Register Allocation

Code generation strategies

- Simple: stack code
 - all variables and user-defined temporaries are allocated on stack
 - use registers as temporaries when evaluating expressions
 x86: and to return values from function calls
- · Better strategy: use registers to reduce loads/stores
 - local variables and user-defined temporaries can be allocated to registers if you have enough registers

 • in our discussion, we will focus on user-defined temporaries

 - also need registers to return values from function calls, to perform some instructions (eg. MUL in x86)
- Approach:
 - generate "abstract" assembly code in which you assume you have an unbounded number of registers
 - perform register allocation
- · Reality is a little more complex but this is the high-level idea

Main idea

- Want to replace temporary variables with some fixed set of registers
- First: need to know which variables are live after each instruction
 - Two simultaneously live variables cannot be allocated to the same register

Register allocation

- For every node n in CFG, we have out[n]
 - Set of temporaries live out of n
- Two variables interfere if
 - both initially live (ie: function args), or
 - both appear in out[n] for any n
- How to assign registers to variables?

Interference graph

- Nodes of the graph = variables
- Edges connect variables that interfere with one another
- Nodes will be assigned a color corresponding to the register assigned to the variable
- Two colors can't be next to one another in the graph

Interference graph

Instructions Live vars b = a + 2 c = b * b b = c + 1 return b * a

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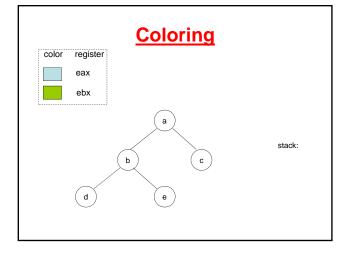
Graph coloring

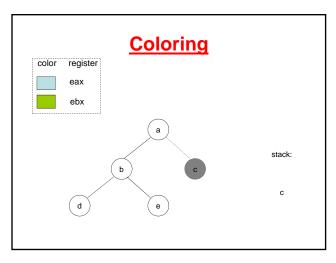
- Questions:
 - Can we efficiently find a coloring of the graph whenever possible?
 - Can we efficiently find an optimal coloring of the graph?
 - How do we choose registers to avoid move instructions?
 - What do we do when there aren't enough colors (registers) to color the graph?

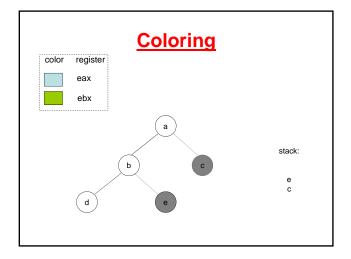
Kempe's heuristic

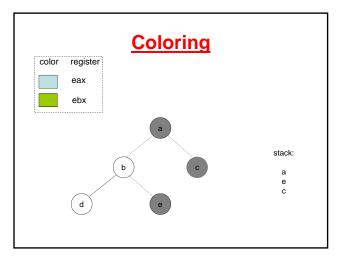
- Kempe's algorithm [1879] for finding a K-coloring of a graph
- Step 1 (simplify):

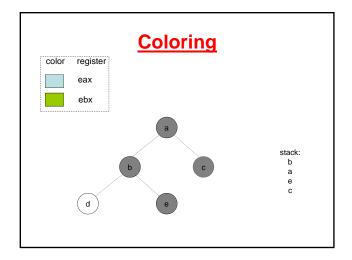
 find a node with at most K-1 edges and cut it out of the graph.
- remember this node on a stack for later stages.
- Intuition: once a coloring is found for the simpler graph, we can always color the node we saved on the stack
- Step 2 (color): when the simplified graph has been colored, add back the node on the top of the stack and assign it a color not taken by one of the adjacent nodes

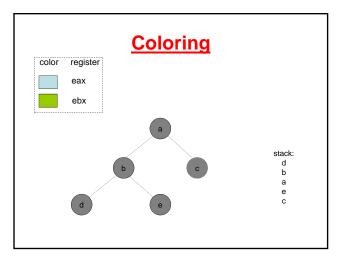


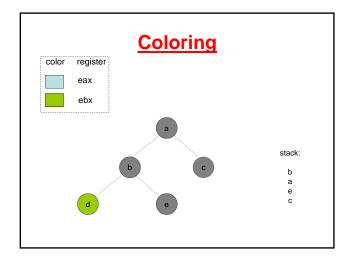


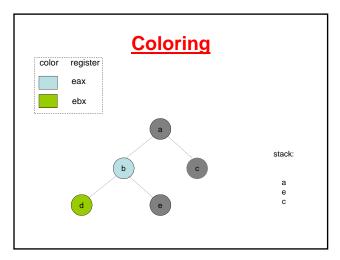


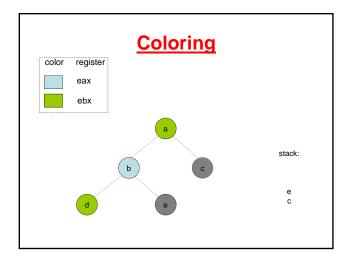


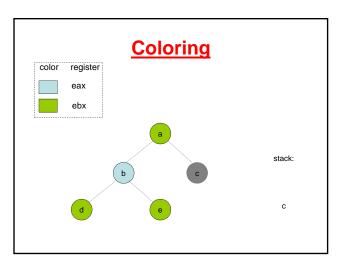


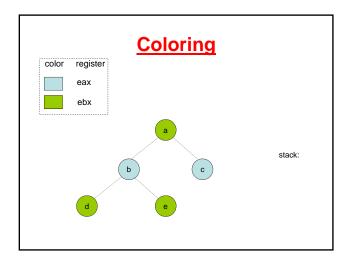






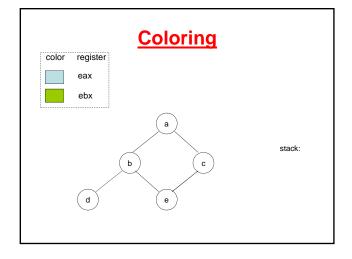


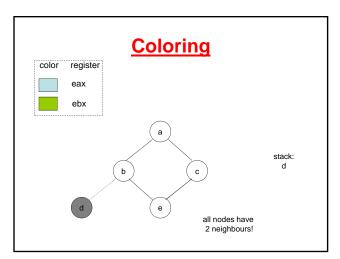


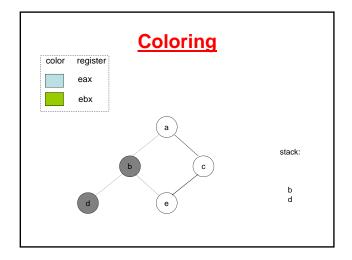


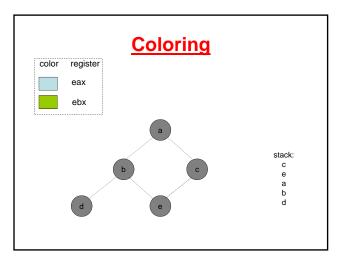
Failure

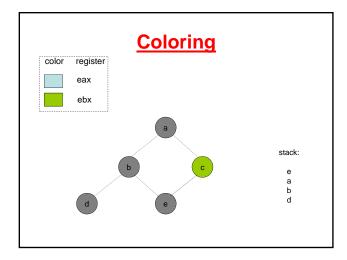
- If the graph cannot be colored, it will eventually be simplified to graph in which every node has at least K neighbors
- Sometimes, the graph is still K-colorable!
- Finding a K-coloring in all situations is an NP-complete problem
 - We will have to approximate to make register allocators fast enough

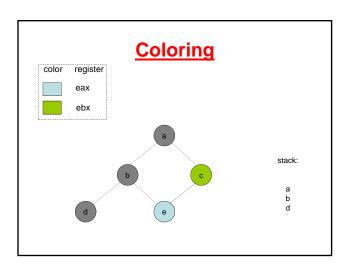


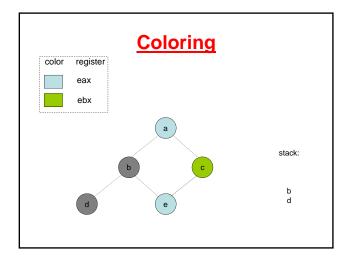


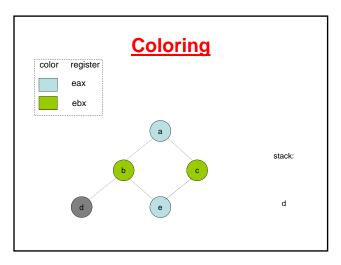


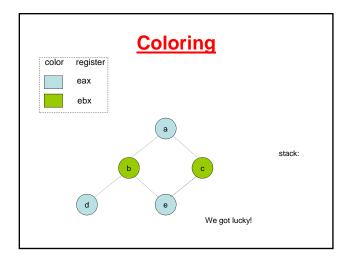


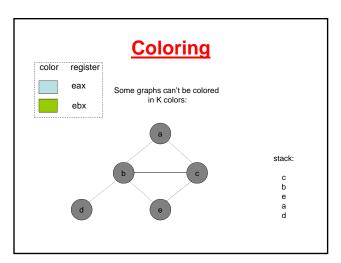


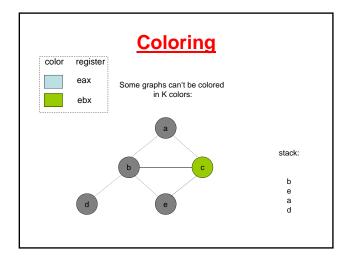


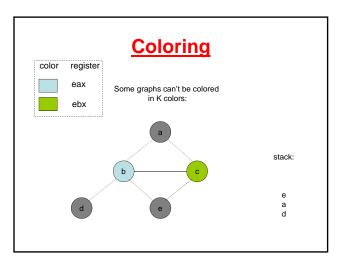


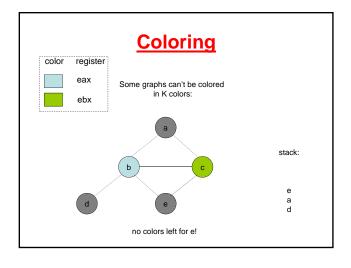












Spilling

- Step 3 (spilling): once all nodes have K or more neighbors, pick a node for spilling
 - Storage on the stack
- There are many heuristics that can be used to pick a node
 - not in an inner loop

Spilling code

- We need to generate extra instructions to load variables from stack and store them
- These instructions use registers themselves. What to do?
 - Stupid approach: always keep extra registers handy for shuffling data in and out
 - Better approach: rewrite code introducing a new temporary; rerun liveness analysis and register allocation
 - Intuition: you were not able to assign a single register to the variable that was spilled but there may be a free register available at each spot where you need to use the value of that variable

Rewriting code

- Consider: add t1 t2
 - Suppose t2 is selected for spilling and assigned to stack location [ebp-24]
 - Invent new temporary t35 for just this instruction and rewrite:
 - mov t35, [ebp 24];
 - add t1, t35
 - Advantage: t35 has a very short live range and is much less likely to interfere.
 - Rerun the algorithm; fewer variables will spill

Precolored Nodes

- Some variables are pre-assigned to registers
 - Eg: mul on x86/pentium
 - uses eax; defines eax, edx
 - Eg: call on x86/pentium
 - Defines (trashes) caller-save registers eax, ecx, edx
- Treat these registers as special temporaries; before beginning, add them to the graph with their colors

Precolored Nodes

- Can't simplify a graph by removing a precolored node
- Precolored nodes are the starting point of the coloring process
- Once simplified down to colored nodes start adding back the other nodes as before

Optimizing Moves

- Code generation produces a lot of extra move instructions
 - mov t1, t2
 - If we can assign t1 and t2 to the same register, we do not have to execute the mov
 - Idea: if t1 and t2 are not connected in the interference graph, we coalesce into a single variable

• Solution 1 (Briggs): avoid creation of high-degree (>= K) nodes • Solution 2 (George): a can be coalesced with b if every neighbour t of a: - already interferes with b, or - has low-degree (< K)

Simplify & Coalesce

- Step 1 (simplify): simplify as much as possible without removing nodes that are the source or destination of a move (move-related nodes)
- Step 2 (coalesce): coalesce move-related nodes provided low-degree node results
- Step 3 (freeze): if neither steps 1 or 2 apply, freeze a move instruction: registers involved are marked not move-related and try step 1 again

