

Action to Dataflow Analysis Anformation computed by live variable analysis and available copies can be expressed as elements of lattices Active variables: If V is the set of all variables in the program and P the power set of V, then: (P, ⊆) is a lattice Active sets of live variables are elements of this lattice

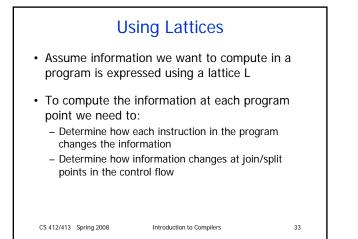
Relation To Dataflow Analysis

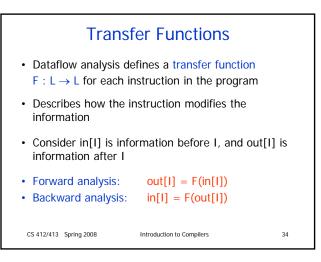
- Copy Propagation:
 - V is the set of all variables in the program
 - V x V the Cartesian product representing all possible copy instructions
 - P the power set of V x V
- Then:
 - (P, \subseteq) is a lattice
 - sets of available copies are lattice elements

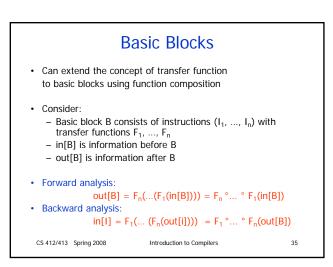
Introduction to Compilers

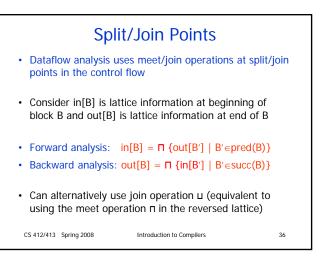
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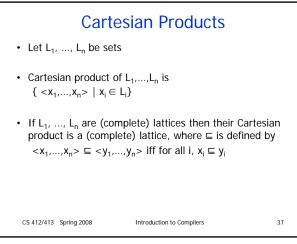
32

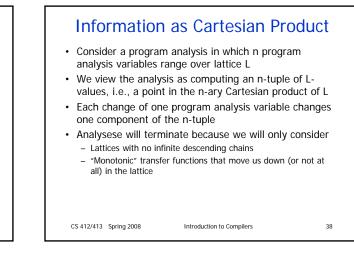












More About Lattices	Proof (1 & 2)
 In a lattice (L, ⊑), the following are equivalent: 1. x ⊑ y 2. x ⊓ y = x 3. x ⊔ y = y 	 Prove that x ⊑ y implies x ⊓ y = x: x is a lower bound of {x,y} All lower bounds of {x,y} are less= than x,y In particular, they are less= than x
 Note: meet and join operations were defined using the partial order relation 	 Prove that x ⊓ y = x implies x ⊑ y : - x is a lower bound of {x,y} - x is less= than x and y - In particular, x is less= than y
CS 412/413 Spring 2008 Introduction to Compilers 39	CS 412/413 Spring 2008 Introduction to Compilers 40

