

# **CS378**

# **Autonomous Multiagent Systems**

## **Spring 2005**

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Department of Computer Sciences  
The University of Texas at Austin

Week 10a: Tuesday, March 28th

# Good Afternoon, Colleagues

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Are there any questions?

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- how do you find NEQ?
- what if there are multiple NEQ?

# T-test vs. Paired T-test

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- Is the right half of the class or the left half taller?

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- Who's better at tetris? Gary or Andrew?

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- Did you weigh less after the class than before?
- Who's better at tetris? Gary or Andrew?
- Who's better at video games in general?

# T-test vs. Paired T-test

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- Test: Your team better than UvA vs. Brainstormers



# T-test vs. Paired T-test

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- Test: Your team better than UvA vs. Brainstormers
- Test: Your team better than UvA vs. a set of 20 opponents

# T-test vs. Paired T-test

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- Test: Your team better than UvA vs. Brainstormers
- Test: Your team better than UvA vs. a set of 20 opponents
- What if neither is significant?

# Bach/Stravinsky

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- Unfortunately, there are 2: Bach and Stravinsky
- No time to get in touch with each other
- I prefer Stravinsky, she prefers Bach
- But most of all, we want to be together
- Propose a payoff matrix



# Bach/Stravinsky

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		Wife	
		S	B
Me	S	2, 1	0, 0
	B	0, 0	1, 2

# Matching Pennies

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- We each put a penny down covered
- If they match, I win, if they don't, you win

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		Player 2	
		H	T
Player 1	H	1, -1	-1, 1
	T	-1, 1	1, -1

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Nash equilibrium?

# Tom's Game 3

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- Every day, the work robot can choose to either work, or shirk.
- The supervisor can choose to spend the day inspecting, or not.
- Every day the worker works, the supervisor makes \$VALUE from his work.
- Every day the supervisor does not catch the worker shirking, he pays \$WAGE.

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- Every day, the work robot can choose to either work, or shirk.
- The supervisor can choose to spend the day inspecting, or not.
- Every day the worker works, the supervisor makes \$VALUE from his work.
- Every day the supervisor does not catch the worker shirking, he pays \$WAGE.
- It costs the worker \$EFFORT\_W to work.
- It costs the supervisor \$EFFORT\_I to inspect.



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- Every day, the work robot can choose to either work, or shirk.
- The supervisor can choose to spend the day inspecting, or not.
- Every day the worker works, the supervisor makes \$VALUE from his work.
- Every day the supervisor does not catch the worker shirking, he pays \$WAGE.
- It costs the worker \$EFFORT\_W to work.
- It costs the supervisor \$EFFORT\_I to inspect.

What are the payoff matrices?

# Tom's matrices

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worker:

	Inspect	NoInspect
Work	$\text{WAGE-EFFORT}_W$	$\text{WAGE-EFFORT}_W$
Shirk	0	WAGE

supervisor:

	Inspect	NoInspect
Work	$\text{VALUE-WAGE-EFFORT}_I$	$\text{VALUE-WAGE}$
Shirk	$-\text{EFFORT}_I$	$-\text{WAGE}$

# Tom's matrices

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worker:

	Inspect	NoInspect
Work	$WAGE - EFFORT\_W$	$WAGE - EFFORT\_W$
Shirk	0	$WAGE$

supervisor:

	Inspect	NoInspect
Work	$VALUE - WAGE - EFFORT\_I$	$VALUE - WAGE$
Shirk	$-EFFORT\_I$	$-WAGE$

The nash equilibrium is as follows:

$$p(I) = EFFORT\_W / WAGE$$

$$p(W) = EFFORT\_I / WAGE$$