















Outline

- Thresholding
- Connected components
- Morphological operators
- Region properties
 - Spatial moments
 - Shape
- Distance transforms
 - Chamfer distance



GIBBON/simplebinary.html

Selecting thresholds

- Partition a bimodal histogram
- Fit Gaussians
- Dynamic or local thresholds



A nice case: bimodal intensity histograms

- Example
- Thresholding a bimodal histogram
- Otsu method (1979) : automatically select threshold by minimizing the weighted *within-group variance* of the two groups of pixels separated by the threshold.









Connected components

- Various algorithms to compute
 - Recursive (in memory)
 - Two rows at a time (image not necessarily in memory)
 - Parallel propagation strategy

Prind an unlabeled pixel, assign it a new label Search to find its neighbors, and recursively repeat to find their neighbors til there are no more Repeat





Morphological operators

- Dilation
- Erosion
- Open, close





Dilation / Erosion

- Dilation: if current pixel is foreground, set all pixels under S to foreground in output (OR)
- Erosion: if every pixel under S is foreground, leave as is; otherwise, set current pixel to background in output










































<section-header><section-header><list-item><list-item><complex-block>



Before closing

After closing











Region properties

Some useful features can be extracted once we have connected components, including

- Area
- Centroid
- Extremal points, bounding box
- Circularity
- Spatial moments





Shapiro & Stockman





Central moments

- 2nd central moment: variance
- 3rd central moment: skewness
- 4th central moment: kurtosis





Distance transform



Edge image



Distance transform image















Binary images

- Pros
 - Can be fast to compute, easy to store
 - Simple processing techniques available
 - Lead to some useful compact shape descriptors
- Cons
 - Hard to get "clean" silhouettes, noise common in realistic scenarios
 - Can be too coarse of a representation
 - Not 3d

Matlab

- N = HIST(Y,M)
- L = BWLABEL(BW,N);
- STATS = REGIONPROPS(L, PROPERTIES) ;
 - 'Area'
 - 'Centroid'
 - BoundingBox'
 - 'Orientation', ...
- IM2 = imerode(IM,SE);
- IM2 = imdilate(IM,SE);
- IM2 = imclose(IM, SE);
- IM2 = imopen(IM, SE);
- [D,L] = bwdist(BW,METHOD);

```
• Everything is matrix
```

```
1
   **** Matrix Definition 1 ****
2 A = [1 2 3 4;5 6 7 8];
3
4 %%%% Matrix Definition 2 %%%%
   A = [1:1:4; 5:1:8];
5
6
7
   **** Matrix Definition 3 ****
8
   for i = 1:2
9
       for j = 1:4
           A(i,j) = (i-1)*4+j;
10
11
       end
12
   end
   13
14
   **** Matrix Definition 4 ****
15 A = [];
   A = zeros(n,n); %ones zeros eye rand randn
16
```

Tutorial adapted from W. Freeman, MIT 6.896
• Matrix index

18	%%%% Matrix	index	
19	A = magic(4)	;	
20	>> A =		
21	16 2	2 3	13
22	5 1:	L 10	8
23	9 '	76	12
24	4 14	1 15	1
25	A(1:2, 1:2)		
26	>> ans =	=	
27	16 2	2	
28	5 1:	L	
29	A(:,1)		
30	>> ans =	=	
31	16		
32	5		
33	9		
34	4		
35	A(1,:)		
36	>> ans =	=	
37	16 2	2 3	13
38	A([6 7])		
39	>> ans =	=	
40	11 7	7	

```
• Manipulate matrices
            44
                A = [1 NaN 2 NaN;3 Inf 4 Inf]; %1/0=Inf 0/0=NaN
            45
               %%%% replace Nan/Inf with O
            46 for i = 1:size(A,1)
            47
                   for j = 1:size(A,2)
            48
                     if isnan(A(i,j)) | isinf(A(i,j))
            49
                          A(i,j) = 0;
            50
                      end
            51
                   end
            52 end
            53
            54 %%%% 'find'
            55 a = [0 1 0 2;0 3 0 4]
                  >> a =
            56
            57
                  0
                        1 0 2
                  0 3 0 4
            58
            59 find(a)
            60
                  >> ans = [3 4 7 8]'
            61 [ii jj] = find(a);
            62
                 >> ii = [1 2 1 2]
            63
                   >> jj = [2 2 4 4]
            64
            65 nanflag = isnan(A)
            66
                 >> nanflag =
                  0 1 0
0 0 0
            67
                                   1
                                 0
            68
            69
               infflag = isinf(A)
                 >> infflag =
            70
               0 0 0
0 1 0
            71
                                   Ο
            72
                                 1
```

• Manipulate matrices

```
75 👫%% Matrix operation
76
   A = [1 2; 3 4];
77
   B = [1 \ 1; 1 \ -1];
78
    A*B
79
        >> ans =
80
        3 -1
        7
81
              -1
82
    A.*B
83
      >> ans =
84
        1
               2
85
        3 -4
86
    A/B \approx A \pm inv(B)
87
       >>ans =
       1.5 -0.5
88
89
       3.5 -0.5
90
    A./B
      >> ans =
91
92
               2
        1
93
       3
             -4
```

```
95 %%%% Matrix concatenation
96 A = [1 2];B = [3 4];
97 C = [A B]
       >>C =
98
            2
99
        1
                   3
                        4
   C = [A;B]
100
101
        >>C =
102
       1
              2
103
        3
              4
```

```
A = [1 2];
A^*A' = 5
A.^*A = 1 4
sum(A.^*A) = 5
```

Scripts and functions

- Scripts are m-files containing MATLAB statements
- Functions are like any other m-file, but they accept arguments
- Name the function file the same as the function name

myfunction.m

myotherfunction.m

```
function [y, z] = myotherfunction(a, b)
% Function of two arguments with two return values
y = a + b;
z = a - b;
```

• Try to code in matrix ways

```
115 %use for loops
116 A = [1 2 3 4;5 6 7 8];
117 sum(A)
118
        >> ans =
119
        6 8 10 12
120 ASUM = sum(A,2)
121
     >> ASUM =
122
       10
123
       26
124 for i = 1:size(A,1)
125
     for j = 1:size(A,2)
126
        APROB(i,j) = A(i,j)/ASUM(i);
127
        end
128 end
129
130 %use matrix
131 A = [1 2 3 4;5 6 7 8];
132 ASUM = sum(A, 2)
133 APROB = A./repmat(ASUM, 1, size(A,2));
134
135 repmat(ASUM, 1, size(A,2))
136
      >> ans =
       10 10 10
137
                      10
      26 26 26
138
                        26
```

• whos

- help
- lookfor
- clear / clear x
- save
- load