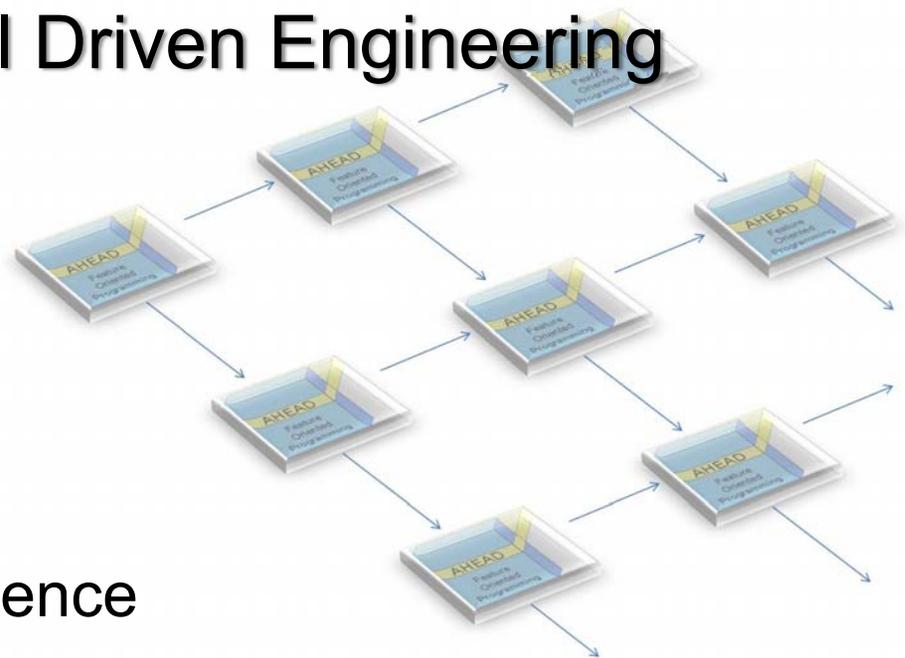


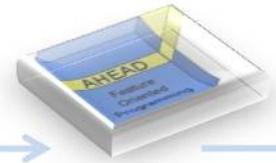
Design by Transformation ($D \times T$)

Principles of Model Driven Engineering



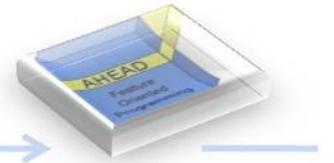
Don Batory
Department of Computer Science
University of Texas at Austin
batory@cs.utexas.edu

Introduction



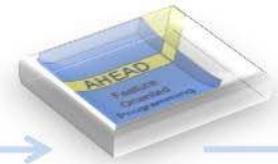
- My research is at intersection of
 - software product-lines (SPLs)
 - program refactoring
 - model driven engineering (MDE)
 - database systems
- I come from world of
 - informal software engineering and design
 - *not* compilers, formal software development, mathematics
- What distinguishes my work
 - start with practice, find a theory that fits practice
 - I use algebra to explain my ideas
 - foundation for more formal theories of automated development

Keys to the Future



- New paradigms will embrace:
 - **Generative Programming (GP)**
 - want software development to be automated
 - **Domain-Specific Languages (DSLs)**
 - not Java & C#, but high-level notations
 - **Automatic Programming (AP)**
 - declarative specs → efficient programs
- Need simultaneous advance in all three fronts to make a significant change

Not Wishful Thinking...

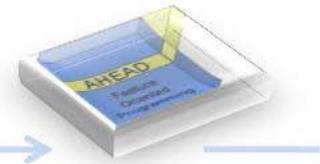


- Example of this futuristic paradigm realized 30 years ago
 - around time when many AI researchers gave up on automatic programming

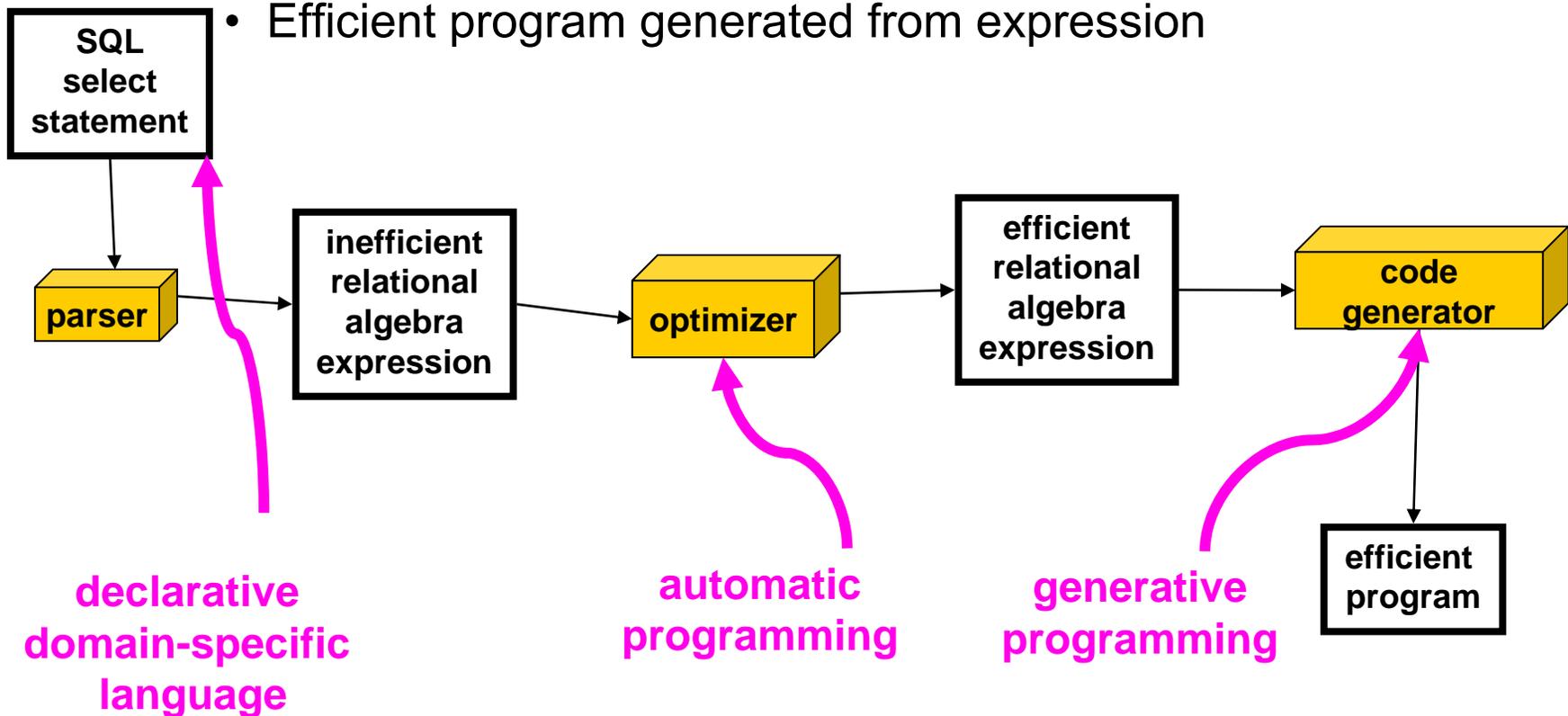
Relational Query Optimization

- The most significant result in automated program design and development, period
- Not mentioned in typical SE texts ...

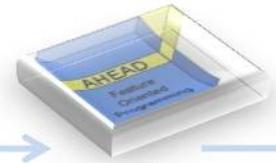
Relational Query Optimization (RQO)



- Declarative query is mapped to an relational algebra expression
- Each expression represents a unique program
- Expression is optimized using algebraic identities
- Efficient program generated from expression

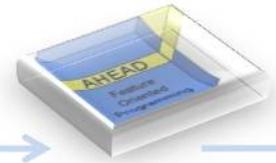


Keys to Success



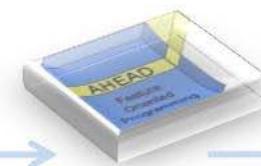
- Automated development of query evaluation programs
 - hard-to-write, hard-to-optimize, hard-to-maintain
 - revolutionized and simplified database usage
- Represented program designs as algebraic **expressions**
 - different expressions represented different programs
 - compositions of relational operations
- Compositionality is hallmark of great engineering
- Use algebraic identities to optimize expressions
 - equates the semantics of different programs

This Tutorial



- Sketch the future:
 - automated software design & maintenance from an algebraic perspective
 - extrapolating 25+ years of experience
 - characteristics of new languages, compilers, tools
- Essential complexity of software structure
 - is exposed when program construction and design is viewed as a computation
 - hides accidental complexity
- **Design by Transformation (D×T)**
 - generalization of RQO paradigm
 - programs are values
 - transformations map programs to programs
 - operators map transformations to transformations
 - **meta-expressions**

Tutorial Overview

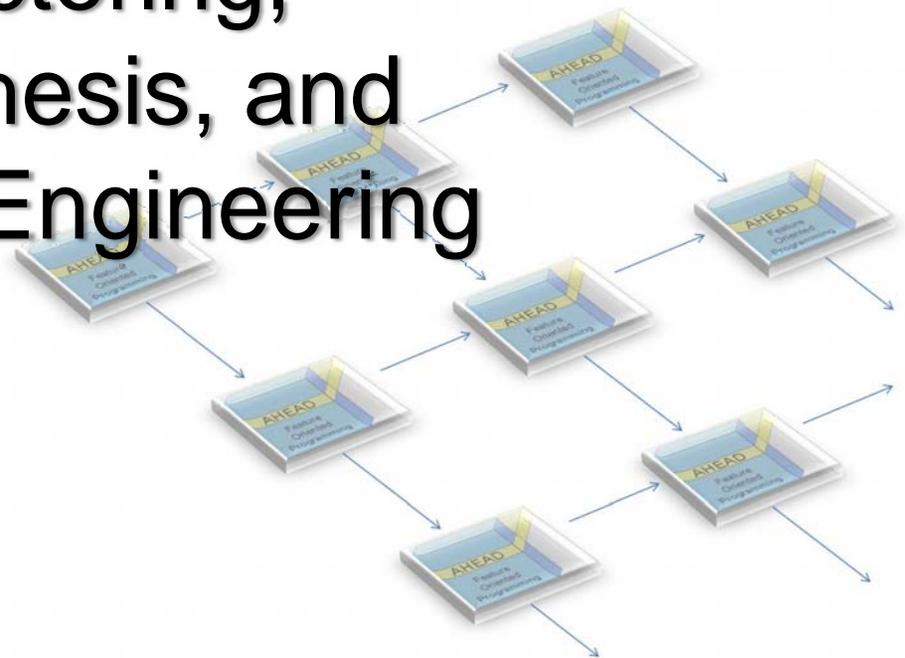


1. Program Refactoring, Program Synthesis, and Model Driven Engineering
algebra underlies program construction
2. Objects and Arrows of $\mathbf{D \times T}$
the relevance of categories and category theory
3. Extraction of MDE Architectures from Parallel Streaming Applications
stepwise development of software architectures by applying domain-specific identities

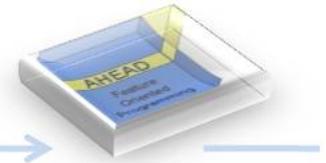
Buckle Up!

Lecture 1:

Program Refactoring, Program Synthesis, and Model Driven Engineering



Upcoming Topics – Four Mini Talks



1. Basics of D×T

2. Program Refactoring

- Dig & Johnson (Illinois)

3. Program Synthesis

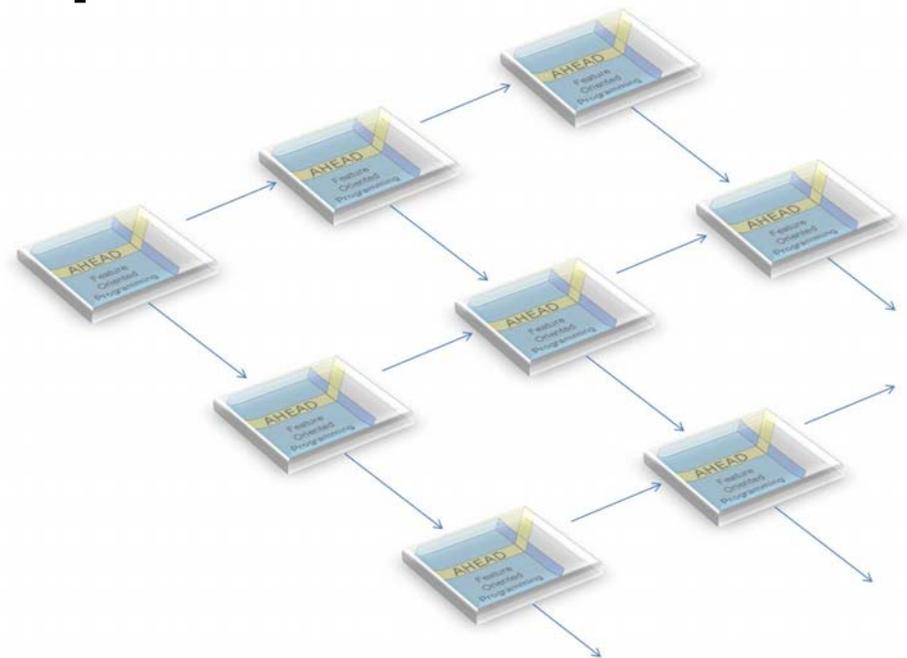
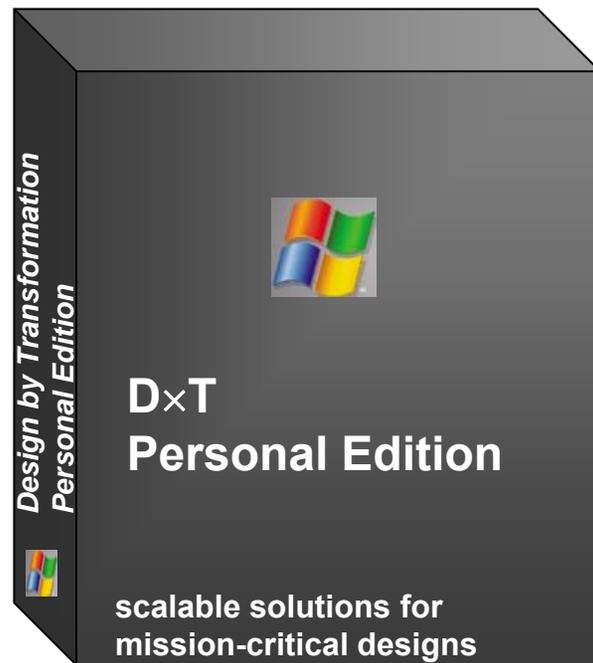
- Lopez-Herrejon (Texas) & Lengauer (Passau)

4. Model Driven Engineering

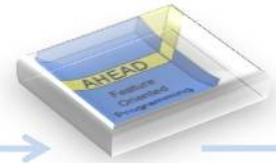
- Trujillo & Diaz (Basque Country)

- All describe systems that have been built
 - step back and give a simple D×T explanation of their results
 - pave way for following lectures

#1: Basics of D×T



D×T



- Programs are **values**

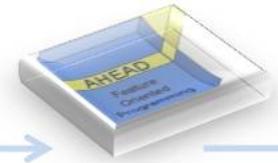
- Here is a value
(Java definition of class C):

```
class C {  
    int x;  
    void inc() {...}  
    ...  
}
```

- Here is another value:

```
class D {  
    void compute()  
    {...}  
    ..  
}
```

1st Operation: + (Sum)



- Let D =

```
class D {  
    void compute()  
    {...}  
}
```

- and C =

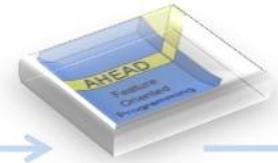
```
class C {  
    int x;  
    void inc() {...}
```

- D + C =

```
class D {  
    void compute()  
    {...}  
}
```

```
class C {  
    int x;  
    void inc() {...}
```

Another Example



- Let C1 =

```
class C {  
    void comp () {...}  
  
}
```

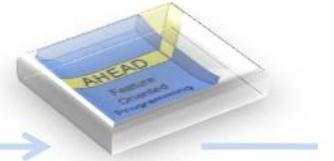
- and C2 =

```
class C {  
  
    int x;  
    void inc() {...}  
  
}
```

- C1 + C2 =

```
class C {  
    void comp () {...}  
    int x;  
    void inc() {...}  
  
}
```

+ (Sum) is Disjoint Union



- Has expected properties:

- 0 is identity (null program)

$$P = 0 + P = P + 0$$

- commutative (because disjoint set union is commutative)

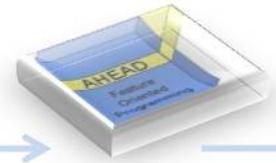
$$A + P = P + A$$

- associative (because disjoint set union is associative)

$$(A + B) + C = A + (B + C)$$

- So what? Why are these properties important?

2nd Operation: – (Subtraction)



- Subtraction is set difference

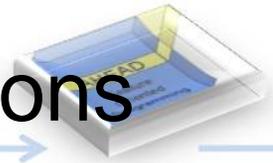
$$(D + C) - C = D$$

- Has expected properties:

- left associative $P - C - D = ((P - C) - D)$
- not commutative $P - C \neq C - P$
- identity $P - 0 = P$

- Again, we need these rules why?

3rd Operation: Distributive Transformations



- **Transformation** is a function that maps a program to another program
- **Rename(p, q, r)** – in program “p” replace name “q” with “r”

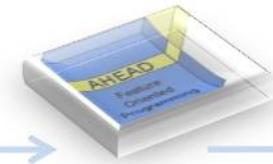
Rename(

```
class C {  
  int x;  
  void inc() {..x..}  
  ...  
}
```

, C.x, C.z) =

```
class C {  
  int z;  
  void inc() {.. z ..}  
  ...  
}
```

Another Example

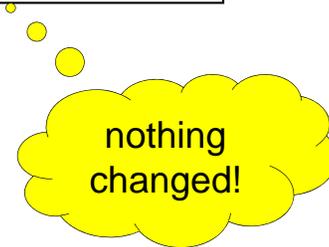


Rename(

```
class D {  
  void compute()  
  {...}  
  ..  
}
```

, C.x, C.z) =

```
class D {  
  void compute()  
  {...}  
  ..  
}
```

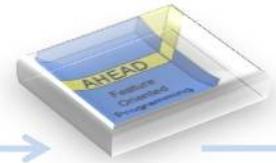


- Called a **fixed point**:

a value x such that $f(x) = x$

- Distributive transformations have lots of fixed points

Key Property (where they get their name)



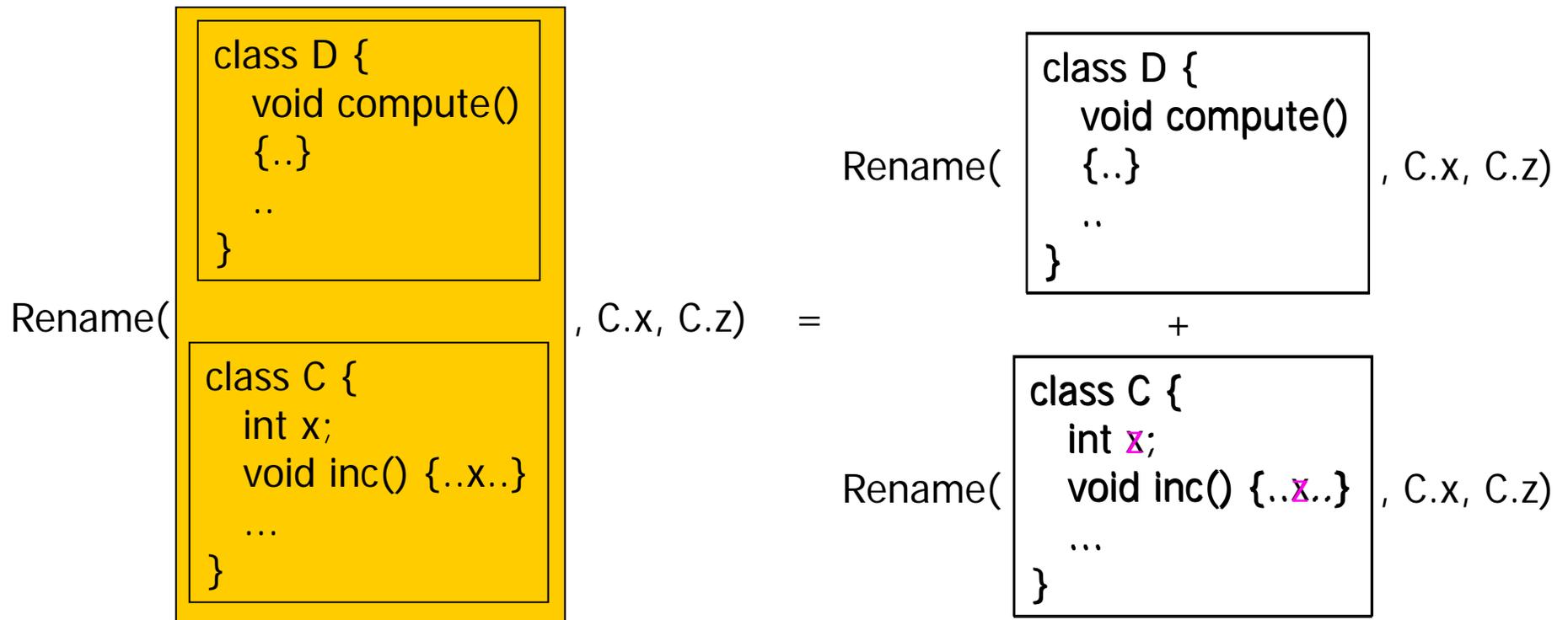
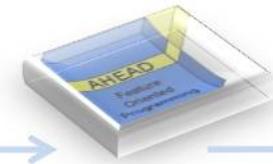
- Transformations **distribute** over + and –

$$f(A + B) = f(A) + f(B)$$

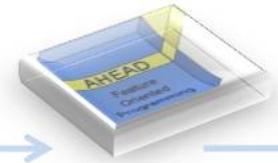
$$f(C - D) = f(C) - f(D)$$

- Here's an example...

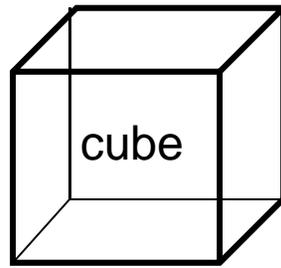
Example of Distributivity



Structures & Properties



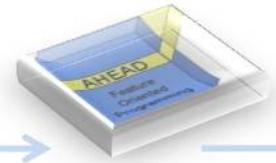
- **Structure** – *what are the parts and how are they connected?*



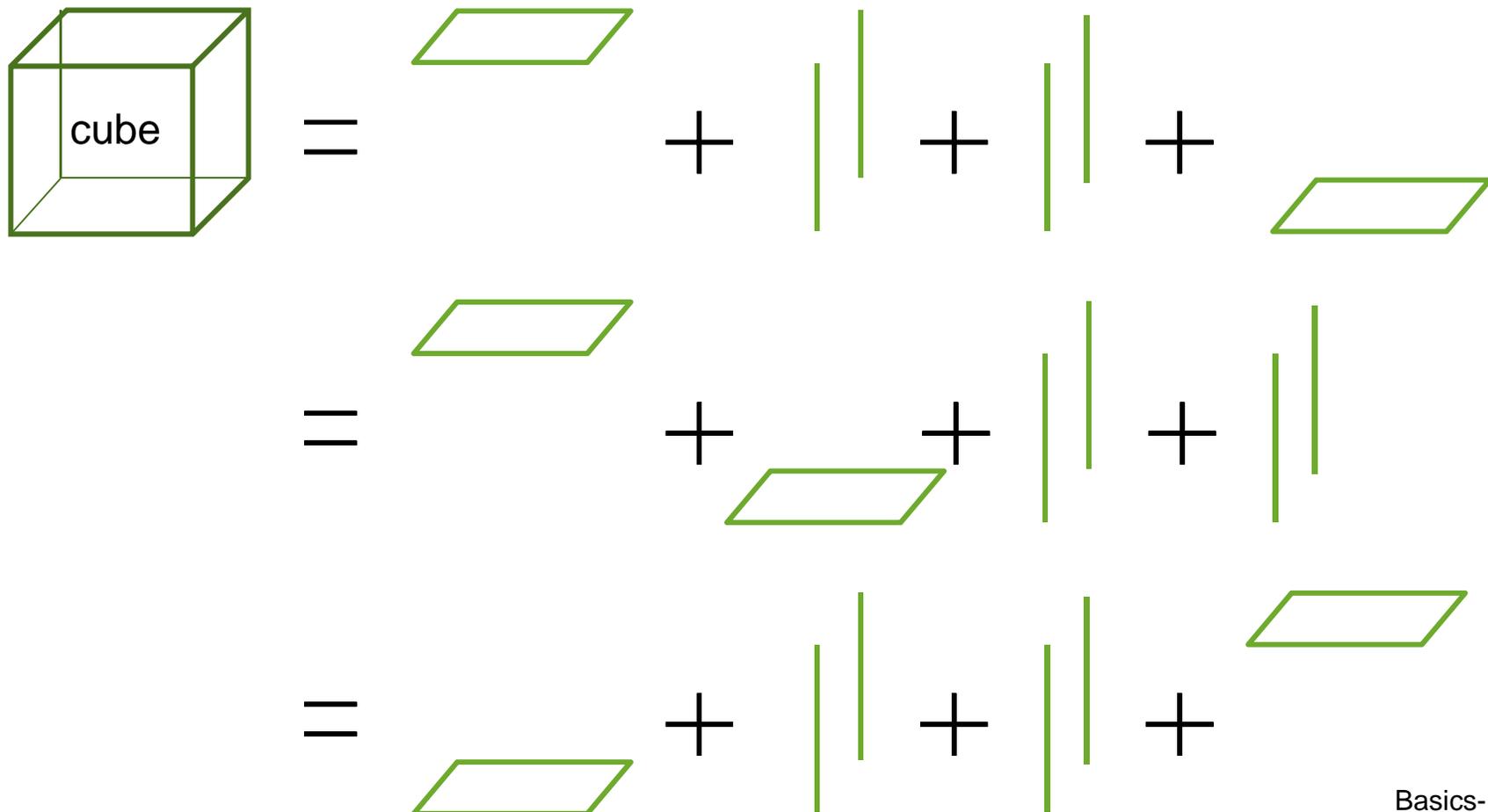
a solid bounded by six equal squares,
the angle between any two adjacent
faces is a right angle.

- **Properties** of structure = *attributes derivable from structure*
 - surface area = $6 \cdot E^2$ // E is edge length
 - volume = E^3

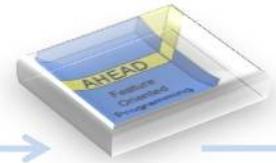
Design



- **Design** is a meta-expression (or more generally a meta-program) that says how to construct a program (structure)

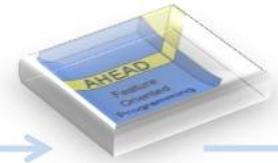


Note!



- Many meta-expressions produce the same program
- This means there are many ways in which a program can be designed and built
- Makes intuitive sense

Properties

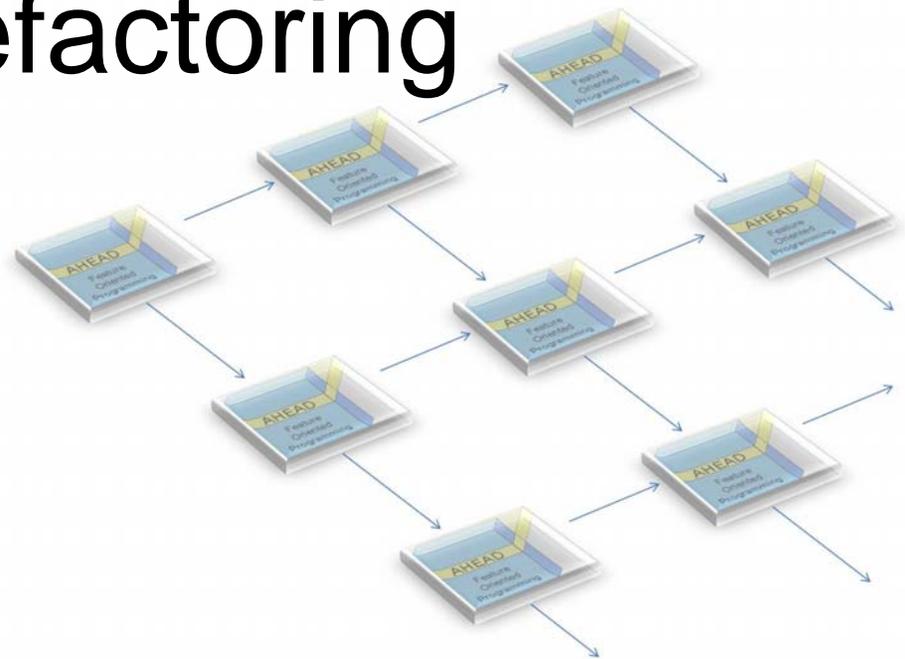


- **Property** of a program – is derived from its structure
 - compilers verify type correctness of programs
(in addition to translating program to bytecodes)
 - other research guarantees other properties (ex. security) of programs – also enforced by special compilers
 - but it is possible to write programs that do not have the properties we want – why we write tests

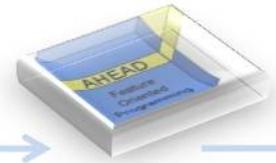
In this lecture,
I focus on program structure.

The above list gives you an idea
of common properties to check.

#2: Advances in Program Refactoring

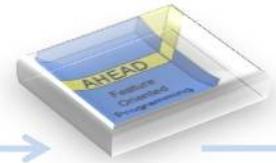


Refactoring



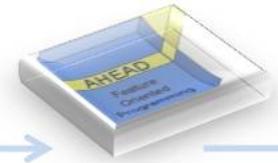
- Is a transformation that changes the structure of a program, **but not the property of its behavior**
 - rename methods
 - move method from subclass to superclass ...
- Most design patterns are end-products of refactorings
 - see Kerievsky, "Refactoring to Patterns" text
- Common IDEs (Eclipse, Visual Studio, IntelliJ) have refactoring tools or plug-ins
- Here's an interesting refactoring problem noticed by Dig and Johnson ~2005
 - resulted in an addition to Eclipse in 2007

Evolution of APIs



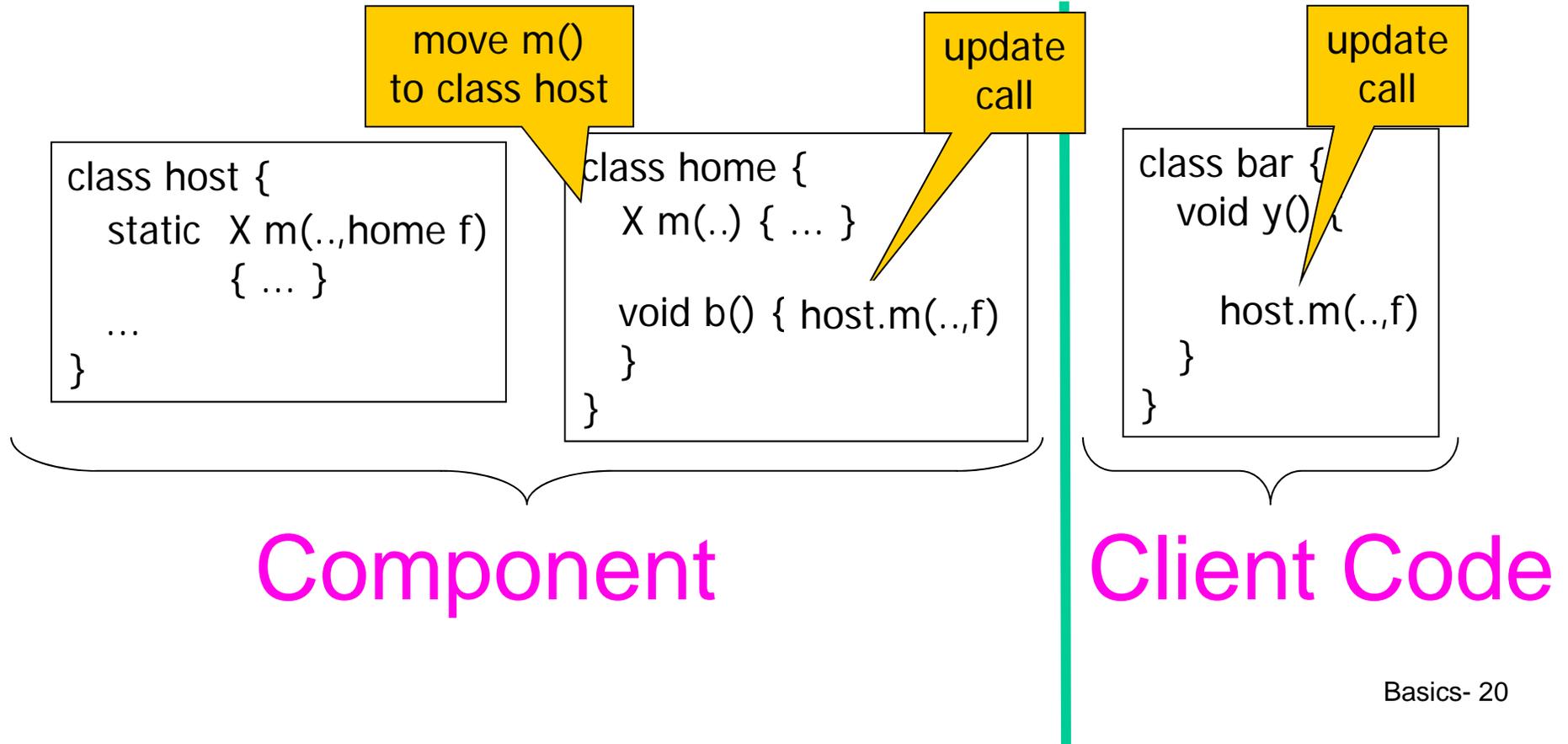
- Use of components (e.g. frameworks, libraries) are common in software development
 - build systems faster and cheaper
- **Application Program Interface (API)** of a component – set of (Java) interfaces and classes that are exported to application developers
 - ideally, APIs don't change, but of course they do!
 - **when APIs change, client code must also change**
 - **very disruptive event in program development**
- Need an easy and safe way to update applications when component's API changes

A Common API Change

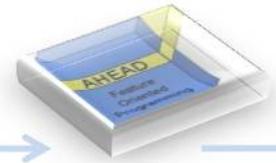


- Move Method

- instance method becomes static method of host class
- moved method takes instance of home class as extra argument
- references to old method replaced with calls to moved method



A Common API Change



Note: although component code changes,
client code must also change.

But a component developer doesn't have the client code!!
User must make changes manually!

```
class host {  
    static X m(...,home f)  
        { ... }  
    ...  
}
```

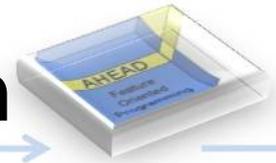
```
class home {  
  
    void b() { host.m(...,f)  
    }  
}
```

```
class bar {  
    void y() {  
        host.m(...,f)  
    }  
}
```

Component

Client Code

Express Change as a Meta-Expression



$$P_{\text{new}} = \rho \bullet \mu \left(P_{\text{old}} \right)$$

move
method

update
calls

```
class host {  
  static X m(...,home f)  
    { ... }  
  ...  
}
```

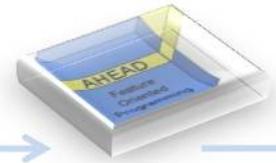
```
class home {  
  X m(..) { ... }  
  
  void b() { host.m(..,f)  
  }  
}
```

```
class bar {  
  void y() {  
  
    host.m(..,f)  
  }  
}
```

Component

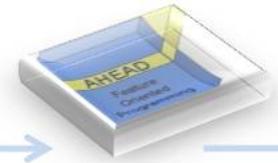
Client Code

Other Common API Changes



- Move Field
- Delete Method
 - usually done after method is renamed or moved
- Change Argument Type
 - ex: replace argument type with its supertype
- Factory Method
 - add a factory method to a class
- Lots of others...
 - preliminary work suggests all can be written as meta-expressions

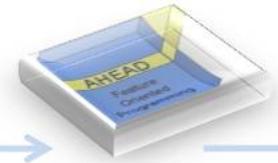
Dig and Johnson Paper



“How do APIs Evolve: A Story of Refactoring”
Jour. Software Maintenance & Evolution:
Research & Practice 2006

- Manually analyzed change logs and documentation of different versions of 5 medium to large systems (50K to 2M LOC)
 - Eclipse, Struts, JHotDraw...
- Found over 80% of API changes are refactorings
 - means LOTS of tedious & error-prone updates can be **automated**
 - explain elegance of their solution using meta-expressions

In the Future



- Programmers will use advanced IDEs that “mark” API classes, methods, fields
 - only way marked elements can change is by refactorings (β)
 - “private” component edits modeled by transformations (e)

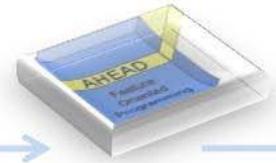
$$\beta_3 \bullet e_3 \bullet e_2 \bullet \beta_2 \bullet \beta_1 \bullet e_1 \left(\begin{array}{c} \text{version} \\ 0 \end{array} \right) = \begin{array}{c} \text{version} \\ 1 \end{array}$$

$$\beta = \beta_3 \bullet \beta_2 \bullet \beta_1$$

transformations to be applied
to update client code w.r.t.
changes in API

- API updates are expressed by β , a projection of changes where “private” edits are removed and only API changes remain

Client Update is a Meta-Function U



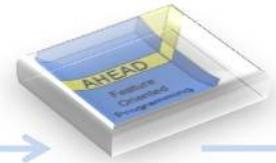
$$U \left(\begin{array}{c} \text{client} \\ \text{program} \end{array} \right) = \beta \left(\begin{array}{c} \text{client} \\ \text{program} \end{array} - \begin{array}{c} \text{version} \\ 0 \end{array} \right) + \begin{array}{c} \text{version} \\ 1 \end{array}$$

$$U \left(\begin{array}{c} \text{client} \\ \text{program} \end{array} \right) = \beta \left(\begin{array}{c} \text{client} \\ \text{code} \end{array} + \begin{array}{c} \text{version} \\ 0 \end{array} - \begin{array}{c} \text{version} \\ 0 \end{array} \right) + \begin{array}{c} \text{version} \\ 1 \end{array}$$

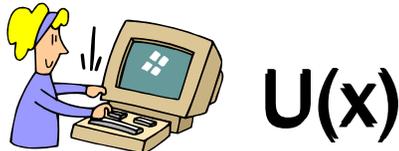
$$= \beta \left(\begin{array}{c} \text{client} \\ \text{code} \end{array} \right) + \begin{array}{c} \text{version} \\ 1 \end{array}$$

**this is not original
presentation of result;
it is a D×T
explanation**

In Eclipse Since 2007



- IDEs create update meta-functions like U to distribute
 - transformations are distributed, not components

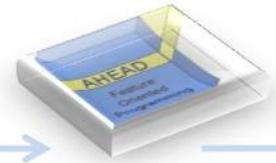


$U(x)$



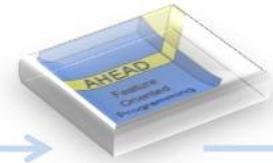
- IDEs transform code bases to automatically update them
- $D \times T$ expresses the core idea elegantly

Background



- Maintaining programs automatically via refactorings is useful
- But we also want to build programs automatically too
- We want simple declarative languages to specify programs
 - that any one could use
 - *not* starting with formal logic specifications
- Ans: **Software Product Lines**
 - **feature** is an increment in product functionality
 - features are a declarative way to specify customized programs

Features used in Engineering



- Dell web pages
 - declarative DSL
 - specify target product by features
- Other examples
 - design your own BMW
 - faucets, sinks

Select Components

1. COMPONENTS 2. SERVICES & SUPPORT 3. ACCESSORIES 4. REVIEW SUMMARY

 **OPTIPLEX 960 MT**
Price: **\$1,198.00**
Preliminary Ship Date: 11/2/2010
[Print Summary](#)

SYSTEM OPTIONS

 **OPTIPLEX 960 MT**
The base selection below will require a matching power supply unit (PSU) in a separate PSU section. For example, a Standard PSU Base will require a Standard PSU and an Up to 90% Efficient Base will require an Up to 90% Efficient PSU.

OptiPlex 960 Minitower Base Standard PSU

- OptiPlex 960 Minitower Base Standard PSU [Included in Price]
- OptiPlex 960 Minitower Base 90 Percent Efficient Power Supply [add \$30.00]

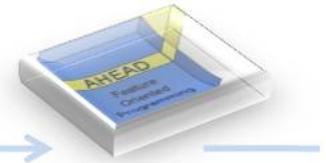
 **Operating System**
Your system does not come with an operating system recovery disk. For an additional cost, you may select a recovery media disk if desired. Operating system options described as "No Media" do not include a recovery media disk. If there is no recovery media disk option here, please go to the system recovery section below.

Genuine Windows® 7 Professional, No Media, 32-bit, English

[Help Me Choose](#)

- Genuine Windows® 7 Home Premium, with Media, 32-bit, English [subtract \$42.00]
- Genuine Windows® 7 Home Premium, No Media, 32-bit, English [subtract \$45.00]
- Genuine Windows® 7 Professional, with Media, 32-bit, English [add \$3.00]
- Genuine Windows® 7 Professional, No Media, 32-bit, English [Included in Price]
- Genuine Windows® 7 Professional, with Media, 64-bit, English [add \$3.00]
- Genuine Windows® 7 Professional, No Media, 64-bit, English add \$0.00
- Genuine Windows® 7 Ultimate, with Media, 32-bit, English [add \$53.00]
- Genuine Windows® 7 Ultimate, No Media, 32-bit, English [add \$50.00]
- Genuine Windows® 7 Professional, w/ XP Mode, Media, 32-bit, English [add \$3.00]
- Genuine Windows® 7 Professional w/XP Mode, No Media, 32-bit, English add \$0.00
- Genuine Windows® 7 Professional, w/ XP Mode, Media, 64-bit, English [add \$3.00]
- Genuine Windows® 7 Professional w/XP Mode, No Media, 64-bit, English add \$0.00
- Genuine Windows® 7 Ultimate with XP Mode, with Media, 32-bit, English [add \$53.00]
- Genuine Windows Vista® Home Basic Service Pack 2, With media, 32 [subtract \$82.00]
- Genuine Windows Vista® Home Basic Service Pack 2, No media, 32 [subtract \$85.00]
- Genuine Windows Vista® Business, SP2, with media, 32 Edition, English [add \$3.00]
- Genuine Windows Vista® Business, SP2, No media, 32 Edition, English add \$0.00
- Genuine Windows Vista® Ultimate, SP2, No media, 32, English [add \$50.00]
- Genuine Windows Vista® Business Service Pack 2, 64-bit, media, English [add \$3.00]
- Genuine Windows Vista® Business Service Pack 2, 64-bit, no media, English add \$0.00
- Genuine Windows® 7 Ultimate, with Media, 64-bit, English [add \$53.00]
- Genuine Windows® 7 Ultimate, No Media, 64-bit, English [add \$50.00]

Declarative Program Specifications



- Graph Product Line

Alg

- Number
- Connected
- StronglyConnected
- Cycle
- MstPrim
- MstKruskal
- Shortest

Search

- DFS
- BFS

Weight

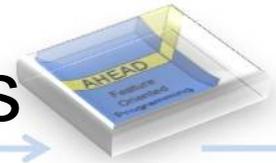
- Weighted
- UnWeighted

GraphType

- Directed
- Undirected

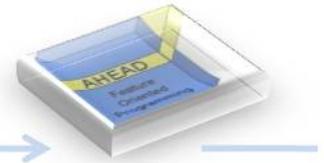
Program = Cycle • Number • DFS • Weighted • Directed

Scalability: Long History of Applications



- 1986 database systems 75K LOC
- 1989 network protocols
- 1993 data structures
- 1994 avionics
- 1997 extensible Java precompilers 35K LOC
- 1998 radio ergonomics
- 2000 program verification tools
- 2001 verified compiler for Java1.0
- 2002 fire support simulators
- 2003 AHEAD tool suite 250K LOC
- 2004 robotics controllers
- 2006 web portlets
- 2008 SGI+JavaScript application
- 2009 ZipMe compression library

Feature Oriented Programming (FOP)



- FOP is an example of $D \times T$:
features are transformations

- Constants (*constant functions or values*)

f – base program with feature f

h – base program with feature h

- Unary Functions (*optional features*)

$i \bullet x$ – adds feature i to program x

$j \bullet x$ – adds feature j to program x

- An FOP “model” of a domain is an algebra

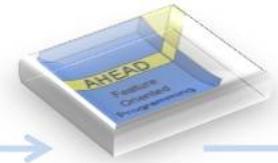
$$M = \{ f, h, \dots i, j, \dots \}$$

- Different meta-expressions represent different programs of a product line

$$P_1 = i \bullet f \quad // P_1 \text{ has } i, f$$

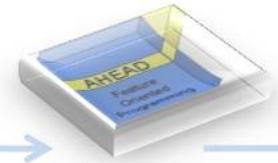
$$P_2 = j \bullet i \bullet h \quad // P_2 \text{ has } j, i, h$$

FOP Implementations



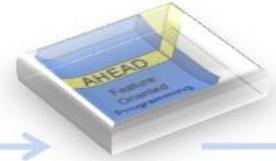
- Use superposition
 - simpler (and more practical) than AOP
 - explore it in more detail in Lecture 2
 - basis for Bracha's most recent language, Newspeak
- If we peer inside FOP features we see familiar ideas popularized by Aspect Oriented Programming (AOP)
 - here I use terminology of AOP, not AOP definitions
 - google "functional aspects"
 - ideas I use appeared long before AOP

Two Ideas



- **Introduction** – adds new members to existing classes
 - metaprogramming addition
- **Advice** – modifies methods at particular points, called **join points**
 - distributive transformation
 - advice is generally behavior-extending, *not* behavior-preserving
- No “subtraction” in AOP or in FOP

Introductions

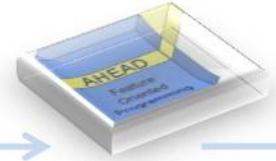


- Incrementally add new members, classes

Program P

```
class C {  
    void foo(){..}  
    int i;  
    String b;  
}  
  
class D {  
    String bar;  
    int cnt(){..}  
}
```

Meta-Expression



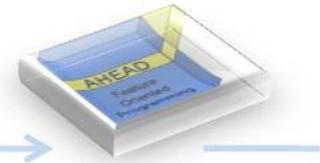
`P = C.b + C.foo + C.i + D.bar + D.cnt`

Program P

```
class C {
    void foo(){..}
    int i;
    String b;
}

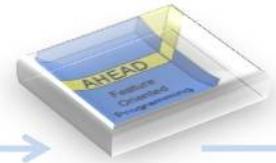
class D {
    String bar;
    int cnt(){..}
}
```

Advice



- Defined in terms of events called **join points**
 - when method is called
 - when method is executed
 - when a field is updated, ...
- **Advice**: when particular join point event occurs, execute a given piece of code
- Although advice has a “dynamic” interpretation, we can give it a “static” metaprogramming interpretation
 - **join point shadows**
 - how aspect compilers work
- View advice as a distributive transformation
 - when you advise a program, you advise all of its parts

Advice

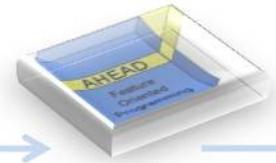


Program P

```
class C {
    int i,j;
    void setI (int x){ i=x; }
    void setJ (int x){ j=x; }
}

after(): execution (void C.set*(..))
{ print("hi"); }
```

Meta-Expression



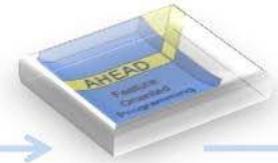
Program P

```
class C {
  int i,j;
  void setI'(int x){ i=x; }
  void setJ'(int x){ j=x; }
}

after(): execution (void C.set*(..))
{ print("hi"); }
```

$$\begin{aligned} P &= hi(C.i + C.j + C.setI + C.setJ) \\ &= hi(C.i) + hi(C.j) + hi(C.setI) + hi(C.setJ) \\ &= C.i + C.j + hi(C.setI) + hi(C.setJ) \\ &= C.i + C.j + C.setI' + C.setJ' \end{aligned}$$

Features



- Features are transformations that:
 - introduce new terms (i)
 - advise or alter (α) existing program (x)

$$F(\mathbf{x}) = \mathbf{i}_f + \alpha_f(\mathbf{x})$$

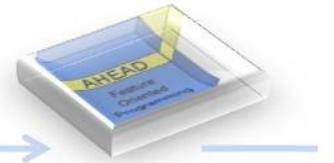
adds new terms

alters existing terms to integrate new functionality

- Composition:

$$G(F(B)) = \mathbf{i}_g + \alpha_g(\mathbf{i}_f + \alpha_f(b))$$

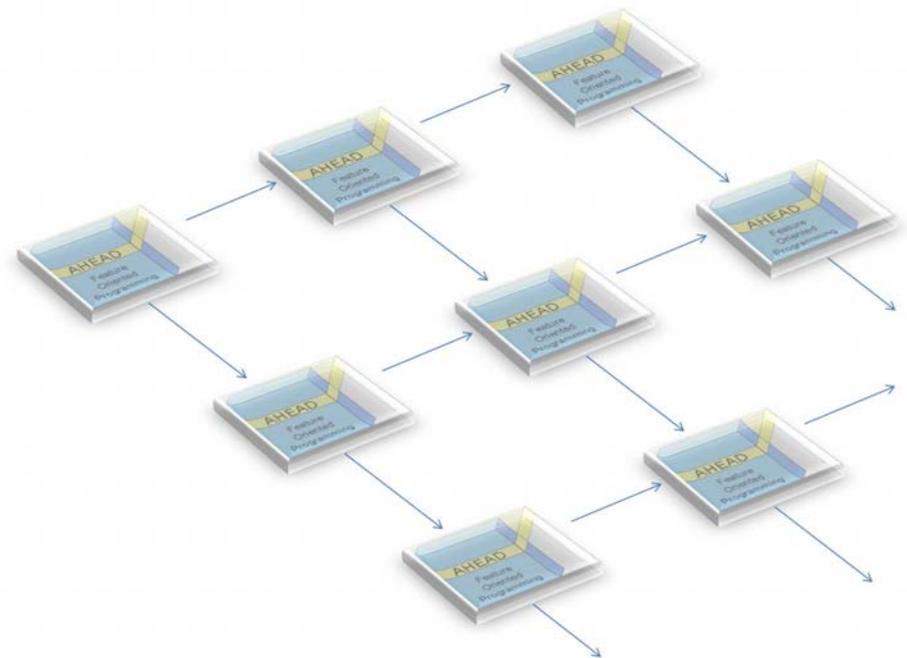
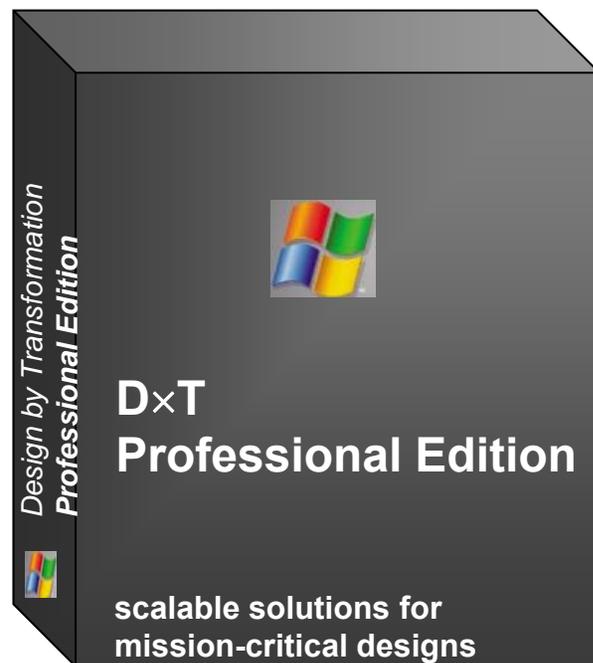
In the Future



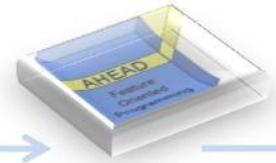
- Program designs will be calculations
- Compilers will be **program calculators**
 - inhale source code
 - generate meta-expression, maybe optimize expression
 - evaluate to synthesize program
- $D \times T$ expresses the core idea elegantly
 - google "AHEAD", "FeatureHouse"
- 3rd Lecture...

An Interesting Question:

What is the Relationship Between Advice and Refactorings?

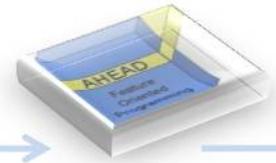


Big Picture



- Refactorings and advice are both transformations
- Suppose we have a refactoring and advice to apply to a program. What does it mean to compose them?
- Note: Advice *does not* modify a refactoring
 - a refactoring is not a language construct;
there are no join points in a refactoring
- Note: But a refactoring *can* modify programs with advice

Example



change method names

Program P

Rename(

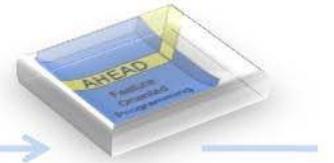
```
class C {  
    int i,j;  
    void SETI (int x){ i=x; }  
    void SETJ (int x){ j=x; }  
}
```

, C.set*, C.SET*)

```
after(): execution (void C.SET* (...))  
    { print("hi"); }
```

change advice declaration

D×T



- Remember differential operators in calculus?

transform expressions

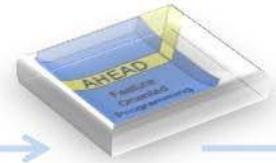
$$\frac{\partial(\mathbf{a}+\mathbf{b}+\mathbf{c})}{\partial\mathbf{y}} = \frac{\partial\mathbf{a}}{\partial\mathbf{y}} + \frac{\partial\mathbf{b}}{\partial\mathbf{y}} + \frac{\partial\mathbf{c}}{\partial\mathbf{y}}$$

each term is transformed

- Rename refactoring is similar – it transforms each term of a meta expression

$$\beta(\mathbf{i} + \mathbf{a}(\mathbf{x})) = \beta(\mathbf{i}) + \beta(\mathbf{a})(\beta(\mathbf{x}))$$

Homomorphisms

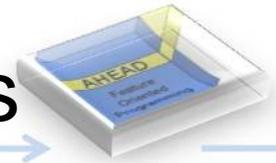


- Operators (expr to expr maps) is an example of:

Homomorphism

- mapping of expressions of one algebra to expressions of another
- Grounded in **Category Theory**
 - theory of mathematical structures and their relationships
 - more later...

How Meta-Calculation Proceeds



Program P

Rename(

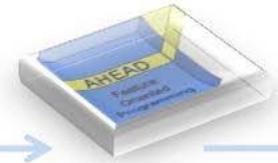
```
class C {
  int i,j;
  void SETI (int x){ i=x; }
  void SETJ (int x){ j=x; }
}

after(): execution (void C.SET* (...))
{ print("hi"); }
```

, C.set*, C.SET*)

$$\begin{aligned}
 & \beta(\text{hi} (\text{C.i} + \text{C.j} + \text{C.setI} + \text{C.setJ})) \\
 = & \beta(\text{hi}) (\beta(\text{C.i}) + \beta(\text{C.j}) + \beta(\text{C.setI}) + \beta(\text{C.setJ})) \\
 = & \beta(\text{hi}) (\text{C.i} + \text{C.j} + \beta(\text{C.setI}) + \beta(\text{C.setJ})) \\
 = & \beta(\text{hi}) (\text{C.i} + \text{C.j} + \text{C.SETI} + \text{C.SETJ}) \\
 = & \text{HI} (\text{C.i} + \text{C.j} + \text{C.SETI} + \text{C.SETJ})
 \end{aligned}$$

Recap



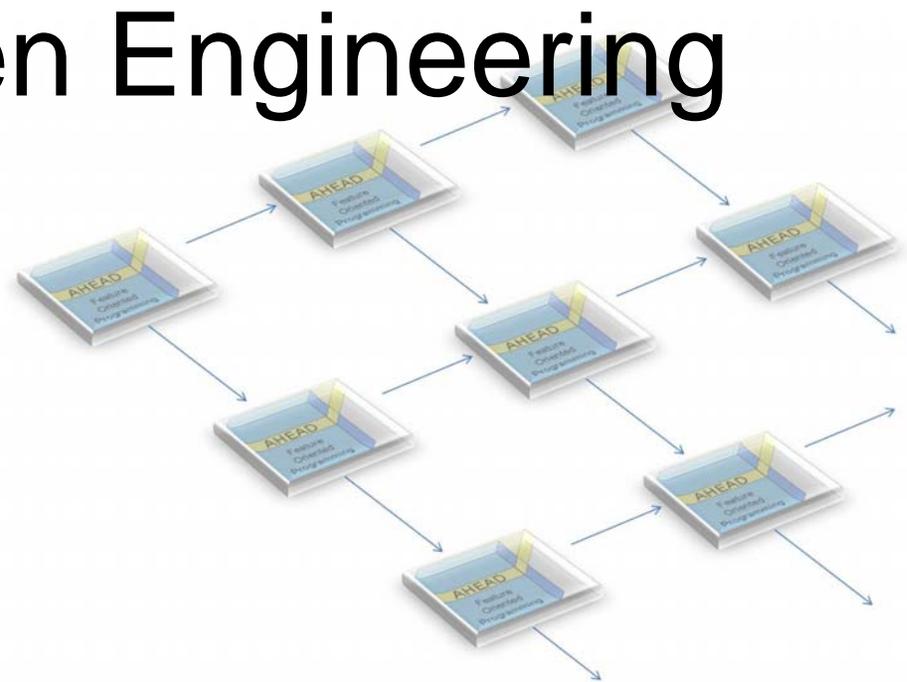
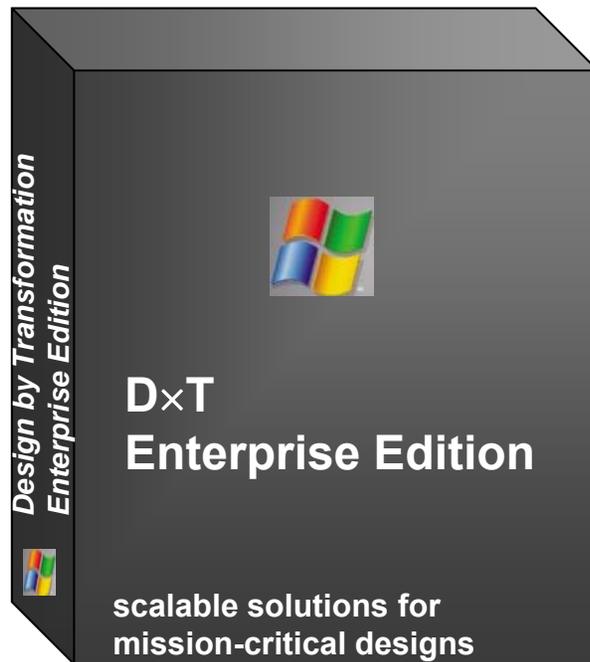
- Refactorings are *operators* on expressions that have higher-precedence than advice in $D \times T$
 - **operator** maps a transformation to another transformation
- Note:
 - refactorings
 - advice
 - introductions

 - modify **structure** of code

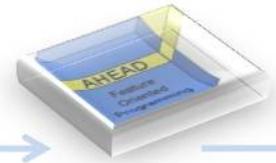
 - but could also modify **structure** of grammars, makefiles, xml documents... as well
- Algebraic viewpoint is universal – it applies to non-code representations as well

leads to our next topic...

#4: Advances in Model Driven Engineering

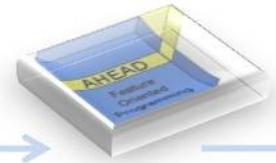


Introduction



- **Model Driven Engineering (MDE)** is a paradigm for software creation
 - uses **domain-specific languages (DSL)**
 - encourages automation
 - exploits data exchange standards
- Model is written in a DSL
 - captures particular details of program's design
 - several models are needed to specify a program
 - **models can be derived from other models by transformations**
 - program synthesis is transforming high-level models into executables (which are also models)

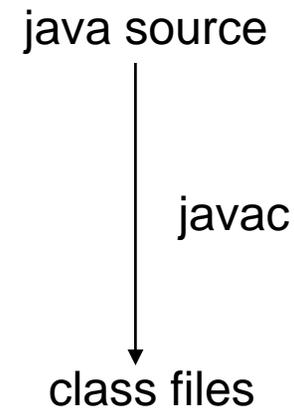
Metaprogramming Connection



- MDE embraces concept that program development is a **computation**

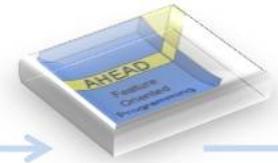
- **claim**: MDE is a metaprogramming & D×T paradigm
- models are values
- transformations map models to models

- Common example

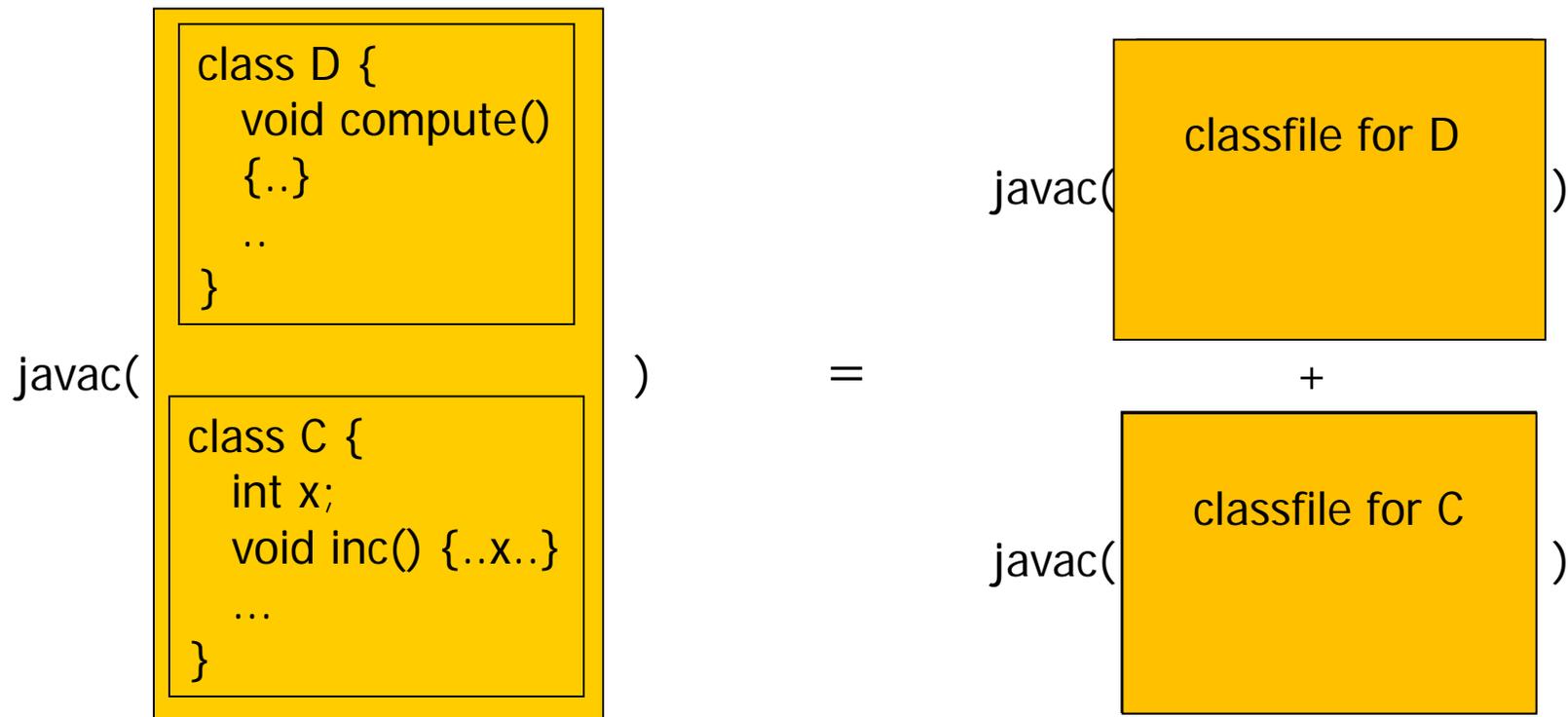


**javac transforms
java source to
class files**

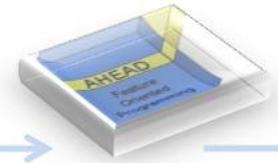
Interesting Question



- If javac is a transformation, is it distributive?



Interesting Question



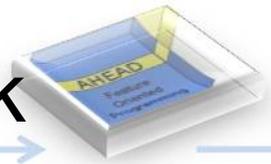
javac is not distributive!

Although there is research by Ancona et. al. on

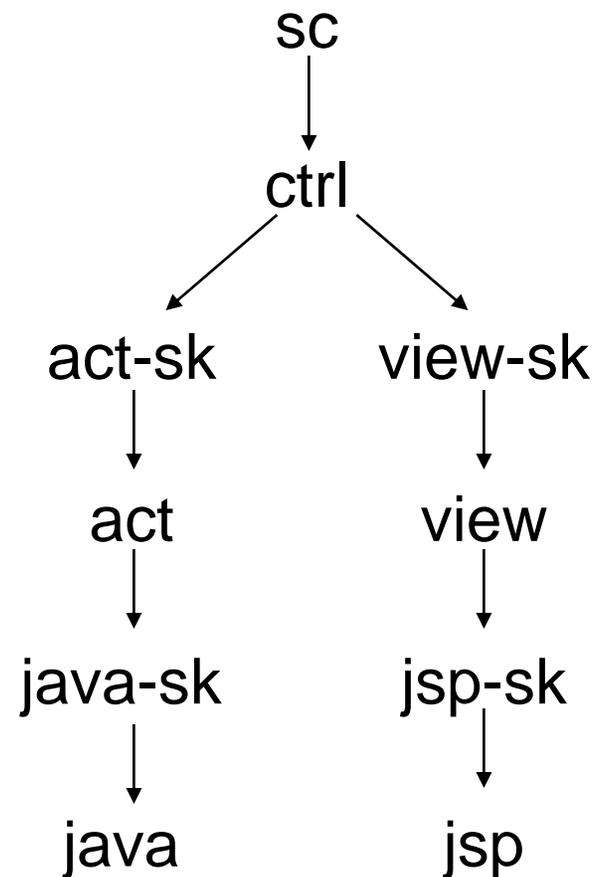
Separate Class Compilation

that makes it so...

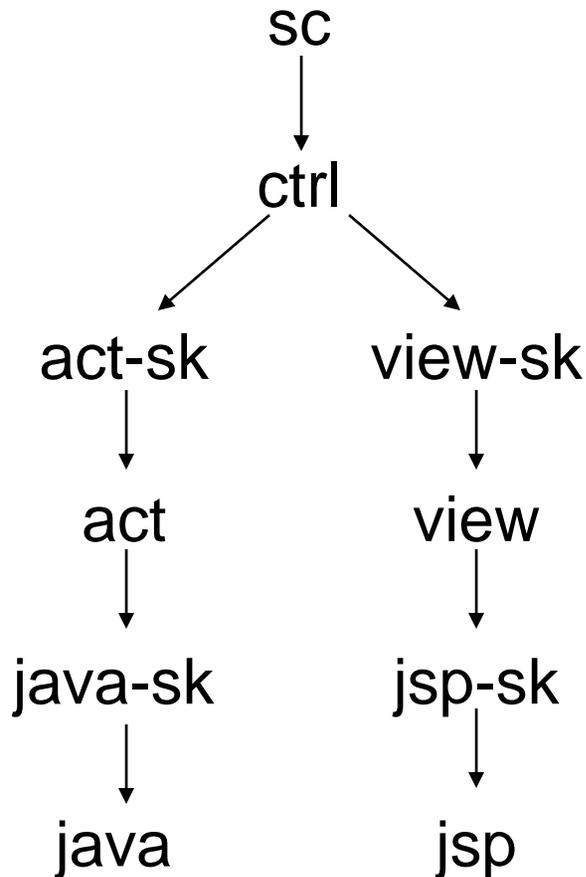
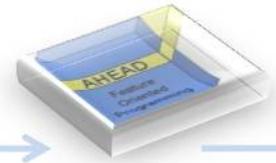
More Typical MDE Example: PinkCreek



- Work with S. Trujillo and O. Diaz
- Portlet is a web component
- PinkCreek is an MDE case study for synthesizing portlets
- Uses transformations to map an annotated state chart (sc) to different representations (Java code, JSP code)



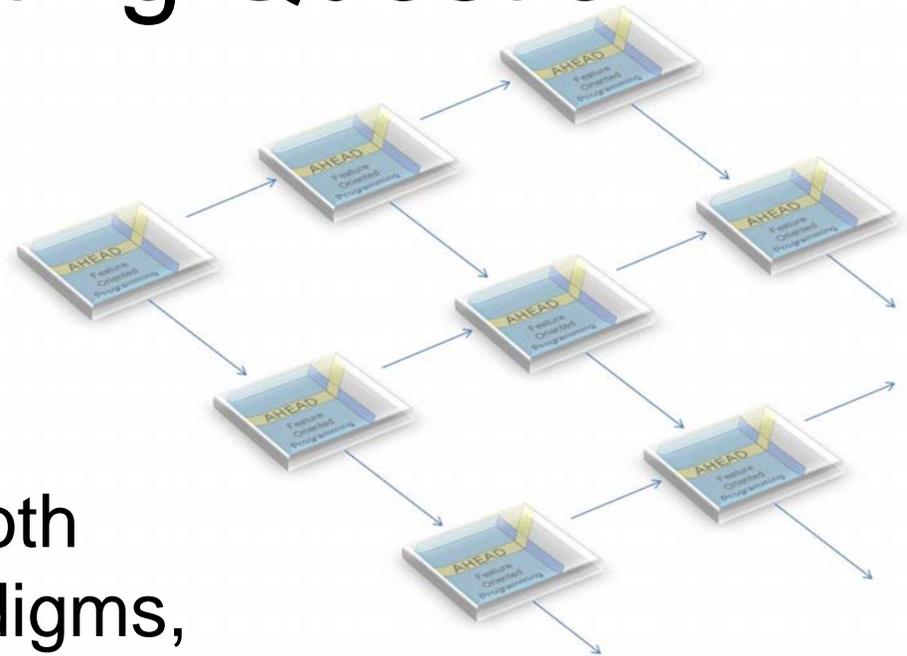
Portlet Synthesis Metaprogram



```
TmkLaw(SC, ΔPSLact-usr, ΔPSLview-usr, ΔJakusr, ΔJspusr) {  
  PSLctrl = Tsc2ctrl (SC);  
  PSLact-sk = Tctrl2act (PSLctrl);  
  PSLact = ΔPSLact-usr • PSLact-sk;  
  PSLview-sk = Tctrl2view (PSLctrl);  
  PSLview = ΔPSLview-usr • PSLview-sk;  
  Jaksk = Tact2jak (PSLact);  
  Jakcode = ΔJakusr • Jaksk;  
  Jspsk = Tview2jsp (PSLview);  
  Jspcode = ΔJspusr • Jspsk;  
  Praw = { PSLctrl, PSLact, PSLview, Jakcode, Jspcode };  
  return Praw;  
}
```

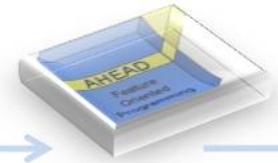
Example of using transformations to derive different models or representations of a program

Another Interesting Question...

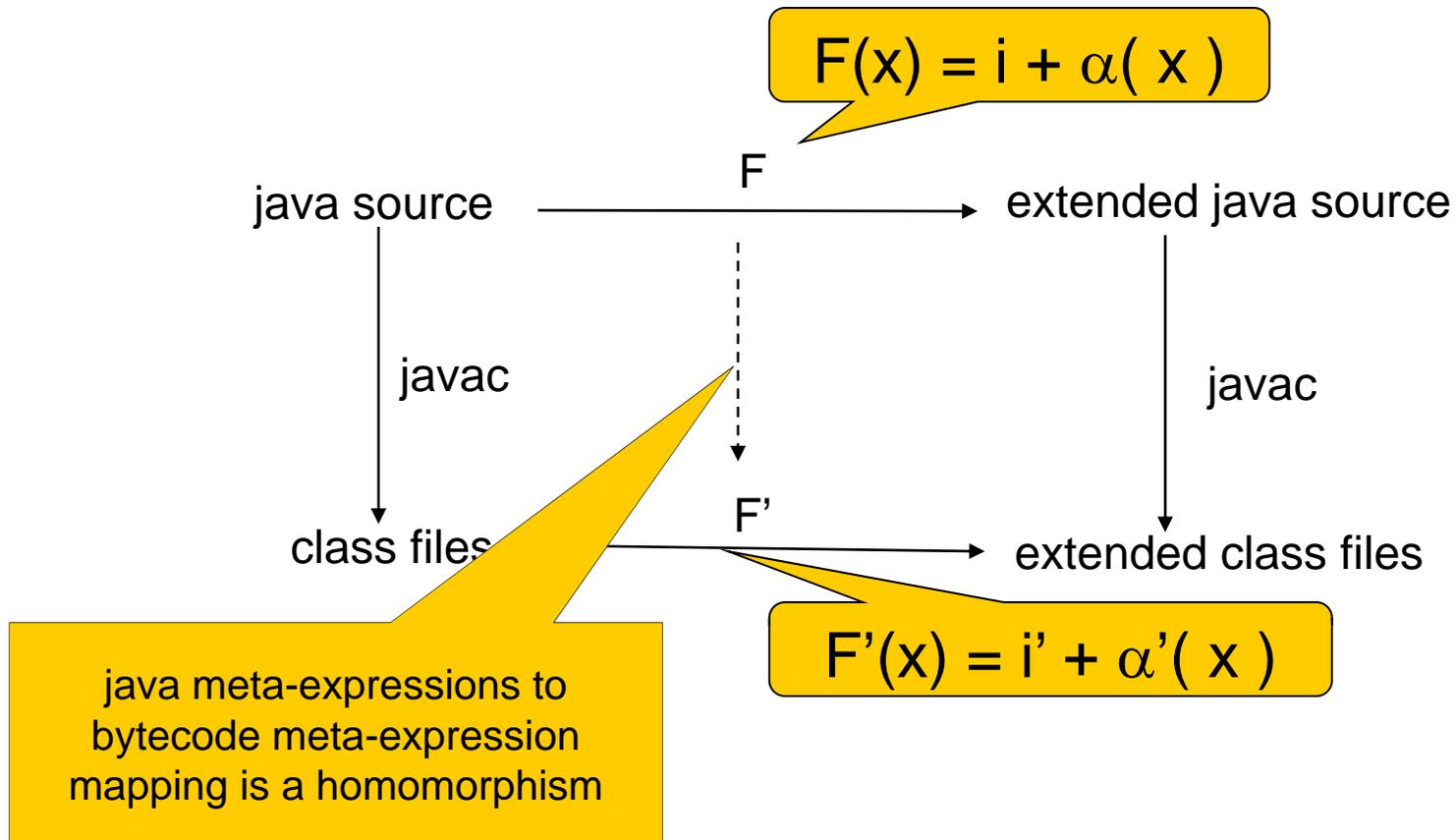


As FOP and MDE are both metaprogramming paradigms, how do they combine?

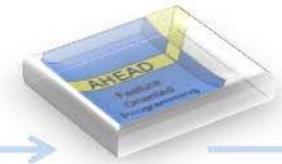
Now and in the Future



- Features “extend” models
- An example:

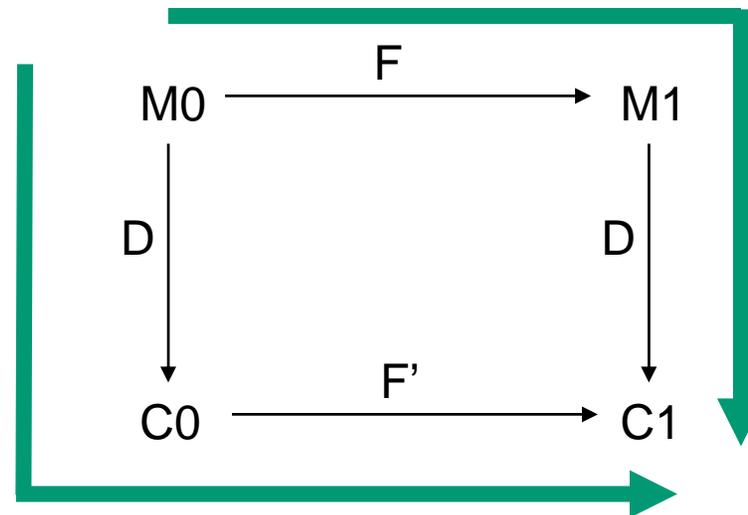


Fundamental Relationship



- Relationship between transformations that derive models from those that extend models

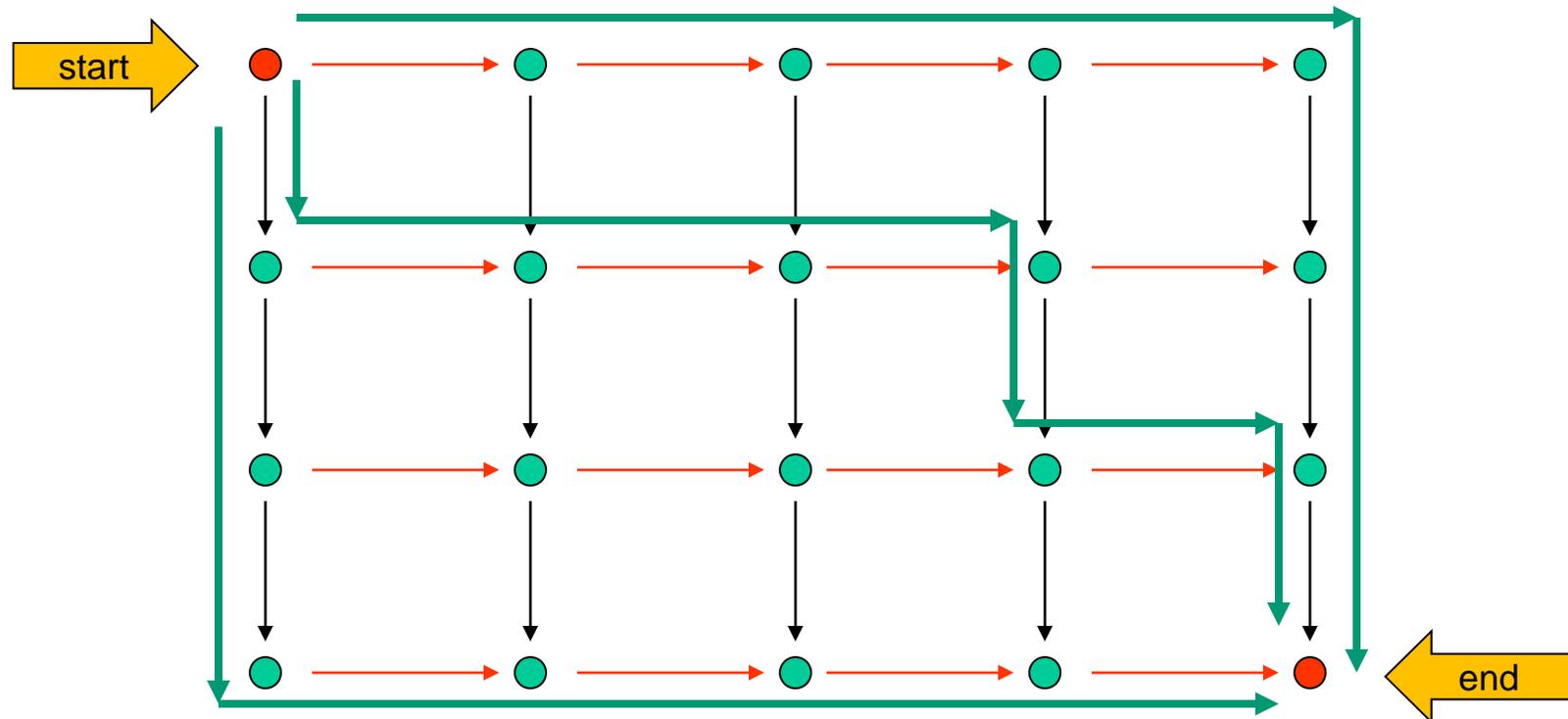
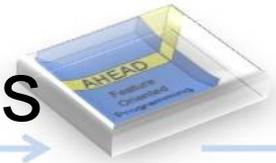
Pushout



$$D \bullet F = F' \bullet D$$

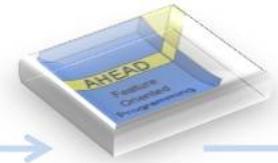
Commuting
Diagram

Property of Commuting Diagrams

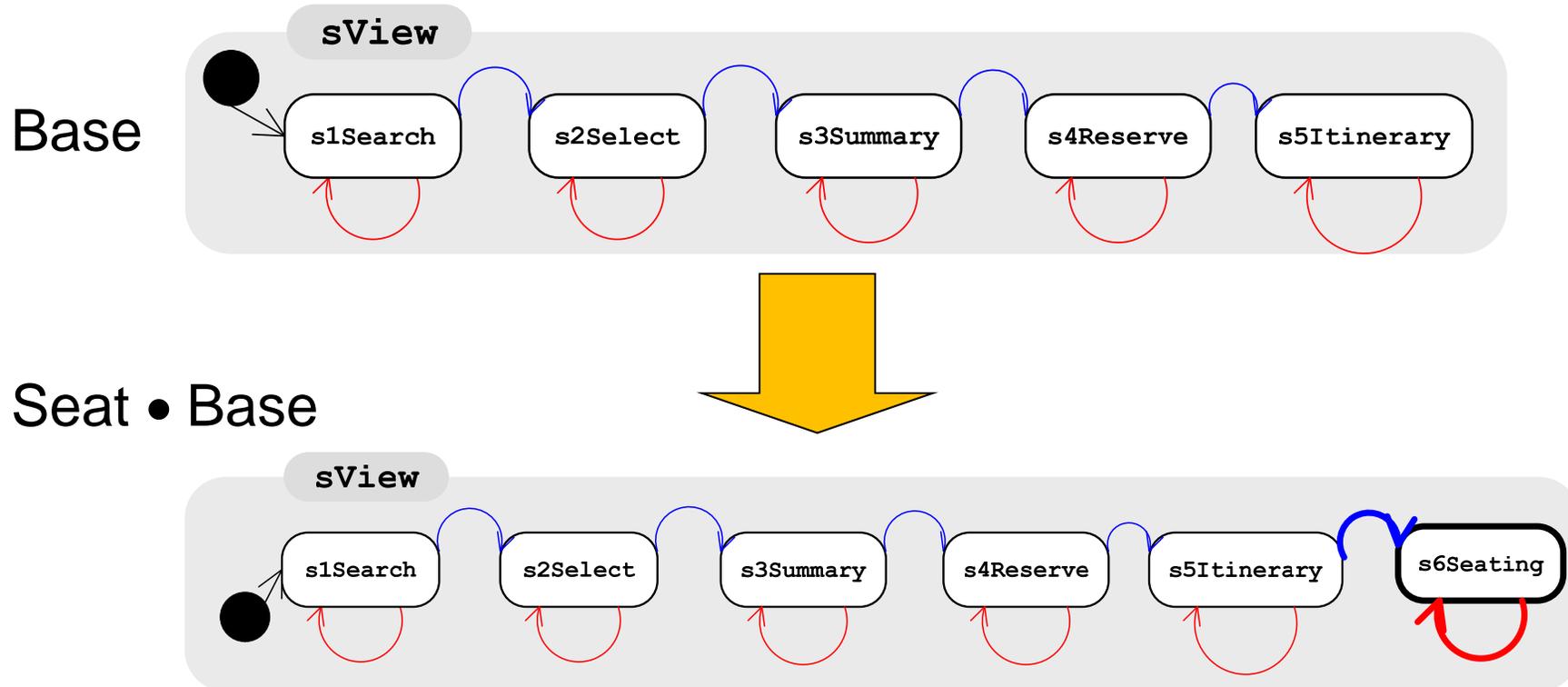


- Diagrams can be “pasted” together
- Given model in upper left, want to compute model in lower right
- Each path represents a different metaprogram
- Every path from upper left to lower right produces same result

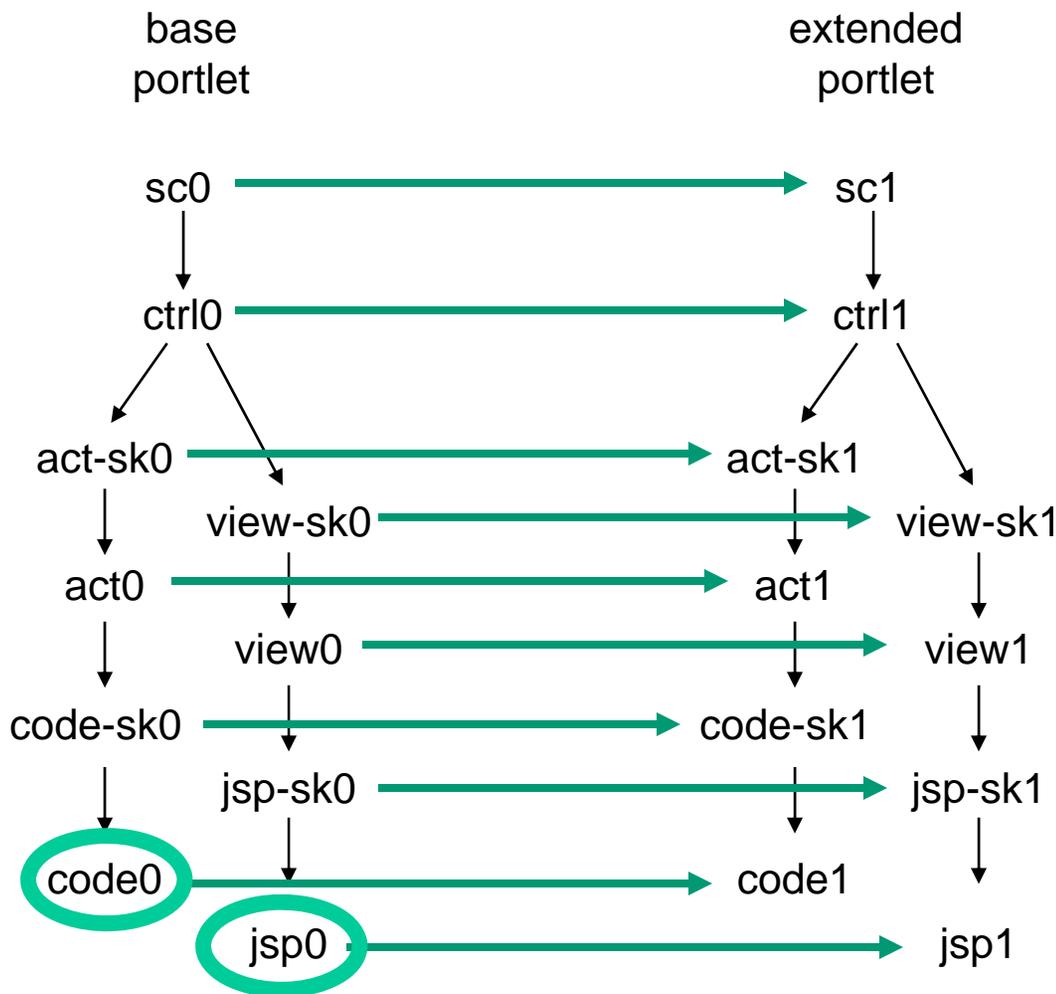
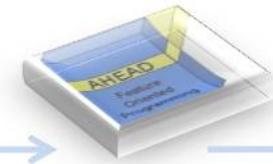
Extending State Charts in PinkCreek



- Features extend state charts by adding new states, transitions, annotations, etc.



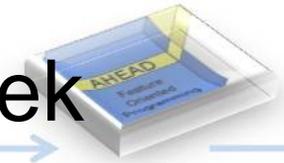
Extending State Charts in PinkCreek



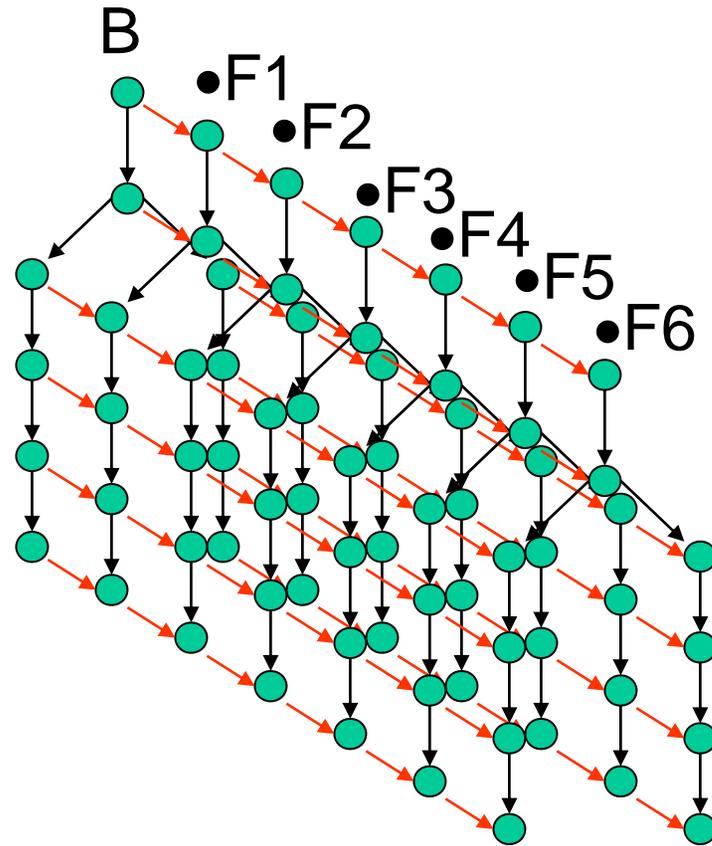
```

T' mkraw(ΔF_sc, ΔF_act-usr, ΔF_view-usr, ΔF_code-usr, ΔF_jsp-usr)
{
  ΔF_ctrl = T' ctrl2act (ΔF_sc);
  ΔF_act-sk = T' ctrl2act (ΔF_ctrl);
  ΔF_view-sk = T' ctrl2view (ΔF_ctrl);
  ΔF_act = ΔF_act-usr * ΔF_act-sk;
  ΔF_view = ΔF_view-usr * ΔF_view-sk;
  ΔF_jak-sk = T' act2jak (ΔF_act);
  ΔF_jsp-sk = T' view2jsp (ΔF_view);
  ΔF_code = ΔF_code-usr * ΔF_jak-sk;
  ΔF_jsp = ΔF_jsp-usr * ΔF_jsp-sk;
  ΔF_raw = { ΔF_ctrl, ΔF_act, ΔF_view, ΔF_jakcode, ΔF_jspcode };
  return ΔF_raw;
}
  
```

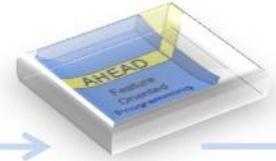
Commuting Diagrams in PinkCreek



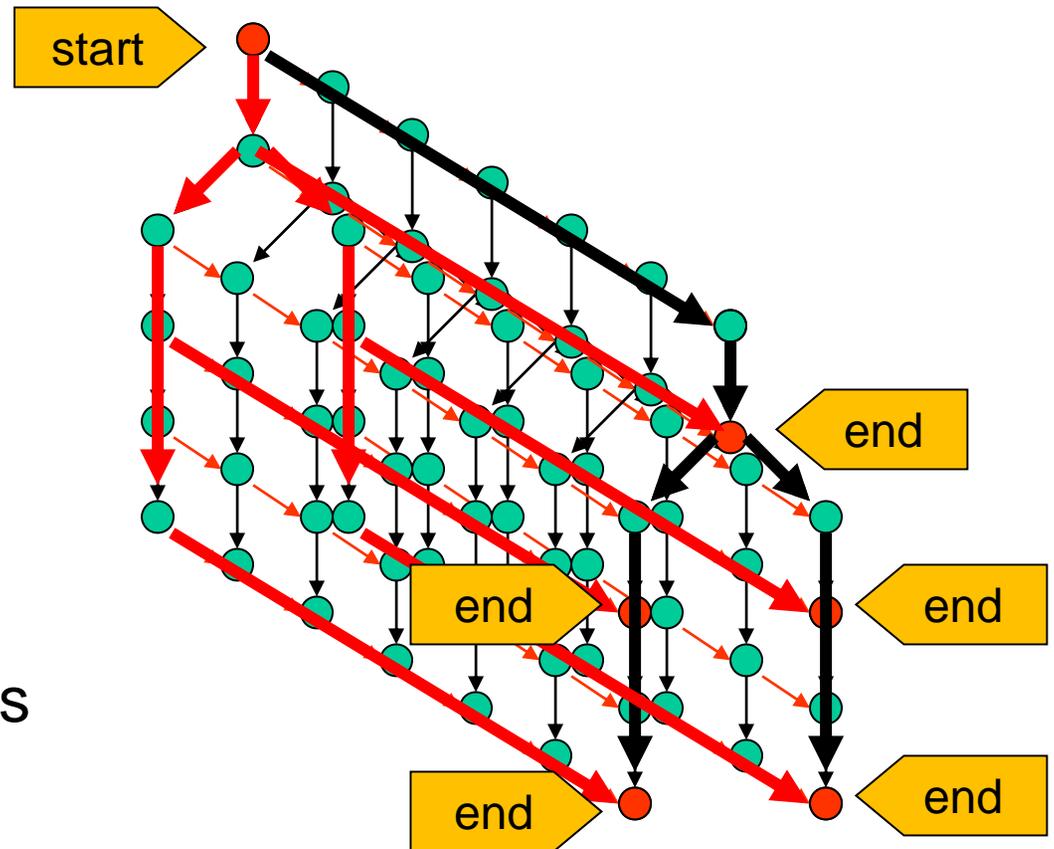
- Features map space of artifacts by extending them
- Composing features sweeps out the commuting diagram to traverse to synthesize portlet representations



Portlet Synthesis

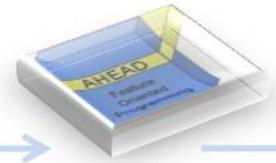


- Shortest path is a **geodesic**
- Start at upper left compute nodes on lower right
- #1: extend models and then derive
- #2: derive representations and then extend
- #2 is faster than #1 by factor of 2-3 times



see ICSE 2007 paper
by Trujillo et al.

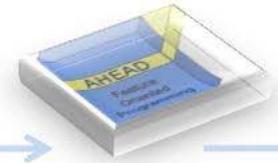
Experience



- Our tools initially did not satisfy properties commuting diagrams
 - synthesizing via different paths yields different results
 - exposed errors in our tools & specifications
- Significance of commuting diagrams

- validity checks provides assurances on the correctness of our model abstractions, portlet specifications, and our tools
- applies also to individual transformations (as they too have commuting diagrams)
- win – better understanding, better model, better tools
- reduce problem to its essence

In the Future

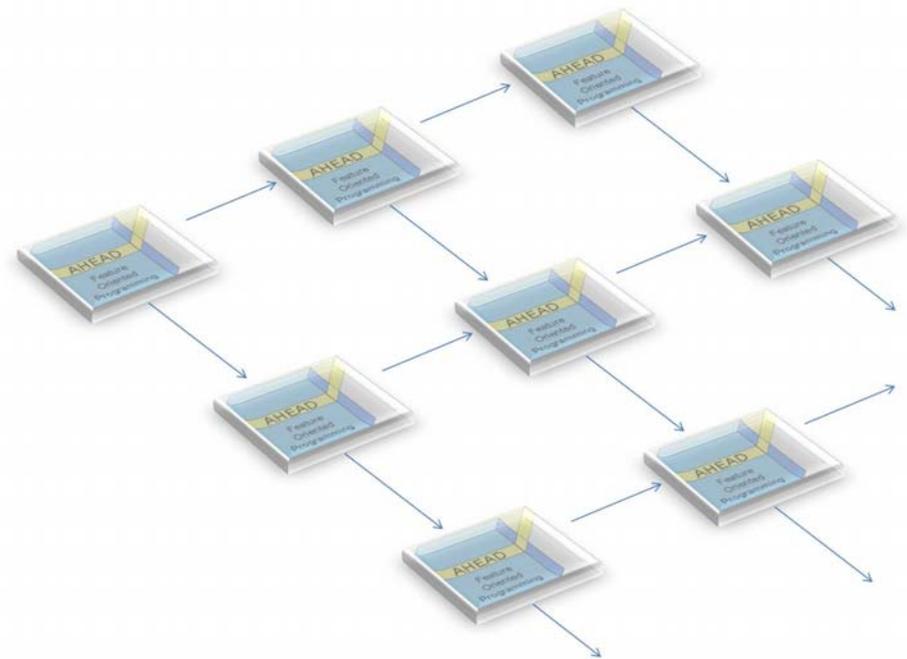


- Better understanding of these ideas & their practicality
- Theory, methodology, tools of architectural metaprogramming use elementary ideas from

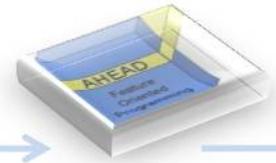
Category Theory

- where homomorphisms, pushouts, and commuting diagrams arise...
- topic of Lecture #2

Conclusions

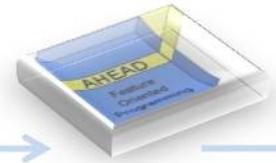


We are...



- Extraordinarily good at:
 - languages
 - compilers
 - optimizations
 - analyses
- Programming in the **small**:
 - understand abstractions
 - their models
 - their relationships
 - their integration
- Not good at:
 - languages
 - compilers
 - optimizations
 - analyses
- Programming in the **large**:
 - \neg understand abstractions
 - \neg their models
 - \neg their relationships
 - \neg their integration

My Message: Getting Closer



- Program design and synthesis has a simple algebraic underpinning

design is all about
structure definition and manipulation

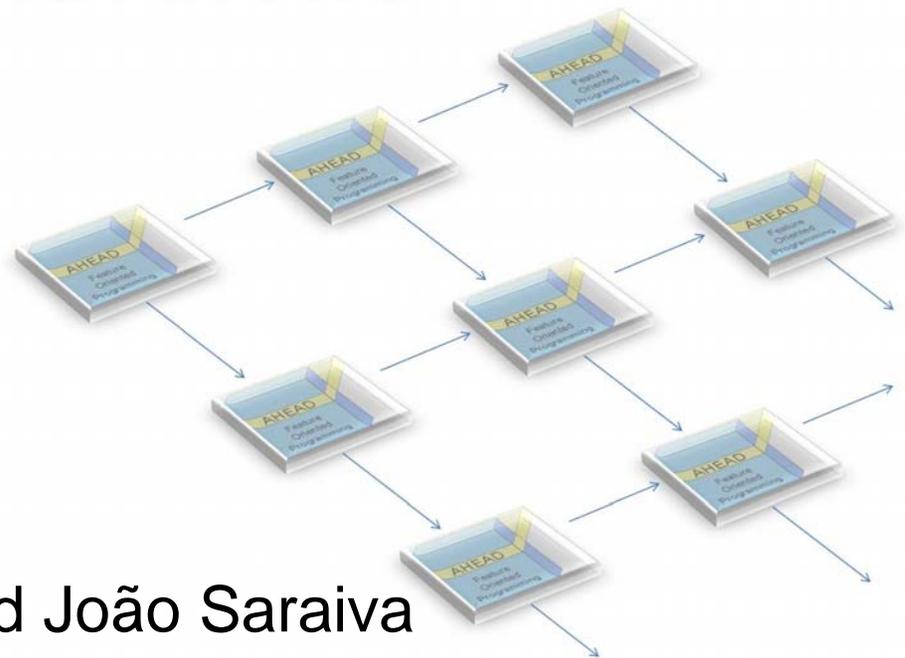
which is what mathematics is about

- This lecture sets the stage for our next lectures

category theory

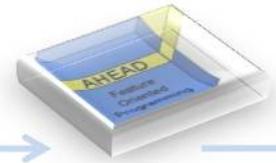
designs by algebra

Lecture 2: The Objects and Arrows of $D \times T$



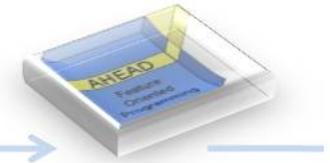
work with Maider Azanza and João Saraiva

Recap from Lecture 1



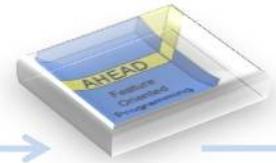
- Future of software design and development is automation
 - mechanize repetitive tasks
 - free programmers for more creative activities
- **Design by Transformation** is a paradigm where program design and synthesis is a computation
- **Design**: steps to take to create an artifact
 - meta-expression
- **Synthesis**: evaluate steps to produce the artifact
 - meta-expression evaluation
- **Design Optimization**: meta-expression optimization

Forefront of Automated Development



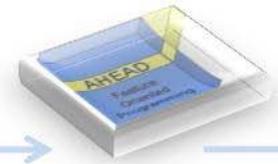
- **Model Driven Engineering (MDE)**
 - general-purpose approach
 - high-level models define applications
 - transformed into lower-level models
- **Software Product Lines (SPL)**
 - domain-specific approach
 - we know the problems, solutions of a domain
 - we want to automate the construction of these programs
- Both complement each other
 - strength of MDE is weakness of SPLs, and vice versa
 - not disjoint, but I will present their strengths as such here

This Lecture

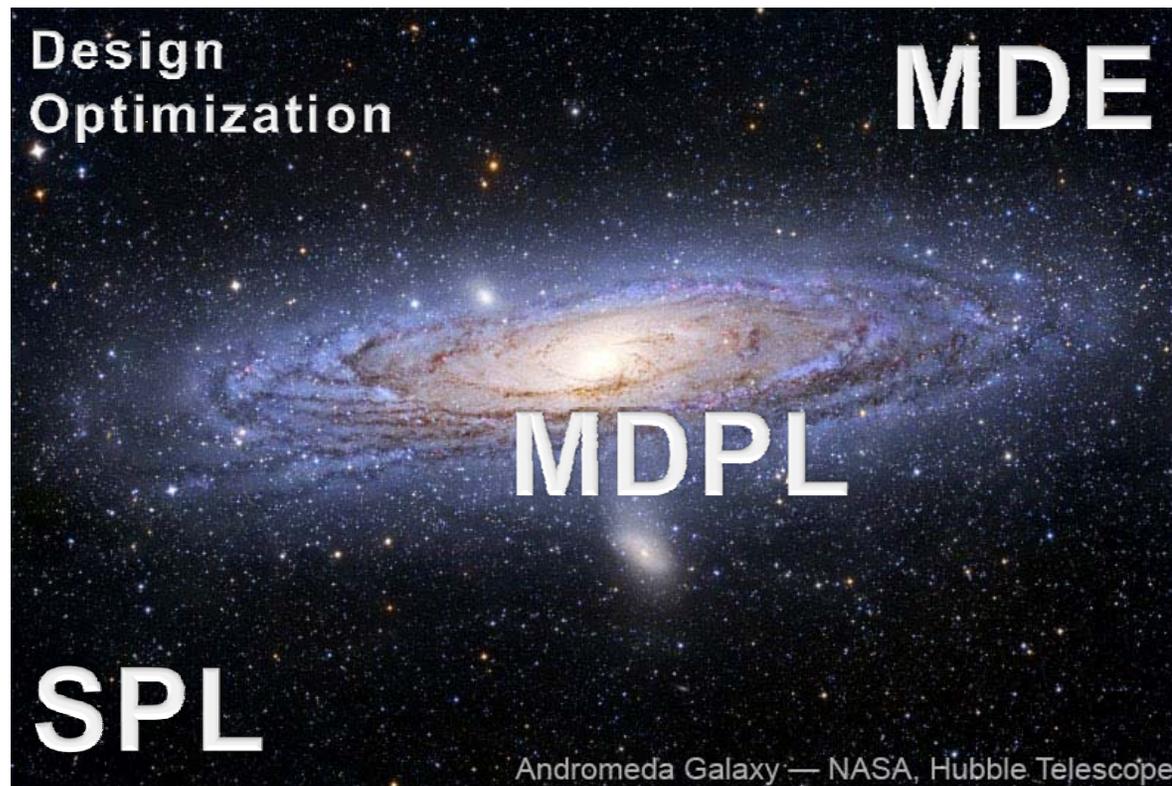


- This is a modeling talk aimed at practitioners
 - no special mathematical background
- Review core ideas in **Category Theory**
 - theory of mathematical structures
 - result of a domain analysis of geometry, topology, algebra...
 - these concepts are fundamental to MDE, SPL

This Lecture

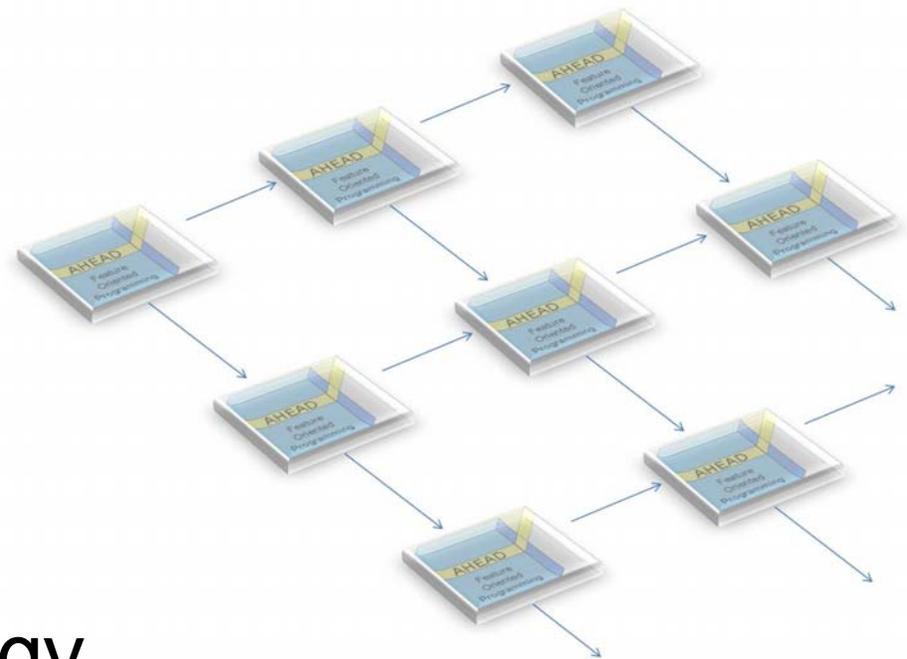


- Show categories provide unifying foundation for MDE & SPLs
- Series of mini-tutorials (10 minutes apiece)



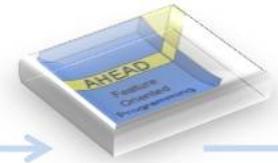
categories
on an
industrial
scale

#1: Categories in MDE

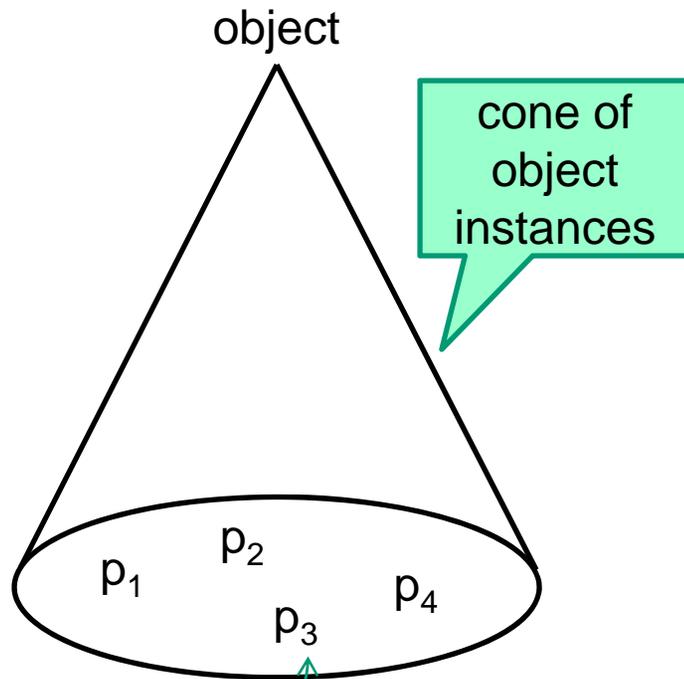


let's start with some
unfortunate terminology...

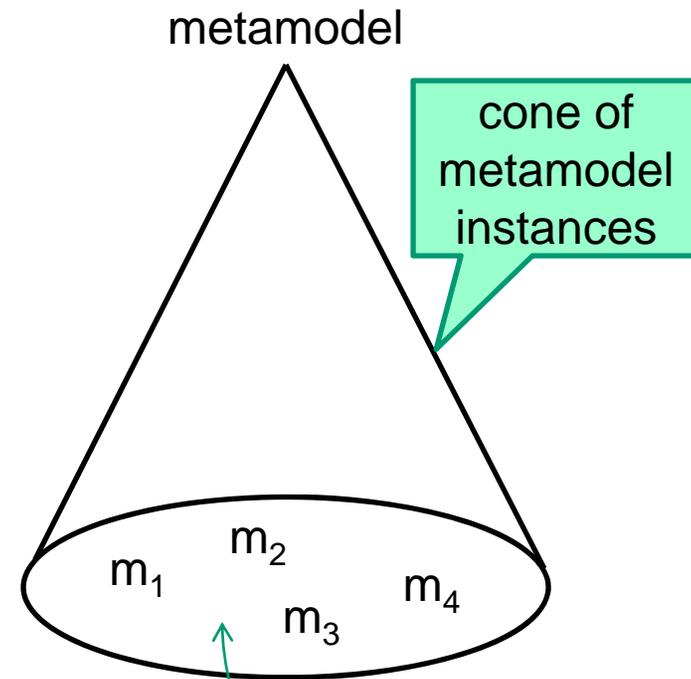
Objects in Categories



- An **object** is a domain of **points** (no standard term)
- **Metamodel** defines a domain of **models**

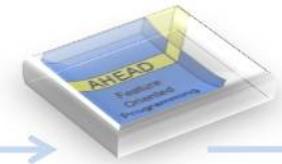


points

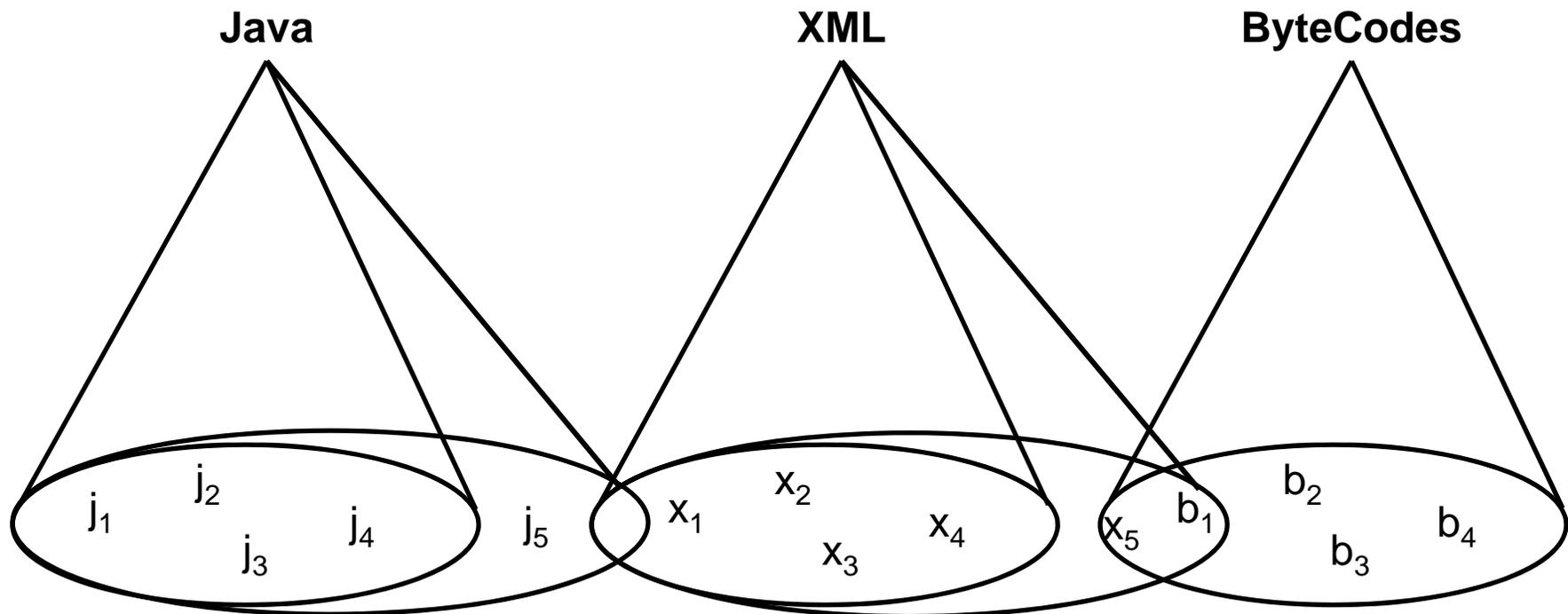


models

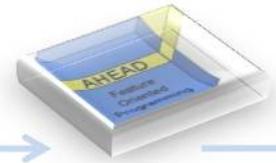
Examples



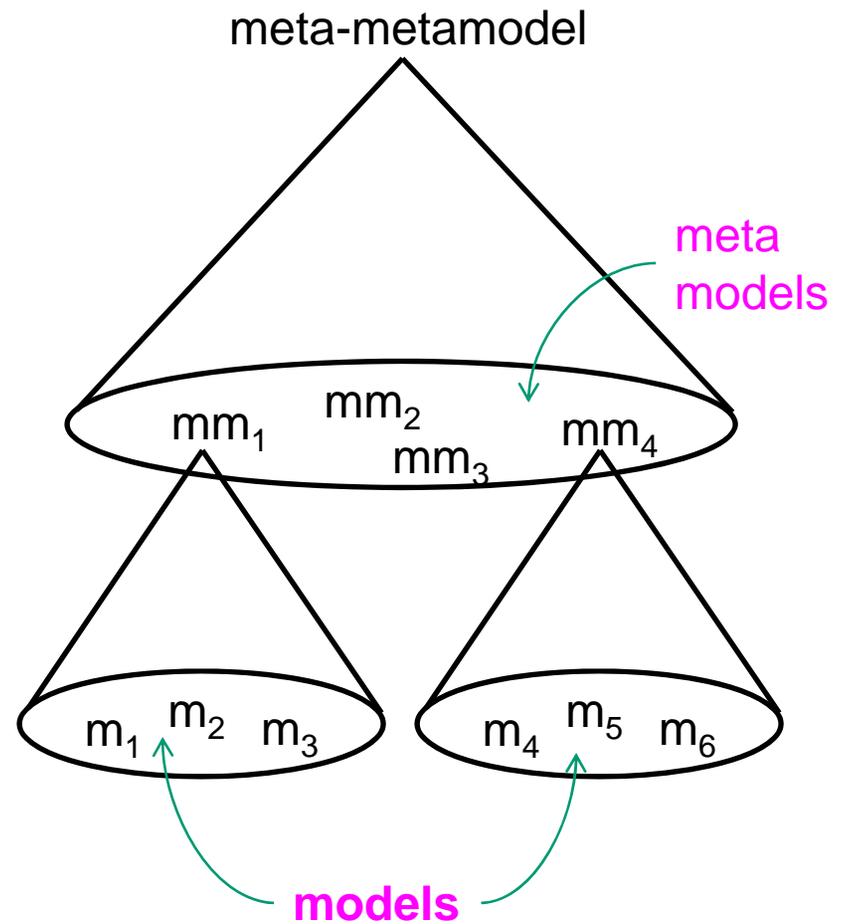
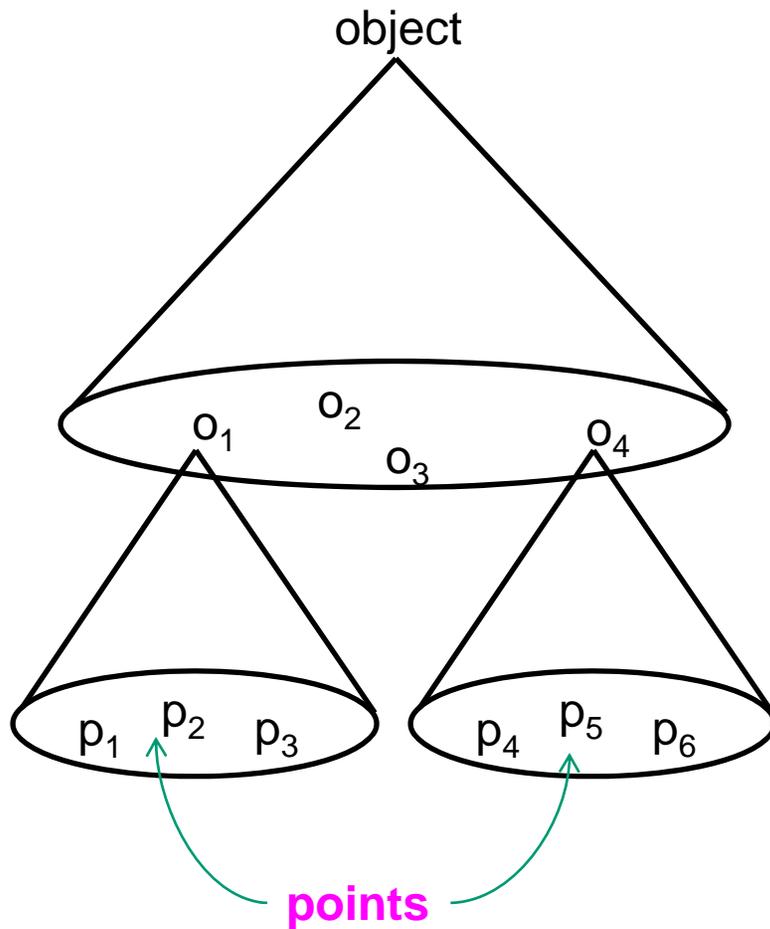
- MDE focuses on UML metamodels and their instances
- Ideas of objects & instances also apply to non-MDE artifacts
 - **technical spaces** of Bezivin, et al.



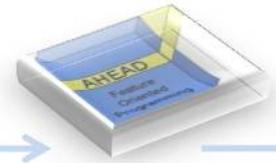
Recursion



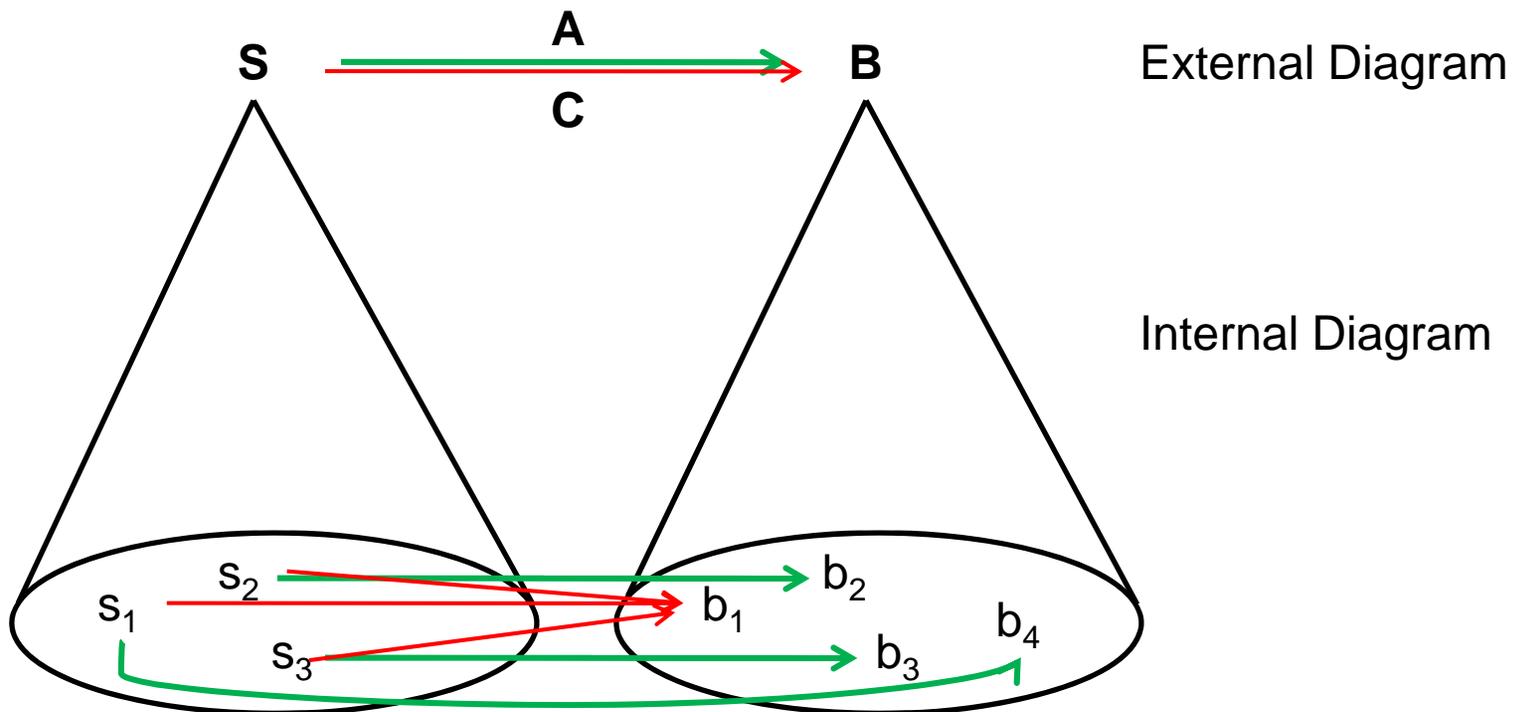
- A point can be an object
- Standard MOF architecture



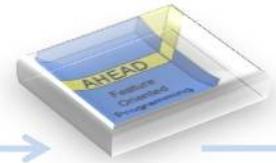
Arrow



- Is a **map** or **function** or **transformation** or **morphism** between objects (all names are used)
 - implementation is unspecified

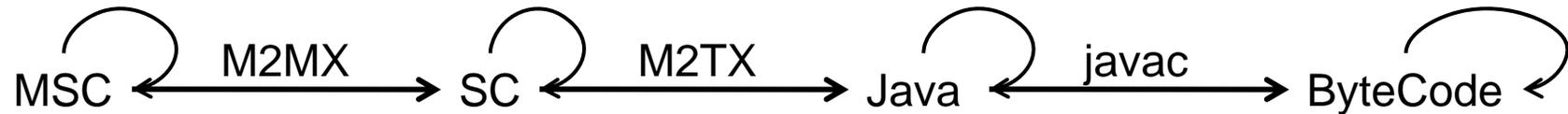
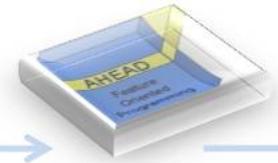


My Terminology (for this lecture)



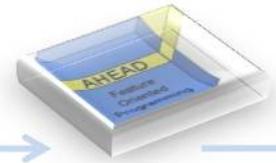
- **Arrow** – denotes a map
- **Transformation** – an MDE implementation of an arrow
 - ATL, RubyTL, GReAT, QVT ...
- **Tool** – is a non-MDE implementation of an arrow
 - standard tools of software engineers

External Diagrams

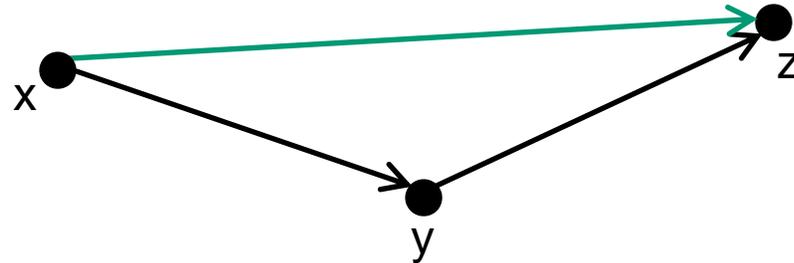


- **Category** – a collection of objects and arrows
 - above is a category of 4 objects, 3 non-identity arrows
 - 4 identity arrows (not always shown)
 - categories satisfy 3 simple properties...

Properties of Categories

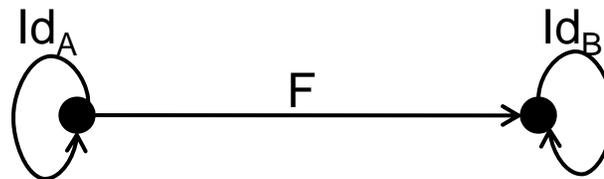


- Arrows are composable:



- Composition is associative: $A \bullet (B \bullet C) = (A \bullet B) \bullet C$

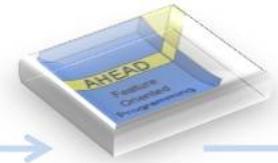
- Identities



$$F \bullet \text{Id}_B = F$$

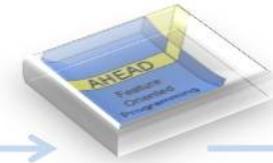
$$\text{Id}_A \bullet F = F$$

External Diagrams in MDE

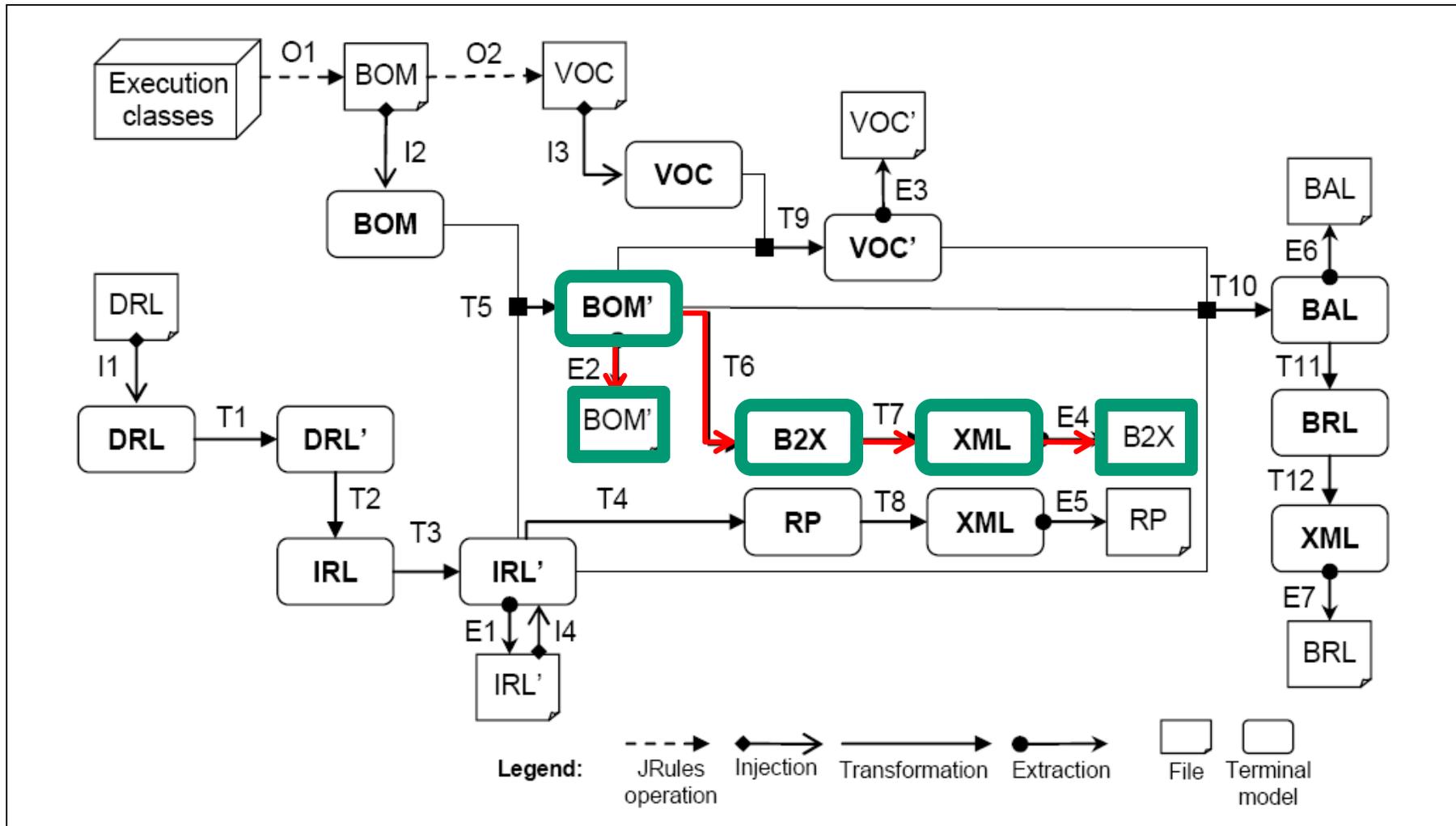


- No standard names for such diagrams in MDE
 - drawn differently (without identity arrows)
 - **Toolchain diagrams** (MIC)
 - **MegaModels** (ATL)
- MDE “designs” are categories on an industrial scale
 - not the microscopic and often obscure examples in texts

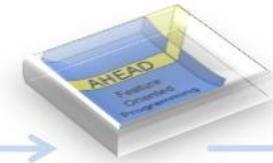
External Diagrams in MDE



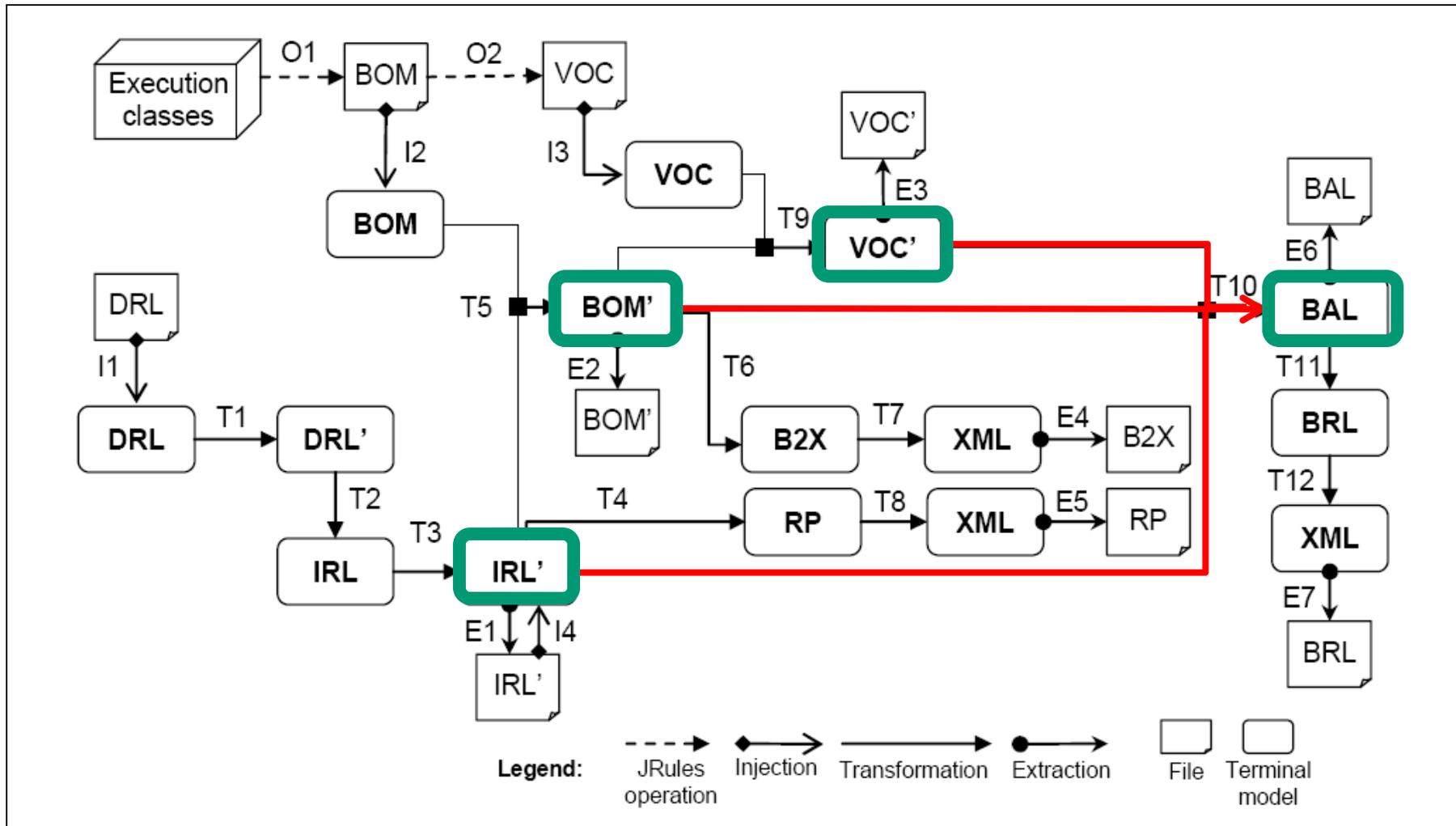
provided by J. Bezivin

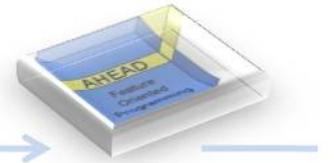


External Diagrams in MDE



provided by J. Bezivin





Arrows with Multiple Inputs, Outputs

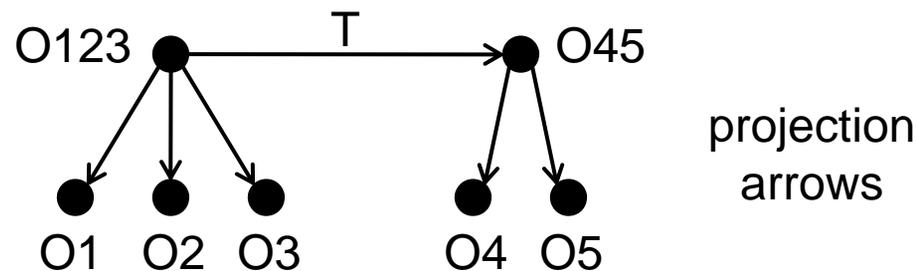
- Arrow maps 1 input object to 1 output object
- But transformation T occurs in model synthesis:

$$T: O1, O2, O3 \rightarrow O4, O5 ?$$

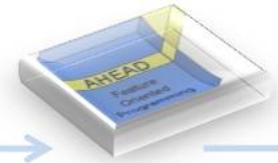
- Ans: create tuple of objects, which is itself an object

$$O123 = [O1, O2, O3]$$

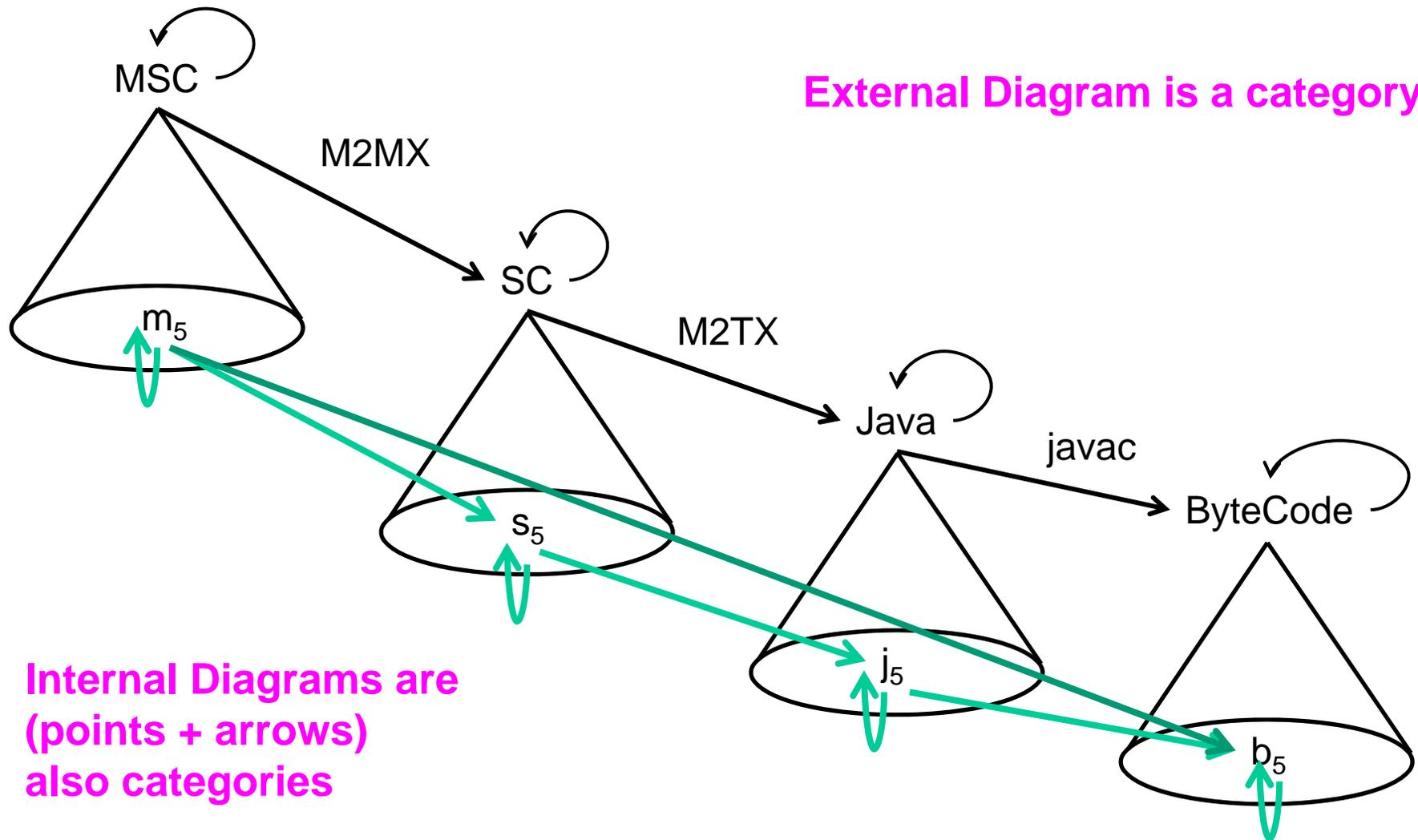
$$O45 = [O4, O5]$$



Internal Diagrams



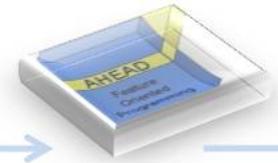
External Diagram is a category



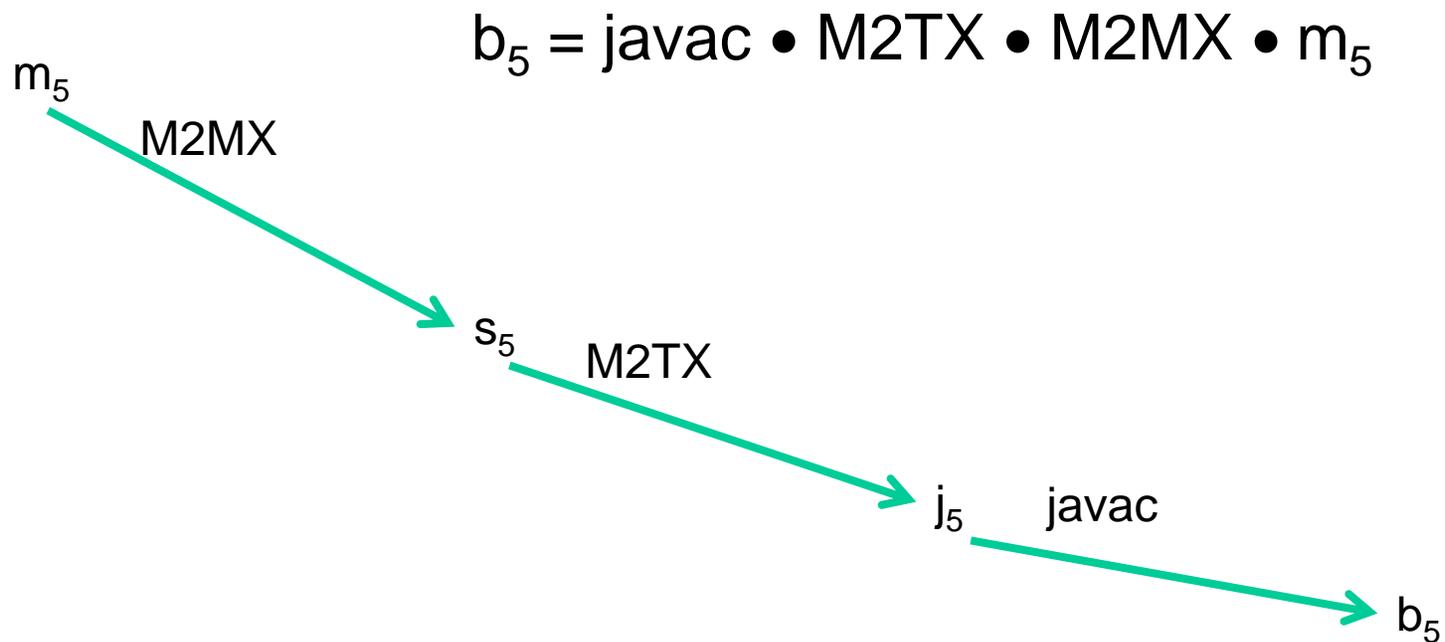
Internal Diagrams are
(points + arrows)
also categories

point is a domain with a single program

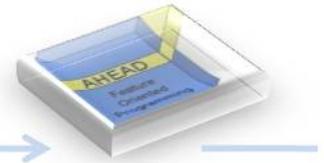
D×T



- Design of an artifact is a meta-expression
 - synthesis is meta-expression evaluation
 - RQO paradigm

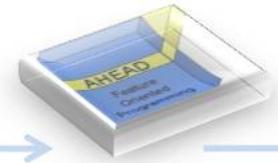


Recap



- Categories lie at the heart of MDE
 - found at all levels in an MDE architecture
 - MDE is categories on an industrial scale
- Informally, categories provide a compact set of ideas to express relationships that arise among objects in MDE
 - language and terminology for MDE $D \times T$
 - can use CT more formally
(e.g., Meseguer, Ehrig, Täntzer, Diskin, Czarnecki, ...)
- Now let's look for categories in Software Product Lines

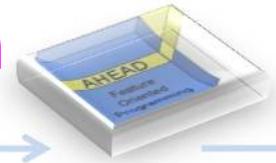
SPL Overview



- SPL is a set of similar programs
- Programs are defined by **features**
 - increment in program functionality that customers use to distinguish one program from another
- Programs are related by features
 - program P is derived from program G by adding feature F
 - from our 1st lecture, a feature is a function:

$$P = F(G)$$

4-Program Product Line with Superposition



```
class calculator {
    float result;
    void add( float x ) { result+=x; }
    void sub( float x ) { result=-x; }
}

class gui {
    JButton format = new JButton("format");
    JButton add     = new JButton("+");
    JButton sub     = new JButton("-");

    void initGui() {
        ContentPane.add( format );
        ContentPane.add( add );
        ContentPane.add( sub );
    }

    void initListeners() {
        add.addActionListener(...);
        sub.addActionListener(...);
    }

    void formatResultString() {...}
}
```

new methods

new fields



new fields

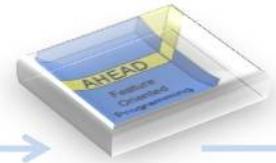
extend existing methods

extend existing methods

format • sub • base = p₄

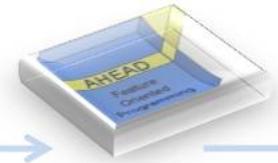
new methods

Scale Reminder (From Lecture #1)

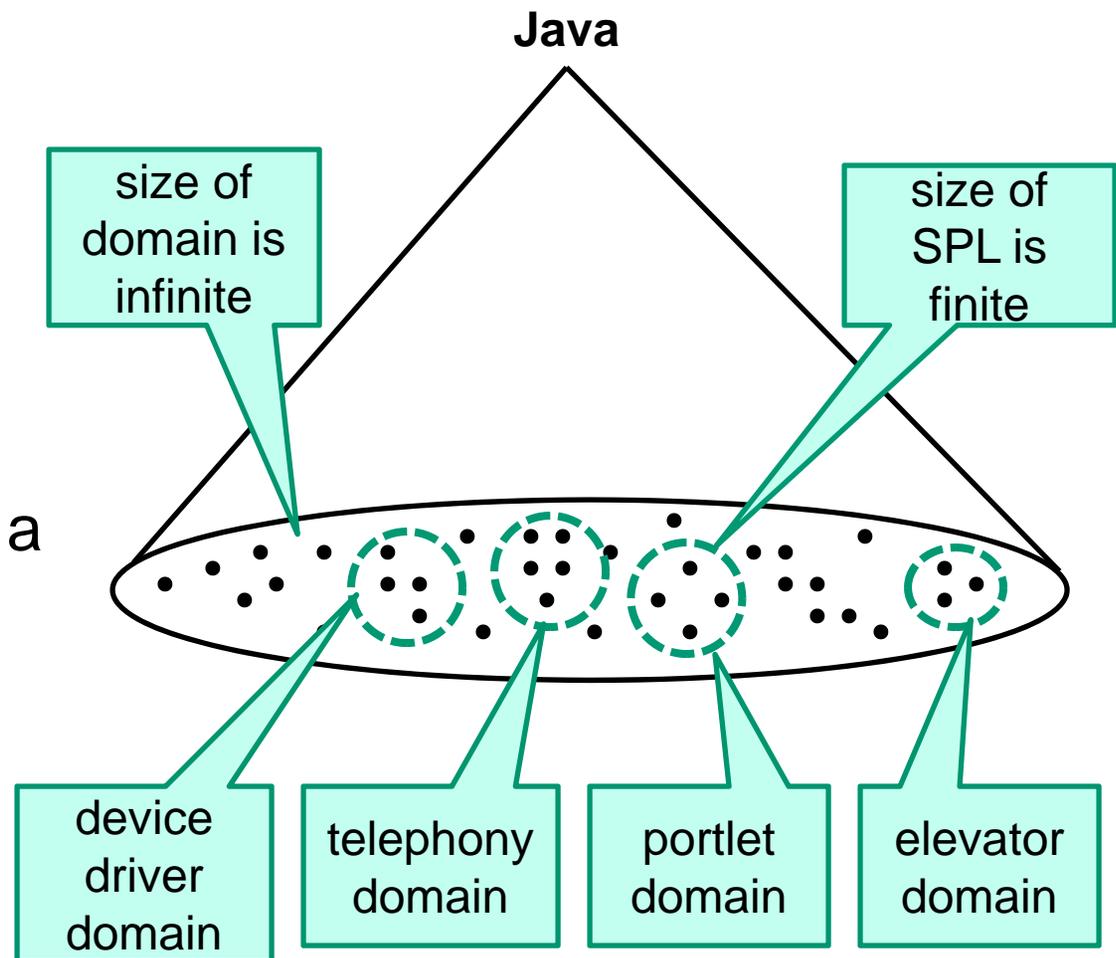


- 1986 database systems 75K LOC
- 1989 network protocols
- 1993 data structures
- 1994 avionics
- 1997 extensible Java precompilers 35K LOC
- 1998 radio ergonomics
- 2000 program verification tools
- 2001 verified compiler for Java1.0
- 2002 fire support simulators
- 2003 AHEAD tool suite 250K LOC
- 2004 robotics controllers
- 2006 web portlets
- 2008 SGI+JavaScript application
- 2009 ZipMe compression library

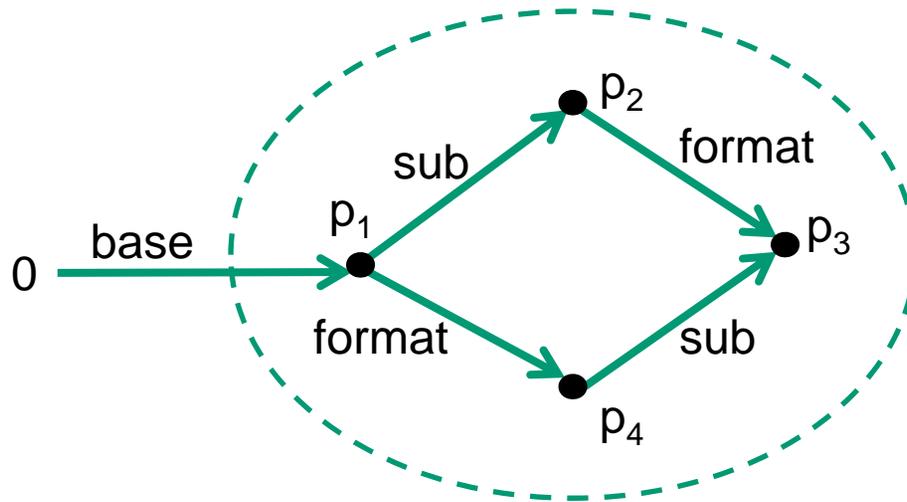
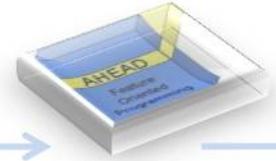
Perspective on Product Lines



- SPL is a *finite* set of similar programs
- Is *miniscule* subset of a domain
- Infinite set of SPLs in a domain

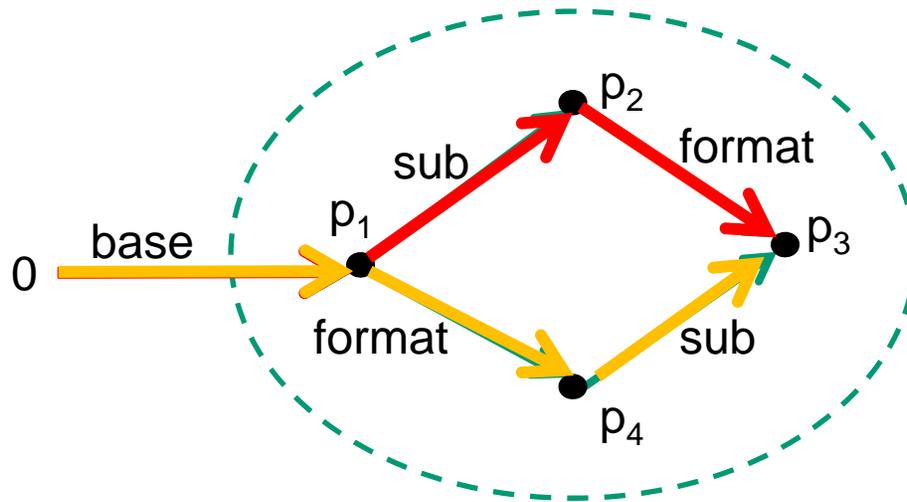
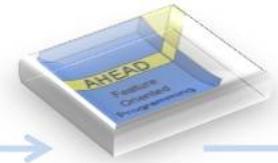


Perspective on Product Lines



- SPL defines relationships between its programs
 - how are programs related?
 - by arrows, of course!
 - each arrow is a **feature**
- Empty program (0) may or may not be part of SPL

D×T



$$p_3 = \text{format} \bullet \text{sub} \bullet \text{base}$$

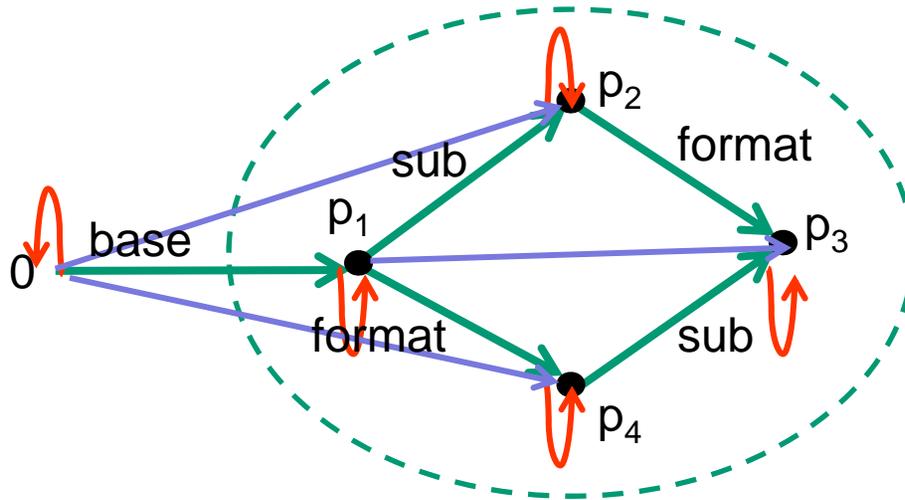
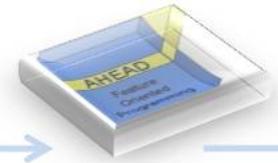
$$p_3 = \text{sub} \bullet \text{format} \bullet \text{base}$$

- Program design is a meta-expression
 - RQO paradigm
 - programs can have multiple designs

evaluating both meta-expressions yields the same program

format, sub are **commutative**

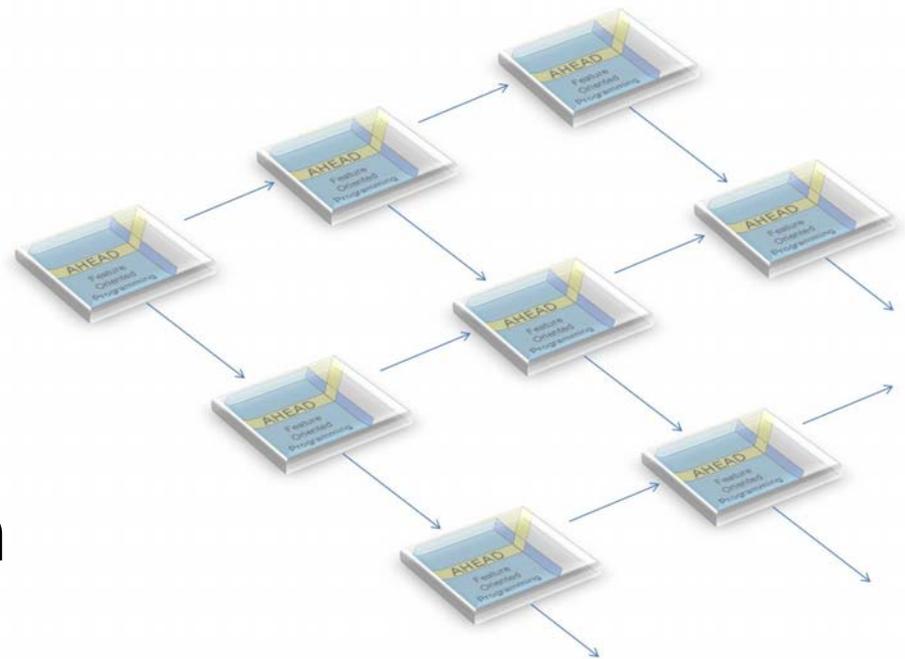
A Product Line is also a Category



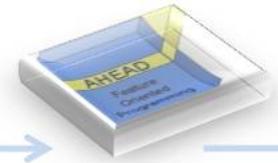
- Category
 - point is a domain with a single program in it
- Has implied identity arrows
- Has implied composed arrows, as required

Fundamental Ideas in SPL Implementations

(devoid of implementation details)

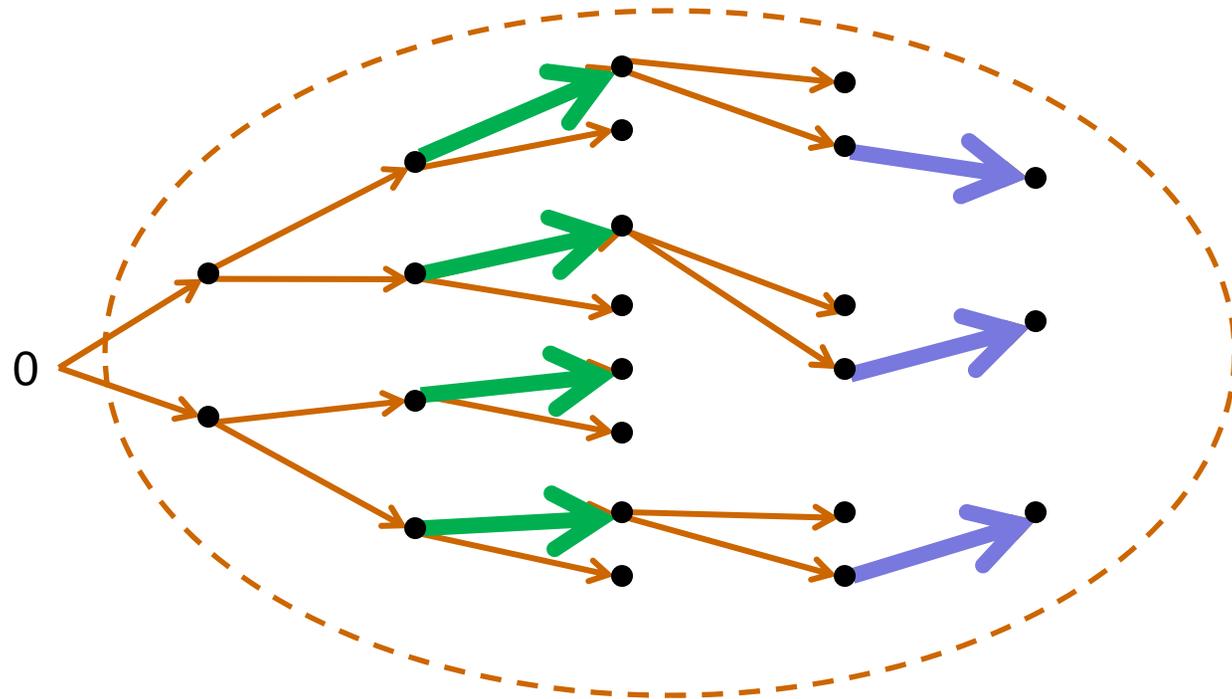


Implementing SPLs



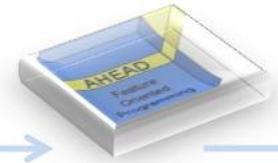
want this:

know this:

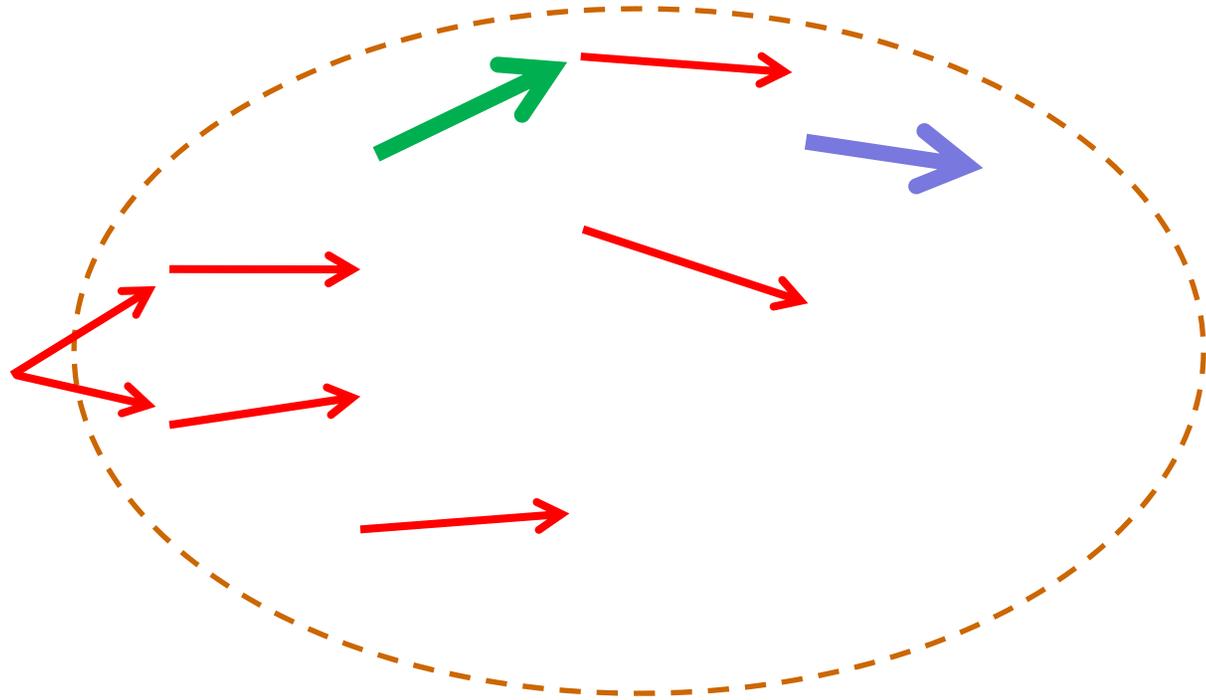


- Same function being applied to different inputs

Implementing SPLs

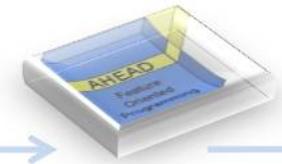


store this:

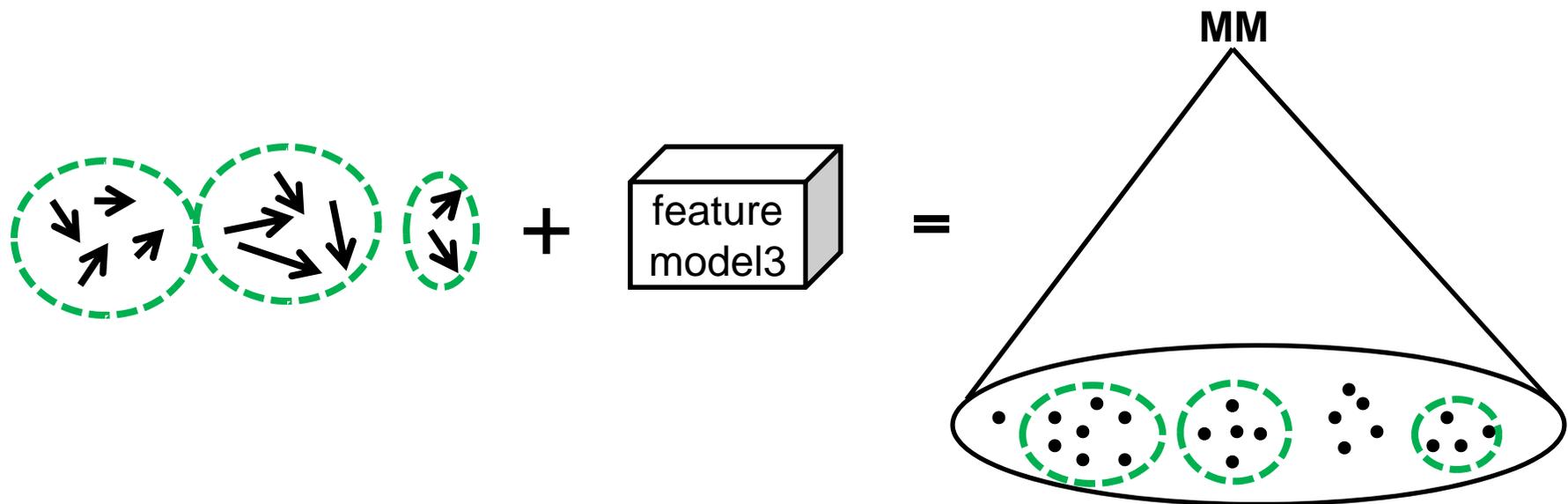


- Just store arrows once and reuse!
 - n optional features, 2^n possible programs
 - compact representation of an SPL

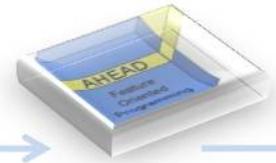
Models of SPLs



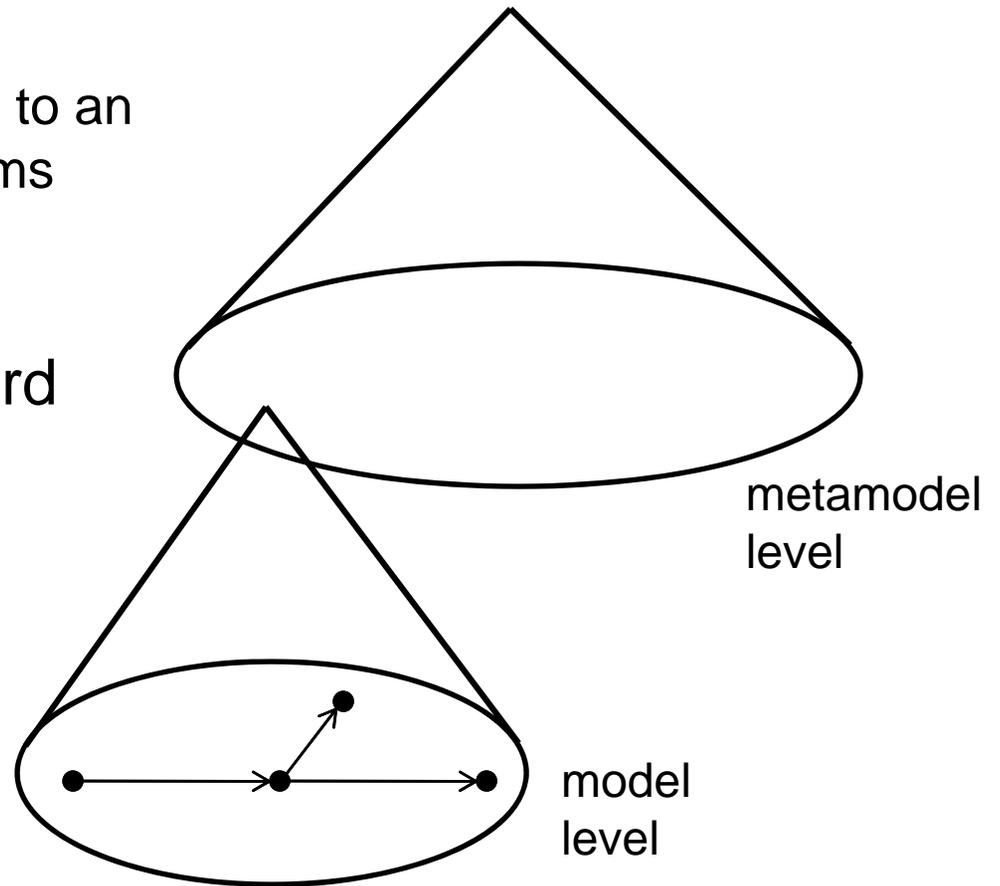
- Implement a set of arrows
 - by transformations, superposition, or whatever
- Feature model defines legal compositions of arrows
- Yields a product line



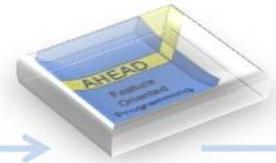
Recursion



- SPLs can appear at any level of an MDE architecture
 - arrow adds same feature to an infinite domain of programs
- **Superposition** is a standard technique, but not always sufficient
 - Kästner's CIDE (preprocessors)

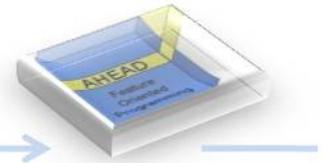


Essential Distinctions of SPL and MDE



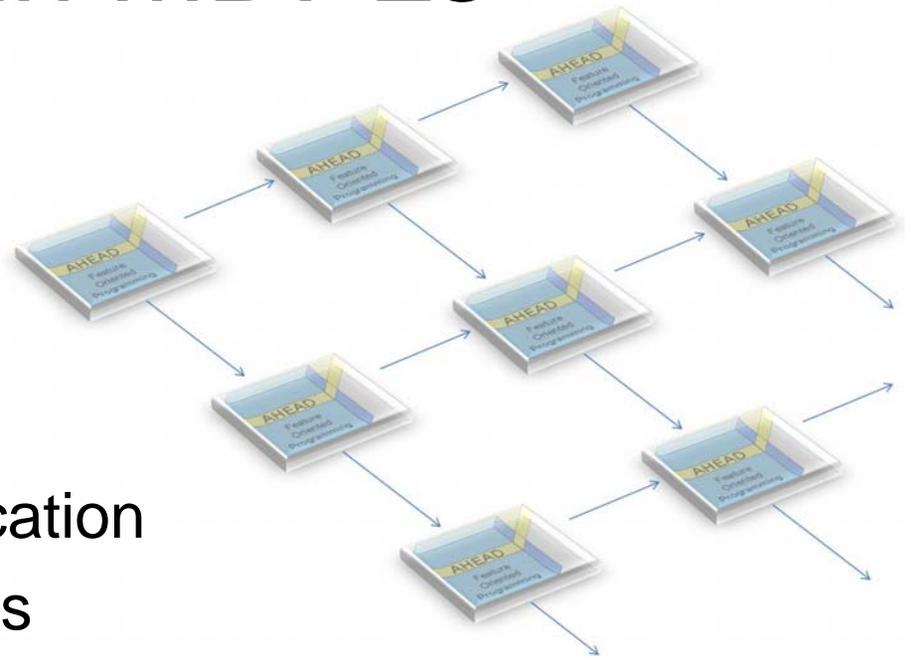
- An MDE “design” is a category with objects (domains) that are **infinite** in size
 - ex: metamodel of all class diagrams
 - # of such diagrams is infinite
- An SPL “design” is a category with objects (domains) that are **finite** in size
 - feature model defines a finite set of programs

Recap



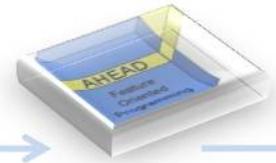
- Categories lie at the heart of Software Product Lines
 - SPLs appear at all levels of an MDE architecture
- Informally, categories provides a compact set of ideas to express relationships that arise among objects in SPL
 - places in perspective what MDE and SPL communities have been doing
 - fundamental concepts that our tools need to support
- Next topic: **model-driven product lines (MDPLs)**

#3: Categories in MDPLs

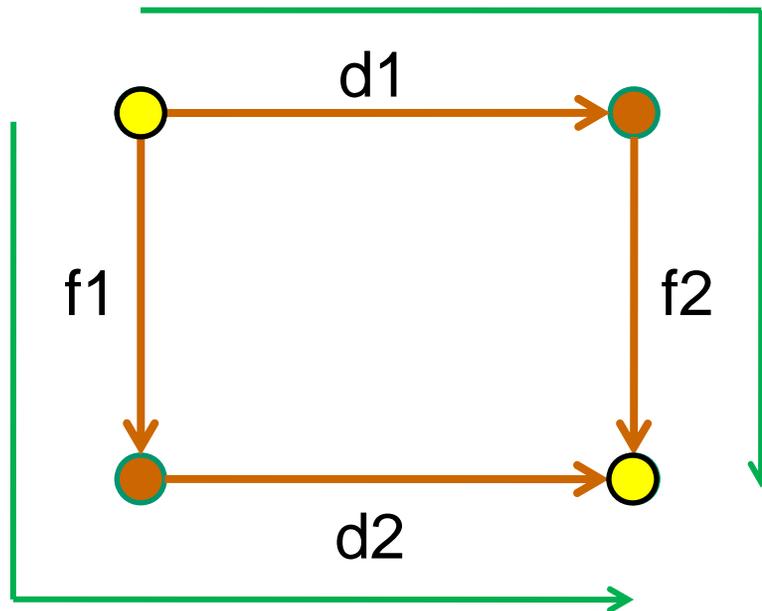


Exposing fundamental verification
and optimization relationships

Recall Commuting Diagrams

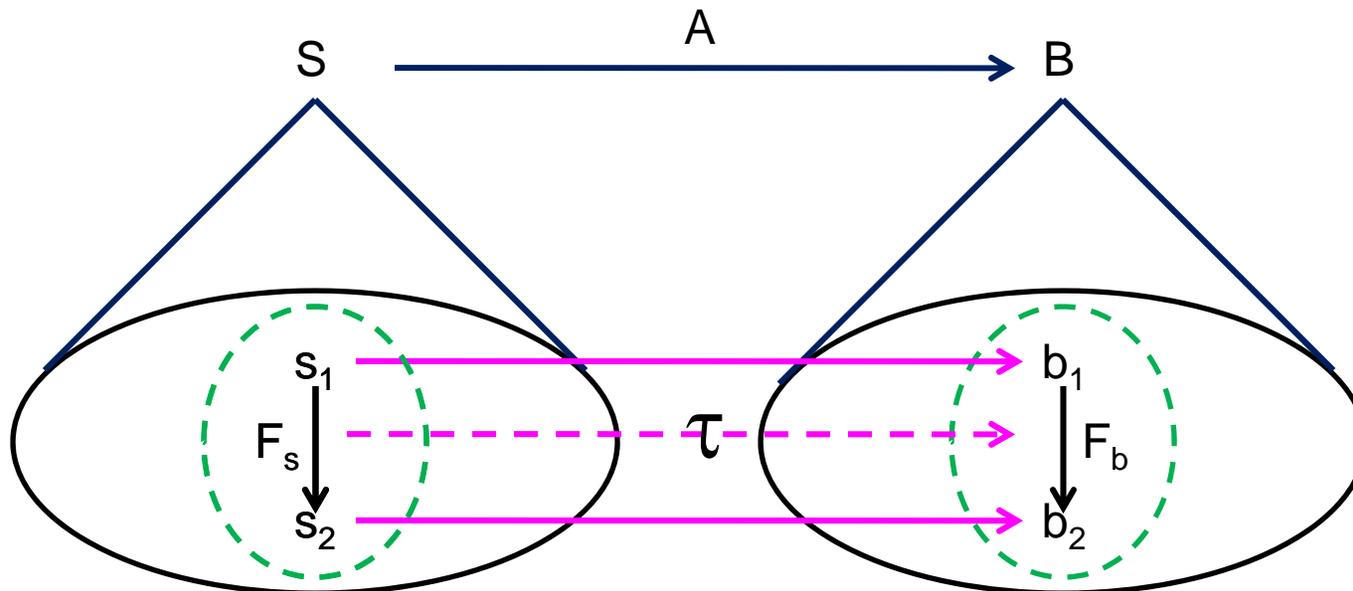
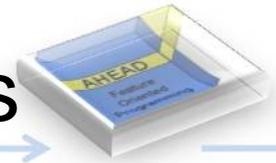


- Fundamental concept in category theory
 - all paths between two objects yield same result
 - theorems of CT



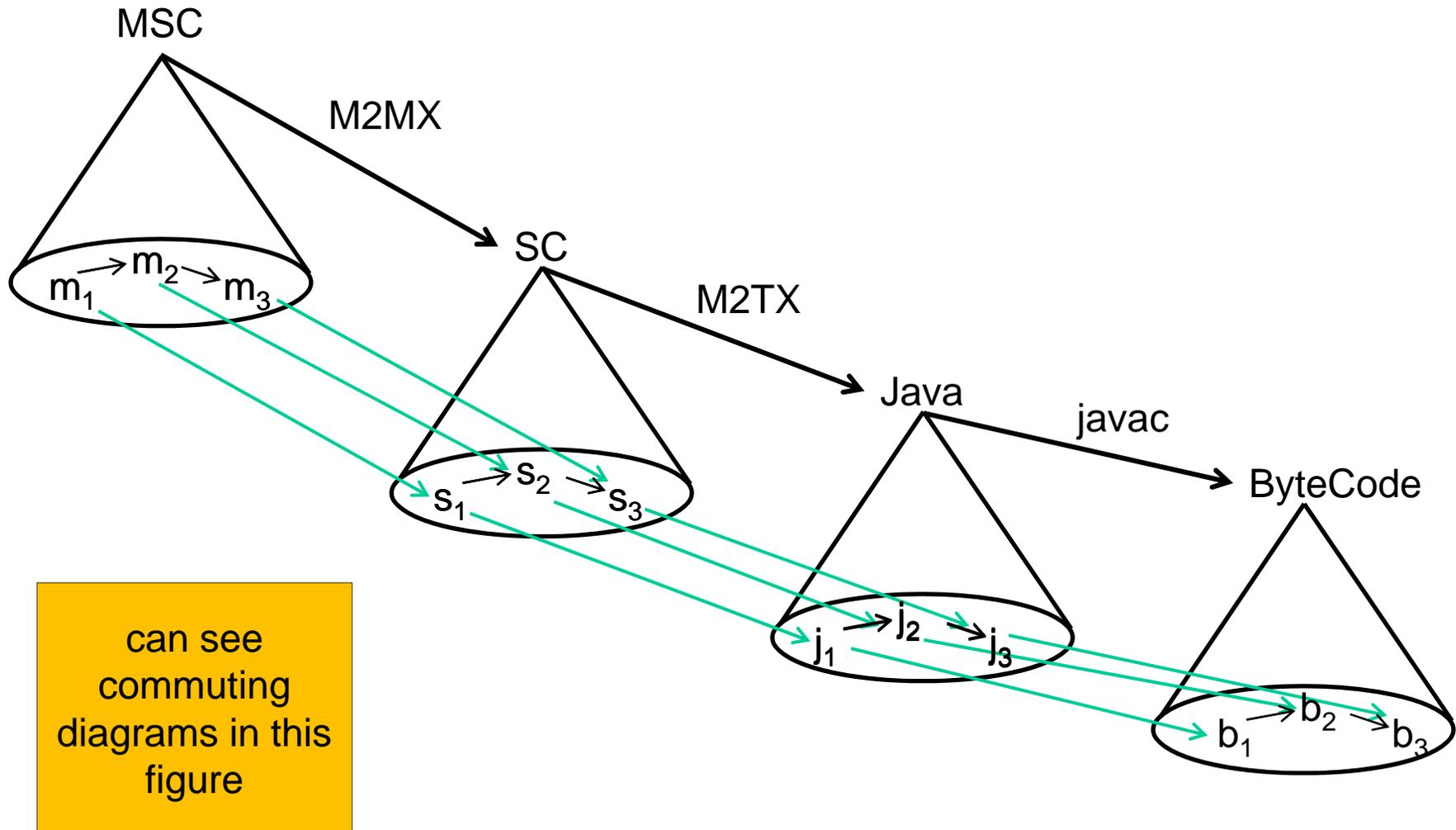
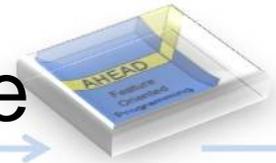
$$f_1 \bullet d_2 = d_1 \bullet f_2$$

Commuting Diagrams in MDPLs

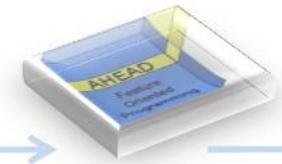


- Want to map a product line of S models to its corresponding product line of B models
 - typical MDE transformations map **only** points, not arrows
- **Operator** τ maps arrow F_s to arrow F_b : $\tau(F_s) = F_b$

How Commuting Diagrams Arise

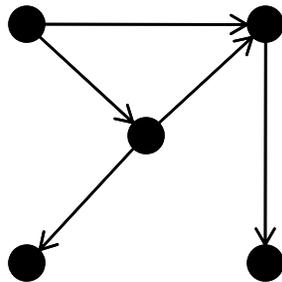


Functors

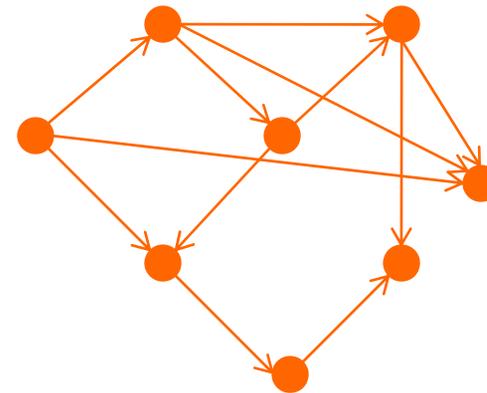


- Are fundamental to Category Theory
- $F:A \rightarrow B$ is an embedding of category A into category B
 - each object of A is mapped to an object in B
 - each arrow of A is mapped to an arrow of B such that arrow compositions in A are preserved in B

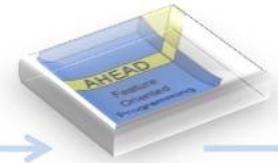
category A



category B

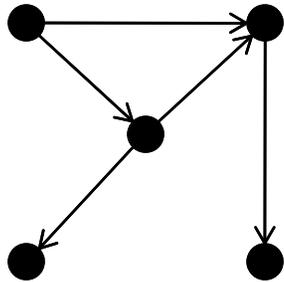


Functors

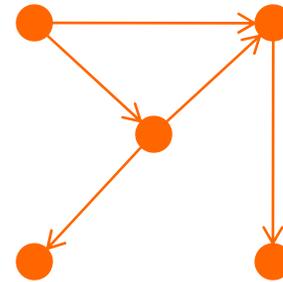


- I have encountered are isomorphic (A looks just like B)

category A

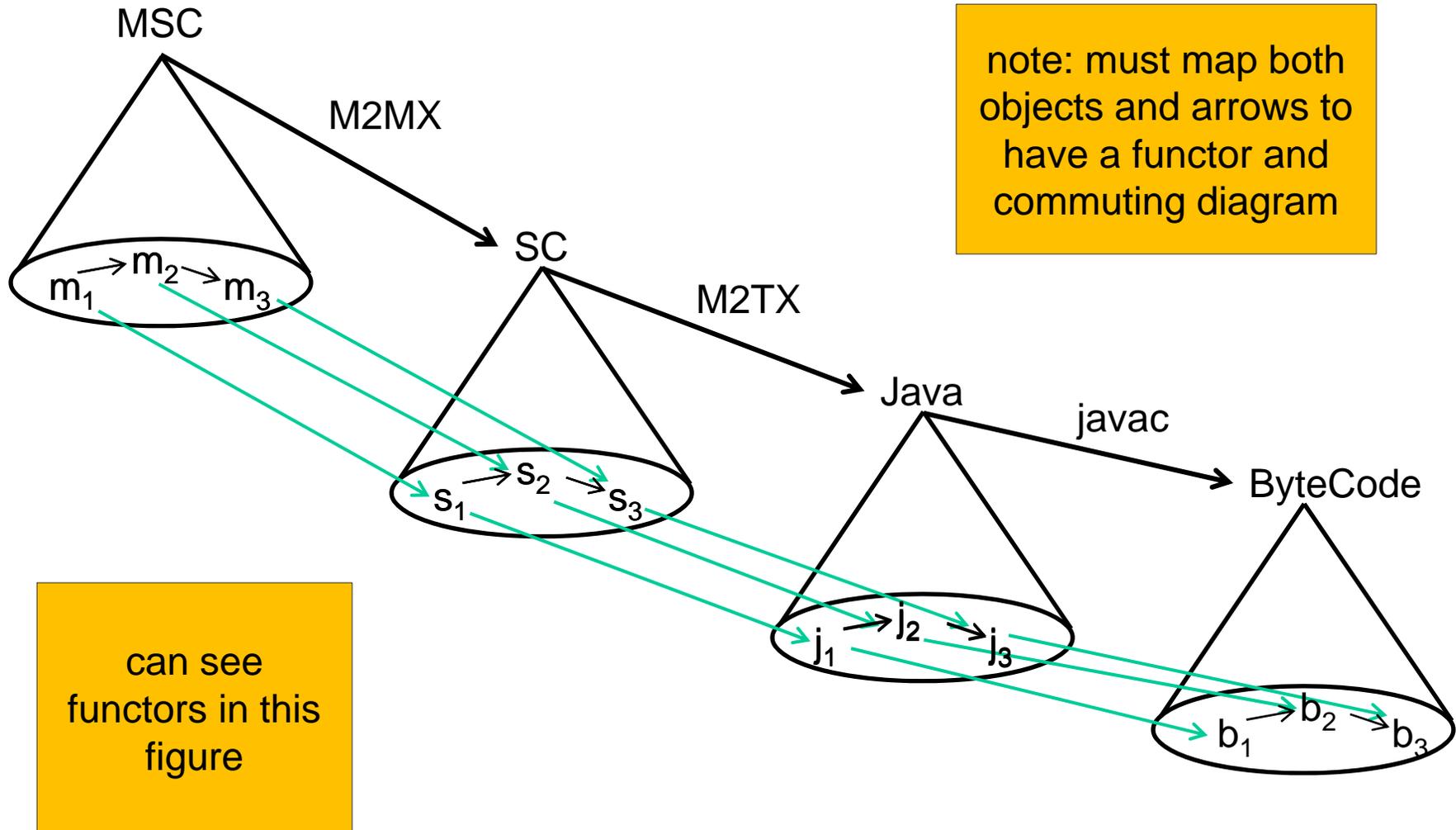
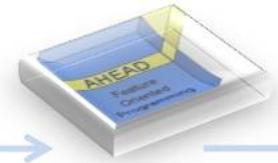


category B

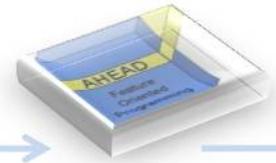


- Product line of Java files \rightarrow product line of bytecodes
- We have seen functors before in this tutorial

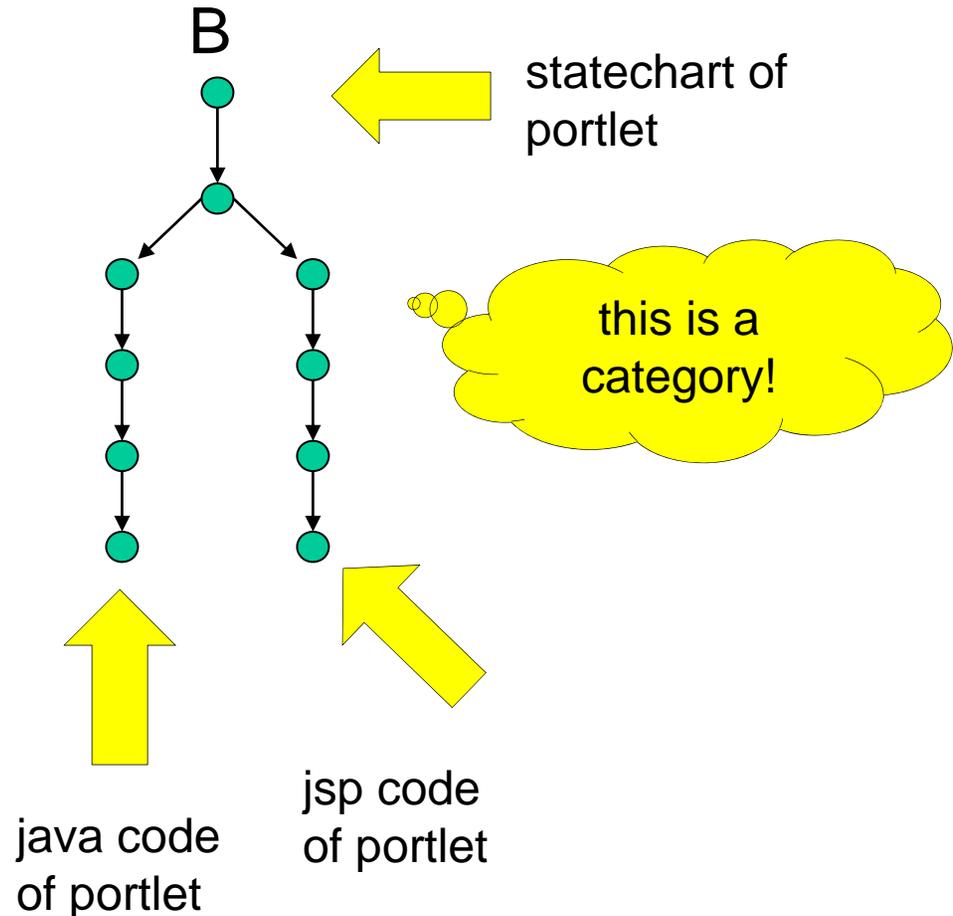
How Functors Arise



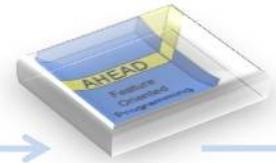
Functors and Commuting Diagrams in PinkCreek



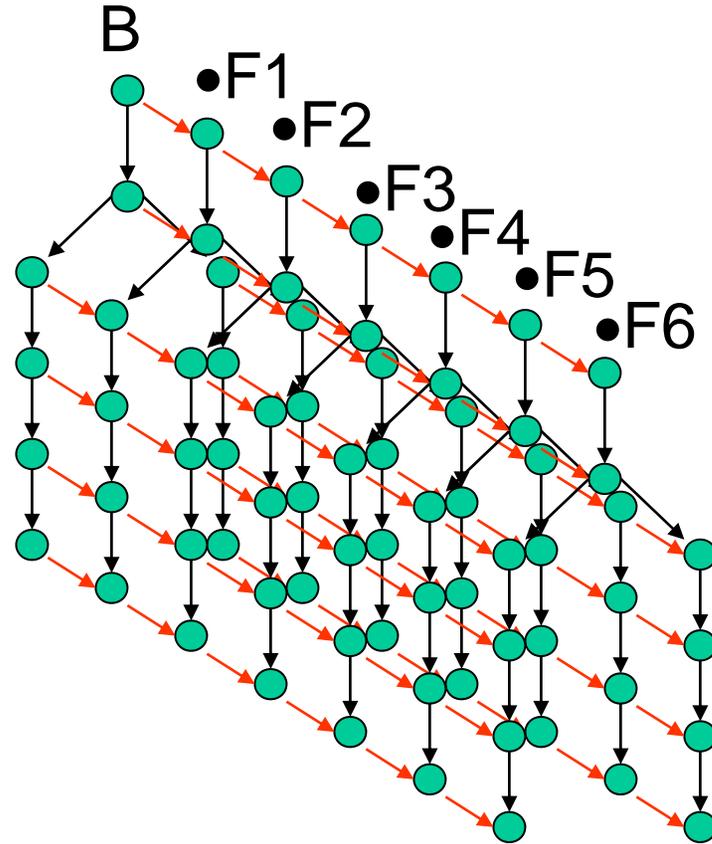
- Trujillo, et al. ICSE 2007
- Portlet synthesis
- Transform state chart into a series of lower level representations until Java and JSP code reached



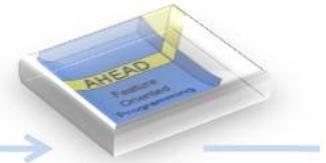
Functors and Commuting Diagrams in PinkCreek



- When a feature is added, each representation is extended (arrows remain the same)
- Features are functors: map each object, arrow of the original category to those of an isomorphic category
- Feature composition = Functor composition

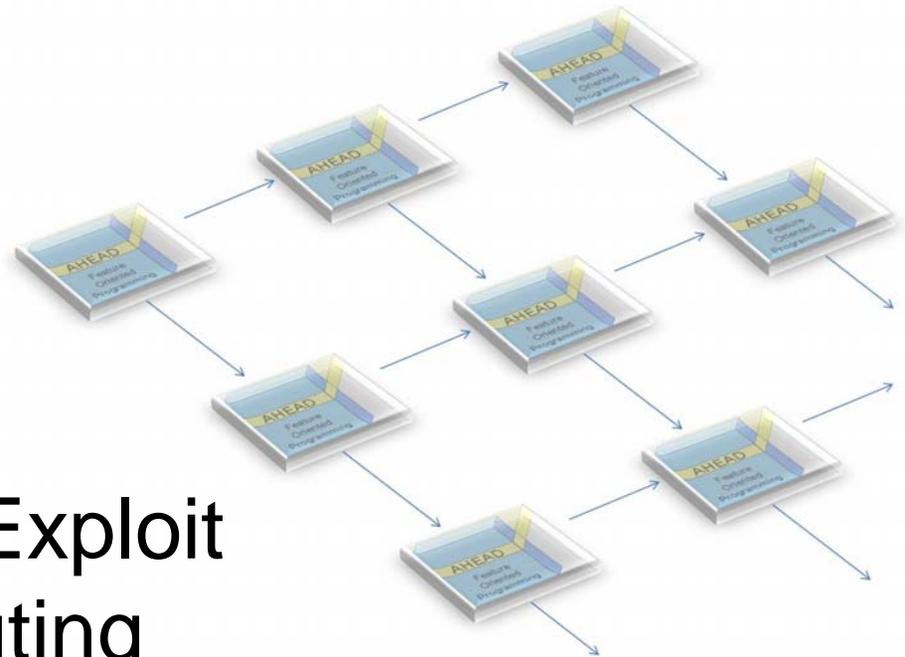


Warning!

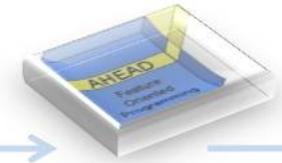


- Arrows are easy to draw...
 - may (or may not) be easy to implement
 - may (or may not) be practical to implement
 - CT is not constructive – it doesn't say how to implement arrows
 - no more than UML class diagrams tell you how to implement a method
- Tells you certain relationships exist, and if you can implement arrows, you can exploit commuting diagrams

More Examples that Exploit Functors and Commuting Diagrams

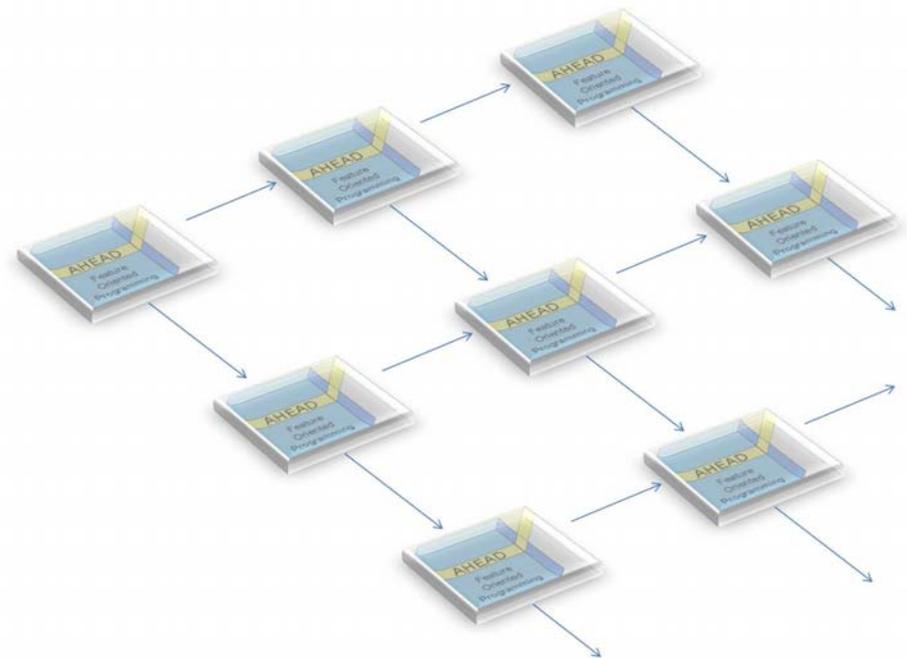


Writing Operators



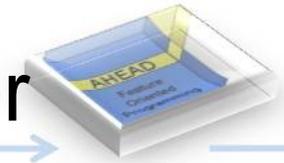
- We found other uses for commuting diagrams and arrow operators in MDPLs:
 - **simplifying implementation (ICMT 2008, SOSYM 2010)**
 - **improving test generation (SIGSOFT 2007, TSE 2010)**
 - understanding feature interactions (GPCE 2008)
 - understanding AHEAD (GPCE 2008)
- Briefly review the **first two** of these...

General Technique for Implementing MDPLs

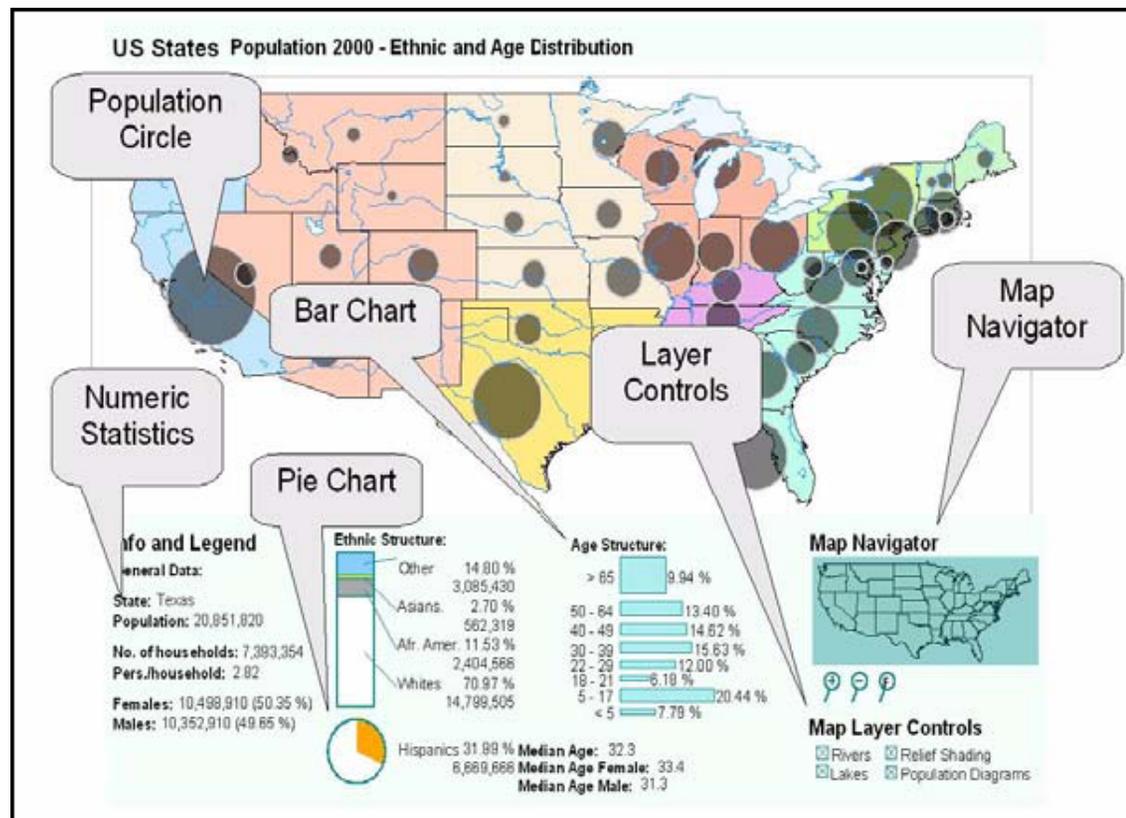


appreciate use of categories to explain what is going on

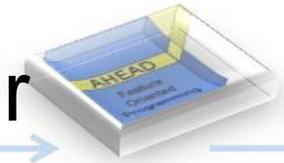
Example 1: SOSYM 2010 Paper



- Work with G. Freeman and G. Lavender
- MDPL of applications written in SVG and JavaScript
 - to customize an application (removing, adding charts, controls)

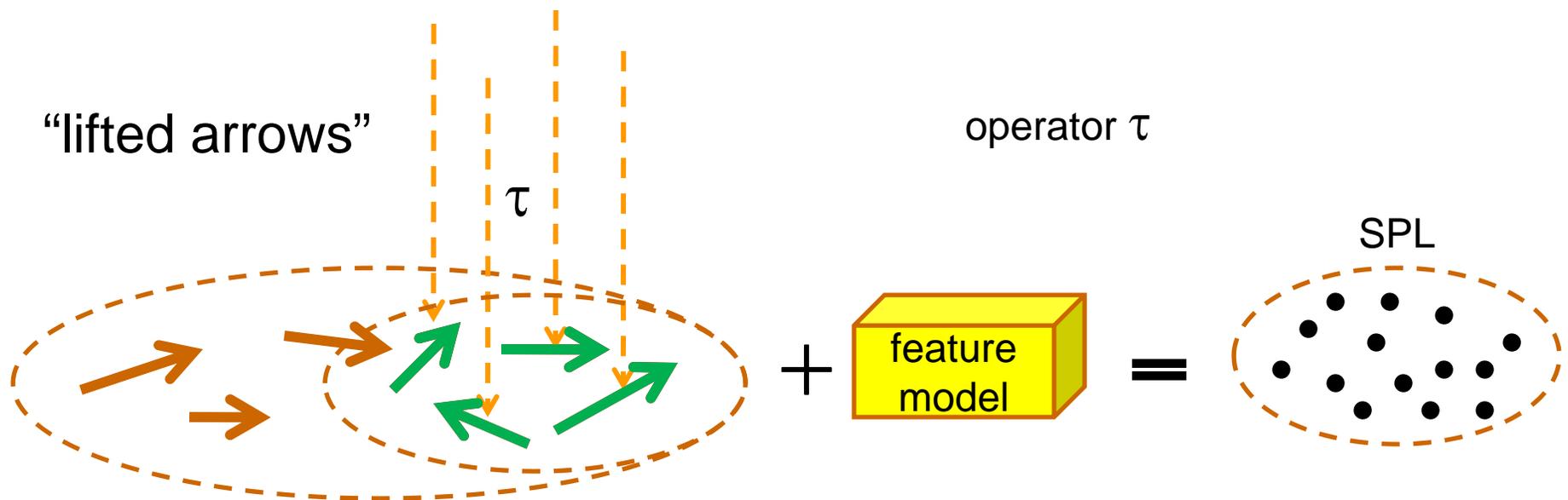


Example 1: SOSYM 2010 Paper



- Created a set of arrows and a feature model for our MDPL
 - red arrows (defining a product line of charts) were tedious to write
 - created DSL for charts, where arrows were easy to write, compose
 - defined an operator τ to map 1:1 from green arrows to red arrows

DSL for chart arrows



τ Mapping of Arrow to Arrow

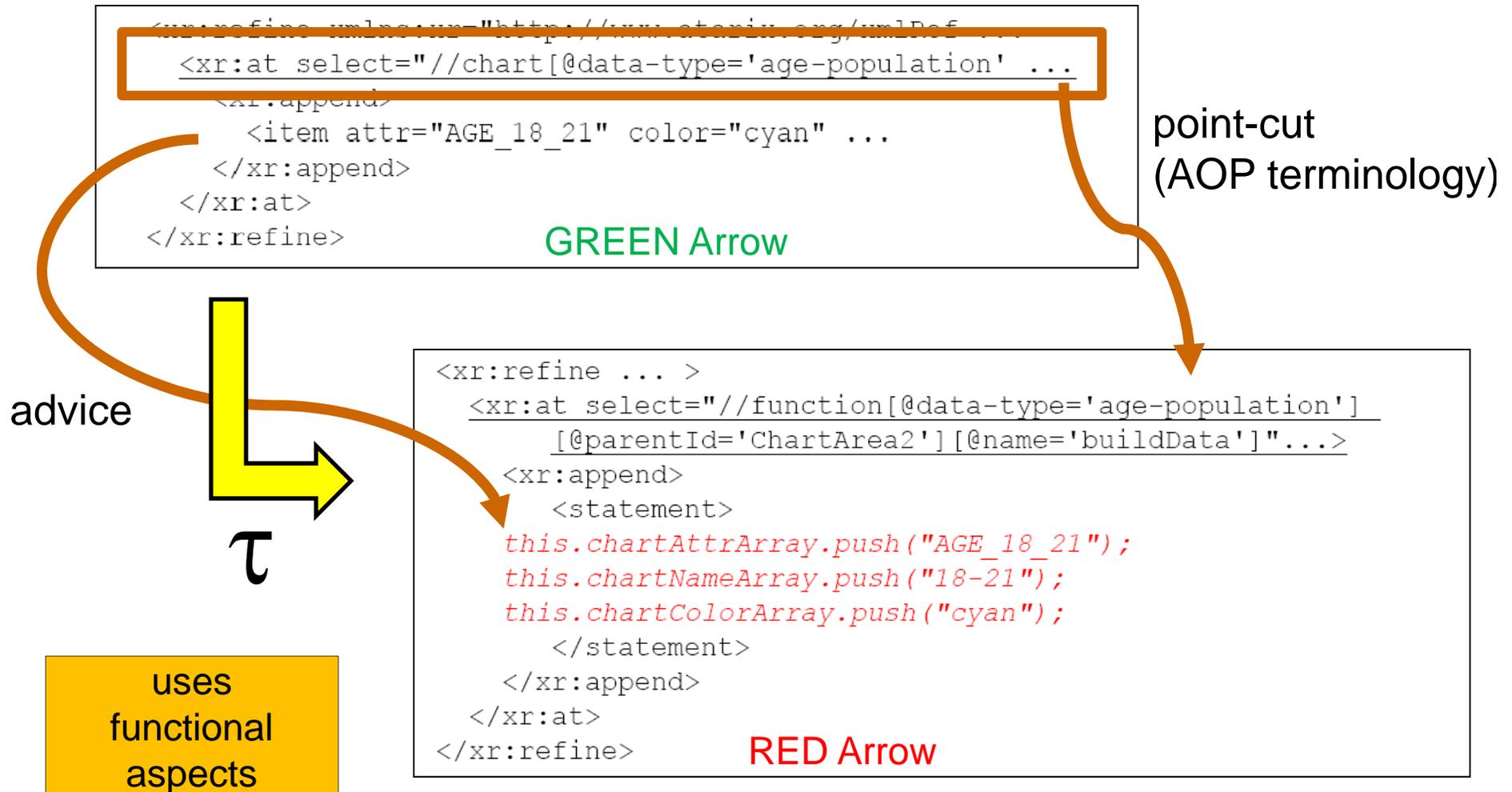
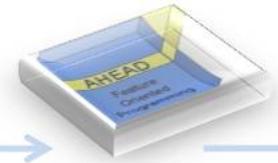
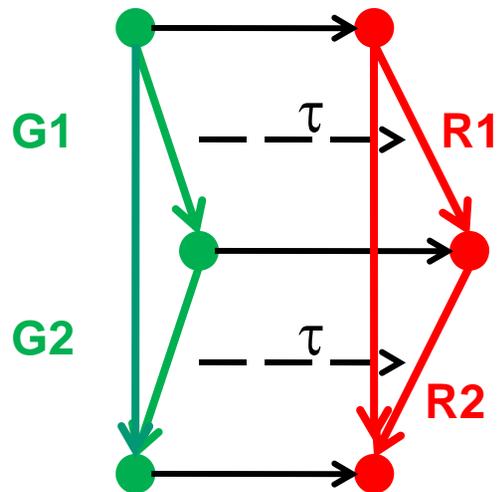
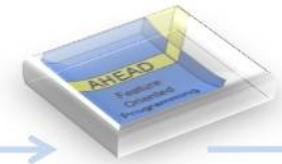


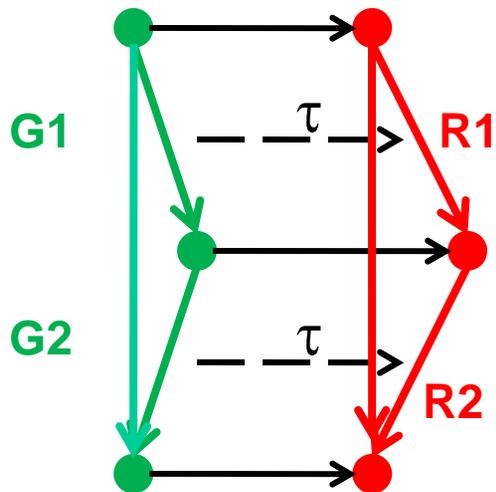
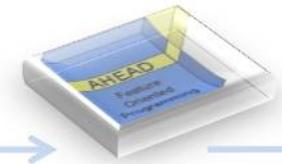
Diagram Constraints



$$\begin{aligned}\tau(\mathbf{G1} \bullet \mathbf{G2}) &= \tau(\mathbf{G1}) \bullet \tau(\mathbf{G2}) \\ &= \mathbf{R1} \bullet \mathbf{R2}\end{aligned}$$

- Same result if we compose green arrows and translate OR we translate green arrows, and compose red arrows
- **Homomorphism** – mapping of expression in one algebra (**GREEN**) to a corresponding expression in another (**RED**)

Diagram Constraints



$$\tau(G1 \bullet G2) = \tau(G1) \bullet \tau(G2)$$

$$= R1 \bullet R2$$

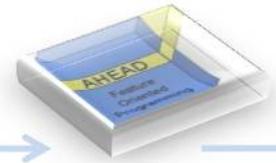
- Same we tra
- **Hom**
(**GRE**)

Verification condition:
 our implementation is correct
 if this equality holds!

translate OR
rows

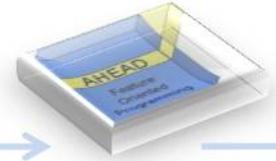
ne algebra
ther (**RED**)

From Lecture #1



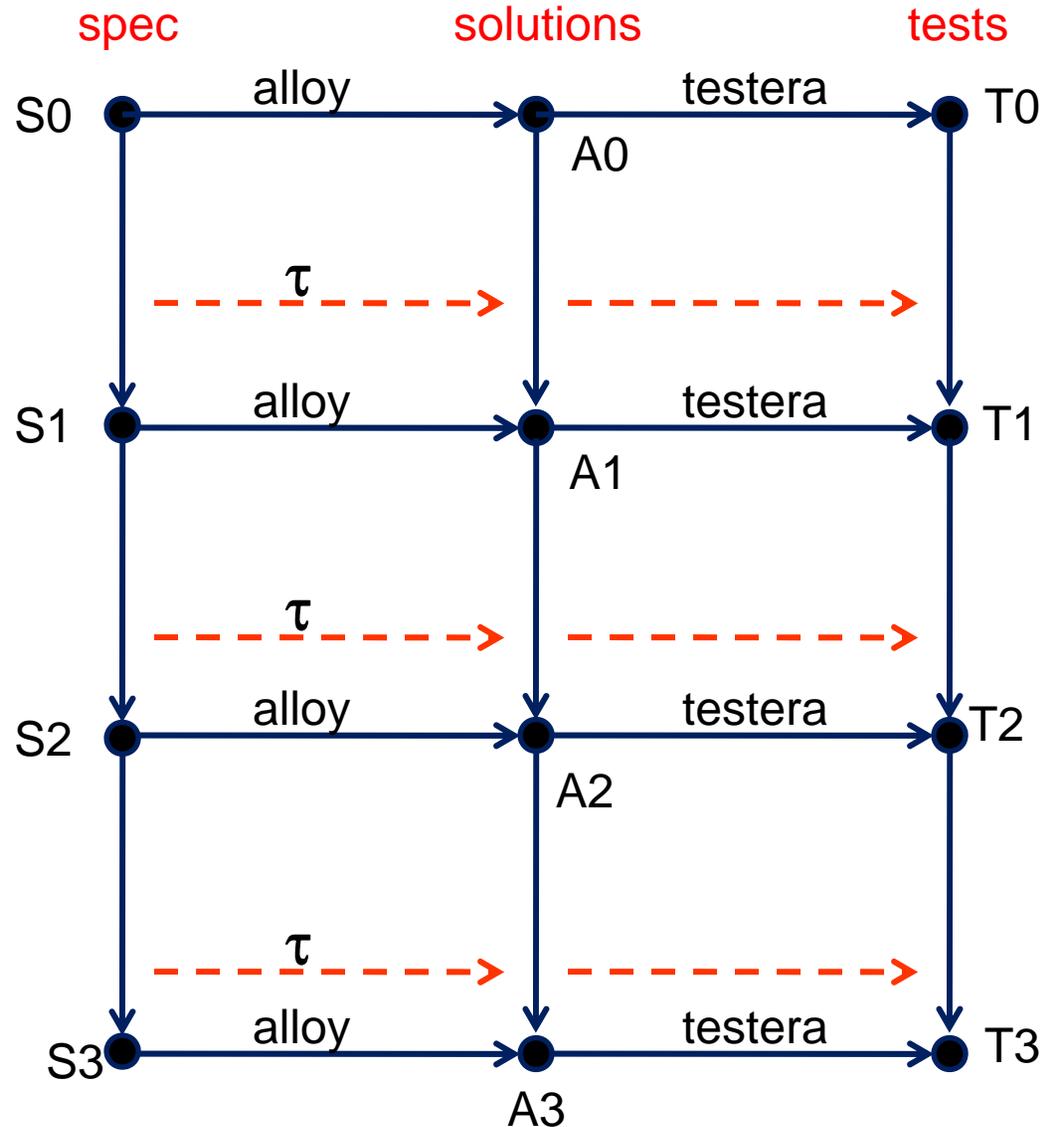
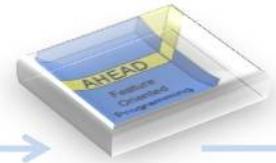
- Initially our tools did not satisfy diagram constraints
 - equalities of homomorphisms didn't hold
 - our tools had bugs – we had to fix our tools
 - now we have greater confidence in tools because they implement explicit relationships of domain models
 - win from engineering perspective
 - » insight into domains that we didn't have before
 - » by imposing categorical structure on our domain, we have better understanding, better models, and better tools
- **Lifting is not specific to our application, it is a general technique for building MDPLs**

Example 2: TSE 2010 Paper



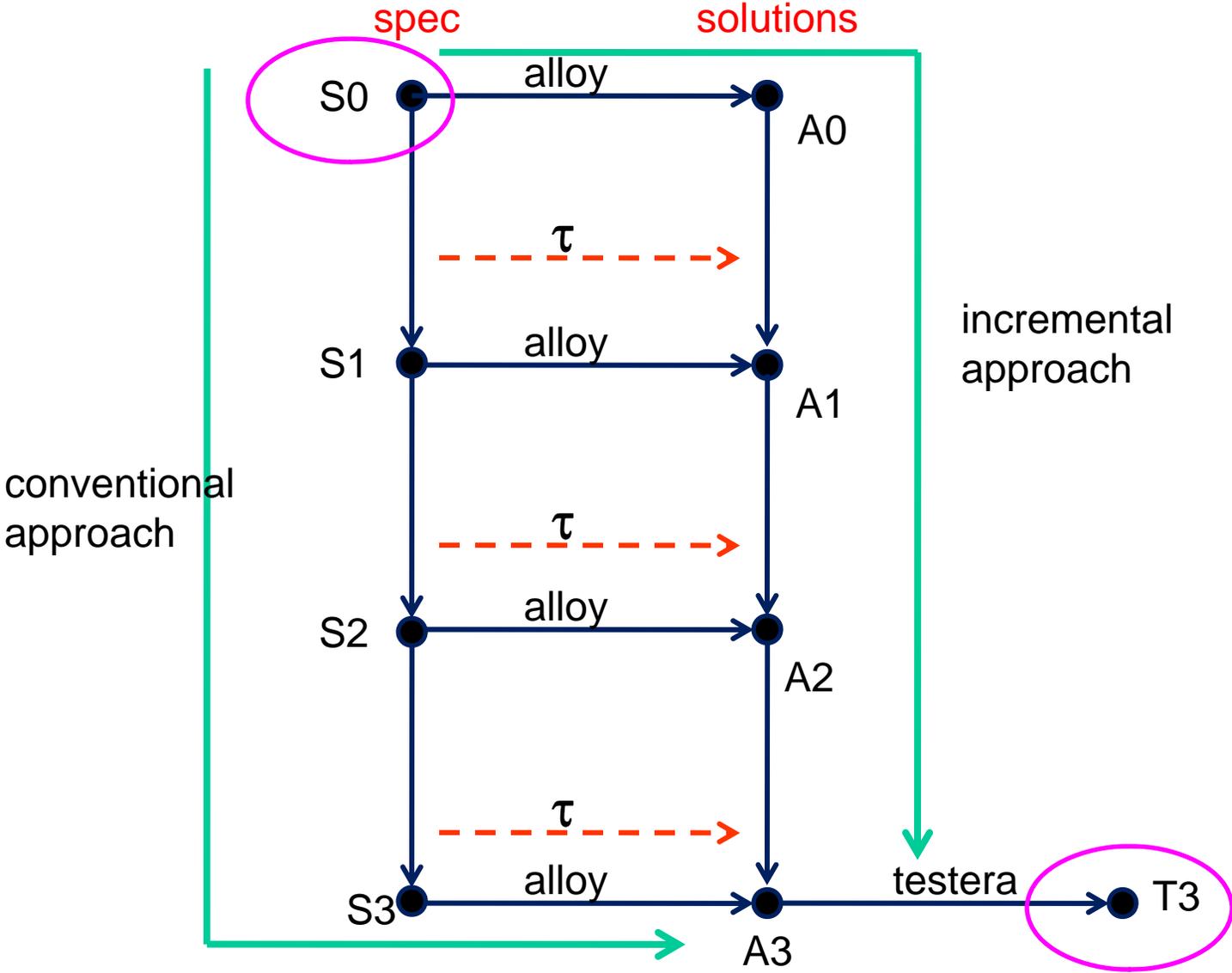
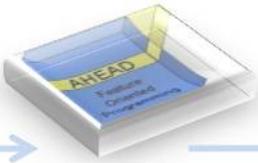
- Work with E. Uzuncaova and S. Khurshid (ECE@UTexas)
- Testing SPLs is a basic problem
 - we can generate different programs, but how do we know that the programs are correct?
- Specification-based testing can be effective
 - start with a spec (model) of program
 - automatically derive tests
 - Alloy is example

Conventional Test Generation

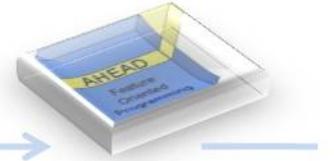


Challenge:
is there
a τ
operator?

Incremental Test Generation



Implementing τ



- Spec S1 = $(A \vee B) \wedge (\neg A \vee C)$ // 20K clauses

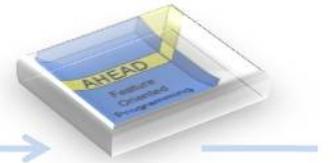
a solution: $[A, B, C] = [1, 0, 1]$

- Spec S2 = $(A \vee B) \wedge (\neg A \vee C) \wedge (D \vee \neg A)$

a solution: $[A, B, C, D] = [1, 0, 1, 1]$

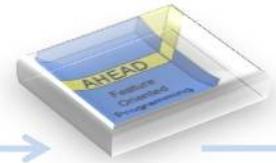
- Solution for S1 “bounds” solution for S2
 - sound, complete
- Reason for efficiency...

Preliminary Results are Encouraging



- In product lines that we examined (typical of Alloy research), majority of cases incremental approach is faster
- 30-50× faster
- can now solve larger problems with Alloy
- See paper(s) for details

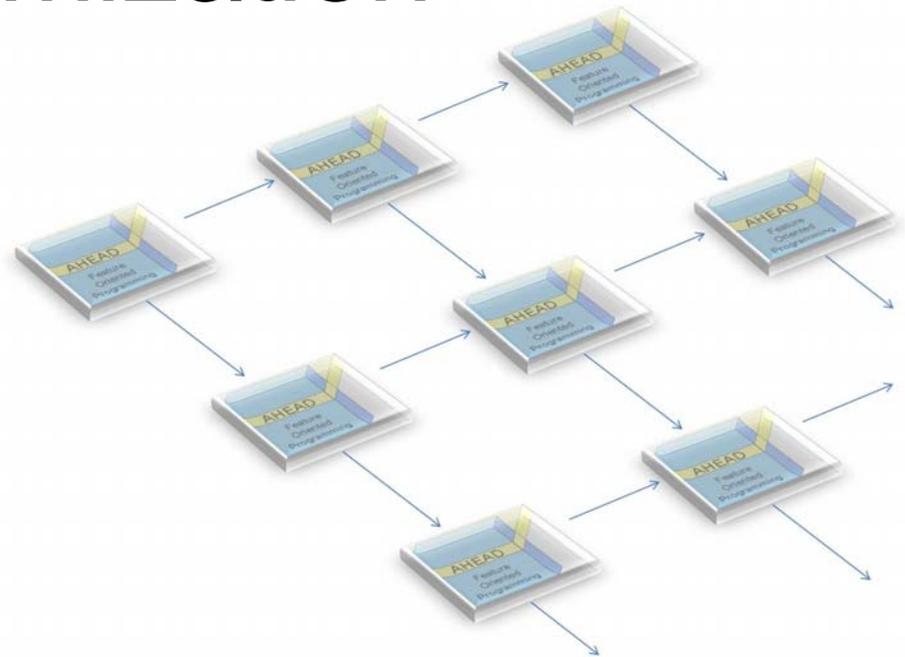
Recap



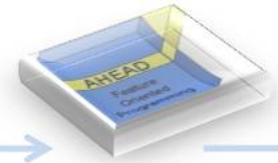
- An SPL or MDE application is an industrial-sized category
- Putting them together reveals foundational ideas of categories – commuting diagrams and functors
 - involves mapping both objects of a category AND arrows
 - need operators (transformation – to – transformation maps)
- Can exploit exposed relationships as
 - verification conditions
 - optimization possibilities

#4: Design Optimization

Frontier of D×T

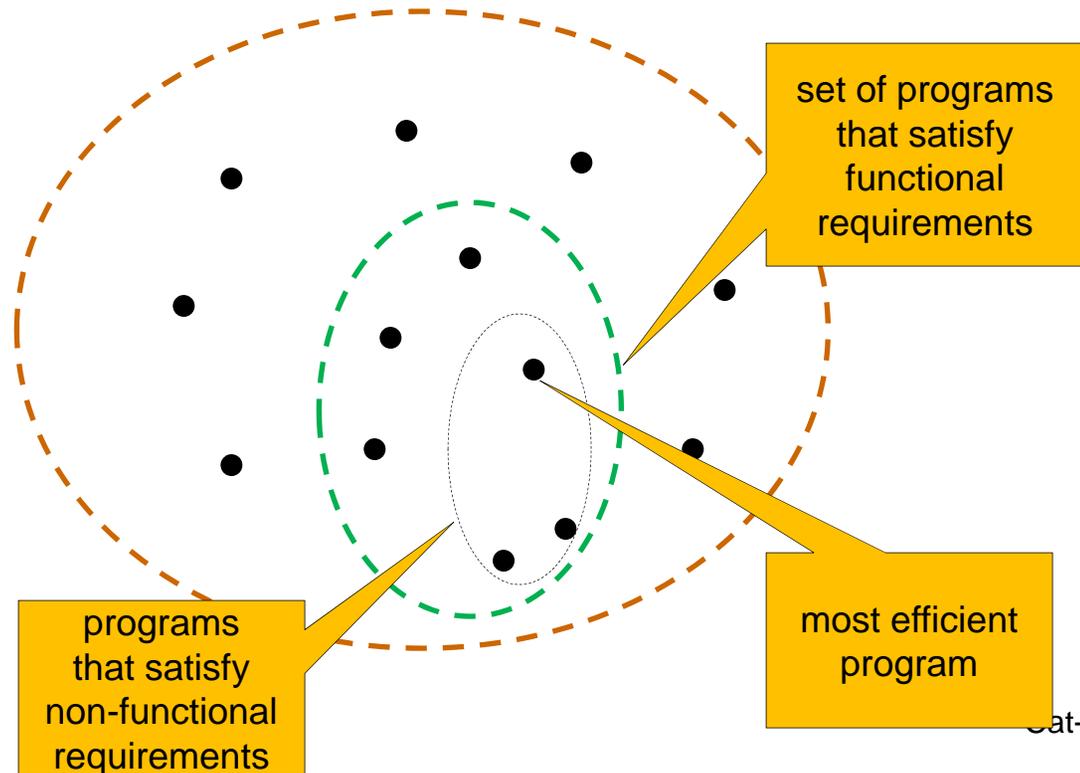


Principles of D×T

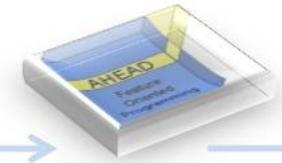


- Design = meta-expression
- Synthesis = meta-expression evaluation
- Design Optimization = meta-expression optimization
 - find program that satisfies functional requirements and optimizes non-functional properties (performance, energy consumption)

paradigm of relational query optimization

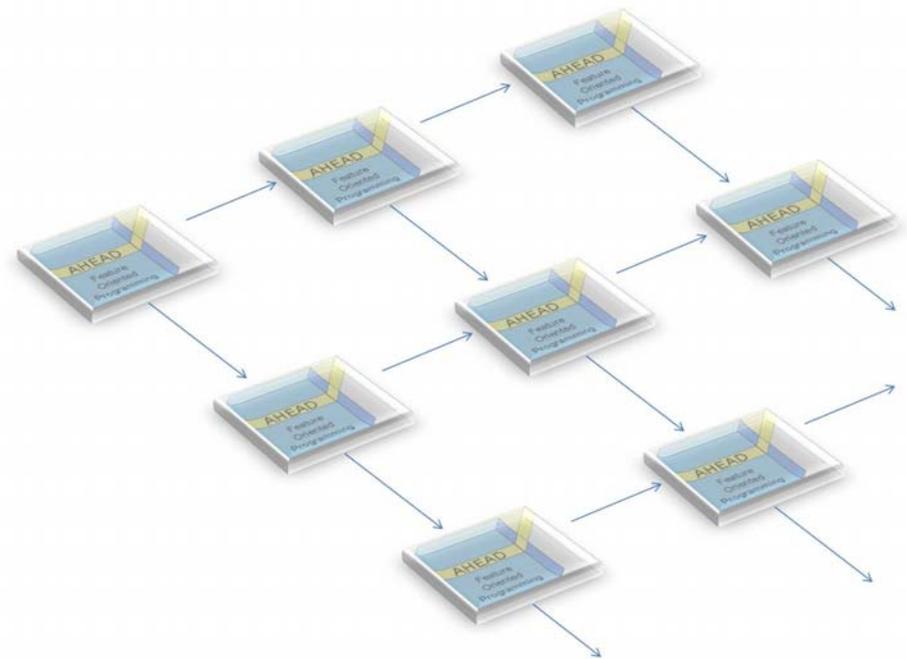


At Present...

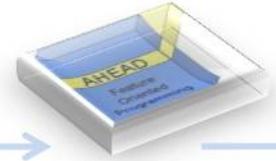


- I know of few examples of design optimization ...
 - relational query optimization (1980s)
 - data structure optimizations (1990s)
 - Neema's work on synthesizing adaptive computing (2001)
 - Püschel's & van de Geign's numerical library synthesis (2006)
 - Benavides work on configurators (2005)
 - ...
- Main challenge: finding domains where there are different ways to implement the same functionality
 - commuting diagrams
 - this is where design optimization occurs
- If you think in terms of arrows, you have a conceptual framework and tools to explain and address design optimization in a principled, non-ad hoc way

Conclusions

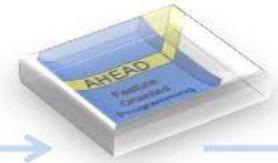


Role of Mathematics in Design



- RQO helped bring database systems out of stone age
- Relational Model was based on set theory
 - this was the key to understanding a modern view of databases
 - set theory used was shallow
 - fortunate for programmers and database users
 - set select, union, join, intersect
 - disappointment for mathematicians
- **D×T** uses category theory
 - provides a language to express our results
 - places research results in context
 - new insight on verification, optimization issues
 - whether theorems from CT are applicable, I don't know

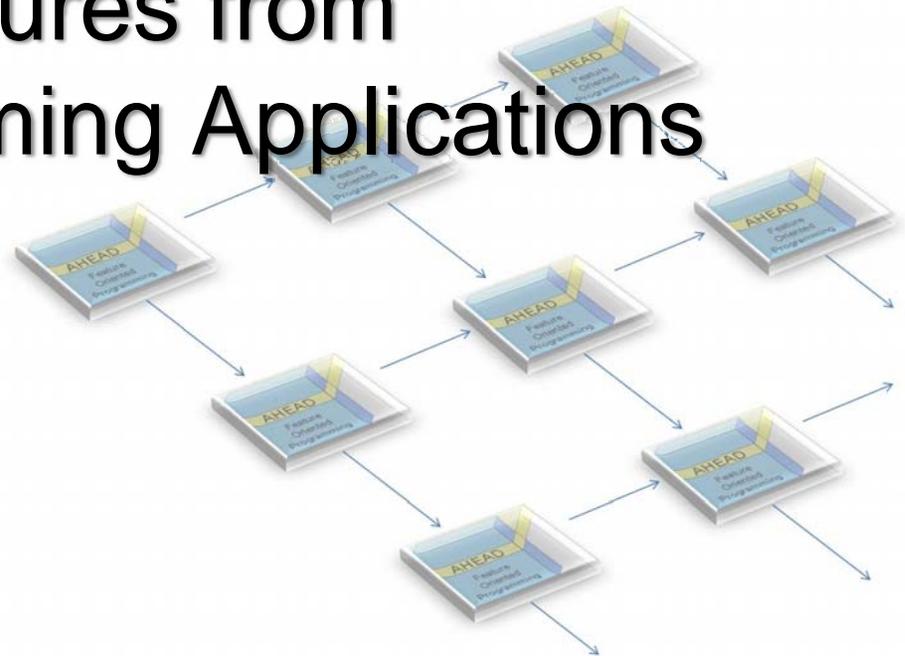
Key To Success



- Educational benefit of the connection
 - common and simple language
 - offers new perspectives
- How often in MDE, SPL, MDPL do commuting diagrams arise?
 - don't know; too early
 - but if you look, you'll find them
 - theory says they exist
 - whether creation of operators practical depends on domain

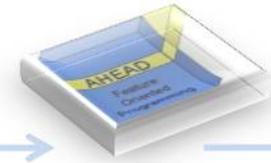
Look for Them!

Lecture 3: Extraction of MDE Architectures from Parallel Streaming Applications



work with Taylor Riché

Introduction

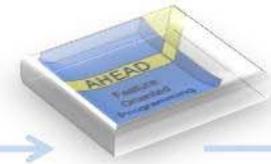


- Challenge of re-engineering complex streaming applications into a component-and-connector architecture
 - to eventually re-implement on a MDE platform

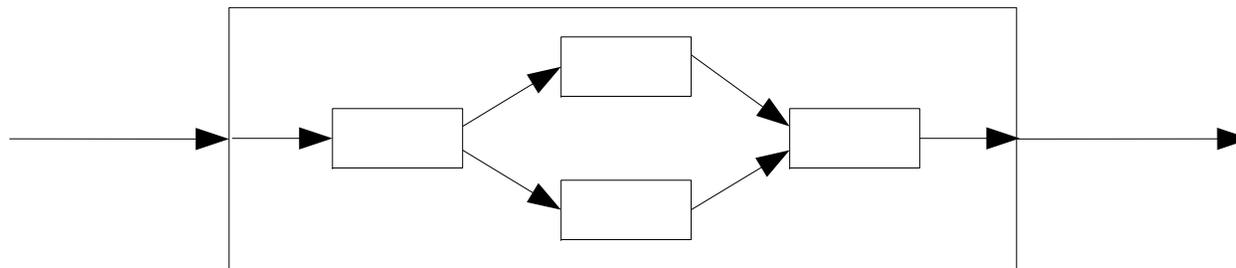
Asynchronous Crash Fault Tolerant (ACFT) servers
Classic Parallel Join of DBMS machines

- They were so complicated, we needed a way to convince ourselves and others that we understood their designs
 - we were not domain experts – not obvious how and why they worked
- We needed a structured way to explain and build our versions of these systems

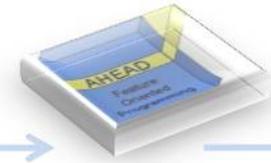
Stepwise Development (SWD)



- Classical & fundamental way to control design complexity
 - our work builds on results of a long line of pioneers (Labview 80, Gorlick 92, Broy 92, Moriconi 94, Garlan 96, Rumpe 97, Kong 03, Clarke 06, ...)
 - use a standard component-connector model of application
 - elaborate it by simple transformations called **refinements**

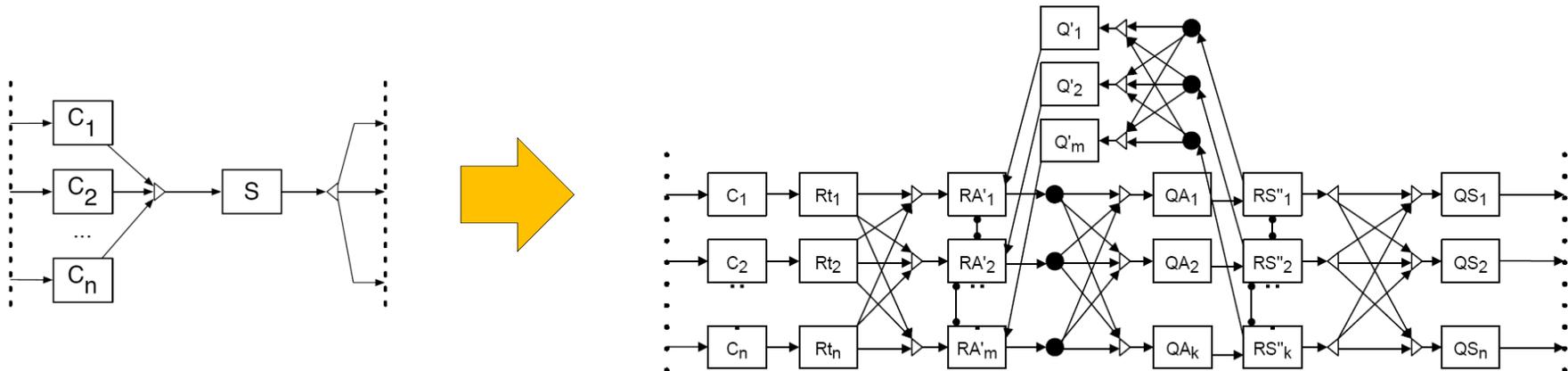


Re-Engineering Result

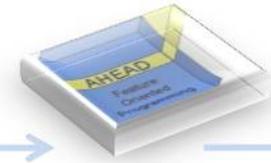


• Model Driven Engineering (MDE) Architecture

- start with executable model of a sequential component-connector architecture
- transform it by **refining**, **optimizing**, **extending** to derive an executable parallel architecture that faithfully captures decisions made by domain experts
- result is easy-to-understand **description** + **prescription** to recreate system on an MDE platform

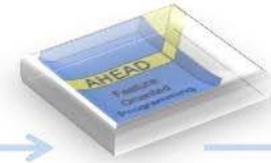


Perspective



- Case Studies are known for their contributions to fault-tolerance and database machines
 - designs were never conceived in terms of transformations
 - novelty of their designs can be expressed by transformations
 - why certain transformations use is part of genius of their designers
- No substitute for domain expertise
 - we use transformations to encode deep domain knowledge
 - express designs by transformations is novel to domain-experts, but the end result is rarely surprising
 - progressively revealing details is so straightforward that even non-domain experts (undergraduates) can follow along
 - although our descriptions are deceptively simple, it takes effort
 - ideal for teaching complex designs to others

Connection to Prior Lectures

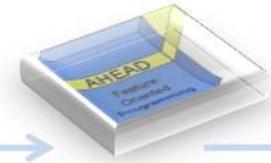


- Incremental Design = SWD
- Express designs by compositions of transformations

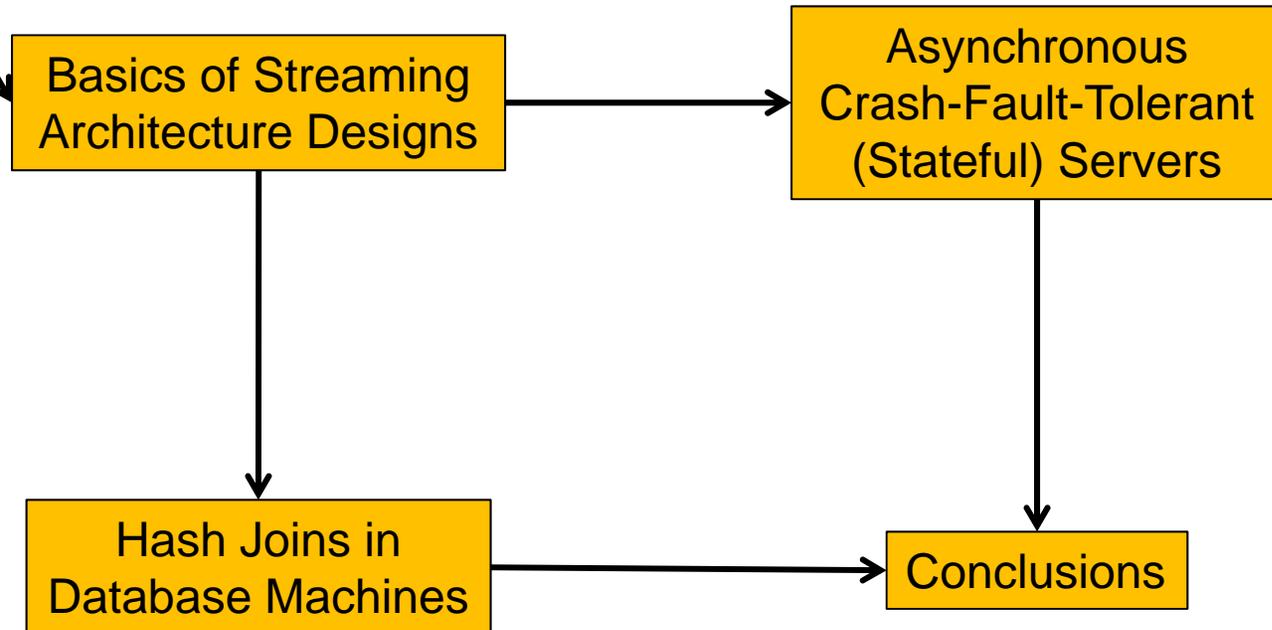
Design by Transformation

- You'll see elements of product lines, commuting diagrams, and MDE all integrated this lecture

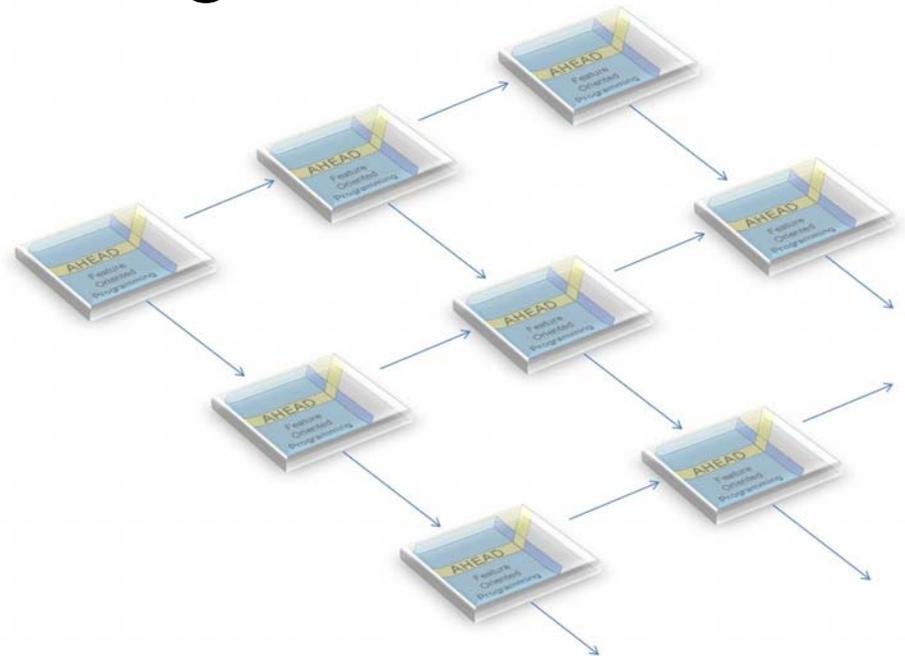
Series of Mini-Presentations



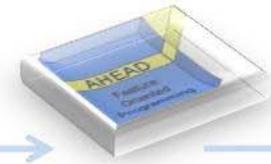
we
are
here



#1: Basics of Streaming Architectures



Basics



- **Component-Connector Architecture** is a directed graph
 - box component or computation
 - connector communication path for messages, tuples drawn in direction of data flow
- Semantics of box is clear from context

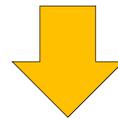
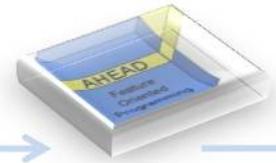


1, 50, 2, 62, 53

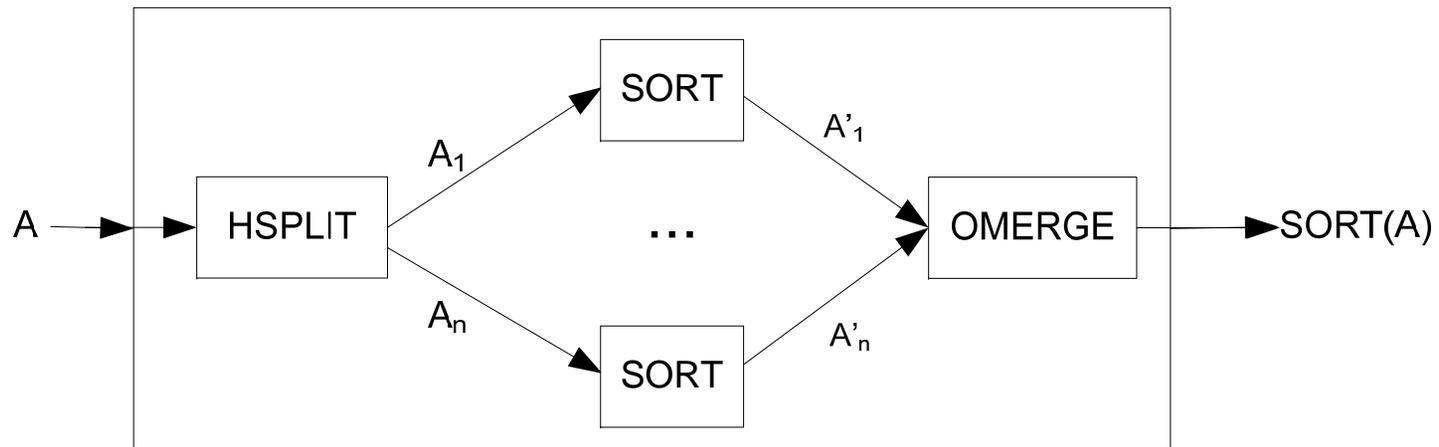
1, 2, 50, 53, 62

- Elide unnecessary details (sort key, sort order, sort type)

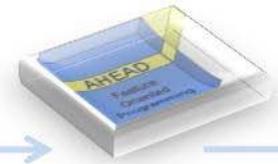
Refinement



map-reduce
parallelizing
refinement



Transformations



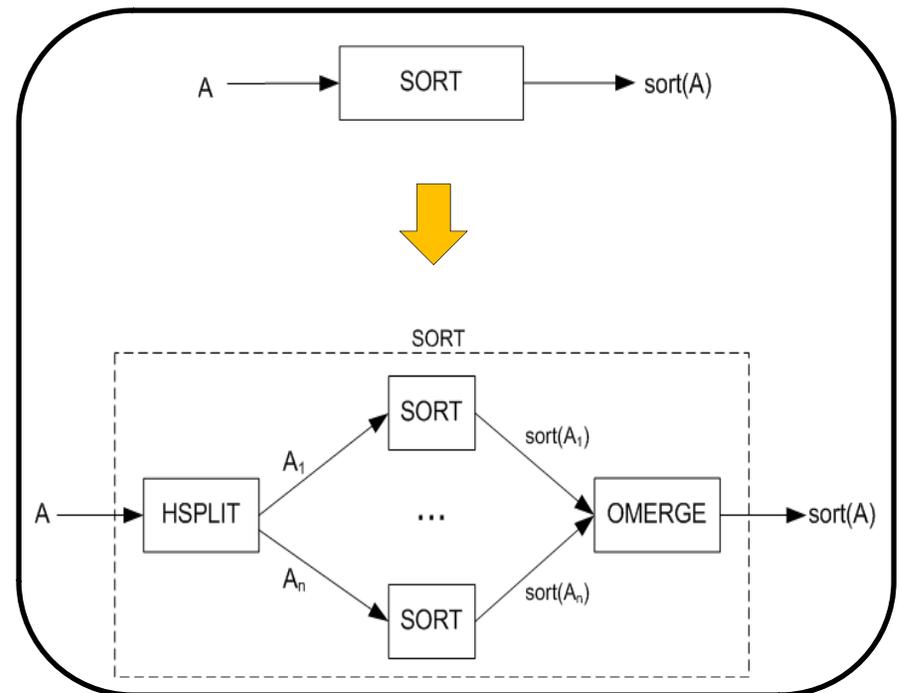
- Refinement is a **transformation**

- input pattern \rightarrow output pattern

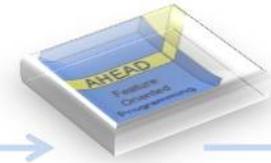
- All **transformations** or compositions of xforms in this talk have been proven correct

- simple enough that intuition suffices
- sometimes need Ph.D.

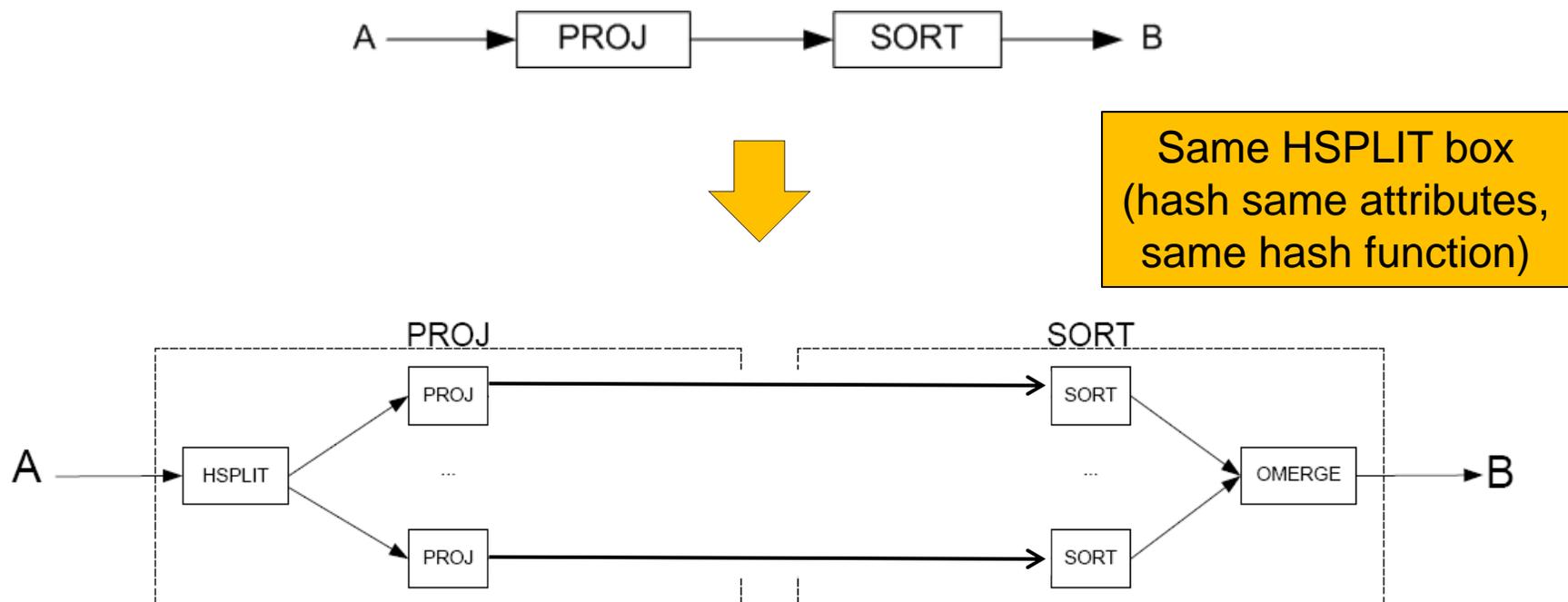
- **Correct by Construction**



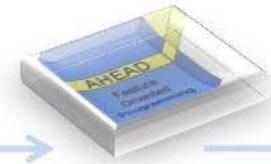
Optimizations



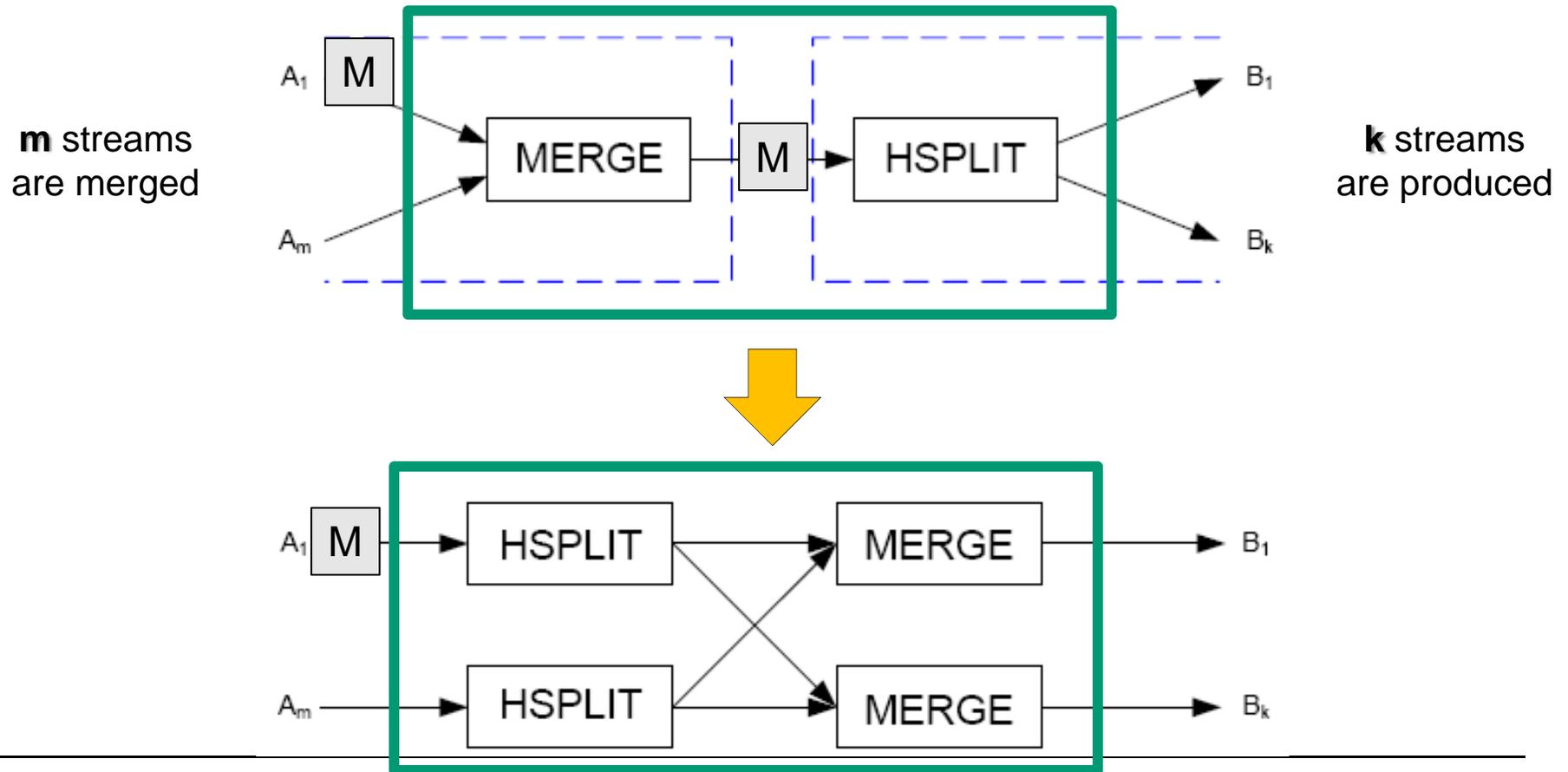
- Break encapsulations to achieve non-functional properties
 - efficiency or availability



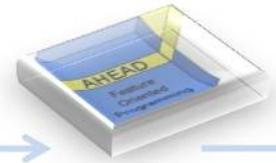
Rotations



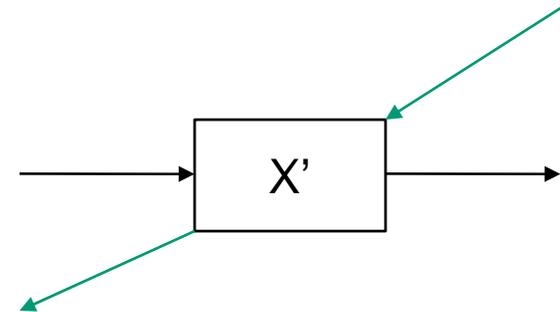
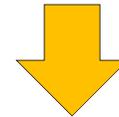
- Optimizations that reorder *stateless* computations
 - ex: property that each A_i message is assigned to a single B_j stream



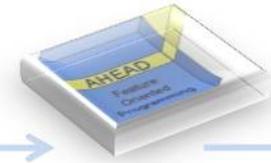
Box Extensions



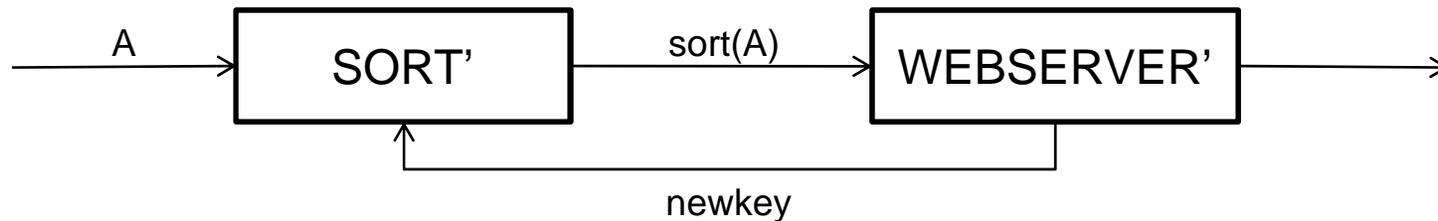
- Extend the capabilities (semantics) of a box
- Extensions add “features”
- Accomplished by preprocessors
#ifdef inclusion of extra code
- Or by more sophisticated means



Model Extensions

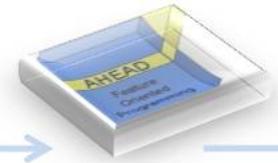


- Example: Webserver takes sorted tuples and creates a web page of sorted results

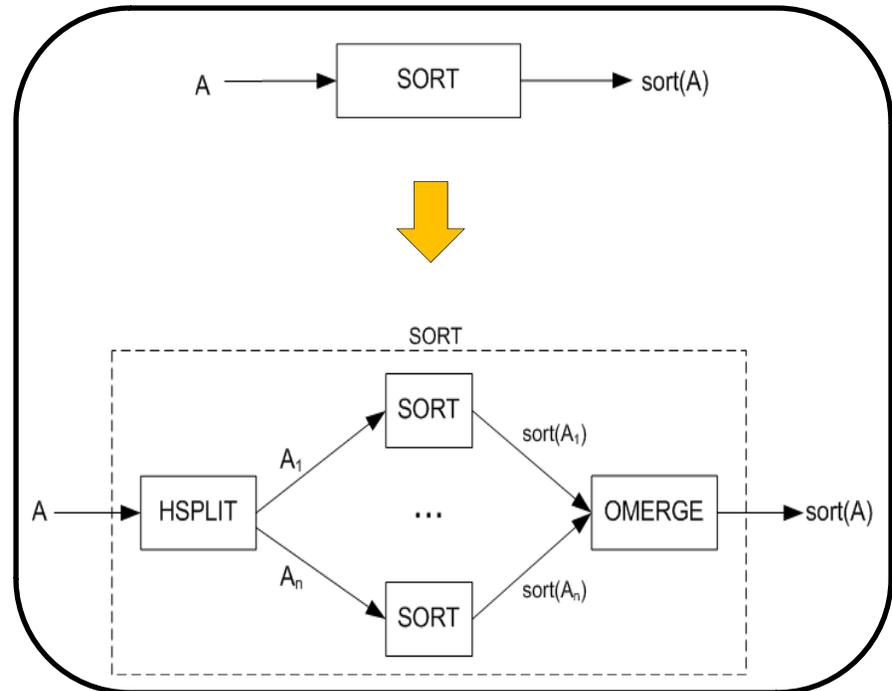


- Extend Webserver & Sort with new ports and add a feedback data flow called newkey which changes the key that sort uses
 - switching from artist names to album titles
 - switching from last names to SS#

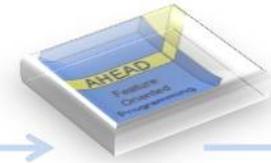
Always Executable



- User supplies boxes and tests for boxes
- Can reuse tests for boxes after refinement
 - logically cannot distinguish input-output response of a single SORT box from its parallel counterpart
- Similar arguments for extensions and optimizations

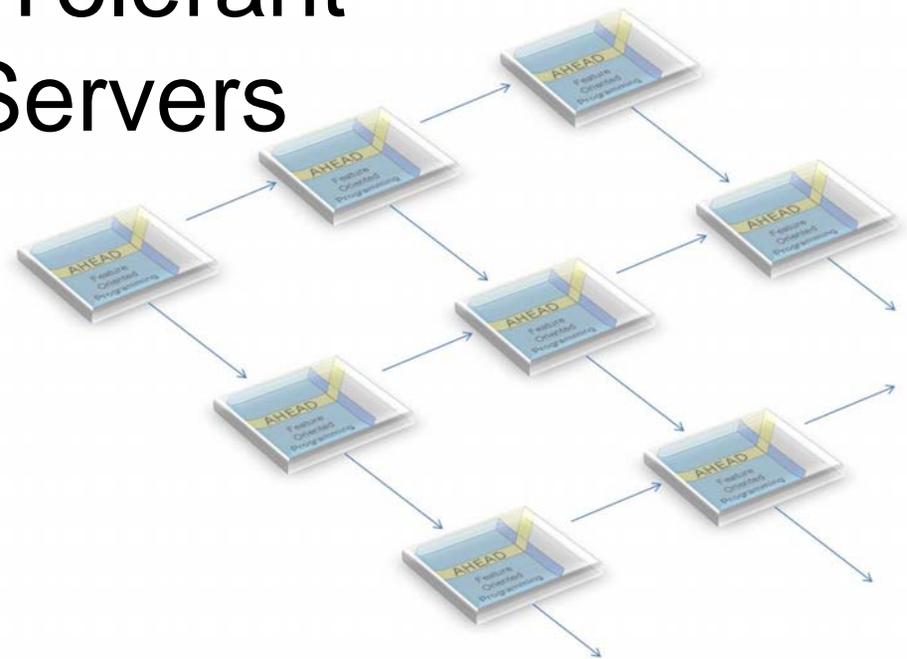


Recap

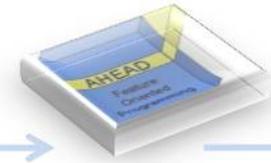


- Component-connector architecture is implementation model
 - transformations progressively elaborate models by refinement, extension, or optimization
 - result is always executable
- Now, let look at some examples...

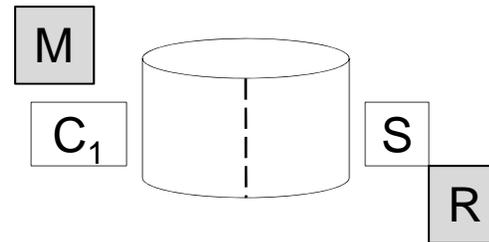
#2: Asynchronous Crash-Fault-Tolerant (Stateful) Servers



Overview

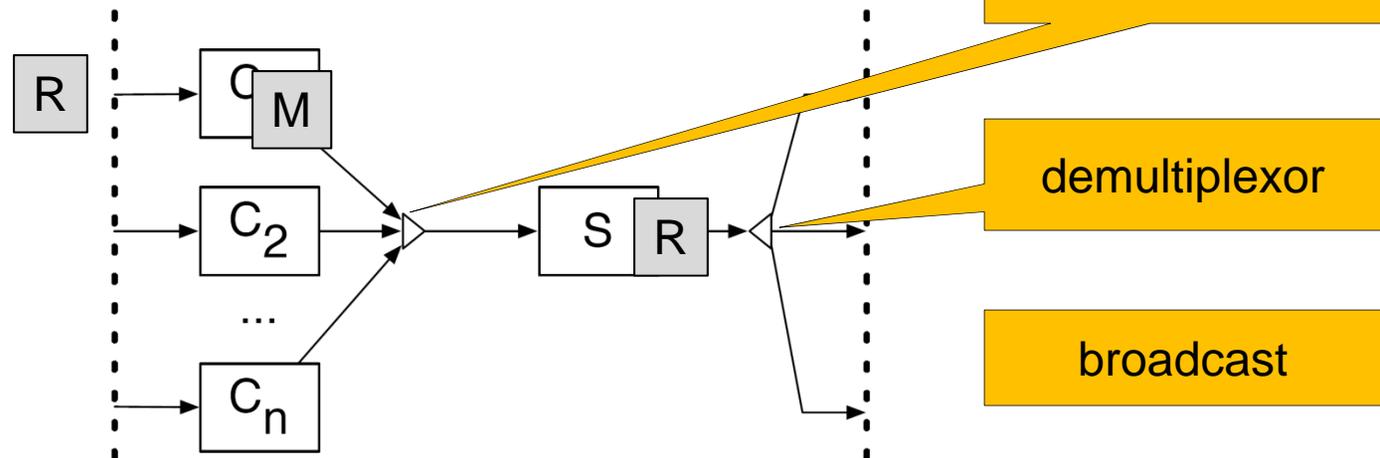


- Sequential server architecture has a cylinder topology

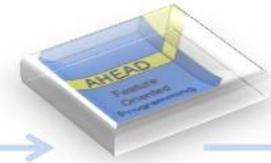


assume server updates state

- Unroll cylinder by breaking along the seam



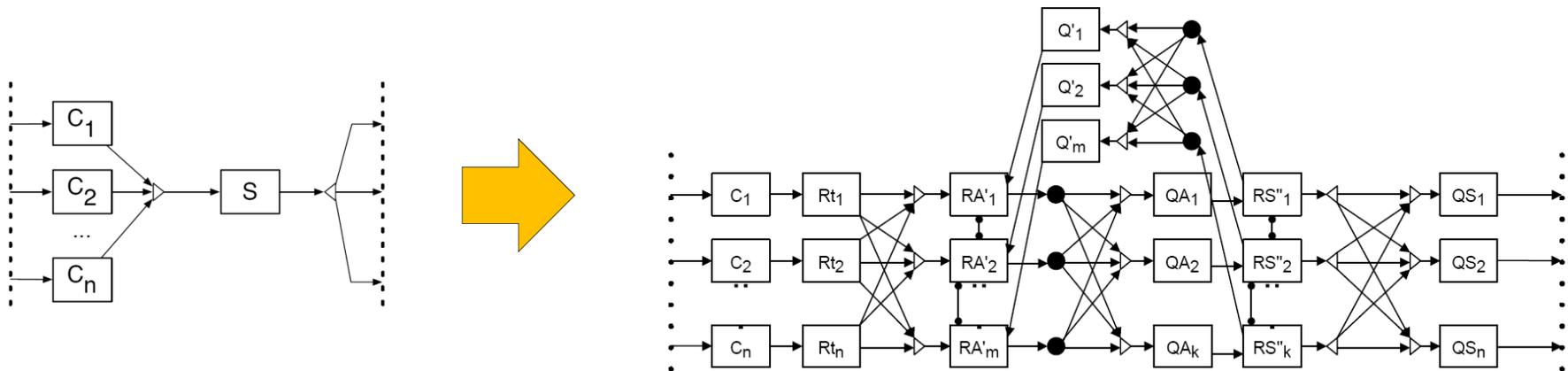
Our Goal



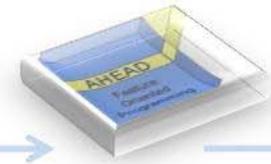
- Transform a (stateful) server that works in the ideal world of synchronous networks and no box failures to an

Asynchronous, Crash-Fault-Tolerant (stateful) Server

- consider Synchronous CFT transformations first
- Asynchronous (recovery) transformations last

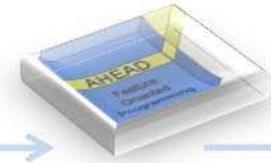


Basics on Crash-Fault-Tolerance



- Ability of a server to survive a number of failures
- **Failure** – when a box stops processing messages
 - no messages pass through a failed box
 - a failed box cannot create new messages
 - *assume each box executes on its own machine*
 - multiple boxes can run on single machine
 - if machine fails, all boxes on that machine fail
 - failures do not propagate across machine boundaries

Standard Failure Assumptions



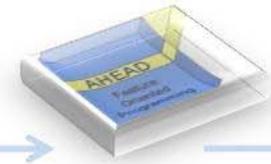
- Failures of network components

serializer (◀)
demultiplexor (▶)
reliable broadcast (•)

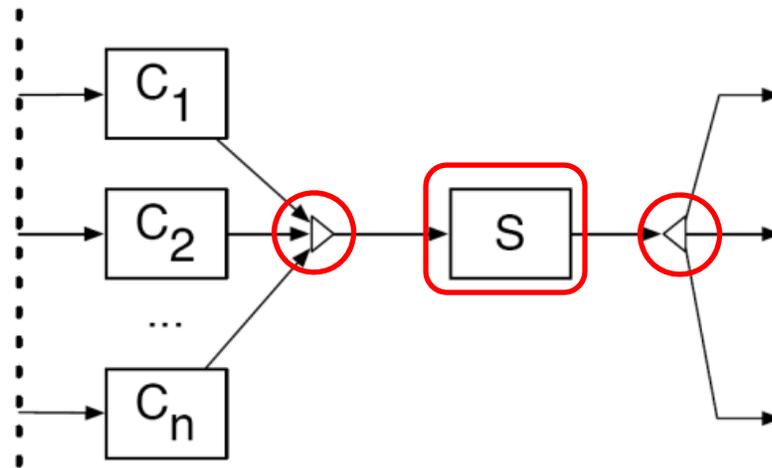
affect a machine the same as pure software boxes

- ex: a machine can't process requests if its network card stops working
- Ultimately we not depend on synchronous networks
 - do expect eventual synchrony
 - use **retransmissions** (in application, network protocol, or both) to deal with transient packet loss
- Requests are benign; BFT removes these assumptions

Technical Goal of CFT

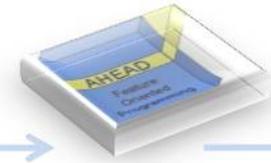


- Eliminate **Single Points of Failure (SPoF)**
 - a failure of a single box (machine) causing the server abstraction to fail
 - our current design has 3 SPoFs

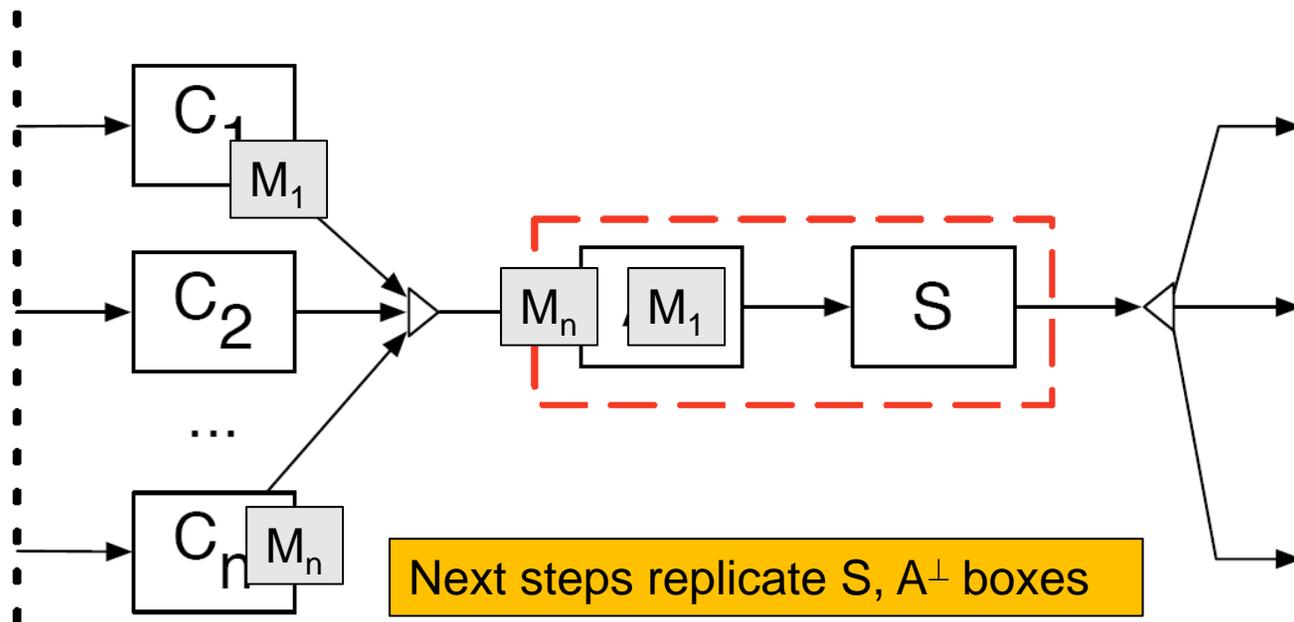


- “Solve” problem by replicating boxes
 - not only solution – we follow most advanced solution to date
 - appeared in SOSP 2009

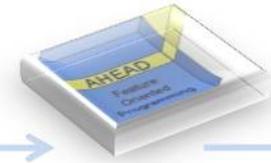
Step 1: Agreement



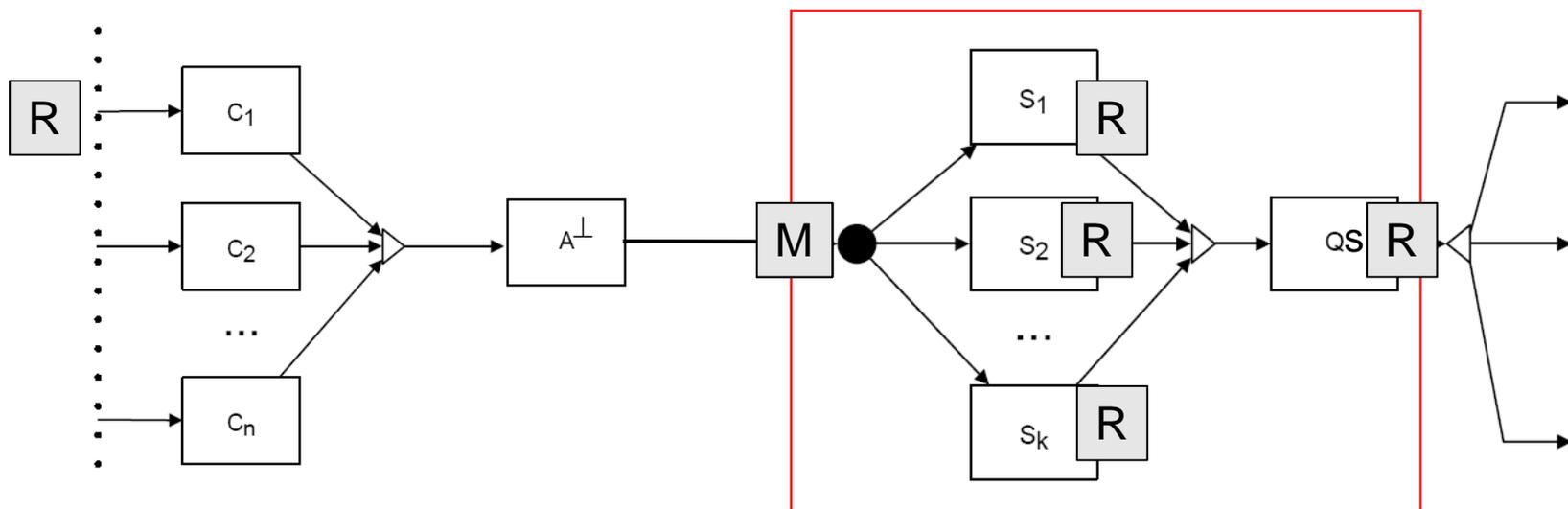
- Add an agreement node A^\perp
- A^\perp materializes implicit network message queue, passing messages one at a time to the server
- In effect, A^\perp does nothing it is a place holder for later refinements



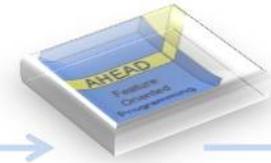
Step 2a: Replicate Servers



- Make k copies of server
- Each server receives exactly the same sequence of messages from the A^\perp abstraction
- QS collects a quorum of identical messages;
transmits message when a sufficient number of copies are received
- *Refinement emulates abstraction of a single correct server*



Why are k Server Replicas Needed?

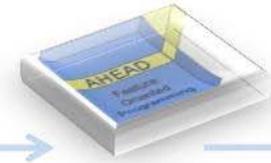


- To tolerate failures of server boxes

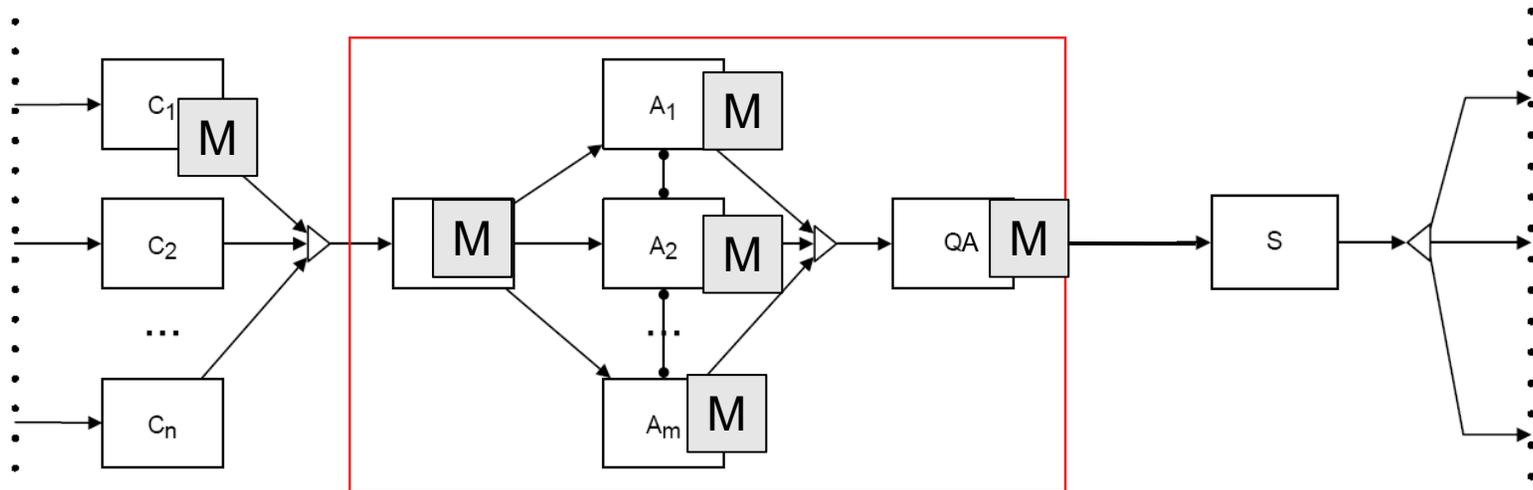
tolerate f failures, $k = f + 1$

- See: *J. Yin, J-P. Martin, A. Venkataramani, L. Alvisi, and M. Dahlin. “Separating Agreement from Execution for Byzantine Fault Tolerant Services”, SOSP 2003.*

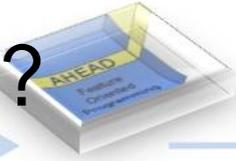
Step 2b: Replicate A^\perp Boxes



- Make m copies of A^\perp
- Client requests are routed by box R_t to *some or all* A replicas
- A replicas run an **agreement protocol** (Lamport 1998) to decide which is the next client message to process
- A replicas vote and a quorum is taken by QA ; when a sufficient number of identical messages is received, QA forwards a single message
- *Refinement emulates abstraction of a single queue*



Why m Replicas of A are Needed?

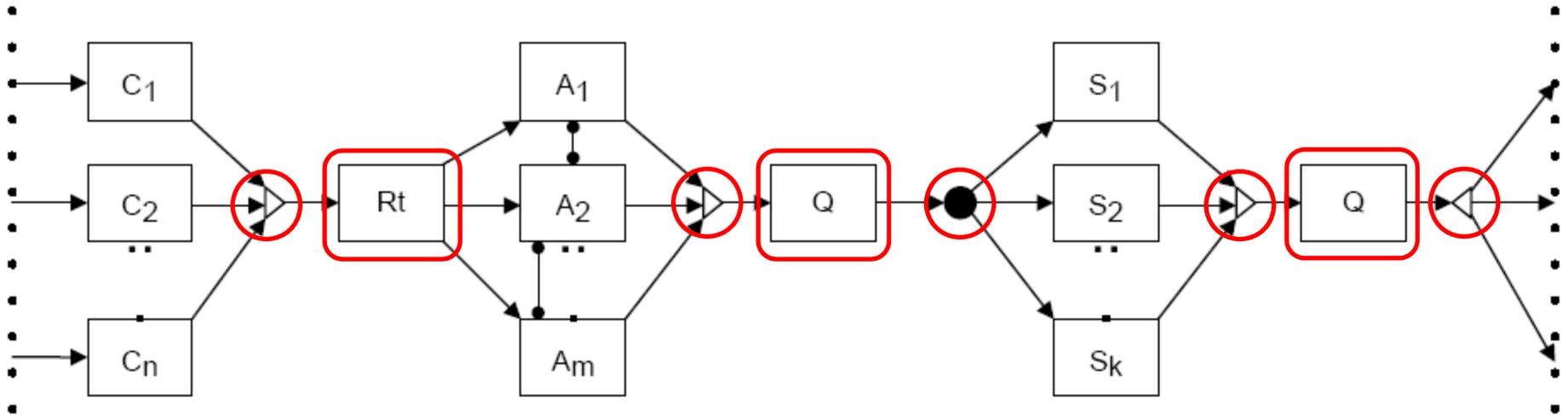
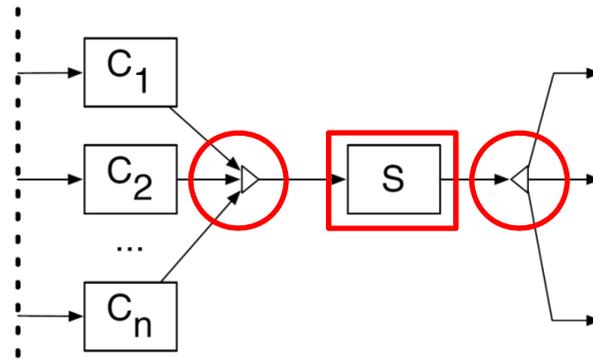
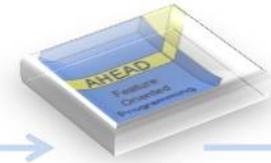


- Ans#1: tolerate failures of A boxes

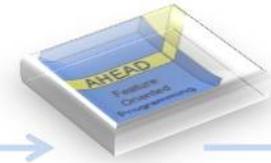
tolerate f failures, need $m = 2f + 1$

- Ans#2: a consistent order of requests is essential for correct server behavior
- If S replicas processed client requests in different orders, server replica states would diverge and responses from different servers for a single client request would be inconsistent
- Inconsistencies violate the one-correct-server abstraction

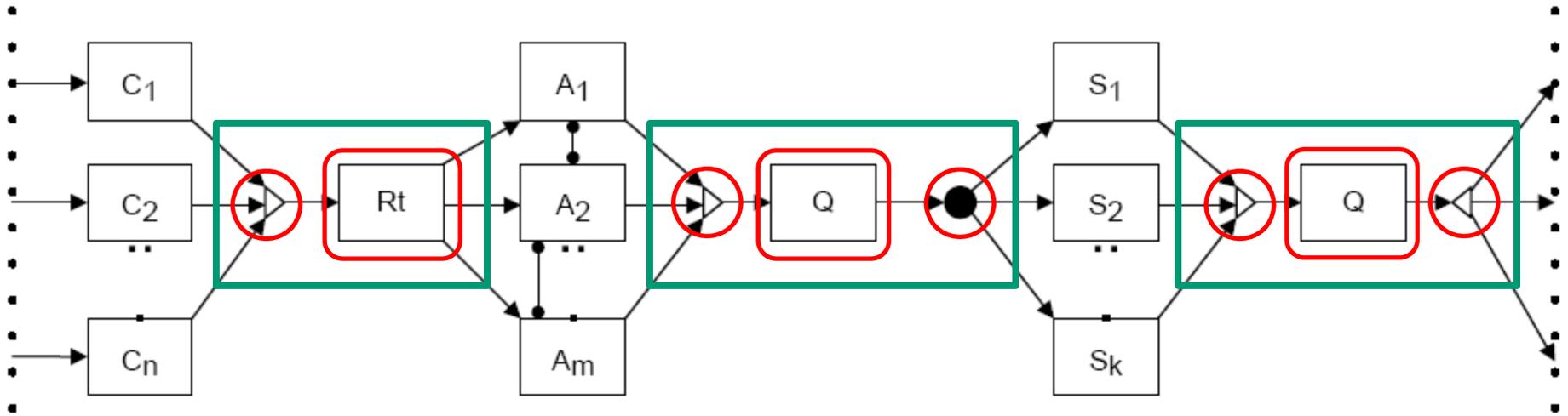
Where We Are...



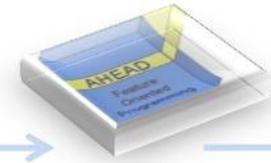
Where We Are Going



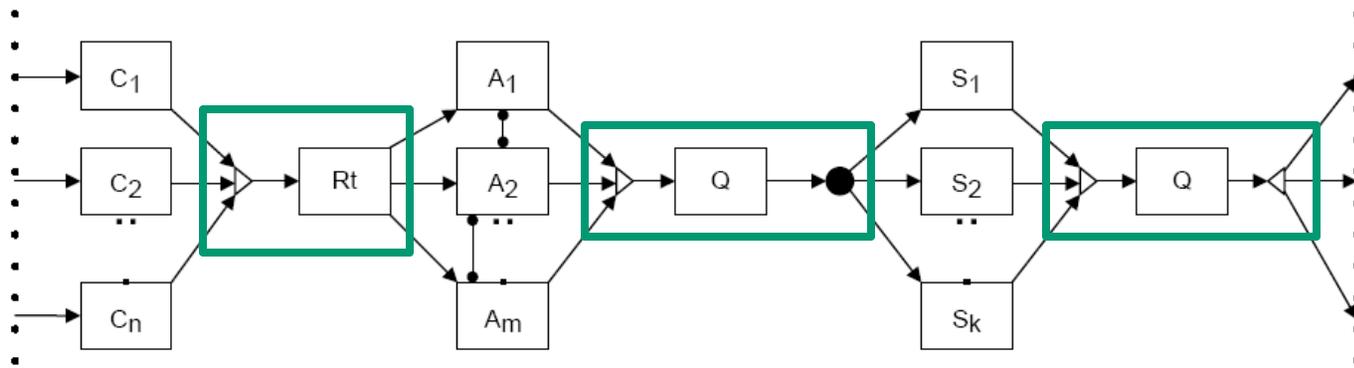
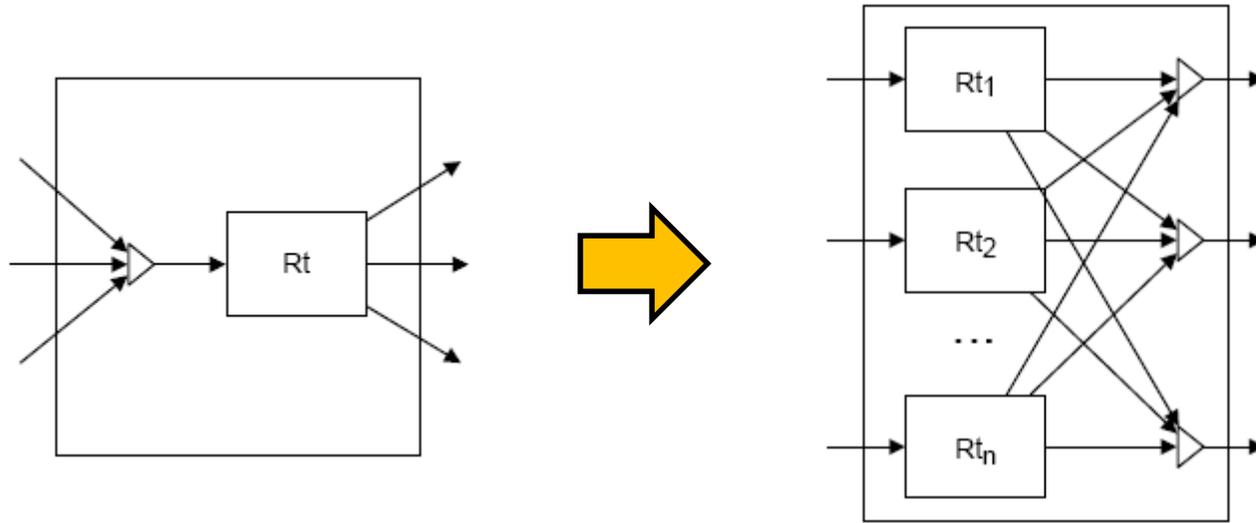
- Dissolve existing module boundaries
- Define new (green) abstractions
- Apply rotations to eliminate SPoFs



Step 3a: (\blacktriangleright, R_t) Rotation



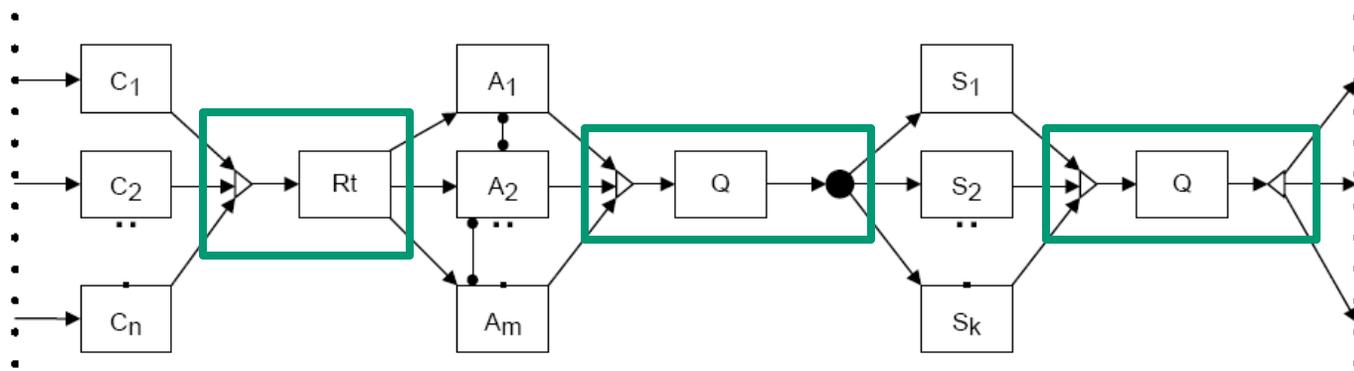
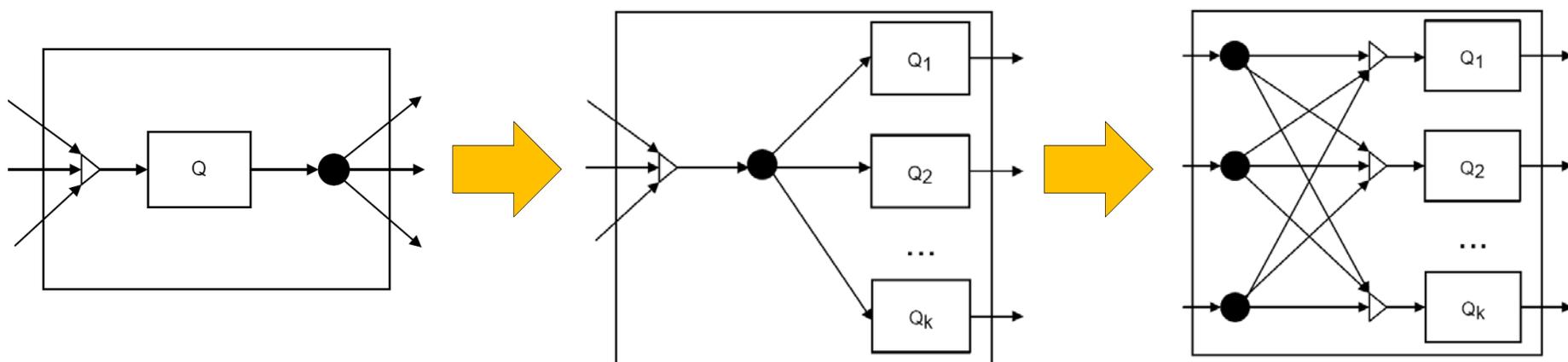
- Each client request is sent to a subset of A replicas



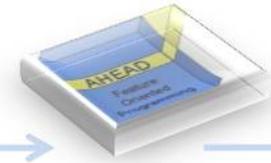
Step 3b: (►, Q, •) Rotation



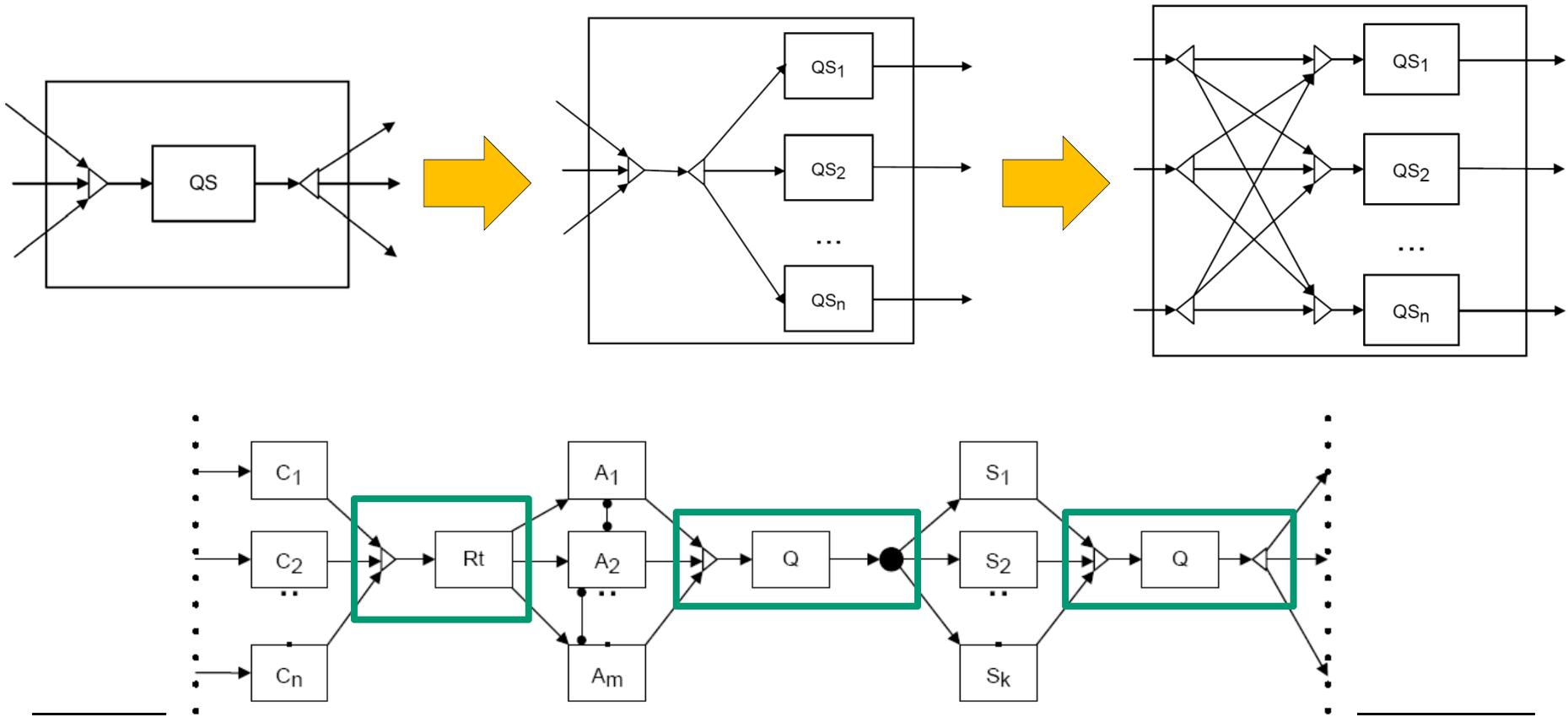
- Each quorum-decided request from replicated A boxes is delivered to all Server replicas



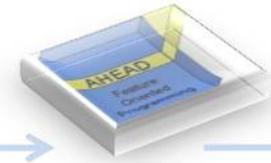
Step 3c: (►, QS, ◀) Rotation



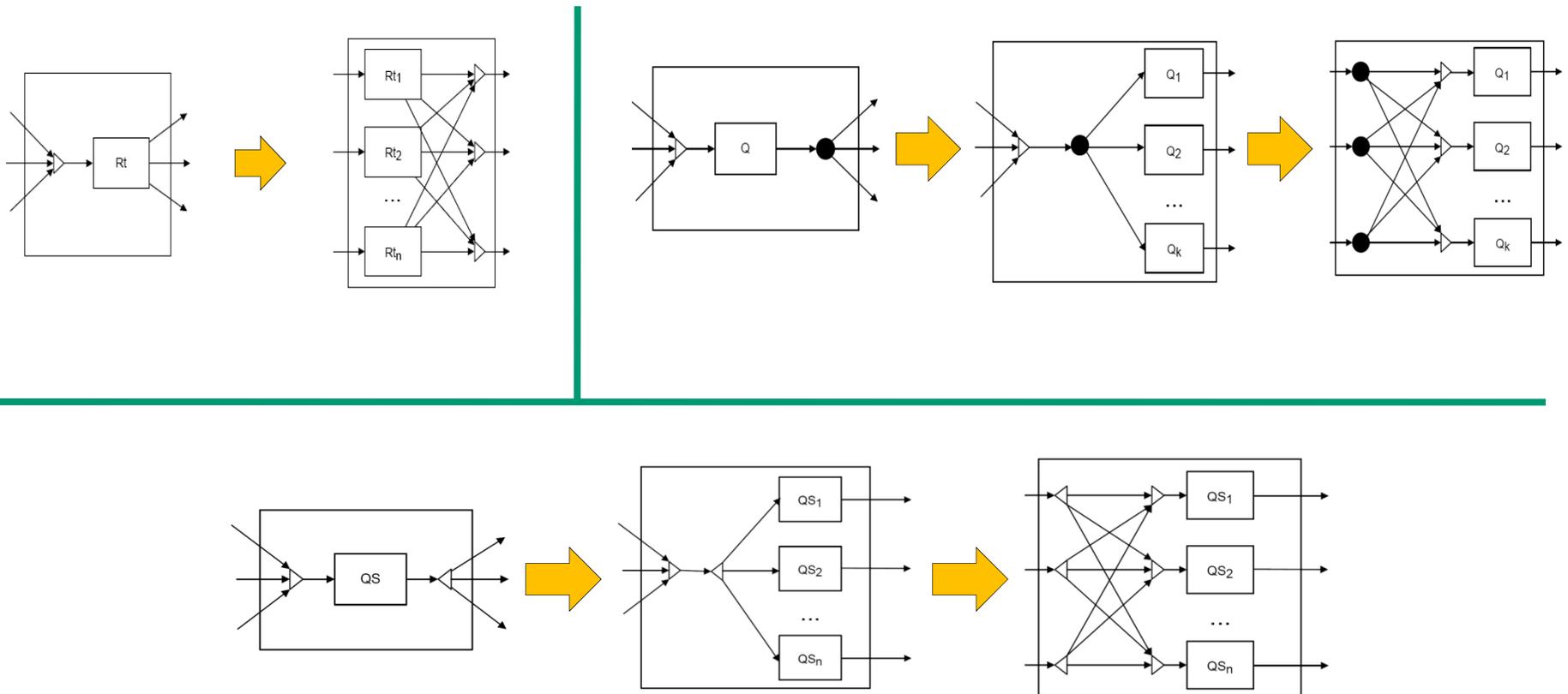
- Each quorum-decided response from replicated S boxes is received by a client box



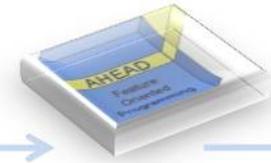
Why So Simple?



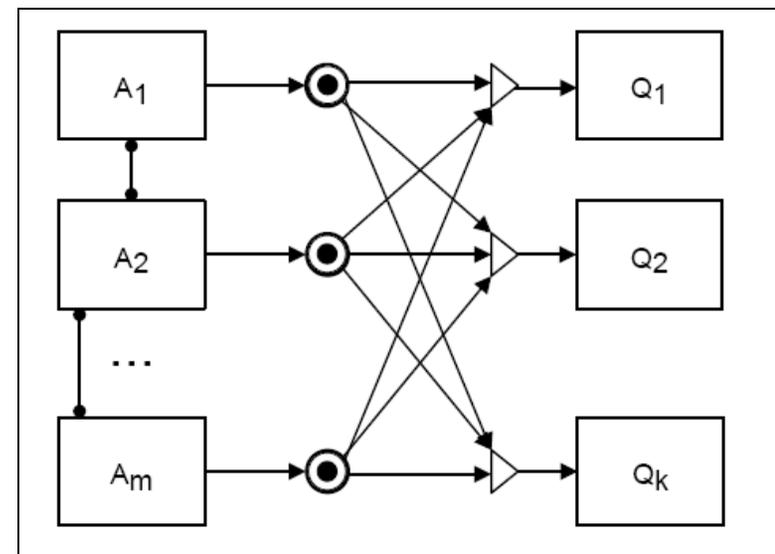
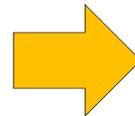
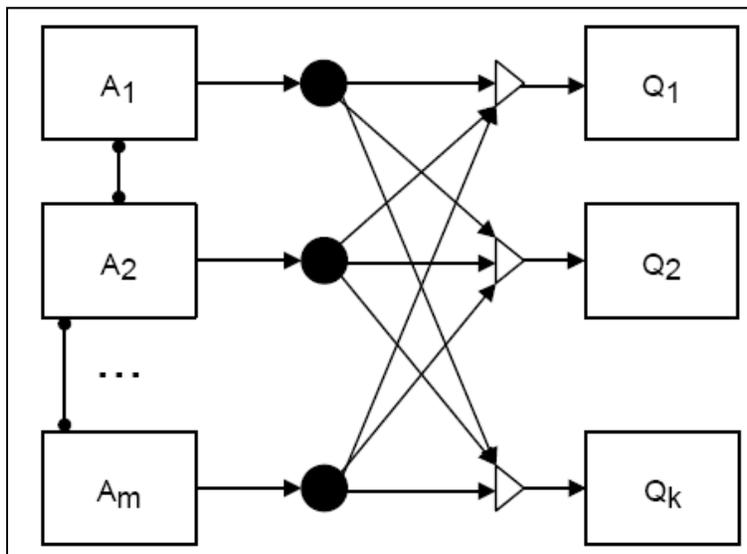
- All rotations involve stateless computations
 - state would require a heavy-weight solution (agreements, etc.)



One More Optimization

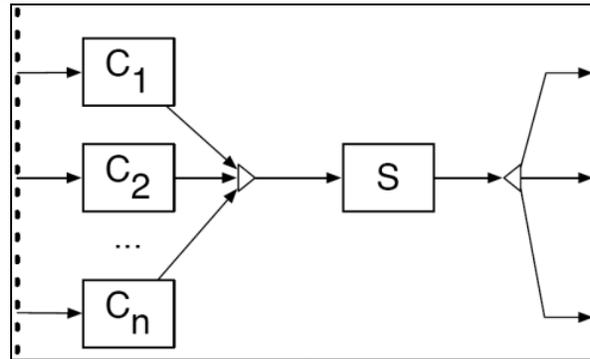
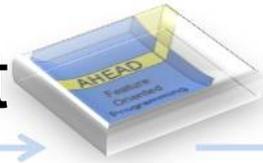


- Reliable broadcast is very expensive
- Under the right conditions (e.g., quorums) reliable broadcast (●) can be replaced with unreliable broadcast (⊙) which is easy to implement

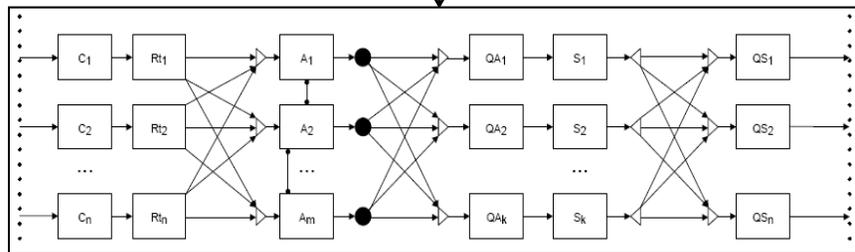


standard way to implement
an efficient, reliable crossbar

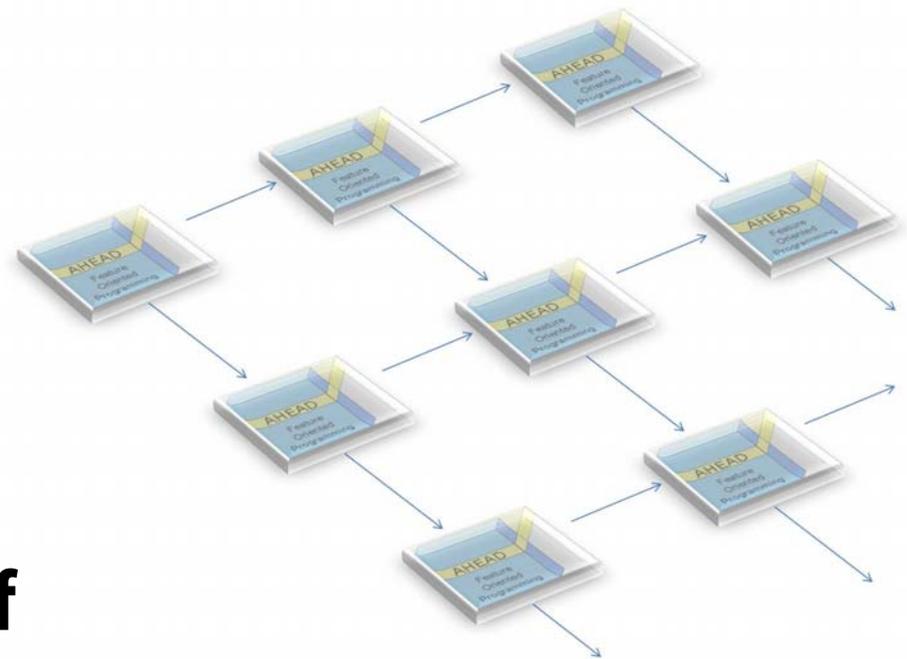
Final Synchronized CFT Result



No SPoF

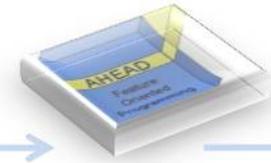


SCFT



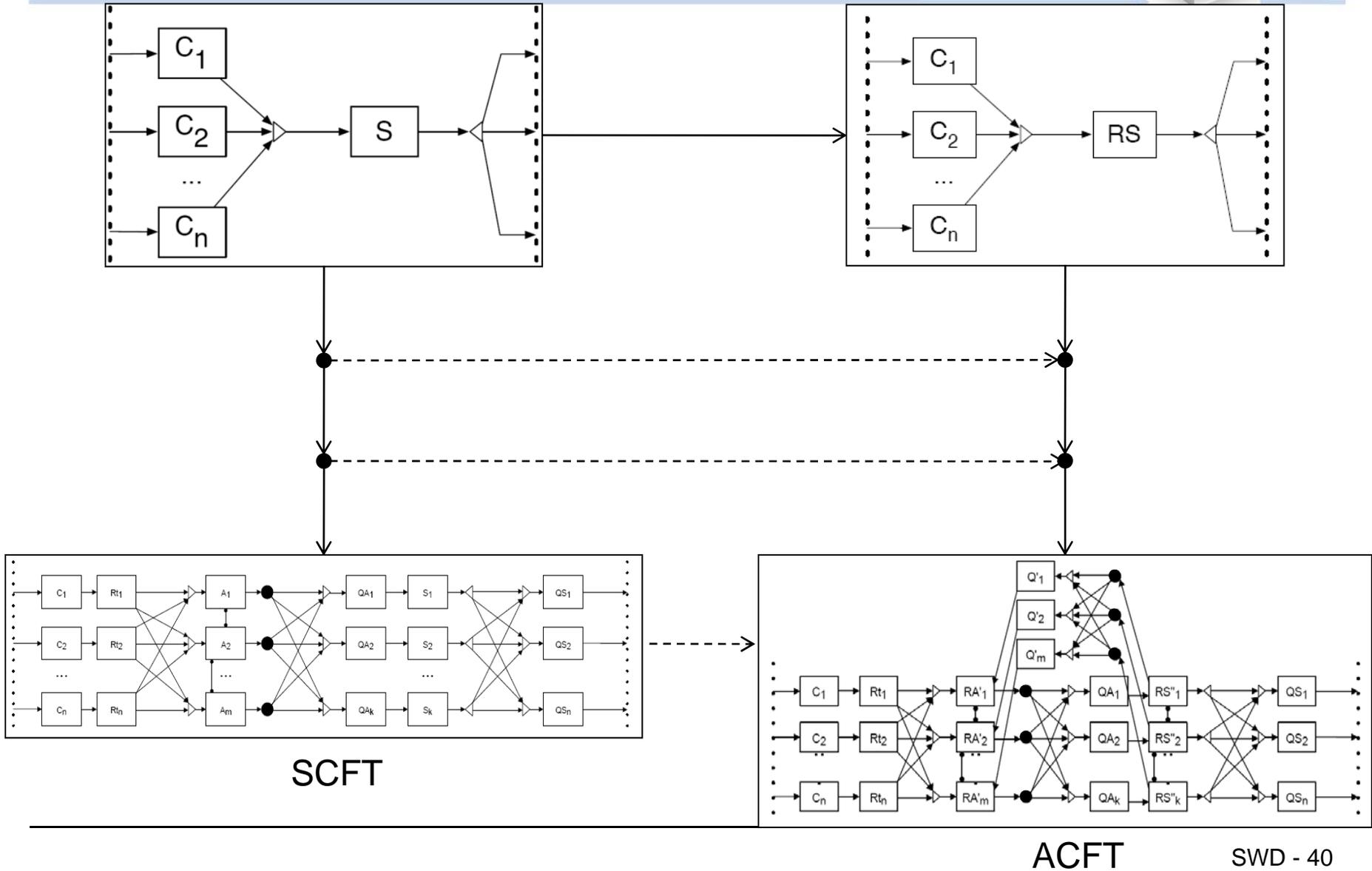
Really Quick Tour of Recovery (Async) Transformations

Overview

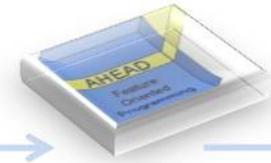


- Just as databases can recover from machine failures, so too can servers
- Recovery limits the situations where clients see unresponsive server abstraction

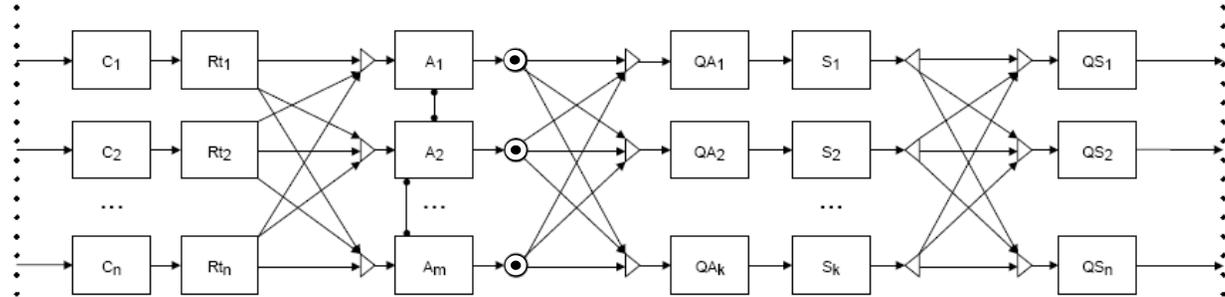
Where We Are...



Extension of SCFT to ACFT

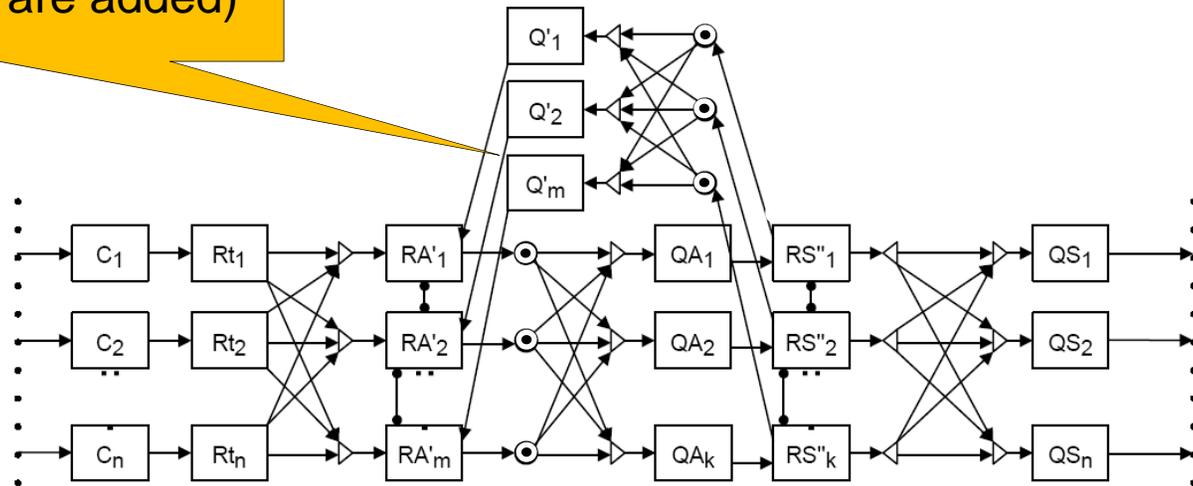


SCFT
Server
Architecture

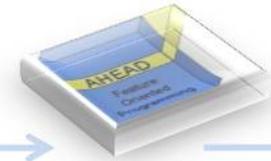


Servers now talk to A boxes
(new connectors are added)

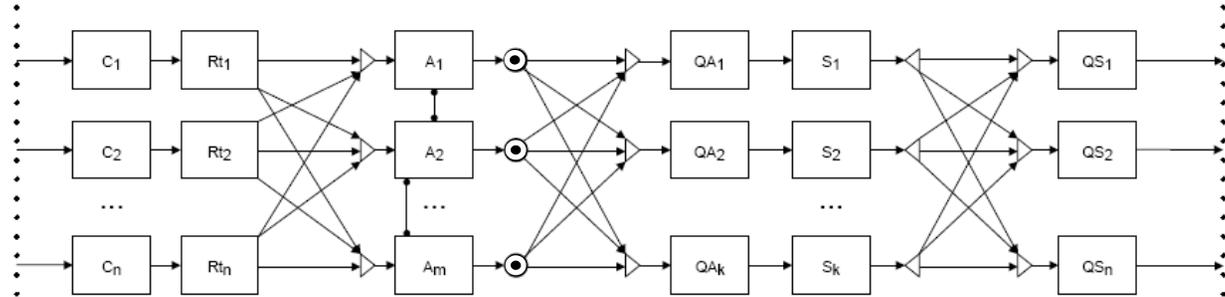
ACFT
Server
Architecture



Extension of SCFT to ACFT



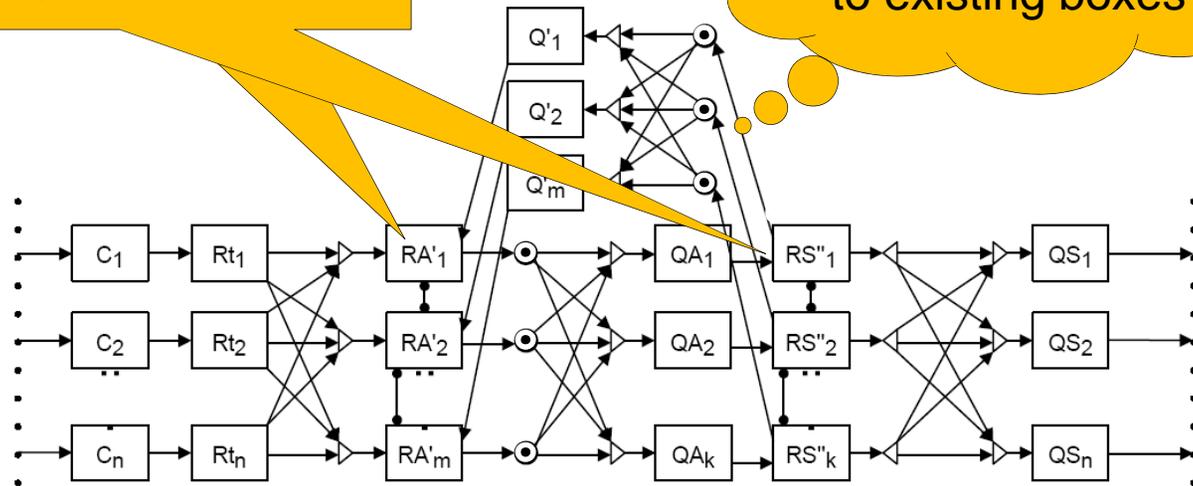
SCFT
Server
Architecture



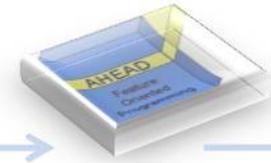
A and S boxes are extended
(new ports, capabilities added)

incrementally
adding features
to existing boxes

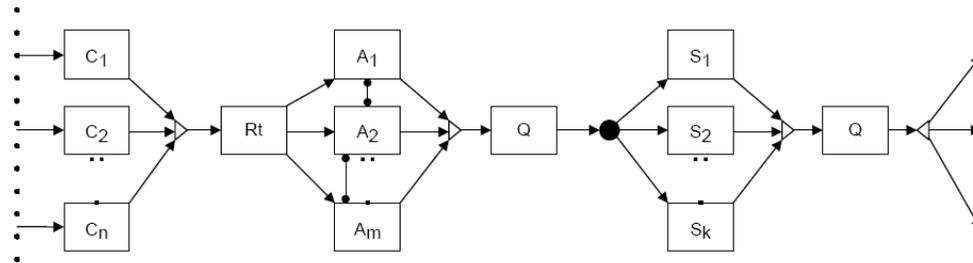
ACFT
Server
Architecture



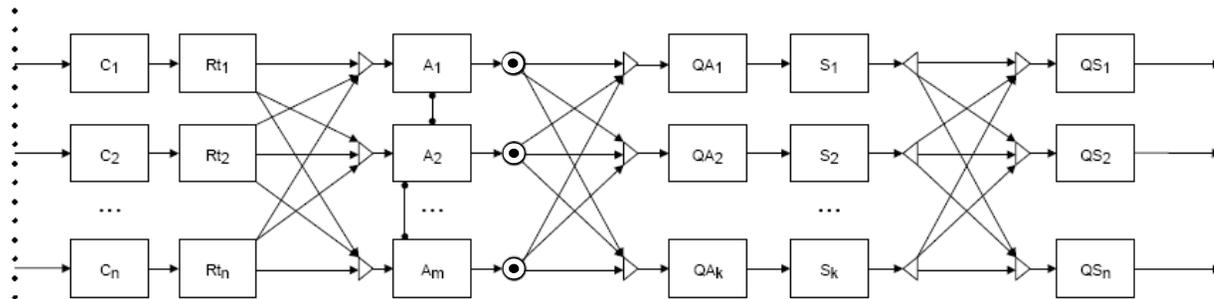
Perspectives



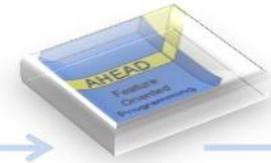
- Rotations were unfamiliar to our domain experts
- Their informal designs jumped directly from



to the one using a reliable crossbar which we derived

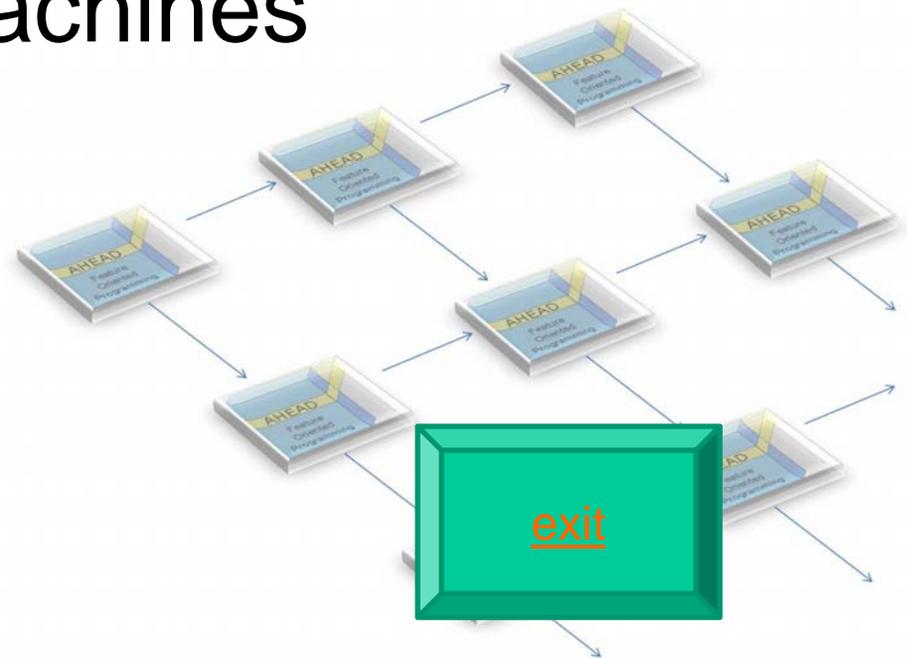


Quick Recap

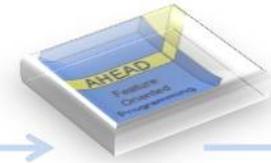


- Incrementally recovered a design created by experts to map a vanilla server to an asynchronous (recoverable), crash-fault-tolerant server
 - starting from a simple client-server model and progressively transforming it into the target architecture
- *LOTS of engineering left*
 - but now we have the architectural plans to recreate it incrementally and in a way that is easy to understand
- Now look at a very different domain where a sequential architecture is mapped to a parallel architecture using *exactly the same principles*

#3: Parallelizing Hash Joins in Database Machines

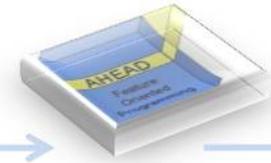


Gamma Database Machine



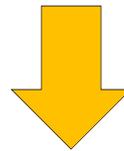
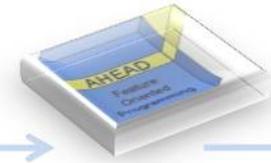
- Gamma was (maybe still is) the most sophisticated relational database machine ever built in academics
 - University of Wisconsin late 1980's early 1990s
- Look at how hash joins were parallelized
 - fundamental result in parallelizing joins
 - representative of commercial systems today
 - presented in a new way
 - derive Gamma hash join architecture from first principles

Sequential Hash Join Architecture

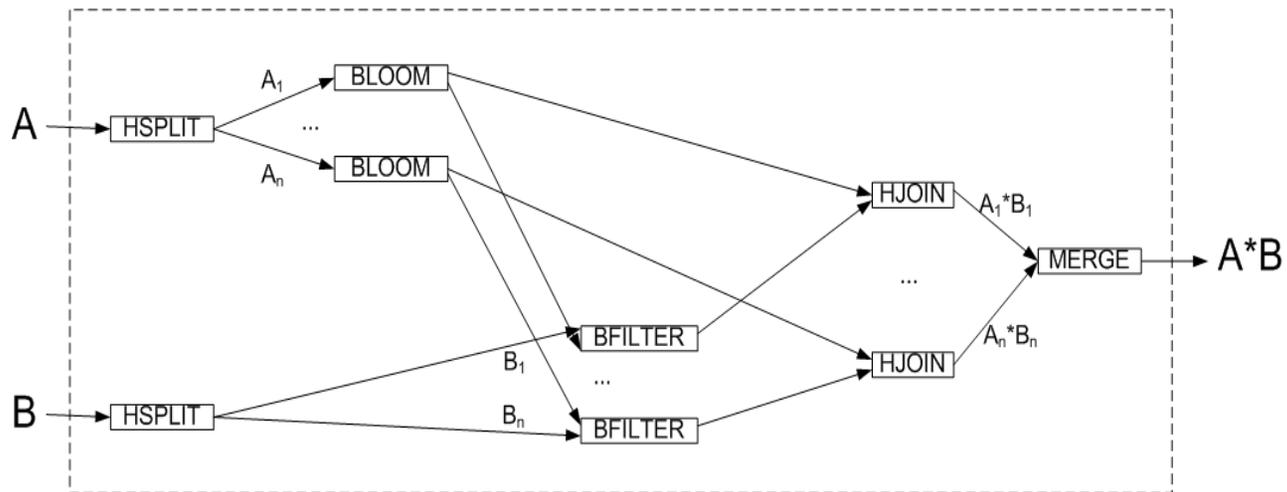


- Hash join takes 2 streams of tuples (A,B) as input and produces the join of these streams (A*B)
- Algorithm:
 - read all of stream A into memory in a hash table
 - read B stream one record at a time;
hash B's record and join it to all A record's with the same key
 - linear algorithm
- *How did Gamma's Designers parallelize HJOIN?*

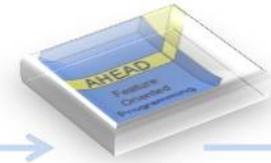
Next Slides Explain Derivation



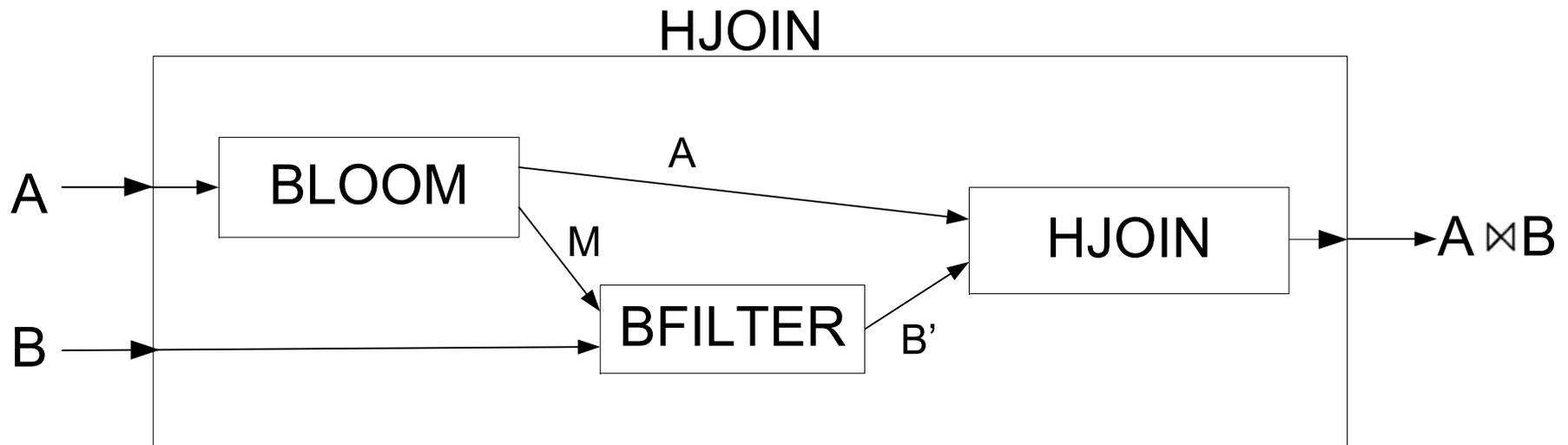
HJOIN



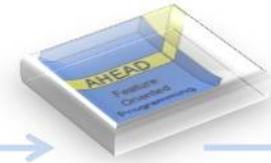
First Refinement



- Because joins are the most complex operator, increase efficiency by reducing the size of its input streams
- Used Bloom filters to eliminate B tuples that do not join with A tuples

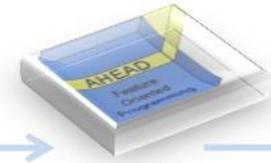


BLOOM BOX



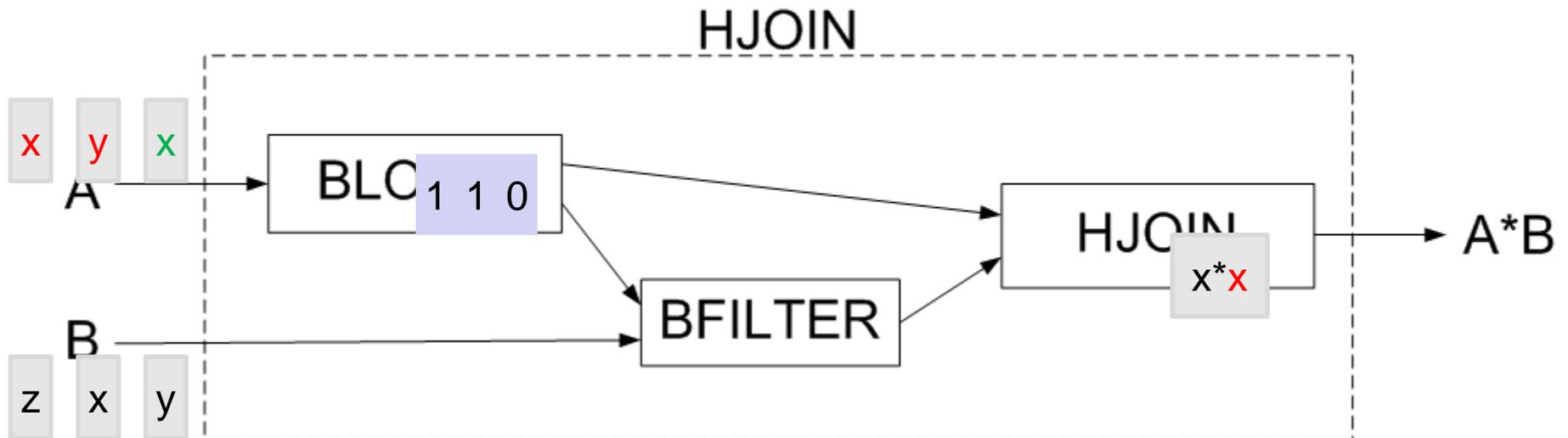
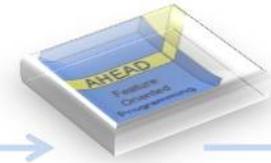
- Bloom filtering is a common technique for disqualifying tuples from further processing
- Algorithm:
 - clear bit map M
 - read each A tuple, hash its key, and mark corresponding bit in M
 - output each tuple A
 - after all A tuples read, output M

BFILTER BOX



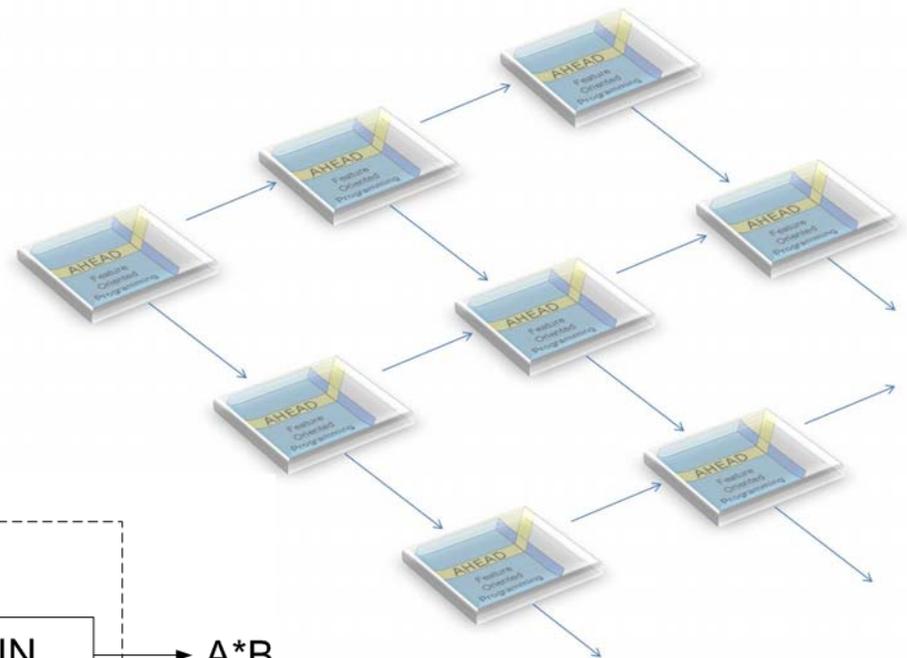
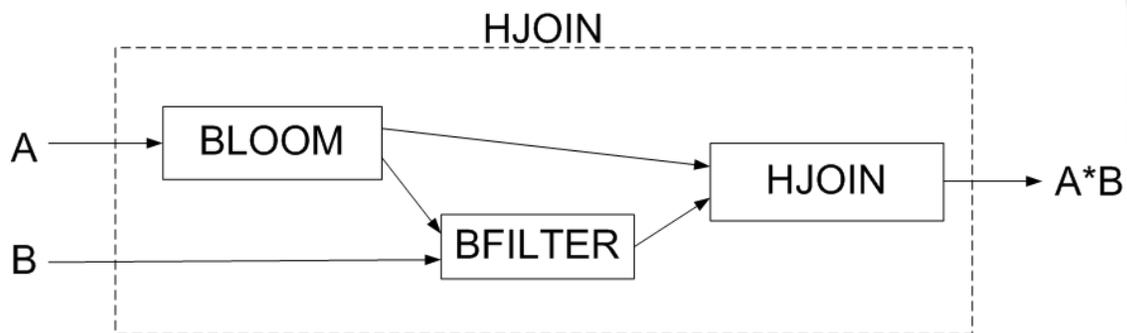
- The filtering part of Bloom filters
 - eliminates B tuples that cannot join with A tuples
- Algorithm:
 - read bit map M
 - read each tuple of B, hash its key: if corresponding bit in M is not set discard tuple (as it will never join with A tuples)
 - else output tuple

The First Refinement

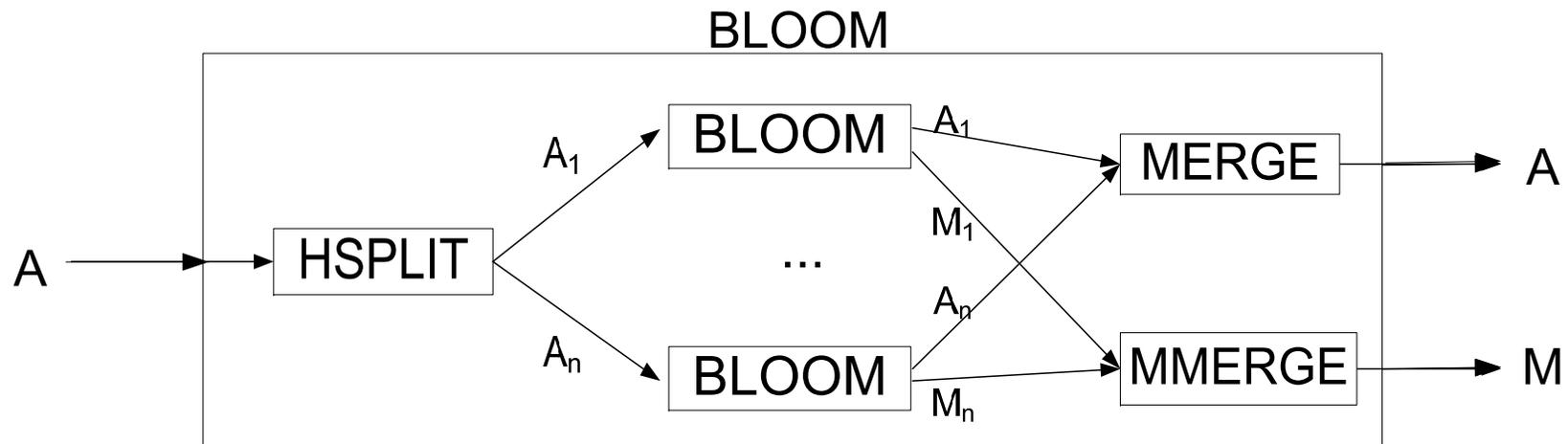
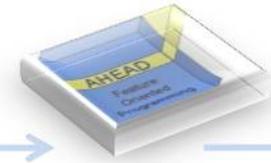


- Expose inner details of HJOIN box
- Can prove correctness of this refinement

Parallelize Each Box in this Architecture:

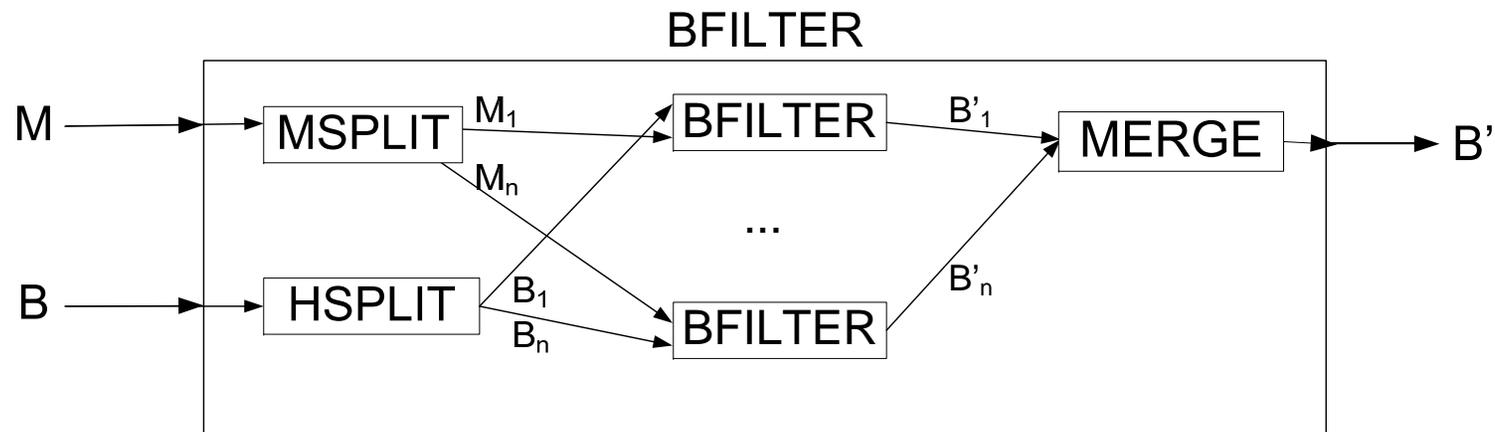
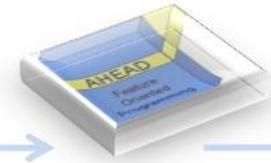


Parallelization of BLOOM Box



- Algorithm:
 - HSPLIT stream A
 - compute Bloom filter on each substream
 - reconstitute stream A
 - form merge bit maps to produce single bit map M

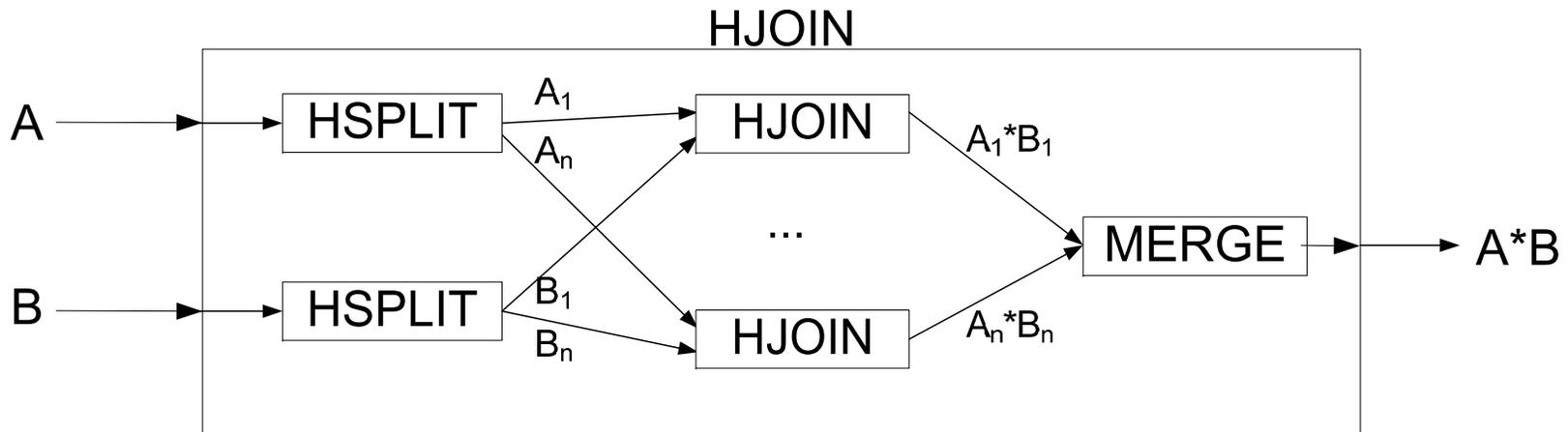
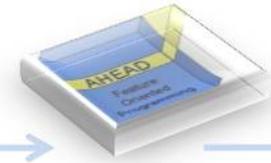
Parallelization of BFILTER Box



- Algorithm:
 - split M into $M_1 \dots M_n$ and distribute
 - hash split stream B
 - filter B substreams in parallel
 - reconstitute stream B'

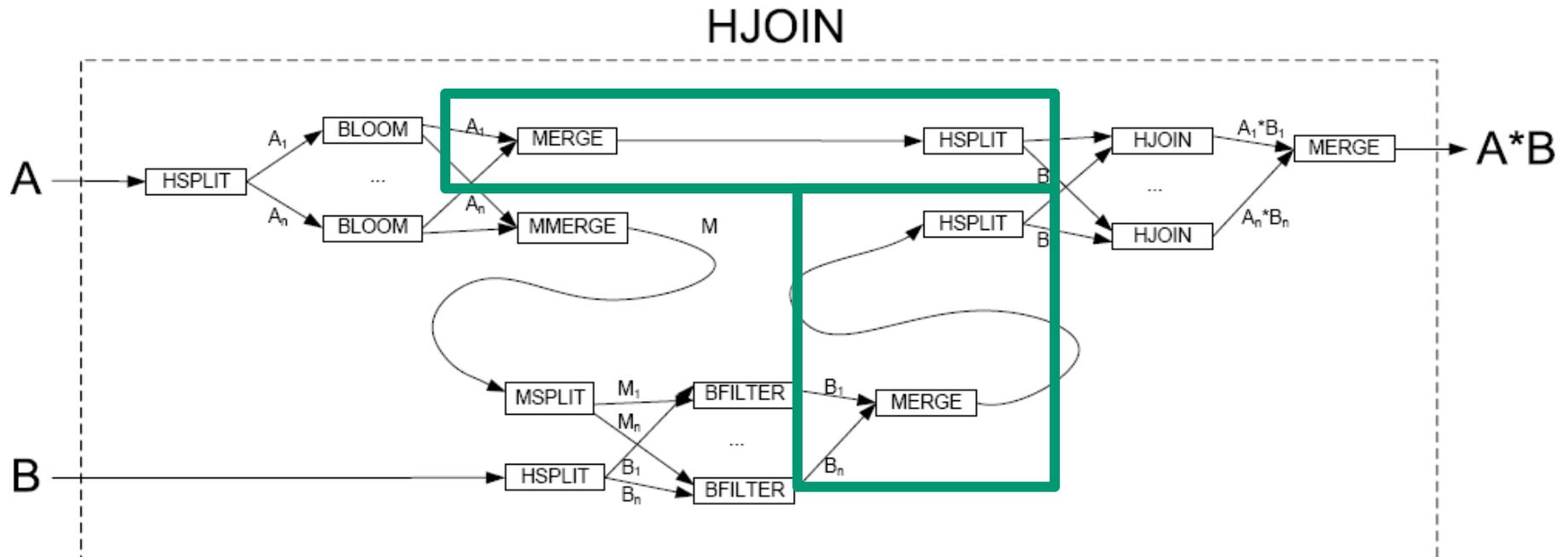
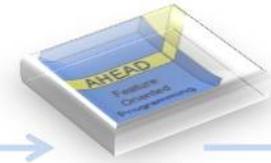
always hash split streams A and B using the same hash function! This gives us properties on which to optimize!

Parallelization of HJOIN Box



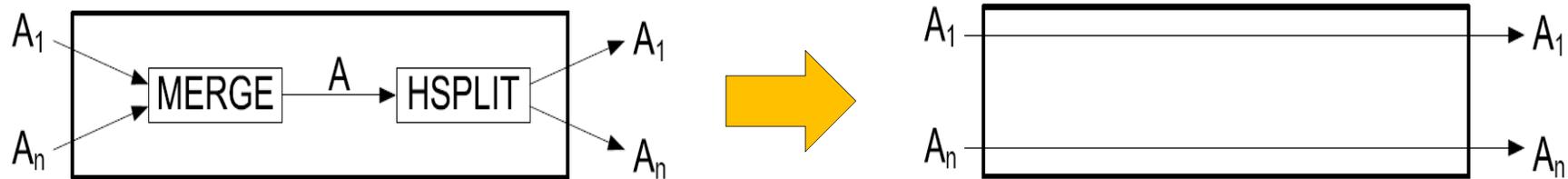
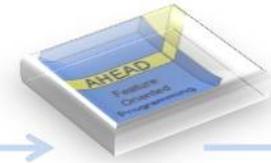
- Algorithm:
 - split both streams using same hash function
 - A and B tuples can join only if they have the same hash key
 - perform n joins (rather than n^2) in parallel
 - reconstitute join

Hierarchical Refinement



- Substitute parallel implementations for each box
- Note 3 optimizations are possible
- Here are the first two...

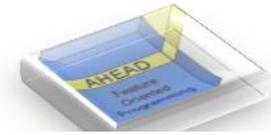
A Better View



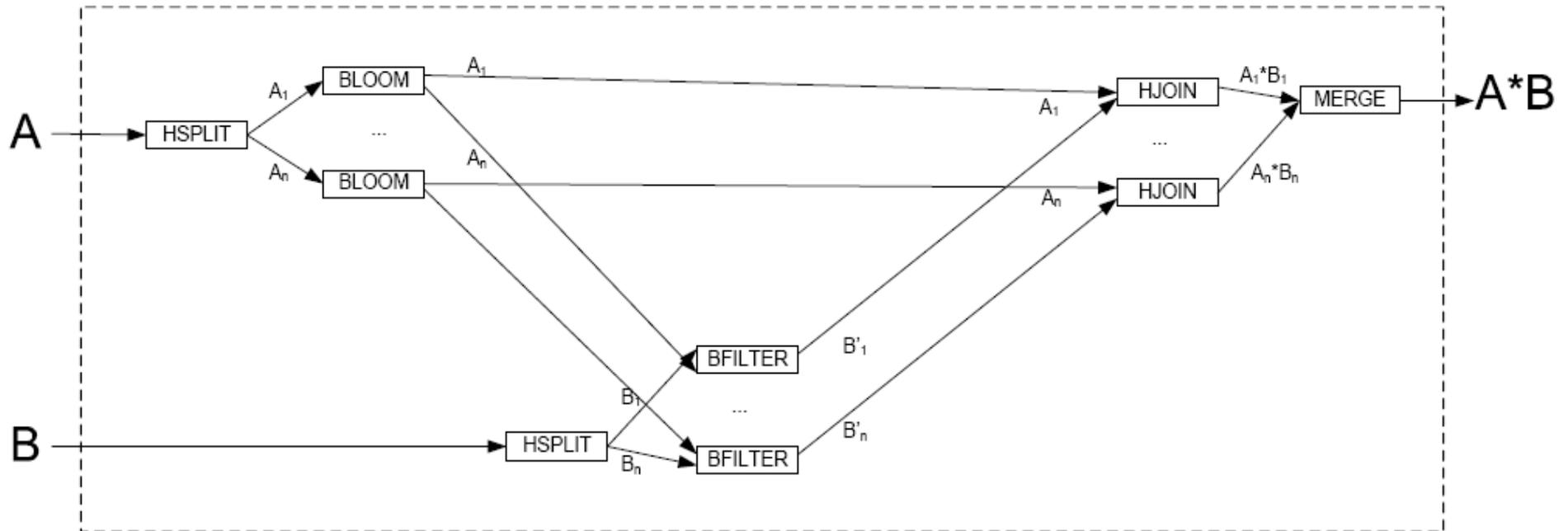
- Stream A is hash split into $A_1 \dots A_n$, reconstituted, then hash split again
- MERGE – HSPLIT combination is the identity map
- Optimization – get rid of MERGE-HSPLIT

- Same for stream B

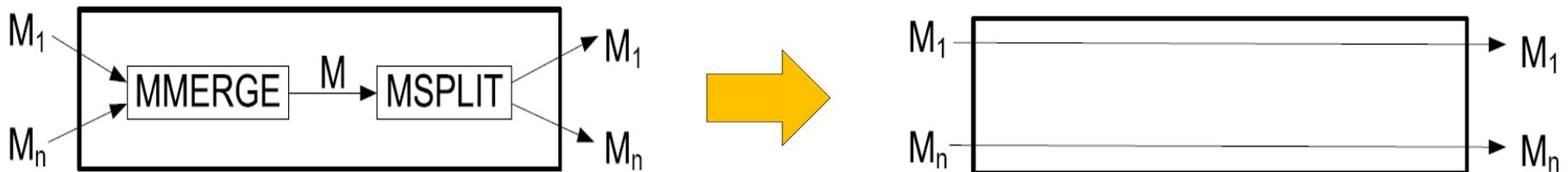
Applying Optimizing Rewrite



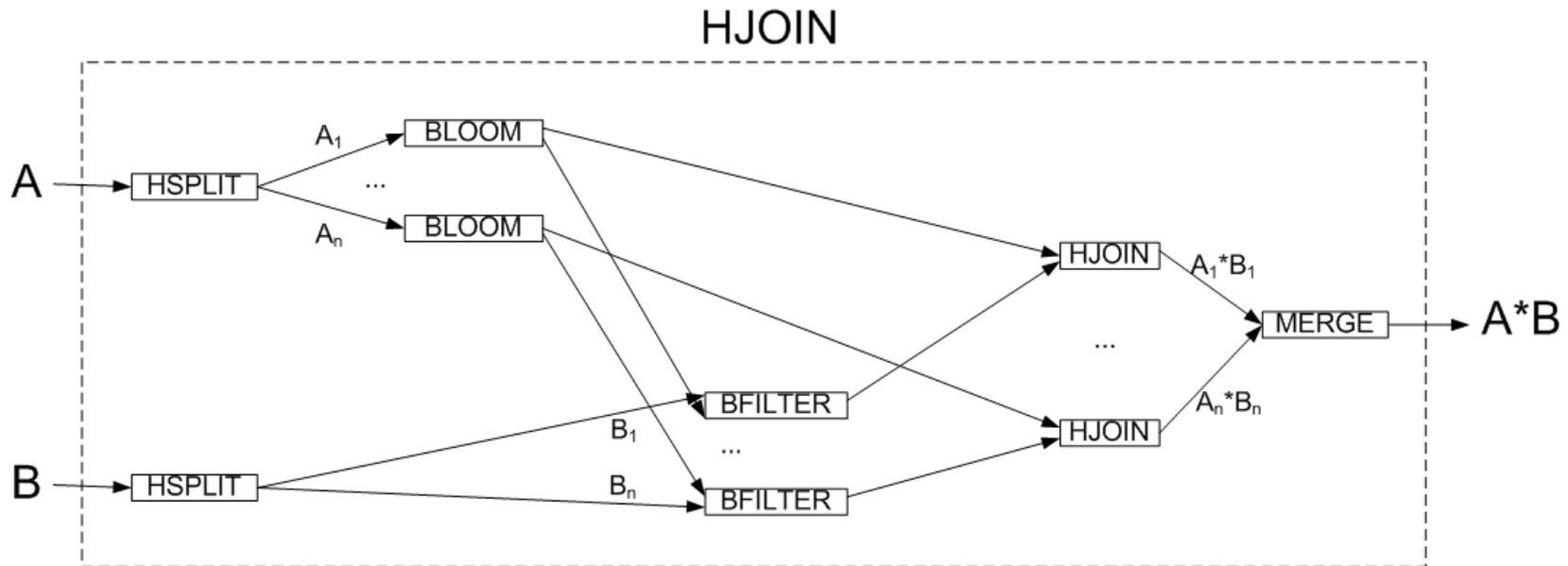
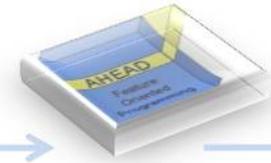
HJOIN



- Still one more optimization to perform...

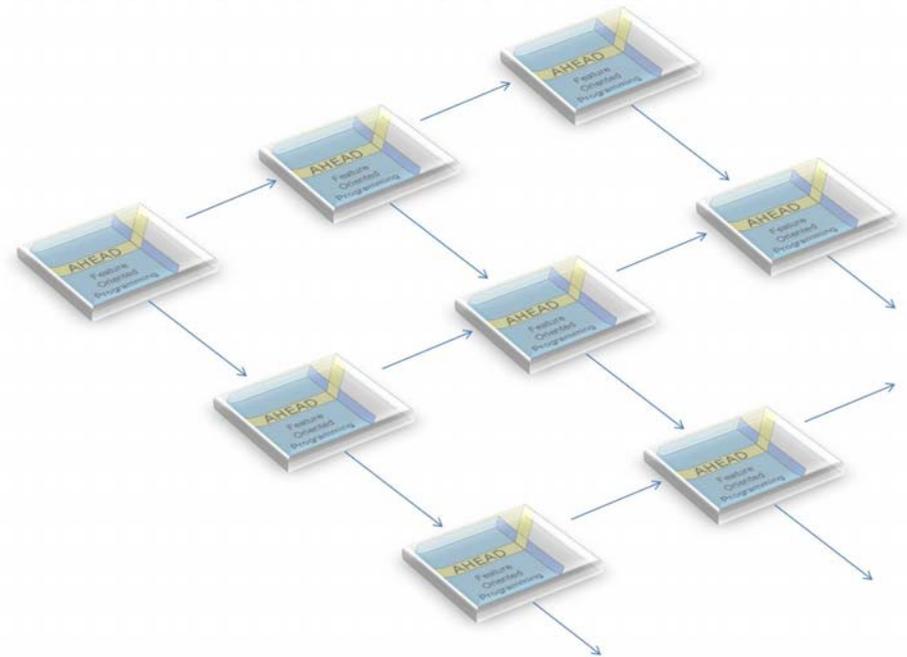


The (Almost) Final Design

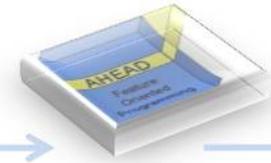


- Elegant
- Easier to remember the derivation than the design itself (!)
- Each step can be proven correct, so the final design is **correct**
- *Not whole picture: rotations rewrites are applied when HJOIN boxes are composed see our paper or original Gamma papers*

#4: Conclusions and Future Work

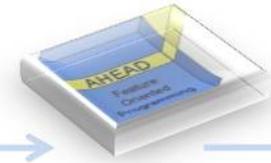


Recap



- Showed how SWD used to extract an MDE architecture from parallel streaming architectures
 - architectures are always executable, derived top-down
 - *architecture is a $D \times T$ meta-expression*
- Used traditional technique of refinement + box and model extensions and optimizations – all are needed to explain the complexities of modern streaming architectures
- Encoded deep domain knowledge by simple xforms, demonstrated approach with 2 case studies, and validated our approach by manually re-creating them in the incremental manner in which we presented them

Recap



- Although our MDE architectures look simple
 - it took effort to refresh our domain knowledge
 - polish core abstractions and transformations
- Worth the effort:
 - complex designs can be explained in a simple way
 - can be appreciated by non-experts
 - techniques (and these examples) can be taught to undergraduates
- Incremental Design is not just “cute”
 - ultimately indispensable for future software development technologies that eventually integrate design, construction, verification, and testing
- D×T is at the heart of all of this

Thank You!

