Topic 15 **Implementing and Using Stacks**

"stack n.

The set of things a person has to do in the future. "I haven't done it yet because every time I pop my stack something new gets pushed." If you are interrupted several times in the middle of a conversation, "My stack overflowed" means "I forget what we were talking about."

-The Hacker's Dictionary

Friedrich L. Bauer German computer scientist who proposed "stack method of expression evaluation" in 1955.



Sharper Tools



Lists



Stacks





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Stacks

Stacks

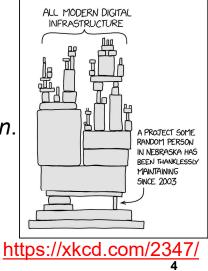
- Access is allowed only at one point of the structure, normally termed the *top* of the stack
 - access to the most recently added item only
- Operations are limited:
 - push (add item to stack)
 - pop (remove top item from stack)
 - top (get top item without removing it)
 - isEmpty
- Described as a "Last In First Out" (LIFO) data structure

Implementing a stack

- need an underlying collection to hold the elements of the stack
- 3 obvious choices?
 - native array
 - linked structure of nodes
 - a list!!!

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- Adding a layer of abstraction. A HUGE idea.
- array implementation
- Inked list implementation



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Uses of Stacks

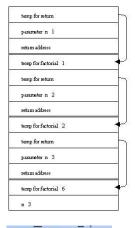
- The runtime stack used by a model process (running program) to keep track of methods in progress
- Search problems
- Undo, redo, back, forward



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```
nethods in
ms
ack, forward
```



factorial

Undo Move Object

5

7

Stack Operations

```
Assume a simple stack for integers.
Stack<Integer> s = new Stack<>();
s.push(12);
s.push(4);
s.push( s.top() + 2 );
s.push( s.top() + 2 );
s.push( s.top() );
//what are contents of stack?
```

Corrected Version

6

```
Stack<Integer> s = new Stack<Integer>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// print out contents of stack
// while emptying it
final int LIMIT = s.size();
for (int i = 0; i < LIMIT; i++)
    System.out.print(s.pop() + " ");
//or
    while (!s.isEmpty())
//
//
         System.out.println(s.pop());
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                                        8
                   Stacks
```

Clicker 1 - What is Output?

Stacks

```
Stack<Integer> s = new Stack<>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// Print out contents of stack.
// Assume there is a size method.
for (int i = 0; i < s.size(); i++)
    System.out.print(s.pop() + " ");
A 0 1 2 3 4
B 4 3 2 1 0
E No output due
C 4 3 2
to runtime error</pre>
```

Stacks

Stack OperationsWrite a method to print out contents of stack in reverse order.	Applications of Stacks	
CS314 9		
 Mathematical Calculations What does 3 + 2 * 4 equal? 2*4+3? 3*2+4? The precedence of operators affects the order of operations. A mathematical expression cannot simply be evaluated left to right. A challenge when evaluating a program. Lexical analysis is the process of interpreting a program. 	 Infix and Postfix Expressions The way we are use to writing expressions is known as infix notation Postfix expression does not require any precedence rules 32*1+ is postfix of 3*2+1 evaluate the following postfix expressions and write out a corresponding infix expression: 2324*+* 1234**+ 	

What about 1 - 2 - 4 ^ 5 * 3 * 6 / 7 ^ 2 ^ 3

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1 2 - 3 2 ^ 3 * 6 / + 2 5 ^ 1 -

Clicker Question 2 • What does the following postfix expression evaluate to? 6 3 2 + * A. 11 B. 18 C. 24 D. 30 E. 36	 Evaluation of Postfix Expressions Easy to do with a stack given a proper postfix expression: get the next token if it is an operand push it onto the stack else if it is an operator pop the stack for the right hand operand pop the stack for the left hand operand apply the operator to the two operands push the result onto the stack when the expression has been exhausted the 		
CS314 13	result is the top (and only element) of the stack CS314 14		
Infix to Postfix • Convert the following equations from infix to postfix: 2^3^3+5*1 11+2-1*3/3+2^2/3 Problems: Negative numbers? parentheses in expression	 Infix to Postfix Conversion Requires operator precedence parsing algorithm parse v. To determine the syntactic structure of a sentence or other utterance Operands: add to expression Close parenthesis: pop stack symbols until an open parenthesis appears Operators: 		
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Simple Example 3 + 2 * 4

Infix Expression:

PostFix Expression:

Operator Stack:

Infix Expression:

Operator Stack:

Symbol

+

*

٨

PostFix Expression:

Precedence Table

Symbol	Off Stack	On Stack
-	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

Stacks

Simple Example

3

+

Precedence Table

Off Stack Precedence

1

1

2

2

10

20

2*4

On Stack

1

1

2

2

9

0

Precedence

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Stacks

On Stack

Precedence Precedence

1

1

2 2

9

0

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Simple Example

Simple Example

3

Precedence Table

Off Stack

1

1

2

2

10

20

Infix Expression: + 2 * 4

PostFix Expression:

Operator Stack:

Symbol

+

*

٨

Infix Expression:	* 4
PostFix Expression:	32
Operator Steek:	т

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
۸	10	9
(20	0

20

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Stacks

Simp	le	Exa	mp	le
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4

+ *

Infix Expression:	
-------------------	--

Infix Expression:

Operator Stack:

Symbol

+

*

٨

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PostFix Expression:

32 PostFix Expression:

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

Stacks

Simple Example

+

Precedence Table

Off Stack Precedence

1

1

2

2

10

20

324*

On Stack

1

1

2

2

9

0

Precedence

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Stacks

Simple Example

Infix Expression:

PostFix Expression: 324

+ * **Operator Stack:**

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

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Simple Example

Infix Expression:

PostFix Expression: 324*+

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

Stacks

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Example $11 + 2^{4} - 3 - ((4 + 5) + 6) + 2$ Show algorithm in action on above equation		 Balanced Symbol Checking In processing programs and working with computer languages there are many instances when symbols must be balanced {},[],() A stack is useful for checking symbol balance. When a closing symbol is found it must match the most recent opening symbol of the same type. Applicable to checking html and xml tags! 			
CS314	Stacks	25	CS314	Stacks	26
 Make an en read symbol if the symbol the stack if it is a close if the stack otherwise not match At the end of 	ols until end of file ol is an opening symbol pu sing symbol do the followin k is empty report an error pop the stack. If the symbol po the closing symbol report an e of the file if the stack is	ush it onto Ig opped does error	 list[i] = 3 * (4 list[i - 1]))/2 Complication – when is it no Processing a – Tokenization Each independent 	ot an error to have non matchi	i + 1) + foo(ng symbols? input stream.
report an er	Stacks	27	CS314	Stacks	28