Efficient Predictive Analysis for Detecting Nondeterminism in Multi-Threaded Programs

Arnab Sinha, Sharad Malik

Princeton University

{sinha,sharad}@princeton.edu

Aarti Gupta

NEC Laboratories America

agupta@nec-labs.com

Abstract—Determinism is often a desired property in multithreaded programs. A multi-threaded program is said to be deterministic if for a given input, different thread interleavings result in the same system state in the execution of the program. This, in turn, requires that different interleavings preserve the values read by each read operation. A related, but less strict condition is for the program to be race-free. A deterministic program is race-free but the converse may not be true. There is much work done in the static analysis of programs to detect races and nondeterminism. However, this can be expensive and may not complete for large programs in reasonable time. In contrast to static analysis, predictive analysis techniques take a given program trace and explore other possible interleavings that may violate a given property - in this case the property of interest is determinism. Predictive analysis can be sound, but is not complete as it is limited to a specific set of program runs. Nonetheless, it is of interest as it offers greater scalability than static analysis. This work presents a predictive analysis method for detecting nondeterminism in multi-threaded programs. Potential cases of nondeterminism are checked by constructing a causality graph from the thread events and confirming that it is acyclic. On average, the number of graphs analyzed per benchamrk is one per potential case of nondeterminism, thereby ensuring that it is efficient. We demonstrate its application on some benchmark Java and C/C++ programs.

I. Introduction

Writing correct and efficient multi-threaded programs is widely accepted as a challenging task. The wide range of possible concurrency errors makes it inherently harder than writing sequential programs [15], [26], [28]. Given the same input, the different runs of a multi-threaded program may produce different outputs because the threads interleave in different ways. This makes it hard to replicate and debug errors through traditional testing methods. These errors are referred to as "Heisenbugs" [2]. The potential nondeterminism of multi-threaded programs lies at the core of these Heisenbugs. For this and other reasons, determinism is often a desired property in multi-threaded programs. A multi-threaded program is said to be deterministic if for a given input, different thread interleavings result in the same system state in the execution of the program. It is important to consider when the system state is observed. If it is observed only at the end of the program execution, then individual read events may not need to read the same value across different interleavings. However, if the system state is

continuously observed, then each read event must read the same value in all possible interleavings. We consider this case. Further, for ease of analysis we consider the stricter condition that each read event reads the value from the *same* write event in all interleavings. This restriction is consistent with other work in predictive analysis [8], [34], and can be supplemented with program analysis to consider specific values rather than specific events, if desired.

A related but less strict condition is a *datarace*. A pair of shared memory accesses are said to be *conflicting* if they are performed by different threads and at least one of them is a write. Also, the events are *unsynchronized* if the threads do not use an explicit mechanism such as locks to prevent the accesses from being simultaneous. A datarace is defined as two conflicting and unsynchronized data accesses. A *deterministic program is race-free but the converse may not be true*. The following example in Fig. 1 illustrates this further.

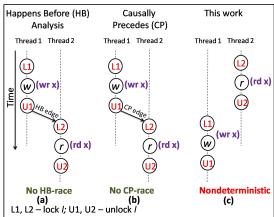


Figure 1. A deterministic program is race-free but the converse may not be true. ('Causally precedes' is defined in [35].)

Consider the example in Fig. 1. In this example, there is a pair of conflicting shared memory accesses, each under the lock-scope of the same lock variable l. Let events L1 and L2 be 'acquire lock' events on l. Similarly, let events U1 and U2 represent 'release lock' events on l. In (a), we show a standard Happens Before (HB) analysis for lock operations. The two events U1 and L2 are ordered by HB, as indicated by the (U1, L2) edge and hence there is no race. Next, in (b), we consider the causally precedes (CP) analysis

proposed by Smaragdakis et al. [35]. Due to the presence of conflicting accesses (w and r) within the lock-scopes, U1 causally precedes L2 introducing the CP edge from U1 to L2. Hence, there is no CP-race. However, observe that in another interleaving (c), where the lock-scopes swap order, the following different order is possible in an interleaving: U2 happens before L1. Thus, while the program is race free, it is nondeterministic because the read event (rd x) reads from a different write event in the interleaving (c) compared to the interleaving in (a) and (b).

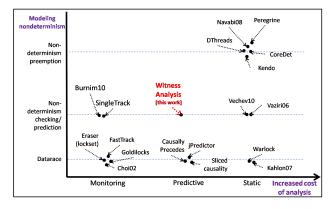


Figure 2. Classification of race and nondeterminism detection techniques based on cost of analysis: Burnim10 [6], SingleTrack [32], Eraser [33], Fast-Track [13], GoldiLocks [11], Sliced Causality [7], jPredictor [8], Causally precedes [35], CoreDet [3], Kendo [29], DThreads [25], Navabi08 [27], Peregrine [10], Vaziri06 [37], Warlock [36], Kahlon07 [20], Choi02 [9], Vechev10 [38]

There is much work done in *static analysis* of programs to detect races and nondeterminism [36], [20], [9], [3], [29], [25], [27], [10], [37] as shown in Fig. 2. Among these, *deterministic multi-threading* (DMT) has attracted a lot of interest recently [25], [10]. DMT deterministically schedules the threads such that the values read by the read operations are preserved. The static analyses for detection or finding schedules can be expensive and may not complete for large programs within reasonable time.

The other end of the spectrum is *monitoring*-based solutions [33], [13], [11]. Although monitoring-based solutions are scalable and sound, the analysis is based only on the runs that are actually executed. In contrast, *predictive analysis* techniques take a given program trace and explore other possible interleavings that may violate a given property [35], [8], [7]. This helps to enhance coverage of a given test input to a larger set of thread interleavings. Predictive analysis can be sound but it is not complete as it may not cover the entire program.

In this work, we adopt a predictive analysis technique for detecting nondeterminism. This provides an effective trade-off between cost and coverage. Our technique is based on the partial order permitted by a trace combined with the reasoning for locks. This technique is fast because it searches a reduced set of sufficient interleavings. Potential cases of non-determinism are checked by constructing a causality graph from the thread events and confirming that this is acyclic. We demonstrate its application on some benchmark Java and C++ programs. Our results show that the average number of graphs analyzed per benchmark is one per potential case of nondeterminism.

This work makes the following contributions:

- It presents a sound and complete¹ predictive analysis technique for checking determinism of multi-threaded programs. It reports only feasible cases of nondeterminism and thus avoids false positives that would require additional test execution after the analysis.
- The proposed technique requires search over a reduced set of sufficient interleavings and hence is fast.
- The technique has been implemented and experimental results on C/C++ and Java benchmark programs are very promising.

II. PRELIMINARIES

We consider a multi-threaded program consisting of a set of threads T_1, T_2, \dots, T_k and a set of shared variables.

Let $\{1, \ldots, k\}$ be the set of thread indices. The remaining aspects of the program, including the control flow and the expression syntax, are intentionally left unspecified for generality.

Program Trace Model: An execution trace $\rho = e_1$, $e_2, \dots e_n$ is a sequence of events, e_i , $i \in \{1, \dots, n\}$, each of which is an instance of a *visible* operation during the execution of the program. The visible operations are: read/write accesses to shared variables and synchronization operations such as wait, notify, notifyall, lock acquire/release and thread fork/join. An event is repre-

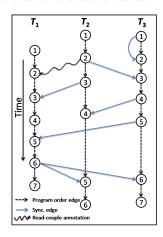


Figure 3. The partial order graph with vertices representing events and the dashed and solid edges are program order and sync. edges respectively. The read-couple annotations are indicated by the squiggly arrows.

sented as a 5-tuple (tid, eid, type, var, child), where tid is the thread index $(tid \in \{1, \ldots, k\})$, eid is the event index (that starts from 1, and increases sequentially within a thread), type is the event type, var is either a shared variable (in read/write operations) or a synchronization object, child is the child thread index (in thread create/join). The event type is one of $\{read, write, fork, join, acquire, release, wait, notify, notifyall\}.$

An execution trace ρ is the observed interleaving of events across the threads and provides a total order on these events. We derive the required partial order for this trace by

¹ over all interleavings of events in the given trace, not over the entire program

retaining only the set of must-happen-before constraints as described below.

Partial Order Graph: Let G(V,E) be a partial order graph such that V(G) is the set of vertices, each of which represents an event in the trace (we use vertices and events interchangeably when the context is clear). Fig. 3 is an example partial order graph with three threads. The number inside each vertex is the eid within the thread. A directed edge (a,b) in E(G) (the set of edges) is either a program order edge, or a synchronization (sync.) edge. Program order edges are indicated by dotted arrows and sync. edges by solid arrows in Fig. 3. An edge in E(G) is referred to as a partial order edge.

We note that locks are not added as sync. edges in E(G). The mutual exclusion due to locks is considered separately by our analysis. We also give special consideration to write-read pairings. If event b reads the value written by event a, then the pair (a,b) is defined as a read-couple. A read-couple is indicated by a squiggly arrow annotation in the partial order graph G. Note that this is not included in the edge set E(G). In a different interleaving τ , if b reads from a different event c, we say that the read-couple for b, and the read b in ρ is broken in τ .

Locked Scope: A locked scope, denoted as $[e_i \dots e_j]_l$, is defined as the sequence of events $e_i \dots e_j$ after an 'acquire lock l' event and before a 'release lock l' event, where l is a lock-variable. Note that the sequence of events $e_i \dots e_j$ and lock acquire/release events belong to the same thread.

III. PREDICTIVE ANALYSIS OF NONDETERMINISM

We assume that the shared variables are implicitly written (or initialized) at the beginning of the execution. Similarly, they are all implicitly read at the end of the program execution. Given the same inputs, if a read instruction of a shared variable reads the value from the same write operation in all interleavings, it is referred to as a *view-preserving* read. Otherwise, the read is *non-view-preserving*. This is related to the well-known notion of view equivalence in database transactions [30].

Definition 1: [Program Nondeterminism] We define a multi-threaded program to be nondeterministic iff there exists at least one non-view-preserving read.

Writer, Readers and Challengers: In the given trace, there can be several read operations reading the value written by a single write operation, w. w is referred to as the writer. Any read event that reads the value written by w is denoted as reader of w. Let R(w) be the set of readers of w. Any write operation c, other than w that writes the same shared variable is denoted as a challenger of w. It is named so since it challenges the set of read-couples induced by w (i.e.

 $\{(w,r) \text{ where, } r \in R(w)\}$) as in an alternate interleaving r may read from c instead of w, thus breaking the read couple (w,r). Let, C(w) be the set of all challengers of writer w.

Problem Formulation: We aim to detect nondeterminism over alternate interleavings of events of a given trace ρ . Thus, we address the following problem: given a trace ρ and a read-couple (w, r) in ρ , is there a challenger c such that it breaks (w, r) in another interleaving τ ?

For a pair of events e_1 and e_2 and an interleaving, let $e_1 \mapsto e_2$ represent " e_1 precedes e_2 in the interleaving". For a given triplet (w,r,c) and a partial order graph G, where $r \in R(w)$ and $c \in C(w)$, the read-couple is broken in an interleaving τ , when any of the following orders is present in τ : (1) $c \mapsto r \mapsto w$, or (2) $w \mapsto c \mapsto r$, or (3) $c \mapsto r$ and w does not occur in τ . In each case, r does not read from w in τ . We refer to these orders as witnesses of nondeterminism and the interleaving containing a witness as a witness interleaving. In cases (1) and (2), w, r and c are the events of the witness and in case (3), c and r are the events of the witness. A triplet is said to be nondeterministic if it can provide a witness of nondeterminism.

Central Idea: There are two phases in our analysis for each witness. For a certain witness ω to exist in an interleaving τ , τ must satisfy the orderings between the members of ω in addition to the HB constraints imposed by program-order, synchronization and possibly between locked scopes. Let $G'(\omega)$ be the graph after incorporating all the mentioned constraints to G in the form of ordering edges but not including any consideration of locked scopes. $G'(\omega)$ cannot contain a cycle since τ must be a total order of events satisfying the ordering constraints imposed by $G'(\omega)$. Thus, in the first phase of our analysis, we check for a cycle in $G'(\omega)$. Presence of cycle in $G'(\omega)$ entails the witness to be infeasible (necessary condition for feasibility of witness). (This phase is similar to a Universal Causality Graph (UCG)-based analysis [23]. We provide a detailed comparison later.) However, absence of a cycle in $G'(\omega)$ does not guarantee feasibility of witness. This is because we still need to consider the locked scopes. For each pair of mutually exclusive locked scopes LS_1 and LS_2 , either LS_1 HB LS_2 or LS_2 HB LS_1 . Since this holds for each pair of mutually exclusive locked scopes, we need to consider all possible combinations of such HB constraints. For d such pairs, there will be 2^d combinations. These choices need to be explored by augmenting G' with each of these 2^d combinations of HB constraints. In the second phase of our analysis, we construct all such possible graphs obtained by augmenting $G'(\omega)$. Let $G''(\omega)$ be one such graph. The witness is infeasible if and only if all 2^d $G''(\omega)$ graphs contain cycles (sufficient condition for feasibility of witness). We now describe these two phases in detail below.

 $^{^2}$ HB edges between fork event in parent thread and first event in child thread, between wait and notify events, and between last event in child thread and join event in parent thread are sync. edges.

A. Necessary Condition for Witness: Witness Order Graph

Let ω be a witness in an interleaving τ . We consider ordering constraints imposed by ω on τ . Note that G already contains program order and synchronization constraints that τ must obey. We now augment G to $G'(\omega)$ to include additional ordering constraints imposed by the witness ω . $G'(\omega)$ is referred to as the witness order graph. The orders imposed by ω are reflected by adding additional edges to $G'(\omega)$ denoted as witness order edges.

We construct $G'(\omega)$ specific to witness ω as follows. (Henceforth, we refer to $G'(\omega)$ as G' when ω is clear from the context.) Without loss of generality consider ω to be of the type $c\mapsto r\mapsto w$. We add witness order edges (c,r) and (r,w) to G'.

For each observed read-couple (a, b) in ρ besides (w, r) in ω , we add a read-couple edge (a,b) to E(G'). In addition, the *induced edges* [23] are added to E(G') as described below. For a pair of locked scopes guarded by same lockvariable $([u, \ldots, v]_l)$ and $[x, \ldots, y]_l$, say), we add an induced edge (v, x) if there is path from u to y in G'^3 . However, if neither v precedes x and nor y precedes u in G' i.e. the locked-scopes are unordered, then the locked-scopes are said to have a *choice* between edges (v, x) and (y, u) in terms of the HB relation between them. This choice will be dealt with later. Fig. 4(a) shows a multi-threaded program trace where x and y are shared variables. The variable x is being written by events c and w in thread T_1 and read by event rin thread T_2 respectively. Event e_2 in thread T_1 assigns the address of x to variable y. Next, in thread T_2 , the value of yis read in a local variable b. The events e_5 , r and e_6 execute in thread T_2 , if b is non-null. The partial order graph G in Fig. 4(b) corresponds to the multi-threaded program trace in Fig. 4(a). Further, Fig. 4(c) shows the witness order graph for the same program trace and witness $c \mapsto r \mapsto w$. The edge (e_3, e_5) is induced by (e_2, e_4) and the presence of locked scopes $[e_1, \ldots, e_3]_l$ and $[e_5, \ldots, e_6]_l$. Note that insertion of one induced edge can trigger insertion of another induced edge if the locked-scopes are nested or overlapping.

G' now contains the following four kinds of ordering constraints due to G (program order edges + sync. edges), witness order edges (including locked scope analysis), read-couple edges except (w,r), and the induced edges due to mutual exclusion of locked scopes. Locked scope analysis enforces the mutual exclusion constraint. However, when combined with the ordering enforced by a specific witness, the mutual exclusion constraint can lead to an ordering constraint which can be added to the partial order ordering constraints [23].

In Fig. 4(c), G' has a cycle $(r \to w \to e_1 \to e_2 \to e_4 \to e_5 \to r)$. Since this cycle represents orderings corresponding to the edges in G', at least one of these orders is not possible.

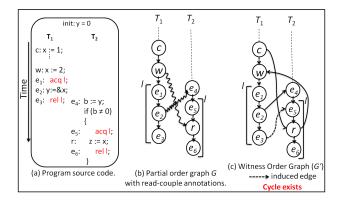


Figure 4. The partial order graph G and the witness order graph $G'(\omega)$, where ω is $(c \mapsto r \mapsto w)$ for the example program source code in (a).

Specifically, in this case, the (e_2, e_4) read-couple will be broken in τ . Therefore, the read for e_4 in τ may result in a different value from the read in the original trace ρ . This may alter the program flow so that the event r may not even happen in τ . In this case the witness is said to be infeasible as τ may not contain r.

Let (w',r') be a read-couple in ρ that is broken in τ . Let x be an event in witness ω . The witness ω is *infeasible* if there is a path from r' to x in G. Intuitively, for ω to be feasible, all the views must be preserved until the events in ω in the interleaving τ . If (w',r') is broken in τ then r' is not view preserving. Otherwise ω is deemed infeasible in G'. The following theorem provides the necessary condition for feasibility.

Theorem 1: [WITNESS ORDER GRAPH THEOREM] A witness is infeasible if there is a cycle in G'.

A proof sketch is provided in the appendix. The reverse direction (infeasibility⇒cycle) is not true. This has to do with the ordering choice between unordered locked scopes and is considered next.

Consider a pair of locked scopes $[a_1,\ldots,b_1]_l$ and $[a_2,\ldots,b_2]_l$ in different threads guarded by the same lock variable l, such that there does not exist a path from a_1 to b_2 or from a_2 to b_1 in G'. In this case the locked scopes are defined to be an *unordered* pair of locked scopes. Moreover due to the mutual exclusion between the two locked scopes one must be ordered before the other. Thus, there exists a *choice* between edges (b_1,a_2) and (b_2,a_1) . The edges (b_1,a_2) and (b_2,a_1) are defined as *choice edges* and the pair $\{(b_1,a_2),(b_2,a_1)\}$ is a *choice edge pair*.

Consider G' shown in Fig. 5. Let there be a witness order edge from y to x (not shown in Fig. 5 for clarity). Let $[a_1,\ldots,b_1]_{l_1}$ and $[a_2,\ldots,b_2]_{l_1}$ be an unordered pair of locked scopes guarded by variable l_1 . Similarly, let $[a_3,\ldots,b_3]_{l_2}$ and $[a_4,\ldots,b_4]_{l_2}$ be an unordered pair of locked scopes guarded by variable l_2 . Let e_1 and e_2 be choice edges $e_1 \in \{(b_1,a_2),(b_2,a_1)\}$ and $e_2 \in \{(b_3,a_4),(b_4,a_3)\}$. Let the edges shown in Fig. 5 represent paths in G'. For finding a feasible witness, we need

³Presence of a path from u to y in G' implies that $[u, \ldots, v]_l$ must be entirely executed before starting the execution of $[x, \ldots, y]_l$.

at least one combination of choice edges e_1 and e_2 such that their addition to G' leads to no cycle. In this example, every combination of e_1 and e_2 results in a path from x to y. This combined with the witness order edge (y,x) leads to a cycle for each combination. In general, if there are d choice edge pairs then we need to check 2^d combinations in conjunction with G'. The number of combinations that actually need to be considered can be reduced as shown in the next subsection.

We would like to point out that this example also illustrates that UCG analysis [23] is incomplete in general, since it does not consider choice edges that may result in cycles with more than two threads.

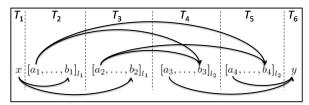


Figure 5. All combinations of choice edges e_1 and e_2 give a path from x to y, where $e_1 \in \{(b_1,a_2),(b_2,a_1)\}$ and $e_2 \in \{(b_3,a_4),(b_4,a_3)\}$

B. Sufficient Condition for Witness: Choice Graph

We first define a lock abstraction graph denoted as $G_a''(\omega)$. (Henceforth, we refer to the lock abstraction graph as $G_a''(\omega)$ when ω is clear from the context.) All vertices within a locked scope in G' are replaced by a single meta-vertex in G_a'' . Any edge originating from or terminating into the locked scope, originates from or terminates into the meta-vertex, respectively. Further, for each unordered pair of locked scopes present in G', an undirected edge connects the corresponding meta-vertices in G_a'' and is referred to as the abstract choice edge. The abstract choice graph for the example shown in Fig. 5 is shown in Fig. 6(a). The vertices m_1, \ldots, m_4 are the meta-vertices and the undirected edges (m_1, m_2) and (m_3, m_4) represent the abstract choice edges in G_a'' .

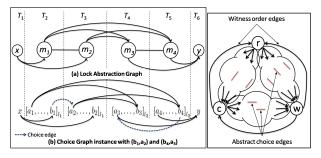


Figure 6. (a) Lock abstraction graph for the example shown in Fig 5. (b) One of the choice graphs with choice edges (b_1, a_2) and (b_4, a_3) .

Figure 7. The undirected edges shown in $G''_a(\omega)$ are the abstract choice edges that constitute S_{choice} for witness $w \mapsto c \mapsto r$

We compute S_{choice} as the set of choice edge pairs such that their exploration is sufficient to detect feasibility of ω .

We construct S_{choice} by collecting all the abstract choice edges present in all paths from x to y in G''_a , for all x and y, where (y,x) is a witness order edge in G'. Fig. 7 illustrates this for a witness $w\mapsto c\mapsto r$. Let $|S_{choice}|=d'$. Usually (d'<< d). This reduction can be viewed as a form of witness-based slicing of G''_a .

Next, we define the choice graph $G''(\omega)$ as follows. (Henceforth, we refer to the choice graph as G'' when ω is clear from the context.) The vertex set V(G'') = V(G'). The edge set E(G'') is E(G') augmented with exactly one choice edge per choice edge pair in S_{choice} . Formally,

$$E(G'') = E(G') \cup \left(\bigcup_{\substack{\forall \{e_{c1}, e_{c2}\} \in S_{choice}, \\ e_c \in \{e_{c1}, e_{c2}\}}} \{e_c\} \right)$$

For instance, in the example shown in Fig 5, there are two choice edge pairs that belong to S_{choice} : $\{(b_1, a_2), (b_2, a_1)\}$ and $\{(b_3, a_4), (b_4, a_3)\}$. Each choice graph must choose exactly one edge from each pair. As there are 2^2 combinations possible, there exist four choice graphs for this example. Fig. 6(b) shows one of those choice graphs with a choice edge combination (b_1, a_2) and (b_4, a_3) .

Theorem 2: [CHOICE GRAPH THEOREM] A witness is infeasible iff all the choice graphs have cycles.

A proof-sketch is provided in the appendix.

C. The Nondeterminism Checking Algorithm

We now summarize the overall algorithm. We first compute the set of possible witnesses, based on challengers for each read event in a trace. For each such witness ω , in the first phase of our analysis, we construct the witness order graph $(G'(\omega))$ and check for a cycle. The witness is infeasible if there is a cycle in $G'(\omega)$. However, if there is no cycle we proceed to the second phase of our analysis. We compute the set S_{choice} . If S_{choice} is empty, the witness is feasible. Otherwise, we construct $2^{d'}$ choice graphs, where $|S_{choice}| = d'$, and check for a cycle until we find a choice graph with no cycle. If an acyclic choice graph exists, the witness is declared feasible. If all choice graphs contain cycles, then the witness is declared infeasible. In practice, we need to explore only a handful (mostly one) of these choice graphs to find one without a cycle.

The complete algorithm is shown in Fig. 8. It generates all feasible witnesses of nondeterminism for a given interleaving ρ . Let, x_i , $i=1\ldots m$ be the shared variables in the observed trace ρ . Further, for each shared variable x_i , let L_{x_i} be the list of read-couples, i.e. $L_{x_i} = \{(w, R(w)) \mid w \text{ writes } x_i\}$.

Optimization: Note that the partial order edges (V(G)) and all the induced edges due to locks and read-couple edges except (w, r) are present in all the choice graphs for a given witness ω . Therefore, we add all the read-couple edges and

Construct partial order graph G from ρ Visit each vertex and if it accesses shared variable x_i a. label vertex with locked scopes. b. populate L_{xi}. if or each L_{xi}, (i = 1 . . . m) for each write w_j in L_{xi} for each read r_k ∈ R(w_j) for each write c_l in L_{xi} such that w_j ≠ c_l Let (w_j, r_k, c_l) be the triplet

8: for each possible witness ω for (w_j, r_k, c_l)
//Witness Order Graph Check
9: Construct G'(ω) and check for cycle in G'(ω).

ReportFeasibleWitnesses (interleaving ρ)

- 10: If cycle found in $G'(\omega)$, report ω is infeasible. 11: Else construct $G''_a(\omega)$ and compute S_{choice} .
- 11: Else construct $G'_a(\omega)$ and compute S_{choice} . 12: Report feasible witness if S_{choice} is empty.
- 13: Construct choice graphs until acyclic graph is found and report ω is feasible.
- 14: If all choice graphs are cyclic, report ω is infeasible.

Figure 8. Algorithm for reporting feasible witnesses

their induced edges to G before line 3 in Fig. 8. Next, for each witness we do the following: (1) delete the read-couple (w,r) and the appropriate induced edges corresponding to the read-couple (w,r), and, (2) insert the witness order edges and the edges induced by them to produce $G'(\omega)$. Moreover, we use vector clocks [24] for keeping track of the causality relationships necessary for incremental addition or removal of an induced edge.

Complexity Analysis: The symbols introduced for complexity analysis are described in Fig. 9. The complexity

of step 1 in procedure **ReportFeasible-Witnesses** is O(M+N)=O(M) as $N\leq M$. The locked scope analysis requires two passes over the trace

Symbol description	Symbol
Number of vertices in G	N
Number of edges in G	M
Number of lock events in G	L
Number of variables	m
Max. number of reads per variable	p
Max. number of writes per variable	q

Figure 9. Symbol table

to label each read/write event with eid's of acquire/release lock events guarding the event. This is O(m(p+q)L). Populating L_{x_i} , for $i = 1 \dots m$ requires one pass over the trace (O(N)). Next we consider the complexity for a single witness. To construct G', we add the read-couple edges (O(mp)) and the witness edges (O(1)). The induced edges order the locked scopes. Therefore, the number of induced edges added is $O(L^2)$. The number of read-couples in G is O(mp). Thus, $|E(G')| = O(M + mp + L^2)$. Then cycle checking in G' is $O(M + N + mp + L^2) = O(M + L^2)$ (since $N \leq M$ and $mp \leq N$). The number of witnesses is $O(mpq^2)$. Note that in our implementation, the construction of G' is done between step 2 and step 3 of procedure ReportFeasibleWitnesses for efficiency, with some simple book-keeping which is omitted here for brevity. Since, the number of choice edge pairs (d) is $O(L^2)$, $d' = O(L^2)$. Therefore, the number of choice graphs is $O(2^{L^2})$. Checking a cycle in a choice graph is $O(M + L^2)$. Therefore, the overall complexity: $O(M+m(p+q)L+mp+mpq^2(M+L^2)+$ $2^{L^{2}}(M+L^{2})) = O(mpL + mqL + (mpq^{2} + 2^{L^{2}})(M+L^{2})).$

IV. RESULTS

We have implemented our technique in a prototype tool. This tool is capable of logging/analyzing execution traces generated by both Java programs and multi-threaded C/C++ programs using pthreads. The program traces used are all available online [18]. The C++ benchmark is available online [16]. All the Java benchmarks are publicly available [12], [14], [17], [19], [31]. These traces are manually chosen aiming to have a good mix with respect to graph size and degree of communication between threads.

The tool logs execution traces at runtime from C++ source code instrumented using the commercial front end from Edison Design Group (EDG). For Java programs, we used execution traces logged at runtime by a modified Java Virtual Machine (JVM). For each test case, we first executed the program using the default OS thread scheduling and logged the execution trace. Next we applied our algorithm to detect the feasible witnesses. The graphs are stored in explicit-state form to facilitate cycle checking. The number of vertices in partial order graphs ranged between 100-26000 and the number of edges in those graphs ranged between 150-31000. We would like to highlight here that we originally implemented exploration of the combination of choice edges using an SMT solver, but the cost was prohibitive, failing to finish on several benchmarks. This motivated our current purely graph-based approach.

All our experiments were conducted on an Intel i7 machine (2.67 GHz, 3 GB memory) running Ubuntu 2.6.31-14-generic. Detailed experimental results are reported in the appendix (Table A1) and a summary is presented in Table I. We make the following observations.

- In 9 out of 25 traces, Phase I alone was sufficient (row 1 in Table I) for our analysis.
- Around 80% of the witnesses in the majority of the traces are found to be infeasible due to the presence of a cycle in the witness order graph G' (Column 4). Since this is a quick check, most of the witnesses are handled quite expeditiously.
- Among the remaining witnesses, a majority of them do not have choice edges (~17% of the total witnesses) (Column 5). For the traces in row 2, ~3% of the witnesses have choice edges to be explored (Column 6).
- For the witnesses left with choice edges, even when the average number of possible choice graphs per witness is large (Column 7), the number of choice graphs actually explored per witness is close to 1 (Column 8).⁴ This is because the exploration stops as soon as an acyclic choice graph is detected. Thus, overall the average number of graphs explored per witness is very close to 1 also (Column 12).

⁴However, 89 of those witnesses were found to be infeasible, i.e., all choice graphs for these witnesses are cyclic.

1.	2.	3.	Witness Order Graph Analysis			Choice Grap	9.	10.	11.	12.	
			4.	5.	6.	7.	8.	1			Avg. number
Categories	#Benchmarks	#Possible	Witnesses	Witnesses	Witnesses	Possible	Choice	Total	Total	Total	of graphs
		witnesses	with cycles	with no choice	with choice	choice graphs	graphs	time	feasible	infeasible	analyzed
			in G'	edges (feasible)	edges (%)	per witness	explored	taken	witnesses	witnesses	per witness
			(infeasible) (%)	(%)		in column 6	per witness	(sec)	(%)	(%)	in column 3
							in column 6				
Phase I	9	104178	85789	18389	0	-	_	44.3	18389	85789	1
sufficient			(82.35)	(17.65)	(0)				(17.65)	(82.35)	
Both phases	16	5604552	4477107	943516	183929	7.53	1.03	8597	1127356	4477196	1.001
required			(79.88)	(16.84)	(3.28)				(20.11)	(79.88)	

Table I

SUMMARY OF THE EXPERIMENTAL DATA ON THE WITNESSES OF NONDETERMINISM IN TRACES OF MULTI-THREADED PROGRAMS.

• The time required for witness order graph analysis is much lower than that of choice graph analysis.

V. RELATED WORK

We have already discussed the broad categories of efforts in detecting dataraces and nondeterminism in Section I (Figure 2). We highlight specific related aspects below.

Datarace detection: Broadly, the approaches can be classified into three groups - (1) monitoring [33], [11], [13], [9], (2) predictive analysis [7], [8], [35] and (3) static analysis [36], [20], [22]. Like many of these techniques, we too use happens-before analysis and reasoning about locks. However, our focus is on detecting nondeterminism that is related to, but distinct from, datarace detection. Specifically, we do not have to provide witnesses with unsynchronized memory accesses, which may involve subtle reasoning about locks, e.g. by using lock acquisition histories [21] or causally-precedes relationships [35]. Rather, we consider witnesses with all possible orderings of related events (w, w)r, and c), where lock reasoning is used only to ensure mutual exclusion. We use a simple notion of lock scopes to enforce mutual exclusion. Chen et al. [8] used a related notion called lock atomicity sets, but they provide a richer abstraction (lock atomicity equivalence) for their purpose of predicting sound interleavings. UCG-based analysis [23] also used cycle-based infeasibility checks, but their analysis is incomplete for more than two threads where choice edges need to be considered. Our lock abstraction graph can be used to identify choice edge pairs in witness-based slicing for other checkers that may use UCG analysis.

Nondeterminism detection: Ensuring deterministic programs has received a lot of attention lately [5]. Vechev et al. proposed a static analysis for verifying determinism in structured parallel programs, based on checking nonoverlapping memory accesses in parallel sections [38]. There is some work on specification and dynamic checking for determinism also [6], [32]. Burnim et al. proposed an assertion framework for specifying that programs should behave deterministically and used it to detect nondeterministic behavior [6]. Sadowski et al. proposed a new noninterference specification for deterministically-parallel code, and used a dynamic analysis tool called SideTrack to enforce it [32]. Many other efforts focus on adding synchronization or deterministic scheduling to preempt nondeterministic be-

havior or related bugs. Vaziri et al. associate synchronization constraints with fields of a class in object-oriented programs, and use static analysis to automatically infer synchronization points to avoid concurrency-related bugs [37]. Navabi et al. insert lightweight synchronization primitives at potential violation points [27]. DThreads replaces the pthreads library with an efficient deterministic multi-threading system [25]. CoreDet is a compiler and runtime system for general-purpose software deterministic multi-threading [3]. Other such systems are Determinator [1], Kendo [29] and dOS [4]. In contrast to these efforts, our work does not target specifying or enforcing determinism, but only to check it under standard synchronization and scheduling semantics. Any enforcements (using synchronization or deterministic thread scheduling) can be easily accounted for by adapting the partial orders we consider in our analysis. To the best of our knowledge, our work is the first to use predictive analysis for detecting nondeterminism.

VI. CONCLUSION

We have proposed a graph-based predictive analysis method for detecting nondeterminism in multi-threaded programs. We analyze each read-couple with all other writes to the same shared variable and determine the conditions for nondeterminism. When these conditions are satisfied, we generate a witness of nondeterminism. Further, we ensure no false positives by ensuring that our witness is feasible, i.e. there exists an interleaving where this witness will be observed. A key property of our method is that we provide a sound and complete⁵ predictive technique that explores a reduced set of sufficient interleavings, thereby ensuring that it is efficient. Our experimental results demonstrate the effectiveness of our proposed method on several C/C++ and Java benchmark programs.

ACKNOWLEDGMENT

The authors acknowledge the support of the Gigascale Systems Research Center, one of six research centers funded under the Focus Center Research Program (FCRP), a Semiconductor Research Corporation program.

⁵complete for predicting from the given trace, not for the entire program

REFERENCES

- [1] Aviram, A., chun Weng, S., Hu, S., Ford, B.: Efficient System Enforced Deterministic Parallelism. In: OSDI (2010)
- [2] Ball, T., Burckhardt, S., de Halleux, J., Musuvathi, M., Qadeer, S.: Deconstructing Concurrency Heisenbugs. In: ICSE. pp. 403–404. IEEE (2009)
- [3] Bergan, T., Anderson, O., Devietti, J., Ceze, L., Grossman, D.: CoreDet: A Compiler and Runtime System for Deterministic Multi-threaded Execution. In: ASPLOS. pp. 53–64 (2010)
- [4] Bergan, T., Hunt, N., Ceze, L., Gribble, S.D.: Deterministic Process Groups in dOS. In: OSDI. pp. 1–16. OSDI'10 (2010)
- [5] Bocchino, Jr., R.L., Adve, V.S., Adve, S.V., Snir, M.: Parallel Programming Must Be Deterministic By Default. In: HotPar. pp. 4–4. HotPar'09 (2009)
- [6] Burnim, J., Sen, K.: Asserting and Checking Determinism For Multi-threaded Programs. Commun. ACM 53 (Jun 2010)
- [7] Chen, F., Rosu, G.: Parametric and Sliced Causality. In: CAV. pp. 240–253 (2007)
- [8] Chen, F., Serbănută, T., Rosu, G.: jPredictor: A Predictive Runtime Analysis Tool for Java. In: ICSE. pp. 221–230 (2008)
- [9] Choi, J.D., Lee, K., Loginov, A., O'Callahan, R., Sarkar, V., Sridharan, M.: Efficient and Precise Datarace Detection for Multithreaded Object-oriented Programs. In: PLDI. pp. 258– 269. PLDI '02 (2002)
- [10] Cui, H., Wu, J., Gallagher, J., Guo, H., Yang, J.: Efficient Deterministic Multithreading Through Schedule Relaxation. In: SOSP. pp. 337–351. SOSP '11 (2011)
- [11] Elmas, T., Qadeer, S., Tasiran, S.: Goldilocks: A Race-Aware Java Runtime. Commun. ACM 53 (Nov 2010)
- [12] Farchi, E., Nir, Y., Ur, S.: Concurrent Bug Patterns and How to Test Them. In: IPDPS. p. 286 (2003)
- [13] Flanagan, C., Freund, S.N.: FastTrack: Efficient and Precise Dynamic Race Detection. In: PLDI. PLDI '09 (2009)
- [14] Havelund, K.: Using Runtime Analysis to Guide Model Checking of Java Programs. In: SPIN. pp. 245–264 (2000)
- [15] Havender, J.W.: Avoiding deadlock in multitasking systems
- [16] http://incubator.apache.org/thrift/:
- [17] http://research.microsoft.com/qadeer/cav_issta.htm: Joint CAV/ISSTA special event on specification, verification, and testing of concurrent software
- [18] http://www.princeton.edu/ \sim sinha/FMCAD12_Traces.zip:
- [19] http://www2.epcc.ed.ac.uk/computing/research_activities/ java_grande/index_1.html: Java grande forum benchmark suite
- [20] Kahlon, V., Yang, Y., Sankaranarayanan, S., Gupta, A.: Fast and accurate static data-race detection for concurrent programs. In: CAV. pp. 226–239. Springer (2007), LNCS 4590
- [21] Kahlon, V., Ivancic, F., Gupta, A.: Reasoning About Threads Communicating via Locks. In: Computer Aided Verification. pp. 505–518 (2005), LNCS 3576
- [22] Kahlon, V., Sankaranarayanan, S., Gupta, A.: Semantic Reduction of Thread Interleavings in Concurrent Programs. In: TACAS. TACAS '09 (2009)
- [23] Kahlon, V., Wang, C.: Universal Causality Graphs: A Precise Happens-Before Model for Detecting Bugs in Concurrent Programs. In: CAV. pp. 434–449. Springer (2010)
- [24] Lamport, L.: Time, Clocks, and the Ordering of Events in a Distributed System. Commun. ACM 21(7) (1978)

- [25] Liu, T., Curtsinger, C., Berger, E.D.: DThreads: Efficient Deterministic Multithreading. In: SOSP. pp. 327–336. SOSP '11 (2011)
- [26] Mcdowell, C.E., Helmbold, D.P.: Debugging Concurrent Programs. ACM Computing Surveys 21, 593–622 (1989)
- [27] Navabi, A., Zhang, X., Jagannathan, S.: Quasi-Static Scheduling For Safe Futures. In: Chatterjee, S., Scott, M.L. (eds.) PPoPP. pp. 23–32. ACM (2008)
- [28] Netzer, R.H.B., Miller, B.P.: What Are Race Conditions?: Some Issues and Formalizations. ACM Lett. Program. Lang. Syst. 1 (March 1992)
- [29] Olszewski, M., Ansel, J., Amarasinghe, S.: Kendo: Efficient Deterministic Multithreading in Software. SIGPLAN Not. 44, 97–108 (Mar 2009)
- [30] Papadimitriou, C.H.: The Serializability of Concurrent Database Updates. J. ACM 26(4), 631–653 (1979)
- [31] von Praun, C., Gross, T.R.: Static Detection of Atomicity Violations in Object-Oriented Programs. Object Technology 3(6) (2004)
- [32] Sadowski, C., Freund, S.N., Flanagan, C.: SingleTrack: A Dynamic Determinism Checker for Multithreaded Programs. In: ESOP. ESOP '09 (2009)
- [33] Savage, S., Burrows, M., Nelson, G., Sobalvarro, P., Anderson, T.: Eraser: A Dynamic Data Race Detector for Multi-threaded Programs. ACM Trans. Comput. Syst. 15(4), 391–411 (1997)
- [34] Sinha, A., Malik, S., Wang, C., Gupta, A.: Predictive Analysis for Detecting Serializability Errors through Trace Segmentation. In: MEMOCODE (2011)
- [35] Smaragdakis, Y., Evans, J., Sadowski, C., Flanagan, J.Y.C.: Sound Predictive Race Detection in Polynomial Time. In: POPL (2012)
- [36] Sterling, N.: WARLOCK A Static Data Race Analysis Tool. In: USENIX Winter. pp. 97–106 (1993)
- [37] Vaziri, M., Tip, F., Dolby, J.: Associating Synchronization Constraints With Data In An Object-Oriented Language. In: POPL (2006)
- [38] Vechev, M., Yahav, E., Raman, R., Sarkar, V.: Automatic Verification of Determinism For Structured Parallel Programs. In: SAS. SAS'10 (2010)

APPENDIX

A. Detailed Experimental Results

The detailed experimental results for a sample of traces are given in Table A1. For each benchmark, column 1 presents various statistics of the logged program traces: threads (thrds), number of events (evs), number of lock events (l-evs) and lock variables (l-vars), number of read/write events (rw-evs) and shared variables (rw-vars) and number of wait-notify events (wn-evs). Column 2 shows the total number of possible witnesses in the observed trace. Columns 3-5 and 6-7 show the results of analyses based on witness order graphs and choice graphs, respectively. For the witness order graphs, we report the number of infeasible witnesses (i.e. cycle found) (column 3), number of feasible witnesses (no choice edges and no cycle) (column 4) and witnesses left with choice edges (column 5). Similarly, for the choice graphs, we report the number of possible choice graphs per witness in column 5 that have choice edges (column 6) and number of choice graphs

explored per witness in column 5 that have choice edges (column 7). Column 8 shows the total time taken for the analysis. Columns 9 and 10 show the total feasible witnesses and the total infeasible witnesses, respectively. Column 11 reports the average number of graphs analyzed per witness in column 2.

B. PROOF SKETCH OF THEOREM 1

Proof Sketch of Witness Order Graph Theorem:

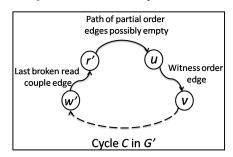


Figure B1. Case 2 of the proof of Theorem 1

Let C be the cycle in G'. The partial order edges/induced edges led by partial order edges and read-couples/induced edges led by read-couples only cannot constitute C^6 (otherwise this contradicts the total order of ρ). Therefore, C must contain a witness order edge.

Case 1: C contains witness order edge and partial order edge/induced edge led by partial order edge only. C does not contain read-couple/induced edge led by read-couple: Let τ be an interleaving that contains ω . Due to C, τ is cyclic. Then there does not exist a valid interleaving τ (since it must be a total order of events) that contains ω . Hence, ω is infeasible.

Case 2: C contains witness order edge, partial order edge/induced edge led by partial order edge and at least one read-couple/induced edge led by read-couple: In interleaving τ , at least one read-couple in C must be broken for τ to be a total order since the witness order edges must be observed for τ to be a witness interleaving. What we now need to show is that such broken read couple can alter program flow so that some event x, where x is an event of ω , may not occur. Thus ω will be infeasible.

Let (w',r') be the last read-couple that is broken in C before a witness order edge or an edge induced by a witness order edge and let (u,v) be such an edge in C after (w',r') (Fig. B1). Note that there cannot be any unbroken read-couple (w'',r'') between (w',r') and (u,v) in C because all such reads after a broken read are not guaranteed to happen.

From the construction of (u, v) we know there are two possible cases.

- 1) The edge (u,v) is an witness order edge: In this case, u is an event in the witness ω . Since the read-couple (w',r') is broken and there are only partial order edges between r' and u, u is not guaranteed to happen in τ , and thus ω is infeasible.
- 2) The edge (u,v) is induced by an witness order edge: In this case, there is a vertex x, where $x \in \omega$ and $[x \dots u]_l$, i.e. x and u are in the same locked scope. Since there is a path through partial order edges from r' to u and (w',r') is broken, u may not occur. If u does not occur, then a) either the entire scope $[x \dots u]_l$ is not executed, in which

 $^{6}\mathrm{either}$ a partial order edge or a read-couple edge leads to an induced edge

case ω is infeasible as x is an event in ω , or b) x occurs, but u does not occur and thus the witness ω cannot continue along (u, v). Thus ω is infeasible. \square

C. PROOF SKETCH OF THEOREM 2

Proof Sketch of Choice Graph Theorem: (\Leftarrow) All choice graphs represent traces that are consistent with the witness order graph $G'(\omega)$. We know that G' does not have a cycle, otherwise it would have been detected before. In a choice graph, all the unordered pairs of locked scopes represented in S_{choice} are ordered. The presence of cycle in a choice graph $G''(\omega)$ implies that the witness ω is infeasible with respect to the particular ordering of locked scopes present in $G''(\omega)$. Similarly, the presence of cycles in all choice graphs implies that the witness is infeasible with respect to all the orderings of locked scopes represented in S_{choice} . Hence, ω is infeasible.

(⇒) It is known that G' is acyclic (otherwise it would have been detected earlier). Therefore, ω is infeasible implies that there does not exist an (acyclic) interleaving τ that is consistent with any of the 2^d combinations of choice edges. Then all those 2^d graphs are cyclic. The cycles in these 2^d graphs can be divided into two categories, (1) cycles that do not contain any choice edge outside S_{choice} , and, (2) cycles that contain at least one choice edge outside S_{choice} . All cycles of the first category are present in $2^{d'}$ choice graphs. We are done if we can prove that (1) there is no cycle in the second category, and, (2) each of the choice graphs contain at least one cycle from the first category.

Subproof 1: We prove by contradiction. Let the witness be infeasible and there exists a cycle C in one of 2^d possible graphs that contains at least one choice edge e_{c1} from a choice edge pair $t = \{e_{c1}, e_{c2}\}$ outside S_{choice} . C must contain at least one witness order edge (y, x) (otherwise ρ is inconsistent). This choice edge e_{c1} in C is on the path between x and y. Therefore, by definition the choice edge pair t must be within S_{choice} leading to contradiction.

Subproof 2: We prove by contradiction. Let the witness ω be infeasible and there exists an acyclic choice graph G''. This implies that the particular combination of d' choice edges present in G'' does not lead to a cycle (since, by subproof 1, we know that there does not exist a cycle in 2^d combinations that contain choice edges from pairs outside S_{choice}). Then there exists an (acyclic) interleaving τ consistent with choice graph G'' containing ω . Then ω is feasible. This leads to the contradiction.

Hence, if the witness is infeasible, then all the choice graphs must have cycles in them. \Box

 $\label{thm:conditional} Table~A1$ Experimental data on the witnesses of nondeterminism in traces of multi-threaded programs.

1.	2.	Witness	Order Graph Ana	lysis	Choice Grap	oh Analysis	8.	9.	10.	11.
Benchmark	#Possible witnesses	3. Witnesses with cycles in G' (infeasible) (%)	4. Witnesses with no choice edges (feasible) (%)	5. Witnesses with choice edges (%) $(\epsilon=\sim0)$	6. Possible choice graphs per witness in column 5	7. Choice graphs explored per witness in column 5	Total time taken	Total feasible witnesses (%)	Total infeasible witnesses (%)	Avg. number of graphs analyzed per witness in column 2
conpool - thrds: 4, evs: 97, l-evs: 16, l-vars: 1, rw-evs: 53, rw-vars: 5, wn-evs: 3	252	221 (88)	31 (12)	0 (0)	_	-	0.007s	31 (12.3)	221 (87.7)	1
liveness - thrds: 7, evs: 283, 1-evs: 44, 1-vars: 9, rw-evs: 163, rw-vars: 12, wn-evs: 6	855	709 (83)	146 (17)	0 (0)	-	-	0.064s	146 (17)	709 (83)	1
SynchBench - thrds: 16, evs: 1510, l-evs: 306, l-vars: 2, rw-evs: 533, rw-vars: 15, wn-evs: 0	47526	39474 (83)	8052 (17)	0 (0)	-	-	8.85s	8052 (17)	39474 (83)	1
Barrier - thrds: 10, evs: 653, l-evs: 108, l-vars: 2, rw-evs: 262, rw-vars: 12, wn-evs: 7	3975	3231 (81)	744 (19)	0 (0)	_	-	0.62s	744 (18.7)	3231 (81.3)	1
account - thrds: 11, evs: 902, 1-evs: 146, 1-vars: 21, rw-evs: 430, rw-vars: 42, wn-evs: 10	1416	1042 (73.6)	326 (23)	48 (3.4)	36.33	2.83	1.352s	374 (26.1)	1058 (73.9)	1.06
DaisyTest - thrds: 3, evs: 2998, 1-evs: 422, 1-vars: 10, rw-evs: 2003, rw-vars: 45, wn-evs: 15	383007	305635 (79.8)	61852 (16.1)	15520 (4.1)	6.35	1.12	244s	77372 (20.2)	305650 (79.8)	1.005
Elevator - thrds: 4, evs: 3004, 1-evs: 370, 1-vars: 11, rw-evs: 1795, rw-vars: 70, wn-evs: 0	3249	2671 (82)	578 (18)	0 (0)	_	ı	0.8s	578 (17.8)	2671 (82.2)	1
philo - thrds: 6, evs: 1141, l-evs: 126, l-vars: 6, rw-evs: 857, rw-vars: 23, wn-evs: 22	4893	4118 (84)	775 (16)	0 (0)	-	ı	0.65s	775 (15.8)	4118 (84.2)	1
ThriftTrace1 - thrds: 4, evs: 2406, 1-evs: 226, 1-vars: 12, rw-evs: 869, rw-vars: 62, wn-evs: 53	618	361 (58)	96 (16)	161 (26)	105.6	1	1.6s	257 (41.6)	361 (58.4)	1
ThriftTrace2 - thrds: 4, evs: 11357, 1-evs: 1384, 1-vars: 48, rw-evs: 3184, rw-vars: 171, wn-evs: 324	35610	29441 (82.7)	5804 (16.3)	365 (1)	296.7	1	28s	6169 (17.3)	29441 (82.7)	1
ThriftTrace3 - thrds: 6, evs: 20640, l-evs: 1724, l-vars: 158, rw-evs: 8818, rw-vars: 519, wn-evs: 349	479142	399814 (83)	79326 (16.5)	2 (6)	18	1	243s	79328 (16.6)	399814 (83.4)	1