

# Wait-Free Synchronization

## Lecture 1

*CS380D—Distributed Computing*  
*The University of Texas at Austin*

# Coöperation

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- *Many large problems require multiple processes to cooperate on a solution*
- *Cooperation requires shared data*

How can we provide efficient concurrent access to shared data?

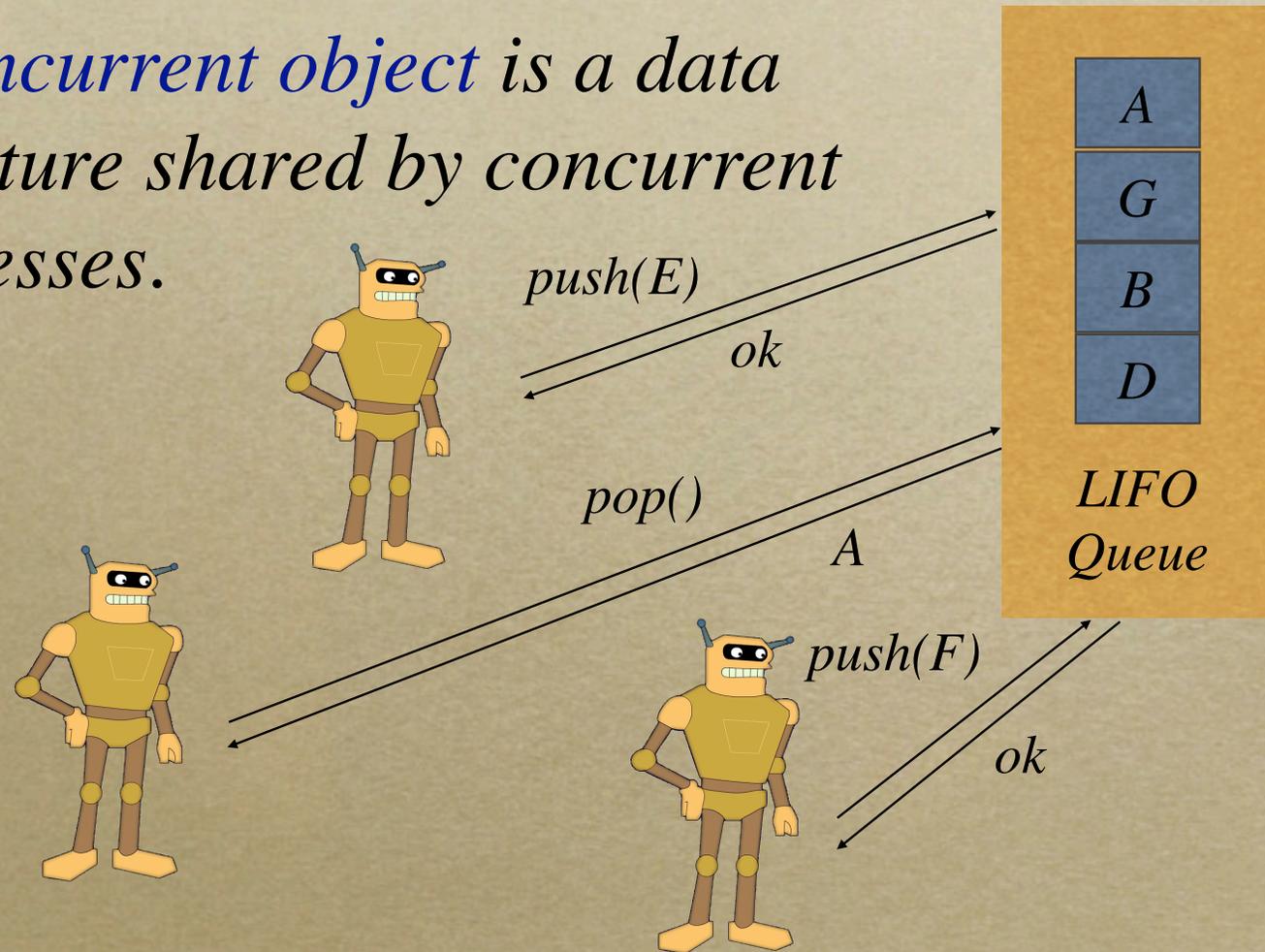
# Concurrency Model (Informal)

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- *Asynchronous*—concurrent processes execute without relative bounds on the speed between processes, and a process's speed may vary over time.
- *Failstop*—processes may fail by halting at any time.

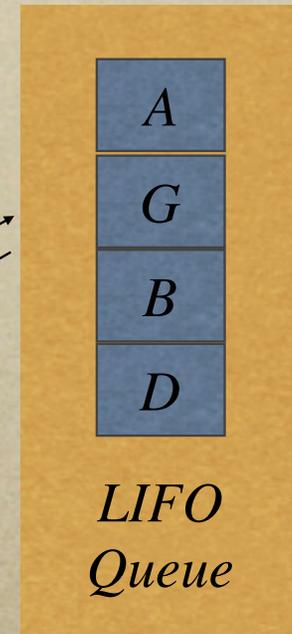
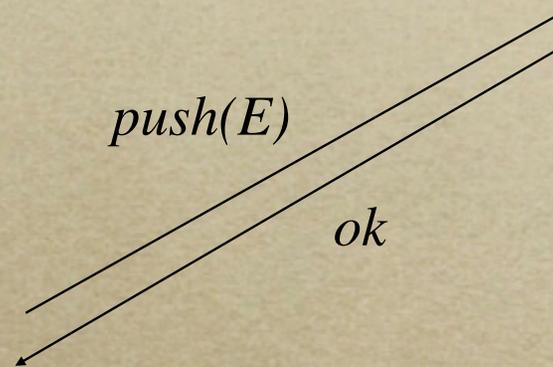
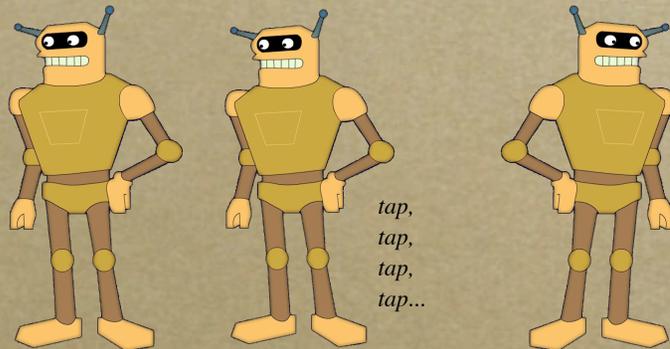
# Concurrent Data Structures

- A *concurrent object* is a data structure shared by concurrent processes.



# Mutual Exclusion

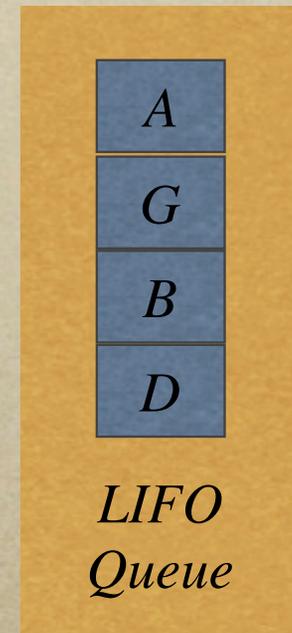
- *Only allow one operation to act on the object at a time*
- *Other operations must wait...*





# Mutual Exclusion's Problems

- *Deadlock (no progress)*
- *Priority Inversion (wrong progress)*
- *Convoying (delayed progress)*
- *Inefficiency (wasted concurrency)*
- *Undo Log (required for recovery)*



# Wait-Free Concurrent Objects

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*A wait-free data structure guarantees that any process can complete any operation in a finite number of steps. (Lamport)*

# Lesser Freedoms

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*A **lock-free data structure** guarantees that some process will complete an operation in a finite number of steps.*

*An **obstruction-free data structure** guarantees that a process will complete an operation provided there is no contention (against the operation) for a sufficient number of steps.*

# Yes, but?

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- *Can we make any object wait-free?*
  - *What primitives are necessary / sufficient for constructing wait-free objects?*
- *How do we build a wait-free object?*
  - *Is there a universal constructor?*
- *How do we know the implementation is correct?*

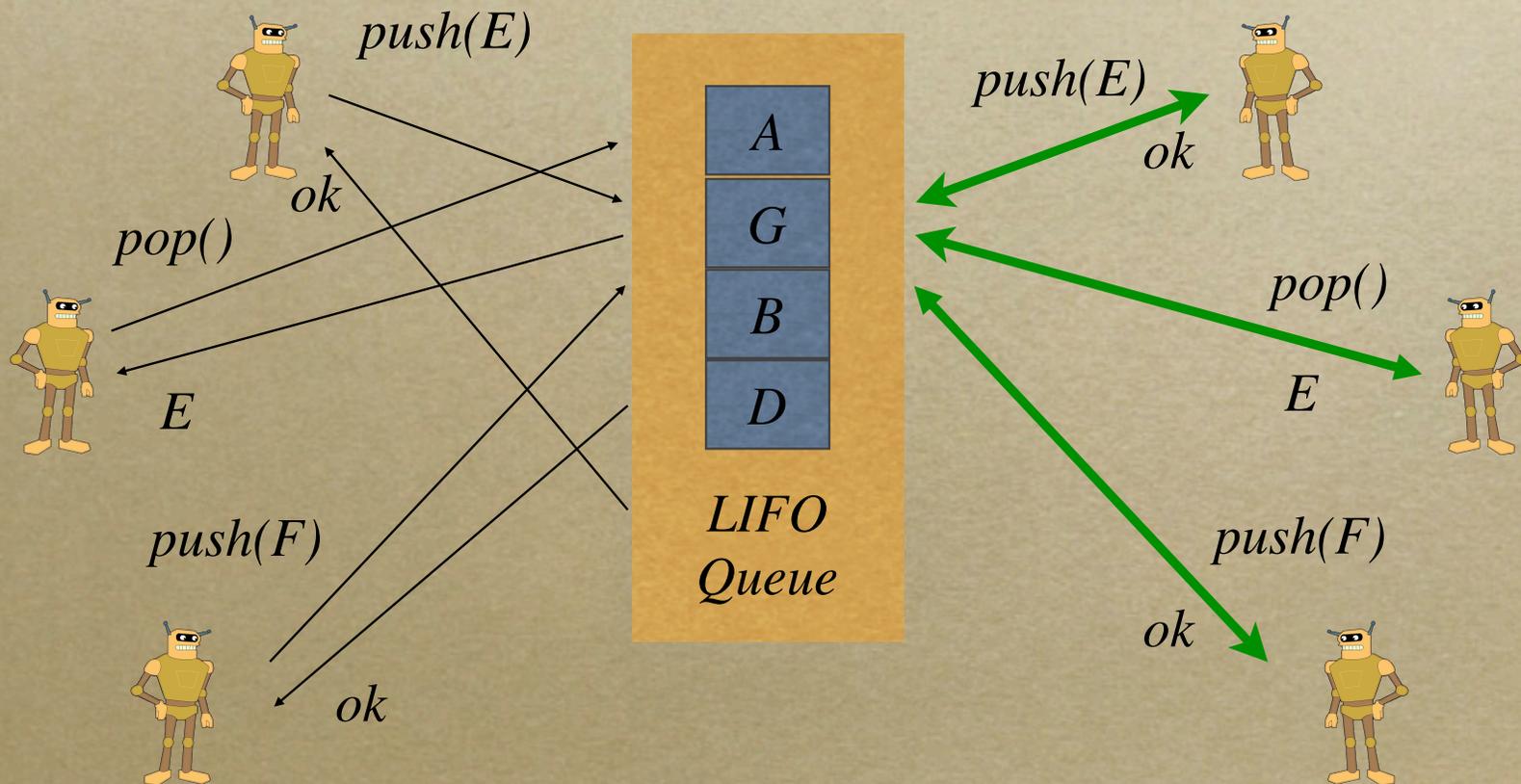
# You can breathe. Thank Herlihy.

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- *A wait-free implementation of an object can be built out of any object with the same consensus number.*
- *There is a universal constructor using an object of infinite consensus number.*
- *We can verify correctness by showing that the implementation is linearizable.*

# Linearizability In a Nutshell

- *Each operation of the system appears to take effect instantaneously between the invocation and response.*



# Linearizability Is...

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- *A local property—a concurrent system is linearizable if and only if each individual object is linearizable*
- *A non-blocking property—a total operation (that is, defined for all object states) is never required to block*

*How does this compare to sequential consistency or serializability?*

# Concurrency Model (Formal)

- *A concurrent system  $\{ P_1 \dots P_n ; O_1 \dots O_m \}$  is a set of processes,  $P_i$ , and objects,  $O_i$*
- *Processes and Objects are I/O automata with the following events:*
  - *INVOKE( $P, op, O$ )— $op$  is an operation of  $O$*
  - *RESPOND( $P, res, O$ )— $res$  is a result value*
- *An object's operations must be total*
  - *If the object has a pending operation there is a matching enabled response*

# An I/O Automaton

- *An I/O automaton  $A$  consists of:*
  1.  *$States(A)$  – a finite or infinite set of states*
  2.  *$In(A)$  – a set of input events (always enabled)*
  3.  *$Out(A)$  – a set of output events*
  4.  *$Int(A)$  – a set of internal events*
  5.  *$Step(A)$  – a transition relation of triples  $(s', e, s)$*
- *An event  $e$  is enabled in state  $s'$  if  $(s', e, s)$  in  $Step(A)$  for some  $s$ .*
- *A history is a sequence of enabled events starting at an initial state.*
- *I/O automata can be composed if they are compatible (that is, they share no output or internal events)*

# Implementations

- *An implementation of an object  $A$  is a concurrent system  $\{F_1 \dots F_r ; R\}$* 
  - *the  $F_i$  are called front-ends*
  - *object  $R$  is called the representation object*
- *The external events of the implementation are just the external events of  $A$ .*
- *The  $F_i$  share no events; they only communicate through  $R$*

# A Consensus Protocol is...

*A concurrent system  $\{ P_1 \dots P_n ; X_1 \dots X_m \}$  of  $n$  processes, where*

- each  $P_i$  starts with an input value from some domain  $D$*
- the  $P_i$  communicate by applying operations to the objects  $X_i$*
- the processes eventually agree on a common input value and halt*

*Required to be*

- consistent—distinct processes never decide on distinct values*
- valid—the common decision value is the input to some process*
- wait-free—each process decides after a finite number of steps*

# The Consensus Number

- *The consensus number of a concurrent object  $X$  is the largest  $n$  for which there exists a consensus protocol  $\{ P_1 \dots P_n ; W, X \}$*
- *$W$  is a set of read/write registers*
- *$W$  and  $X$  can be initialized to any state*
- *If no largest  $n$  exists, the consensus number is said to be infinite*

# Consensus Number Antics

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- *Theorem: If  $X$  has consensus number  $n$ , and  $Y$  has consensus number  $m < n$ , then there exists no wait-free implementation of  $X$  by  $Y$  in a system of more than  $m$  processes.*
- *The theorem implies that there is a hierarchy where each level  $n$  of the hierarchy contains concurrent objects with consensus number  $n$*

# Theorem Proof

*By contradiction. Assume  $X$  has consensus number  $n$ , and  $Y$  has consensus number  $m < n$ . Let  $k > m$ , assume for contradiction that  $X = \{ G_1 \dots G_k ; Y \}$  has consensus number  $k$ .*

- $\{ P_1 \dots P_k ; W, X \}$  is a consensus protocol*
- $\{ P_1 \dots P_n ; W, \{ G_1 \dots G_n ; Y \} \}$  is wait-free*
- $\{ P_1 \cdot G_1 \dots P_n \cdot G_n ; W, Y \}$  is a consensus protocol because composition is associative*

# Herlihy's Wait-Free Hierarchy

Consensus Number	Object
1	atomic read/write registers
2	test&set, fetch&add
$2n - 2$	n-register assignment
$\infty$	compare&swap, FIFO queue w/ peek

# Compare-and-Swap

*atomically*

```
val CAS( val* addr, val old, val new)
{
    val prev = *addr;
    if (prev == old) { *addr = new; }
    return prev;
}
```

- *CMPXCHG (with “lock”) – Intel x86*
- *Load Linked / Store Conditional – MIPS, PowerPC*

# Compare&Swap Register

*Theorem: A CAS register has infinite consensus number.*

```
value_t decision =  $\perp$ ;  
value_t decide( value_t input) {  
    first = CAS( &decision,  $\perp$ , input);  
    if ( first ==  $\perp$  ) // CAS succeeded?  
        return input;  
    else  
        return first;  
}
```

# Wait-Free Synchronization

## Lecture 2

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# Summary so far...

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- *Wait-free synchronization provides guaranteed progress to all correct processes*
- *There is a wait-free hierarchy determined by an object's consensus number*
- *Compare&Swap is a universal primitive and thus can be used to implement any wait-free object*

# Hierarchy Redux

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- *The wait-free hierarchy states that an object with consensus number  $n$  (and some registers) cannot be used to implement an object of consensus number  $m > n$*
- *How useful is this wait-free hierarchy?*
  - *Can we use multiple objects of consensus number  $n$  to implement a higher object?*

# A Robust Hierarchy

- A *robust hierarchy* requires that an object at level  $n$  be impossible to implement using any set composed of objects at level  $n-1$  or lower
  - Such a hierarchy would imply that there are no clever ways to combine inferior objects to create superior objects
  - *Is Herlihy's wait-free hierarchy robust?*

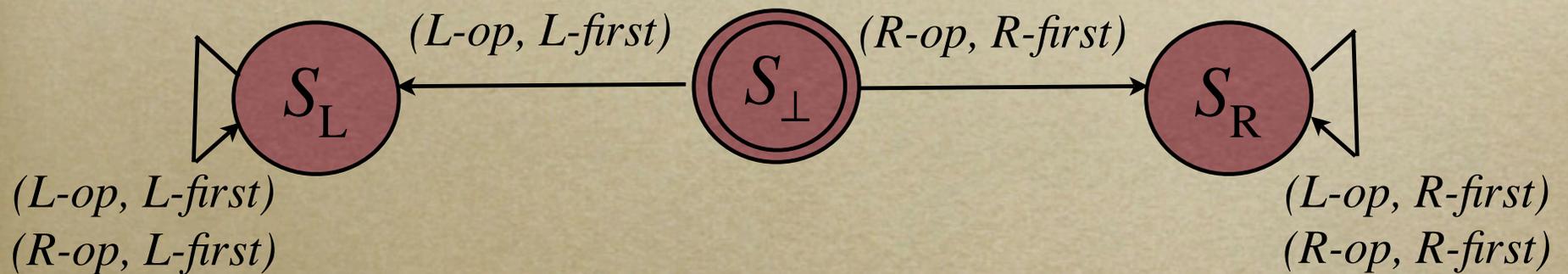
# The wait-free hierarchy is not robust.

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- *The weak-sticky object has the property that  $k$  objects (together with read/write registers) can implement an object with consensus number  $k+1$  (Jayanti)*
- *The weak-sticky object is based upon the sticky bit object that solves 1-bit consensus*

# Plotkin's Sticky Bit

*State diagram:*



- *The sticky bit provides a global order for the first operation only*

# Plotkin's Sticky Bit

◦ *1-bit consensus object using  $O_s$ :*

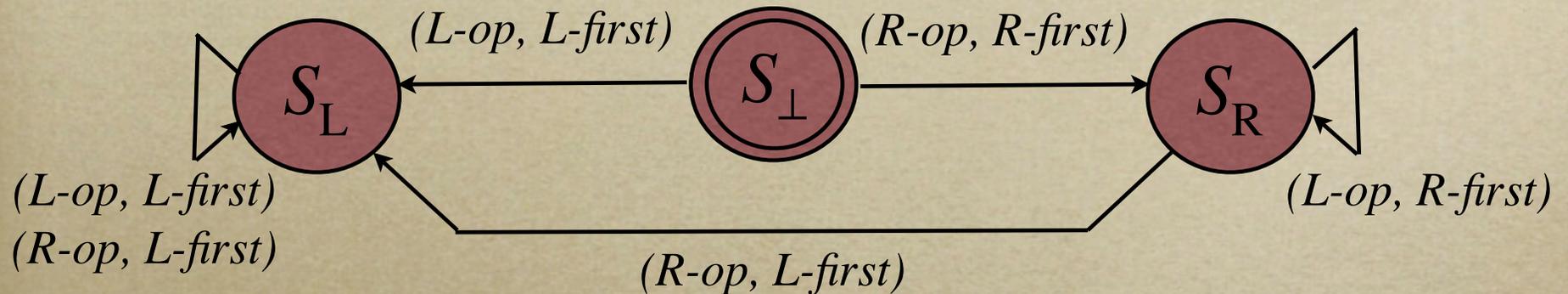
*( $O_s$  is a sticky bit object,*

*$O_n$  is an  $n$ -process consensus object)*

```
Apply( $P_i$ , propose  $b_i$ ,  $O_n$ )  
  return ( L-first = Apply( $P_i$ ,  $b_i = 1 ? L\text{-op} : R\text{-op}$ ,  $O_s$ ) )
```

*Why does the sticky bit object have consensus number  $\infty$ ?*

# Weak-Sticky Objects



- *Asymmetric version of sticky bit object*
  - *Second R-op locks bit to L-first result*
  - *Provides a global order to first operation for only 2 participants*
  - *Asymmetry prevents consensus number  $\infty$*

# Weak-Sticky Objects

◦ *Consensus object with  $\{O_{ws}, L, R\}$ :*

*( $O_{ws}$  is a weak-sticky object,  $L$  &  $R$  are shared registers,*

*$O_2$  is a 2-process consensus object)*

```
Apply( $P_0$ , propose  $v_0$ ,  $O_2$ )  
L :=  $v_0$   
w := Apply( $P_0$ , L-op,  $O_{ws}$ )  
if w = L-first  
    return (L)  
else  
    return (R)
```

```
Apply( $P_1$ , propose  $v_1$ ,  $O_2$ )  
R :=  $v_1$   
w := Apply( $P_1$ , R-op,  $O_{ws}$ )  
if w = L-first  
    return (L)  
else  
    return (R)
```

*Is this valid? agreeable? wait-free?*

# Building Consensus

◦ *Consensus object with  $\{O_{ws}, O_{n-1}, L, R\}$ :*

*( $O_{ws}$ ,  $L$ ,  $R$  as before,  $O_{n-1}$  is an  $(n-1)$ -process consensus object,  $O_n$  is an  $n$ -process consensus object)*

```
Apply( $P_i$ , propose  $v_i$ ,  $O_n$ )  $\{0 < i < n\}$ 
L := Apply( $P_i$ , propose  $v_i$ ,  $O_{n-1}$ )
w := Apply( $P_i$ , L-op,  $O_{ws}$ )
if w = L-first
  return (L)
else
  return (R)
```

```
Apply( $P_n$ , propose  $v_n$ ,  $O_n$ )
R :=  $v_n$ 
w := Apply( $P_n$ , R-op,  $O_{ws}$ )
if w = L-first
  return (L)
else
  return (R)
```

*Can other objects be used similarly to build objects with higher consensus number?*

# Universal Objects

- *An object is universal if it can be used to construct a wait-free implementation of any object (that is, it has consensus number  $\infty$ ).*
- *In a system of  $n$  processes, an object is universal if and only if the object has consensus number  $n$ .*
- *CAS has consensus number  $\infty$  and thus is a universal object.*

# How do we build using CAS?

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- *Use CAS to guarantee consistency during concurrent operations*
  - *CAS can ensure that the update that succeeds is consistent with the previous view of the object*
- *Wait-freedom seems to require helping to guarantee progress to all threads*
  - *Disjoint-set parallel algorithms only help operations of other threads that “conflict”*

# A Simple Stack Object

```
struct elem {
    elem *link;
    any data;
}

elem* qhead;
```

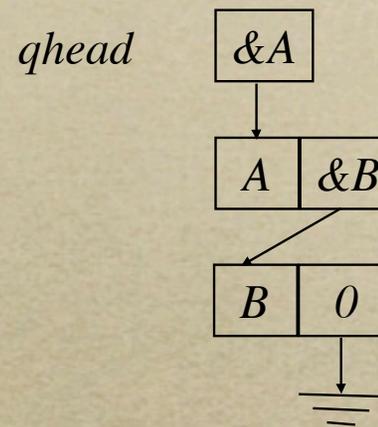
```
Push(elem *x)
do
    old = qhead;
    x->link = old;
    new = x;
    cc = CAS(qhead, old, new);
until (cc == old);
```

*Is this solution:*  
*wait-free?*  
*lock-free?*  
*obstruction-free?*

```
Pop()
do
    old = qhead;
    new = old->link;
    cc = CAS(qhead, old, new);
until (cc == old);
return old;
```

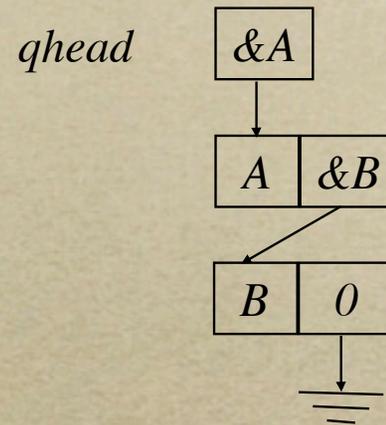
# Is this implementation correct?

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
    cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```



# Is this implementation correct?

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
→ cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```



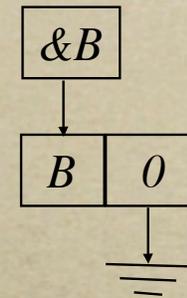
*old*    &A

*new*    &B

# Is this implementation correct?

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
→ cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```

*qhead*



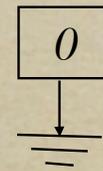
*old*    &A

*new*    &B

# Is this implementation correct?

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
→ cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```

*qhead*



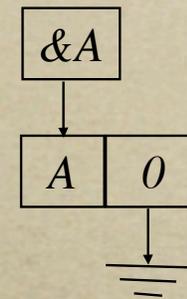
*old*    &A

*new*    &B

# Is this implementation correct?

```
Pop()
do
  old = qhead;
  new = old->link;
  → cc = CAS(qhead, old, new);
  until (cc == old);
  return old;
```

*qhead*



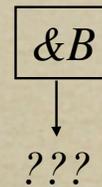
*old*    &A

*new*    &B

# Is this implementation correct?

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
    cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```

*qhead*



- *This is called the “ABA problem”*
- *How do we solve the problem?*

# How can we handle ABA?

*Use CAS2 (often called DCAS)*

*atomically*

```
boolean CAS2( val*  addr1,  val*  addr2,  
              val  old1, val  old2, val  new1, val  new2) {  
    if (*addr1 == old1 && *addr2 == old2) {  
        *addr1 = new1;  *addr2 = new2;  
        return true;  
    } else  
        return false;  
}
```

*How is this useful?*

# Proposed Stack with CAS2

```
Pop()
do
  old = qhead;
  link_field = &(old->link);
  new = *link_field;
  cc = CAS2(qhead, *link_field,
           old, new, new, new);
until (cc);
return old;
```

- *Does it make sense to CAS(link, new, new)?*
- *Is there a more general way to ensure the object hasn't changed?*

# DWCAS

---

- *Double-wide CAS (DWCAS) performs a CAS on memory locations comprised of two adjacent words*
- *Adding a version number to each location ensures the location is the expected version*
  - *Update version number when object is modified*
  - *Included expected version number in DWCAS*

# Stack with DWCAS

```
struct elem {  
    elem *link;  
    any data;  
}
```

```
struct qhead {  
    elem *link;  
    int seq;  
} qhead;
```

```
Push(elem *x)  
do  
    old = qhead.link;  
    oldseq = qhead.seq;  
    x->link = old;  
    cc = DWCAS(qhead,  
                <old, oldseq>,  
                <x, oldseq+1>);  
until (cc);
```

```
Pop()  
do  
    old = qhead.link;  
    oldseq = qhead.seq;  
    new = old->link;  
    cc = DWCAS(qhead,  
                <old, oldseq>,  
                <new, oldseq+1>);  
until (cc);  
return old;
```

# Problems with DWCAS

---

- *Requires more memory per object*
- *Does it really solve the problem?*
  - *Version representation is finite*
- *Assumes type-stable memory*
  - *Restricts reuse to same type*
- *We need lock-free garbage collection*
  - *Allows for simpler implementation of lock-free objects*

# Lock-free Garbage Collection

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- *We have to address the garbage collection problem while maintaining lock-free access to data structures*
- *How do we tell whether an object is really garbage?*
- *How do we track memory using lock-free data structures?*

# Hazardous References

- A hazardous reference *is an address that without further validation can be used to access a node after it has been deleted*
- Hazard pointers are used for each thread to *track hazardous references*

*old is hazardous*

```
Pop()  
do  
    old = qhead;  
    new = old->link;  
    cc = CAS(qhead, old, new);  
until (cc == old);  
return old;
```

# Safe Memory Reclamation

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- *Safe Memory Reclamation (SMR)*

*Whenever a thread holds a hazardous reference, it must guarantee that a hazard pointer contains the reference (Michael)*

# SMR Stack Object

- *HP is shared array of hazard pointers*
- *hp = &HP[p] (where p is current thread)*

Validity check

```
Pop( )
do
    old = qhead;
    *hp = old;
    if (old != qhead) { continue; }
    new = old->link;
    cc = CAS(qhead, old, new);
until ( cc != old );
*hp = NULL;
return old;
```

# When is memory “garbage”?

---

- *A node can queue an object for deletion when the object is semantically dead*
  - *When the object is not reachable using the current state of all other objects*
  - *In lieu of a call to `free( object )`*

# Memory Deallocation

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- *Periodically check the list of queued deletes to see whether any hazardous references exists*
- *If no hazard pointers contain an object in the list, the object's memory may safely be deallocated*

*How can we tell if there are hazard pointers to the object?*

# SMR Algorithm

```
// constants
int R; // batch size
int N; // # hazard ptrs

// shared variables
Node *HP[N] = { NULL, };

// static private vars
int dcount = 0;
Node *dlist[R];
```

```
SMR_free( Node *n )
    dlist[dcount++] = n;
    if( R == dcount )
        Scan();
```

```
Scan( )
    // Stage 1: copy hp
    < copy HP to local plist >
    // Stage 2: sort for search
    < sort plist >
    // Stage 3: free garbage
    for( i=0; i<R; ++i )
        if( find(dlist[i],plist) )
            *(new_dlist++) = dlist[i];
        else
            free( dlist[i] );
    // Stage 4: save remainder
    < copy new_dlist to dlist >
```

# Multiple Hazard Pointers

- *The HP array is scanned non-atomically, requiring hazard pointers to be maintained in the same order that the HP array is scanned*

```
Dequeue( )
while( true )
    h = qhead;
    *hp0 = h;
    if( h != qhead ) { continue; }
    t = qtail;
    next = h->link;
    *hp1 = next;
    if( h != qhead )
        { *hp0 = NULL; return EMPTY; }
    if( h == t )
        { CAS(&qtail, t, next); continue; }
    data = next->data;
    if( h == CAS(&qhead, h, next) )
        break;
    *hp0 = NULL; *hp1 = NULL;
    SMR_free( h );
    return data;
```

# SMR Questions

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- *Does SMR really solve ABA?*
- *Is SMR really wait-free?*

# SMR Answers

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- *Does SMR really solve ABA?*
  - *SMR addresses only reallocation*
- *Is SMR really wait-free?*
  - *The operations complete in finite steps*
  - *Memory is not guaranteed to be deallocated*