Problem  A finite state machine has input alphabet \{1, 2\}. It accepts a string if the sum of its digits is 0 modulo 3. Thus, 12 is accepted and 112 rejected. The empty string’s digits add up to 0.

Solution  Let $d$ be the sum of the digits of the string seen so far. I label each state with $d \mod 3$. 