A Tool for Simplifying ACL2 Definitions

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In this talk we present a tool for simplifying ACL2 definitions.

- Used in Kestrel MUSE project
- In the spirit of earlier ACL2 Workshop 2003 paper, *A Tool for Simplifying Files of ACL2 Definitions* ...
  ... but the two tools don’t share any code.

**OUTLINE:**
- What the tool does
- How the tool does it
- Some challenges, wrinkles, bells, and whistles

I’ll illustrate with examples.
Feel free to ask questions!
What the tool does

Very simple running example for the first two sections of this talk:

ACL2 !(defun foo (x) (+ 1 1 x))

...  

ACL2 !(simplify-defun foo)

(DEFUN FOO$1 (X)
  (DECLARE (XARGS :NORMALIZE NIL
    :GUARD T
    :VERIFY-GUARDS NIL))
  (+ 2 X))

ACL2 !>
Next we explore the events generated by `simplify-defun`. We will focus mostly on how those events automate a proof that the original and simplified functions are equal.

The next several slides show the following, and I’ll explain them during the talk.

- Bird’s-eye view of it all (not really readable!)
- Outline view, focusing attention on key sub-events
- Some details about key sub-events
BIRD’S-EYE VIEW OF IT ALL

ACL2 !>(show-simplify-defun foo)
(PROGN
  (ENCAPSULATE NIL (SET-INHIBIT-WARNINGS "theory")
  (SET-IGNORE-OK T) (SET-IRRELEVANT-FORMALS-OK T)
  (LOCAL (INSTALL-NOT-NORMALIZED FOO))
  (DEFUN FOO$1 (X)
    (DECLARE (XARGS :NORMALIZE NIL :GUARD T :VERIFY-GUARDS NIL))
    (+ 2 X))
  (LOCAL ; local proof details
    (PROGN
      (DEFCONST *FOO-RUNES* ...)
      (DEFTHM FOO$1-BEFORE-VS-AFTER-0
        (IMPLIES (AND)
          (EQUAL (+ 1 1 X) (+ 2 X)))
        :HINTS ...
        :RULE-CLASSES NIL)
      (ENCAPSULATE (((FOO-COPY *) => *)) ...)
      (DEFTHM FOO-IS-FOO-COPY
        (EQUAL (FOO X) (FOO-COPY X))
        :HINTS (("Goal" :IN-THEORY '(FOO$NOT-NORMALIZED FOO-COPY-DEF))
          :RULE-CLASSES NIL)
      (DEFTHM FOO-BECOMES-FOO$1
        (EQUAL (FOO X) (FOO$1 X))
        :HINTS ...)))
    (DEFTHM FOO-BECOMES-FOO$1
      (EQUAL (FOO X) (FOO$1 X))
      :HINTS ...))
  (TABLE TRANSFORMATION-TABLE ...)
  (VALUE-TRIPLE '(DEFUN FOO$1 (X)
    (DECLARE (XARGS :NORMALIZE NIL :GUARD T :VERIFY-GUARDS NIL))
    (+ 2 X)))
)

ACL2 !>
OUTLINE VIEW

(PROGN
  (ENCAPSULATE NIL
    ... ; Preamble (set-ignore-ok etc.)
    (DEFUN FOO$1 (X) ; Simplified definition
      (DECLARE (XARGS ...))
      (+ 2 X))
    (LOCAL ; Proof of ‘‘BECOMES’’ lemma
      (PROGN ...))
    (DEFFTHM FOO–BECOMES–FOO$1 ; ‘‘BECOMES’’ lemma
      (EQUAL (FOO X) (FOO$1 X))
      (:HINTS ...)); We’ll ignore the rest:
    (TABLE TRANSFORMATION–TABLE
      ... ) ; For database (e.g., redundancy)
    (VALUE–TRIPLE ; Value returned in the loop
      '(DEFUN FOO$1 (X) (DECLARE (XARGS ...)) (+ 2 X))))
PREAMBLE

(SET-INHIBIT-WARNINGS "theory")
(SET-IGNORE-OK T)
(SET-IRRELEVANT-FORMALS-OK T)
(LOCAL (INSTALL-NOT-NORMALIZED FOO))
(DEFUN FOO$1 (X) ; Simplified definition
   (DECLARE (XARGS ...))
   (+ 2 X))
(LOCAL ; Proof of ``BECOMES'' lemma
   (PROGN ...))
(DEFTHM FOO-BECOMES-FOO$1 ; ``BECOMES'' lemma
   (EQUAL (FOO X) (FOO$1 X))
   :HINTS ...)
**Simplified definition**

The expander (books/misc/expander.lisp) provides our interface to the rewriter, to simplify the definition.

... ; Preamble (set-ignore-ok etc.)
(DEFUN FOO$1 (X); Simplified definition
 (DECLARE (XARGS :NORMALIZE NIL
 :GUARD T
 :VERIFY-GUARDS NIL))

(+ 2 X))
(LOCAL ; Proof of ``` ``BECOMES'' ``` lemma
 (PROGN ...))
(DEFTHM FOO-BECOMES-FOO$1; ``` ``BECOMES'' ``` lemma
 (EQUAL (FOO X) (FOO$1 X))
 :HINTS ...)


"BECOMES" LEMMA

... ; Preamble (set-ignore-ok etc.)
(DEFUN FOO$1 (X) ; Simplified definition
  (DECLARE (XARGS ...))
  (+ 2 X))
(LOCAL ; Proof of "BECOMES" lemma
  (PROGN <proof_of_becomes-lemma>))
(DEFTHM FOO-BECOMES-FOO$1 ; redundant
  (EQUAL (FOO X) (FOO$1 X))
  :HINTS ...))

Let’s look at <proof_of_becomes-lemma>.
Proof of “Becomes” lemma (1): Overview

(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
  (IMPLIES (AND)
    (EQUAL (+ 1 1 X) (+ 2 X)))
  :HINTS ... :RULE-CLASSES NIL)
(ENCAPSULATE (((FOO-COPY *) => *)
  (LOCAL (DEFUN FOO-COPY (X)
    (DECLARE (XARGS :NORMALIZE NIL))
    (FOO X)))
  (DEFTHM FOO-COPY-DEF
    (EQUAL (FOO-COPY X)
      (BINARY+- 1 (BINARY+- 1 X)))
    :HINTS ... :RULE-CLASSES ...))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X))
  :HINTS ... :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
  :HINTS ... )
Proof of “Becomes” lemma (2)

(defconst *foo-runes*
  ’((:rewrite fold-consts-in-+)
    (:executable-counterpart binary+-)
    (:definition synp)))
(deftthm foo$1-befor- vs-after-0 ...)
(encapsulate ((foo-copy *) => *)
  (local ...)
  (deftthm foo-copy-def ...))
(deftthm foo-is-foo-copy
  (equal (foo x) (foo-copy x))
  :hints ... :rule-classes nil)
(deftthm foo-becomes-foo$1
  (equal (foo x) (foo$1 x))
  :hints ...)

roof of "becomes" lemma (2)
Proof of "Becomes" Lemma (3)

(DEFCNST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
  (IMPLIES (AND)
    (EQUAL (+ 1 1 X) (+ 2 X)))
  :HINTS
    ("Goal":IN-THEORY *FOO-RUNES*:EXPAND NIL))
  :RULE-CLASSES NIL)
(ENCAPSULATE (((FOO-COPY *) => *)
  (LOCAL ...)
    (DEFTHM FOO-COPY-DEF ...)))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X))
  :HINTS ... :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
  :HINTS ...)


PROOF OF "BECOMES" LEMMA (4)

(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
  ... (EQUAL (+ 1 1 X) (+ 2 X)) ...)
(ENCAPSULATE ((FOO-COPY *) => *)
  (LOCAL (DEFUN FOO-COPY (X)
    (DECLARE (XARGS :NORMALIZE NIL))
    (FOO X)))
  (DEFTHM FOO-COPY-DEF
    (EQUAL (FOO-COPY X)
      (BINARY+- '1 (BINARY+- '1 X)))
    :HINTS ("Goal"
      :IN-THEORY '(:D FOO-COPY)
      :EXPAND ((FOO X)))
    :RULE-CLASSES (:DEFINITION :INSTALL-BODY T)))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X))
  :HINTS ... :RULE-CLASSES NIL)
(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
  :HINTS ...)
Proof of "Becomes" Lemma (5)

(DEFCONST *FOO-RUNES* ...) 
(DEFTHM FOO$1-BEFORE-VS-AFTER-0 
  ... (EQUAL (+ 1 1 X) (+ 2 X)) ...) 
(ENCAPSULATE (((FOO-COPY *) => *) )) 
  (LOCAL (DEFUN FOO-COPY (X) ...)) 
(DEFTHM FOO-COPY-DEF 
  (EQUAL (FOO-COPY X) 
    (BINARY+- '1 (BINARY+- '1 X))) 
  :HINTS ... :RULE-CLASSES ...)) 
(DEFTHM FOO-IS-FOO-COPY 
  (EQUAL (FOO X) (FOO-COPY X)) 
  :HINTS ("Goal" :IN-THEORY 
    '(FOO$NOT-NORMALIZED FOO-COPY-DEF)) 
  :RULE-CLASSES NIL) 
(DEFTHM FOO-BECOMES-FOO$1 
  (EQUAL (FOO X) (FOO$1 X)) 
  :HINTS ... )
Proof of “Becomes” Lemma (6)

(DEFCONST *FOO-RUNES* ...)
(DEFTHM FOO$1-BEFORE-VS-AFTER-0
  ... (EQUAL (+ 1 1 X) (+ 2 X)) ...)
(ENCAPSULATE (( (FOO-COPY *) => *) )
  (LOCAL (DEFUN FOO-COPY (X) ...))
  (DEFTHM FOO-COPY-DEF
    (EQUAL (FOO-COPY X)
      (BINARY++ '1 (BINARY++ '1 X)))) ...))
(DEFTHM FOO-IS-FOO-COPY
  (EQUAL (FOO X) (FOO-COPY X)) ...)

(DEFTHM FOO-BECOMES-FOO$1
  (EQUAL (FOO X) (FOO$1 X))
  :HINTS
  ("Goal" ; Avoid induction in recursive case
    :BY (:FUNCTIONAL-INSTANCE FOO-IS-FOO-COPY
      (FOO-COPY FOO$1))
    :IN-THEORY (THEORY 'MINIMAL-THEORY)
    '(' (:USE (FOO$1-BEFORE-VS-AFTER-0 FOO$1))))
Proof of "Becomes" Lemma (7)

The value of functional instantiation is more clear for a recursive definition. Given

(defun bar (x)
  (if (zp x)
      0
      (+ 1 1 (bar (+ -1 x)))))

— we generate:

(defthm bar-becomes-bar$1
  (equal (bar x) (bar$1 x))
  :hints
  ('("Goal"
      :by (:functional-instance bar-is-bar-copy (bar-copy bar$1))
      :in-theory (theory 'minimal-theory)
      (:use (bar$1-before-vs-after-0 bar$1))))
PROOF OF “BECOMES” LEMMA (8)

The :by hint works, so the proof proceeds as follows.

Goal’ ; bar$1 satisfies the definition of bar-copy
(EQUAL (BAR$1 X)
   (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X))))).

We augment the goal with the hypotheses provided by the :USE hint. These hypotheses can be obtained from BAR$1-BEFORE-VS-AFTER-0 and BAR$1. We are left with the following subgoal.

Goal’’
(IMPLIES
 (AND (IMPLIES ; use bar$1-before-vs-after-0 T
             (EQUAL (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X)))))
                    (IF (ZP X) 0 (+ 2 (BAR$1 (+ -1 X))))))
 (EQUAL (BAR$1 X) ; use bar$1
             (IF (ZP X) 0 (+ 2 (BAR$1 (+ -1 X))))))
 (EQUAL (BAR$1 X)
             (IF (ZP X) 0 (+ 1 1 (BAR$1 (+ -1 X))))).

But we reduce the conjecture to T, by primitive type reasoning.
Some challenges, wrinkles, bells, and whistles

Next we look at a few interesting aspects of `simplify-defun`. We’ll do the following.

- Consider some challenges and how they were overcome.
- Skim the documentation.
- Look at some of the many knobs to turn.

Let’s start by looking at some challenges and their solutions.
New general features developed for MUSE are in **color**.

<table>
<thead>
<tr>
<th>Feature</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>prove termination</td>
<td>appeal to previous function’s <em>unnormialized</em> body (<strong>install-not-normalized</strong>) and <strong>:termination-theorem</strong></td>
</tr>
<tr>
<td>verify guards</td>
<td>appeal to the previous function’s <strong>:guard-theorem</strong></td>
</tr>
<tr>
<td>support assumptions</td>
<td>require a proof that assumptions are preserved on recursive calls</td>
</tr>
<tr>
<td>preserve structure</td>
<td>use <strong>directed-untranslate</strong></td>
</tr>
<tr>
<td>use context</td>
<td>simplify and <em>flatten</em> assumptions and governing <strong>IF tests</strong></td>
</tr>
<tr>
<td>suppress output</td>
<td>turn off warnings; return and print only the new definition</td>
</tr>
<tr>
<td>ease debugging</td>
<td><strong>show-simplify-defun</strong>, <strong>:verbose t</strong></td>
</tr>
<tr>
<td>control</td>
<td>patterns, hints, . . .</td>
</tr>
<tr>
<td>support redundancy</td>
<td>use a table</td>
</tr>
<tr>
<td>automate reasoning</td>
<td>functional instantiation, theories, . . .</td>
</tr>
</tbody>
</table>
Let’s skim the documentation.
Let’s **skim the documentation**.

Now we focus our attention on some of the many knobs to turn.
REUSE FOR GUARDS, MEASURES, AND THEIR PROOFS

ACL2 !>(defun bar (x)
   (declare (xargs :guard (natp x)))
   (if (zp x) 0 (+ 1 1 (bar (+ -1 x)))))

... 

ACL2 !>(simplify-defun bar)
(defun bar$1 (x)
 (declare
  (xargs
   :
   :normalize NIL
   :
   :guard (natp x)
   :
   :measure (acl2-count x)
   :
   :verify-guards T
   :
   :guard-hints
   ("Goal" :use (:guard-theorem bar)))
   :
   :hints
   ("Goal" :use (:termination-theorem bar)))
   (if (zp x) 0 (+ 2 (bar$1 (+ -1 x))))
SIMPLIFYING UNDER ASSUMPTIONS (1)

ACL2 !>(defun f (x)
  (declare (xargs :guard (true-listp x)))
  (if (consp x)
    (f (cdr x))
    x))

ACL2 !>(defun f (x)
  (declare (xargs :guard (true-listp x)))
  (if (consp x)
    (f (cdr x))
    x))

ACL2 !>(simplify-defun f :assumptions :guard)

ACL2 !>(simplify-defun f :assumptions :guard)

ACL2 !>

Note that we get the same result from the following; the use of
:assumptions :guard is just a handy shortcut.

(simplify-defun f :assumptions '((true-listp x)))
Simplifying under assumptions (2)

The generated events are a bit more complicated when the keyword `:assumptions` is provided. For example, in the following we see use of the `:guard-theorem` because `:assumptions :guard` was specified.

```lisp
(DEFUN F-HYPS (X)  
  (TRUE-LISTP X))

(DEFFTHM F-HYPS-PRESERVED-FOR-F  
  (IMPLIES (AND (F-HYPS X) (CONSP X))  
    (F-HYPS (CDR X)))  
  :HINTS ("Goal"  
    :EXPAND ((:FREE (X) (F-HYPS X)))  
    :USE (:GUARD-THEOREM F))  
  :RULE-CLASSES NIL)
```
OBTAINING PRETTY RESULTS

We use

books/kestrel/system/directed-untranslate.lisp:

ACL2 !>(defun f3 (x y)
    (implies (car (cons x x)) (not y)))
...

ACL2 !>(trace$ directed-untranslate)
  ((DIRECTED-UNTRANSLATE))
ACL2 !>(simplify-defun f3)
1> (DIRECTED-UNTRANSLATE (IMPLIES (CAR (CONS X X))
    (IMPLIES (CAR (CONS X X))
      (IF X (IF Y 'NIL 'T) 'T)
      NIL |current-acl2-world|))
<1 (DIRECTED-UNTRANSLATE (IMPLIES X (NOT Y)))
  (DEFUN F3$1 (X Y)
    (DECLARE (XARGS ...))
    (IMPLIES X (NOT Y)))

ACL2 !>
SIMPLIFYING SUBTERMS

ACL2 !>(defun h (x)
  (list (+ 1 1 x)
       (and (integerp x) (+ 2 -2 x))
       (+ 3 -3 x)
       (+ 4 4 x)))
...
ACL2 !>(simplify-defun h
    :simplify-body
    (list @ (and _ @) @ _))
(DEFUN H$1 (X)
  (DECLARE (XARGS ...))
  (LIST (+ 2 X)
       (AND (INTEGERP X) X)
       (IF (ACL2-NUMBERP X) X 0)
       (+ 4 4 X)))
ACL2 !>
Additional options for:

▶ hints, including theory control
▶ specifying the new function name
▶ providing a measure
▶ specifying enable status for resulting events
▶ simplifying the measure and/or guard
▶ controlling guard verification
▶ untranslating in full (instead of using directed-untranslate)

More options may come; demand-driven!
Not discussed here, but analogous: simplify-defun-sk.
CONCLUSION

The `simplify-defun` tool is being used in the Kestrel MUSE project.

Additional enhancements are planned, including support for mutual recursion and for transforming a non-recursive function to a recursive function.

Its implementation (another talk?) may give clues on how to write other tools that manipulate ACL2 events.

I’m hoping that `simplify-defun` will be made publicly available.