

Programming Uncertain **<T>**hings

Kathryn S. McKinley

Microsoft Research

Todd Mytkowicz

Microsoft Research

James Bornholt

University of Washington

Na Meng

Virginia Tech

Adrian Sampson

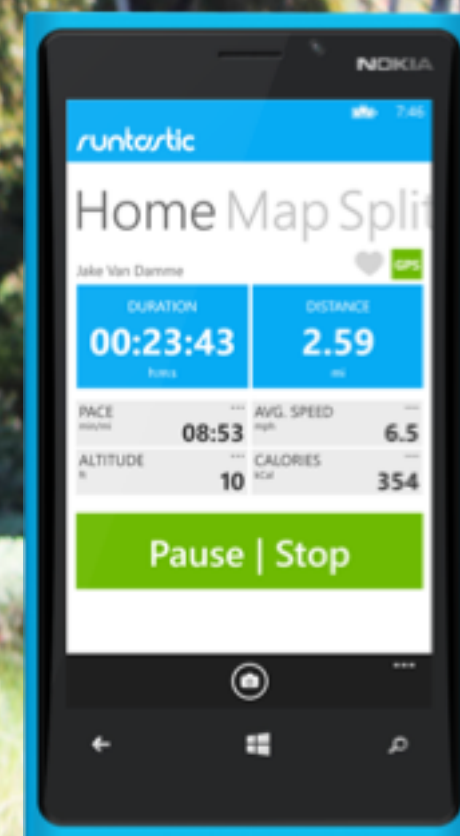
Microsoft Research, Cornell

Diman Zad Tootaghaj

University of Pittsburgh

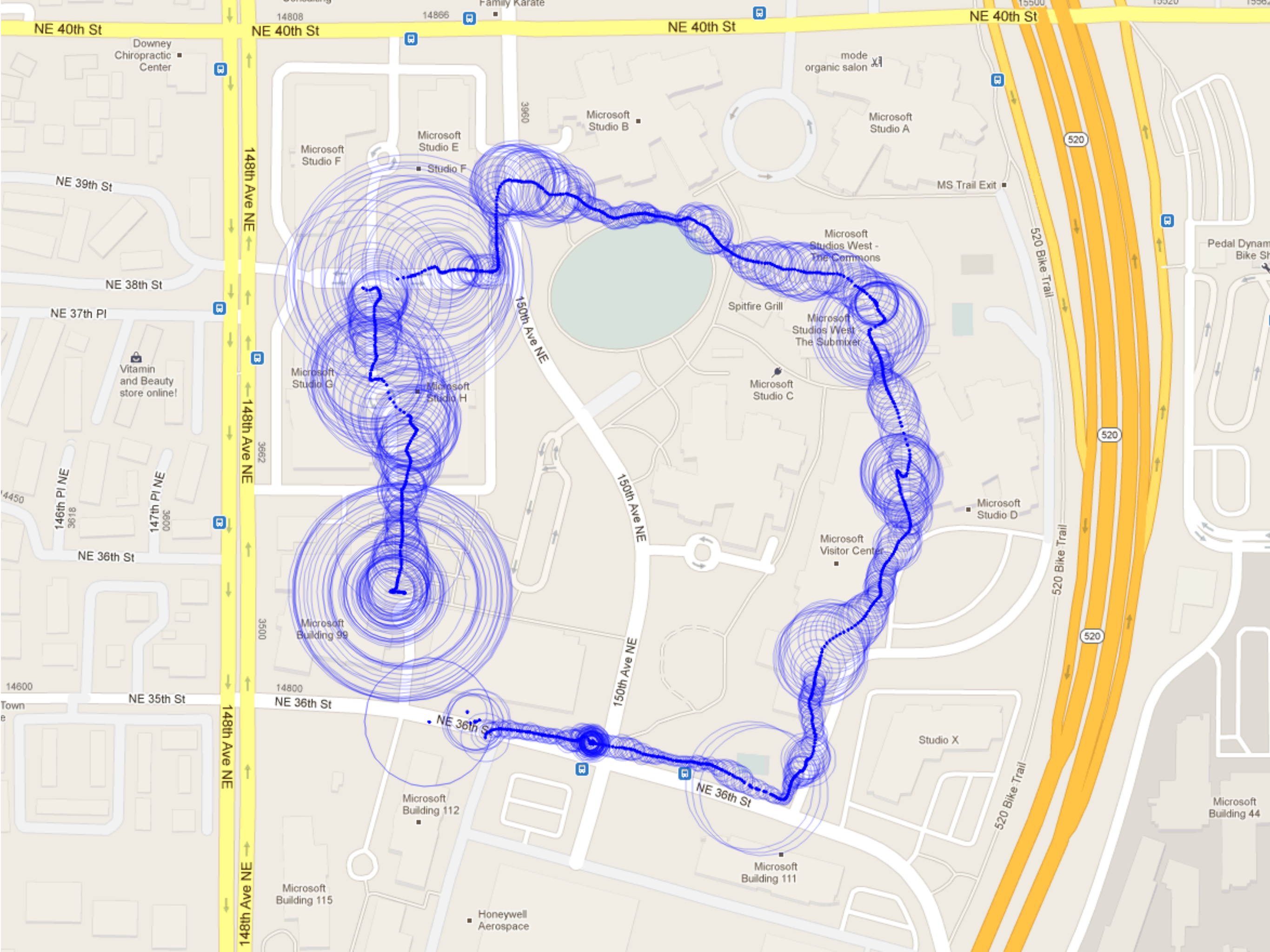


24 mph



59 mph


```
GeoCoordinate Location = GPS.Get();
```


```
GeoCoordinate PrevLocn = Get();  
Sleep(5);  
GeoCoordinate Location = Get();
```



```
GeoCoordinate PrevLocn = Get();  
Sleep(5);  
GeoCoordinate Location = Get();  
double Dist =  
    Distance(PrevLocn, Location);  
double Speed = Dist / 5;
```

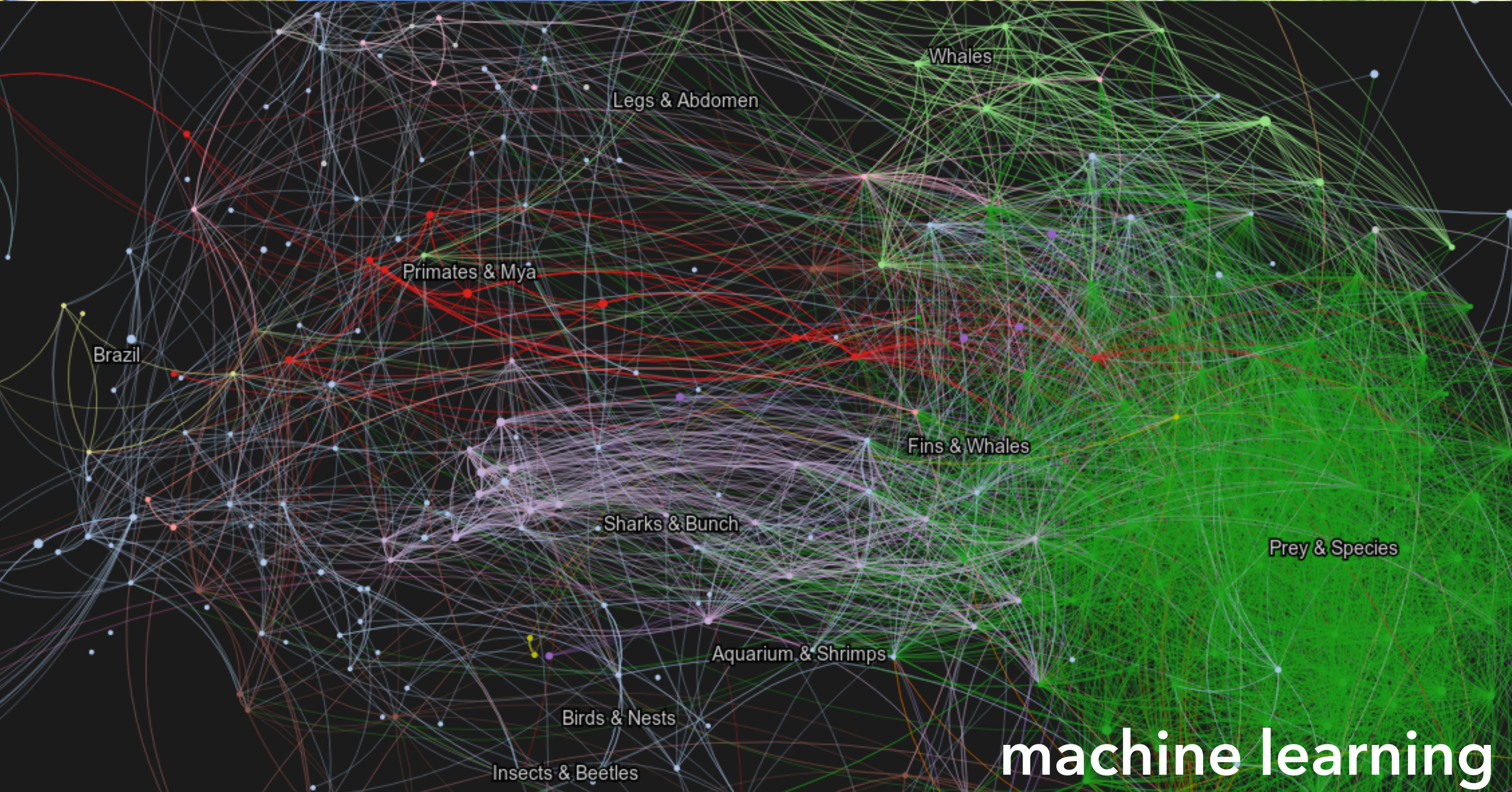
```
GeoCoordinate PrevLocn = Get();  
Sleep(5);  
GeoCoordinate Location = Get();  
double Dist =  
    Distance(PrevLocn, Location);  
double Speed = Dist / 5;  
  
Print(Speed);
```

59 mph





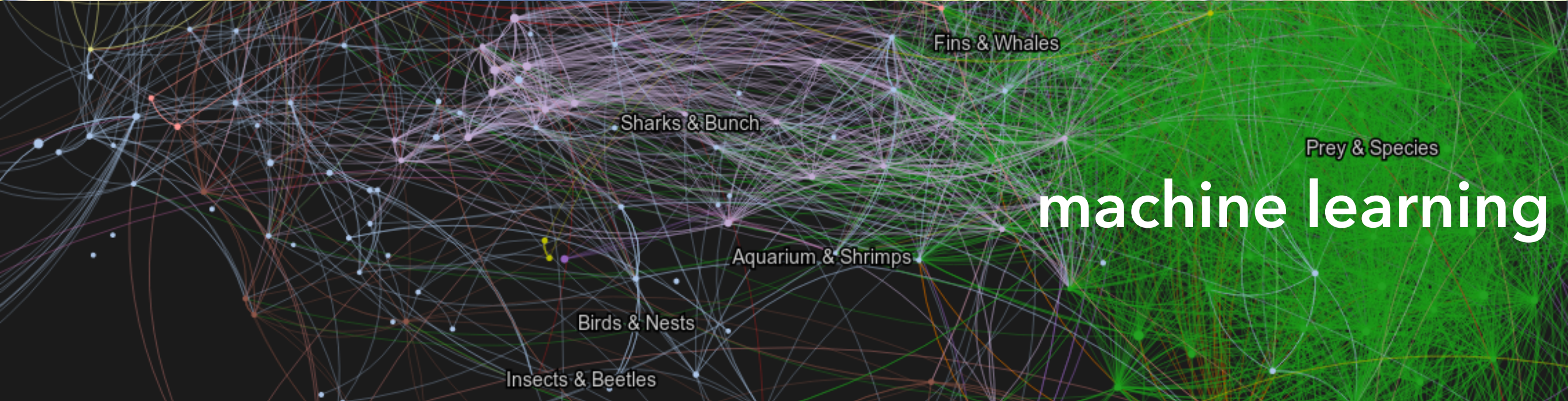
sensors



machine learning



sensors



machine learning



approximate
computing

Uncertain<T>

an abstraction for reasoning about noise

[ASPLOS'14]

exploiting context

improving accuracy with more language & inference

[rejected so far]

what does it mean?

probabilistic assertions

[PLDI'14]

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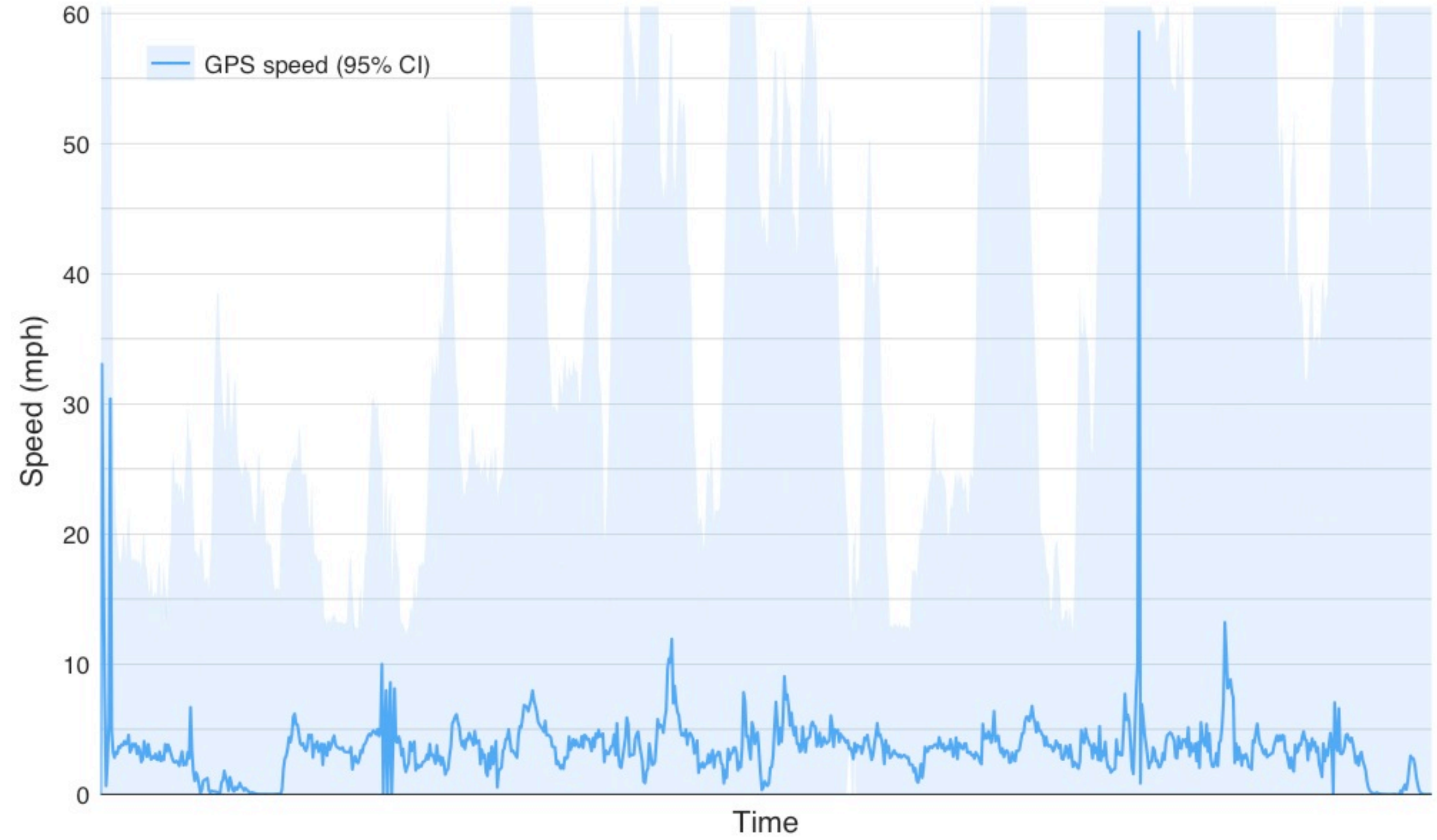
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what does it mean?

probabilistic assertions

[PLDI'14]

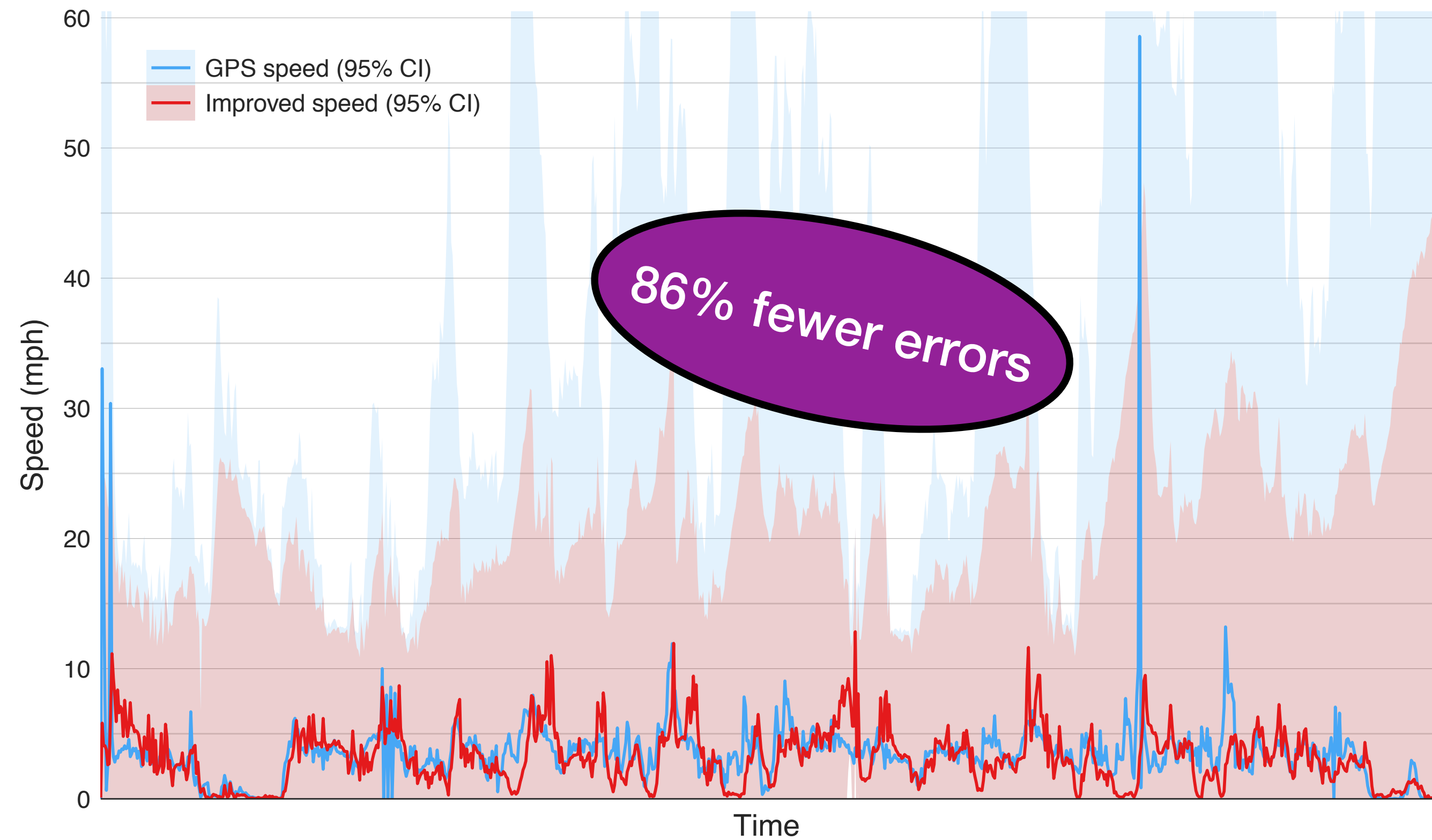
```
GeoCoordinate PrevLocn = Get();  
Sleep(5);  
GeoCoordinate Location = Get();  
double Dist =  
    Distance(PrevLocn, Location);  
double Speed = Dist / 5;  
  
Print(Speed);
```

```
GeoCoordinate PrevLocn = Get();  
Sleep(5);  
GeoCoordinate Location = Get();  
double Dist =  
    Distance(PrevLocn, Location);  
double Speed = Dist / 5;  
  
Print(Speed);
```



```
Uncertain<GeoCoordinate> PrevLocn = Get();  
Sleep(5);  
Uncertain<GeoCoordinate> Location = Get();  
Uncertain<double> Dist =  
    Distance(PrevLocn, Location);  
Uncertain<double> Speed = Dist / 5;  
  
Print (Speed); // Expected value at 95 CI
```



Fitness application

```
Uncertain<GeoCoordinate> PrevLocn = Get();  
Sleep(5);
```

```
Uncertain<GeoCoordinate> Location = Get();
```

```
Uncertain<double> Dist =  
    Distance(PrevLocn, Location);
```

```
Uncertain<double> Speed = Dist / 5;
```

```
if (Speed > 4)  
    Alert("Keep it up!");
```

Hypothesis Test
more likely than
not Speed > 4

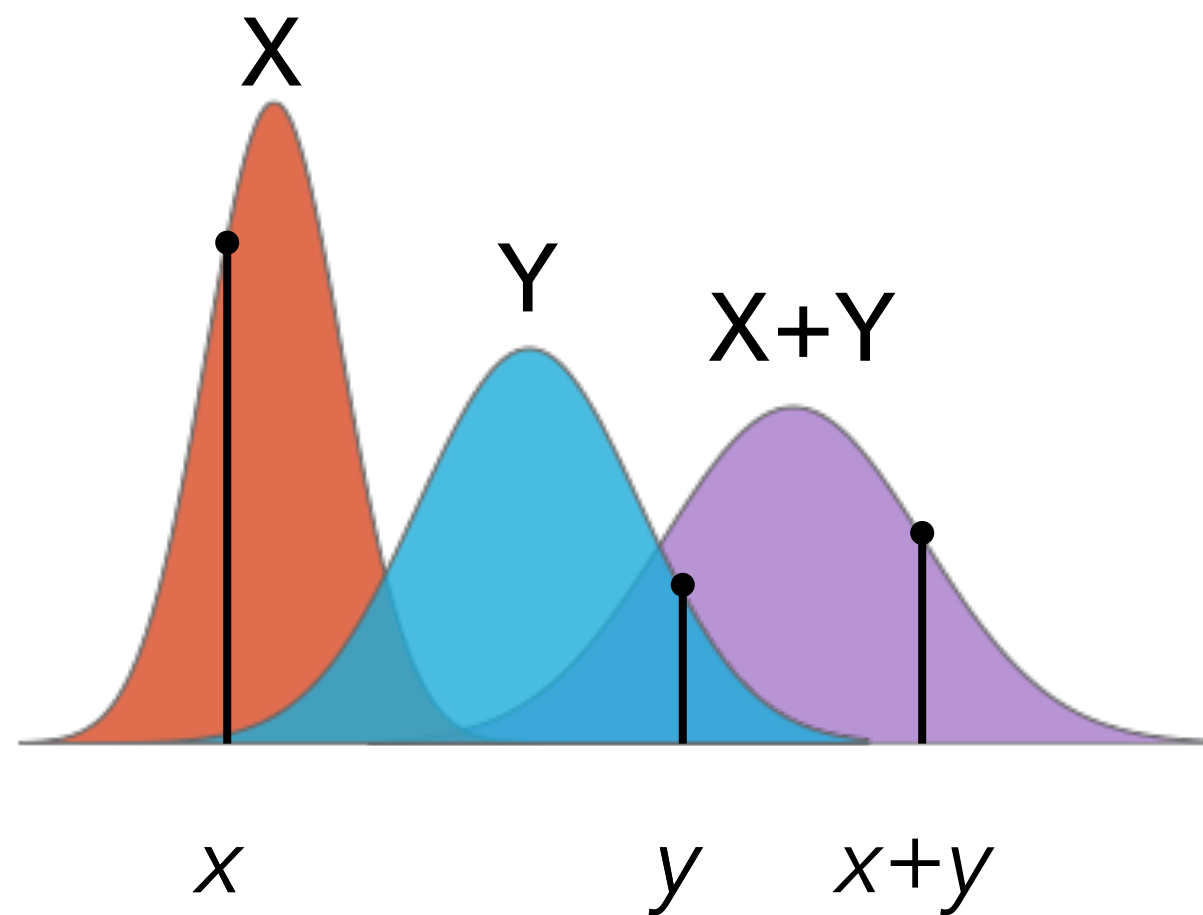
Semantics

Uncertain<T> encapsulates probability distributions and hides statistical complexity.

- Computing over random variables
- Evaluating expected value & conditionals

Computations

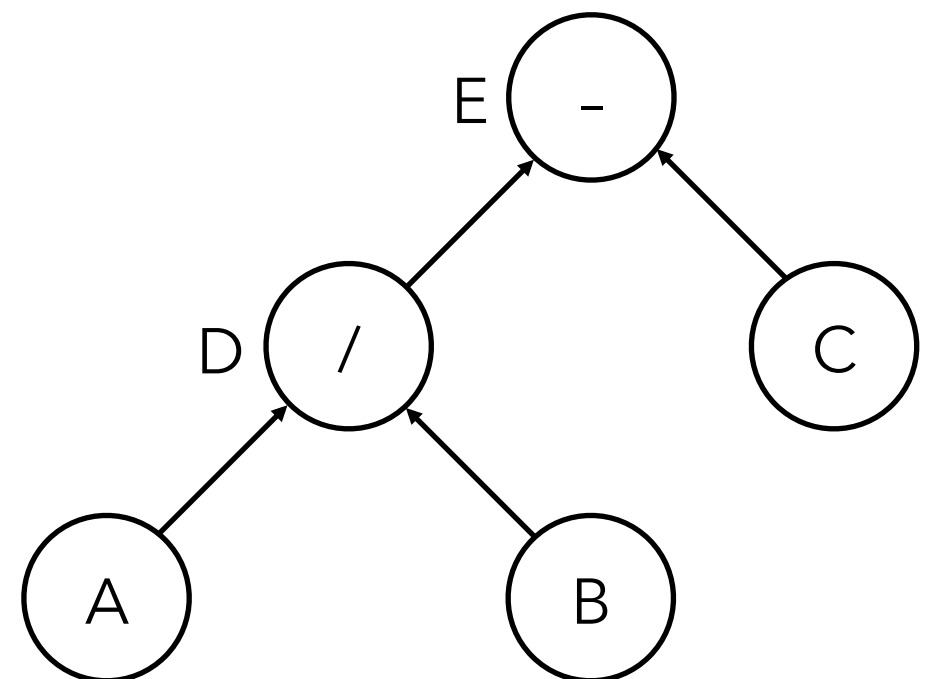
Represent distributions by random samples



Computations - lazy evaluation

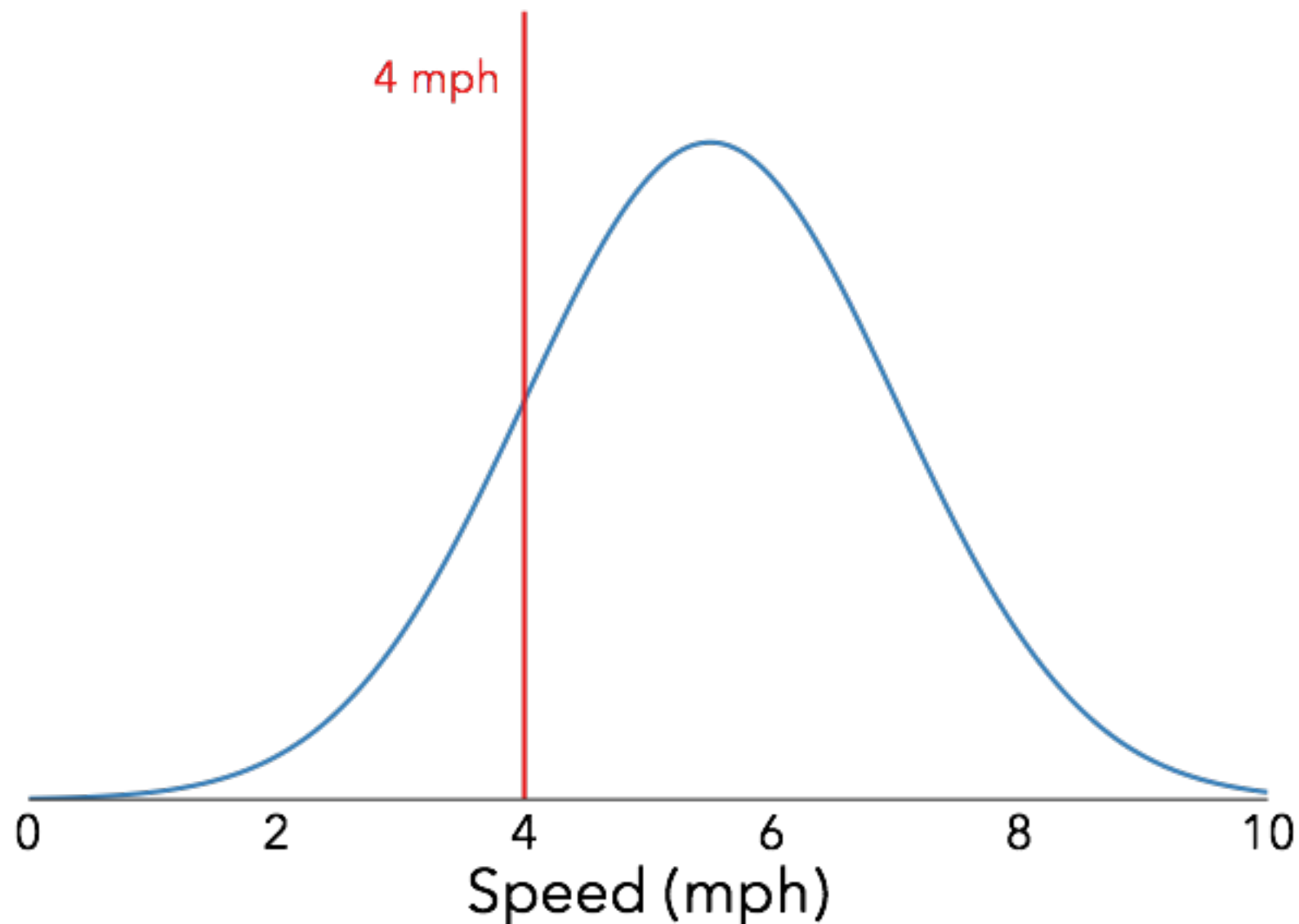
Operators build a Bayesian network rather than evaluating immediately.

$$D = A / B$$
$$E = D - C$$



Evaluating conditionals

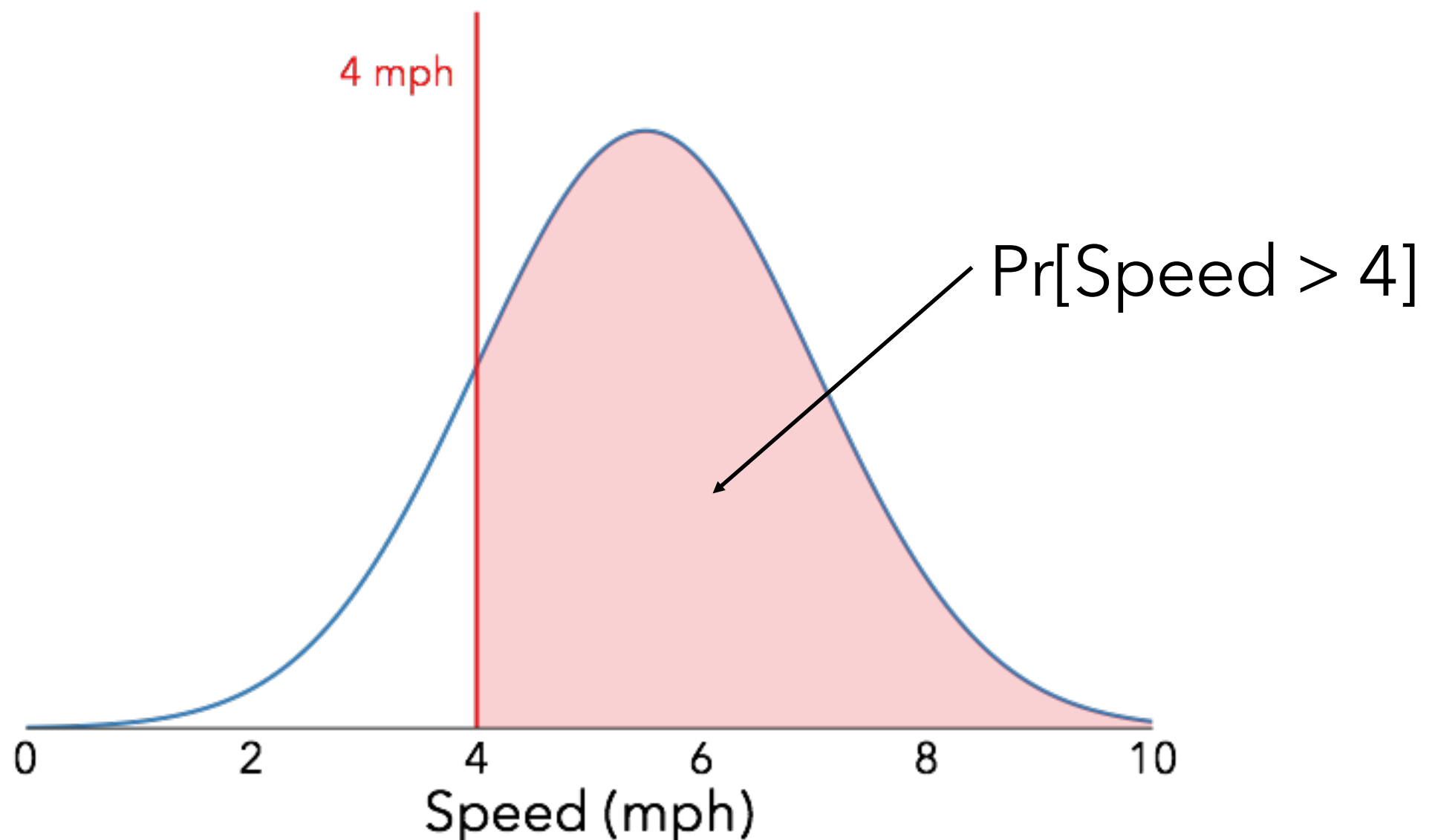
```
if (Speed > 4)  
    Alert("Keep it up!");
```



Evaluating conditionals

```
if (Speed > 4)  
    Alert("Keep it up!");
```

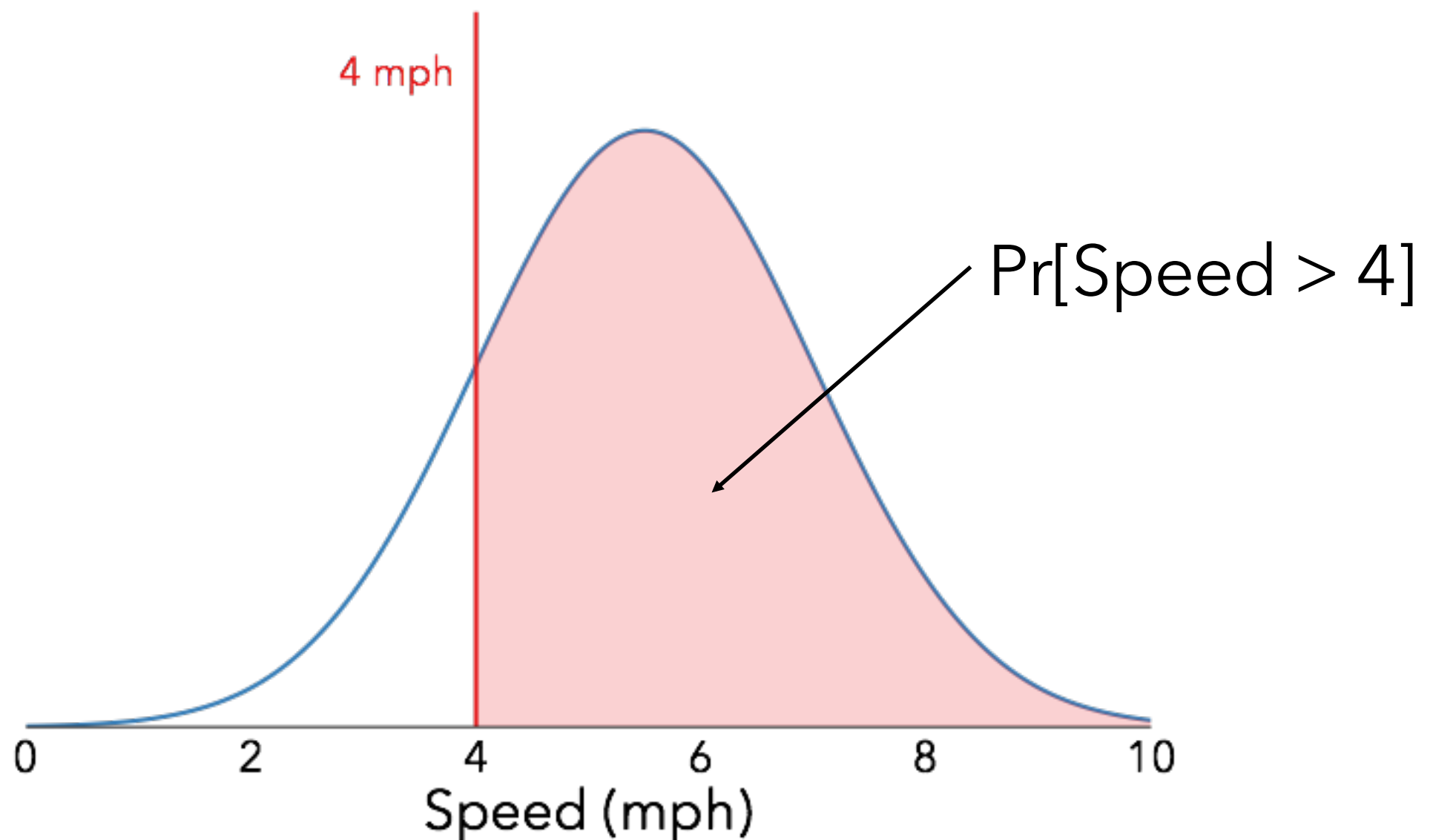
More likely than not
that $\text{Speed} > 4$?



Evaluating conditionals

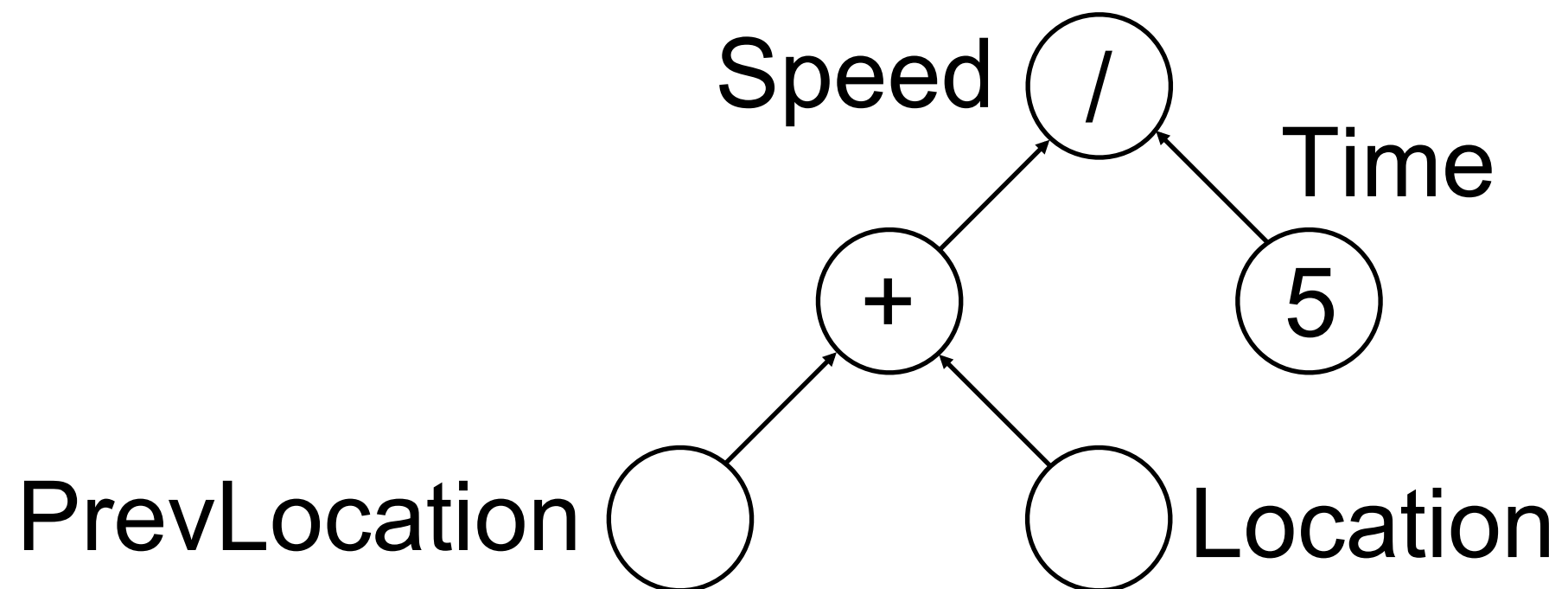
```
if ((Speed > 4).Pr(0.9))  
    Alert("Keep it up!");
```

At least 90% likely
that $\text{Speed} > 4$?



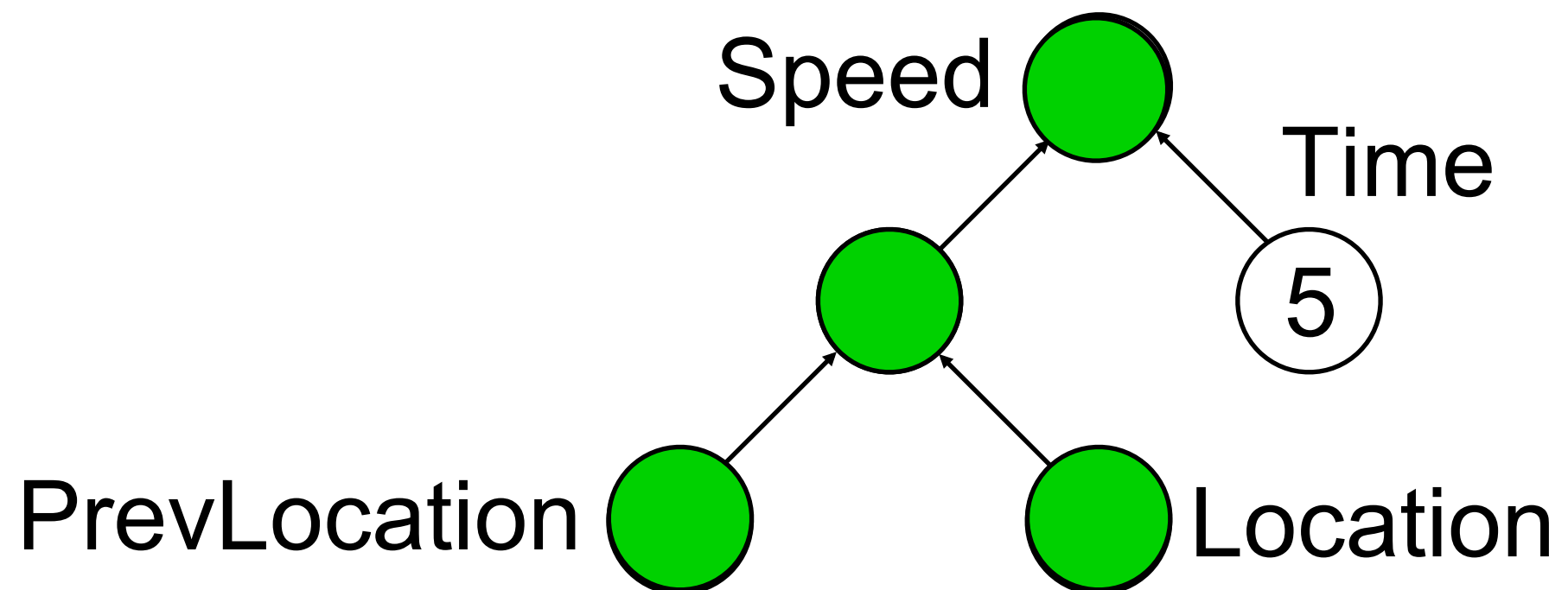
Sampling at runtime

```
if (Speed > 4)  
    Alert("Keep it up!");
```



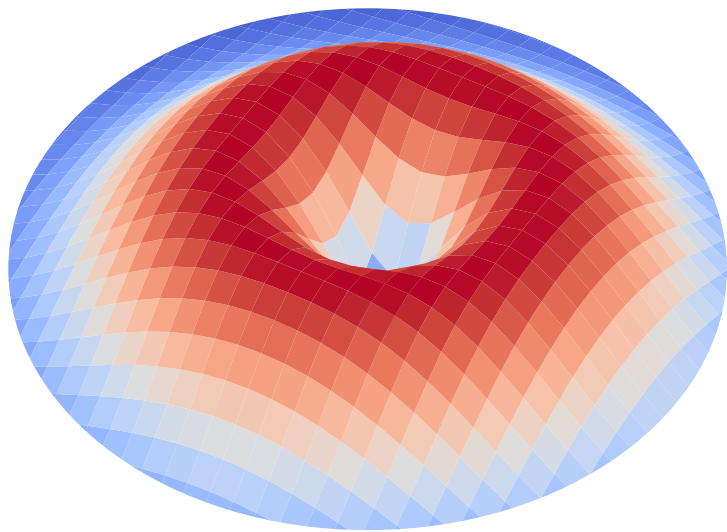
Sampling at runtime

```
if (Speed > 4)  
    Alert("Keep it up!");
```



Sampling functions

Data source responsible for describing errors in estimate



3 D Raleigh Distribution
GPS error



Arbitrary
non-continuous functions

Sampling functions

Data source responsible for describing errors in estimate

```
GeoCoordinate Sample (GeoCoordinate location,  
    double accuracy) {  
    return SampleRayleigh(location, accuracy);  
}
```

Identifying absurd data

```
GeoCoordinate PrevLocn = Get();
```

```
Sleep(5);
```

```
GeoCoordinate Location = Get();
```

```
double Dist =
```

```
    Distance(PrevLocn, Location);
```

```
double Speed = Dist / 5;
```

```
if (Speed > 4)
```

```
    Alert("That's crazy!");
```

Naïve 30 false positives

Identifying absurd data

```
Uncertain<GeoCoordinate> PrevLocn = Get();  
Sleep(5);
```

```
Uncertain<GeoCoordinate> Location = Get();
```

```
Uncertain<double> Dist =  
    Distance(PrevLocn, Location);
```

```
Uncertain<double> Speed = Dist / 5;
```

```
if (Speed > 4)                                Naïve 30 false positives  
    Alert("That's crazy!"); 50% 4 false positives
```


Identifying absurd data

```
Uncertain<GeoCoordinate> PrevLocn = Get();  
Sleep(5);
```

```
Uncertain<GeoCoordinate> Location = Get();
```

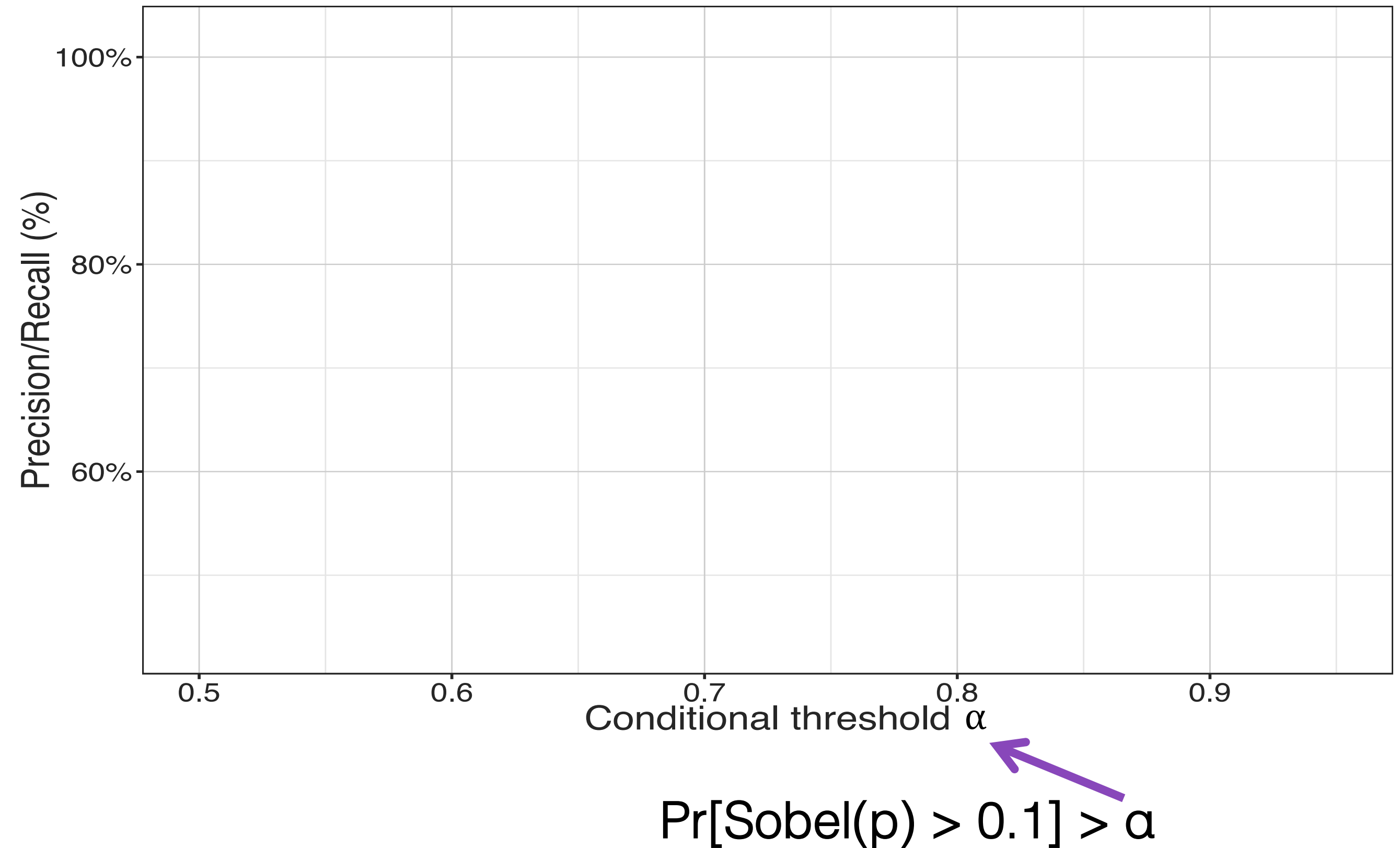
```
Uncertain<double> Dist =  
    Distance(LastLocn, Location);
```

```
Uncertain<double> Speed = Dist / 5;
```

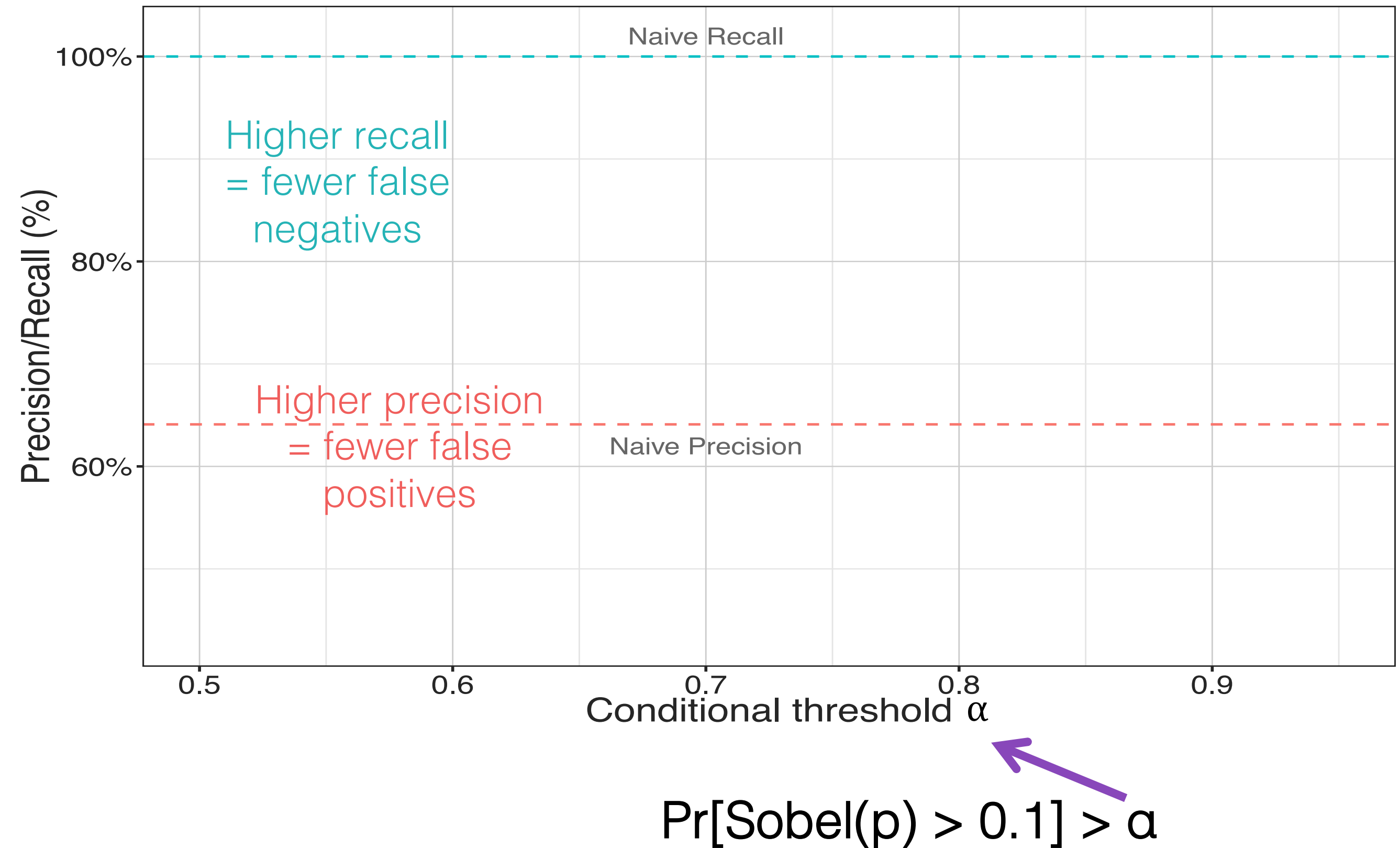
```
if ((Speed > 4).Pr(0.9))  
    Alert("That's crazy!");
```

Naïve	30 false positives
50%	4 false positives
90%	none

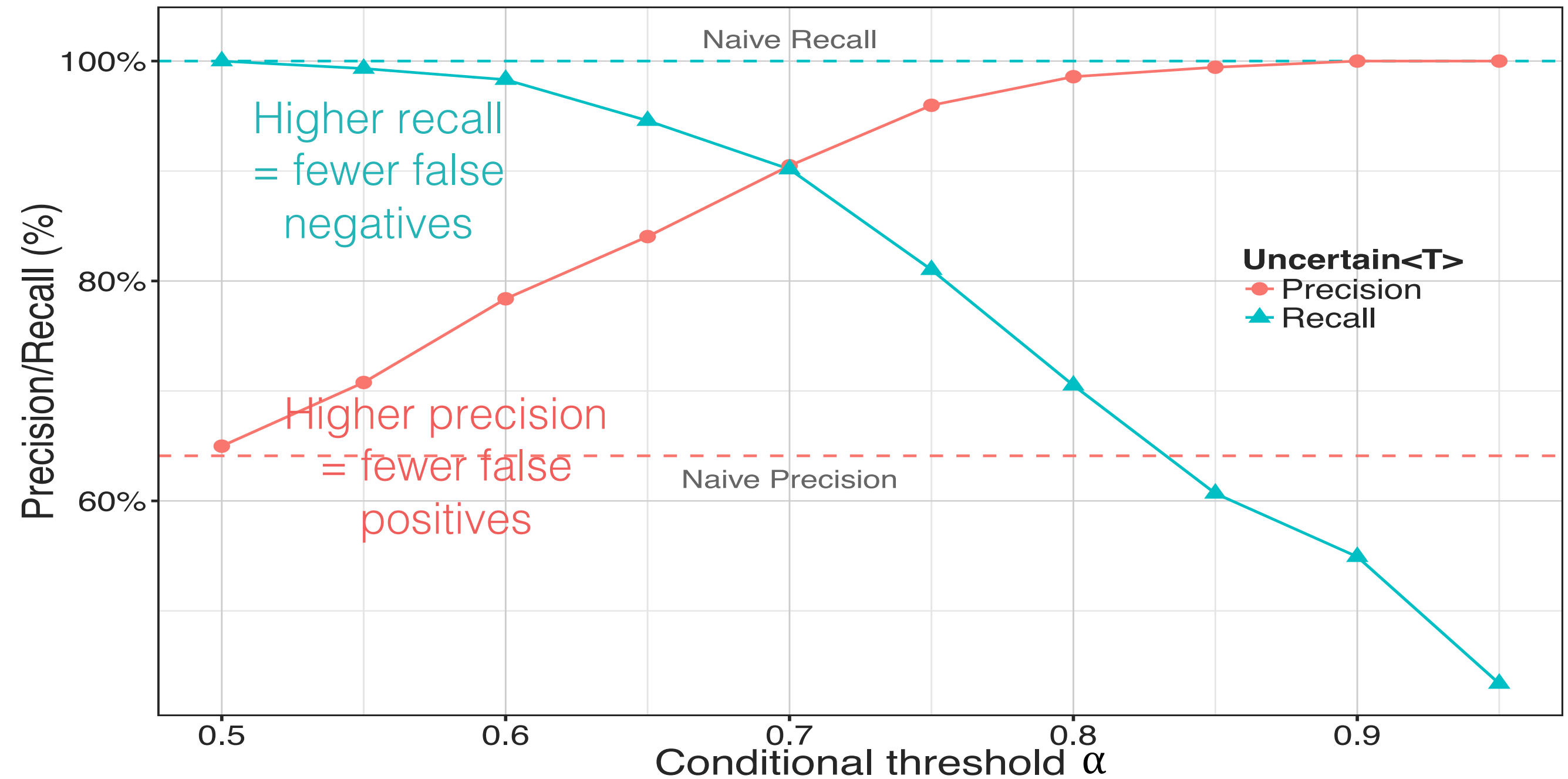
Edge Detection



Edge Detection



Edge Detection



$\Pr[\text{Sobel}(p) > 0.1] > \alpha$

Uncertain<T>

an abstraction for reasoning about noise

[ASPLOS'14]

exploiting context

improving accuracy with more language & inference

[rejected so far]

what does it mean?

probabilistic assertions

[PLDI'14]

Context



AUSTIN RATINGS & REVIEWS LISTS BUZZ

Search Austin

Austin **restaurants** ▾

Zagat Ratings

1-15 OF 492

Sort by: **Relevance**

Food
0 or higher

Decor
0 or higher

Service
0 or higher

Cost
\$134 or lower



Uchi Restaurant
Japanese Bouldin Creek

FOOD	DECOR	SERVICE	COST
29	27	27	\$73



Franklin Barbecue
Barbecue East Austin

FOOD	DECOR	SERVICE	COST
28	20	23	\$23



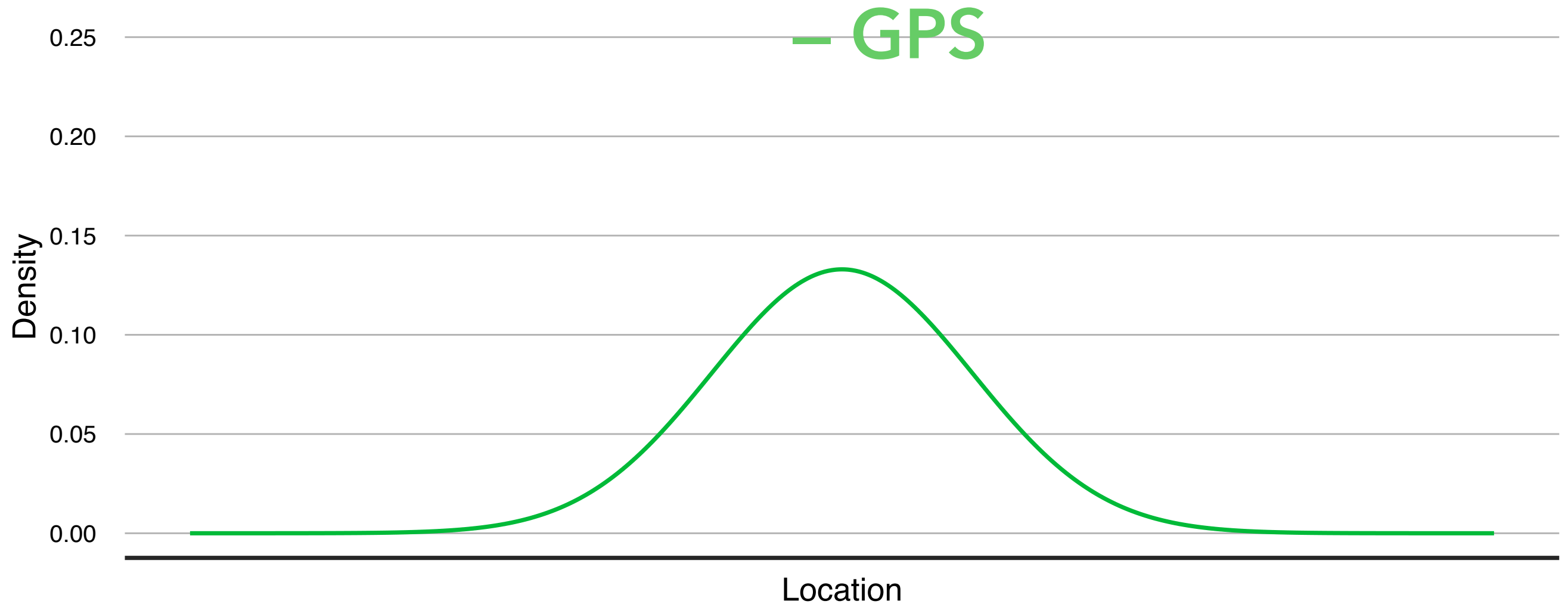
Uchiko
Japanese Rosedale

FOOD	DECOR	SERVICE	COST
------	-------	---------	------

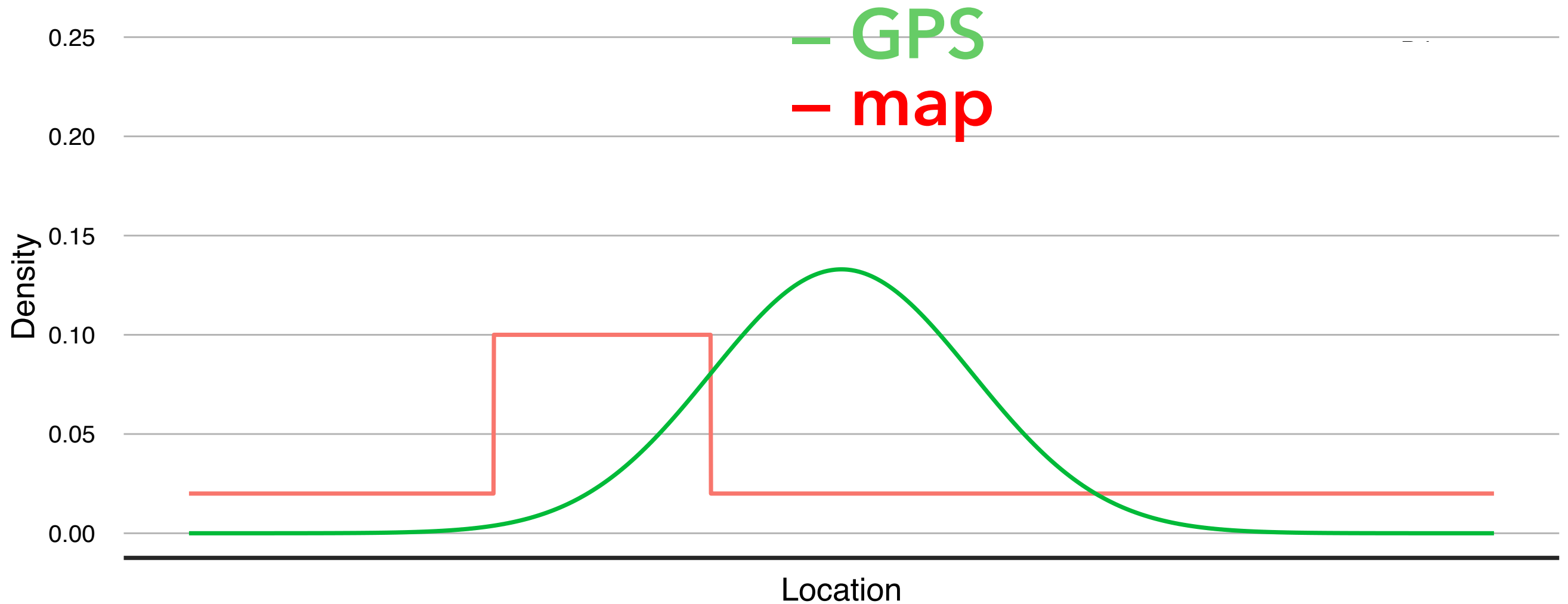


E

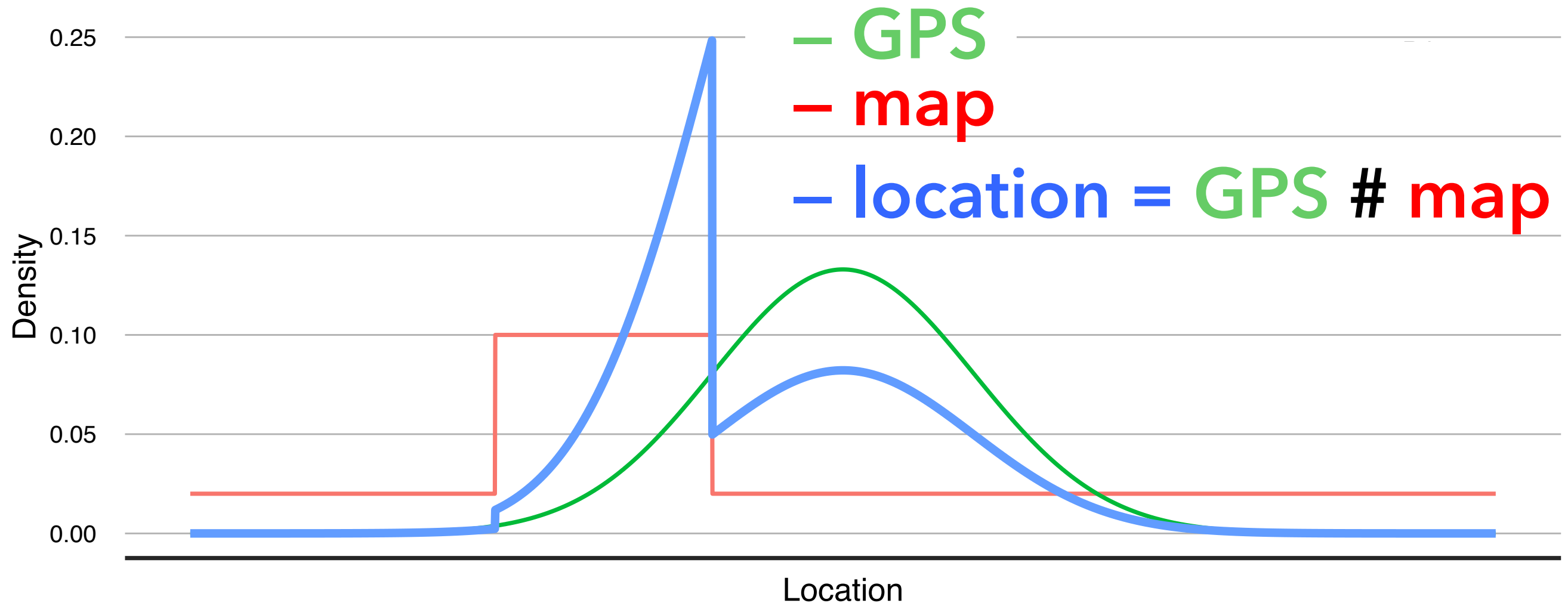
Adding domain knowledge



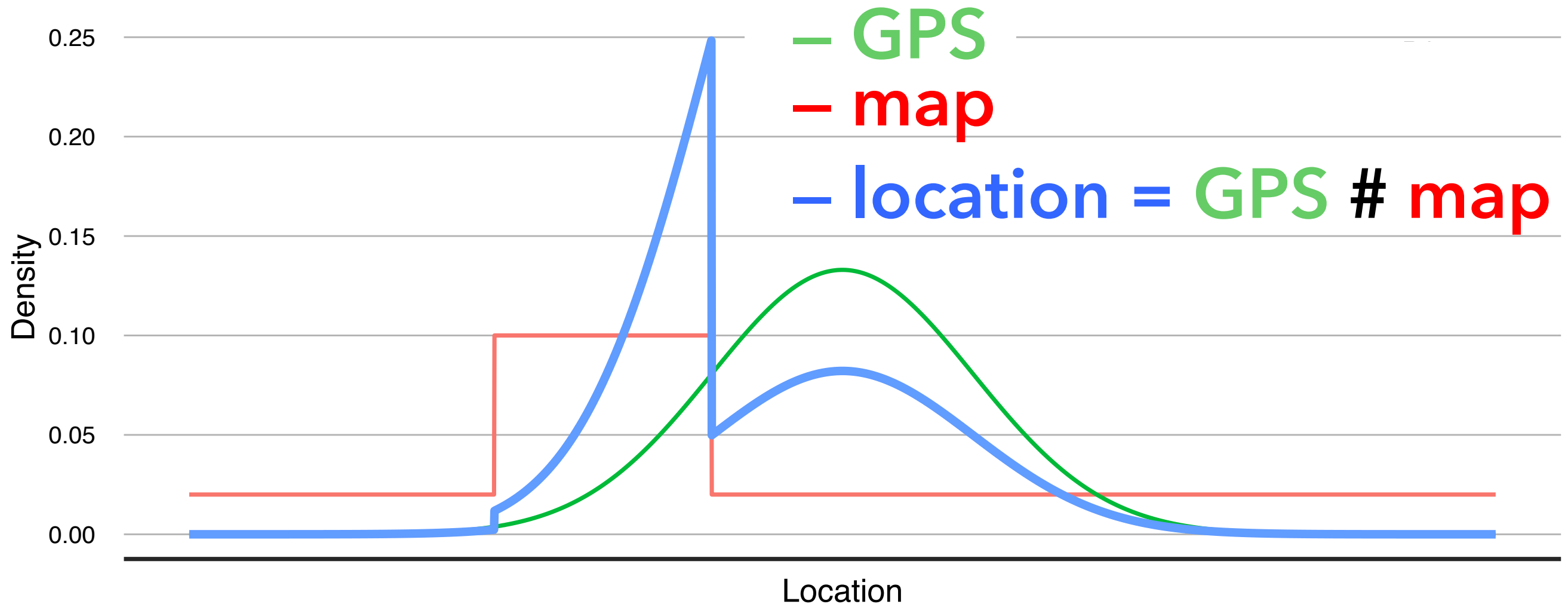
Adding domain knowledge



Adding domain knowledge



Adding domain knowledge



Bayes Rule

posterior

likelihood

prior

$$\Pr[H|E] = \Pr[E|H] \Pr[H] / \Pr[E]$$

Two constructs

<|

**Building probability
distributions**

conditional probability

#

**Composing context
and estimates**

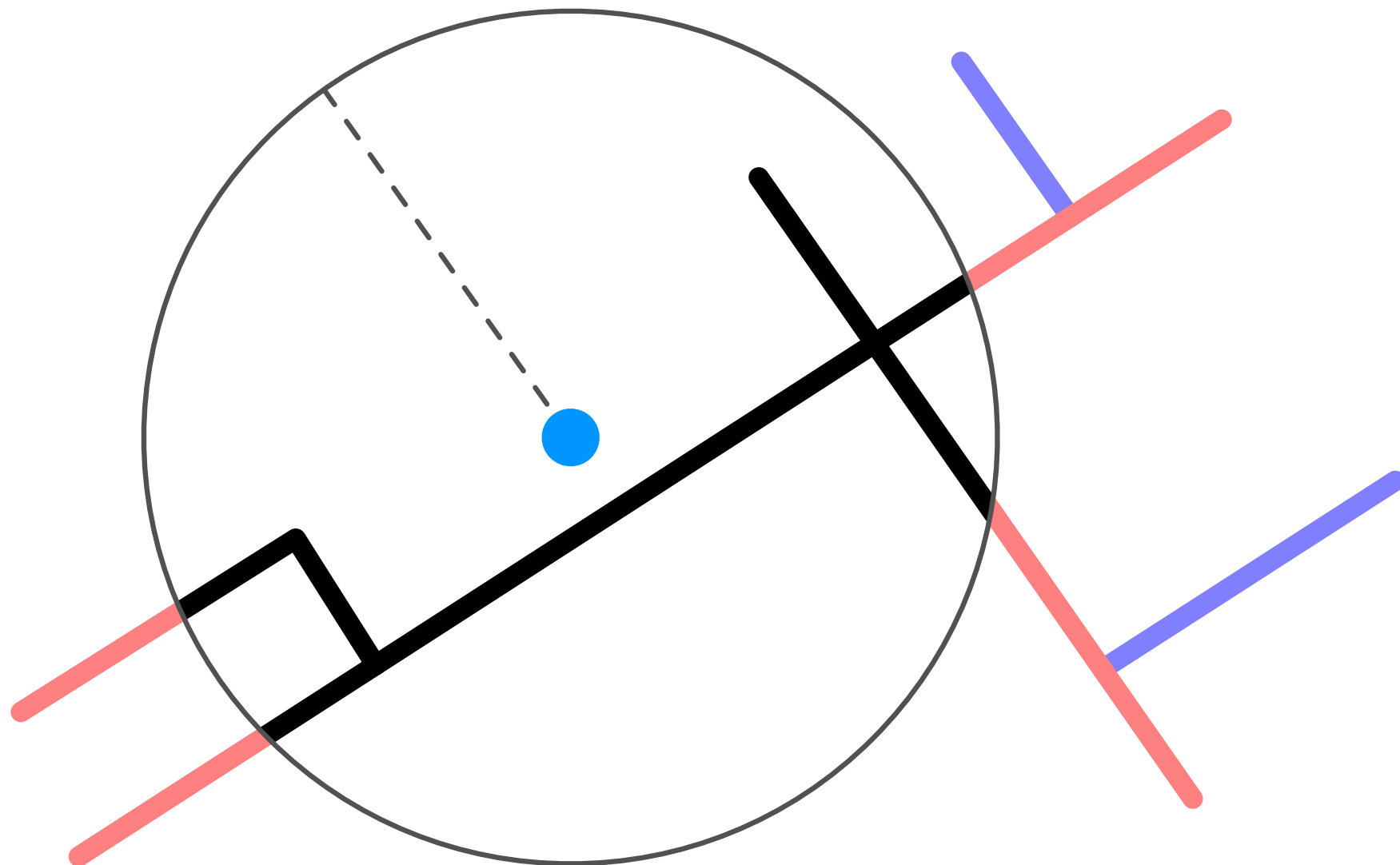
Bayesian inference

Implementation *a new sequential
likelihood reweighting* algorithm

GPS navigation - road snapping

```
// find relevant roads
```

```
Uncertain<Point> roadPrior = new uncertain<Point>(()=>  
SamplePrior(location, accuracy, radiusFactor, weight))
```



GPS navigation – road snapping

```
// find relevant roads
```

```
Uncertain<Point> roadPrior = new uncertain<Point>(()=>  
SamplePrior(location, accuracy, radiusFactor, weight))
```

```
// improve location estimate
```

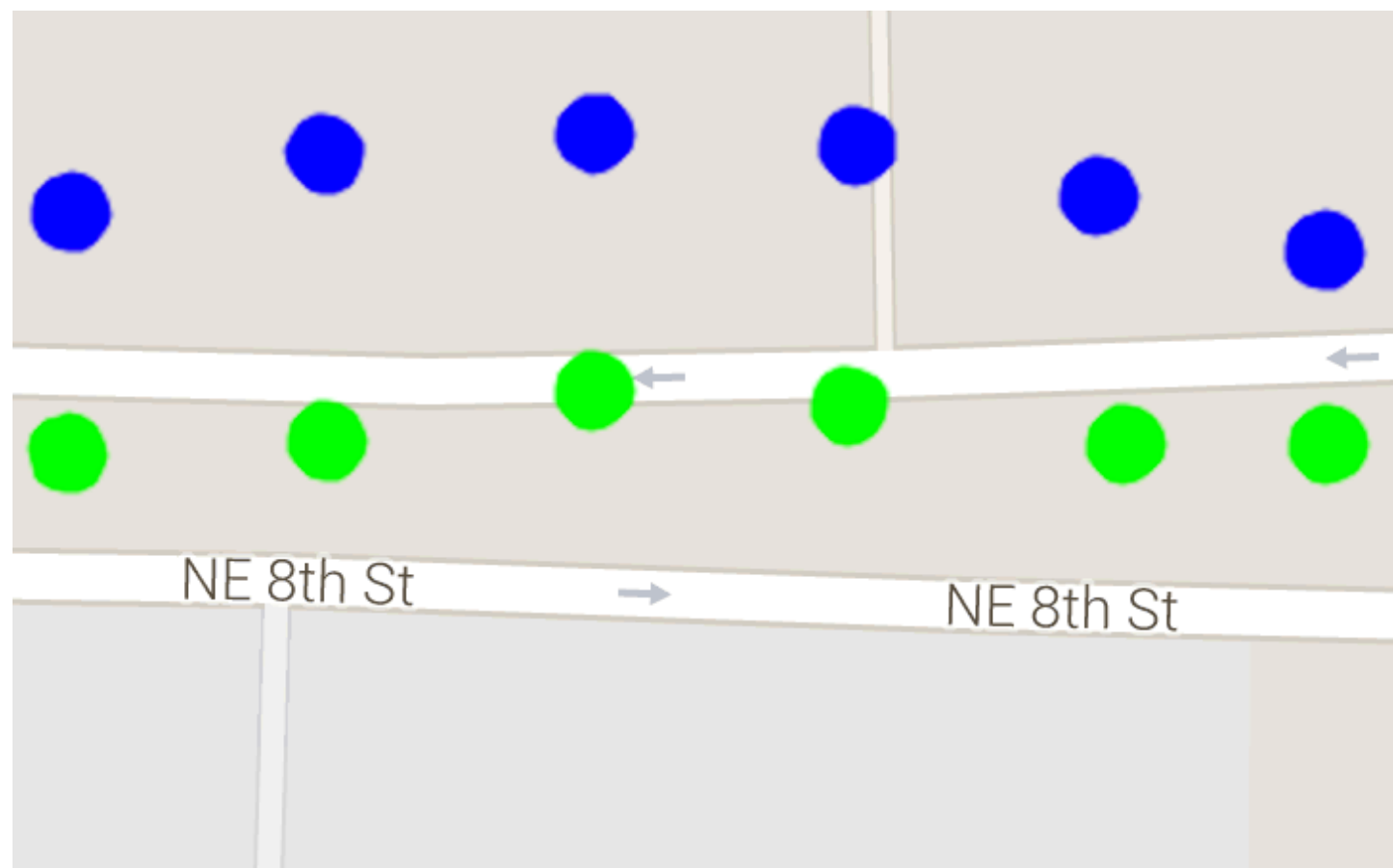
```
Uncertain<Point>
```

```
    NewLocation = GPSLikelihood # roadPrior
```

GPS navigation

Driver is *likely* on a road!

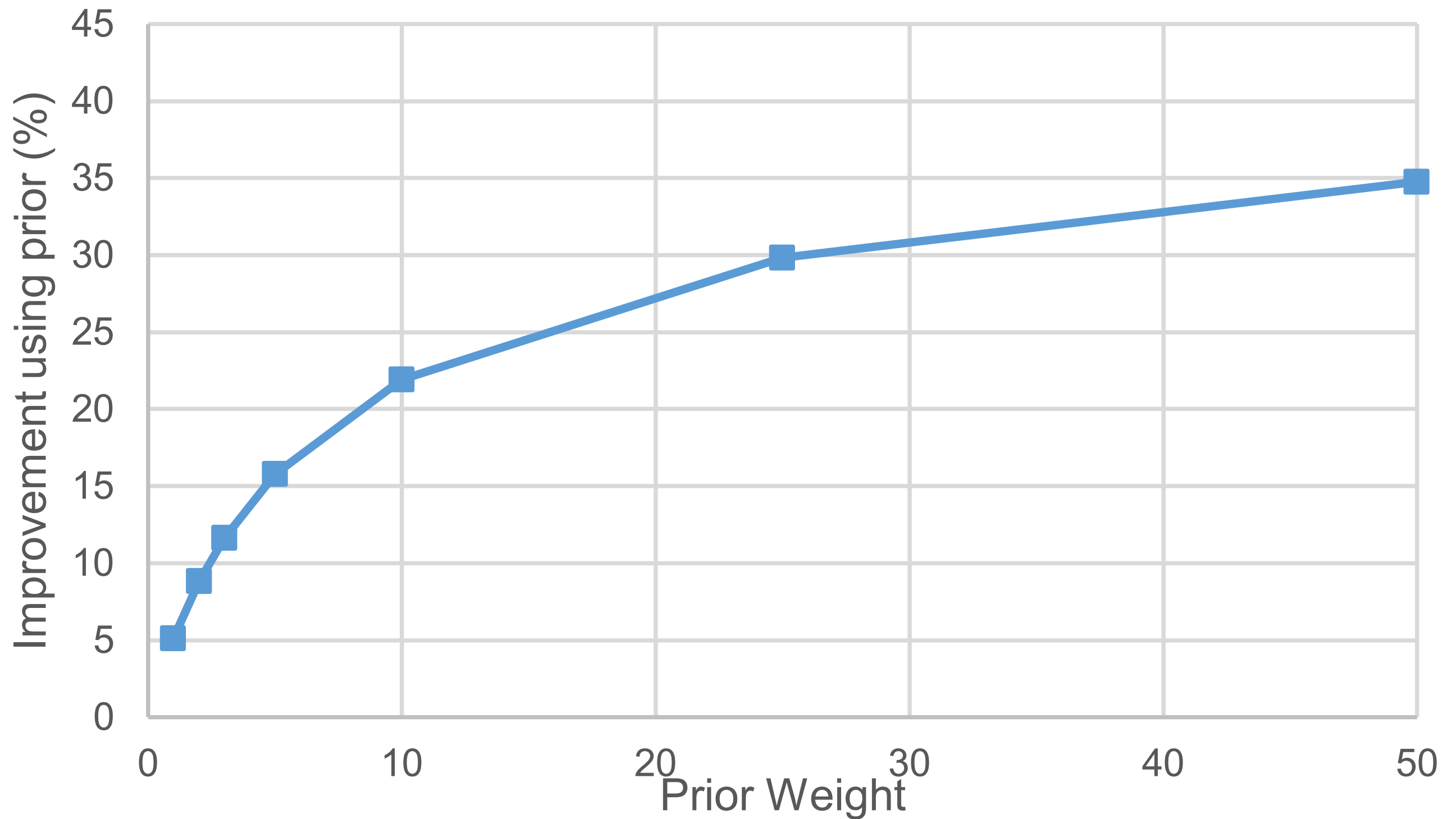
Driving on a road (or not!)



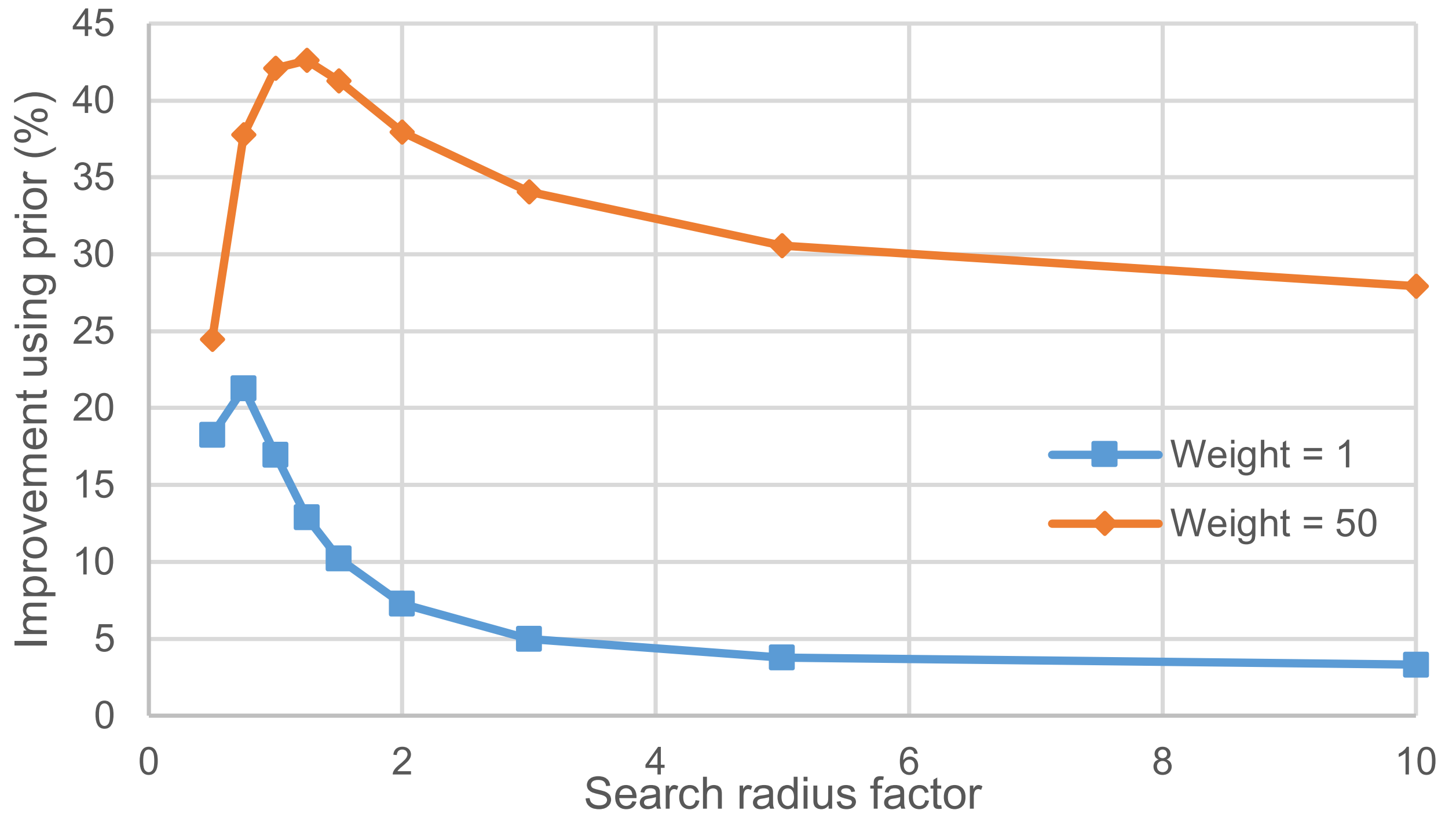
● GPS

● GPS + road snapping

Weighing the map prior

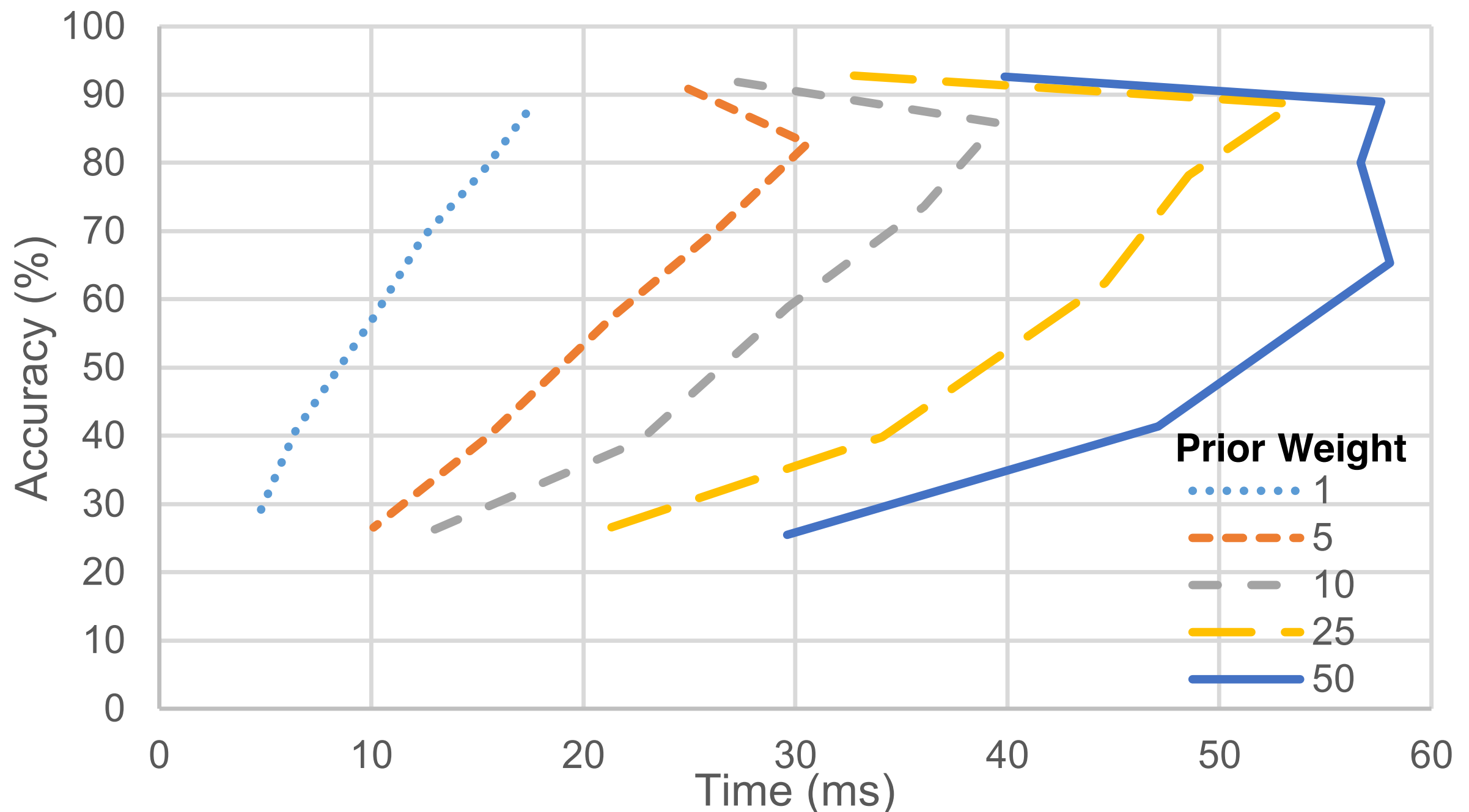


Map radius factor



Sequential likelihood reweighing

Time to sample as a function of prior strength



Uncertain<T>

an abstraction for reasoning about noise

[ASPLOS'14]

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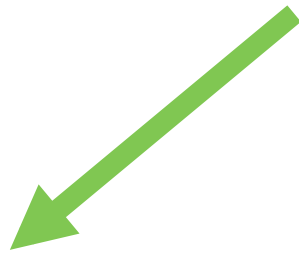
[rejected so far]

what does it mean?

probabilistic assertions

[PLDI'14]

assert file != NULL



test



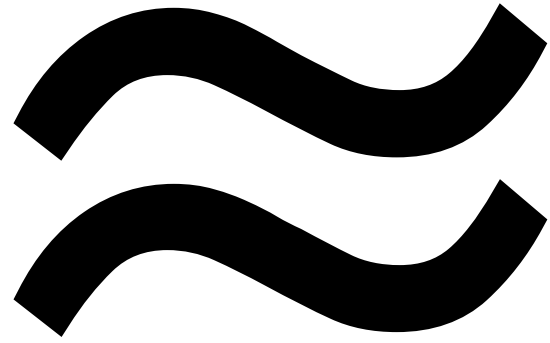
verify



check

assert e

e must hold on **every** execution



Approximate computing

The approximate image is close to the precise version

k-means clustering is likely to converge on unreliable hardware

assert e

e must hold on **every** execution



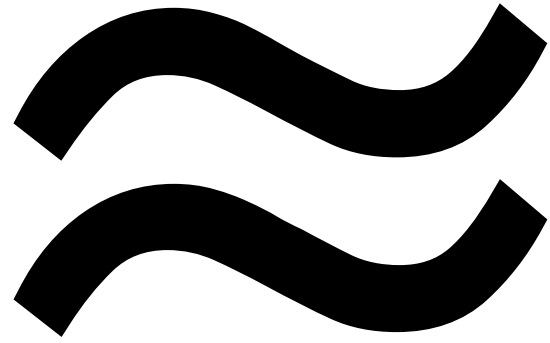
Obfuscation for privacy

obfuscated data is still useful in aggregate

Sensing

within 5 mph of actual speed





Approximate computing

The approximate image is close to the precise version

k-means clustering is likely to converge on unreliable hardware

Traditional assertions are insufficient for programs with probabilistic behavior

Obfuscation for privacy

obfuscated data is still useful in aggregate

Sensing

within 5 mph of actual speed



Assertions are insufficient for data obfuscation

```
true_avg = average(salaries)
private_avg =
    average(obfuscate(salaries))
assert true_avg - private_avg
    <= 10,000
```



Assertions are insufficient for data obfuscation

```
true_avg = average(salaries)
private_avg =
    average(obfuscate(salaries))
assert true_avg - private_avg
    <= 10,000
```

probability
distribution



Assertions

assert *e*

Probabilistic assertions

passert e, p, c

Probabilistic assertions

passert e, p, c

e must hold with probability p
at confidence c

Probabilistic assertion

```
true_avg = average(salaries)
private_avg =
    average(obfuscate(salaries))
passert (true_avg - private_avg
          <= 10,000), 90, 99
```



Verification

probabilistic
program

```
float obfuscated(float n) {  
    return n + gaussian(0.0, 1000.0);  
}  
float average_salary(float* salaries) {  
    total = 0.0;  
    for (int i = 0; i < COUNT; ++i)  
        total += obfuscated(salaries[i]);  
    avg = total / len(salaries);  
    p_avg = ...;
```

```
passert e, p, c
```

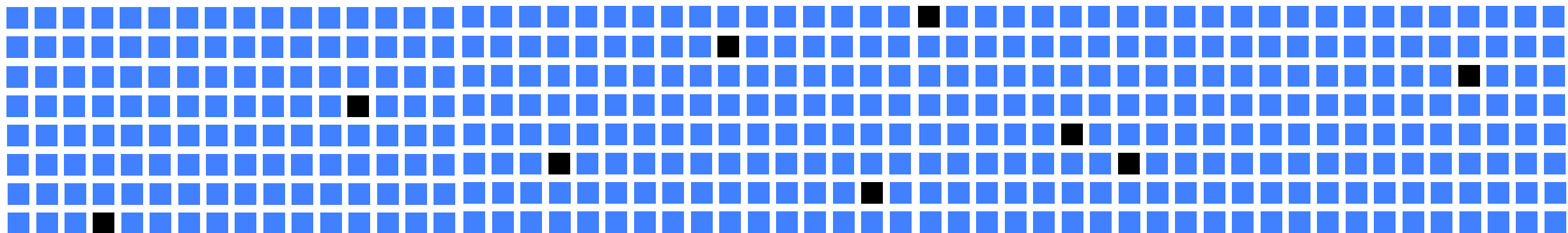
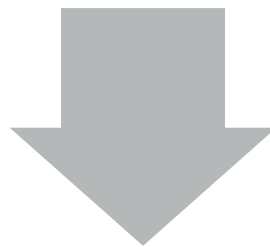
?

Naïve verification

probabilistic
program

```
float obfuscated(float n) {  
    return n + gaussian(0.0, 1000.0);  
}  
float average_salary(float* salaries) {  
    total = 0.0;  
    for (int i = 0; i < COUNT; ++i)  
        total += obfuscated(salaries[i]);  
    avg = total / len(salaries);  
    p_avg = ...;  
  
    passert e, p, c
```

?



Efficient verification

distribution extraction

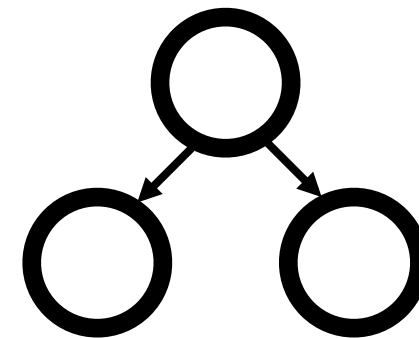
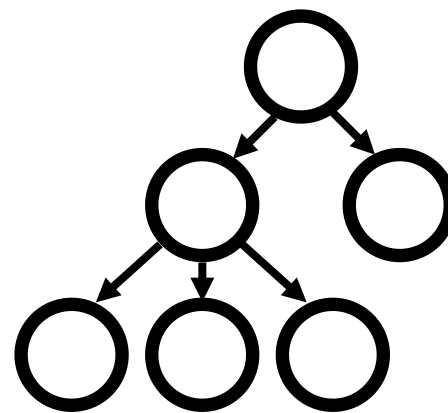
via symbolic execution

statistical

optimizations

verification

```
float obfuscated(float n) {  
    return n + gaussian(0.0, 1000.0);  
}  
float average_salary(float* salaries) {  
    total = 0.0;  
    for (int i = 0; i < COUNT; ++i)  
        total += obfuscated(salaries[i]);  
    avg = total / len(salaries);  
    p_avg = ...;  
    passert e, p, c  
}
```



Bayesian network

IR

Evaluation

sensing

gpswalk

privacy

salary

salary-abs

approximate
computing

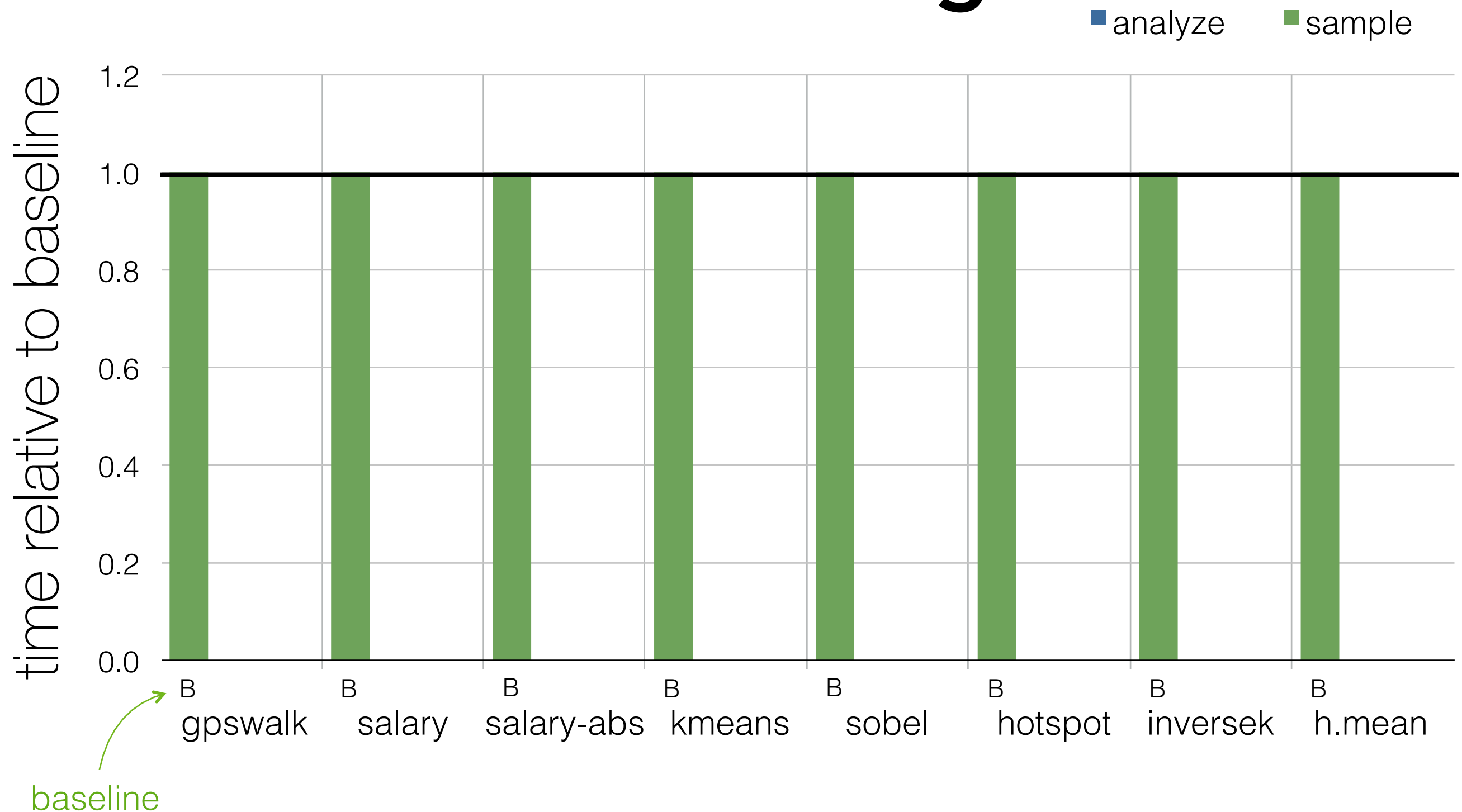
kmeans

sobel

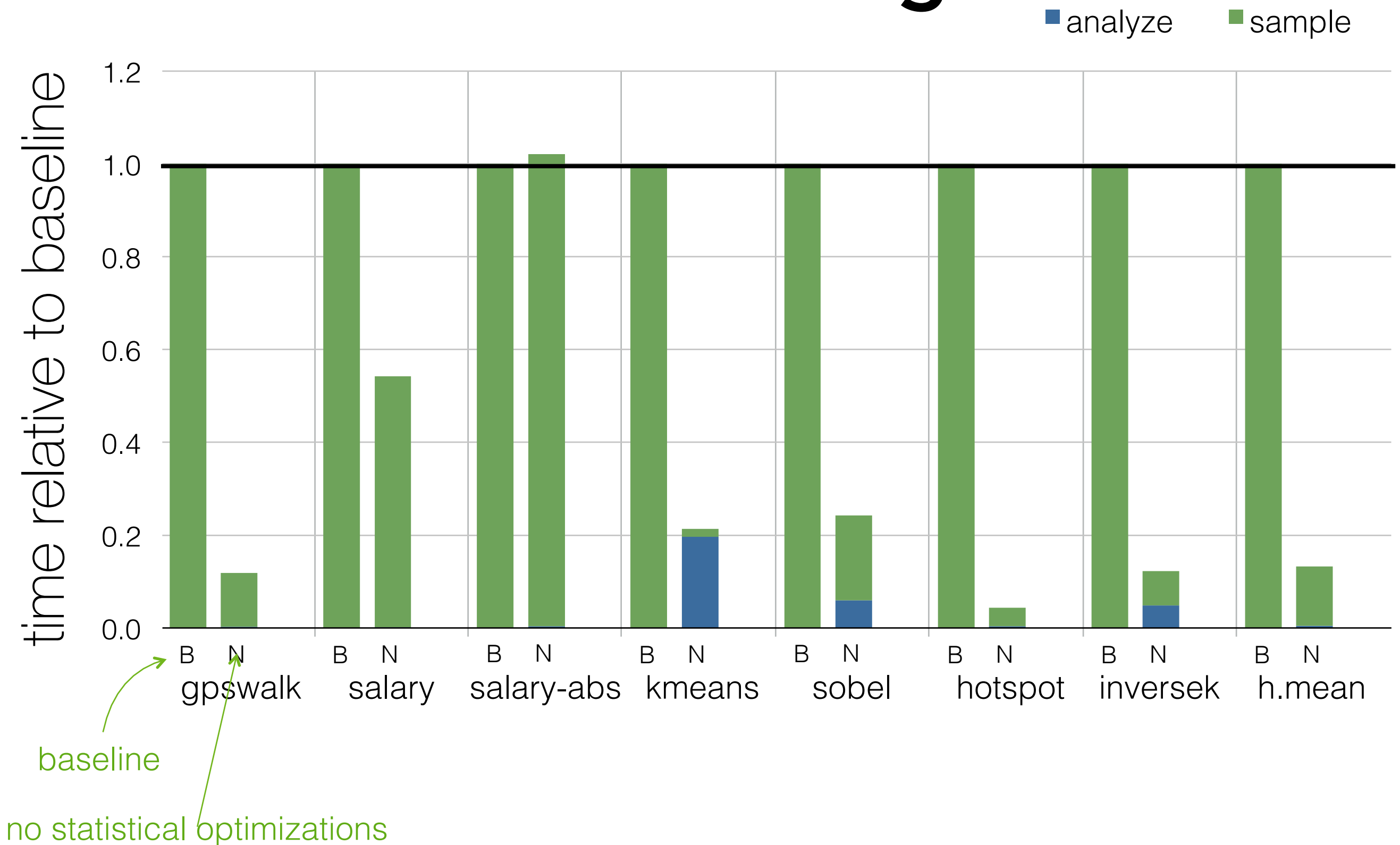
hotspot

inversek2j

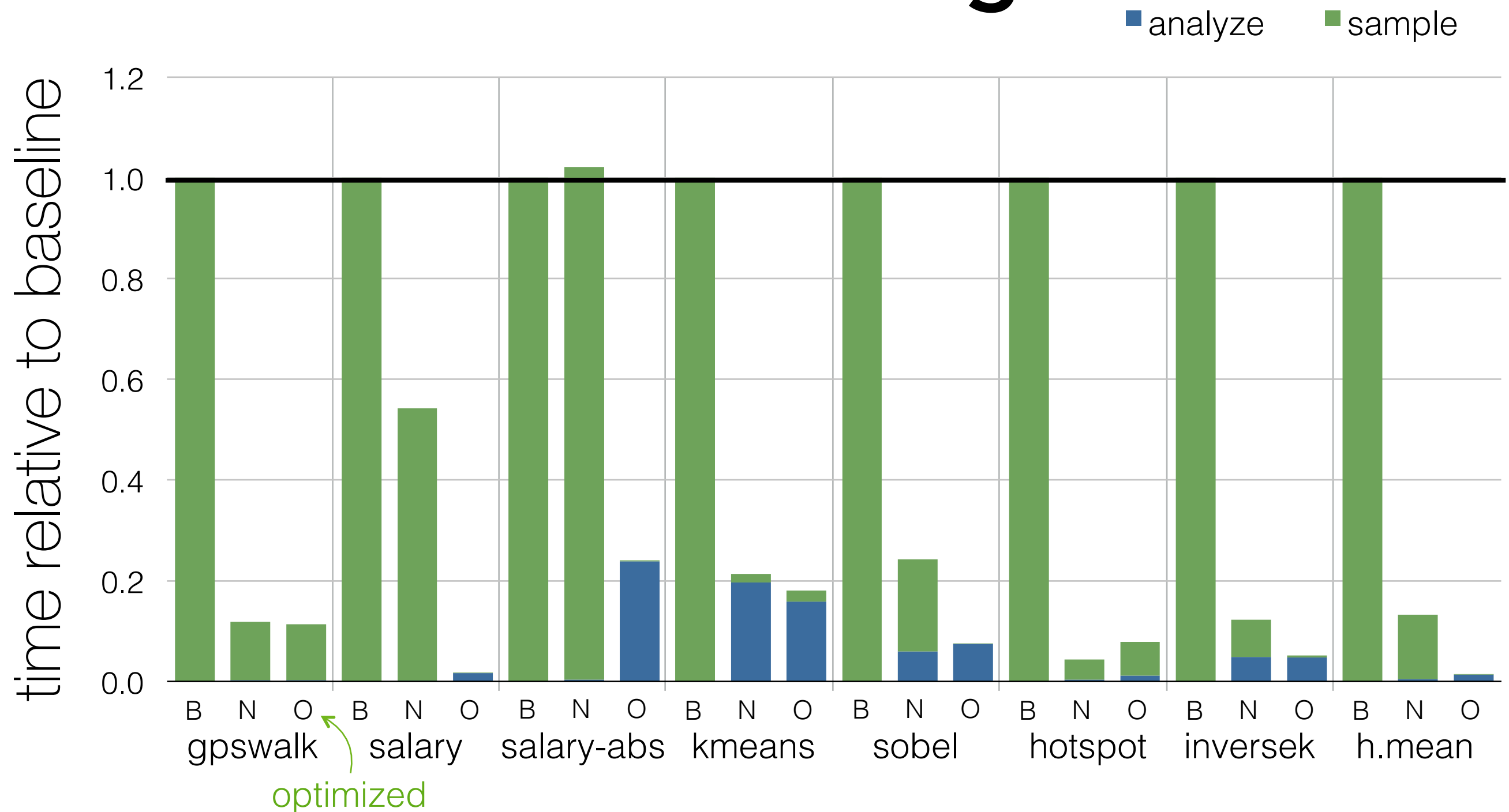
Time vs Stress Testing



Time vs Stress Testing



Time vs Stress Testing



- 24× faster than baseline verifier on average
- Mostly analysis time

Uncertain<T>

an abstraction for reasoning about noise

[ASPLOS'14]

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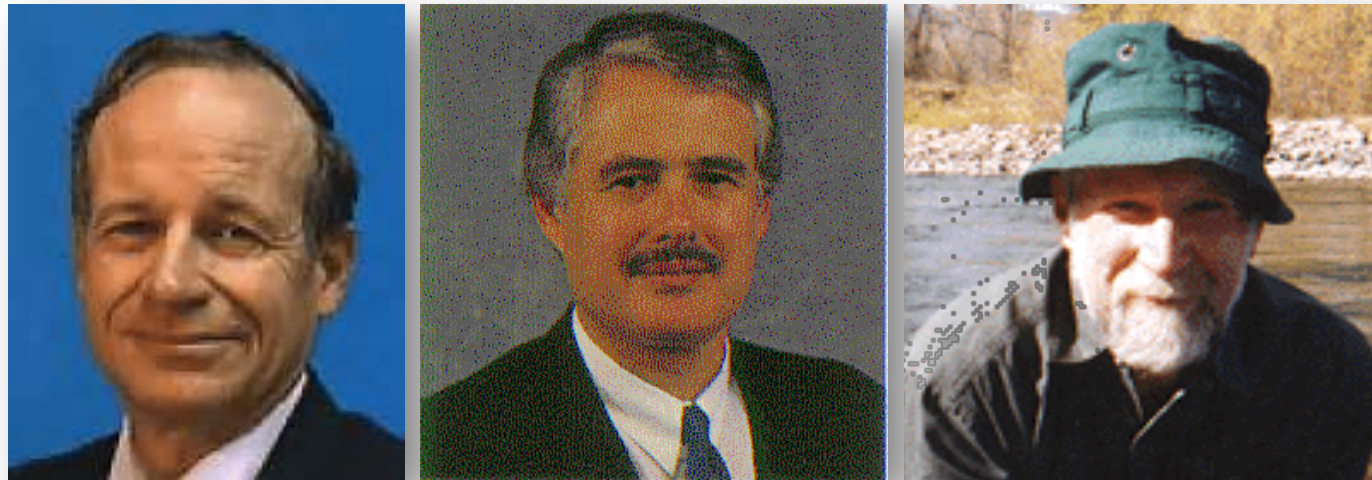
1985 IEEE floating point

**Computing is at a similar point
in history for estimates**

Thank you!

A Byte of My Story

A Byte of My Story



Mentors



Family



Congressional Testimony

Fail, learn, succeed, repeat

- Rejected job applications
 - 1984 (all), 1993 (8 of 11), 2011 (4 of 8)
- Failed PhD qualifying exam
- Rejected first three grant applications
- Rejected 3 times one of my most cited papers
- Rejected papers, grants, papers, ...