Topic 15 Implementing and Using Stacks

"stack n.

The set of things a person has to do in the future. "I haven't done it yet because every time I pop my stack something new gets pushed." If you are interrupted several times in the middle of a conversation, "My stack overflowed" means "I forget what we were talking about."

-The Hacker's Dictionary

Friedrich L. Bauer
German computer scientist
who proposed "stack method
of expression evaluation"
in 1955.



Sharper Tools



Lists



Stacks



Stacks

- Access is allowed only at one point of the structure, normally termed the top of the stack
 - access to the most recently added item only
- Operations are limited:
 - push (add item to stack)
 - pop (remove top item from stack)
 - top (get top item without removing it)
 - isEmpty
- Described as a "Last In First Out" (LIFO) data structure

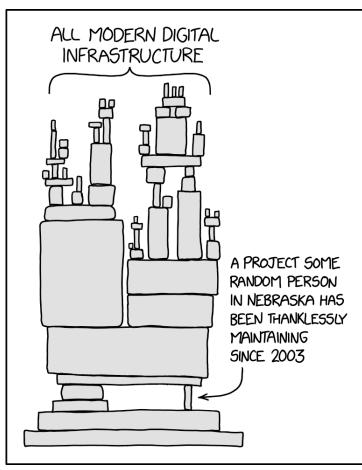


Implementing a stack

need an underlying collection to hold the elements

of the stack

- 3 obvious choices?
 - native array
 - linked structure of nodes
 - a list!!!
- Adding a *layer of abstraction*. A HUGE idea.
- array implementation
- linked list implementation

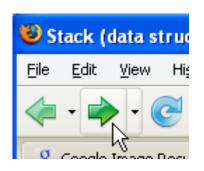


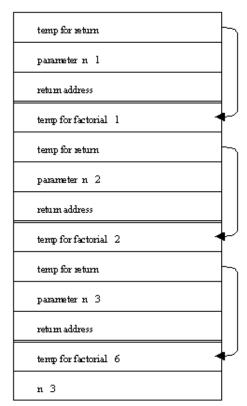
https://xkcd.com/2347/

Uses of Stacks

- The runtime stack used by a factorial process (running program) to keep track of methods in progress
- Search problems
- Undo, redo, back, forward







factorial

main



CS314 Stacks

Stack Operations

Assume a simple stack for integers. Stack<Integer> s = new Stack<>(); s.push(12); s.push(4); s.push(s.top() + 2);**s.pop()**; s.push(s.top()); //what are contents of stack?

CS314 Stacks

Clicker 1 - What is Output?

```
Stack<Integer> s = new Stack<>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// Print out contents of stack.
// Assume there is a size method.
for (int i = 0; i < s.size(); i++)
    System.out.print(s.pop() + " ");
A 0 1 2 3 4
                  D 2 3 4
B 4 3 2 1 0
                  E No output due
C 4 3 2
                       to runtime error
```

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Corrected Version

```
Stack<Integer> s = new Stack<Integer>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// print out contents of stack
// while emptying it
final int LIMIT = s.size();
for (int i = 0; i < LIMIT; i++)
    System.out.print(s.pop() + " ");
//or
// while (!s.isEmpty())
//
         System.out.println(s.pop());
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```

Stack Operations

Write a method to print out contents of stack in reverse order.



Applications of Stacks

Mathematical Calculations

- What does 3 + 2 * 4 equal?
 2 * 4 + 3?
 3 * 2 + 4?
- The precedence of operators affects the order of operations.
- A mathematical expression cannot simply be evaluated left to right.
- A challenge when evaluating a program.
- Lexical analysis is the process of interpreting a program.

What about 1 - 2 - 4 ^ 5 * 3 * 6 / 7 ^ 2 ^ 3

CS314 Stacks

Infix and Postfix Expressions

- The way we are use to writing expressions is known as infix notation
- Postfix expression does not
- require any precedence rules
- 32 * 1 + is postfix of 3 * 2 + 1
- evaluate the following postfix expressions and write out a corresponding infix expression:



Clicker Question 2

What does the following postfix expression evaluate to?

```
632 + *
```

- A. 11
- B. 18
- C. 24
- D. 30
- E. 36

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Evaluation of Postfix Expressions

- Easy to do with a stack
- by given a proper postfix expression:
 - get the next token
 - if it is an operand push it onto the stack
 - else if it is an operator
 - pop the stack for the right hand operand
 - pop the stack for the left hand operand
 - apply the operator to the two operands
 - push the result onto the stack
 - when the expression has been exhausted the result is the top (and only element) of the stack

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Infix to Postfix

Convert the following equations from infix to postfix:

Problems:

Negative numbers?

parentheses in expression

Infix to Postfix Conversion

- Requires operator precedence parsing algorithm
 - parse v. To determine the syntactic structure of a sentence or other utterance
- Operands: add to expression
- Close parenthesis: pop stack symbols until an open parenthesis appears

Operators:

Have an on stack and off stack precedence Pop all stack symbols until a symbol of lower precedence appears. Then push the operator

End of input: Pop all remaining stack symbols and add to the expression

Infix Expression: 3 + 2 * 4

PostFix Expression:

Operator Stack:

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression: + 2 * 4

PostFix Expression: 3

Operator Stack:

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression: 2 * 4

PostFix Expression: 3

Operator Stack: +

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression: * 4

PostFix Expression: 3 2

Operator Stack: +

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression: 4

PostFix Expression: 3 2

Operator Stack: + *

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression:

PostFix Expression: 3 2 4

Operator Stack: + *

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
^	10	9
(20	0

Infix Expression:

PostFix Expression: 3 2 4 *

Operator Stack: +

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Infix Expression:

PostFix Expression: 3 2 4 * +

Operator Stack:

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Example

11 + 2 ^ 4 ^ 3 - ((4 + 5) * 6) ^ 2

Show algorithm in action on above equation

Balanced Symbol Checking

In processing programs and working with computer languages there are many instances when symbols must be balanced {},[],()

A stack is useful for checking symbol balance. When a closing symbol is found it must match the most recent opening symbol of the same type.

Applicable to checking html and xml tags!

Algorithm for Balanced Symbol Checking

- Make an empty stack
- read symbols until end of file
 - if the symbol is an opening symbol push it onto the stack
 - if it is a closing symbol do the following
 - if the stack is empty report an error
 - otherwise pop the stack. If the symbol popped does not match the closing symbol report an error
- At the end of the file if the stack is not empty report an error

Algorithm in practice

list[i] = 3 * (44 - method(foo(list[2 * (i + 1) + foo(list[i - 1])) / 2 *) - list[method(list[0])];

- Complications
 - when is it not an error to have non matching symbols?
- Processing a file
 - Tokenization: the process of scanning an input stream.
 Each independent chunk is a token.
- Tokens may be made up of 1 or more characters