

### Last time

- Appearance-based recognition: using global appearance descriptions within a window to characterize a class.
  - Classification: basic idea of supervised learning
    - Skin color detection example
  - Sliding windows: detection via classification
    - Make a yes/no decision at every window
    - Face detection example using boosting and rectangular features [Viola-Jones 2001]

### Misc notes

- · Extra disk space
- SIFT extraction
  - http://www.cs.ubc.ca/~lowe/keypoints/

Demo Software: SIFT Keypoint Detector

This page provides scores to a denso version of Devid Lover's SET keypoint detector in the form of coupled binaries that can remade Lance or Windows. The dense software ware PCM forms for image squet. It can empt keypoint and all advantages seen for marking form to a file in a simple ACM Life issue. A Software program of the program and supple C code or provided that can read the

The image on the right shows an example of southing producley the dones software. Features are extracted from each of the two images, and there are chosen between features of the laws of meetches. In this example, many matches are found and only a small fraction are incorrect.

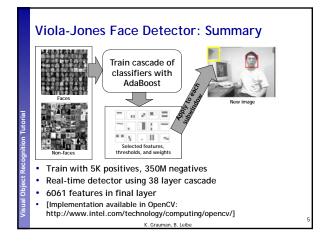
and first time are incorrect.

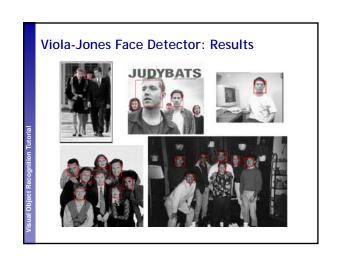
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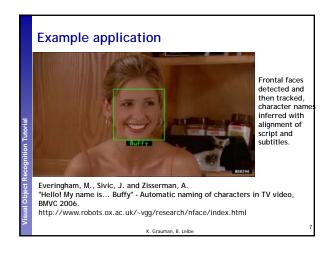
SEET dense program (Nicolan 4, July 2005)

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- Additional classes well-suited by global appearance representations
- Discriminative classifiers
  - Boosting (last time)
  - Nearest neighbors
  - Support vector machines
    - Application to pedestrian detection
    - Application to gender classification

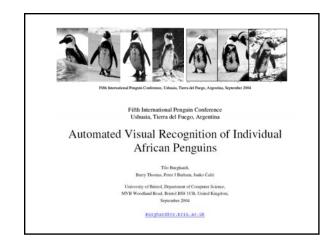








 Other classes that might work with global appearance in a window?



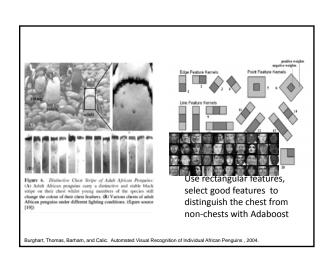
# Penguin detection & identification

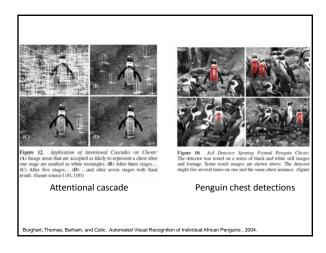


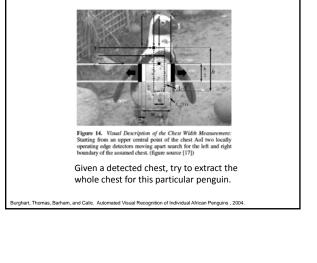
African penguins (Spheniscus demersus) carry a pattern of black spots on their chests that does not change from season to season during their adult life. Further, as far as we can tell, no two penguins have exactly the same pattern. We have developed a real-time system that can confidently locate African penguins whose chests are visible within video sequences or still images. An extraction of the chest spot pattern allows the generation of a unique biometrical identifier for each penguin. Using these identifiers an authentication of filmed or photographed African penguins against a population database can be performed. This paper provides a detailed technical description of the developed system and outlines the scope and the conditions of applications.

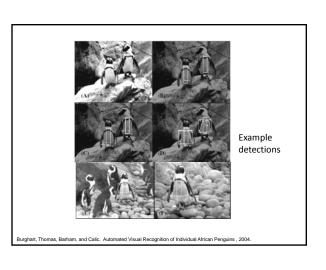
This project uses the Viola-Jones Adaboost face detection algorithm to detect penguin chests, and then matches the pattern of spots to identify a particular penguin.

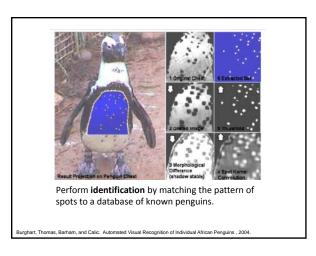
Burghart, Thomas, Barham, and Calic. Automated Visual Recognition of Individual African Penguins , 2004.

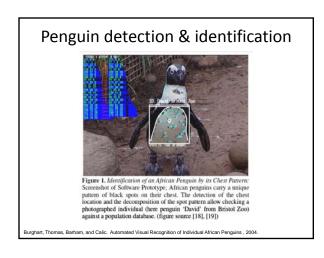


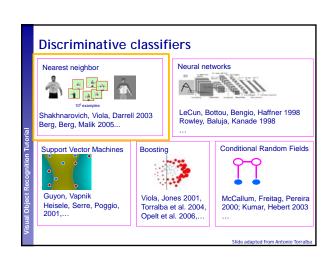












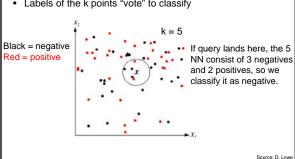
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### **Nearest Neighbor classification** · Assign label of nearest training data point to each test data point Black = negative Novel test example Red = positive Closest to a positive example from the training set, so classify it as positive. Voronoi partitioning of feature space for 2-category 2D data

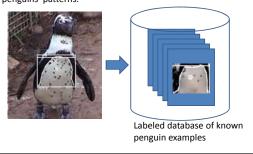
# K-Nearest Neighbors classification · For a new point, find the k closest points from training data

- · Labels of the k points "vote" to classify



# Example: nearest neighbor classification

• We could identify the penguin in the new view based on the distance between its chest spot pattern and all the stored penguins' patterns.

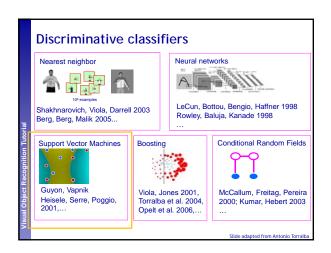


# Example: nearest neighbor classification • Similarly, if the video frames we were indexing in the Video

Google database had labels, we could classify the query. NN #1 NN #2 Querv NN #3 Labeled database of frames from movie

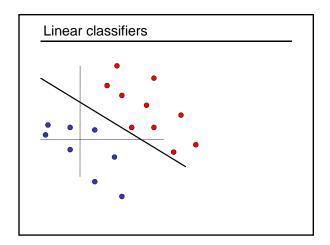
# Nearest neighbors: pros and cons

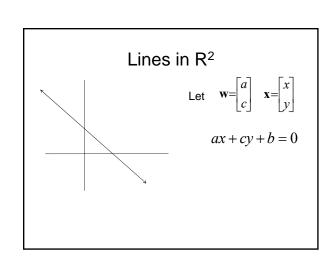
- Pros:
  - Simple to implement
  - Flexible to feature / distance choices
  - Naturally handles multi-class cases
  - Can do well in practice with enough representative
- · Cons:
  - Large search problem to find nearest neighbors
  - Storage of data
  - Must know we have a meaningful distance function

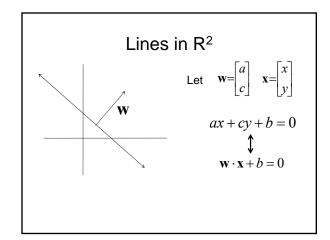


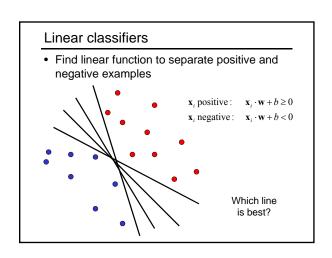
# Today

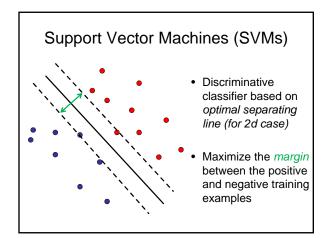
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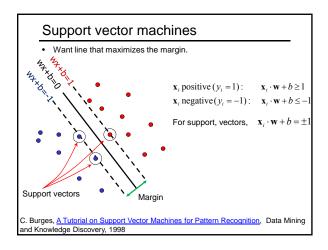


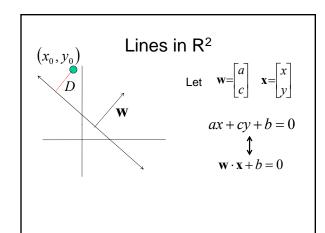


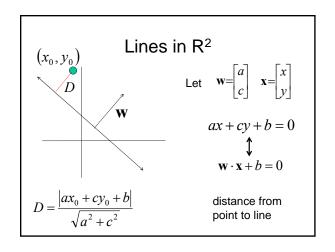


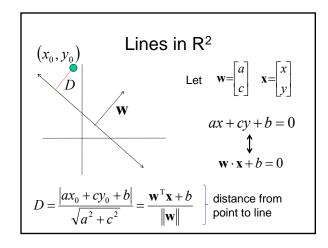


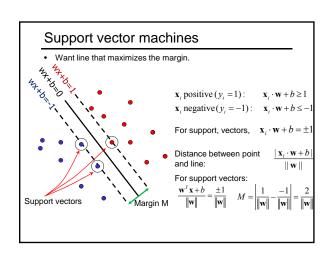












# 

### Finding the maximum margin line

- 1. Maximize margin  $2/||\mathbf{w}||$
- 2. Correctly classify all training data points:

$$\mathbf{x}_i$$
 positive  $(y_i = 1)$ :  $\mathbf{x}_i \cdot \mathbf{w} + b \ge 1$   
 $\mathbf{x}_i$  negative  $(y_i = -1)$ :  $\mathbf{x}_i \cdot \mathbf{w} + b \le -1$ 

Quadratic optimization problem:

Minimize 
$$\frac{1}{2} \mathbf{w}^T \mathbf{w}$$
  
Subject to  $y_i(\mathbf{w}: \mathbf{x}_i + b) \ge 1$ 

One constraint for each training point.

Note sign trick.

C. Burges, A Tutorial on Support Vector Machines for Pattern Recognition, Data Mining and Knowledge Discovery,

## Finding the maximum margin line

• Solution:  $\mathbf{w} = \sum_{i} \alpha_{i} y_{i} \mathbf{x}_{i}$ 

weight

vector

### Finding the maximum margin line

• Solution:  $\begin{aligned} \mathbf{w} &= \sum_i \alpha_i y_i \mathbf{x}_i \\ b &= y_i - \mathbf{w} \cdot \mathbf{x}_i \end{aligned}$  (for any support vector)

$$\mathbf{w} \cdot \mathbf{x} + b = \sum_{i} \alpha_{i} y_{i} \mathbf{x}_{i} \cdot \mathbf{x} + b$$

Classification function:

$$f(x) = \operatorname{sign}(\mathbf{w} \cdot \mathbf{x} + \mathbf{b})$$

$$= \operatorname{sign}(\sum_{i} \alpha_{i} \mathbf{x}_{i} \cdot \mathbf{x} + \mathbf{b})$$
If  $f(x) < 0$ , classify as negative, if  $f(x) > 0$ , classify as positive

- Notice that it relies on an *inner product* between the test point  ${\bf x}$  and the support vectors  ${\bf x}_i$
- (Solving the optimization problem also involves computing the inner products x<sub>i</sub> · x<sub>j</sub> between all pairs of training points)

Burges, A Tutorial on Support Vector Machines for Pattern Recognition, Data Mining and Knowledge Discovery, 1

# How is the SVM objective different from the boosting objective?

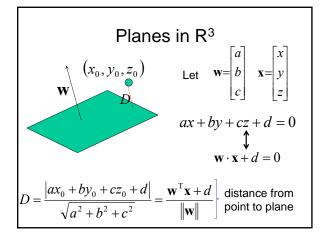


### Questions

- What if the features are not 2d?
- What if the data is not linearly separable?
- What if we have more than just two categories?

### Questions

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  - Generalizes to d-dimensions replace line with "hyperplane"
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# Hyperplanes in R<sup>n</sup>

Hyperplane H is set of all vectors  $\mathbf{X} \in \mathbb{R}^n$  which satisfy:

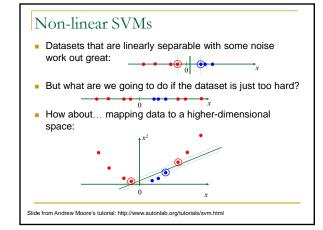
$$w_1 x_1 + w_2 x_2 + \ldots + w_n x_n + b = 0$$

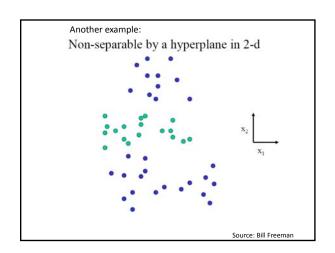
$$\mathbf{w}^{\mathsf{T}} \mathbf{x} + b = 0$$

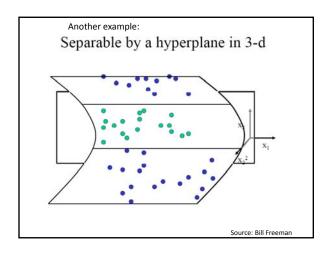
$$D(H,\mathbf{x}) = \frac{\mathbf{w}^{\mathsf{T}}\mathbf{x} + b}{\|\mathbf{w}\|} \quad \begin{array}{l} \text{distance from} \\ \text{point to} \\ \text{hyperplane} \end{array}$$

### Questions

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# Non-linear SVMs: Feature spaces ■ General idea: the original input space can be mapped to some higher-dimensional feature space where the training set is separable: Φ: x → φ(x) Slide from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/svm.html

### Nonlinear SVMs

• The kernel trick: instead of explicitly computing the lifting transformation  $\varphi(\mathbf{x})$ , define a kernel function K such that

$$K(\mathbf{x}_i, \mathbf{x}_i) = \boldsymbol{\varphi}(\mathbf{x}_i) \cdot \boldsymbol{\varphi}(\mathbf{x}_i)$$

• This gives a nonlinear decision boundary in the original feature space:

$$\sum_{i} \alpha_{i} y_{i} K(\mathbf{x}_{i}, \mathbf{x}) + b$$

C. Burges, <u>A Tutorial on Support Vector Machines for Pattern Recognition</u>, Data Mining and Knowledge Discovery, 1998

# Examples of General Purpose Kernel Functions

- Linear:  $K(\mathbf{x}_i, \mathbf{x}_i) = \mathbf{x}_i^\mathsf{T} \mathbf{x}_i$
- Polynomial of power p:  $K(\mathbf{x}_i, \mathbf{x}_i) = (1 + \mathbf{x}_i^T \mathbf{x}_i)^p$
- Gaussian (radial-basis function network):

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\frac{\|\mathbf{x}_i - \mathbf{x}_j\|^2}{2\sigma^2})$$

Slide from Andrew Moore's tutorial: http://www.autonlab.org/tutorials/svm.html

### Questions

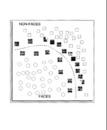
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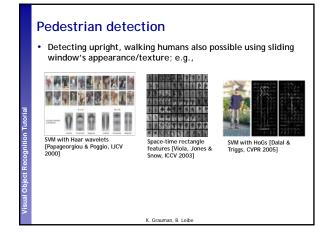
### Multi-class SVMs

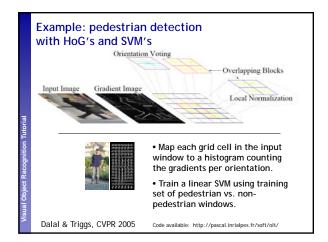
- Achieve multi-class classifier by combining a number of binary classifiers
- One vs. all
  - Training: learn an SVM for each class vs. the rest
  - Testing: apply each SVM to test example and assign to it the class of the SVM that returns the highest decision value
- One vs. one
  - Training: learn an SVM for each pair of classes
  - Testing: each learned SVM "votes" for a class to assign to the test example

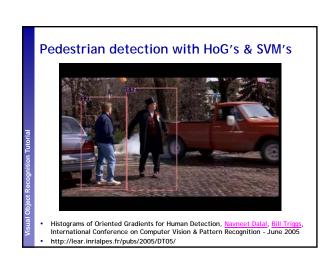
# SVMs for recognition

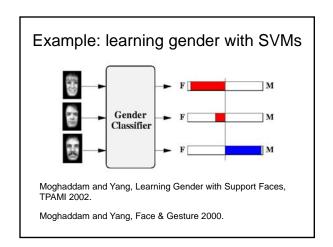
- 1. Define your representation for each example.
- 2. Select a kernel function.
- 3. Compute pairwise kernel values between labeled examples
- Given this "kernel matrix" to SVM optimization software to identify support vectors & weights.
- To classify a new example: compute kernel values between new input and support vectors, apply weights, check sign of output.

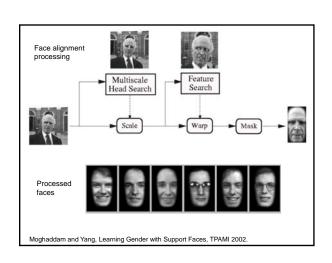








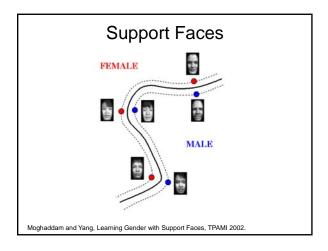




# Learning gender with SVMs

- Training examples:
  - 1044 males
  - -713 females
- Experiment with various kernels, select Gaussian RBF

$$K(\mathbf{x}_i, \mathbf{x}_j) = \exp(-\frac{\left\|\mathbf{x}_i - \mathbf{x}_j\right\|^2}{2\sigma^2})$$



# Classifier Performance

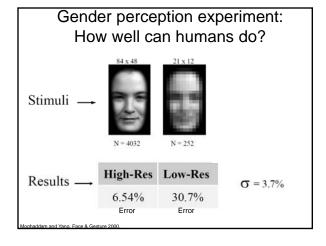
Classifier	Error Rate		
	Overall	Male	Female
SVM with RBF kernel	3.38%	2.05%	4.79%
SVM with cubic polynomial kernel	4.88%	4.21%	5.59%
Large Ensemble of RBF	5.54%	4.59%	6.55%
Classical RBF	7.79%	6.89%	8.75%
Quadratic classifier	10.63%	9.44%	11.88%
Fisher linear discriminant	13.03%	12.31%	13.78%
Nearest neighbor	27.16%	26.53%	28.04%
Linear classifier	58.95%	58.47%	59.45%

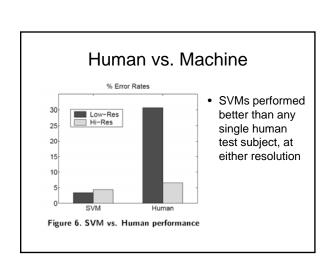
Moghaddam and Yang, Learning Gender with Support Faces, TPAMI 2002.

# Gender perception experiment: How well can humans do?

- Subjects:
  - 30 people (22 male, 8 female)
  - Ages mid-20's to mid-40's
- · Test data:
  - 254 face images (6 males, 4 females)
  - Low res and high res versions
- Task:
  - Classify as male or female, forced choice
  - No time limit

Moghaddam and Yang, Face & Gesture 2000





# Hardest examples for humans



Top five human misclassifications

Moghaddam and Yang, Face & Gesture 2000.

## SVMs: Pros and cons

### Pros

- Many publicly available SVM packages: http://www.kernel-machines.org/software
- http://www.csie.ntu.edu.tw/~cjlin/libsvm/
- Kernel-based framework is very powerful, flexible
- Often a sparse set of support vectors compact at test time
- Work very well in practice, even with very small training sample sizes

### • Cons

- No "direct" multi-class SVM, must combine two-class SVMs
- Can be tricky to select best kernel function for a problem
- · Computation, memory
  - During training time, must compute matrix of kernel values for every pair of examples
  - Learning can take a very long time for large-scale problems

. . . . . . . . .

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