# CS429: Computer Organization and Architecture Optimization II

Dr. Bill Young
Department of Computer Science
University of Texas at Austin

Last updated: April 24, 2019 at 07:47

### Cache Performance Metrics

#### Miss Rate

- Fraction of memory references not found in cache (misses / references)
- Typical numbers: 3-10% for L1; can be quite small (e.g., < 1%) for L2, depending on size, etc.

#### Hit Time

- Time to deliver a line in the cache to the processor (including time to determine whether the line is in the cache).
- Typical numbers: 1-3 clock cycles for L1; 5-12 clock cycles for L2.

#### Miss Penalty

- Additional time required because of a miss.
- Typically 100-300 cycles for main memory.

CS429 Slideset 21: 1

Optimization II

CS429 Slideset 21: 2

Optimization

### Writing Cache Friendly Code

- Repeated references to variables are good (temporal locality).
- Stride-1 reference patterns are good (spatial locality).

#### **Examples:**

Assume cold cache, 4-byte words, 4 word (16-byte) cache blocks.

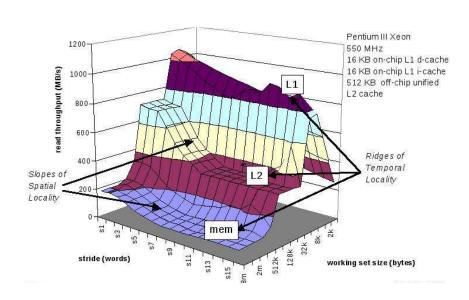
```
int sumarrayrows(int a[M][N])
{
   int i, j, sum = 0;
   for( i = 0; i < M; i++ )
      for( j = 0; j < N; j++ )
      sum += a[i][j];
   return sum;
}</pre>
```

Miss rate = 1/4 = 25%

```
int sumarraycols(int a[M][N])
{
   int i, j, sum = 0;
   for( j = 0; j < N; j++ )
      for( i = 0; i < M; i++ )
      sum += a[i][j];
   return sum;
}</pre>
```

Miss rate = 100%

### The Memory Mountain



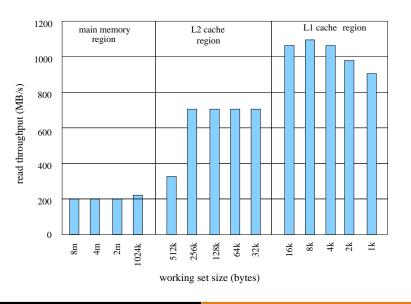
Why would performance drop as the working set gets very small?

CS429 Slideset 21: 3 Optimization II

### Ridges of Temporal Locality

### Slice through the memory mountain with stride = 1.

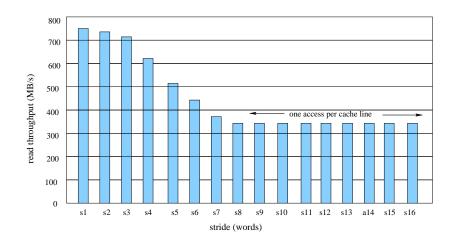
This illustrates read throughput with different caches and memory.



### A Slope of Spatial Locality

#### Slice through memory mountain with size = 256KB.

This shows cache block size.



CS429 Slideset 21: 5

Optimization II

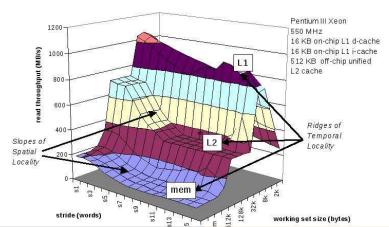
CS429 Slideset 21: 6

Ontimization

### **Anomaly in Memory Mountain**

#### Why does the memory mountain drop off at the back? Prof.

Warren Hunt told me: "When I looked into this issue, I didn't come to a clean resolution. Perhaps the dropoff is a measurement anomaly; the times are so short in comparison to the measurement costs that it appears that the performance is degrading."



### Matrix Multiplication Example

### Major Cache Effects to Consider.

- Total cache size: Exploit temporal locality and keep the working set small
- Block size: Exploit spatial locality.

#### Description

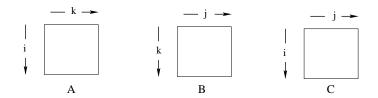
- Multiply  $N \times N$  matrices.
- $O(N^3)$  total operations.
- Accesses:
  - N reads per source element
  - N values summed per destination (but may be held in register).

### Miss Rate for Matrix Multiply

#### Assume:

- Line size = 32B (big enough for 4 64-bit words)
- Matrix dimension N is very large.
- We can approximiate 1/N as 0.0.
- Cache is not even big enough to hold multiple rows.

Analysis Method: Look at access pattern of the inner loop.



CS429 Slideset 21: 9

### Layout of C Arrays in Memory (review)

#### C arrays are allocated in row-major order.

• Each row is allocated in contiguous memory locations.

#### Stepping through columns in one row:

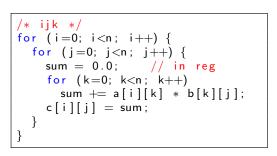
- This accesses successive elements.
- If block size B > 4 bytes, exploits spatial locality.
- Compulsary miss rate = 4 bytes / B.

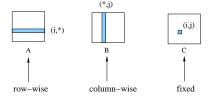
#### Stepping through rows in one column:

- Accesses distant elements.
- No spatial locality!
- Compulsary miss rate = 1 (i.e., 100%).

CS429 Slideset 21: 10

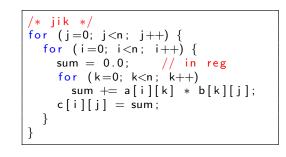
### Matrix Multiplication (ijk)

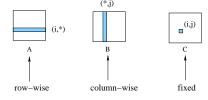




Misses per Inner Loop Iteration:

## Matrix Multiplication (jik)



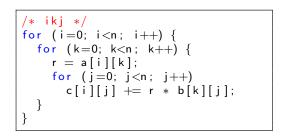


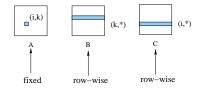
Misses per Inner Loop Iteration:

```
/* kij */
for (k=0; k< n; k++) {
 for (i=0; i< n; i++) {
    r = a[i][k];
    for (j=0; j< n; j++)
      c[i][j] += r * b[k][j];
```

```
fixed
                            row-wise
            row-wise
```

Misses per Inner Loop Iteration:





Misses per Inner Loop Iteration:

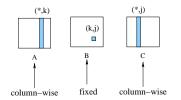
CS429 Slideset 21: 13

CS429 Slideset 21: 14

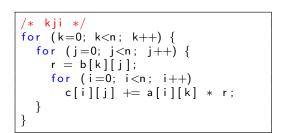
### Matrix Multiplication (jki)

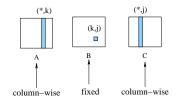
### Matrix Multiplication (kji)

```
/* iki */
for (j=0; j< n; j++) {
 for (k=0; k< n; k++) {
    r = b[k][j];
    for (i=0; i< n; i++)
      c[i][j] += a[i][k] * r;
```



Misses per Inner Loop Iteration:





Misses per Inner Loop Iteration:

### Summary of Matrix Multiplication

### Concluding Observations

### ijk (& jik):

- 2 loads, 0 stores
- misses / iteration = 1.25

### kij (& ikj):

- 2 loads, 1 store
- misses / iteration = 0.5

#### jki (& kji):

- 2 loads, 1 store
- misses / iteration = 2.0

Miss rates are important, but not perfect predictors of performance.. Code scheduling matters, also.

#### The programmer can optimize for cache performance.

- How data structures are organized.
- How data are accessed (e.g., nested loop structure).

#### All systems favor "cache friendly code."

- Getting absolute optimum performance is very platform specific.
- Involves cache sizes, line sizes, associativities, etc.
- Can get most advantage with generic code.
- Keep working set reasonably small (temporal locality).
- Use small strides (spatial locality).

CS429 Slideset 21: 17

Optimization II

CS429 Slideset 21: 18

Optimization