Continuum Diffusion Reaction Rate Calculations of Wild-Type and Mutant Mouse Acetylcholinesterase: Adaptive Finite Element Analysis

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ABSTRACT As described previously, continuum models, such as the Smoluchowski equation, offer a scalable framework for studying diffusion in biomolecular systems. This work presents new developments in the efficient solution of the continuum diffusion equation. Specifically, we present methods for adaptively refining finite element solutions of the Smoluchowski equation based on a posteriori error estimates. We also describe new, molecular-surface-based models, for diffusional reaction boundary criteria and compare results obtained from these models with the traditional spherical criteria. The new methods are validated by comparison of the calculated reaction rates with experimental values for wild-type and mutant forms of mouse acetylcholinesterase. The results show good agreement with experiment and help to define optimal reactive boundary conditions.

INTRODUCTION

Because of the important role that diffusion plays in a variety of biomolecular processes, computational models of diffusion have been widely studied using both discrete (Ermak and McCammon, 1978; Northrup et al., 1984; Agmon and Edelstein, 1997; Gabdoulline and Wade, 1998; Stiles and Bartol, 2000) and continuous methods (Smart and McCammon, 1998; Kurnikova et al., 1999; Schuss et al., 2001; Song et al., 2003; Tai et al., 2003). In a previous work (Song et al., 2003), we presented finite element methods for solving the Smoluchowski equation (SE) and thereby determined the steady-state behavior of diffusion-limited ligand binding events. These methods were shown to be significantly more efficient than traditional Brownian dynamics (BD) approaches for evaluating steady-state rate constants for diffusion-limited binding of simple ligands. However, the SE solution methods presented in the earlier work used only a fixed mesh and thereby neglected the powerful adaptive refinement features provided by finite element theory. Additionally, the previous work demonstrated the applicability of the finite element solvers using traditional spherical reactive surfaces used for calculation of reaction rate constants (Northrup et al., 1984; Antosiewicz et al., 1995, 1996; Elcock et al., 1996; Gabdoulline and Wade, 1998; Tara et al., 1998). However, finite element methods can easily represent much more complicated reaction criteria and therefore enable the assessment of alternative reactive boundaries.

In this work, we apply adaptive finite element methods using a posteriori error estimation to describe binding of substrate to wild-type and mutant mouse acetylcholinesterases (mAChEs). The AChE system has been a popular research target for both computational model and experimental studies because its hydrolysis of acetylcholine is diffusion-controlled and strongly influenced by electrostatics (Anglister et al., 1995; Radic et al., 1997). Previous computational studies of AChE ligand binding used the traditional spherical reactive surface (Radic et al., 1997; Song et al., 2003; Tara et al., 1998). In this work, we introduce a reactive boundary based on the molecular surface, thereby permitting the mapping of “active site” residues directly to the reactive boundary conditions.

Adaptive finite element solution of SE

Original and discretized steady-state SE

A detailed description of the steady-state SE, its application to bimolecular rate constant calculations, and its solution by finite element discretization of the SE were provided in the previous work (Song et al., 2003). Here, we present a brief review of the SE and the calculation of rate constants from its solutions.

For a stationary diffusion process, the SE has the following (steady-state) form:

\[
L_p(x) = \nabla \cdot J(p; x) = \nabla \cdot \left[ D(x) \nabla p(x) + \beta p(x) \nabla W(x) \right] = 0, \tag{1}
\]

where \( L \) is the Smoluchowskian operator, \( p(x) \) is the probability (concentration) of ligand at position \( x \in \mathbb{R}^3 \), \( J(p; x) \) is the probability flux, \( D(x) \) is the scalar diffusion coefficient,
\( \beta = (k_B T)^{-1} \) is the inverse thermal energy, and \( W(x) \) is the potential of mean force (PMF). Calculation of the reaction rate involves the solution of the above equation in a three-dimensional domain \( \Omega \) with the following boundary conditions. First, we specify the bulk concentration \( p_{\text{bulk}} \) via a Dirichlet condition on the outer boundary \( \Gamma_b \subset \partial \Omega \):

\[
p(x) = p_{\text{bulk}} \quad \text{for} \quad x \in \Gamma_b. \tag{2}
\]

Additionally, we specify the reaction condition on the active site boundary \( \Gamma_a \subset \partial \Omega \) for either a finite reactivity \( \alpha(x) \) via the Robin condition,

\[
\mathbf{n}(x) \cdot \mathbf{J}(p; x) = \alpha(x) p(x) \quad \text{for} \quad x \in \Gamma_a, \tag{3}
\]

or an infinite reactivity via the Dirichlet condition,

\[
p(x) = 0 \quad \text{for} \quad x \in \Gamma_a. \tag{4}
\]

Finally, we define the nonreactive boundary at \( \Gamma_r \subset \partial \Omega \) via the Neumann condition

\[
\mathbf{n}(x) \cdot \mathbf{J}(p; x) = 0 \quad \text{for} \quad x \in \Gamma_r. \tag{5}
\]

As can be seen from the above equations, the biomolecular surface is the union of the reactive and nonreactive boundaries: \( \Gamma_r \cup \Gamma_a \). Our observable is the diffusion-influenced biomolecular reaction rate constant \( k \), which can be calculated by integration of the flux over the active site boundary:

\[
k = p_{\text{bulk}}^{-1} \int_{\Gamma_a} \mathbf{n}(x) \cdot \mathbf{J}(p; x) \, dx. \tag{6}
\]

To numerically solve the SE, it is necessary to discretize the differential equation. Galerkin finite element methods (Axelsson and Barker, 1984) accomplish this discretization through integration by basis functions to give the bilinear form \( \langle F(p), v \rangle \):

\[
\langle F(p), v \rangle = \int_{\Omega} \nabla v \cdot \mathbf{J}(p; x) \, dx \\
- \int_{\Gamma_r \cup \Gamma_a} v(s) J(p; s) \cdot \mathbf{n}(s) \, ds, \tag{7}
\]

defined in terms of a test function \( v \), which is a member of the basis function set. The original SE (Eq. 1) can then be expressed in its so-called “weak form”:

Find \( p_h - \tilde{p}_h \in V_h \) such that \( \langle F(p_h), v_i \rangle = 0 \)

for all \( v_i \in V_h, \tag{8} \)

where \( p_h (x) \) is the approximate solution found by the numerical method, \( \tilde{p}_h(x) \) is a trace function satisfying the Dirichlet boundary conditions, and \( V_h \) is the function space spanned by the discrete basis set.

**Error estimation and mesh refinement**

As demonstrated in the previous work (Song et al., 2003), Eq. 8 can be used to solve the SE on a given finite element mesh. However, the quality of the resulting approximate solution depends strongly on the underlying finite element discretization of the problem. As their name implies, error estimation methods assess the accuracy of finite element solutions by providing estimates of the difference between the approximate and “true” solutions (Axelsson and Barker, 1984; Braess, 1997). These methods are often used in finite element solutions to guide selective refinement of the finite element mesh (Baker et al., 2000, 2001a; Holst et al., 2000; Holst, 2001; M. Holst and D. Bernstein, unpublished) and thereby adaptively improve the quality of the numerical solution.

In this article, adaptive mesh refinement methods are used in a “solve-estimate-refine” algorithm as described by Holst and co-workers (Baker et al., 2000, 2001a; Holst et al., 2000; Holst, 2001; M. Holst and D. Bernstein, unpublished) and implemented in the FEtk software (http://www.fetk.org/).

The first step of this procedure (solve) is the calculation of an approximate solution to the SE \( p_h (x) \) on the current finite element mesh (Song et al., 2003). In the second step (estimate), this solution is used to provide a per-simplex residual-based a posteriori error estimate \( \eta \) of the form (Holst, 2001):

\[
\eta^2_s = h_s^2 \left| \left| \mathbf{J}_s \right| \right|_{L^2(s)}^2 + \frac{1}{2} \sum_{f \in s} h_f^2 \left| \left| \nabla \cdot \mathbf{J}_f \right| \right|_{L^2(f)}^2, \tag{9}
\]

for a simplex \( s \), where \( h_s \) is the size of the element, \( \mathbf{J}_s(p; x) \) is the current numerical estimate of the flux, \( f \in s \) denotes a face of simplex, \( h_f \) is the size of the face \( f \), \( \left| \left| \nabla \cdot \mathbf{J}_f \right| \right|_{L^2(f)} \) denotes the jump across the face of some function \( v \), \( \mathbf{n}(s) \times \mathbf{J}_s(s) \) is the component of the flux normal to element face \( f \), and the Lebesgue norms are defined as

\[
\left| \left| v \right| \right|_{L^2(\text{ref})}^2 = \int_{\text{ref}} \left| v(x) \right|^2 \, dx. \tag{10}
\]

Finally, in the third step (refine), this per-simplex error estimate \( \eta \) is used to identify simplices of the finite element mesh where the error is above a particular tolerance. Simplices with a high error estimate value are refined by longest-edge bisection. This entire “solve-estimate-refine” cycle is repeated until the global error \( \sqrt{\sum \eta^2_s} \) is reduced to an acceptable user-defined level.

As described previously, methods for solving the SE have been implemented in a software package called “SMOL.” This software uses the Holst group FETk toolkit (http://www.fetk.org/) for finite element geometric routines,
Validation of the adaptive SMOL finite element solver with a spherical system

To validate the new adaptive finite element features of the SMOL software, we examined a classic spherical test case (Krissinel and Agmon, 1996) and compared calculated rate constants with the analytical results. For this test case, we chose a fixed sphere with an 8 Å radius and a diffusing sphere with a 2 Å radius; both spheres had variable charge. The smaller sphere’s diffusion constant $D(x)$ was chosen as a constant $7.8 \times 10^4 \text{Å}^2 \mu s$, a value obtained from the Stokes-Einstein relationship for a 2–3 Å substrate (tetramethyl ammonium) in water (Tara et al., 1998). The PMF ($W(x)$ in Eq. 1) for these calculations was obtained from Coulomb’s law for a homogeneous dielectric of 78.54.

The outer boundary of the diffusion domain was chosen to be 40 times the combined size of the fixed and diffusing spheres (i.e., a 400 Å radius) and the inner boundary (at 10 Å) was uniformly reactive with the perfectly-absorbing boundary condition described by Eq. 4. The entire domain was initially discretized into 445,488 tetrahedral elements using the contouring methods of Zhang and co-workers (Song et al., 2003; Zhang et al., 2003). Note that this is a much coarser mesh than used in the previous work (Song et al., 2003). However, the surface area of the spherical inner boundary of this coarser mesh (1257.98 Å$^2$) differed by only 0.11% from the actual area of a 10 Å sphere (1256.64 Å$^2$), indicating that the finite element mesh realistically represents the boundary geometry.

Fig. 1 presents the binding rate constant calculations as a function of ligand charge for fixed spheres with $\pm 1$ e and $\pm 10$ e charges. Results from $\pm 1$ e fixed-sphere charge show that the adaptive methods generate results which are in much better agreement ($<1\%$ relative error) with the analytical solutions than nonadapted results (8% relative error). Furthermore, for the $\pm 10$ e fixed sphere charge, the adaptive methods can provide up to $\sim 25\%$ improvement in the rate constants compared to the nonadapted calculations.

Because of the error estimation and adaptive meshing during the finite element solution, the adaptive calculations require more computational effort compared to the nonadaptive calculations. The following timing results were obtained using a version of SMOL compiled with Intel FORTRAN and C (version 8.0, ‘‘-O2’’ optimization) and running on a 2.4 GHz Intel Xeon machine with 1.5 GB RAM. The nonadaptive method requires an average of 180 s per calculation whereas the adaptive technique requires an average of 6000 s per calculation. This factor of $\sim 30$ increase in computation time represents an extreme case of adaptive refinement—the current case was specifically chosen to demonstrate the ability of the method to refine from a very coarse initial mesh to the correct answer. As described in the Conclusions of this work, the ‘‘real world’’ application of the adaptive method would likely start from a much finer mesh and therefore require substantially fewer rounds of adaptive refinement and lower overall computation time.

Rate constant calculations for mAChE ligand binding

AChE (E. C. 3.1.1.17) is a serine esterase which hydrolyzes the neurotransmitter acetylcholine at diffusion-limited rates (Anglister et al., 1995). Previously, we investigated the ligand-binding kinetics of mAChE by calculating steady-state rate constants using a nonadaptive version of the SMOL software and the spherical reactive boundary condition commonly used in Brownian dynamics reaction rate calculations (Song et al., 2003). Here, we use our new adaptive finite element scheme to investigate the binding kinetics of mutant and wild-type mAChE using a new reactive boundary based on the biomolecular surface.

mAChE domain geometry

Like the previous calculations (Song et al., 2003), the starting geometry for these calculations is the ‘‘open’’ mAChE structure used by Tara et al. (1998) to study mAChE binding kinetics. Using an outer boundary 40 times the size of the biomolecule (an ellipsoid with dimensions 3130 Å $\times$ 2770 Å $\times$ 3680 Å), this domain was discretized using the dual contouring methods described previously (Song et al., 2003; Zhang et al., 2003) into an initial mesh containing 656,823 tetrahedral elements. Fig. 2 shows a cross section of the mesh between the mAChE surface and the outer sphere generated from the LBIE-Mesh software (http://www.ices.utexas.edu/CCV/software). Note that the
Adaptive Finite Element Solution of Diffusion to mAChE

mesh near the biomolecule is extremely fine and captures the
details of the biomolecular surface; mesh elements increase
in size with increasing distance from the biomolecule.

The outer boundary of the domain was assigned bulk
Dirichlet boundary conditions (Eq. 2), the nonreactive
portions of the inner boundary were assigned reflective
Neumann conditions (Eq. 5), and the reactive portions were
assigned the “infinite reactivity” Dirichlet condition (Eq. 4).
This reactive condition was chosen to agree with previous
BD (Tara et al., 1998) and SE (Song et al., 2003) simulations
and is justified by the extremely high catalytic efficiency of
mAChE (Anglister et al., 1995). In the previous finite
element SE studies, the reactive boundary was defined as the
spherical reactive surface typical for Brownian dynamics
calculations (Song et al., 2003). In the current study, the
reactive boundary is defined using the biomolecular surface.
Following Tara et al. (1998), the mAChE structure was
reoriented to center the carbonyl carbon of the active site
S203 at the origin and to align the active site gorge with the
y axis. Reactive boundaries were based on 6 spheres placed
along the y axis: sphere 1 centered at (0.0, 16.6, 0.0) with a 12
Å radius, sphere 2 centered at (0.0, 13.6, 0.0) with a 9 Å
radius, sphere 3 centered at (0.0, 10.6, 0.0) with a 6 Å radius,
sphere 4 centered at (0.0, 7.6, 0.0) with a 6 Å radius, sphere 5
centered at (0.0, 4.6, 0.0) with a 6 Å radius, and sphere 6
centered at (0.0, 1.6, 0.0) with a 6 Å radius. For the
biomolecular surface-based reaction criteria, each reactive
surface \( N \) was defined as that portion of the mAChE
molecular surface inside the union of spheres \( N \) through 6.
For example, surface 1 was the portion of the mAChE
surface inside the union of spheres 1–6 whereas surface 6
was the portion of the mAChE surface inside 6. The six
reactive surfaces defined in this manner are shown in Fig. 3
a. This definition differs considerably from the spherical
reaction criteria used in the previous work (Song et al., 2003)
wherein each reactive surface \( N \) was defined by explicitly
including the union of spheres \( N–6 \) in the mAChE structure.
For comparison, the first reactive surface of based on the
spherical definition is shown in Fig. 3 b.

**Wild-type mAChE reaction rates**

mAChE reaction rates were calculated with the initial mesh
and new reactive boundary definitions described. The
diffusing ligand was treated as a sphere with a +1 e charge,
a 2.0 Å exclusion radius, a diffusion constant of \( 7.8 \times 10^3 \)
Å\(^2\)/μs; this spherical model and its parameters are similar to
those used in previous BD models of the TFK ligand (Tara
et al., 1998). Following standard procedure in BD-based rate
constant calculations, only electrostatic contributions to the
PMF for the SE were included in these calculations,
reflecting the known importance of electrostatics in mAChE
binding kinetics (Radic et al., 1997). Although the true PMF
is certainly more complex than this simple description, such
simple interaction models have successfully been used in
numerous BD calculations of binding rate constants (for
elements, see Allison and McCammon, 1985; Antosiewicz
and McCammon, 1995; Tara et al., 1998). (For an excellent
example of diffusion simulations with more detailed PMFs,
see Im and Roux, 2002). Other considerations in developing
more accurate effective ligand-protein interactions are pre-
sented in the context of protein-protein encounter simul-
ations by Elcock et al. (2001). Finally, Roux and Simonson
(1999) provide a very good general discussion of the caveats
associated with the simple implicit solvent electrostatic
PMF used here.

The electrostatic potential used for our PMF was obtained
from the Poisson-Boltzmann equation using the APBS
software (http://agave.wustl.edu/apbs/) (Baker et al., 2001b).
The CHARMM22 force field was used to assign the partial
changes and radii of the atoms for mAChE, the dielectric
values of 4 and 78 were assigned for the protein and solvent,
a solvent probe radius is 1.4 Å, and an ion exclusion layer is
2.0 Å. Various ionic strengths (between 0 and 0.670 M) were
used in the PMF calculations.

Additionally, the adaptive finite element methods de-
scribed above were used to calculate the reaction rates for
both the molecular-surface-based (Fig. 3 a) and spherical
(Fig. 3 b) reactive boundary No. 1 as a function of ionic
strength. Iterative error-based refinement of the initial
656,823-simplex mesh was performed until the global error
was \(<10^7\), a problem-value chosen to provide reaction rates
which did not change appreciably upon further refinement
(see Fig. 4). The reaction rate results from these calculations
are shown in Fig. 5. As this figure illustrates, the spherical
and molecular-surface-based reaction criteria both give
results that are in good overall agreement with each other
and experiment. The comparison (at 150 mM ionic strength)
between the molecular and spherical boundary definitions for
the 6 reactive surfaces is shown in Fig. 6. Again, the two
methods are in good overall agreement but do show some

**FIGURE 2** Cross section of the initial finite element mesh used for
mAChE calculations.
differences at surfaces No. 1 and No. 2 where the differences between the reactive boundaries—in particular, their surface areas—are most extreme (see Fig. 3).

Table 1 illustrates the rate constants for various ionic strengths obtained with and without error-based adaptation of the mesh. The reaction rates calculated from the adaptive finite element solution for wild-type mAChE deviate by \( \sim 10\% \)–100\% from the nonadapted calculation for the molecular reactive surface and by \( \sim 1\% \)–10\% for the spherical reactive surface. Therefore, although the mesh used in the previous work (Song et al., 2003) is fine enough for the qualitative description of ionic strength dependence, there are cases where substantial improvement is provided by the

**FIGURE 3** Reactive boundary definitions for mAChE: (a) molecular reactive boundaries Nos. 1–6 (left to right) and (b) spherical reactive boundary No. 1.

**FIGURE 4** Percent change in the calculated wild-type mAChE reaction rates during adaptive refinement for 0 ( ), 50 ( ), 100 ( ), 150 ( ), 300 ( ), 450 ( ), and 670 (*) mM ionic strengths.

**FIGURE 5** Comparison mAChE wild-type ligand binding rates calculated with various methods: adaptive calculation with molecular reactive boundary No. 1 ( ), nonadaptive calculation with molecular reactive boundary No. 1 ( ), adaptive calculation with spherical reactive boundary No. 1 ( ), Brownian dynamics calculation with spherical reactive boundary No. 1 ( ), and from Debye-Hückel fit to experimental data (Tara et al., 1998) (solid line).
adaptive method. Furthermore, it is important to note that the simple geometric definitions used to generate the initial nonadapted mesh for mAChE may not always give even a qualitative level of predictive power without subsequent error-based refinement. In particular, molecules with high charge densities (nucleic acids, actin, etc.) will likely require error-based adaptive refinement to generate reliable diffusion profiles and rate constants. Therefore, when applying this method, it is recommended that users examine the sensitivity of the results to adaptive refinement before using rates from any nonadapted calculations.

As with the spherical case, adaptive finite element calculations are significantly more expensive than their nonadapted counterparts. As for the sphere test case, the following timing data was obtained using a version of SMOL compiled with Intel FORTRAN and C (version 8.0, ‘‘−O2’’ optimization) and running on a 2.4 GHz Intel Xeon machine with 1.5 GB RAM. For the molecular reactive boundary, the average nonadapted runtime was 415 seconds and the average adapted runtime was 8800 seconds; for the spherical reactive boundaries the average nonadapted and adapted runtimes were 415 and 6600 seconds, respectively. The impact of this increased computational effort is discussed in the Conclusions section of this work.

**TABLE 1 Nonadaptive and adaptive solution results of reaction rates (in units of 10⁹ M⁻¹ min⁻¹) for reactive surface 1 of wild-type mAChE**

<table>
<thead>
<tr>
<th>Ionic Strength</th>
<th>Nonadapted results</th>
<th>Adapted results</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>758 (971)</td>
<td>853 (1040)</td>
</tr>
<tr>
<td>50</td>
<td>249 (324)</td>
<td>293 (354)</td>
</tr>
<tr>
<td>100</td>
<td>209 (277)</td>
<td>237 (294)</td>
</tr>
<tr>
<td>150</td>
<td>188 (254)</td>
<td>213 (265)</td>
</tr>
<tr>
<td>300</td>
<td>152 (223)</td>
<td>165 (227)</td>
</tr>
<tr>
<td>450</td>
<td>117 (208)</td>
<td>131 (207)</td>
</tr>
<tr>
<td>670</td>
<td>35 (191)</td>
<td>77 (189)</td>
</tr>
</tbody>
</table>

Values not in parentheses are from the molecular reactive surface; results in parentheses are from the spherical reactive surface.
two methods. Such discrepancies in predicted rates are not too surprising and simply reflect differences in methods, particularly their definitions of reactions and reactive boundaries.

CONCLUSIONS AND DISCUSSIONS

We have presented an adaptive version of the finite element solver described in an earlier work (Song et al., 2003) and demonstrated that error-based refinement of the mesh improves the calculation of reaction rates. Additionally, we have described a new molecular-surface reactive boundary definition for the SE and applied this definition to the calculation of ligand-binding rates for mAChE. The molecular-surface reactive boundary condition showed good agreement with the experimental dependence of binding rate on ionic strength and mutations. Additionally, the adaptive molecular-surface calculation results were comparable to the trends observed in BD simulations, although specific values varied by as much as two orders of magnitude between the two methods. Comparisons with experimental mutation results show that molecular reactive surface within 10.6 Å from the active site best represents the effect of D74N, E202Q, and D74N/E202Q mutations on the reaction rate of mAChE.

The timing information provided for the adaptive method illustrates that it is definitely more computationally-demanding than the nonadaptive calculations and, in some cases, even more expensive than the traditional BD simulations. However, judicious use of these expensive calculations can save substantial time and still provide an overall gain over BD simulations. As mentioned earlier, the initial mesh is generated based on the biomolecular geometry and does not necessarily provide the best possible basis set for solution of the SE. Therefore, adaptive refinement should be a standard part of finite element SE calculations to ensure the most accurate results. In particular, a “benchmark” adaptive refinement calculation is needed for each system studied to determine the error in rates calculated on the initial mesh and to obtain the global error tolerance at which the calculated rates are converged (cf. Fig. 4). However, much of the refinement performed in the each of the various adaptive calculations described above is redundant; i.e., the same regions of the initial mesh are refined for each system. Therefore, substantial time could be saved by reusing the refined mesh from the benchmark calculation as a starting point for subsequent simulations and thereby avoiding some of the expensive refinement steps.
Furthermore, as mentioned in the previous work, these continuum diffusion methods are designed to address a different scale of simulation from traditional BD methods; specifically, laying the groundwork for integration of molecular-scale information into cellular-scale systems (Smart and McCammon, 1998; Tai et al., 2003). In particular, this ability of FE-based continuum methods to integrate scales demonstrates by performing the diffusion calculations on a finite element mesh of 0.31 μm × 0.28 μm × 0.37 μm, or ~5 times the length of the BD domain (600 Å long). The adaptive methods developed in this work further facilitate our ultimate goal of multiscale modeling by enabling the efficient solution of the SE through adaptively allocating the unknowns based on error estimates.

Finally, one particularly useful aspect of the molecular surface boundary definition introduced in this work is the ability to directly connect the reactive surfaces of the simulation with the underlying biomolecule. For example, surface 6 maps directly onto the catalytic triad and are the most intuitive reactive boundary definitions available for this system. Additionally, these surfaces performed well in quantifying the impact of mutation on binding-rate constants. Such molecular-based reactive definitions suggest future possibilities of connecting coarse-grained simulations of diffusion with more detailed descriptions of enzyme function; in particular molecular dynamics and quantum mechanics worked describing the details of biomolecular binding and catalysis (Luty et al., 1993; Zhang et al., 2002).

REFERENCES


