

# Digital Signatures for Flows and Multicasts\*

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## Abstract

We present chaining techniques for signing/verifying multiple packets using a single signing/verification operation. We then present flow signing and verification procedures based upon a tree chaining technique. Since a single signing/verification operation is amortized over many packets, these procedures improve signing and verification rates by one to two orders of magnitude compared to the approach of signing/verifying packets individually. Our procedures do not depend upon reliable delivery of packets, provide delay-bounded signing, and are thus suitable for delay-sensitive flows and multicast applications. To further improve our procedures, we propose several extensions to the Feige-Fiat-Shamir digital signature scheme to speed up both the signing and verification operations, as well as to allow “adjustable and incremental” verification. The extended scheme, called eFFS, is compared to four other digital signature schemes (RSA, DSA, ElGamal, Rabin). We compare their signing and verification times, as well as key and signature sizes. We observe that (i) the signing and verification operations of eFFS are highly efficient compared to the other schemes, (ii) eFFS allows a tradeoff between memory and signing/verification time, and (iii) eFFS allows adjustable and incremental verification by receivers.

## 1. Introduction

Data confidentiality, authenticity, integrity, and non-repudiation are basic concerns of securing data delivery over an insecure network, such as the Internet. *Confidentiality* means that only authorized receivers will get the data; *authenticity*, an authorized receiver can verify the identity of the data’s source; *integrity*, an authorized receiver can verify that received data have not been modified; *non-repudiation*, an authorized receiver can prove to a third party the identity of the data’s source.<sup>1</sup>

Most investigations on securing data delivery over packet networks have focused on unicast delivery of data

sent as independent packets. Exceptions include recent papers on scalable secure multicasting [1, 13, 20] and a flow-based approach to datagram security [14]. All of these papers are mainly concerned with data confidentiality.

In this paper, our concerns are data authenticity, integrity and non-repudiation for delay-sensitive packet flows, particularly flows to be delivered to large groups of receivers. For an individual message (packet), these concerns can be addressed by one of many available digital signature schemes [6, 15, 17, 19]. However, these schemes are not efficient enough for signing/verifying packets individually for delay-sensitive flows, such as packet video.

In the Internet, multicast has been used successfully to provide an efficient, best-effort delivery service to large groups [2]. Consider a packet flow multicasted to a group of receivers. A consequence of best-effort delivery is that many receivers will not receive all of the packets in the multicasted flow. Furthermore, many multicast applications allow receivers to have widely varying capabilities (e.g., to receive layered video and audio transmissions) or needs (e.g., to receive different stock quotes, news, etc.). Consequently, receivers get different subsequences of packets from the same multicasted flow.

### 1.1. Existing techniques for signing flows

Conceptually, a digital signature scheme is defined by functions for key generation, signing, and verification. The signer (sender) uses the key generation function to create a pair of keys, a signing key,  $k_s$ , and a verification key,  $k_v$ . The signer keeps the signing key private, and makes the verification key publicly known to all verifiers (receivers).<sup>2</sup>

To sign a message  $m$  using signing key  $k_s$ , the signer calls the signing function which returns the signature of message  $m$ . The signer then sends the signed message, consisting of message  $m$  and its signature, to verifiers. Having received the signed message, a verifier calls the verification function with key  $k_v$ . If the verification function returns true, then the verifier concludes that the signer did sign the message and the message has not been altered. Moreover,

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<sup>1</sup>In the balance of this paper, we use “receiver” to mean “authorized receiver” unless otherwise stated.

<sup>2</sup>The signing and verification keys are also referred to as private and public keys, respectively.

the signer cannot deny having signed the message (non-repudiation).

In practice, a message digest function, such as MD5 [18], is first applied to the message to generate a fixed-size message digest which is independent of message size. Signing a message means signing the digest of the message. (MD5 message digests are 128 bits long.)

A *flow* is a sequence of packets characterized by some attribute [16, 22]. Packets in a flow may be obtained from segmenting the bit stream of digitized video, digitized audio, or a large file. Or they may be related data items, such as stock quotes, news, etc., generated by the same source.

It is easy and efficient to sign an *all-or-nothing* flow, that is, a flow whose entire content is needed before any part of it can be used, e.g., a long file. In this case, the signer simply generates a message digest of the entire flow (file) and sign the message digest.

Most applications, however, create flows that are not all-or-nothing, i.e., a receiver needs to verify individual packets and use them before the entire flow is received. For these flows, a straightforward solution is to sign each packet individually and each packet is verified individually by receivers. This solution is called the *sign-each* approach.

The sign-each approach is computationally expensive. The signing rate and verification rate are at most  $1/(T_d(l) + T_{sign})$  and  $1/(T_d(l) + T_{verify})$  packets per second, respectively, where  $T_d(l)$  is the time to compute the message digest of an  $l$ -byte packet,  $T_{sign}$  is signing time, and  $T_{verify}$  is verification time for the message digest. The signing and verification rates,<sup>3</sup> in packets per second, of two widely used digital signature schemes, RSA [19] and DSA [15], with 512-bit modulus and using 100% processor time of a Pentium II 300 MHz machine are shown below.

packet size (bytes)	Signing rate		Verification rate	
	RSA	DSA	RSA	DSA
512	78.8	176	2180	128
1024	78.7	175	1960	127
2048	78.0	172	1620	126

If a slower machine is used, or only a fraction of processor time is available for signing/verification (e.g., a receiver machine has only 20% processor time for verification because the other 80% is needed for receiving and processing packets), then the rates should be decreased proportionally.

The signing rate is not important for a *non-real-time generated* flow, i.e., a flow whose entire content is known in advance (such as stored video). This is because packets in the flow can be signed in advance. For a real-time generated flow, however, the signing rate must be higher than the packet generation rate of the flow. Furthermore, for delay-sensitive flows, real-time generated or not, the verification

rate is important. From the table, we see that the signing and verification rates of the sign-each approach, using either RSA or DSA, are probably inadequate for many applications.

Two techniques were proposed for signing digital streams in [7] which, at first glance, may be used for signing packet flows. To describe the technique in [7] for signing a non-real-time generated flow, consider a sequence of  $m$  packets. The sender first computes message digest  $D_m$  of packet  $m$  (the last packet) and concatenates packet  $m - 1$  and  $D_m$  to form augmented packet  $m - 1$ . Then, for  $i = 1, \dots, m - 2$ , the sender computes message digest  $D_{m-i}$  of augmented packet  $m - i$ , and concatenates packet  $m - i - 1$  and  $D_{m-i}$  to form augmented packet  $m - i - 1$ . Message digest  $D_1$  of augmented packet 1 is computed and signed. In this manner, only one expensive signing/verification operation is needed for the sequence of  $m$  packets. However, a necessary condition for using the above technique is the following *get-all-before* requirement: To verify packet  $i$  in the sequence, a receiver must have received every packet from the beginning of the sequence.

For a real-time generated flow, a similar technique is suggested in [7] with the same get-all-before requirement. For a sequence of  $m$  packets, only one expensive signing/verification operation is needed, plus one inexpensive *one-time signature* signing/verification for each packet in the sequence. However, since one-time signatures and keys are very large, this technique has a large communication overhead (around 1000 bytes per packet) [9, 10].

The get-all-before requirement of both techniques in [7] is too strong for practical Internet applications. Reliable packet delivery is not used by many applications for flows and multicasts. For example, reliable delivery is generally not used for video and audio flows due to the extra delays associated with retransmissions; either losses are tolerated or forward error correction techniques are used instead.

For large-scale multicast applications, reliable delivery of multicast packets is a difficult problem [5]. Moreover, even if reliable multicasting is available, receivers with different needs/capabilities may choose to get different subsequences of packets in a multicasted flow. In short, the get-all-before requirement is not satisfied.

## 1.2. Characteristics and requirements

We have observed various characteristics in the delivery of flows and multicasts by an unreliable packet network, such as the Internet. They are summarized below:

- Each packet in a flow may be used as soon as it is received.
- A receiver may get only a subsequence of the packets in a flow. Different receivers may get different subsequences.
- Delay sensitive flows require fast processing at a sender as well as receivers. Some flows are generated

<sup>3</sup>The signing and verification rates are for signing and verifying 128-bit MD5 message digests of packets.

in real time by their senders.

- For a multicasted flow, many receivers are limited in resources (processing capacity, memory, communication bandwidth, etc.) compared to the sender, which is typically a dedicated server machine. In some environments, both senders and receivers may be limited in resources, e.g., mobile computers using wireless communications.
- Receivers may have widely different capabilities/resources. For example, receivers may be personal digital assistants, notebook computers, or desktop machines. Moreover, the resources available to a receiver for verifying signatures may vary over time.

Given the above characteristics, we design procedures for signing and verifying flows in Section 2 as well as a digital signature scheme in Section 3 to meet the the following requirements:

- The signing procedure is efficient and delay-bounded (for real-time generated flows).
- The verification procedure is highly efficient (since many receivers have limited resources).
- Packets in a flow are *individually verifiable*.
- Packet signatures are small (i.e., small communication overhead).
- *Adjustable and incremental verification*: The verification operation is adjustable to the amount of resources a receiver has. It allows a receiver/verifier to verify a message at a lower security level using less resources, and later increase the security level by using more resources (e.g., if the message is important).

### 1.3. Contributions of this paper

In Section 2, we first describe and compare two chaining techniques (star and tree) for signing/verifying multiple packets using a single signing/verification operation (without the get-all-before requirement in [7]). We then present flow signing and verification procedures based upon the tree chaining technique. Since a single signing/verification operation is amortized over many packets, these procedures improve signing and verification rates by one to two orders of magnitude compared to the sign-each approach. The signing procedure also provides delay-bounded signing. Thus the procedures can be used for delay-sensitive flows.

In Section 3, we turn our attention to improving the signing and verification operations in the procedures. Specifically, we present several extensions to the Feige-Fiat-Shamir digital signature scheme to speed up both signing and verification as well as to allow adjustable and incremental verification. In Section 4, the extended Feige-Fiat-Shamir (eFFS) scheme is compared to four well-known signature schemes [6, 15, 17, 19]. We compare their signing and verification times, as well as key and signature

sizes. We observe that (i) the signing and verification operations of eFFS are highly efficient compared to the other schemes, (ii) eFFS allows a tradeoff between memory and signing/verification time, and (iii) eFFS allows adjustable and incremental verification by receivers.

## 2. How to Sign a Flow

To digitally sign/verify delay-sensitive flows, the sign-each approach is computationally too expensive for many applications, particularly those applications that generate packet flows in real time.

As an alternative to the sign-each approach, we present two chaining techniques (star and tree) for providing authenticity to a group of packets, called a *block*, using a single signing operation. The basic idea is to compute a block digest which is signed. In order to make packets *individually verifiable*, each packet needs to carry its own authentication information consisting the signed block digest (*block signature*) together with some chaining information as proof that the packet is in the block.

### 2.1. Star chaining

Consider  $m$  packets that constitute a block. In star chaining, the block digest is simply the message digest of the  $m$  packet digests (listed sequentially). Let  $h(\cdot)$  denote the message digest function being used (e.g., MD5). Consider, for example, a block of eight packets with packet digests  $D_1, \dots, D_8$ . The block digest is  $D_{1-8} = h(D_1, \dots, D_8)$ , and the block signature,  $sign(D_{1-8})$ , is the block digest signed with some digital signature scheme (such as RSA, DSA or eFFS).

The relationship between the packet digests and the block digest can be represented by a one-level rooted tree, called an *authentication star*. Figure 1 illustrates an authentication star for eight packets, with packet digests at leaf nodes, and the block digest at the root.

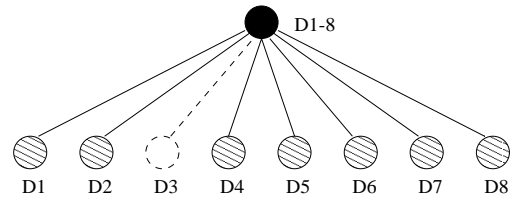


Figure 1. Star chaining technique.

For packets to be individually verifiable, each packet needs its own authentication information. Such authentication information, called *packet signature*, consists of the block signature, the packet position in the block, and the digests of all other packets in the block. (We use the term *chaining overhead* to refer to all information in a packet signature except the block signature.)

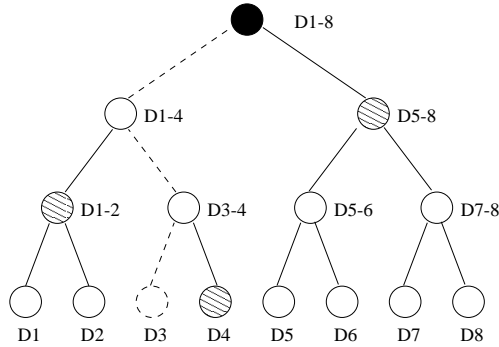
Suppose the third packet in the above example is received. Its authenticity can be individually verified as follows. The verifier computes the digest  $D'_3$  of the

packet received, and then the block digest  $D'_{1-8} = h(D_1, D_2, D'_3, D_4, \dots, D_8)$ , where  $D_1, D_2, D_4, \dots, D_8$  are carried in the packet signature. The verifier then calls the verification operation to verify  $D'_{1-8}$ , i.e., to determine whether  $D'_{1-8}$  is equal to block digest  $D_{1-8}$  in block signature  $sign(D_{1-8})$ . The packet is verified if the verification operation returns true, i.e.,  $D'_{1-8} = D_{1-8}$ .

Suppose the third packet is the first in the block to arrive and its authenticity has been verified. Afterwards, the verifier knows every node in the authentication star, i.e., all nodes in the authentication star are verified and can be cached. With caching, when another packet in the block arrives later, say the sixth packet, the verifier only needs to compute the digest  $D'_6$  of the packet received and compare it to the verified node  $D_6$  in the authentication star. If they are equal, the packet is verified.

## 2.2. Tree chaining

Tree chaining subsumes star chaining as a special case. With tree chaining, the block digest is computed as the root node of an *authentication tree*.<sup>4</sup> Consider, for example, a block of eight packets with packet digests  $D_1, \dots, D_8$ . The packet digests are the leaf nodes of a degree two (binary) authentication tree, with other nodes of the tree computed as message digests of their children, as shown in Figure 2. For example, the parent of the leaves  $D_1$  and  $D_2$  is  $D_{12} = h(D_1, D_2)$  where  $h(\cdot)$  is the message digest function being used. The root is the block digest, with the block signature being the signed block digest.



**Figure 2. Tree chaining technique.**

For a packet to be individually verifiable, each packet needs to carry its own authentication information (packet signature). In tree chaining, a packet signature consists of the block signature, the packet position in the block, and the siblings of each node in the packet's path to the root. (Again we use the term *chaining overhead* to denote all information in a packet signature except the block signature.)

To verify a packet individually, a verifier needs to verify its path to the root. Consider, for example, the dashed path

<sup>4</sup>Tree chaining was first presented in [11]. Any rooted tree can be used as an authentication tree with packet digests at leaf nodes and the block digest at the root. In particular, there is no need to use a balanced tree.

in Figure 2 for the third packet. Each node in the path needs to be verified. A verifier computes the digest  $D'_3$  of the received packet, and then each of its ancestors in the tree. That is,  $D'_{3-4} = h(D'_3, D_4)$ ,  $D'_{1-4} = h(D_{1-2}, D'_{3-4})$ , and  $D'_{1-8} = h(D'_{1-4}, D_{5-8})$ , where  $D_4, D_{1-2}$  and  $D_{5-8}$  are carried in the packet signature. The verifier then calls the verification operation to determine whether  $D'_{1-8}$  is equal to block digest  $D_{1-8}$  in block signature  $sign(D_{1-8})$ . The packet is verified if the verification operation returns true, i.e.,  $D'_{1-8} = D_{1-8}$ .

Suppose the third packet is the first in the block to arrive. After verifying it, the verifier knows the following nodes<sup>5</sup> in the authentication tree:  $D_3, D_4, D_{1-2}, D_{3-4}, D_{1-4}, D_{5-8}$  and the block digest  $D_{1-8}$ . These are verified nodes which can be cached. By caching verified nodes, the verifier only needs to compute each node in the authentication tree at most once.

For example, after verifying the third packet, to verify the sixth packet which arrives later, the verifier computes the digest of the packet received  $D'_6$ , its parent  $D'_{5-6} = h(D_5, D'_6)$ , and its grandparent  $D'_{5-8} = h(D'_{5-6}, D_{7-8})$ . If  $D'_{5-8}$  is equal to the cached node  $D_{5-8}$ , the sixth packet is verified.

## 2.3. Comparison of chaining techniques

We performed experiments on a Pentium II 300 MHz machine running Linux, and compared star and tree chaining. We used MD5 as the message digest function [18] for generating 128-bit message digests.

For each chaining technique, an authentication tree is first built for a block of packets,<sup>6</sup> i.e., each node is computed as the message digest of its children. The time to build an authentication tree (excluding time to compute packet digests) is called the *tree build time*. The block signature is then obtained by signing the block digest at the root. After that, the packet signature of each packet is built from the authentication tree and the block signature. The time to build a packet signature is called *packet signature build time*. The *chaining time* for a block at a signer is the sum of tree build time and packet signature build time for all packets in the block (excluding signing time of the block digest). Table 1(a) shows the chaining time for a block of packets at a signer.

Note that the total signing time for all packets in a block is the block's chaining time plus the signing time of the block digest, which is 12.7 ms using 512-bit RSA and 5.6 ms using 512-bit DSA. Consider a block of 16 packets. From Table 1(a), the chaining time is 0.214 ms for a degree two authentication tree. The total signing time is

<sup>5</sup>Some are carried in the packet signature and the others have been computed.

<sup>6</sup>We will use "tree" instead of "tree/star" since star chaining is a special case of tree chaining.

$0.214 + 12.7 = 12.9$  ms using 512-bit RSA. Thus the average signing time for one packet is  $12.9/16 = 0.81$  ms, which is more than 15 times smaller than one 512-bit RSA signing operation.

To verify packets in a block, an authentication tree is built from packet signatures as packets arrive. The *chaining time* for a block at a verifier is the sum of tree build time and time to verify chaining information in the packet signature of every packet in the block (excluding verification time of the block signature). The chaining time for a block at a verifier *with caching* of verified nodes is shown in Table 1(b).

The total verification time for all packets in a block is the block's chaining time plus the verification time of the block signature, which is 0.40 ms using 512-bit RSA and 7.6 ms using 512-bit DSA. Consider a block of 16 packets. From Table 1(b), the chaining time is 0.241 ms for a degree two authentication tree. The total verification time is  $0.241 + 0.40 = 0.64$  ms using 512-bit RSA. Thus the average verification time for one packet is  $0.64/16 = 0.04$  ms, which is 10 times smaller than one 512-bit RSA verification operation.

	block size (number of packets)						
	2	4	8	16	32	64	128
star	0.014	0.022	0.034	0.063	0.137	0.376	1.283
tree deg 2	0.016	0.043	0.100	0.214	0.445	0.912	1.852
tree deg 4	0.016	0.028	0.068	0.133	0.285	0.573	1.174
tree deg 8	0.016	0.028	0.058	0.131	0.262	0.531	1.098

(a) Chaining time (ms) at a signer.

	block size (number of packets)						
	2	4	8	16	32	64	128
star	0.014	0.021	0.030	0.049	0.085	0.158	0.305
tree deg 2	0.016	0.047	0.109	0.241	0.499	1.036	2.153
tree deg 4	0.016	0.026	0.070	0.133	0.291	0.584	1.236
tree deg 8	0.016	0.026	0.044	0.110	0.221	0.440	0.963

(b) Chaining time (ms) at a verifier (with caching).

**Table 1. Chaining time (ms) for a block.**

For each chaining technique, a packet signature has two parts, the block signature and the chaining overhead. In general, if a tree is not balanced and full, the chaining overhead sizes of different packets are different. Table 2 shows the average chaining overhead size per packet. The size of the block signature is not included in Table 2 since it depends on which signature scheme is used (e.g., the block signature is 64 bytes for 512-bit RSA, and 40 bytes for 512-bit DSA).

From Table 1(a), note that for any block size smaller than or equal to 64 packets, star chaining takes less time at a signer than tree chaining (degrees two to eight). However, for a larger block size, star chaining takes more time at a signer than tree chaining, because the chaining time for a star is  $O(m^2)$  and the chaining time for a tree is

	block size (number of packets)						
	2	4	8	16	32	64	128
star	17	49	113	241	497	1009	2033
tree deg 2	18	35	52	69	86	103	120
tree deg 4	18	50	78	99	130	148	180
tree deg 8	18	50	114	172	204	227	290

**Table 2. Average chaining overhead size (bytes) per packet.**

$O(m \log(m))$  where  $m$  denotes block size.

As shown in Table 1(b), star chaining takes less time at a verifier than tree chaining for all block sizes.

From Table 2, note that the chaining overhead of star chaining is much greater than tree chaining for block sizes larger than eight. If a small communication overhead is important, packet signature sizes should be reduced. We recommend the use of degree two tree chaining which requires the smallest chaining overhead. (Any improvement in chaining time is insignificant if the signature scheme being used has a signing/verification time much larger than the chaining time. See Table 3 in Section 2.4.)

## 2.4. Flow signing and verification procedures

A flow is signed by partitioning it into blocks of packets, with each block signed using tree chaining. For a non-real-time generated flow, blocks are of the same size  $m$ , chosen to be a power of the authentication tree degree  $d$ . The flow signing procedure,  $\text{flowsign}(m, d)$ , for a non-real-time generated flow is shown in Figure 3.

For a real-time generated flow, the packet generation rate is time-varying for many applications, such as compressed video and voice-activated audio. For these applications, partitioning the flow into fixed size blocks may lead to an unpredictable (perhaps unbounded) signing delay. Instead, the flow is partitioned by fixed time periods, and packets generated in the same time period are grouped into a block (see Figure 4). The flow signing procedure,  $\text{flowsignRT}(T, d)$ , for a real-time generated flow, where  $T$  is the time period and  $d$  is the authentication tree degree, is shown in Figure 3.

For both real-time and non-real-time generated flows, the flow verification procedure, shown in Figure 5, is the same. For the first received packet in a block, i.e., the block signature carried in the packet signature is new to a verifier, the verifier computes the packet digest, and every ancestor of the packet digest.<sup>7</sup> For the computed block digest (the root of authentication tree), the verifier calls the verification operation to verify that it is equal to the block digest in the block signature. If so verified, then all computed nodes and their children are verified and cached.

For a packet that is not the first received packet in a block, the verifier computes the packet digest. If the packet

<sup>7</sup>A node is computed as the message digest of its children which are either computed or carried in the packet signature.

```

procedure flowsign( $m, d$ )
for each block of  $m$  packets,  $P_1, \dots, P_m$ 
  compute packet digests;
  build a degree  $d$  authentication tree;
  let  $root$  be the block digest;
  compute the block signature  $sign(root)$ ;
  for each packet  $P_i$  in the block /* build its signature */
    let  $p$  be its path to  $root$ ;
    its signature consists of the block signature  $sign(root)$ ,
      siblings of each node in  $p$ , and the packet position
  endfor
endfor

procedure flowsignRT( $T, d$ )
for each period  $T$ 
  let  $P_1, \dots, P_m$  be the packets generated
    with digests computed in period  $T$ ;
  build a degree  $d$  authentication tree;
  let  $root$  be the block digest;
  compute the block signature  $sign(root)$ ;
  for each packet  $P_i$  in the block /* build its signature */
    let  $p$  be its path to the  $root$ ;
    its signature consists of the block signature  $sign(root)$ ,
      siblings of each node in  $p$ , and the packet position
  endfor
endfor

```

Figure 3. Flow signing procedures.

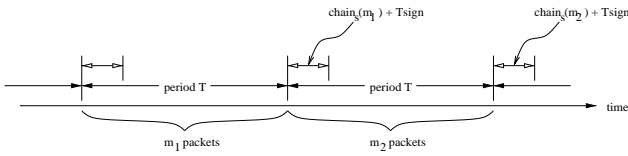


Figure 4. Signing a real-time generated flow.

digest has been cached and the cached value is equal to the computed packet digest, then the packet is verified. Otherwise, the verifier computes every non-cached ancestor of the packet digest. For the highest non-cached ancestor, the verifier computes its parent. If the computed parent and its cached value are equal, then the packet is verified and all computed nodes and their children are verified and cached.

We implemented the flow signing and verification procedures, and performed experiments on a Pentium II 300 MHz machine running Linux. We used MD5 as the message digest function, and experimented with both 512-bit RSA and 512-bit DSA as the signature scheme for block signatures.

Table 3 shows the flow signing and verification rates for 1024-byte packets.<sup>8</sup> Note that tree and star chaining are one to two orders of magnitude more efficient than the sign-each approach. The flow signing and verification rates increase with block size. However, the rates vary only slightly with the chaining technique used and with the tree degree in tree chaining. Since degree two tree chaining has the lowest chaining overhead (packet signature size), we recommend

<sup>8</sup>Verification rates were computed assuming no packet loss. Due to page limitation, we only show results for RSA. Results for DSA can be found in [21].

```

procedure flowverify()
for each received packet
  if the block signature  $sign(root)$  in the packet signature is new then
    /* this is the first received packet in the block */
    compute the packet digest;
    compute each ancestor of the packet digest
      as the message digest of its children;
    let  $root'$  be the computed block digest;
    if (verify( $root'$ ,  $sign(root)$ ) = false) then
      the packet is not verified
    else
      the packet is verified;
      cache all computed nodes and their children as verified
    endif
  else /* this is not the first received packet in the block */
    compute the packet digest;
    if (packet digest has been cached) then
      if (computed packet digest  $\neq$  its cached value) then
        the packet is not verified
      else
        the packet is verified
      endif
    else
      compute all non-cached ancestors of the packet digest;
      let  $node$  be the highest node computed;
      compute the parent of  $node$ ;
      if (computed parent  $\neq$  its cached value) then
        the packet is not verified
      else
        the packet is verified;
        cache all computed nodes and their children as verified
      endif
    endif
  endif
endfor

```

Figure 5. Flow verification procedure (with caching of verified nodes).

the use of degree two tree chaining.

Table 4 shows the flow signing and verification rates for packets of size 512, 1024, or 2048 bytes. We used degree two tree chaining. From the tables, observe that the flow signing and verification rates decrease as the packet size increases. It is because more time is needed to compute the message digest of a larger packet. The decrease is more pronounced when the block size used is large, since more time is used to compute packet digests for a large block than a small block. Observe also that the flow signing and verification rates increase with block size and the increase is greater for a smaller packet size.

## 2.5. Bounded delay signing

Consider Figure 4. Assume that, in period  $T$ , at most  $m$  packets are generated and their packet digests computed. The delay for signing a block of packets is bounded by  $D_s = T + chain_s(m) + T_{sign}$  where  $chain_s(m)$  is the chaining time for a block of  $m$  packets at a signer, and  $T_{sign}$  is the signing time of the block digest.

Table 5 shows the delay bound for period  $T = 50$  ms. Note that the delay bound is fairly insensitive to the block size since the block's chaining time is much smaller than

	block size (number of packets)							block size (number of packets)						
	2	4	8	16	32	64	128	2	4	8	16	32	64	128
sign-each	78.7							1960						
star	152	302	582	1090	1920	3090	4310	3090	4530	5870	6900	7600	7930	8180
tree deg 2	153	304	570	1080	1890	3010	4310	3020	4320	5540	6360	6910	7210	7350
tree deg 4	153	301	579	1080	1900	3070	4380	3000	4400	5650	6640	7230	7590	7760
tree deg 8	153	302	581	1080	1900	3060	4350	2960	4400	5680	6660	7340	7740	7860

(a) signing rates using 512-bit RSA

(b) verification rates using 512-bit RSA

**Table 3. Flow signing/verification rates (packets/sec) for 1024-byte packets.**

packet size (bytes)	block size (number of packets)							block size (number of packets)						
	2	4	8	16	32	64	128	2	4	8	16	32	64	128
512	157	310	605	1160	2130	3640	5670	3600	5630	7740	9560	10800	11600	12000
1024	153	304	570	1080	1890	3010	4310	3020	4320	5540	6360	6910	7210	7350
2048	153	296	552	982	1600	2330	3010	2320	2980	3520	3860	4040	4140	4160

(a) signing rates using 512-bit RSA

(b) verification rates using 512-bit RSA

**Table 4. Flow signing/verification rates (packets/sec) for degree two tree chaining.**

the block digest's signing time.

For a given application, with a specified delay bound,  $D_s$ , for signing a real-time generated flow at a known packet rate, we can work backwards and derive an appropriate value for the parameter  $T$  needed for procedure  $\text{flowsignRT}(T, d)$ . From Figure 4, observe that  $T$  must be larger than  $T_{\text{sign}} + \text{chain}_s(m)$ , and  $D_s$  must be larger than  $2(T_{\text{sign}} + \text{chain}_s(m))$ .

	number of packets generated in period $T$						
	2	4	8	16	32	64	128
tree deg 2	62.6	62.6	62.8	62.8	63.1	63.5	64.6
tree deg 4	62.6	62.7	62.7	62.7	63.0	63.2	64.0
tree deg 8	62.5	62.6	62.7	62.7	63.0	63.2	63.9

**Table 5. Signing delay bound (ms) for period  $T = 50$  ms using 512-bit RSA.**

## 2.6. Selecting a digital signature scheme

For non-real-time generated flows, signing efficiency is not critical. Thus a signature scheme with an efficient verification operation, such as RSA, can be used in the flow signing and verification procedures. For real-time generated flows, however, it is critical that both signing and verification are highly efficient. Furthermore, in choosing a digital signature scheme, we must also consider machine capabilities (sender and receiver), as well as the fraction of processor time available for signing and verification.

Using 100% processor time of a Pentium II 300 MHz machine, the flow signing and verification rates for 1024-byte packets, degree two tree chaining, and block size sixteen, are shown below.

	signing rate	verification rate
512-bit RSA	1080 packets/sec	6360 packets/sec
512-bit DSA	2100 packets/sec	1530 packets/sec

Note that using DSA, the flow verification rate is smaller than the flow signing rate. This is undesirable because receivers/verifiers are generally less powerful than the signer/sender, e.g., the receivers may be personal digital assistants or low-end notebook computers. Using RSA, the flow signing rate may not be high enough for some applications. Although we can increase the flow signing and verification rates by using a longer period or a larger block size, neither option is desirable. A larger block size increases the chaining overhead (packet signature size). A longer period increases the delay for signing real-time generated flows.

To obtain a signature scheme better than RSA and DSA for signing/verifying flows, we propose several extensions to the Feige-Fiat-Shamir signature scheme. The extended scheme, called eFFS, is presented in the next section. The eFFS scheme has a very efficient signing operation (more efficient than those of RSA and DSA) and a verification operation as efficient as that of RSA. A performance comparison of eFFS with four other signature schemes (including RSA and DSA) is given in Section 4.

## 3. The eFFS Signature Scheme

The eFFS signature scheme is derived from the Feige-Fiat-Shamir signature scheme [3, 4] with several extensions. In Section 3.1, we describe the basic Feige-Fiat-Shamir signature scheme. In Section 3.2, we describe an improvement suggested in [12], called small verification key (small v-key) which reduces verification time by an order of magnitude. In Section 3.3, we propose to use a speedup technique suggested by the Chinese Remainder Theorem (crt), which reduces signing time. In Section 3.4, we propose to use a technique, called *precomputation* (pre-comp), which reduces signing and verification times by using more memory. With precomputation, the signing operation time is reduced by a factor of two to three using

	eFFS parameter $(k, t)$					
	(32, 1)	(32, 2)	(64, 1)	(32, 4)	(64, 2)	(128, 1)
basic FFS	3.75	7.45	6.19	14.83	12.33	11.85
small v-key	3.71	7.38	6.42	14.75	12.79	12.45
crt + small v-key	3.24	6.41	5.44	12.78	10.83	9.91
4-bit precomp + crt + small v-key	2.00	3.95	3.03	7.85	5.98	5.11
8-bit precomp + crt + small v-key	1.48	2.92	2.03	5.79	4.00	3.14

**Table 6. eFFS signing time (ms) with 512-bit modulus.**

	eFFS parameter $(k, t)$					
	(32, 1)	(32, 2)	(64, 1)	(32, 4)	(64, 2)	(128, 1)
basic FFS	3.12	6.28	5.94	13.51	11.29	11.14
small v-key	0.30	0.58	0.39	1.14	0.71	0.60
4-bit precomp + small v-key	0.29	0.57	0.36	1.10	0.66	0.55
8-bit precomp + small v-key	0.28	0.56	0.36	1.09	0.65	0.54

**Table 7. eFFS verification time (ms) with 512-bit modulus.**

only a few hundred bytes of additional memory. Lastly, in Section 3.5, we design an extension to provide *adjustable* and *incremental* signature verification. With this extension, a signature can be verified at different security levels, i.e., a verifier can use less resources to verify a signature at a lower security level. Moreover, the verification is incremental, i.e., the verifier can first verify a signature at a lower security level, and later increase the security level by using more resources.

We implemented the basic Feige-Fiat-Shamir (FFS) scheme and the eFFS scheme (i.e., with the improvements and extensions mentioned above) using the large integer arithmetic routines from CryptoLib [8]. Table 6 and Table 7 show the times for signing and verifying (with 512-bit modulus) 128-bit message digests, using different speedup techniques and different eFFS/FFS parameters  $(k, t)$ .<sup>9</sup> The results were obtained on a Pentium II 300 MHz machine running Linux.

### 3.1. Feige-Fiat-Shamir signature scheme

In the basic FFS signature scheme with parameter  $(k, t)$  [3, 4], each signer chooses two large primes  $p$  and  $q$ , and computes modulus  $n = pq$ . Then, the signer chooses  $k$  integers  $v_1, \dots, v_k$  (or  $k$  integers  $s_1, \dots, s_k$ ), and compute  $s_1, \dots, s_k$  (or  $v_1, \dots, v_k$ ) by  $s_i^2 = v_i^{-1} \bmod n$ . The signing key is  $\{s_1, \dots, s_k, n\}$  and the verification key is  $\{v_1, \dots, v_k, n\}$ .

To sign message  $m$ , the signer does the following steps: (1) choose  $t$  random integers,  $r_1, \dots, r_t$ , between 1 and  $n$ , and compute  $x_i = r_i^2 \bmod n$  for  $i = 1, \dots, t$ ; (2) calculate the message digest  $h(m, x_1, \dots, x_t)$  where the message digest function  $h(\cdot)$  is public knowledge and the message di-

gest is at least  $k \times t$  bits long; let  $\{b_{ij}\}$  be the first  $k \times t$  bits of the message digest where  $i = 1, \dots, t$ , and  $j = 1, \dots, k$ ; (3) compute  $y_i = r_i \times (s_1^{b_{i1}} \times \dots \times s_k^{b_{ik}}) \bmod n$  for  $i = 1, \dots, t$ . The signature of message  $m$  consists of  $\{y_i\}$  for  $i = 1, \dots, t$  and  $\{b_{ij}\}$  for  $i = 1, \dots, t$  and  $j = 1, \dots, k$ .

To verify the signature of message  $m$ , a verifier computes  $z_i = y_i^2 \times (v_1^{b_{i1}} \times \dots \times v_k^{b_{ik}}) \bmod n$  for  $i = 1, \dots, t$ . The signature is valid if and only if the first  $k \times t$  bits of  $h(m, z_1, \dots, z_t)$  are equal to the  $\{b_{ij}\}$  received.

Assuming  $|v_i| = |n|$  and  $|s_i| = |n|$ , where  $|x|$  denotes the size of  $x$  in bits, both the signing key and verification key sizes are  $(k + 1) \times |n|$  bits, and the signature size is  $t \times |n| + k \times t$  bits. The signing/verification key size only depends on  $k$ , but the signature size is proportional to  $t$ . For example, with 512-bit modulus and  $(k, t) = (128, 1)$ , the signing/verification key size is 8256 bytes, and the signature size is 80 bytes.

The security level of FFS( $k, t$ ) depends on the following: (1) the size of modulus  $n$ , (i.e., the size of the primes  $p$  and  $q$ ), and (2) the value of product  $kt$ . A system with a longer modulus is more secure, and a system with a larger  $kt$  product is more secure. If two systems with the same modulus and same  $kt$  product (but different  $k$  and  $t$  values), then their security levels are about the same. For a fixed  $kt$  product, we can reduce the signature size by using a smaller  $t$  (and a larger  $k$ ). For  $t = 1$ , the signature size is minimized, but the signing/verification key size is maximized. Moreover, for a fixed  $kt$  product, the signing/verification time is smaller when  $t$  is smaller (see Table 6 and Table 7). Therefore, we recommend to use  $t = 1$  except when adjustable verification is needed.<sup>10</sup>

<sup>9</sup>Note that the product  $kt$  determines the security level of eFFS/FFS for the same modulus. We discuss more about parameters  $(k, t)$  later in Section 3.1.

<sup>10</sup>Our extension to provide adjustable and incremental signature verification, which is described in Section 3.5, requires  $t > 1$ .



### 3.2. Small verification key components

In FFS, the sizes of signing key components  $\{s_i\}$  affect the signing time, and the sizes of verification key components  $\{v_i\}$  affect the verification time. An improvement idea suggested in [12] is to use small prime numbers<sup>11</sup> as the verification key components  $\{v_i\}$  and compute the signing key components  $\{s_i\}$  by  $s_i^2 = v_i^{-1} \bmod n$ . This improvement (labeled as “small v-key” in Table 6 and Table 7) has two advantages. First, the verification time is an order of magnitude smaller than without this improvement (and the signing time is not affected). Second, the verification key size becomes smaller. In practice, for  $k$  up to 128, the verification key components  $\{v_i\}$  are always less than  $2^{16}$ . Thus, for a 512-bit modulus and  $k = 128$ , the signing key size is 8256 bytes, and the verification key size is 320 bytes. Since a signing key is private to a signer, the relatively large signing key size does not pose a problem.

### 3.3. Chinese remainder theorem speedup

We propose to use the following improvement (labeled as “crt” in Table 6), which is based on the Chinese Remainder Theorem, to speed up signing operation. In FFS, the signing operation involves the computing of  $y_i = r_i \times (s_1^{b_{i1}} \times \dots \times s_k^{b_{ik}}) \bmod n$  where  $\{s_i\}$  do not change and only  $\{r_i\}$  and  $\{b_{ij}\}$  change from message to message. Let  $f(r_i, \{b_{ij}\}, s_1, \dots, s_k)$  denote the arithmetic function  $r_i \times (s_1^{b_{i1}} \times \dots \times s_k^{b_{ik}})$ . Basically, the function  $f(\cdot)$  computes the product of some large integers, and  $y_i$  is the integer  $f(\cdot) \bmod n$ . Since only  $y_i$  is needed (and the actual value of  $f(\cdot)$  is not needed), the multiplication operations in  $f(\cdot)$  can be done in  $\bmod n$  for efficiency.

Moreover, as  $n = pq$ , by using Chinese Remainder Theorem,  $y_i (= f(\cdot) \bmod n)$  can be computed from two smaller integers  $a_i = f(\cdot) \bmod p$ , and  $b_i = f(\cdot) \bmod q$ . In particular, the Chinese Remainder Theorem says that  $y_i = (a_i \times q \times p_q^{-1} + b_i \times p \times p_p^{-1}) \bmod n$  where  $p_q^{-1} = p^{-1} \bmod q$  and  $p_p^{-1} = p^{-1} \bmod p$ . Therefore, instead of computing  $y_i$  directly by one  $f(\cdot)$  function call with multiplication operations in  $\bmod n$ , a signer first computes  $a_i$  and  $b_i$  by two  $f(\cdot)$  function calls, one with multiplication operations in  $\bmod p$ , and the other in  $\bmod q$ . Then, the signer computes  $y_i$  from  $a_i$  and  $b_i$  by Chinese Remainder Theorem. Since there are many multiplication operations in  $f(\cdot)$  and multiplication operations in  $\bmod p$  and  $\bmod q$  are more efficient than in  $\bmod n$ , the signing time is decreased.

This Chinese Remainder Theorem improvement can only be used by a signer because knowledge of the factors of modulus  $n$  is required. It reduces the signing time by

<sup>11</sup> Actually, [12] suggests using the first  $k$  prime numbers as the verification key components  $\{v_i\}$ . However, since not every prime number  $p$  satisfies the condition that there exists an integer  $s$  such that  $s^2 = p^{-1} \bmod n$ , we use the first  $k$  prime numbers that satisfy the condition as the verification key components.

12% to 20% (see Table 6). The amount of additional memory needed is only a few hundred bytes for storing a few large integers (with 512-bit modulus).

### 3.4. Precomputation: memory-time tradeoff

One important feature of FFS is that a signer/verifier can trade memory for signing/verification time. We propose to use the following improvement (labeled “precomp” in Table 6 and Table 7) to speed up signing/verification operation by using more memory at signer/verifier.

To illustrate the basic idea of this improvement, consider the signing operation with  $k = 4$ . To sign a message, a signer computes  $y_i = r_i \times (s_1^{b_{i1}} \times \dots \times s_4^{b_{i4}}) \bmod n$ , for  $i = 1, \dots, t$ . Since  $s_1, \dots, s_4$  do not change from message to message, and  $b_{i1}, \dots, b_{i4}$  are either one or zero, the signer can precompute and store the product  $(\bmod n)$  of every non-empty subset of  $\{s_1, \dots, s_4\}$ . Let  $S_{b_{i1} \dots b_{i4}}$  denote the precomputed product  $s_1^{b_{i1}} \times \dots \times s_4^{b_{i4}} \bmod n$ . Then, to sign a message, the signer can compute  $y_i$  by  $r_i \times S_{b_{i1} \dots b_{i4}} \bmod n$ .

For large  $k$ , it is not practical to precompute the product  $(\bmod n)$  of every non-empty subset of  $\{s_1, \dots, s_k\}$ . Instead, the signer partitions  $\{s_1, \dots, s_k\}$  into smaller sets and precomputes each of them. If each smaller set contains four  $s_i$ , then it is a 4-bit precomputation. Similarly, if each smaller set contains eight  $s_i$ , then it is an 8-bit precomputation.

Compared to the basic FFS (with small v-key), 4-bit precomputation plus crt speedup reduces the signing time by 45% to 55%, and 8-bit precomputation plus crt speedup reduces the signing time by 60% to 70% (see Table 6). For 4-bit precomputation with  $k = 128$  and 512-bit modulus, a signer needs to store  $128/4 \times (2^4 - 1) = 480$  products. That is, additional memory of  $480 \times 512$  bits or 31 kilobytes is required. The additional memory required by 8-bit, 12-bit, and 16-bit precomputation are 261 kilobytes, 2.88 megabytes, and 33.6 megabytes, respectively. Given that a low-end desktop PC or a notebook computer has at least 16 or 32 megabytes of memory, the additional memory required by 8-bit precomputation does not pose a problem. In the remaining experiments, we use signing with small v-key, 8-bit precomputation and crt speedup.

Although similar precomputation can be used in verification operations, it is not effective with the small v-key extension. This is because with the small v-key extension, small primes are used as public key components, and their products can be computed very efficiently. For example, with the small v-key extension, 8-bit precomputation in verification operations reduces the verification time by less than 10% (see Table 7). In the remaining experiments, we use verification with small v-key and no precomputation.

### 3.5. Adjustable and incremental verification

In multicast or group communications, receivers typically have different amounts of resources, and the resources

available to a receiver for verification vary over time. It is thus desirable to have an adjustable and incremental signature verification operation. An adjustable verification allows a receiver/verifier to verify a message at a lower security level using less processor time. An incremental verification allows a receiver/verifier to verify a message at a lower security level first, and later increase the security level by using more processor time (e.g., if the message is important).

Since the security level of a signature scheme depends on its parameters, e.g., the modulus size, an obvious approach to provide adjustable and incremental verification is to use multiple keys (with different modulus sizes) to generate multiple signatures for different security levels. To verify at a lower security level, the verification key with a shorter modulus size is used to verify the corresponding signature. This approach is simple but very inefficient. In the following, we design an extension to FFS that provides adjustable and incremental verification efficiently.

The security level of  $\text{FFS}(k, t)$  depends on the product  $kt$  as well as the modulus size. Generally speaking, if two systems have the same modulus and same  $kt$  product, then their security levels are about the same. Our extension to provide adjustable and incremental verification is to use  $t$  greater than one, and to include  $\{x_i\}$  for  $i = 2, \dots, t$  in signatures. This is called a *t-level signature*.<sup>12</sup> This extension is as secure as the original scheme because  $x_i = y_i^2 \times (v_1^{b_{i1}} \times \dots \times v_k^{b_{ik}}) \bmod n$  for  $i = 2, \dots, t$  can be computed easily from the original signature, which consists of  $\{b_{ij}\}$  and  $\{y_i\}$ , together with the verification key  $\{v_1, \dots, v_k, n\}$  which is publicly known.

To verify a  $t$ -level signature of message  $m$  at security level  $l$  of  $t$  (where  $l \leq t$ ), a verifier does the following: (1) compute  $z_i = y_i^2 \times (v_1^{b_{i1}} \times \dots \times v_k^{b_{ik}}) \bmod n$  for  $i = 1, \dots, l$ , and (2) verify that  $z_2, \dots, z_l$  are equal to  $x_2, \dots, x_l$  respectively, and the first  $k \times t$  bits of  $h(m, z_1, x_2, \dots, x_t)$  are equal to the  $\{b_{ij}\}$  received.

To increase the verification security level from  $l_1$  to  $l_2$ , a verifier does the following: (1) compute  $z_i = y_i^2 \times (v_1^{b_{i1}} \times \dots \times v_k^{b_{ik}}) \bmod n$  for  $i = l_1 + 1, \dots, l_2$ , and (2) verify that  $z_{l_1+1}, \dots, z_{l_2}$  are equal to  $x_{l_1+1}, \dots, x_{l_2}$  respectively.

The size of a  $t$ -level signature is  $kt + (2t - 1) \times |n|$  bits. For a 512-bit modulus and product  $kt = 128$ , a 1-level signature is 80 bytes and a 2-level signature is 208 bytes.

Table 8 shows different  $t$ -level signature signing times. For the same  $kt$  product, the signing time increases as the  $t$  value increases. However, the signing time is still smaller than using multiple keys for different security levels. For example, the 2-level signature signing time, which is 4.08 ms for  $kt = 128$ , is smaller than the time to sign two (original 1-level) signatures, one for  $(k, t) = (64, 1)$  and the other

	$kt$ product		
	$kt = 32$	$kt = 64$	$kt = 128$
1-level signature	1.48	2.03	3.14
2-level signature		3.02	4.08
4-level signature			5.89

**Table 8. eFFS  $t$ -level signature signing times (ms).**

security level	$kt$ product		
	$kt = 32$	$kt = 64$	$kt = 128$
level 1 of 1	0.302	0.388	0.598
level 1 of 2		0.321	0.401
level 2 of 2		0.603	0.752
level 1 of 4			0.336
level 2 of 4			0.612
level 4 of 4			1.164

**Table 9. eFFS verification times (ms) at different security levels.**

To	level 1	level 2
From level 0	0.401	0.752
From level 1		0.368

(a) 2-level signature

To	level 1	level 2	level 3	level 4
From level 0	0.336	0.612	0.884	1.164
From level 1		0.288	0.564	0.841
From level 2			0.287	0.567
From level 3				0.291

(b) 4-level signature

**Table 10. eFFS incremental verification times (ms) for  $kt = 128$ .**

for  $(k, t) = (128, 1)$ , which is  $2.06 + 3.19 = 5.25$  ms.

Table 9 shows the (adjustable) verification times at different verification security levels. Table 10 shows the (incremental) verification times from one level to a higher level. For  $kt = 128$  and a 2-level signature, a verifier can first verify a message at level 1 of 2 using 0.401 ms processor time, and later increase to level 2 (of 2) by using 0.368 ms additional processor time.

#### 4. Comparison with other Signature Schemes

In this section, we compare eFFS(128,1) to four other signature schemes available from CryptoLib [8], namely: DSA [15], ElGamal [6], RSA [19], and Rabin [17]. We compare their key and signature sizes, and signing and verification times. Then, we compare their signing and verification rates for 1024-byte packets when each is used as the signature scheme in our flow signing and verification procedures presented in Section 2. Experiments were performed on a Pentium II 300 MHz machine running Linux. Four different modulus sizes, 384, 512, 768, and 1024 bits, were

<sup>12</sup>Note that the original (1-level) signature does not provide adjustable and incremental verification.

used in the comparison. (Note that it is difficult to compare the security levels of different signature schemes even if they use the same modulus size.)

#### 4.1. Key and signature sizes

Table 11 shows the signing/verification key and signature sizes. The signing keys are from 96 to 384 bytes in all schemes except eFFS whose signing keys are much larger, from 6,192 to 16,512 bytes. Note that a signing key is private to a signer. We do not expect the relatively large eFFS signing keys to pose a problem for sources/signers of packet flows.<sup>13</sup>

		modulus size (bits)			
		384	512	768	1024
RSA (e=3)	signing key	96	128	192	256
	verification key	48	64	96	128
	signature	48	64	96	128
Rabin	signing key	96	128	192	256
	verification key	48	64	96	128
	signature	48	64	96	128
DSA	signing key	136	168	232	296
	verification key	164	212	308	404
	signature	40	40	40	40
ElGamal	signing key	144	192	288	384
	verification key	144	192	288	384
	signature	96	128	192	256
eFFS (128,1)	signing key	6192	8256	12384	16512
	verification key	304	320	352	384
	signature	64	80	112	144

**Table 11. Signing key, verification key, and signature sizes (bytes) of different signature schemes.**

In RSA and Rabin, verification keys are from 48 to 128 bytes. In DSA, ElGamal, and eFFS, verification keys are slightly larger, from 144 to 404 bytes. Even for receivers with limited resources, we believe that a verification key as large as 400 bytes would not pose a problem.

The signature of DSA is the smallest and is 40 bytes for all modulus sizes. For all of the other schemes, the signatures are larger and about the same size, 48 to 256 bytes. In particular, the signature sizes of eFFS and the popular RSA are about the same.

#### 4.2. Signing and verification times

Table 12 shows the signing and verification times for a 16-byte message (digest).<sup>14</sup> DSA and ElGamal have been designed to achieve efficient signing (e.g., for use in smart-card applications), and RSA and Rabin have been designed to achieve efficient verification. From Table 12, note that the signing operations of DSA and ElGamal, with times

<sup>13</sup>Such signing keys are indeed too large for small devices, such as smartcards, but it is unlikely that these devices would generate flows.

<sup>14</sup>We use e=3 in RSA to obtain its fastest verification time without affecting its signing time.

		modulus size (bits)			
		384	512	768	1024
RSA (e=3)	sign	6.2	12.7	36.2	79.4
	verify	0.26	0.40	0.70	1.14
Rabin	sign	11.3	19.5	47.5	95.9
	verify	0.14	0.20	0.38	0.56
DSA	sign	3.9	5.6	10.2	16.3
	verify	5.1	7.6	14.7	24.2
ElGamal	sign	5.1	6.8	12.3	18.9
	verify	24.4	51.9	157.5	350.3
eFFS (128,1)	sign	2.25	3.14	5.34	8.13
	verify	0.49	0.60	0.79	1.06

**Table 12. Signing and verifying times (ms) of different signature schemes.**

from 3.9 to 18.9 ms, are much more efficient than those of RSA and Rabin, with times from 6.2 to 95.9 ms. On the other hand, the verification operations of RSA and Rabin, with times from 0.14 to 1.14 ms, are much more efficient than those of DSA and ElGamal, with times from 5.1 to 350.3 ms.

By comparison, eFFS has a signing operation even more efficient than those of DSA and ElGamal, and a verification operation as efficient as that of RSA. This combination of the most efficient signing and highly efficient verification makes eFFS the best choice for most applications.

#### 4.3. Flow signing and verification rates

		modulus size (bits)			
		384	512	768	1024
RSA (e=3)	flow signing	1910	1080	415	193
	flow verification	6730	6360	5590	4930
Rabin	flow signing	1190	743	323	165
	flow verification	7440	7130	6680	6170
DSA	flow signing	2740	2100	1310	871
	flow verification	2230	1530	935	606
ElGamal	flow signing	2330	1850	1140	740
	flow verification	602	294	99	45
eFFS (128,1)	flow signing	3750	3060	2180	1570
	flow verification	6140	5930	5540	4980

**Table 13. Flow signing and verification rates (packets/sec) for 1024-byte packets, degree two tree chaining, and block size sixteen.**

Table 13 shows the flow signing and verification rates of our flow signing and verification procedures (for 1024-byte packets, degree two tree chaining, block size sixteen, and 100% of processor time of a Pentium II 300 MHz machine). Both DSA and ElGamal have low flow verification rates, rendering them inappropriate for receivers with limited resources, such as personal digital assistants and low-end notebook computers. Both RSA and Rabin have low flow signing rates, rendering them inappropriate for real-time generated flows, such as live video/audio applications.

By comparison, eFFS provides high flow signing rates suitable for real-time generated flows while its flow verification rates are also very high.

## 5. Conclusions

We investigated the problem of signing/verifying delay-sensitive packet flows to provide data authenticity, integrity, and non-repudiation for Internet applications. We have designed flow signing and verification procedures, based upon a tree chaining technique, to meet the following requirements: (i) flow signing is efficient and delay-bounded (for real-time generated flows), (ii) flow verification is highly efficient (for receivers with limited resources), (iii) packets in a flow are individually verifiable (for best-effort multicast delivery), (iv) packet signatures are small (for a small communication overhead), and (v) verification at a receiver is adjustable to different security levels and can be carried out incrementally (for receivers with limited resources).

We implemented our flow signing and verification procedures and performed experiments to compare different chaining techniques. From experimental results, we recommend the use of degree two (binary) tree chaining since it requires the smallest packet signature size (i.e., smallest communication overhead) while its signing and verification rates are comparable to the rates of other chaining techniques. Our flow signing and verification procedures are very efficient and achieve one to two orders of magnitude improvement compared to the sign-each approach.

To further improve our procedures, we propose several extensions to the Feige-Fiat-Shamir digital signature scheme [3, 4] to speed up both the signing and verification operations, as well as to allow adjustable and incremental verification. The extended scheme, called eFFS, is compared to four other digital signature schemes, RSA [19], Rabin [17], DSA [15], and ElGamal [6], on the same computing platform (Pentium II 300 MHz machine running Linux).

The signing operation of eFFS is more efficient than those of the other four schemes. The verification operation of eFFS is as efficient as that of RSA (tie for a close second behind the verification operation of Rabin). In addition to efficient signing and verification, we have extended the eFFS scheme to allow a receiver to efficiently carry out adjustable and incremental verification. Such a capability is useful for large-scale multicast applications with a variety of receivers including some with limited resources.

Additional experimental results can be found in our technical report [21] available at the following URLs.

[http://www.cs.utexas.edu/users/lam/NRL/network\\_security.html](http://www.cs.utexas.edu/users/lam/NRL/network_security.html)

<http://www.cs.utexas.edu/users/ckwong>

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