A Few Small Orc Programs

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A Orc program

An experiment tosses two dice.
 Experiment is a success if the dice throws sum to 7.

def toss() = Random(6) + 1

• exp(n) runs n experiments and reports the number of successes.

```
-- toss returns a random number between 1 and 6

def exp(0) = 0

def exp(n) = exp(n-1)

+ (if toss() + toss() = 7 then 1 else 0)
```

Translation of the dice throw program

```
def toss() = add(x, 1) < x < Random(6)
def exp(n) =
   (Ift(b) \gg 0
   |Iff(b)| \gg
     (add(x, y))
          \langle x \langle (exp(m) \langle m \langle sub(n, 1)) \rangle
          \langle y \langle (Ift(bb)) \gg 1 | Iff(bb) \gg 0 \rangle
             < bb < equals(p, 7)

                   < q < toss()
                   < r < toss()
     < b < equals(n, 0)
```

Note: 2n parallel calls to toss().

Orc Calculus

- External sites:
 - A site is called like a procedure with parameters.
 - Site returns any number of values.
 - The value is published.
- Combinators
- Definitions

No notion of data type, thread, process, channel, synchronization, parallelism · · ·

Orc Language

- Orc Calculus
- Syntactic Sweeteners
 - Data Types: Number, Boolean, String, with Java operators
 - Conditional Expression: if E then F else G
 - Data structures: Tuple, List, Record
 - Pattern Matching; Clausal Definition
 - Closure
 - Class for active objects
- Site Library

Every Orc language program is translated to Orc calculus.



- Simple: just a site call, CNN(d)Publishes the value returned by the site.
- Composition of two Orc expressions:

```
do f and g in parallel f \mid g Symmetric composition for all x from f do g f > x > g Sequential composition
```

 $f \mid g$: Evaluate f and g independently. Publish all values from both.

```
f > x > g:
```

For all values published by f do g. Publish only the values from g.

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Schematic of Sequential composition

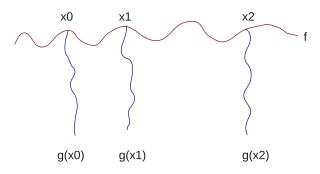


Figure: Schematic of f > x > g

Sequential composition: f > x > g

For all values published by f do g. Publish only the values from g.

- CNN(d) > x > Email(address, x)
 - Call CNN(d).
 - Bind result (if any) to x.
 - Call Email(address, x).
 - Publish the value, if any, returned by *Email*.
- $(CNN(d) \mid BBC(d)) > x > Email(address, x)$
 - May call *Email* twice.
 - Publishes up to two values from *Email*.

Notation: $f \gg g$ for f > x > g, if x is unused in g.

Right Associative: f > x > g > y > h is f > x > (g > y > h)

Subset Sum

Given integer n and list of integers xs. parsum(n,xs) publishes all sublists of xs that sum to n. parsum(5,[1,2,1,2]) = [1,2,2], [2,1,2] parsum(5,[1,2,1]) is silent $def \ parsum(0,[]) = []$ $def \ parsum(n,[]) = stop$

 $\begin{array}{ll} \textit{def} \;\; parsum(n,x:xs) = \\ parsum(n,xs) & -- \;\; \text{all sublists that do not include } x \\ | \;\; parsum(n-x,xs) \;\; > ys > x:ys \;\; -- \;\; \text{all sublists that include } x \end{array}$

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    def parsum(0, []) = []
    def parsum(n, []) = stop
    def parsum(n, x : xs) =
         parsum(n, xs) —— all sublists that do not include x
       parsum(n-x,xs) > ys > x : ys -- all sublists that include x
```

Structure of Orc Expression

- Simple: just a site call, CNN(d)
- Composition of two Orc expressions:

```
do f and g in parallel f \mid g Symmetric composition for all x from f do g f > x > g Sequential composition \rightarrow if f halts without publishing do g f; g Otherwise
```

Subset Sum (Contd.), Backtracking

Given integer n and list of integers xs. segsum(n, xs) publishes the first sublist of xs that sums to n. "First" is smallest by index, lexicographically. segsum(5,[1,2,1,2]) = [1,2,2]segsum(5,[1,2,1]) is silent def segsum(0, []) = [] $def \ seqsum(n, []) = stop$ def seqsum(n, x : xs) =x : seqsum(n - x, xs)

; segsum(n, xs)

Structure of Orc Expression

- Simple: just a site call, CNN(d)
- Composition of two Orc expressions:

```
do f and g in parallel f \mid g Symmetric composition for all x from f do g f > x > g Sequential composition \rightarrow for some x from g do f f < x < g Pruning if f halts without publishing do g f; g Otherwise
```

Pruning: f < x < g

For some value published by g do f.

- Evaluate f and g in parallel.
 - Site calls that need x are suspended. Consider $(M() \mid N(x)) < x < g$
- When g returns a (first) value:
 - Bind the value to x.
 - Kill g.
 - Resume suspended calls.
- Values published by f are the values of (f < x < g).

Notation: $f \ll g$ for f < x < g, if x is unused in f.

Left Associative: f < x < g < y < h is (f < x < g) < y < h

Note: Concurrent computation of f, g and h, above.

Subset Sum (Contd.), Concurrent Backtracking

Publish the first sublist of xs that sums to n.

Run the searches concurrently.

```
def parseqsum(0,[]) = []

def parseqsum(n,[]) = stop

def parseqsum(n,x:xs) =
    (p;q)
        <p< x: parseqsum(n-x,xs)
        <q< parseqsum(n,xs)</pre>
```

Note: Neither search in the last clause may succeed.

val; a syntactic sweetener

Write f < x < g as $val \ x = g$ f

Deflation

- Given expression C(...,e,..), single value expected at e. Translated to C(...,x,..) < x < e where x is fresh.
- Applicable hierarchically.

$$(1|2) * (10|100)$$
 is translated to
 $(Times(x, y) < x < (1|2)) < y < (10|100)$, or without parentheses $Times(x, y) < x < (1|2) < y < (10|100)$

• Implication:

Arguments of site calls are evaluated in parallel.

Note: A strict site is called when all arguments have been evaluated.

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Parsing using Recursive Descent

Consider the grammar:

```
expr ::= term \mid term + expr
term ::= factor \mid factor * term
factor ::= literal \mid (expr)
literal ::= 3 \mid 5
```

Parsing strategy

For each non-terminal, say expr, define expr(xs) for string xs: publish all suffixes of xs such that the prefix is a expr.

$$def isexpr(xs) = expr(xs) > [] > true ; false$$

To avoid multiple publications (in ambiguous grammars),

def isexpr(xs) =

:: true

Site for each non-terminal

```
Given: expr ::= term \mid term + expr
Rewrite: expr ::= term(\epsilon + expr)
def \ expr(xs) = term(xs) > ys > (ys \mid ys > "+" : zs > expr(zs))
def term(xs) = factor(xs) > ys > (ys \mid ys > "*" : zs > term(zs))
def factor(xs) = literal(xs)
                     |xs\rangle"(": ys\rangle expr(ys)\rangle")": zs\rangle zs
def \ literal(n:xs) = n > "3" > xs \mid n > "5" > xs
def \ literal([]) = stop
```

Parallel or

Expressions f and g return single booleans. Compute the parallel or.

```
If t(b), If t(b): boolean t(b), Returns a signal if t(b) is true/false; remains silent otherwise.
```

```
\begin{aligned}
val & x = f \\
val & y = g
\end{aligned}

Ift(x) \gg true \mid Ift(y) \gg true \mid (x \mid \mid y)
```

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Ift(x) \gg true \mid Ift(y) \gg true \mid (x \mid \mid y)
```

Parallel or; contd.

Compute the parallel or and return just one value:

```
val x = f

val y = g

val z = Ift(x) \gg true \mid Ift(y) \gg true \mid (x \mid\mid y)
```

But this continues execution of g if f first returns true.

```
val z = val x = f
val y = g
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Parallel or; contd.

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```
val z = val x = f
val y = g
Ift(x) \gg true \mid Ift(y) \gg true \mid (x \mid\mid y)
```

Mutable Store: Some Factory Sites

Ref(n) Mutable reference with initial value n
Array(n) Array of size n of Refs
Semaphore(n) Semaphore with initial value n
Channel() Unbounded (asynchronous) channel
Table(n,f) Array of size n of immutable values of f

$$Ref(3) > r > r.write(5) \gg r.read()$$
, or $Ref(3) > r > r := 5 \gg r$?
 $Array(3) > a > a(0) := true \gg a(1)$?
 $Semaphore(1) > s > s.acquire() \gg Println(0) \gg s.release()$
 $Channel() > ch > (ch.get() \mid ch.put(3) \gg stop)$
 $val \ ch = Table(10, lambda() = Channel())$

Exception Handling

Client calls site server to request service.

The server "may" request authentication information.

```
\begin{array}{l} \textit{def} \ \ \textit{request}(x) = \\ \textit{val} \ \ \textit{exc} = \ \textit{Channel}() \ \ -- \ \text{returns a channel site} \\ \\ \textit{server}(x, \textit{exc}) \\ | \ \textit{exc.get}() \ \ \textit{>r>} \ \textit{exc.put}(\textit{auth}(r)) \ \gg \ \textit{stop} \end{array}
```

Packet Reassembly Using Sequence Numbers

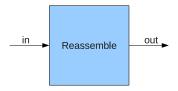


Figure: Packet Reassembler

- Packet with sequence number i is at position p_i in the input channel.
- Given: $|i p_i| \le k$, for some positive integer k.
- Then $p_i \le i + k \le p_{i+2 \times k}$. Let $d = 2 \times k$.

Packet Reassembly Program

```
\begin{array}{ll} \textit{def} \;\; \textit{reassembly}(\textit{read}, \textit{write}, \textit{d}) = & -- \text{d must be positive} \\ \\ \textit{val} \;\; \textit{ch} = \;\; \textit{Table}(\textit{d}, \textit{lambda}(\_) = \textit{Channel}()) \\ \\ \textit{def} \;\; \textit{input}() = \;\; \textit{read}() \;\; > (n, v) > \;\; \textit{ch}(n\%\textit{d}).\textit{put}(v) \;\; \gg \;\; \textit{input}() \\ \\ \textit{def} \;\; \textit{output}(i) = \;\; \textit{ch}(i).\textit{get}() \;\; > v > \;\; \textit{write}(v) \;\; \gg \;\; \textit{output}((i+1)\%\textit{d}) \\ \\ \textit{input}() \;\; | \;\; \textit{output}(0) \qquad -- \;\; \text{Goal expression} \end{array}
```

Note: n%d is $n \mod d$.

Depth-first search of undirected graph Recursion over Mutable Structure

N: Number of nodes in the graph.

conn: conn(i) the list of neighbors of node i, $0 \le i < N$

parent: Mutable array of length N.

parent(i) = v, $v \ge 0$, means v is the parent node of i parent(i) < 0 means parent of i is yet to be determined

Once *i* has a parent, it continues to have that parent.

Start Depth-first search from node 0.

$$parent(0) = N$$



Invariant

dfs(i, xs): starts a depth-first search from all nodes in xs in order, i already has a parent or i = N.

 $xs \subseteq conn(i)$, i.e., xs is some set of neighbors of i.

All neighbors of i not in xs already have parents.

Depth-first search

```
val N = 6 — N is the number of nodes in the graph
val parent = Table(N, lambda(\_) = Ref(-1))
def dfs(\_,[]) = signal
def dfs(i, x : xs) =
  if (parent(x)? > 0) then dfs(i, xs)
  else parent(x) := i \gg dfs(x, conn(x)) \gg dfs(i, xs)
dfs(N, [0])
                   -- start depth-first search from node 0
```

Quicksort

- In situ permutation of an array.
- Array segments are simultaneously sorted.
- Partition of an array segment proceed from left and right simultaneously.
- Combine Concurrency, Recursion, and Mutable Data Structures.

Traditional approaches

- Pure functional programs do not admit in-situ permutation.
- Imperative programs do not highlight concurrency.
- Typical concurrency constructs do not combine well with recursion.

Program Structure

- array *a* to be sorted.
- segmentsort(u, v) sorts the segment a(u)...a(v-1) in place and publishes a signal.
- To sort the whole array: segmentsort(0, a.length?)

Program Structure; Contd.

• part(p, s, t) partitions segment (s, t) with element p. Publishes m where:

```
left subsegment: a(i) \le p for all i, s \le i \le m, and right subsegment: a(i) > p, for all i, m < i < t.
```

• Assume a(s)? $\leq p$, so the left subsegment is non-empty.

```
\begin{array}{l} \textit{def swap}(i,j) = (i?,j?) > & (x,y) > (i:=y,\,j:=x) \gg \textit{signal} \\ \textit{def quicksort}(a) = \\ \textit{def segmentsort}(u,v) = \\ \textit{if } v - u > 1 \textit{ then} \\ \textit{part}(a(u)?,u,v) > m > \\ \textit{swap}(a(u),a(m)) \gg \\ \textit{(segmentsort}(u,m),\textit{segmentsort}(m+1,v)) \gg \textit{signal} \\ \textit{else signal} \\ \textit{segmentsort}(0,a.length?) \end{array}
```

Partition segment (s, t) with element p, given $a(s) \le p$

- *lr*(*i*) publishes the index of the leftmost item in the segment that exceeds *p*; publishes *t* if no such item.
- rl(i) publishes the index of the rightmost item that is less than or equal to p. Since $a(s) \le p$, item exists.

$$\begin{array}{ll} \textit{def} & \textit{lr}(i) = & \textit{lft}(i <: t) \gg \textit{lft}(a(i)? \leq p) \gg \textit{lr}(i+1) \text{ ; } i \\ \\ \textit{def} & \textit{rl}(i) = & \textit{lft}(a(i)? :> p) \gg \textit{rl}(i-1) \text{ ; } i \end{array}$$

Goal Expression of part(p, s, t):

$$(lr(s+1), rl(t-1)) > (s', t') >$$

 $(if (s' < t') then swap(a(s'), a(t')) \gg part(p, s', t')$
 $else t')$

Putting the Pieces together: Quicksort

```
def \ swap(i,j) = (i?,j?) > (x,y) > (i:=y, j:=x) \gg signal
def quicksort(a) =
     def segments ort(u, v) =
       def part(p, s, t) =
          def lr(i) = Ift(i < t) \gg Ift(a(i)? \le p) \gg lr(i+1); i
          def rl(i) = Ift(a(i)? :> p) \gg rl(i-1); i
          (lr(s+1), rl(t-1)) > (s', t') >
          (if (s' < t') then swap(a(s'), a(t')) \gg part(p, s', t')
          else t'
       if v - u > 1 then
         part(a(u)?, u, v) > m >
          swap(a(u), a(m)) \gg
          (segmentsort(u, m), segmentsort(m + 1, v)) \gg signal
       else signal
segmentsort(0, a.length?)
                                               4□ → 4団 → 4 豆 → 4 豆 → 9 へ ○
```

#

#

Class: Pure Rendezvous

```
def class pairSync() =
   val s = Semaphore(0)
   val t = Semaphore(0)

   def put() = s.acquire() >> t.release()
   def get() = s.release() >> t.acquire()
stop
```

Rendezvous with Data Transfer

```
\begin{array}{l} \textit{def} \;\; \textit{class} \; \textit{zeroChannel}() = \\ \textit{val} \;\; s = \; \textit{Semaphore}(0) \\ \textit{val} \;\; w = \; \textit{BoundedChannel}(1) \\ \textit{def} \;\; \textit{put}(x) = \; \textit{s.acquire}() \gg \textit{w.put}(x) \\ \textit{def} \;\; \textit{get}() = \;\; \textit{s.release}() \gg \textit{w.get}() \\ \textit{stop} \end{array}
```

Class: Readers-Writers

- Readers and Writers need access to a shared file.
- Any number of readers may read the file simultaneously.
- A writer needs exclusive access.

Readers-Writers API

- A reader calls *start(true)*, writer *start(false)* to gain access.
- The system (class) returns a signal to grant access.
- Both readers and writers call *end()* on completion of access.
- $start(\cdots)$ is blocking, end() non-blocking.

Implementation Strategy

- Each call to *start* is queued with the id of the caller.
- A *manager* loops forever, maintaining the invariant: There is no active writer (no writer has been granted access). Number of active readers = *na.value*, where *na* is a counter.
- On each iteration, manager picks the next queue entry. If a reader: grant access and increment na.
 If a writer:
 wait until all readers complete (na's value = 0), grant access to writer,
 wait until the writer completes.

Implementation Strategy; Callback

- The id assigned to a caller is a new semaphore.
- A request is (b, s): b boolean, s semaphore.
 b = true for reader, b = false for writer,
 each caller waits on s.acquire()
- The manager grants a request by executing *s.release*()

Reader-Writer; Call API

```
val req = Channel()
val na = Counter()
def startread() =
     val \ s = Semaphore(0)
    req.put((true, s)) \gg s.acquire()
def startwrite() =
     val \ s = Semaphore(0)
    req.put((false, s)) \gg s.acquire()
def endread() = na.dec()
def endwrite() = na.dec()
```

Reader-Writer; Main Loop

```
def \ manager() = grant(req.get()) \gg manager()
def \ grant((true, s)) = na.inc() \gg s.release() -- Reader
def \ grant((false, s)) = -- Writer
na.onZero() \gg na.inc() \gg s.release() \gg na.onZero()
```

Putting the pieces together: Reader-Writer

```
def class readerWriter1() =
    val req = Channel() val na = Counter()
    def startread() = val \ s = Semaphore(0)
    reg.put((true, s)) \gg s.acquire()
    def \ startwrite() = val \ s = Semaphore(0)
    req.put((false, s)) \gg s.acquire()
    def endread() = na.dec()
    def endwrite() = na.dec()
    def grant((true, s)) = na.inc() \gg s.release() -- Reader
    def grant((false, s)) = -- Writer
    na.onZero() \gg na.inc() \gg s.release() \gg na.onZero()
    def manager() = grant(req.get()) \gg manager()
manager()
                                           4 D > 4 A > 4 B > 4 B > B 9 Q C
```

Callback using one semaphore each for Readers and Writers

```
def class readerWriter2() =
    val reg = Channel()
    val na = Counter()
    val(r, w) = (Semaphore(0), Semaphore(0))
    def startread() = req.put(true) \gg r.acquire()
    def startwrite() = req.put(false) \gg w.acquire()
    def endread() = na.dec()
    def endwrite() = na.dec()
    def grant(true) = na.inc() \gg r.release() -- Reader
    def\ grant(false) = -- Writer
       na.onZero() \gg na.inc() \gg w.release() \gg na.onZero()
    def manager() = grant(req.get()) \gg manager()
manager()
```

Reader-Writer; dispense with the queue

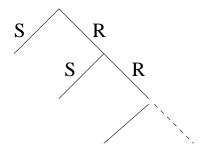
- Dispense with the queue.

 Introduce a class that keeps *nr* and *nw*, counts of readers and writers.
- Calling *put(true/false)* increments the appropriate count.
- Calling *get()* decrements a count and returns *true/false*.
- Simulate fairness for *get*, as in removing from a channel.
 If *nr*? > 0, *nr*? is eventually decremented.
 If *nw*? > 0, *nw*? is eventually decremented.
 Use coin toss to simulate fairness.

Real time: Metronome

External site Rwait(t) returns a signal after t time units. metronome publishes a signal every time unit.

$$\underset{S}{\textit{def}} \ \textit{metronome}() = \underbrace{\underset{S}{\textit{signal}}} \ | \ (\underbrace{\textit{Rwait}(1) \gg \textit{metronome}()}_{\textit{R}})$$



Unending string of Random digits

```
metronome() \gg Random(10) — one every unit def \ rand\_seq(dd) =  — at a specified rate Random(10) \mid Rwait(dd) \gg rand\_seq(dd)
```

A time-based class; Stopwatch

• A stopwatch allows the following operations:

```
start(): (re)starts and publishes a signal
halt(): stops and publishes current value
```

• Other operations: *reset()* and *isrunning()*.

Application: Measure running time of a site

```
def class profile(f) =
  val \ sw = Stopwatch()
  def\ runningtime() = sw.start() \gg f() \gg sw.halt()
  stop
-- Usage
def\ burntime() = Rwait(100)
profile(burntime).runningtime()
```

Response Time Game

- Show a random digit, v, for 3 secs.
- Then print an unending sequence of random digits.
- The user presses a key when he thinks he sees v.
- Output (*true*, *response time*), or (*false*, _) if *v* has not appeared. Then end the game.

Response Game: Program

```
val \ sw = Stopwatch()
val (id, dd) = (3000, 100) — initial delay, digit delay
def rand_seq() = -- Publish a random sequence of digits
  Random(10) \mid Rwait(dd) \gg rand seq()
def\ game() =
  val v = Random(10) -- v is the seed for one game
  val(b, w) =
    Rwait(id) \gg sw.reset() \gg rand\_seq() > x > Println(x) \gg
    Ift(x = v) \gg sw.start() \gg stop
   | Prompt("Press ENTER for SEED"+\nu) \gg
    sw.isrunning() >b> sw.pause() >w> (b,w)
if b then -- Goal expression of game()
  ("Your response time = " + w + " milliseconds.")
else ("You jumped the gun.")
game()
```

Shortest Path Algorithm with Lights and Mirrors

- Source node sends rays of light to each neighbor.
- Edge weight is the time for the ray to traverse the edge.
- When a node receives its first ray, sends rays to all neighbors. Ignores subsequent rays.
- Shortest path length = time for sink to receive its first ray.
 Shortest path length to node *i* = time for *i* to receive its first ray.

Graph structure in *Succ*()

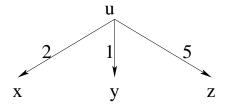


Figure: Graph Structure

Succ(u) publishes (x, 2), (y, 1), (z, 5).

Algorithm

```
def \ eval(u,t) = \ record value \ t \ for \ u \gg  for every successor v with d = length \ of \ (u,v) :  wait for d time units \gg eval(v,t+d) Goal: \ eval(source,0) \mid  read the value recorded for the sink
```

Record path lengths for node u in FIFO channel u.

```
Algorithm(contd.)
```

```
\begin{array}{ll} \textit{def} \ \textit{eval}(u,t) = & \text{record value } t \text{ for } u \gg \\ & \text{for every successor } v \text{ with } d = \text{length of } (u,v) : \\ & \text{wait for } d \text{ time units } \gg \\ & \textit{eval}(v,t+d) \end{array}
```

Goal: eval(source, 0) | read the value recorded for the sink

A cell for each node where the shortest path length is stored.

```
def \ eval(u,t) = \ u := t \gg \\ Succ(u) > (v,d) > \\ Rwait(d) \gg \\ eval(v,t+d)
\{-\ \textit{Goal} :-\} \ eval(source,0) \mid sink?
```

Algorithm(contd.)

```
def \ eval(u,t) = \quad u := t \gg \\ Succ(u) > (v,d) > \\ Rwait(d) \gg \\ eval(v,t+d)
\{- \ \textit{Goal} :-\} \qquad eval(source,0) \mid sink?
```

- Any call to eval(u, t): Length of a path from source to u is t.
- First call to eval(u, t): Length of the shortest path from source to u is t.
- *eval* does not publish.

Drawbacks of this algorithm

- Running time proportional to shortest path length.
- Executions of *Succ*, *put* and *get* should take no time.