

CS378
Autonomous Multiagent Systems
Spring 2005

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Week 13b: Thursday, April 21st

Good Afternoon, Colleagues

Are there any questions?

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- How did they the FCC make the decisions in the end? What were they?
- Is TAC ongoing? What changes have been made?
- How do people at different places co-author papers?

Logistics

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- Some games from last year available

Open vs. Sealed Bid

- Open increases information, reducing winner's curse
 - Leads to higher bids
- **But...**
 - Risk aversion leads to higher bids in sealed bid auctions
 - Sealed bid auctions deter collusion
- Decided former outweighed latter
- Went with announcing bids, but not the bidders
 - Circumvented!

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 - Close licenses almost simultaneously
 - be simple and understandable

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Went with activity rules

Combinatorial Bids

- Nationwide bidding could decrease efficiency and revenue

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- Nationwide bidding could decrease efficiency and revenue
- Full combinatorial bidding too complex
 - Winner determination problem
 - Active research area

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- Decided against

Reserve Prices

- Not necessary in such a competitive market
- Did include withdrawal penalties

Results

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 - Lots of bidders
 - Lots of revenue

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- Incremental design changes
 - New problems always arise
 - Bidders indeed find ways to circumvent mechanisms
- Lessons to be learned via agent-based experiments

Class Discussion

Ankit Srivastava on auctions in RoboCup Rescue

Trading Agent Competition

- Put forth as a **benchmark problem** for e-marketplaces (Wellman, Wurman, et al., 2000)
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 - **Client:** TACTown ↔ Tampa within 5-day period

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 - **Game:** 8 *agents*, 12 min.
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 - **Client:** TACtown ↔ Tampa within 5-day period
- **Auctions** for flights, hotels, entertainment tickets
 - **Server** maintains markets, sends prices to agents
 - Agent sends bids to server **over network**

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Flights: Inflight days 1-4, Outflight days 2-5 (8)

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- Random auction closes minutes 4 – 11

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Entertainment: Wrestling/Museum/Park days 1-4 (12)

- Continuous double auction; initial endowments; quote is bid-ask spread; resale allowed

Client Preferences and Utility

Preferences: randomly generated per client

- Ideal arrival, departure days
- Good Hotel Value
- Entertainment Values

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Score: Sum of client utilities – expenditures

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Prices known $\Rightarrow G^*$ known \Rightarrow optimal bids known

High-Level Strategy

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Goal: analytically calculate optimal bids

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- Hotel closing times
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New algorithm for conditional density estimation

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- Value of i th copy is $\text{avg}(V_i - V_{i-1})$

Other Uses of Sampling

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Entertainment: Bid more (ask less) than expected value of having one more (fewer) ticket

Finals

Team	Avg.	Adj.	Institution
ATTac	3622	4154	AT&T
livingagents	3670	4094	Living Systems (Germ.)
whitebear	3513	3931	Cornell
Urlaub01	3421	3909	Penn State
Retsina	3352	3812	CMU
CaiserSose	3074	3766	Essex (UK)
Southampton	3253*	3679	Southampton (UK)
TacsMan	2859	3338	Stanford

- ATTac improves over time
- livingagents is an open-loop strategy

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- *EarlyBidder*: motivated by TAC-01 entry living agents
 - Immediately bids high for G^* (with *SimpleMean_{n,s}*)
 - Goes to sleep

Stability

- 7 *EarlyBidder*'s with 1 *ATTac*

Agent	Score	Utility
<i>ATTac</i>	2431 \pm 464	8909 \pm 264
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EarlyBidder gets more utility; *ATTac* pays less

Results

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<i>Agent</i>	<i>Relative Score</i>	
	<i>Phase I</i>	<i>Phase III</i>
<i>ATTac_{ns}</i>	105.2 ± 49.5 (2)	166.2 ± 20.8 (1)
<i>ATTac_s</i>	27.8 ± 42.1 (3)	122.3 ± 19.4 (2)
<i>EarlyBidder</i>	140.3 ± 38.6 (1)	117.0 ± 18.0 (3)
<i>SimpleMean_{ns}</i>	−28.8 ± 45.1 (5)	−11.5 ± 21.7 (4)
<i>SimpleMean_s</i>	−72.0 ± 47.5 (7)	−44.1 ± 18.2 (5)
<i>ConditionalMean_{ns}</i>	8.6 ± 41.2 (4)	−60.1 ± 19.7 (6)
<i>ConditionalMean_s</i>	−147.5 ± 35.6 (8)	−91.1 ± 17.6 (7)
<i>CurrentPrice</i>	−33.7 ± 52.4 (6)	−198.8 ± 26.0 (8)

FCC Spectrum Auction #35

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- Other complex rules

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It's a poker game!

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 - goals based on published data

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- Agent goals
 - desire 0, 1, or 2 licences per market
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- Utility is profit $\Rightarrow \sum_l (value - cost)$
- modeled 5 most important bidders
 - others served mainly to raise prices (small bidders)
 - lower valuations (75% \rightarrow pessimistic)

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 - explicit communication not allowed...

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 - convention: unlucky bidders may take licences until fair
- Small bidders take licences from owners
 - big bidders remember licence's owner
 - allocate while small bidders active

RSDR vs. Knapsack

<i>Method</i>	<i>Agent</i>	<i>Profit (\$M)</i>	<i>Ratio</i>	<i>Cost</i>
Knapsack	1	980 (± 170)	1.00	.82
	2	650 (± 85)	1.00	.82
	3	830 (± 91)	1.00	.84
	4	170 (± 20)	1.00	.84
	5	550 (± 96)	1.00	.86
PRSDR	1	1240 (± 210)	1.26	.76
	2	820 (± 83)	1.25	.77
	3	1300 (± 290)	1.58	.74
	4	300 (± 44)	1.78	.79
	5	930 (± 240)	1.68	.76

44% more profit; avg. ratio 1.51

Robustness

- What if someone cheats?
 - cheat: defect back to knapsack
 - others stay out of its way \Rightarrow big win
- Solution: Punishing RSDR (PRSDR)
 - cheaters may not own licences
 - recall: non-cheaters take licence from owner = fairing
 - convention: cheater takes your licence \Rightarrow take it back
 - * take it back first while still have money
 - * aggressively punitive: skips optimizers

Simplification: pointing out cheaters by hand

PRSDR Results

<i>Method</i>	<i>Ratio</i>	<i>Cost</i>
Knapsack	1.00	.84
(P)RSDR	1.51	.76
RSDR Cheater	1.63	.76
RSDR Victims	1.22	.79
PRSDR Cheater	1.02	.83
PRSDR Enforcers	1.17	.81

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PRSDR Enforcers	1.17	.81

Threats work!

Extensions

- Change small bidder valuations
 - test robustness
 - RSDR is optimal for preserving profit
- Multiple cheaters
 - current punishment too aggressive
 - collapse back to knapsack instead

Extensions

<i>Method</i>	<i>Ratio</i>	<i>Local Ratio</i>	<i>Cost</i>
Multiple Cheater	1.03		.84
Multiple Enforcer	1.01		.83

Extensions

<i>Method</i>	<i>Ratio</i>	<i>Local Ratio</i>	<i>Cost</i>
Multiple Cheater	1.03		.84
Multiple Enforcer	1.01		.83
50%, Knapsack	1.70	1.00	.74
50%, PRSDR	3.42	2.02	.51
75%, Knapsack	1.00	1.00	.84
75%, PRSDR	1.51	1.51	.76
85%, Knapsack	0.68	1.00	.89
85%, PRSDR	0.81	1.19	.87

Future Work

- Robustness enhancements
 - better punishment method
- More complex value functions
 - inter-market dependencies
- Automatic cheater detection
 - partial cheating vs. detection arms race
 - smack back into compliance
- Generalization to other auctions
 - more robust to tie-breaking procedure variations

Summary

- Communication-free coordination
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- Works even uncertain knowledge
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Summary

- Communication-free coordination
- Enables much higher profits
- Works even uncertain knowledge
- Real-world functionality relies on simple assumptions:
 - bidders want more profit
 - bidders familiar with PRSDR and its benefits
 - bidders willing to try it risk-free

Last-minute bidding (R,O, 2001)

- eBay: first-price, ascending auction
- Amazon: auction extended if bid in last 10 minutes
- eBay: bots exist to incrementally raise your bid to a maximum
- Still people *snipe*. Why?
 - There's a risk that the bid might not make it
 - However, common-value \implies bid conveys info
 - Late-bidding can be seen as implicit collusion
 - Or . . . , lazy, unaware, etc. (Amazon and eBay)
- Finding: more late-bidding on eBay,
 - even more on antiques rather than computers

Small design-difference matters

Late Bidding as Best Response

- Good vs. incremental bidders
 - They start bidding low, plan to respond
 - Doesn't give them time to respond
- Good vs. other snipers
 - Implicit collusion
 - Both bid low, chance that one bid doesn't get in
- Good in common-value case
 - protects information

Overall, the analysis of multiple bids supports the hypothesis that last-minute bidding arises at least in part as a response by sophisticated bidders to unsophisticated incremental bidding.