Virtual Memory and Address Translation

Review

- Program addresses are virtual addresses.
  - Relative offset of program regions can not change during program execution. E.g., heap can not move further from code.
  - Virtual addresses == physical address inconvenient.
    - Program location is compiled into the program.
- A single offset register allows the OS to place a process’ virtual address space anywhere in physical memory.
  - Virtual address space must be smaller than physical.
  - Program is swapped out of old location and swapped into new.
- Segmentation creates external fragmentation and requires large regions of contiguous physical memory.
  - We look to fixed sized units, memory pages, to solve the problem.
Virtual Memory
Concept

- Key problem: How can one support programs that require more memory than is physically available?
  - How can we support programs that do not use all of their memory at once?

- Hide physical size of memory from users
  - Memory is a "large" virtual address space of $2^n$ bytes
  - Only portions of VAS are in physical memory at any one time (increase memory utilization).

- Issues
  - Placement strategies
    - Where to place programs in physical memory
  - Replacement strategies
    - What to do when there exist more processes than can fit in memory
  - Load control strategies
    - Determining how many processes can be in memory at one time

Realizing Virtual Memory
Paging

- Physical memory partitioned into equal sized page frames
  - Page frames avoid external fragmentation.

A memory address is a pair $(f, o)$
- $f$ — frame number ($f_{\text{max}}$ frames)
- $o$ — frame offset ($o_{\text{max}}$ bytes/frames)

Physical address = $o_{\text{max}} \times f + o$

PA: \[ \begin{array}{c}
\log_2 (f_{\text{max}} \times o_{\text{max}}) \\
\log_2 o_{\text{max}} \\
\end{array} \]

\[
(f, o) \quad \begin{array}{c}
\text{Physical Memory} \\
\end{array}
\]

\[
(0, 0) \quad \begin{array}{c}
\text{0} \\
\end{array} \\
2^{n-1} \quad \begin{array}{c}
\text{Program} \\
\end{array}
\]

VAS
Physical Address Specifications
Frame/Offset pair v. An absolute index

Example: A 16-bit address space with \( o_{\text{max}} \)
512 byte page frames
- Addressing location \((3, 6) = 1,542\)

![Diagram of physical memory and addressing]

Questions

- The offset is the same in a virtual address and a physical address.
  - A. True
  - B. False

- If your level 1 data cache is equal to or smaller than \( 2^{\text{number of page offset bits}} \) then address translation is not necessary for a data cache tag check.
  - A. True
  - B. False
A process’s virtual address space is partitioned into equal sized pages. A virtual address is a pair \( (p, o) \)
- \( p \) — page number \( (p_{max} \) pages) 
- \( o \) — page offset \( (o_{max} \) bytes/pages) 
Virtual address = \( o_{max} \times p + o \)

\[
2^n - 1 = (p_{max} - 1, o_{max} - 1)
\]

Pages map to frames. Pages are contiguous in a VAS...
- But pages are arbitrarily located in physical memory, and
- Not all pages mapped at all times.
Frames and pages

- Only mapping virtual pages that are in use does what?
  - A. Increases memory utilization.
  - B. Increases performance for user applications.
  - C. Allows an OS to run more programs concurrently.
  - D. Gives the OS freedom to move virtual pages in the virtual address space.

- Address translation is
  - A. Frequent
  - B. Infrequent

- Changing address mappings is
  - A. Frequent
  - B. Infrequent

Paging
Virtual address translation

- A page table maps virtual pages to physical frames.
Virtual Address Translation Details

Page table structure

1 table per process
Part of process's state

Contents:
- Flags — dirty bit, resident bit, clock/reference bit
- Frame number

Virtual Addresses

CPU

Physical Addresses

PTBR

0 1
f

Page Table

Example

A system with 16-bit addresses
- 32 KB of physical memory
- 1024 byte pages

Virtual Address Space

Physical Memory

Page Table
Virtual Address Translation
Performance Issues

- Problem — VM reference requires 2 memory references!
  - One access to get the page table entry
  - One access to get the data

- Page table can be very large; a part of the page table can be on disk.
  - For a machine with 64-bit addresses and 1024 byte pages, what is the size of a page table?

- What to do?
  - Most computing problems are solved by some form of...
    - Caching
    - Indirection

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Virtual Address Translation
Using TLBs to Speedup Address Translation

- Cache recently accessed page-to-frame translations in a TLB
  - For TLB hit, physical page number obtained in 1 cycle
  - For TLB miss, translation is updated in TLB
  - Has high hit ratio (why?)
Dealing With Large Page Tables
Multi-level paging

- Add additional levels of indirection to the page table by sub-dividing page number into $k$ parts
  - Create a "tree" of page tables
  - TLB still used, just not shown
  - The architecture determines the number of levels of page table

Example: Two-level paging

```
CPU
  p1  p2  o
  20  16  10
  Virtual Addresses

PTBR + page table +
First-Level Page Table

Second-Level Page Table

Memory
  f
  16  10  1
  Physical Addresses
```
## The Problem of Large Address Spaces

- With large address spaces (64-bits) forward mapped page tables become cumbersome.
  - E.g. 5 levels of tables.

- Instead of making tables proportional to size of virtual address space, make them proportional to the size of physical address space.
  - Virtual address space is growing faster than physical.

- Use one entry for each physical page with a hash table
  - Size of translation table occupies a very small fraction of physical memory
  - Size of translation table is independent of VM size

## Virtual Address Translation
### Using Page Registers (aka Inverted Page Tables)

- Each frame is associated with a register containing
  - Residence bit: whether or not the frame is occupied
  - Occupier: page number of the page occupying frame
  - Protection bits

- Page registers: an example
  - Physical memory size: 16 MB
  - Page size: 4096 bytes
  - Number of frames: 4096
  - Space used for page registers (assuming 8 bytes/register): 32 Kbytes
  - Percentage overhead introduced by page registers: 0.2%
  - Size of virtual memory: irrelevant
Page Registers

How does a virtual address become a physical address?

- CPU generates virtual addresses, where is the physical page?
  - Hash the virtual address
  - Must deal with conflicts
- TLB caches recent translations, so page lookup can take several steps
  - Hash the address
  - Check the tag of the entry
  - Possibly rehash/traverse list of conflicting entries
- TLB is limited in size
  - Difficult to make large and accessible in a single cycle.
  - They consume a lot of power (27% of on-chip for StrongARM)

Dealing With Large Inverted Page Tables

Using Hash Tables

- Hash page numbers to find corresponding frame number
  - Page frame number is not explicitly stored (1 frame per entry)
  - Protection, dirty, used, resident bits also in entry
### Searching Inverted Page Tables
Using Hash Tables

- Page registers are placed in an array
- Page \( i \) is placed in slot \( f(i) \) where \( f \) is an agreed-upon hash function
- To lookup page \( i \), perform the following:
  - Compute \( f(i) \) and use it as an index into the table of page registers
  - Extract the corresponding page register
  - Check if the register tag contains \( i \), if so, we have a hit
  - Otherwise, we have a miss

### Searching the Inverted Page Table
Using Hash Tables (Cont’d.)

- Minor complication
  - Since the number of pages is usually larger than the number of slots in a hash table, two or more items may hash to the same location
  - Two different entries that map to same location are said to collide
- Many standard techniques for dealing with collisions
  - Use a linked list of items that hash to a particular table entry
  - Rehash index until the key is found or an empty table entry is reached (open hashing)
Questions

- Why use inverted page tables?
  - A. Forward mapped page tables are too slow.
  - B. Forward mapped page tables don’t scale to larger virtual address spaces.
  - C. Inverted pages tables have a simpler lookup algorithm, so the hardware that implements them is simpler.
  - D. Inverted page tables allow a virtual page to be anywhere in physical memory.

Virtual Memory (Paging)
The bigger picture

- A process’s VAS is its context
  - Contains its code, data, and stack
- Code pages are stored in a user’s file on disk
  - Some are currently residing in memory; most are not
- Data and stack pages are also stored in a file
  - Although this file is typically not visible to users
  - File only exists while a program is executing
- OS determines which portions of a process’s VAS are mapped in memory at any one time
Virtual Memory
Page fault handling

- References to non-mapped pages generate a page fault

Page fault handling steps:
- Processor runs the interrupt handler
- OS blocks the running process
- OS starts read of the unmapped page
- OS resumes/initiates some other process
- Read of page completes
- OS maps the missing page into memory
- OS restart the faulting process

Virtual Memory Performance
Page fault handling analysis

- To understand the overhead of paging, compute the effective memory access time (EAT)
  \[ EAT = \text{memory access time} \times \text{probability of a page hit} + \text{page fault service time} \times \text{probability of a page fault} \]

- Example:
  - Memory access time: 60 ns
  - Disk access time: 25 ms
  - Let \( p \) = the probability of a page fault
  - \( EAT = 60(1-p) + 25,000,000p \)

- To realize an \( EAT \) within 5\% of minimum, what is the largest value of \( p \) we can tolerate?
Vista reading from the pagefile

Vista writing to the pagefile
### Virtual Memory

**Summary**

- Physical and virtual memory partitioned into equal size units
- Size of VAS unrelated to size of physical memory
- Virtual pages are mapped to physical frames
- Simple placement strategy
- There is no external fragmentation
- Key to good performance is minimizing page faults

### Segmentation vs. Paging

- Segmentation has what advantages over paging?
  - A. Fine-grained protection.
  - B. Easier to manage transfer of segments to/from the disk.
  - C. Requires less hardware support
  - D. No external fragmentation

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