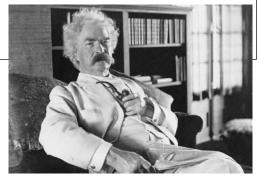
Topic 12 Introduction to Recursion

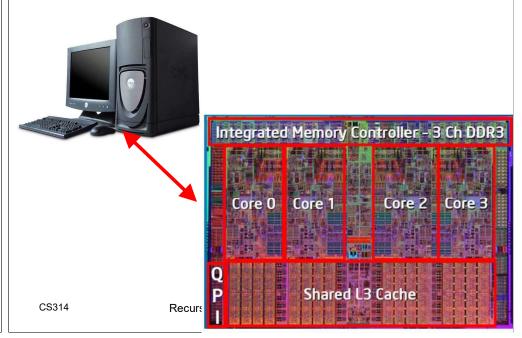
"To a man with a hammer, everything looks like a nail"

-Mark Twain

CS314



Underneath the Hood.



The Program Stack

When you invoke a method in your code what happens when that method is done?

```
public class Mice {
    public static void main(String[] args) {
        int x = 37;
        int y = 12;
        method1(x, y);
        int z = 73;
        int m1 = method1(z, x);
        method2(x, x);
    }
    // method1 and method2
    // on next slide
```

Recursion

method1 and method2

```
// in class Mice
public static int method1(int a, int b) {
    int r = 0;
    if (b != 0) {
        int x = a / b;
        int y = a % b;
        r = x + y;
    }
    return r;
}
public static void method2(int x, int y) {
        x++;
        y--;
        int z = method1(y, x);
        System.out.print(z);
cs314 Recursion
```

<pre>The Program Stack • When your program is run on a processor, the commands are converted into another set of instructions and assigned memory locations. – normally a great deal of expansion takes place public static void main(String[] args) { int x = 37; // 0 int y = 12; // 1 method1(x, y); // 2 int z = 73; // 3 int m1 = method1(z, x); // 4 method2(x, x); // 7 }_{cs314} Recursion Keep Recursion Recursion</pre>	 Basic CPU Operations A CPU works via a fetch command / execute command loop and a program counter Instructions stored in memory (Instructions are data!) int x = 37; // 0 int y = 12; // 1 method1(x, y); // 2 int z = 73; // 3 int m1 = method1(z, x); // 4 What if the first instruction of the method1 is stored at memory location 50? 6
<pre>// in class Mice public static int method1(int a, int b) { int r = 0; // 51 if (b != 0) { // 52 int x = a / b; // 53 int y = a % b; // 54 r = x + y; // 55 } return r; // 56 } public static void method2(int x, int y) { x++; // 60 y; // 61 int z = method1(y, x); // 62 System.out.print(z); // 63 cs314 Recursion 7 </pre>	<pre>Clicker 1 - The Program Stack int x = 37; // 1 int y = 12; // 2 method1(x, y); // 3 int z = 73; // 4 int m1 = method1(z, x); // 5 method2(x, x); // 6 Instruction 3 is really saying jump to instruction 50 with parameters x and y In general what happens when method1 finishes? A. program ends B. goes to instruction 4 C. goes back to whatever method called it </pre>

Activation Records and the	The Program Stack		
 Program Stack When a method is invoked all the relevant information about the current method (variables, values of variables, next line of code to be executed) is placed in an <i>activation record</i> The activation record is pushed onto the 	 Data may either be added (<i>pushed</i>) or removed (<i>popped</i>) from a stack but it is always from the top. A stack of dishes which dish do we have 		
The activation record is <i>pushed</i> onto the program stack	- which dish do we have easy access to?		
A stack is a data structure with a single access point, the top.			
CS314 Recursion 9	CS314 Recursion 10		
	A Problem		
	Write a method that determines how much space is take up by the files in a directory		
Using Recursion	A directory can contain files and directories		
	How many directories does our code have to examine?		
	How would you add up the space taken up by the files in a single directory		
	 Hint: don't worry about any sub directories at first 		
	CS314 Recursion 12		

Clicker 2

How many levels of directories have to be visited?

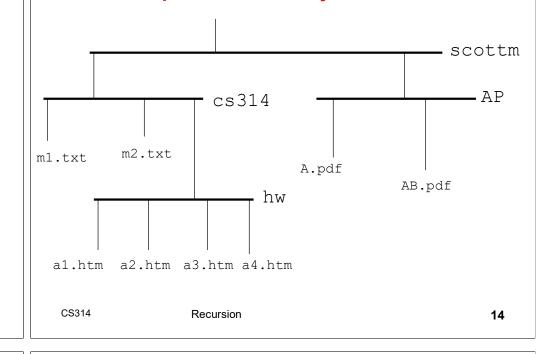
Α.	0
----	---

- B. 1
- C. 8

CS314

- D. Infinite
- E. Unknown

Sample Directory Structure



Java File Class

Recursion

- File (String pathname) Creates a new File instance by converting the given pathname.
- boolean isDirectory() Tests whether the file denoted by this abstract pathname is a directory.
- File[] listFiles() Returns an array of abstract pathnames denoting the files in the directory denoted by this abstract pathname.

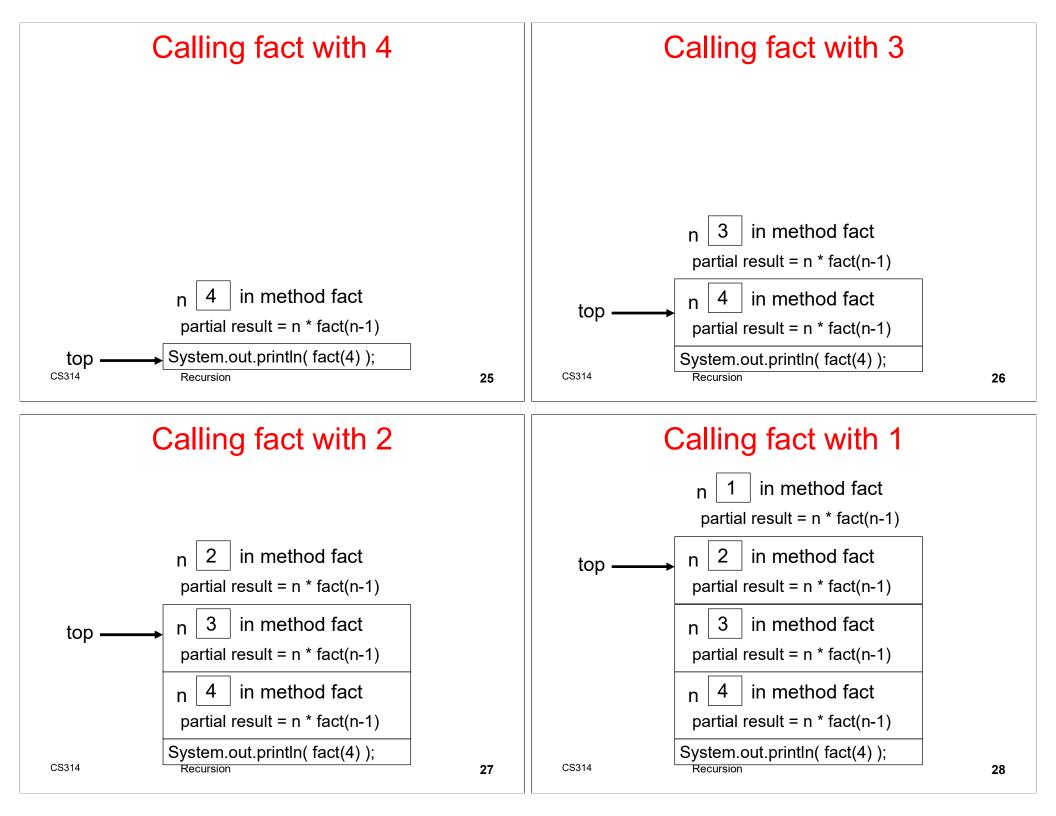
Code for getDirectorySpace()

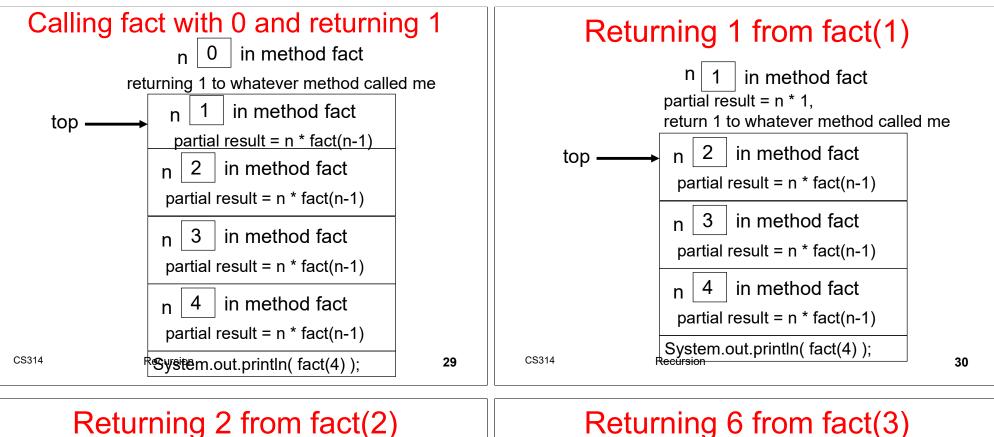
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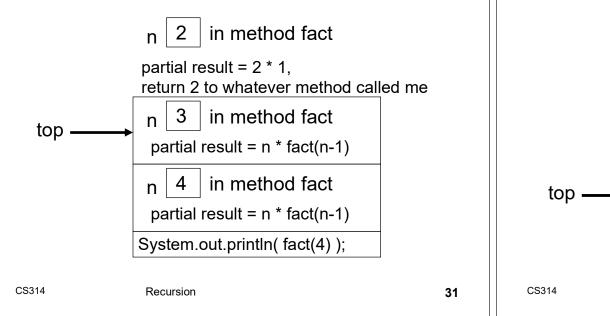
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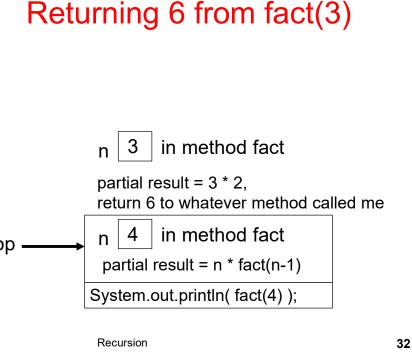
Iterative getDirectorySpace() Clicker 3 public long getDirectorySpace(File d) { Is it possible to write a non recursive method ArrayList<File> dirs = new ArrayList<>(); dirs.add(d); to determine space taken up by files in a long total = 0;directory, including its subdirectories, and while (dirs.size() > 0) { File temp = dirs.remove(dirs.size() - 1); their subdirectories, and their subdirectories, File[] filesAndSubs = temp.listFiles(); if (filesAndSubs != null) { and so forth? for (File f : filesAndSubs) { if (f != null) { A. No if (f.isFile()) total += f.length(); B. Yes else if (f.isDirectory()) dirs.add(f); C. It Depends return total; CS314 17 CS314 Recursion Recursion 18 The 3 plus 1 rules of Recursion 1. Know when to stop 2. Decide how to take one step 3. Break the journey down into that step and a Wisdom for Writing Recursive smaller journey **Methods** 4. Have faith From Common Lisp: A Gentle Introduction to Symbolic Computation by David Touretzky CS314 Recursion 20

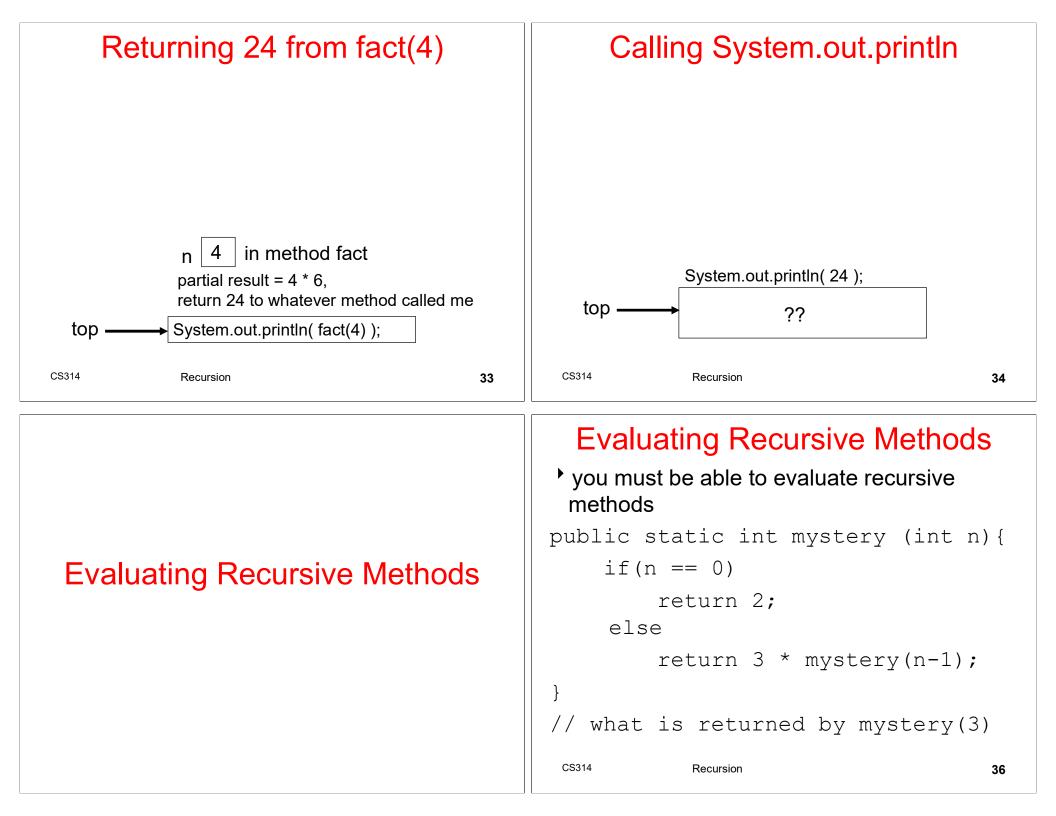
Writing Recursive Methods	N!	
 Rules of Recursion 1. Base Case: Always have at least one case that can be solved without using recursion 2. Make Progress: Any recursive call must progress toward a base case. 3. "You gotta believe." Always assume that the recursive call works. (Of course you will have to design it and test it to see if it works or prove that it always works.) A recursive solution solves a small part of the problem and leaves the rest of the problem in the same form as the original 	<pre></pre>	
CS314 Recursion 21	CS314 Recursion 22	
Factorial Recursively	Tracing Fact With the	
Mathematical Definition of Factorial	Program Stack	
	i i ografi otaok	
<pre> for N >= 0, N! is: 0! = 1 N! = N * (N = 1)! (for N > 0) </pre>	System.out.println(fact(4));	
,	Ŭ	
0! = 1 N! = N * (N - 1)! (for N > 0)	Ŭ	











 Evaluating Recursive Methods Draw the program stack! 	Clicker 4 What is returned by fact (-3)?	
m(3) = 3 * m(2) -> 3 * 18 = 54 m(2) = 3 * m(1) -> 3 * 6 = 18	A. 0 B. 1 C. Infinite Icon	
m(1) = 3 * m(0) -> 3 * 2 = 6 m(0) = 2 -> 54	C. Infinite loop D. Syntax error E. Runtime error	
with practice you can see the result	<pre>E. Rufftime enfor public static int fact(int n) { if (n == 0) { return 1; } else { return n * fact(n - 1);</pre>	
CS314 Recursion 37	} } 38	
Evaluating Recursive Methods	Evaluating Recursive Methods	

What about multiple recursive calls? public static int bar(int n) { if (n <= 0)return 2; else return 3 + bar(n-1) + bar(n-2);Clicker 5 - What does bar(4) return? A. 2 B. 3 C. 12 D. 22 E. 37

```
What is returned by bar(4)?
b(4) = 3 + b(3) + b(2)
b(3) = 3 + b(2) + b(1)
b(2) = 3 + b(1) + b(0)
b(1) = 3 + b(0) + b(-1)
b(0) = 2
b(-1) = 2
```

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Evaluating Recursive Method • What is returned by $bar(4)$? b(4) = 3 + b(3) + b(2) b(3) = 3 + b(2) + b(1) b(2) = 3 + b(1) + b(0) //substitute in results b(1) = 3 + 2 + 2 = 7 b(0) = 2 b(-1) = 2			b(2) + b(1)	;
CS314 Recursion	41	CS314	Recursion	42

Evaluating Recursive Methods

 What is returned by bar(4)? b(4) = 3 + b(3) + b(2) b(3) = 3 + 12 + 7 = 22 b(2) = 12 b(1) = 7 b(0) = 2 b(-1) = 2

Evaluating Recursive Methods

 What is returned by bar(4)? b(4) = 3 + 22 + 12 = 37 b(3) = 22 b(2) = 12 b(1) = 7 b(0) = 2 b(-1) = 2

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 Recursion Practice Write a method raiseToPower(int base, int power) //pre: power >= 0 Simple recursion (also called tail recursion) 		 Finding the Maximum in an Array public int max(int[] data) { Helper method or create smaller arrays each time 		
CS314 Recursion	45	CS314	Recursion	46
 Clicker 6 When writing recursive methods w be done first? A. Determine recursive case B. Determine recursive step C. Make a recursive call D. Determine base case(s) E. Determine the Big O 	hat should	 Rement It is not In factorization In factorization After le recursion 	bur Meta Cognit nber we are learning t a good tool for <i>all</i> p t we will implement seve ods where an iterative (le sion) solution would wor earning the mechanic on the real skill is kno ns or class of probler	to use a tool. roblems. eral algorithms and ooping without k just fine s and basics of owing what
CS314 Recursion	47	CS314	Recursion	48

 Big O and Recursion Determining the Big O of recursive methods can be tricky. A recurrence relation exits if the function is defined recursively. The T(N), actual running time, for N! is recursive T(N)_{fact} = T(N-1)_{fact} + O(1) This turns out to be O(N) There are N steps involved 	Common Recurrence Relations • $T(N) = T(N/2) + O(1) -> O(logN)$ - binary search • $T(N) = T(N-1) + O(1) -> O(N)$ - sequential search, factorial • $T(N) = T(N/2) + T(N/2) + O(1) -> O(N)$, - tree traversal • $T(N) = T(N-1) + O(N) -> O(N^2)$ - selection sort • $T(N) = T(N/2) + T(N/2) + O(N) -> O(NlogN)$ - merge sort • $T(N) = T(N-1) + T(N-1) + O(1) -> O(2^N)$ - Fibonacci
CS314 Recursion 49	CS314 Recursion 50