoint, our technique provides faster convergence and higher accuracy while using fewer packets than previous techniques, and that it also accurately determines when there is no shared congestion. Furthermore, we show that our technique is robust and accurate for paths without a common endpoint or synchronized clocks; more specifically, it can tolerate a synchronization offset of up to one second between two packet flows.

#### I. INTRODUCTION

**C** ONGESTION control has been performed on a per-flow basis; each flow adjusts its sending rate according to feed-back regarding the network's congestion status. The stability of today's Internet is mainly due to congestion control, especially the additive increase/multiplicative decrease approach of TCP.

Better utilization of network resources is achievable with cooperation between flows. For example, Congestion Manager [2] examines all flows of the host where it resides and groups flows passing through the same bottleneck link into a single flow aggregate. By performing congestion control over flow aggregates, rather than over each individual flow separately, Congestion Manager can improve fairness and efficiency significantly.

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The recent proliferation of overlay systems poses a new challenge in cooperative congestion control. There are many applications of overlay systems that would benefit from cooperative congestion control, including end system multicast [3], file download from multiple servers, and overlay QoS routing. Such systems usually consist of a large number of end hosts and unicast flows between them. Unlike flows controlled by Congestion Manager, these unicast flows have different source and destination nodes, but still may interfere with each other by sharing one or more intermediate links. If the system can tell which flows are sharing a bottleneck link, it can improve overall performance by changing the overlay topology to avoid such interference.

The basic primitive required for cooperative congestion control is to decide whether two flows are sharing a bottleneck link or not. Techniques for inferring shared congestion use two kinds of information from feedback: packet loss and delay. Techniques based on packet loss assume bursty packet loss [4], [5]. Thus, they work well with drop-tail queues and lossy links, but are slow and inaccurate with low loss rate or with other queueing disciplines, such as RED. Techniques based on delay [5], [6] show more robust behavior in such an environment. They are adequate for the case where two flows have a common source or a common destination. The major weakness of both kinds of techniques is that they require that the two tested paths share an endpoint, usually at the source. Thus, they cannot be used for general overlay networks.

We propose a novel technique (delay correlation with wavelet denoising or DCW) to detect shared congestion between two Internet paths. Like previous techniques, it is based on a simple observation: two paths sharing congested links have high correlation between their one-way delays. However, naive correlation measurements may be inaccurate, due to random fluctuation of queueing delay and mild congestion on non-shared links. In our technique, these interfering delay variations are filtered out with *wavelet denoising*, which is a signal processing method to separate signal from noise.

We evaluate our technique through extensive simulations and Internet experiments. When two paths have a common source, for which previous approaches can also detect shared congestion, our technique shows fast convergence with fewer packets. It takes at most 10 s to reach near 100% accuracy with both drop-tail and RED queues, while previous techniques often take longer or fail. We also show that our technique maintains its accuracy without a common endpoint; more specifically, it tolerates a synchronization offset between flows of up to one second.

The remainder of this paper is organized as follows. Section II describes our basic technique using cross correlation. Section III



Fig. 1. Two paths sharing links.

introduces wavelet denoising and explains how to apply it to our technique. Section IV addresses implementation issues, and Section V presents results of simulations and Internet experiments. We conclude in Section VI.

## II. BASIC TECHNIQUE

We first present a basic technique to detect shared congestion using cross correlation. This technique is effective when clocks of the nodes measuring delay are synchronized and there is only one point of congestion. With this as a basis, we will develop a general technique that tolerates a large synchronization offset and allows multiple points of congestion in Section III.

#### A. Model

Two paths sharing links on the Internet are illustrated in Fig. 1. Paths X from  $X_{src}$  to  $X_{dst}$  and Y from  $Y_{src}$  to  $Y_{dst}$  are sharing links between S and T. Let the one-way delay of path X be  $D_X$ , and that of path Y be  $D_Y$ . Each of them has two components:  $d_S$ , the delay from S to T, and the remainder denoted by  $d_X$  or  $d_Y$ 

$$D_X = d_S + d_X$$
  
$$D_Y = d_S + d_Y.$$
 (1)

A key observation is that the delay of a congested link has large fluctuations due to queueing delay changes, while the delay of a link with light load is relatively stable. A persistently congested link may have stable delay because its queue is persistently full. However, a measurement study shows that packet loss processes caused by congestion are better thought of as spikes rather than persistent congestion periods, and that loss runs of most spikes are shorter than 220 ms [7]. It confirms that a congested link shows large fluctuations in delay. In order to detect shared congestion, we need to determine whether such fluctuations occur between S and T.

## B. Cross Correlation

Our basic technique is based on the observation that measured delays of two paths show strong correlation if the paths share one or more congested links and little correlation if they do not share any congested links [5]. Suppose that paths X and Y in Fig. 1 are sharing congested links between S and T and that the other links are lightly loaded. Then  $D_X$  and  $D_Y$  will show strong similarity, since the only strongly varying component  $d_S$ is shared by both paths. On the other hand, if congestion occurs on links other than the links between S and T, then  $D_X$  and  $D_Y$  become independent. We use the cross-correlation coefficient to measure such similarity. Let  $\{X_i\}$  and  $\{Y_i\}$  be one-way delay sequences of paths X and Y, respectively, assuming that each  $\langle X_i, Y_i \rangle$  pair was measured at the same time. Then their crosscorrelation coefficient  $XCOR_{XY}$  is defined as follows:

$$XCOR_{XY;n} = \frac{\sum_{i=1}^{n} (X_i - \overline{X})(Y_i - \overline{Y})}{\sqrt{\sum_{i=1}^{n} (X_i - \overline{X})^2 \cdot \sum_{i=1}^{n} (Y_i - \overline{Y})^2}}.$$
 (2)

Note that  $XCOR_{XY} = 1$  if both  $d_X$  and  $d_Y$  are constant and  $d_S$  is not constant (shared congestion), and  $XCOR_{XY} = 0$  if  $d_S$  is constant and  $d_X$  or  $d_Y$  varies independently (no shared congestion). Of course, other network effects could make  $XCOR_{XY} = 1$  in the absence of shared congestion, or make  $XCOR_{XY} = 0$  in the presence of shared congestion. We follow earlier work by assuming that this rarely happens [5]; further Internet experimentation may be required.

One of the properties of the cross-correlation coefficient is that its value is independent of any constant component of  $\{X_i\}$ or  $\{Y_i\}$  and dominated by components with large fluctuations. It matches well with our purpose to determine if any of the shared links has large delay fluctuations. Also note that, due to this property, no clock synchronization between the source and destination nodes of paths X and Y is required in measuring one-way delay between them. However, clock skew may affect measurement. We will examine the effects of clock skew on shared congestion detection in Section V-A2. In this paper, except for the results presented in Figs. 14 and 23, we assume that there is no clock skew.

## C. Basic Technique Implementation

The basic technique consists of two stages: sampling and processing. In the sampling stage,  $X_{src}$  sends to  $X_{dst}$  a sequence of UDP packets with a timestamp, starting at time  $t_0$  with its own clock. Each such UDP packet is called a *probe packet*. Probe packets are sent at a constant rate until  $t_0 + T$ , where Tis the probe interval. On receiving a probe packet,  $X_{dst}$  calculates one-way delay and sends it, with the original timestamp, back to  $X_{src}$ . Then  $X_{src}$  records the one-way delay together with the timestamp as a delay sample. Missing samples are linearly interpolated from neighboring samples, because if missing samples are discarded,  $X_i$  and  $Y_i$  are very likely out of synchronization from then on. The sampling stage ends when the last delay sample from  $X_{dst}$  is received (or upon timeout if the last probe or the reply to it is lost).  $Y_{src}$  and  $Y_{dst}$  also collect delay samples in the same way.

In the processing stage, the cross-correlation coefficient of two sequences of delay samples is computed as defined in (2). The actual procedure to gather delay sequences collected by different nodes is application-dependent. For example, in application-layer multicast, a common ancestor node of  $X_{src}$  and  $Y_{src}$  in the multicast tree can gather and process delay sequences.

<sup>&</sup>lt;sup>1</sup>Although the cross correlation is a function of two time series and the number of samples used in computation, we refer to it as  $XCOR_{XY}$  or simply *XCOR* in this paper for brevity.



Fig. 2. Cross-correlation coefficient between two delay sequences versus synchronization offset.



Fig. 3. Simple topology with a common source.

#### D. Limitations

Applicability of the basic technique is limited because it makes two assumptions that generally do not hold for the Internet.

The first assumption is that the two delay sequences are synchronized. Ideally, the basic technique expects packets measuring  $X_i$  and  $Y_i$  to pass through S at the same time. To achieve this, the endpoints would need precisely synchronized clocks, and to predict the delays from  $X_{src}$  and  $Y_{src}$  to S. However, one-way delays cannot be measured without network support, and network clock synchronization protocols are not accurate enough for our purposes, since they still allow errors up to half of the round-trip time between the nodes [8]. To quantify such synchronization errors, we define synchronization offset as the time difference between arrivals of two probe packets at S, one sent by  $X_{src}$  at time t with  $X_{src}$ 's clock and the other by  $Y_{src}$ at time t with  $Y_{src}$ 's clock. As the synchronization offset increases, the delay sequences collected by the two nodes show less and less correlation. Fig. 2 illustrates this; it plots the crosscorrelation coefficient for two paths sharing a congested link as synchronization offset rises from 0 to 1 s. Each point is the mean coefficient over 300 simulations; the bars show 5th and 95th percentiles. In each simulation, two delay sample sequences were collected for 100 s on the topology shown in Fig. 3 using ns-2.2 The bandwidth of every link was 1.5 Mb/s, and its propagation delay was chosen randomly between 20 and 30 ms for each simulation. The delay sequences represent one-way delays of two paths, from  $X_{src}$  to  $X_{dst}$  and from  $Y_{src}$  to  $Y_{dst}$ . Pareto ON-OFF constant-bit-rate (CBR) flows were used as background traffic, so that the congestion level could be controlled easily by changing the number of flows. The average ON and OFF times were selected uniformly between 0.2 and 3 s. The CBR rate

was selected uniformly between 20 and 40 kb/s, and its Pareto shape parameter was 1.2. The loss rate of the shared link was about 10%; the other links did not have any loss. Without synchronization offset, the mean cross correlation between the two delay sequences is about 0.99. However, the mean cross correlation drops as synchronization offset increases so that a 600 ms synchronization offset results in half of the mean cross correlation without offset.

The second assumption required by the basic technique is that *queueing delay variation on noncongested links is close to zero*. If such delay variation is not negligible, it confuses the basic technique and will give an obscure cross-correlation coefficient not close to zero or one. Then it is difficult to determine the threshold to differentiate shared congestion and independent congestion cases.

In Section III, we propose wavelet denoising to enhance the basic technique. It effectively filters out delay variations in non-congested links and short-term fluctuations that confuse the basic technique, as well as negative effects of synchronization offset. With the combination of wavelet denoising and cross correlation, our new technique can detect shared congestion for paths with a large synchronization offset and varying delays at noncongested links. It also determines quickly when there is no shared congestion.

#### E. Related Work

Previous approaches to detect shared congestion using probe packet streams are also based on the assumption of strong correlation between packet delays or losses of two paths that share a bottleneck. Thus, these approaches have the same limitation as our basic technique, i.e., two probe packet streams should be synchronized for such technique to be effective.

Rubenstein et al. proposed two techniques, one based on one-way delays and the other based on packet losses [5]. These techniques assume that the paths being probed share a common end point (either source or destination). The delay-based technique uses a Poisson process with an average interval of 40 ms to generate a sequence of delay samples. When two delay sequences are obtained for different paths, an auto-measure  $M_a$  is computed from the delays of pairs of adjacent packets in the first sequence. A cross measure  $M_x$  is computed from a new delay sequence obtained by merging the two delay sequences. Only adjacent packet pairs with the first element in each pair from the first sequence and the second element in each pair from the second sequence are used in computing  $M_x$ . If  $M_a < M_x$ , it is inferred that the two paths are sharing a congested point. In their loss-based technique,  $M_a$  and  $M_x$  are conditional probabilities that a packet is lost when its following packet is lost. In their simulations, the delay-based technique was always more robust than the loss-based one.

Harfoush *et al.* [4], [9] proposed a loss-based technique that outperforms the loss-based technique of Rubenstein *et al.* In their technique, a common source sends a packet pair back-toback at 15 Hz. The probability that only the second packet is lost is computed from packet losses. If the probability exceeds the threshold of 0.4, it is inferred that the paths are sharing a congested point.

(a) Light traffic (a) Light traffic (a) Light traffic (b) Heavy and light traffic (c) Heavy traffic

Fig. 4. Time series of one-way delay of a single-hop path.

A different problem on detecting shared points of congestion was posed and investigated by Katabi *et al.* [6]. They consider a large number of sources that send to a common destination. The paths form a tree rooted at the destination. Some of the tree nodes (routers) are bottlenecks such that every path goes through exactly one of the bottlenecks. They presented a passive measurement technique, based upon the entropy of packet interarrival times, to group sources into different clusters, one for each bottleneck along the way. Another approach to address a similar problem using the technique of Rubenstein *et al.* [5] was presented by Younis and Fahmy [10].

#### **III. WAVELET DENOISING**

To provide efficient solutions to network problems, various types of signal processing techniques have been employed for modeling [11] and analysis [12]–[14] of Internet traffic. However, they are mainly used to infer static or long-term network information from a large set of data collected over a long time span. In order to obtain dynamic information such as congestion status in a timely manner, techniques capable of online processing and fast response are required.

In this section, we first examine the time series of packet delay in a flow and its characteristics. Based on these characteristics, we introduce a signal processing technique—wavelet denoising [15]—that overcomes limitations of the basic cross-correlation technique in Section II-D. Wavelet denoising takes the original delay time series, and generates another time series with reduced interfering fluctuations that might affect cross correlation adversely. Finally, we discuss a procedure to find a wavelet basis that minimizes negative effects of synchronization offset.

## A. Nature of Delay Data in Time and Frequency Domain

Fig. 4 demonstrates an example set of time series of packet delay for a link with two different congestion levels. The source and destination nodes were connected through a 1.5 Mb/s link on ns-2. The delay between them was measured using UDP packets as explained in Section II-C. The time series in Fig. 4(a) is the one-way delay under light traffic load (76 ON-OFF CBR flows, no packet loss) while the time series added in Fig. 4(b) is the delay under heavy traffic load (92 ON-OFF CBR flows, loss rate between 2% and 10%). ON-OFF CBR flow parameter set-



Fig. 5. Power spectral densities of time series of delay data for light traffic and heavy traffic.

tings were identical to those described in Section II-D. The 95th percentile of loss run length (the number of consecutive packet losses) for heavy traffic load was about 180 ms, which is close to the Internet measurement result (220 ms) in [7].<sup>3</sup> Observe that the one-way delay with light traffic is a noise-like waveform with small amplitude, while the delay with heavy traffic shows an irregular pulse pattern with larger amplitude. Such pulses result from network congestion.

The corresponding frequency-domain power spectral densities of the individual time series, normalized to unity area, are provided in Fig. 5. In the frequency domain, the delay with heavy traffic shows larger amplitude at low frequencies than the delay with light traffic. Such large amplitude components at low frequencies correspond to the irregular pulses in Fig. 4(b), caused by congestion, while others are introduced by the randomness of queue behavior, well demonstrated in Fig. 4(a). Therefore, for a proper assessment of network traffic under congestion via delay data, it is necessary to reduce the effects associated with random queue behavior which corrupts the traffic delays in both the time and frequency domains. In addition, if a synchronization offset is introduced in delay sampling, the measure of network traffic via delay will be less reliable.

If we are only interested in extracting the large amplitude components at low frequencies, a simple low-pass filter seems to be an intuitive solution. Low-pass filtering would smooth the delay signals, increasing cross correlation when there is shared congestion. On the other hand, low-pass filtering may fail to diagnose nonshared congestion cases. Consider the extreme case that there is no congestion on either path. In such a case, nearzero cross correlation is expected since the delay signals will be dominated by random queue behavior. However, simple lowpass filtering may over-smooth the signal, resulting in an inappropriately high value of cross correlation. This is because the frequency spectrum in network delay data varies in a dynamic fashion due to the fact that network traffic changes in time. Therefore, any attempt to mitigate the interference effects should include an approach based on both time and frequency (or scale) analysis, e.g., the wavelet transform. Hence, we use wavelet denoising rather than simple filtering. We will show an empirical comparison between simple low-pass filtering and wavelet denoising in Section V-B3.

We will show that wavelet denoising is highly effective for the purpose of detecting shared congestion. A major advantage of wavelet denoising is that it preserves the dominant characteristics of one-way delay and filters out nondominant ones in a time and scale localized manner, thus it can deal with the time-varying spectrum of network delay data. Therefore, even when there is no congestion, wavelet denoising preserves strong transients at high frequencies and thus maintains low cross correlation between denoised signals.

## B. Wavelet Transform and Denoising

The wavelet transform is a signal processing technique that represents a transient or nonstationary signal in terms of time and scale distribution. Due to its light computational complexity, the wavelet transform is an excellent tool for online data compression, analysis, and denoising.

Assume that a signal f(t) is contaminated by an additive noise n(t); then, the measured data are x(t) = f(t) + n(t). The measured time series x(t) can be represented as an orthonormal expansion with wavelet basis  $\psi_{i,j}(t) = 2^{-i/2}\psi(2^{-i}t - j)$  as follows [16]:

$$x(t) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} X_j^i \psi_{i,j}(t)$$
(3)

where the wavelet coefficients are calculated from

$$X_j^i = \int_{-\infty}^{\infty} x(t)\psi_{i,j}(t)dt.$$
 (4)

Note that  $X_j^i$  is the discrete wavelet transform of x(t) at scale i and at translation j and represents how x(t) is correlated with the i scaled and j translated basis function.

Wavelet denoising removes noise components from the noisecorrupted signal by suppressing those wavelet coefficients that fall below a threshold. In this paper, the interfering effects such as synchronization offset and random fluctuations are regarded as "noise" to be filtered out, and the congestion related information is regarded as the original "signal."

Two cases should be taken into account to achieve robust and reliable cross-correlation results. When there is congestion, the slowly varying congestion information (at high scale) should be extracted from the delay data, which are corrupted by synchronization offset and random queue behavior. Without congestion, strong random transients should be extracted to ensure a low correlation. Wavelet denoising is capable of selecting the desired signal while removing others in each case.

Wavelet denoising lets us build a nonlinear approximation of the signal f(t) using the wavelet coefficients of the measured data x(t). The wavelet coefficients for the measured data x(t) = f(t) + n(t) become  $X_j^i = F_j^i + N_j^i$ , where  $F_j^i = \int_{-\infty}^{\infty} f(t)\psi_{i,j}(t)dt$  and  $N_j^i = \int_{-\infty}^{\infty} n(t)\psi_{i,j}(t)dt$ . Then,  $\tilde{f}(t)$ , an approximation of the signal f(t), is obtained from the wavelet coefficients of the measured data x(t) by suppressing noise with a nonlinear thresholding function,  $d_T$ . In this paper, we employ a soft thresholding operation on  $d_T$  with the following definition [15]:

$$d_T(x) = \begin{cases} x - T, & \text{if } x \ge T \\ x + T, & \text{if } x \le -T \\ 0, & \text{if } |x| < T. \end{cases}$$
(5)

The value of the threshold T can be determined by various methods, and the threshold selection varies with different applications and the types of background noise (e.g., white or nonwhite). The typical threshold selection rules for wavelet denoising are documented in [17] (and also implemented in the MATLAB wavelet toolbox [18]). In this paper, we utilize the most general threshold selection rule which minimizes the maximum means square error assuming non-white noise. The selection of the threshold needs further investigation, but we believe that the threshold value may depend on the network traffic characteristics. Once the threshold is selected, the denoised signal  $\tilde{f}(t)$  is obtained by applying the threshold to the wavelet coefficients  $X_i^i$  in (3).

$$\tilde{f}(t) = \sum_{i=-\infty}^{\infty} \sum_{j=-\infty}^{\infty} d_T \left( X_j^i \right) \psi_{i,j}(t).$$
(6)

Soft thresholding plays a key role in the approximation of the traffic delay data under congestion. If there is shared congestion, the dominant low-frequency term, which corresponds to the true traffic congestion information, will exhibit relatively large wavelet coefficient values at high scale (low frequency) so that true traffic information will remain after the thresholding operation. Meanwhile, the high-frequency components, which can be assumed to be the effects of random queue behavior, will have relatively small wavelet coefficients at low scale (high frequency) and will be filtered by the thresholding operation. Soft thresholding also has the effect of smoothing the transient irregular peaks in the delay data. In the basic cross-correlation technique, randomly occurring peaks in the delay data could have a dominant deleterious effect on the cross-correlation value. Wavelet denoising smooths these irregular peaks, making the cross-correlation value more robust. On the other hand, when there is no congestion, delay variations caused by random queue behavior will have relatively large wavelet coefficient values, and thus will be preserved by soft thresholding.

## C. Selection of Wavelet Basis

The wavelet transform provides a time- and scale-localized representation of a measured time series; however, the time and scale resolution of the representation depends on the selection of a wavelet basis. Hence, in order to get the most robust and reliable results from wavelet analysis including wavelet denoising, it is crucial to select the best basis function for wavelet decomposition [19]. In this paper, selection of a wavelet basis is confined to be within the Daubechies family of wavelets, which are widely used due to its simplicity of implementation.

The correlation between a data signal and a wavelet basis is determined by time and frequency localized characteristics. Such characteristics of a data signal and wavelet basis can be represented by the time and frequency localized moments, which enable the approximation of the individual time-frequency signal elements as a Gabor logon [20]. Then, the trace of the signal elements on the time-frequency plane is defined as an elliptic curve as shown in Fig. 6. The time duration and frequency bandwidth of the data and wavelet basis determine semimajor and semiminor axes as indicated in Fig. 6.  $T_s$  and  $F_s$  are the time duration and frequency bandwidth of the signal, while  $T_b$  and  $F_b$  are those of the wavelet basis [19]; the areas, C,



Fig. 6. Schematic description of localized time–frequency characteristics for a data signal (horizontally hatched area) and a wavelet basis (vertically hatched area).

 $D_1$ , and  $D_2$ , are derived from them. Based on these variables, we define a metric, instantaneous signal-to-noise ratio (SNR), to indicate how closely a wavelet basis matches a data signal on the time-frequency plane.

1) Instantaneous SNR: Fig. 6 provides a schematic description of localized time and frequency characteristics for a data signal and wavelet basis. The quarter ellipse including C and  $D_1$  represents the localized time-frequency characteristics of the data signal, and the quarter ellipse including C and  $D_2$  represents those of the wavelet basis. For the two quarter ellipses to be well-matched, the size of the common area C should be large while the discrepancy  $D = D_1 + D_2$  should be small. To quantify how closely the time-frequency characteristics of a data signal and wavelet basis match, we postulate a transient resolution index named "instantaneous SNR" (ISNR) whose dimension is dB/s and is given as

$$\text{ISNR} = \frac{1}{T_b} 10 \log_{10} \frac{C}{D}.$$
 (7)

ISNR provides a measure of similarity between the data signal and wavelet basis within the time frame of the wavelet basis function.

2) Minimizing Adverse Effects of Synchronization Offset: In our application, the measured data consist of two parts, slowly varying congestion information and interference from random queue behavior and synchronization offset; such interference can be mitigated by employing a soft thresholding technique in wavelet denoising. We can further reduce the interference from synchronization offset by choosing a wavelet basis carefully.

Synchronization offset in the delay data can be interpreted as the difference of the time-shifted version of delay data and the original one. Therefore, the synchronization offset depends on the characteristics of the original data. Hence, the basis  $\psi_{i,j}(t)$ should be chosen to maximize the ISNR of f(t) and  $\psi_{i,j}(t)$  and minimize the ISNR of n(t) and  $\psi_{i,j}(t)$ , where f(t) is the delay changes caused by network congestion and n(t) is the interference caused by the synchronization offset. Therefore, it suffices to find the basis that maximizes the difference between the two ISNRs, which we call the *differential ISNR*. However, since the true f(t) and n(t) are not available directly, an approximation is required; we used the delay data of a congested path as f(t), and the difference between the delay data and its shifted version as an approximation of  $n(t) = f(t) - f(t - \Delta_{max})$ , where  $\Delta_{max}$  is the maximum possible synchronization error (1 s in this



Fig. 7. Differential ISNR between congestion signal and other noise for Daubechies wavelets.

paper). More discussion on the maximum possible synchronization error is presented in Section IV-C.

In Fig. 7, we plot the differential ISNR for Daubechies wavelets 2–10. The delay sequences were obtained by repeating the simulation used to draw Fig. 4(b) 120 times to approximate f(t), and the interference n(t) is directly computed from f(t). Each point in Fig. 7 is the mean value of the differential ISNR for the 120 sequences. As shown in the figure, Daubechies wavelet 6 has the highest differential ISNR, which implies that it is best matched with congestion information and least matched with the noise due to synchronization offset on the time–frequency plane. Therefore, the Daubechies wavelet 6 basis will be employed for wavelet denoising in this paper. Note that this result is based on the data shown in Fig. 4; other bases may perform better in different setups, although the Daubechies wavelet 6 wavelet 6 was among the best few in all the setups we tested.

#### IV. IMPLEMENTATION

The wavelet-based technique has the same sampling stage as described in Section II-C. The sampling stage produces two sequences of delay samples,  $D_1(t)$  and  $D_2(t)$ . The processing stage uses wavelet denoising to produce new, denoised sequences  $\tilde{D}_1(t)$  and  $\tilde{D}_2(t)$ , as explained in Section III-B. The cross-correlation coefficient  $XCOR_{12}$  is computed from  $\tilde{D}_1(t)$ and  $\tilde{D}_2(t)$ . (The computational overhead of these operations is very low. We found that when delay samples were collected at 10 Hz for 100 s for each of two paths, a machine with a 2.53-GHz Intel Pentium 4 CPU took only a few milliseconds to finish the operations.) As in the basic technique, the procedure to gather delay sequences for different paths is applicationdependent and beyond the scope of this paper.

There are three issues to discuss in implementing the waveletbased technique: the delay sampling rate, synchronization offset between delay sequences, and the threshold for the binary decision.

## A. Sampling Rate

There is a tradeoff in choosing the sampling rate of a delay sequence. High-rate sampling is more accurate but incurs a large overhead on the network. On the other hand, low-rate sampling has little overhead while being slow to converge. To investigate the effect of sampling rate on performance, we performed simulations with different sampling rates on the topology shown



Fig. 8. Cross-correlation coefficients for sampling rate of 10 Hz.



Fig. 9. Effect of sampling rate.

in Fig. 3. The sequence of delay samples for each path was processed with our wavelet denoising method. To minimize effects from synchronization offset, we used a topology with a common source. The source nodes were colocated and their clocks were synchronized. A full evaluation involving synchronization offset will be presented in Section V. Each link had a bandwidth of 1.5 Mb/s, and ON-OFF CBR flow parameter settings were identical to those in Section II-D. To simulate shared congestion, we put 100 ON-OFF CBR flows on the shared link, and 60 on the other two links. With 60 flows, no packet loss was observed. The loss rate with 100 flows varied between 2% and 12%. For independent congestion, we put 60 ON-OFF CBR flows on the shared link, and 100 on the others.

Given a sampling rate, an experiment was repeated 500 times for each of shared and independent congestion. Fig. 8 plots the cross-correlation coefficient with the sampling rate of 10 Hz as time elapses. Each curve is the mean cross-correlation coefficients over 500 experiments, and a vertical bar represents the interval between the 5th and 95th percentile values at a specific time.

Fig. 9 plots the mean cross-correlation coefficient over 500 experiments for five different sampling rates. The behavior consistent over all sampling rates is that the coefficients converge either to one or to zero as more and more samples are collected. With all sampling rates except 1 Hz, the cross-correlation coefficient converges within 10 s. Their variance is also small; after 5 s, the interval between the 5th and 95th percentile values with shared congestion never overlaps with the corresponding interval with independent congestion for every rate but 1 Hz.

Since our technique is implemented in user space, the granularity of a timer in an operating system kernel should also be taken into account. Though recent operating systems provide clock rate of 100 Hz, older ones have only 10 Hz. From the figure, we conclude that a sampling rate of 10 Hz is fast enough in convergence and feasible to implement on most operating systems.

#### B. Limiting Synchronization Offset

There is a synchronization offset in the two sequences of delay samples collected. However, using simple techniques, the synchronization offset between any two paths on the Internet can usually be limited to 1 s. In Fig. 1, the synchronization offset of two paths, from  $X_{src}$  to  $X_{dst}$  and from  $Y_{src}$  to  $Y_{dst}$ , is caused by: 1) the difference of the delay from  $X_{src}$  to S and the delay from  $Y_{src}$ . 1) is bounded by the maximum one-way delay on the network and 2) by half the round-trip time between  $X_{src}$  and  $Y_{src}$  since the clocks in these two nodes can be synchronized by exchanging packets. So the maximum offset is roughly the maximum round-trip time on the network. Measurement studies including one by CAIDA<sup>4</sup> confirm that round-trip time is less than 1 s for the vast majority of paths on the Internet.

#### C. Threshold for Binary Decision

Though cross correlation itself is a reasonable measure of shared congestion, in situations where a binary answer is preferred, a threshold should be set. Since cross correlation converges to one (or zero) for shared (or independent) congestion as in Fig. 9, our technique is not sensitive to the threshold in such cases. However, because synchronization offset reduces correlation of paths sharing a congested link (as shown in Fig. 2), it is still important to investigate an appropriate value for the threshold.

When cross-correlation coefficients of delay sample sequences with shared and independent congestion are close to each other, two types of errors may occur: false positives and false negatives. The former is the case where the technique reports shared congestion when there is no shared congested link, and the latter is the case where it reports nonshared congestion when there is one or more congested links shared by two paths. The error rate of each type can be estimated from distributions of cross-correlation coefficients for shared and independent congestion. Then the threshold can be adjusted to minimize the total cost of errors using Bayesian testing. Our implementation assumes that the cost of false positive and the cost of false negative are equal, and minimizes the total error rate, which is the sum of the false positive ratio and the false negative ratio. Actual costs may differ from application to application.

To determine the best threshold value, we need an estimate of the synchronization offset for any two paths on the Internet. According to measurements by CAIDA, most paths from the F DNS root server to its customers have a round-trip time of less than 300 ms. Considering that customer hosts of a DNS root



Fig. 10. Cross-correlation coefficient distributions.

server are close to the server, we take 600 ms as the target synchronization offset to optimize the threshold for. More investigation is needed on the actual distribution of round-trip times and the relationship between the target offset and the accuracy of the binary decision.

Fig. 10 shows the distributions of cross-correlation coefficients with 600 ms synchronization offset. The distributions were obtained from the same delay sequences used in Section IV-A. We used the delay samples collected during the first 10 s, with the sampling rate of 10 Hz. The left histogram represents the distribution for independent congestion, and the right one for shared congestion. If we approximate the histograms with normal distributions, they intersect when the cross-correlation coefficient (*XCOR*) is 0.512, which would be the threshold value that minimizes the total error rate. (The error rate is not sensitive to the choice of the threshold value as long as the threshold is between 0.3 and 0.6, because *XCOR* is rarely close to 0.512.) We use this value as the threshold in later experiments, unless stated otherwise. We will investigate the effect of the threshold on false positive and false negative ratio in Section IV-B.

## V. PERFORMANCE EVALUATION

In simulations, we compare our technique against two representative techniques: a delay-based approach of Rubenstein *et al.* [5] and a loss-based one of Harfoush *et al.* [4], [9]. Below we refer to them respectively as MP (Markovian probing) and BP (Bayesian probing). See Section II-E for descriptions of both techniques.

We define *Positive Ratio* as a metric to represent the accuracy of each technique:

Positive Ratio  
= 
$$\frac{\# \text{ of answers indicating shared congestion}}{\# \text{ of experiments}}$$
. (8)

If an experimental setup involves shared congestion, Positive Ratio should be close to one; otherwise, it should be close to zero.

We first compare our technique with MP and BP when paths share a common source node and have either shared congestion or independent congestion only. Then we investigate how they perform in more challenging environments involving paths not sharing a common source or destination and multiple points of congestion. Finally, we present initial results on the performance of our technique on the Internet.



Fig. 11. Topology with a common source.

#### A. Probing With a Common Source

Both MP and BP assume that there is a common source (or a common destination for MP). For such a topology, clocks for the two paths can be synchronized and two samples can be merged into one in chronological order. This is a critical requirement for both techniques. In fact, BP requires the stronger condition that two probe packets with different destinations must be sent back to back.

Fig. 11 shows a network topology where two paths share a source node. Each link has a bandwidth of 1.5 Mb/s. A similar topology was used in simulations for MP [5]. We ran experiments for the following three scenarios depending on the type of background traffic.

**Long-lived TCP flows:** A small number of long-lived TCP flows with different round-trip times are used to cause congestion, and non-congested links are left idle. In shared congestion cases, a link is chosen from links 1 through 3, and 20 TCP flows are created to traverse the link. In independent congestion cases, links 1 through 3 are idle, and the other links have TCP flows, of which the number is chosen uniformly between 0 and 20.

**ON-OFF CBR flows:** A large number of ON-OFF CBR flows are used as background traffic. The congestion level is controlled with the number of such flows. For shared congestion, a link chosen from links 1 through 3 has 100 ON-OFF CBR flows. The number of ON-OFF CBR flows on the other links is chosen uniformly between 31 and 70. For independent congestion, links 1 through 3 have ON-OFF CBR flows between 31 and 70, and the other links between 61 to 100. The same parameter settings of ON-OFF CBR flows as in Section II-D are used.

Short-lived TCP flows A large number of short-lived TCP flows with different round-trip times, created by ns-2's web traffic generator, are used as background traffic. The generated traffic consists of many "web sessions," in each of which a client node continually downloads from a server a web page containing multiple objects. For shared congestion, a link chosen from links 1 through 3 has 250 web sessions created by 25 web servers and 250 clients. The number of web sessions on the other links is chosen uniformly between 1 and 25. For independent congestion, links 1 through 3 have web sessions between 1 and 25, and the other links have web sessions between 151 and 250.

1) Detection Accuracy: Fig. 12 plots Positive Ratio of each technique over 500 experiments as time progresses when links are using drop-tail queues. In the legend, DCW refers to our delay correlation technique with wavelet denoising. With long-lived TCP background, MP is fast in detecting both shared and independent congestion, while BP is relatively slow in both cases. DCW is slightly faster than MP for shared congestion, but as slow as BP for independent congestion. Overall, every technique works well and reaches accuracy of over 90% within 10 s.



Fig. 12. Convergence for a common source and drop-tail queues.



Fig. 13. Convergence for a common source and RED queues.

With ON-OFF CBR background traffic, however, all three techniques are slower in detecting shared congestion than with longlived TCP background traffic. For DCW and MP, this is because noncongested links have small queueing delay fluctuations. For DCW, such fluctuations add noise to delay samples; for MP, they change the order in the merged samples and thus decrease  $M_x$ . Nevertheless, since DCW removes most noise through wavelet denoising, its degradation is not as severe as MP's. BP experiences the most notable degradation among the three; though it is the fastest for independent congestion, its Positive Ratio for shared congestion is still less than 0.6 after 100 s. This is because our ON-OFF CBR background flows include some with very short ON/OFF time, while all ON-OFF CBR flows in the simulations of [4] have relatively long ON time-2 s. BP requires the probability that both packets in a packet pair are lost to be high to detect shared congestion. A longer ON time means a queue remains full for a long time causing both packets in the pair to be dropped. However, it is less likely with short ON time. That leaves DCW to be the only technique that reaches 90% accuracy after 10 seconds with ON-OFF CBR background. Degradation of BP is even more pronounced with short-lived TCP background, because a loss period is even shorter in that scenario. As a result, BP fails to detect shared congestion. On the other hand, DCW and MP are not affected much.

Fig. 13 presents results from simulations with links using RED. DCW and MP showed similar performance as with droptail queues. However, BP did not work at all with RED queues. Its problem with RED was already pointed out using ON-OFF CBR flows [4], but the problem was more serious in our simulations because their simulation setup had a higher loss rate and smaller queues, which means that a RED queue's behavior was close to that of a drop-tail queue. Neither DCW nor MP had



Fig. 14. Effects of clock skew (the vertical axis does not start from zero.).

such a problem; they maintained performance as good as with drop-tail queues.

2) Effects of Clock Skew: The clock skew between two hosts measuring delay may affect the cross-correlation coefficient value, reducing the Positive Ratio for shared congestion. In Fig. 14, we plot XCOR with clock skew using the simulation data for the DCW curve with shared congestion in Fig. 12(b). To simulate clock skew, a linearly increasing offset was added to one of the two delay sequences. The value of the horizontal axis is the maximum time skew, or the offset at the end the measurement (after 100 s). Fig. 14 shows the decrease of XCOR as the clock skew increases. Nevertheless, XCOR is still close to



Fig. 15. Topology with no common endpoint.



Fig. 16. Effect of synchronization offset.

0.9 when the maximum time skew is 1 s. As this corresponds to gaining more than 14 min every day, clock skew is expected to be much less and thus its effects on *XCOR* is negligible.

## B. Probing With No Common Endpoint

The topology in Fig. 15 is an extended version of that in Fig. 11. The paths have different source and destination nodes. Delay samples collected at different nodes cannot be synchronized because of two reasons. First, the clocks of node  $X_{src}$  and node  $Y_{src}$  are not synchronized. Second, the delay from  $X_{src}$  to S is different from the delay from  $Y_{src}$  to S.

1) Effects of Synchronization Offset: To investigate the effect of synchronization offset between two paths, we plot, in Fig. 16, the Positive Ratio for experiments with shared congestion as we increase the synchronization offset for all three types of background traffic. The original sets of delay samples were obtained from the two paths on the topology in Fig. 11; the synchronization offset was added to the set of delay samples between  $Y_{src}$  and  $Y_{dst}$ . Only the overlapping portions were used. BP is excluded; its Positive Ratio with shared congestion is 0.2 or less even with 10 ms offset [4], due to its requirement that two packets (for different paths) be sent back-to-back. Because MP is slower than DCW in Positive Ratio convergence for shared congestion, MP may exhibit lower performance because of low accuracy if the number of delay samples is not large. Thus, detection used delay samples belonging to the first 100 seconds of



Fig. 17. Effect of wavelet denoising on cross correlation with synchronization offset.

the overlapping period to ensure that both MP and DCW had near-100% accuracy. The Positive Ratio drops to zero between 30 and 70 ms for MP, and between 1 and 2 s for DCW. The sharp decrease of MP happens in the [30 ms, 70 ms] interval because the average probe rate in MP is 25 Hz, equivalent to 40 ms inter-departure time. Therefore, if the offset exceeds that value, most packets in a merged sequence are out of order, and the cross measure  $M_x$  becomes low. Though we plot the results for drop-tail queues only, the results for RED queues are similar.

Next, we examine how wavelet denoising helps our technique in tolerating a large synchronization offset. The dotted curve and vertical bars crossing it in Fig. 17 are copied from Fig. 2, which shows the cross-correlation coefficients without wavelet denoising. We processed the data used in Fig. 2 with our wavelet denoising and plotted cross-correlation coefficient versus synchronization offset. The solid curve represents the mean cross-correlation coefficients, and the vertical bars indicate the 5th and 95th percentile values. Without wavelet denoising, the cross correlation of the delay sequences decays very fast with increase of synchronization offset; with a 600 ms offset, the mean coefficient approaches the horizontal line representing the threshold (0.512). This means that the cross-correlation technique without denoising is only as good as a random decision at this point. However, the cross correlation of the delay sequences after wavelet denoising is less sensitive to the synchronization offset, so that one can properly determine the state of congestion even with a fair amount of synchronization offset between the data. On the other hand, for independent congestion, the mean cross-correlation coefficients are not affected by wavelet denoising and are almost zero regardless of the synchronization offset. It is also confirmed in Fig. 20.

Since synchronization offset may vary during delay measurements, we also performed an experiment with a randomized synchronization offset. For a given value of average synchronization offset m, the actual synchronization offset for a particular pair of packets in the two sequences of an experiment was chosen randomly over the interval [0, 2 m]. The mean cross-correlation results were almost the same as those in Fig. 17; the variances were larger due to the presence of randomized synchronization offsets.



Fig. 18. ROC with and without wavelet denoising.

2) Threshold Value and False Positive/negative: We use the receiver operating characteristic (ROC) curves to show the effect of the threshold value on false positive and false negative ratio in the presence of synchronization offset. ROC is a performance test methodology that measures the probability of detection  $P_D$  against the probability of false positive  $P_F[21]$ . In our application, they are defined as follows for a certain threshold value of cross correlation  $T_{XCOR}$ .

 $P_D = P(XCOR \ge T_{XCOR} \mid \text{shared congestion})$  $P_F = P(XCOR \ge T_{XCOR} \mid \text{independent congestion}).$ 

ROC performance can be graphically detected for all possible values of threshold  $T_{XCOR}$ ; as we move along an ROC curve from the lower left corner to the upper right corner, the threshold varies from 1 to -1. The dashed straight line is the characteristics of the worst case, where the detection probability  $P_D$  equals the false positive probability  $P_F$ .

Fig. 18 has two ROC curves drawn using the DCW simulation data for Fig. 12. An offset of 600 ms was added to one of the delay sequences of each experiment. The dotted curve is an ROC curve before wavelet denoising, and the solid curve is after denoising. Since our technique converges in 10 s, delay samples for the first 10 s were used to compute the cross-correlation coefficient. With wavelet denoising, our technique shows an improved curve (higher detection probability  $P_D$  with the same false positive probability  $P_F$ ) compared with the curve without denoising.

Note that the area under the curve, called the ROC area, provides a quantitative measure of performance for comparison of different curves; the area of an ideal curve is 1, while the area of a random decision maker is  $\frac{1}{2}$ . Fig. 19 demonstrates the effect of wavelet denoising for different synchronization offsets using ROC area. Two curves show the ROC area with and without wavelet denoising as the synchronization offset increases. With tight synchronization, wavelet denoising makes little difference. As the offset increases, however, the basic technique curve drops to 0.6 at an offset of 1 second, becoming close to random decision. On the other hand, the technique with denoising degrades smoothly, maintaining 0.8 at the 1 s offset.

3) Comparison With Low-Pass Filtering: When congestion occurs on shared links, wavelet denoising makes cross-correlation evaluation more robust by smoothing delay data curves. We



Fig. 19. ROC performance versus synchronization offset (the vertical axis does not start from zero.).



Fig. 20. Comparison of low-pass filtering and wavelet denoising for independent congestion.

tested a simpler mechanism to achieve this smoothing, namely a simple low-pass filter. With suitable parameters, a moving average was able to provide similar improvement as wavelet denoising for cases with shared congestion. (We set the span of the moving average to 1.1 s, which provides the same improvement as wavelet denoising for the experiments of Fig. 17.) The problem with this filter appears in experiments with independent congestion. Fig. 20 shows the convergence of the cross-correlation coefficient for the moving average (MA) and DCW when there is independent congestion in the experiment of Fig. 12(b). Each point is the mean coefficient over 500 simulations; the bars show 5th and 95th percentiles. The mean coefficient of the moving average at 100 s is still 0.6, while that of DCW is almost zero from the beginning. That is, a simple low-pass filter may over-smooth transients at small scales, and thus require more delay samples to detect independent congestion. The ability of wavelet denoising to preserve strong transients at both small and large scales is critical for fast convergence in both shared and independent congestion scenarios.

## C. Multiple Points of Congestion

So far, queueing delay variation on noncongested links was filtered out with wavelet denoising. However, if noncongested links have significant queueing delay variation, or there is more than one point of congestion, the delay variation on such links cannot be eliminated and makes shared congestion detection more difficult. In fact, it is unclear what 'shared congestion'



Fig. 21. Positive Ratio for multiple points of congestion.

should mean under such conditions. Therefore, instead of deciding whether a technique detects shared congestion correctly, we investigate how the technique responds as the degree of shared congestion changes. One possible metric to represent the degree of shared congestion is how large the loss rate on shared links is compared with that on nonshared links. Hence, we define a new quantity called *shared loss rate ratio*. Let the loss rate of the shared portion of two paths be  $L_{\text{shared}}$  and the loss rate of the nonshared portion of the first path to be  $L_1$  and the second path  $L_2$ . Then, the shared loss rate ratio is defined as follows:

$$L_s = \frac{L_{\text{shared}}}{L_{\text{shared}} + \max(L_1, L_2)}.$$
(9)

If  $L_{\text{shared}} > 0$  and  $L_1 = L_2 = 0$ , then  $L_s$  becomes 1; if  $L_{\text{shared}} = 0$  and at least one of  $L_1$  and  $L_2$  is not zero, then  $L_s$  becomes 0. If there is no loss at all, then  $L_s$  is defined as 0, indicating no shared congestion. Note that  $L_s$  is useful only when the maximum queueing delays of congested links are in the similar order of magnitude. Otherwise, the one-way delay variation would be dominated by the queueing delay fluctuations of links with larger queues, and the losses on other links would not matter. In other words, DCW may fail to detect shared congestion on links with small delays.

In the following simulation, we used the topology in Fig. 3. The number of ON-OFF CBR background flows on each link was chosen uniformly between 81 and 100, resulting in loss rate between 0% and 12%, and delay samples were collected for 100 seconds.  $L_s$  was computed from the actual loss rates of the links. 1000 experiments were classified into ten groups depending on the interval their  $L_s$  belonged to. If  $L_s$  of an experiment is in [0, 0.1) then it is in the first group, if in [0.1, 0.2) then the second, and so on. If  $L_s = 1$ , the experiment is in the same group as those with  $L_s$  in [0.9, 1). Positive Ratio [defined in (8)] was calculated over all experiments in the same group. The results for DCW, MP, and BP are presented in Fig. 21.

Positive Ratio of DCW is only about 0.1 when  $L_s < 0.1$ , but 0.8 or larger when  $L_s \ge 0.3$ . Thus, DCW has a cutoff at  $L_s = 0.2$  differentiating shared and independent congestion. MP shows very different behavior. Positive Ratio is 0 for most intervals, and only 0.1 for the last one. Since we know that Positive Ratio of MP reaches 1 after 100 s if  $L_s = 1$ , this indicates that MP answers positively (meaning shared congestion) only



Fig. 22. Experimental topology on the Internet.



Fig. 23. Convergence for Internet traces.

when  $L_s$  is very close to 1. In other words, MP always gives a negative answer if there are multiple points of congestion, regardless of the degree of shared congestion. BP gives more and more positive answers as  $L_s$  increase, but does not have any sharp increase such as DCW has. Therefore, for those applications requiring a cutoff in shared congestion detection, DCW is preferred. However, the preferred cutoff value depends on the application. DCW can be customized for applications with different needs by adjusting its the threshold. Some applications need to determine whether two paths share *all* congested links [22], which corresponds to  $L_s = 1$ . In this case, MP would be a good choice.

## D. Internet Experiments

We applied our technique to a large-scale network, the Internet. Our first Internet experiments involved six end hosts. Fig. 22 shows their abstract topology. Note that each hop in the figure may consist of multiple physical hops. Three hosts,  $A_1$ ,  $A_2$ , and  $A_3$ , are located in Austin, TX. The other three hosts, K, T, and H, are located in Korea, Taiwan, and Hong Kong, respectively.

Delay samples were collected from the paths from  $A_1$  to Kand from  $A_2$  to T between October 28 and November 2, 2003. We can reasonably conclude that there was no congested link because no probe packet was lost during measurement. In order to create a shared bottleneck, we opened 40 TCP sessions between H and  $A_3$ . The loss rate was about 5% while they were running. Since both paths experienced a similar loss rate, we conclude that the congestion occurred on one of the shared links.

The Positive Ratio for shared congestion and independent congestion (or no congestion in this case) is shown in Fig. 23. The delay samples were collected for 15 seconds, and time was adjusted with measured clock difference between  $A_1$  and  $A_2$ 



Fig. 24. Results on PlanetLab.

by exchanging packets between them. Each experiment was repeated 100 times to calculate the Positive Ratio. The result resembles what we obtained through simulations. The accuracy of our technique exceeds 80% using the samples for the first 3 seconds, and reaches 98% after 8 s. We also performed experiments on PlanetLab<sup>5</sup> using the topology in Fig. 1. The experimental setup is similar to the one used in [23]. We selected arbitrary six nodes, among which two functioned as application-level routers (S and T in Fig. 1), forwarding UDP probe packets sent by  $X_{src}$ and  $Y_{src}$  for 150 s per experiment. We verified with traceroute that the paths from  $X_{src}$  and  $Y_{src}$  to S as well as the paths from T to  $X_{dst}$  and  $Y_{dst}$  did not share links. Delay samples were collected from about 100 experiments conducted in August and September 2006. We assume that there is shared congestion if the loss rate on the shared path is larger than that of any other paths. The solid curve in Fig. 24 represents the Positive Ratio for shared congestion, which converges after 7 s. The Positive Ratio of the other experiments, plotted as a dotted curve, reaches 0.3 after 30 s and remains as such. Note that the low accuracy in the latter experiments is in part due to our "conservative" criteria for shared congestion; even though the shared loss rate is lower than nonshared loss rates in those experiments, it does not necessarily mean that there was no shared congestion. In fact, visual inspection of delay traces revealed that there were often indications of congestion (large delay fluctuations) on the shared path, even though the shared loss rate was negligible.

## VI. CONCLUSION AND FUTURE WORK

Network resources are better utilized when multiple flows cooperate. However, such cooperation is feasible only when we can identify flows sharing a congested bottleneck. Previously proposed techniques had limitations, including a common endpoint and (sometimes) drop-tail routers. But they are not effective under other conditions, such as RED queueing, multiple points of congestion, or paths with different sources and destinations.

We proposed a robust technique based on wavelet denoising and cross correlation, namely DCW. The denoising process effectively removes noise and makes our technique more resilient to synchronization offset, which confuses other techniques. In simulations with shared congestion, DCW achieves faster convergence and broader application than previous techniques, while using fewer probe packets. Experiments on the Internet confirmed the simulation results. DCW can also handle a large number of paths in a scalable manner [24]. We believe that applications requiring topology construction in the application layer can benefit from our delay correlation technique with wavelet denoising.

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