Topic 1 CS314 Course Introduction

Chapman: I didn't expect a kind of Spanish Inquisition. **Cardinal Ximinez:** NOBODY expects the Spanish Inquisition! Our chief weapon is surprise...surprise and fear...fear and surprise.... Our two weapons are fear and surprise...and ruthless efficiency.... Our **three** weapons are fear, surprise, and ruthless efficiency...and an almost fanatical devotion to the Pope.... Our **four**...no... **Amongst** our weapons.... Amongst our weaponry...are such diverse elements as fear, surprise....

In class: please close laptops and put away mobile devices.

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Who Am I?

- Professor of Instruction (lecturer) in CS department since 2000
- Undergrad Stanford, MSCS RPI
- US Navy for 8 years, submarines
- 2 years Round Rock High School prior to coming to UT





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Rensselaer

Purpose of these Slides

- Discuss
 - course content
 - procedures
 - tools
- For your TO DO list:
 - complete items on the startup page

www.cs.utexas.edu/~scottm/cs314/handouts/startup.htm

Course Goals

- Analyze algorithms and code for efficiency
- Be able to create and use canonical data structures: lists (array and linked), stacks, queues, trees, binary search trees, balanced binary search trees, maps, sets, graphs, hash tables, heaps, tries
- Know and use the following programming tools and techniques: object oriented programming (encapsulation, inheritance, polymorphism), Java Interfaces, iterators, sorting, searching, recursion, dynamic programming, functional programming

Course Goals		Prerec	quisites
After CS314 you can design and implement		Formal: CS312 with	a grade of C- or higher
medium size programs (several 100's of lines of code split between multiple classes) to		Informal: Ability to de programs in Java usi	č
solve interesting problems		 variables and data types 	•arrays (vectors, lists)
Recall, the three core areas of the UTCS undergrad degree:		•expressions, order of operations	•top down design (breaking big rocks into little rocks)
Programming, Theory, Systems		 Conditionals (if statements) including boolean logic and boolean expressions 	 algorithm and data design create and implement program of at least 200 - 300 loc
After this class your instructors shall expect		•iteration (loops)	•could you write a program to let two people play connect 4?
you can write complex programs given a specification or problem statement.		 Methods (functions, procedures) Parameters 	
– You have to design the algorithm in many cases.	5	•structures or records or	e Overview

CS314 Topics

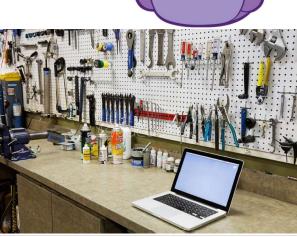
- 1. Introduction
- 2. Algorithm Analysis
- 3. Encapsulation
- 4. Inheritance
- 5. Polymorphism
- 6. Generics
- 7. Interfaces
- 8. Iterators
- 9. Abstract Classes
- 10. Maps, Sets
- 11. Linked Lists
- 12. Recursion
- 13. Recursive Backtracking

- 14. Searching, Simple Sorts
 15. Stacks
 16. Queues
 17. Faster Sorting
 18. Trees
 19. Binary Search Trees
 20. Red-Black Trees
 21. Huffman Code Trees
 22. Graphs
- 23. Hash tables
- 24. Tries
- 25. Heaps
- 26. Dynamic Programming

27. Functional Programming

Data Structures

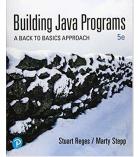
- simple definition:
 - a variable that stores other variables, a container
- We will learn a toolbox full of data structures .
- ... and how to build them ...
- ... and how to use new ones.

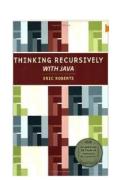


Clicker Question 1 Which of the following is a data structure? A. a method 	 Resources Class web site – most course material Class discussion
B. a try / catch block C. a double	group – Ed Monday -> Canvas -> Grades,
D. an array E. more than one of A - D	Program Submissions
	(GradeScope), Access Zoom Links,
CS314 Course Overview C	Recorded Lectures,

Books

- books are recommended, not required
- free alternatives on the web, see schedule
 - BJP strongly recommended
 - Thinking Recursively in Java recursion





Clicker Question 2

Which of these best describes you?

- A. First year at UT and first year college student
- B. First year at UT, transferring from another college or university
- C. Second year at UT
- D. Third year at UT
- E. Other

Course Overview

 Course Grades Admittedly a complex system see syllabus complete syllabus quiz +/- grades used My CS314 Historical Grades 82% C- or higher: 28% A's, 34% B's, 20% C's 8% D or F 10% Q or W (drop) 	 Programming Assignments Individual – do your own work (no copying or use of generative Als such as ChatGPT) Programs checked automatically with plagiarism detection software (MOSS) Turn in the right thing - correct name, correct format or you will lose points / slip days Graded on Correctness AND program hygiene "Code is read more often than it is written." - <i>Guido Van Rossum</i>, Creator of Python
 WORK LOAD EVALUATED AS <u>HIGH</u> (but not	 Slip days: 8 for term, max 2 per assignment,
EXCESSIVE) ON COURSE SURVEYS	don't use frivolously

Succeeding in the Course

- Randy Pausch, CS Professor at CMU said:
- When I got tenure a year early at Virginia, other

Assistant Professors would come up to me and say, 'You got tenure early ???! What's your secret?????' and I would tell them, 'Call me in my office at 10pm on Friday night and I'll tell you.' '

* "A lot of people want a shortcut. I find the best shortcut is the long way, which is basically two words: work hard."

Succeeding in the Course - Meta

- "Be the first penguin"
 - Ask questions!!!
 - lecture, section, Ed Discussion, help hours, co-study
- DOPS "It is impossible to be perfect"
 - Mistakes are okay.
 - That is how we learn.
 - Trying to be perfect means not taking risks.
 - no risks, no learning
- "Find a Pack"
 - Make friends.

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- Study with them!





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<section-header> Required Software and Hardware Java - Oracle or OpenJDK, limit ourselves to Java 8 (see program hygiene requirements for disallowed features) IDE such as IntelliJ or Eclipse Do not use a code assist tool such as Copilot on programming assignments Device to access Canvas Instapoll during lectures Device to take images of section problems and submit to Gradescope Zoom, used occasionally </section-header>	<section-header><section-header><text><text><list-item><list-item><list-item><list-item><list-item><list-item></list-item></list-item></list-item></list-item></list-item></list-item></text></text></section-header></section-header>

Clicker Question 1 Topic Number 2 Efficiency – Complexity -* "A program finds all the prime numbers" between 2 and 1,000,000,000 from scratch **Algorithm Analysis** in 0.37 seconds." - Is this a fast solution? "bit twiddling: 1. (pejorative) An exercise in tuning A. no (see tune) in which incredible amounts of time and effort go to produce little noticeable improvement, B. yes often with the result that the code C. it depends becomes incomprehensible." - The Hackers Dictionary, version 4.4.7 CS 314 Efficiency - Complexity 2 Technique Efficiency Semi-formal approach for this class Computer Scientists don't just write programs. - more formal techniques in theory classes, CS331 They also analyze them. How many computations will this program (method, algorithm) perform to get the answer? How efficient is a program? Many simplifications - How many computations does it take program to complete? - view algorithms as Java programs - How much memory does a program use? - determine by analysis the total number executable statements (computations) in - How do these change as the amount program or method as a function of the amount of data changes? of data - What is the difference between the average case - focus on the *dominant term* in the function and worst case efficiency if any? T(N) = 17N³ + 25N² + 35N + 251 *IS ORDER N*³ CS 314 Efficiency - Complexity 3

<pre>Counting Statements int x; // one statement x = 12; // one statement int y = z * x + 3 % 5 * x / i; // 1 x++; // one statement boolean p = x < y && y % 2 == 0 z >= y * x; // 1 int[] data = new int[100]; // 100 data[50] = x * x + y * y; // 1</pre>	<pre>Clicker 2 • What is output by the following code? int total = 0; for (int i = 0; i < 13; i++) for (int j = 0; j < 11; j++) total += 2; System.out.println(total); A. 24 B. 120 C. 143 D. 286 E. 338</pre>
CS 314 Efficiency - Complexity 5	CS 314 Efficiency - Complexity 6
Clicker 3	Example
<pre> What is output when method sample is called? // pre: n >= 0, m >= 0 public static void sample(int n, int m) { int total = 0; for (int i = 0; i < n; i++) for (int j = 0; j < m; j++) total += 5; System.out.println(total); } </pre>	<pre>public int total(int[] values) { int result = 0; for (int i = 0; i < values.length; i++) result += values[i]; return result; } How many statements are executed by method total as a function of</pre>

- values.length
 Let N = values.length
 - N is commonly used as a variable that denotes the amount of data

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A. 5

B. n * m

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C. n * m * 5

D. n^m

Efficiency - Complexity

E. (n * m)⁵

<pre>Counting Up Statements int result = 0; 1 int i = 0; 1 i < values.length; N + 1 i++ N result += values[i]; N return total; 1 T(N) = 3N + 4 T(N) is the number of executable statements in method total as function of values.length CS 314 Efficiency-Complexity 9</pre>	 Another Simplification When determining complexity of an algorithm we want to simplify things ignore some details to make comparisons easier Like assigning your grade for course At the end of CS314 your transcript won't list all the details of your performance in the course it won't list scores on all assignments, quizzes, and tests simply a letter grade, B- or A or D+ So we focus on the dominant term from the function and ignore the coefficient
 Big O The most common method and notation for discussing the execution time of algorithms is <i>Big O</i>, also spoken <i>Order</i> Big O is a mathematical technique that allows us to take a function and, typically, simplify it. So that when we talk about efficiency in a simpler "language", a language of functions Big O is an upper bounds Hido a lot of unimportant dotails by appigning 	 Formal Definition of Big O T(N) is O(F(N)) if there are positive constants c and N₀ such that T(N) ≤ cF(N) when N ≥ N₀ N is the size of the data set the algorithm works on T(N) is a function that characterizes the <i>actual</i> running time of the algorithm F(N) is a function that characterizes an upper bounds on T(N). It is a limit on the running time of the algorithm. (The typical Big functions table) c and N₀ are constants

Hide a lot of unimportant details by assigning a simple grade (function) to algorithms

-c and N₀ are constants

algorithm – can be e stateme F(N) is th rate – may be T(N) may – constant	What it Means he actual growth rate of the equated to the number of exec nts in a program or chunk of o he function that bounds the upper or lower bound y not necessarily equal F(N ts and lesser terms ignored be ling function	cutable code e growth	 Recall the T(N) is O(and N₀ such Recall metain of the show metai	wing O(N) is Co formal definition of B F(N)) if there are position of that $T(N) \le cF(N)$ wh hod total, $T(N) = 3$ hod total is O(N).	ig O ve constants c en N > N ₀ N + 4
CS 314	Efficiency - Complexity	13	CS 314	Efficiency - Complexity	14
number of exec	the for algorithm to complete. (simplutable statements) C * F(N), in this case, C = 4, $C * F(N) = 4NT(N), actual function of number ofIn this case 3N + 4F(N), approximate functionof computations. In this caseC = 5axis: N, number of elements$	computations. n ase N	Typical IFunctionN! 2^N N^d , $d > 3$ N^d , $d > 3$ N^3 N^2 $N\sqrt{N}$ $N \log N$ N \sqrt{N} $\log N$ 1	Big O Functions –Common NamefactorialfactorialExponentialPolynomialCubicQuadraticN Square root NN log NLinearRoot - nLogarithmicConstant	"Grades" Running time grows 'quickly' with more input. Running time grows 'slowly' with more input.
CS 314	Efficiency - Complexity	15	CS 314	Efficiency - Complexity] 16

	Clicker 4		Showing	g Order More	e Formally	••••
Which	of the following is true?		▶ Show 10N	J ² + 15N is O(N ²)		
Recall	$T(N)_{total} = 3N + 4$		Break into	o terms.		
 A. Method total is O(N^{1/2}) B. Method total is O(N) C. Method total is O(N²) D. Two of A – C are correct 						
			• $10N^2 \le 10N^2$ • $15N \le 15N^2$ for $N > 1$ (New odd)			
				—		
			E. All OI L	hree of A – C are correct		▶ 10N ² + 15
			C = 25, N₀	, = 1		
			Note, the	choices for c and	l N ₀ are not uniq	ue.
CS 314	Efficiency - Complexity	17	CS 314	Efficiency - Complexity		18
Dea	aling with other metho	ods	Deali	na With Oth	er Methods	
	aling with other metho	ods		ng With Oth		
	o I do about method calls?	ods	public int int tot	foo(int[] data) + al = 0;	{	
• What do double sum for (int i	<pre>b I do about method calls? = 0.0; = 0; i < n; i++)</pre>	ods	public int int tot for (in	foo(int[] data) { al = 0; t i = 0; i < data	{ a.length; i++)	
What do double sum for (int i sum +=	<pre>D I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i);</pre>	ods	public int int tot for (in	foo(int[] data) { al = 0; t i = 0; i < data al += countDups(c	{ a.length; i++)	
<pre> What do double sum for (int i sum += Long wat</pre>	<pre>b I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i); ay</pre>	ods	<pre>public int int tot for (in tot return }</pre>	<pre>foo(int[] data) + al = 0; t i = 0; i < data al += countDups(c total;</pre>	{ a.length; i++) data[i], data);	
<pre> What do double sum for (int i sum += Long wa - go to th</pre>	<pre>D I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i);</pre>	ods	<pre>public int int tot for (in tot return } // method c</pre>	foo(int[] data) { al = 0; t i = 0; i < data al += countDups(c	{ a.length; i++) data[i], data); where N is the	
<pre> What do double sum for (int i sum += Long wa - go to th</pre>	<pre>b I do about method calls? a = 0.0; = 0; i < n; i++) Math.sqrt(i); Ay nat method or constructor and statements</pre>	ods	<pre>public int int tot for (in tot return } // method c</pre>	<pre>foo(int[] data) + al = 0; t i = 0; i < data al += countDups(c total; ountDups is O(N)</pre>	{ a.length; i++) data[i], data); where N is the	
 What do double sum for (int i sum += Long wa go to the count sum Short wa substitute 	<pre>b I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i); ay nat method or constructor and statements ay ute the simplified Big O function f</pre>		<pre>public int int tot for (in tot return } // method c // length o Clicker 5, V</pre>	<pre>foo(int[] data) { al = 0; t i = 0; i < data al += countDups(c total; ountDups is O(N) f the array it is Vhat is the Big O</pre>	{ a.length; i++) data[i], data); where N is the s passed of foo?	
 What do double sum for (int i sum += Long wa go to the count set Short wa substituting that mediated 	<pre>b I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i); ay nat method or constructor and statements ay ute the simplified Big O function freethod.</pre>	or	<pre>public int</pre>	<pre>foo(int[] data) { al = 0; t i = 0; i < data al += countDups(c total; ountDups is O(N) f the array it is Vhat is the Big O</pre>	{ a.length; i++) data[i], data); where N is the s passed	
 What do double sum for (int i sum += Long wa go to the count set Short wa substitution and the matching 	<pre>b I do about method calls? = 0.0; = 0; i < n; i++) Math.sqrt(i); ay nat method or constructor and statements ay ute the simplified Big O function f</pre>	or ly count	<pre>public int int tot for (in tot return } // method c // length o Clicker 5, V</pre>	<pre>foo(int[] data) { al = 0; t i = 0; i < data al += countDups(c total; ountDups is O(N) f the array it is Vhat is the Big O</pre>	{ a.length; i++) data[i], data); where N is the s passed of foo?	

```
Independent Loops
// from the Matrix class
public void scale(int factor) {
     for (int r = 0; r < numRows(); r++)
           for (int c = 0; c < numCols(); c++)
                 iCells[r][c] *= factor;
}
numRows () returns number of rows in the matrix iCells
numCols() returns number of columns in the matrix iCells
Assume iCells is an N by N square matrix.
Assume numRows and numCols are O(1)
What is the T(N)? Clicker 6, What is the Order?
A. O(1)
                B. O(N)
                                 C. O(NlogN)
D. O(N^2)
                E. O(N!)
Bonus question. What if numRows is O(N)?
```

Just Count Loops, Right?

```
// Assume mat is a 2d array of booleans.
// Assume mat is square with N rows,
// and N columns.
public static void count(boolean[][] mat,
                                  int row, int col) {
int numThings = 0;
for (int r = row - 1; r \le row + 1; r++)
      for (int c = col - 1; c \le col + 1; c++)
           if (mat[r][c])
                 numThings++;
Clicker 7. What is the order of the method count?
A. O(1)
           B. O(N^{0.5}) C. O(N)
                                 D. O(N<sup>2</sup>)
                                            E. O(N<sup>3</sup>)
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                                                  22
```

It is Not Just Counting Loops

```
// "Unroll" the loop of method count:
int numThings = 0;
if (mat[r-1][c-1]) numThings++;
if (mat[r-1][c]) numThings++;
if (mat[r-1][c+1]) numThings++;
if (mat[r][c-1]) numThings++;
if (mat[r][c]) numThings++;
if (mat[r][c+1]) numThings++;
if (mat[r+1][c-1]) numThings++;
if (mat[r+1][c]) numThings++;
if (mat[r+1][c+1]) numThings++;
```

Just Count Loops, Right?

```
private static void mystery(int[] data) {
              stopIndex = data.length - 1;
             int j = 1;
             while (stopIndex > 0) {
                    if (data[j - 1] > data[j]) {
                          int t = data[j];
                          data[j] = data[j - 1];
                          data[j - 1] = t;
                    }
                    if (j == stopIndex) {
                          stopIndex--;
                          i = 1;
                    } else {
                          j++;
                    }
                                  N = data.length
             }
Clicker 8, What is the order of method mystery?
A. O(1)
             B. O(N^{0.5})
                         C. O(N)
                                       D. O(N<sup>2</sup>)
                                                    E. O(N<sup>3</sup>)
```

 Sidetrack, the logarithm Thanks to Dr. Math 3² = 9 	 When Do Logarithms Occur Algorithms tend to have a logarithmic term when they use a divide and conquer technique the size of the data set keeps getting divided by 2
 likewise log₃ 9 = 2 "The log to the base 3 of 9 is 2." The way to think about log is: "the log to the base x of y is the number you can raise x to to get y." Say to yourself "The log is the exponent." (and say it over and over until you believe it.) In CS we work with base 2 logs, a lot log₂ 32 = ? log₂ 8 = ? log₂ 1024 = ? log₁₀ 1000 = ? 	<pre>public int foo(int n) { // pre n > 0 int total = 0; while (n > 0) { n = n / 2; total++; } return total; } Clicker 9, What is the order of the above code? A. O(1) B. O(logN) C. O(N) D. O(Nlog N) E. O(N²)</pre>
CS 314 Efficiency - Complexity 25	The base of the log is typically not included as we can switch from26one base to another by multiplying by a constant factor.

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Significant Improvement – Algorithm with Smaller Big O function

 Problem: Given an array of ints replace any element equal to 0 with the maximum positive value to the right of that element. (if no positive value to the right, leave unchanged.)

Given:

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```
[0, 9, 0, 13, 0, 0, 7, 1, -1, 0, 1, 0]
Becomes:
```

```
[<u>13</u>, 9, <u>13</u>, 13, <u>7</u>, <u>7</u>, 7, 1, -1, <u>1</u>, 1, 0]
```

Efficiency - Complexity

```
Replace Zeros – Typical Solution
public void replace0s(int[] data) {
  for(int i = 0; i < data.length; i++){
    if (data[i] == 0) {
       int max = 0;
       for(int j = i+1; j < data.length; j++)
           max = Math.max(max, data[j]);
       data[i] = max;
Assume all values are zeros. (worst case)
Example of a dependent loops.
Clicker 10 - Number of times j < data.length evaluated?
A.O(1)
               B. O(N)
                             C. O(NlogN)
D. O(N<sup>2</sup>)
               E. O(N!)
```

A VERY Useful Proportion

Since F(N) is characterizes the running time of an algorithm the following proportion should hold true:

 $F(N_0) / F(N_1) \sim = time_0 / time_1$

- An algorithm that is O(N²) takes 3 seconds to run given 10,000 pieces of data.
 - How long do you expect it to take when there are 30,000 pieces of data?
 - common mistake
 - logarithms?

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Efficiency - Complexity

Why Use Big O?

- As we build data structures Big O is the tool we will use to decide under what conditions one data structure is better than another
- Think about performance when there is a lot of data.
 - "It worked so well with small data sets..."
 - Joel Spolsky, Schlemiel the painter's Algorithm
- Lots of trade offs

- some data structures good for certain types of problems, bad for other types
- often able to trade SPACE for TIME.
- Faster solution that uses more space
 Slower solution that uses less space

Big O Space	Quantifiers on Big O
 Big O could be used to specify how much space is needed for a particular algorithm 	It is often useful to discuss different cases for an algorithm
 in other words how many variables are needed 	Best Case: what is the best we can hope for?
Often there is a time – space tradeoff	 least interesting, but a good exercise
 – can often take less time if willing to use more memory 	 Don't assume no data. Amount of date is still variable, possibly quite large
 – can often use less memory if willing to take longer 	Average Case (a.k.a. expected running time): what usually happens with the algorithm?
 truly beautiful solutions take less time and space 	Worst Case: what is the worst we can expect
The biggest difference between time and space is	of the algorithm?
that you can't reuse time Merrick Furst	 very interesting to compare this to the average case

```
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```

Efficiency - Complexity

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Best, Average, Worst Case

- To Determine the best, average, and worst case Big O we must make assumptions about the data set
- Best case -> what are the properties of the data set that will lead to the fewest number of executable statements (steps in the algorithm)
- Worst case -> what are the properties of the data set that will lead to the largest number of executable statements
- Average case -> Usually this means assuming the data is randomly distributed
 - or if I ran the algorithm a large number of times with different sets of data what would the average amount of work be for those runs?

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Another Example

Efficiency - Complexity

<pre>double minimum(double[] values)</pre>	{
n = values.length;	
le minValue = values[0];	
(int i = 1; i < n; i++)	
f (values[i] < minValue)	
<pre>minValue = values[i];</pre>	
rn minValue;	
1	<pre>n = values.length; le minValue = values[0]; (int i = 1; i < n; i++) f (values[i] < minValue)</pre>

}

- T(N)? F(N)? Big O? Best case? Worst Case? Average Case?
- If no other information, assume asking average case

Example of Dominance

Look at an extreme example. Assume the actual number as a function of the amount of data is:

N²/10000 + 2Nlog₁₀ N+ 100000

- Is it plausible to say the N² term dominates even though it is divided by 10000 and that the algorithm is O(N²)?
- What if we separate the equation into (N²/10000) and (2N log₁₀ N + 100000) and graph the results.

Summing Execution Times

blue line is

 $N^{2}/10000$

 For large values of N the N² term dominates so the algorithm is O(N²)

100,000

When does it make sense to use a computer?

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900,000 800.000

200 000

600,000

500.000

400,000 300.000

100 000

Efficiency - Complexity

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Comparing Grades

Efficiency - Complexity

- Assume we have a problem
- Algorithm A solves the problem correctly and is O(N²)
- Algorithm B solves the same problem correctly and is O(N log₂N)
- Which algorithm is faster?
- One of the assumptions of Big O is that the data set is large.
- The "grades" should be accurate tools if this holds true.

Running Times

Assume N = 100,000 and processor speed is 1,000,000,000 operations per second

Function	Running Time
2 ^N	3.2 x 10 ^{30,086} years
N ⁴	3171 years
N ³	11.6 days
N ²	10 seconds
N/ N	0.032 seconds
N log N	0.0017 seconds
Ν	0.0001 seconds
\sqrt{N}	3.2 x 10 ⁻⁷ seconds
log N	1.2 x 10 ⁻⁸ seconds

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Theory to Practice OR Dykstra says: "Pictures are for the Weak."

	1000	2000	4000	8000	16000	32000	64000	128K
O(N)	2.2x10 ⁻⁵	2.7x10 ⁻⁵	5.4x10 ⁻⁵	4.2x10 ⁻⁵	6.8x10 ⁻⁵	1.2x10 ⁻⁴	2.3x10 ⁻⁴	5.1x10 ⁻⁴
O(NlogN)	8.5x10⁻⁵	1.9x10 ⁻⁴	3.7x10 ⁻⁴	4.7x10 ⁻⁴	1.0x10 ⁻³	2.1x10 ⁻³	4.6x10 ⁻³	1.2x10 ⁻²
O(N ^{3/2})	3.5x10⁻⁵	6.9x10 ⁻⁴	1.7x10 ⁻³	5.0x10 ⁻³	1.4x10 ⁻²	3.8x10 ⁻²	0.11	0.30
O(N ²) ind.	3.4x10 ⁻³	1.4x10 ⁻³	4.4x10 ⁻³	0.22	0.86	3.45	13.79	(55)
O(N²) dep.	1.8x10 ⁻³	7.1x10 ⁻³	2.7x10 ⁻²	0.11	0.43	1.73	6.90	(27.6)
O(N ³)	3.40	27.26	(218)	(1745) 29 min.	(13,957) 233 min	(112k) 31 hrs	(896k) 10 days	(7.2m) 80 days

Times in Seconds. Red indicates predicated value. Efficiency - Complexity

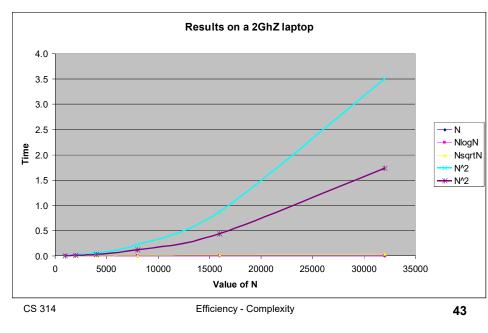
Change between Data Points

	1000	2000	4000	8000	16000	32000	64000	128K	256k	512k
O(N)	-	1.21	2.02	0.78	1.62	1.76	1.89	2.24	2.11	1.62
O(NlogN)	-	2.18	1.99	1.27	2.13	2.15	2.15	2.71	1.64	2.40
O(N ^{3/2})	-	1.98	2.48	2.87	2.79	2.76	2.85	2.79	2.82	2.81
O(N ²) ind	-	4.06	3.98	3.94	3.99	4.00	3.99	-	-	-
O(N²) dep	-	4.00	3.82	3.97	4.00	4.01	3.98	-	-	-
O(N ³)	-	8.03	-	-	-	-	-	-	-	-
Value obtained by Time _x / Time _{x-1}										
CS 314		Efficiency - Complexity 42					42			

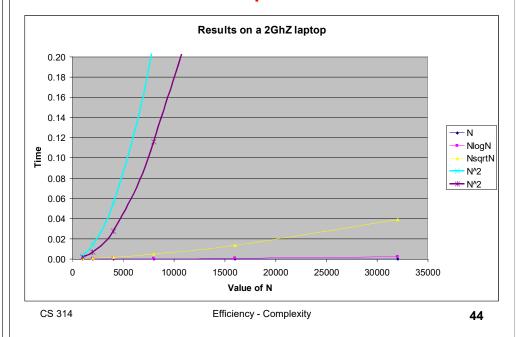
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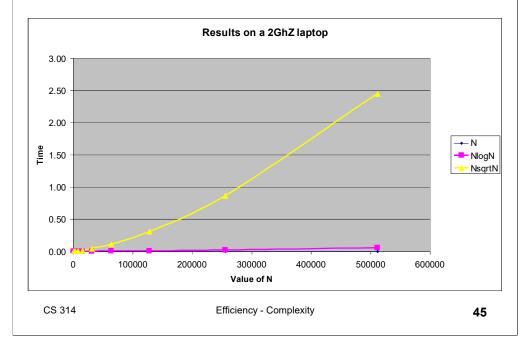
Okay, Pictures



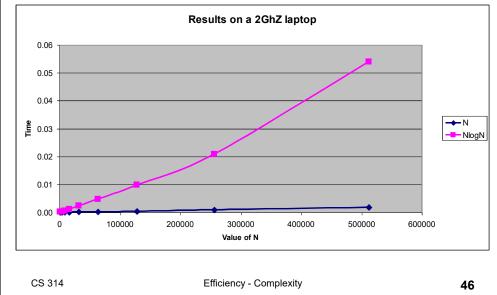
Put a Cap on Time



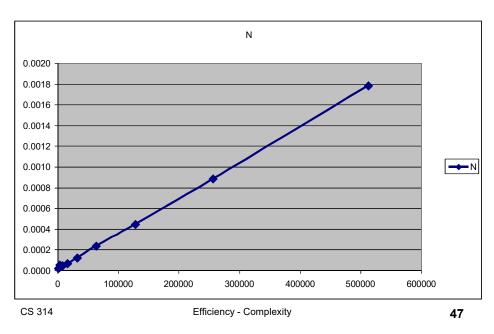
No O(N^2) Data



Just O(N) and O(NlogN)



Just O(N)



10⁹ instructions/sec, runtimes

N	O(log N)	O(N)	O(N log N)	O(N ²)
10	0.00000003	0.00000001	0.00000033	0.000001
100	0.000000007	0.00000010	0.000000664	0.0001000
1,000	0.000000010	0.00000100	0.000010000	0.001
10,000	0.00000013	0.00001000	0.000132900	0.1 min
100,000	0.000000017	0.00010000	0.001661000	10 seconds
1,000,000	0.000000020	0.001	0.0199	16.7 minutes
1,000,000,000	0.00000030	1.0 second	30 seconds	31.7 years

Forma	Definition of Big O (repeated)	More on the Formal Definition		
constants when N <u>></u> – N is the – T(N) is a running – F(N) is a bounds the algo	size of the data set the algorithm works or a function that characterizes the <i>actual</i> time of the algorithm a function that characterizes an upper on T(N). It is a limit on the running time of	 There is a point N₀ such that for all values of N that are past this point, T(N) is bounded by some multiple of F(N) Thus if T(N) of the algorithm is O(N^2) then, ignoring constants, at some point we can <i>bound</i> the running time by a quadratic function. given a <i>linear</i> algorithm it is <i>technically correct</i> to say the running time is O(N ^ 2). O(N) is a more precise answer as to the Big O of the linear algorithm thus the caveat "pick the most restrictive function" in Big O type questions. 		
CS 314	Efficiency - Complexity 49	CS 314 Efficiency - Complexity 50		
	What it All Means	Other Algorithmic Analysis Tools		
algorithn – can be stateme	he actual growth rate of the n equated to the number of executable ents in a program or chunk of code he function that bounds the growth	 Big Omega T(N) is Ω(F(N)) if there are positive constants c and N₀ such that T(N) ≥ cF(N)) when N ≥ N₀ Big O is similar to less than or equal, an upper bounds Big Omega is similar to greater than or equal, a 		
	upper or lower bound	lower bound		

- may be upper or lower bound

- T(N) may not necessarily equal F(N)
 - constants and lesser terms ignored because it is a *bounding function*

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is O(F(N))and T(N) is $\Omega(F(N))$.

- Big Theta is similar to equals

• Big Theta T(N) is $\theta(F(N))$ if and only if T(N)

	_						
	Relat	ive Rates o	f Growth				
	Analysis Type	Mathematical Expression	Relative Rates of Growth				
	Big O	T(N) = O(F(N))	T(N) <u><</u> F(N)				
	Big Ω	T(N) = Ω(F(N))	T(N) <u>></u> F(N)				
	Big θ	$T(N) = \theta(F(N))$	T(N) = F(N)				
"In spite of the additional precision offered by Big Theta, Big O is more commonly used, except by researchers in the algorithms analysis field" - Mark Weiss							
01	т	Enciency - Complexity		53			

Topic 3 Encapsulation - Implementing Classes

"And so, from Europe, we get things such as ... object-oriented analysis and design (a clever way of breaking up software programming instructions and data into small, reusable objects, based on certain abstraction principles and design hierarchies.)"

> -Michael A. Cusumano, The Business Of Software



Object Oriented Programming

- Creating large programs that work turns out to be very difficult
 - DIA Automated baggage handling system
 - Ariane 5 Flight 501
 - -<u>More</u>
- Object oriented programming is one way of managing the complexity of programming and software projects
- Break up big problems into smaller, more manageable problems

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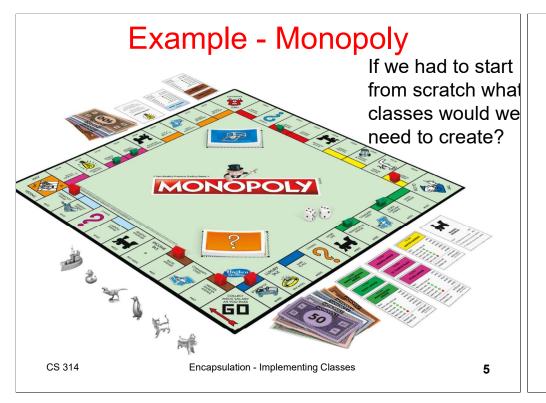
Encapsulation - Implementing Classes

Object Oriented Programming

- "Object-oriented programming is a method of programming based on a hierarchy of classes, and well-defined and cooperating objects. "
- What is a class?
- "A class is a structure that defines the data and the methods to work on that data. When you write programs in the Java language, all program data is wrapped in a class, whether it is a class you write or a class you use from the Java platform API libraries."
 - a new data type

Object Oriented Programming

- In other words break the problem up based on the things / data types that are part of the problem
- Not the only way
- One of many different kinds of strategies or paradigms for software development
 - functional, procedural, event driven, data flow, formal methods, agile or extreme, ...
- In 314 we will do a lot of object based programming



Data Structures

- A data structure is a variable that stores other variables. (overly simplified definition)
 - aka Collection, Container
- May be ordered or unordered (from client's) perspective)
 - Order a first element, second element,...
 - Lists are ordered, sets are typically unordered
- May allow duplicate values or not
 - Lists allow duplicates, sets typically do not

Encapsulation

- One of the features of object oriented languages
- Allows programmers to define new data types
- Hide the data of an object (variable)
- Group operations and data together into a new data type
- Usually easier to use something than understand exactly how it works

- microwave, car, computer, software, mp3 player

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Encapsulation - Implementing Classes

The IntList Class

- We will develop a class that models a list of ints
 - initially a pale imitation of the Java ArrayList class
- Improvement on an array of ints
 - resize automatically
 - insert easily
 - remove easily
- A list our first data structure
 - a variable that stores other variables
- Lists maintain elements in a definite order and duplicates are allowed

0	1	2	3	4	<- indices / positions
[5,	12,	5,	17,	-5]	<- elements

Clicker 1 Our IntList class has an array of ints instance variable (int[] container). What should the length of this internal array be?	Array length less than the number of elements in the list?!?
 A. less than the size of the list B. equal to the size of the list C. greater than or equal to the size of the list D. some fixed amount that never changes E. 0 	 What if most elements are all the same value? Only store the elements (and their position) not equal to the default? Sparse List
Clicker 2	IntList Design
\A/h and a lating a second to a list	Create a new omnty Intlift
When adding a new element to a list, where should the new element be added by default?	 Create a new, empty IntList new IntList -> [] The above is not code. It is a notation that shows what the results of operations. [] is an empty list. add to a list.
where should the new element be	<pre>new IntList -> [] The above is not code. It is a notation that shows</pre>
where should the new element be added by default?	 new IntList -> [] The above is not code. It is a notation that shows what the results of operations. [] is an empty list. add to a list.
where should the new element be added by default? A. The beginning	<pre>new IntList -> []</pre>
where should the new element be added by default? A. The beginning B. The end	<pre>new IntList -> []</pre>
where should the new element be added by default? A. The beginning B. The end C. The middle	<pre>new IntList -> []</pre>

<pre>IntList aList = new IntList(); aList.add(42); aList.add(12); aList.add(37);</pre>	Instance Variables Internal data
Abstract view of list of integers 0 1 2 [42, 12, 37] The wall of abstraction.	 also called instance variables because every instance (object) of this class has its own copy of these something to store the elements of the list size of internal storage container? if not what else is needed Must be clear on the difference between the internal data of an IntList object and the IntList that is being represented Why make internal data private?
Constructors	Default add method
For initialization of objects	where to add?
IntList constructors	what if not enough space?
– default	[].add(3) -> [3]
– initial capacity?	[3].add(5) -> [3, 5]
<pre>redirecting to another constructor this(10);</pre>	[3, 5].add(3) -> [3, 5, 3]

class constants
 - what static means

Testing, testing, testing! – a toString method would be useful

The IntList Class instance variables constructors 	 toString method return a Java String of list empty list -> [] 			
– default	• one element -> [12]			
 initial capacity preconditions, exceptions, postconditions, assert meaning of static 	• multiple elements -> [12, 0, 5, 4]			
add method				
get method				
size method				
CS 314 Encapsulation - Implementing Classes 17	CS 314 Encapsulation - Implementing Classes 18			
<pre>Clicker 3 - Timing Experiment Add N elements to an initially empty IntList then call toString. Time both events. How does the time to add compare to the time to complete toString? IntList list = new IntList(); for (int i = 0; i < N; i++) list.add(i); // resize, cap * 2 String s = list.toString(); A. time to add << time for toString() B. time to add < time for toString() C. time to add > time for toString() E. time to add >> time for toString()</pre>	 The IntList Class testing!!! toString "beware the performance of String concatenation" – Joshua Bloch insert method (int pos, int value) remove method (int pos) insertAll method (int pos, IntList other) queens and kings of all the IntLists!!! 			

Clicker Question 4	get and size methods		
What is output by the following code? IntList list list = new IntList(25); System.out.println(list.size()); A. 25 B. 0 C1 D. unknown E. No output due to runtime error. CS 314 Encapsulation Implementing Classes 21	 get access element from list preconditions? [3, 5, 2].get(0) returns 3 [3, 5, 2].get(1) returns 5 size number of elements in the list Do not confuse with the capacity of the internal storage container The array is not the list! [4, 5, 2].size() returns 3 CS314 Encapsulation-Implementing Classes 22		
insert method	Clicker 5		
<pre>* add at someplace besides the end [3, 5].insert(1, 4) -> [3, 4, 5] where what</pre>	<pre>What is output by the following code? IntList list = new IntList(); list.add(3); list.insert(0, 4); // position, value list.insert(1, 1); list.add(5);</pre>		

- [3, 4, 5].insert(0, 4) -> [4, 3, 4, 5]
- preconditions?
- overload add?
- chance for internal loose coupling

```
IntList list = new IntList();
list.add(3);
list.insert(0, 4); // position, value
list.insert(1, 1);
list.add(5);
list.insert(2, 9);
System.out.println(list);
A. [4, 1, 3, 9, 5]
B. [3, 4, 1, 5, 9]
C. [4, 1, 9, 3, 5]
D. [3, 1, 4, 9, 5]
E. Something else
```

remove method	Clicker Question 6
 remove an element from the list based on location [3, 4, 5].remove(0) -> [4, 5] [3, 5, 6, 1, 2].remove(2) -> [3, 5, 1, 2] preconditions? return value? accessor methods, mutator methods, and mutator methods that return a value 	<pre>What is output by the following code? IntList list = new IntList(); list.add(12); list.add(15); list.add(12); list.add(17); list.remove(1); System.out.println(list); A. [15, 17] B. [12, 17] C. [12, 0, 12, 17] D. [12, 12, 17] E. [15, 12, 17]</pre>
CS 314 Encapsulation - Implementing Classes 25	CS 314 Encapsulation - Implementing Classes 26

insertAll method

add all elements of one list to another starting at a specified location

```
[5, 3, 7].insertAll(2, [2, 3]) ->
```

```
[5, 3, 2, 3, 7]
```

The parameter [2, 3] would be unchanged.

- Working with other objects of the same type -this?
 - where is private private?
 - loose coupling vs. performance

- queens and kings of all the IntLists!!! CS 314 Encapsulation - Implementing Classes

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Clicker 7 - InsertAll First Version

What is the order of the first version of InsertAll? Assume both lists have N elements and that the insert position is halfway through the calling list.

- D. O(N)
- E. O(N²)

Class Design and Implementation – Another Example This example will not be covered in class.	<list-item> The Die Class Consider a class used to model a die What is the interface? What actions should a die be able to perform? </list-item>
	The methods or behaviors can be broken up
	into constructors, mutators, accessors
	CS 314 Encapsulation - Implementing Classes 30
The Die Class Interface	
The Die Class Interface	Visibility Modifiers
 Constructors (used in creation of objects) default, single int parameter to specify the 	 All parts of a <i>class</i> have visibility modifiers Java keywords
number of sides, int and boolean to determine if should roll	 public, protected, private, (no modifier means package access) do not use these modifiers on local variables (syntax error)
 Mutators (change state of objects) 	 public means that constructor, method, or field may
– roll	be accessed outside of the class.
Accessors (do not change state of objects)	 part of the interface constructors and methods are generally public
– getResult, getNumSides, toString	• private means that part of the class is hidden and
 Public constants 	inaccessible by code outside of the class
- DEFAULT_SIDES	 part of the implementation data fields are generally private
CS 314 Encapsulation - Implementing Classes 31	CS 314 Encapsulation - Implementing Classes 32

 Implementation method code, ar 	Class Implementation is made up of constructor code and private data members of the	e,		DieTester method	
 private data menoritate data menoritations or la constructors or la constructors Implementation can be changed affecting clients 	embers / instance variables mbers may be used in any of the methods of a class is hidden from users of a class without changing the interface (other classes that use this cla ous version of Die class, a	e or	final final Die d Die d Die d final	<pre>ic void main(String[] args) { l int NUM_ROLLS = 50; l int TEN_SIDED = 10; d1 = new Die(); d2 = new Die(); d3 = new Die(TEN_SIDED); l int MAX_ROLL = d1.getNumSides() + d2.getNumSides() + d3.getNumSides(); int i = 0; i < NUM_ROLLS; i++) d1.roll(); d2.roll();</pre>	
requiring a Die c numbers betwee	completed can be used in any or situation requiring random en 1 and N What does it do?	thing	}	System.out.println("d1: " + d1.getResu + " d2: " + d2.getResult() + " + (d1.getResult() + d2.getResul	Total: "
CS 314 E	Encapsulation - Implementing Classes	33	CS 314	Encapsulation - Implementing Classes	34

DieTester continued

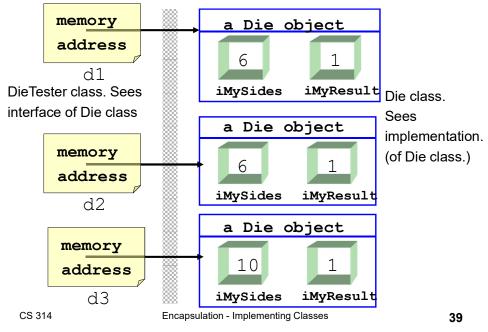
```
int total = 0;
int numRolls = 0;
do
     dl.roll();
{
     d2.roll();
     d3.roll();
     total = d1.getResult() + d2.getResult()
          + d3.getResult();
     numRolls++;
}
while(total != MAX ROLL);
```

Correctness Sidetrack

careful tho you are cr	ating the public interface of a class giv ought and consideration to the <i>contrac</i> reating between yourself and users (or ners) of your class	ct
	<i>onditions</i> to state what you assume to e a method is called	be
 caller of table are true 	the method is responsible for making sure the second second second second second second second second second se	nese
•	conditions to state what you guarantee ter the method is done if the precondit	
	nter of the method is responsible for making se are true	1
CS 314	Encapsulation - Implementing Classes	36

<pre>Precondition and postcondition Example /* pre: numSides > 1 post: getResult() = 1, getNumSides() = sides */ public Die(int numSides) { assert (numSides > 1) : "Violation of precondition: Die(int)"; iMyNumSides = numSides; iMyResult = 1; assert getResult() == 1 && getNumSides() == numSides; }</pre>	 Object Behavior - Instantiation Consider the DieTester class Die d1 = new Die(); Die d2 = new Die(); Die d3 = new Die(10); When the new operator is invoked control is transferred to the Die class and the specified constructor is executed, based on parameter matching Space(memory) is set aside for the new object's fields The memory address of the new object is passed back and stored in the object variable (pointer) After creating the object, methods may be called on it.
CS 314 Encapsulation - Implementing Classes 37	CS 314 Encapsulation - Implementing Classes 38

Creating Dice Objects

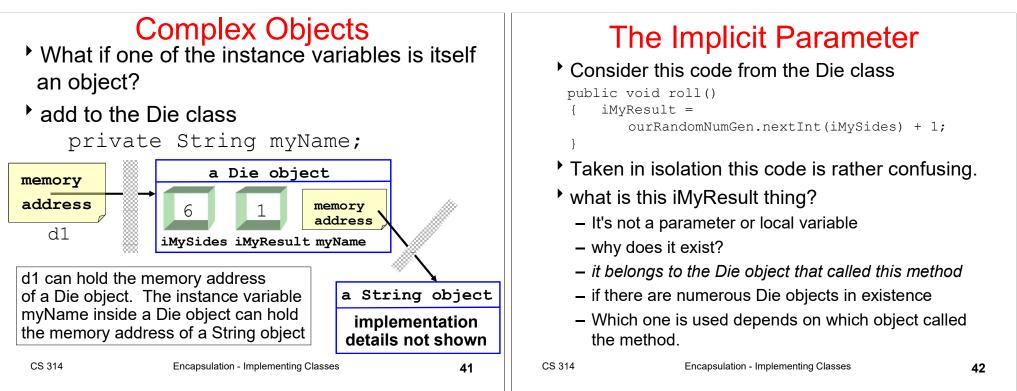


Objects

 Every Die object created has its own instance of the variables declared in the class blueprint

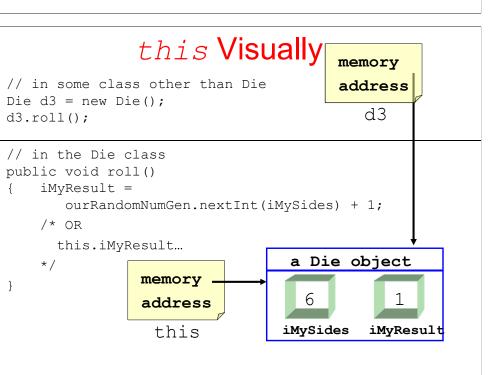
private int iMySides;
private int iMyResult;

- thus the term instance variable
- the instance vars are part of the hidden implementation and may be of any data type
 - unless they are public, which is almost always a bad idea if you follow the tenets of information hiding and encapsulation



The this Keyword

- When a method is called it may be necessary for the calling object to be able to refer to itself
 - most likely so it can pass itself somewhere as a parameter
- when an object calls a method an implicit reference is assigned to the calling object
- the name of this implicit reference is this
- this is a reference to the current calling object and may be used as an object variable (may not declare it)



 working class can write an assume e 	An equals method with objects of the same type of be confusing equals method for the Die cla every Die has a myName ins as well as iMyNumber and iM	e in a	A Possible Equals Method Lic boolean equals (Object otherObject) Die other = (Die)otherObject; return iMySides == other.iMySides && iMyResult== other.iMyResult && myName.equals(other.myName); clared Type of Parameter is Object not Die erride (replace) the equals method instead of erload (present an alternate version) easier to create generic code will see the equals method is <i>inherited</i> from Object class cess to another object's private instance iables?
CS 314	Encapsulation - Implementing Classes	45 CS 314	Encapsulation - Implementing Classes 46
public boole	other equals Method	Free Provide P	A "Perfect" Equals Method om Cay Horstmann's <i>Core Java</i>
1 // aano	rerous! Not checking for null	l or type. public	boolean equals(Object otherObject)
Die oth return &&	<pre>gerous! Not checking for null her = (Die)otherObject; this.iMySides == other.iMySi this.iMyNumber == other.iMy this.myName.equals(other.r</pre>	l or type. public { / i ides yNumber / j myName);	<pre>/ check if objects identical f(this == otherObject) return true; / must return false if explicit parameter null f(otherObject == null) return false;</pre>
Die oth return && && } Using the this key instance variables If a method within	<pre>mer = (Die)otherObject; this.iMySides == other.iMySides this.iMyNumber == other.iMySides this.myName.equals(other.reference to access the implicit participation of the second sec</pre>	l or type. public { / / / / / / / / / / / / / / / / / /	<pre>/ check if objects identical f(this == otherObject) return true; / must return false if explicit parameter null f(otherObject == null)</pre>

the instance of Operator

instanceof is a Java keyword.

part of a boolean statement

```
public boolean equals(Object otherObj)
  if otherObj instanceof Die
{
       //now go and cast
   {
       // rest of equals method
```

- Should not use instanceof in equals methods.
- instanceof has its uses but not in equals because of the contract of the equals method

```
CS 314
```

Encapsulation - Implementing Classes

Class Variables and Class Methods

- Sometimes every object of a class does not need its own copy of a variable or constant
- The keyword static is used to specify class variables, constants, and methods

private static Random ourRandNumGen = new Random(); public static final int DEFAULT SIDES = 6;

- The most prevalent use of static is for class constants.
 - if the value can't be changed why should every object have a copy of this non changing value

```
CS 314
```

Encapsulation - Implementing Classes

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Class Variables and Constants the Die class memory 6 address DEFAULT SIDES ourRandNumGen a Random object All objects of type Die have implementation access to the class variables details not shown and constants. A public class variable or constant may be referred to via the class name.

Syntax for Accessing Class Variables

```
public class UseDieStatic
{ public static void main(String[] args)
      System.out.println( "Die.DEFAULT SIDES "
          + Die.DEFAULT SIDES );
       // Any attempt to access Die.ourRandNumGen
      // would generate a syntax error
      Die d1 = new Die (10);
       System.out.println( "Die.DEFAULT SIDES "
          + Die.DEFAULT SIDES );
       System.out.println( "d1.DEFAULT SIDES "
          + d1.DEFAULT SIDES );
      // regardless of the number of Die objects in
       // existence, there is only one copy of DEFAULT SIDES
       // in the Die class
   } // end of main method
} // end of UseDieStatic class
CS 314
                    Encapsulation - Implementing Classes
```

Static Methods

- static has a somewhat different meaning when used in a method declaration
- static methods may not manipulate any instance variables
- in non static methods, some object invokes the method

d3.roll();

the object that makes the method call is an implicit parameter to the method

Static Methods Continued

- Since there is no implicit object parameter sent to the static method it does not have access to a copy of any objects instance variables
 - unless of course that object is sent as an explicit parameter
- Static methods are normally utility methods or used to manipulate static variables (class variables)
- The Math and System classes are nothing but static methods

```
CS 314 Encapsulation - Implementing Classes 53 CS 314 Encapsulation - Implementing Classes 54
```

static and this

```
 Why does this work (added to Die class)
public class Die
  {
    public void outputSelf()
    { System.out.println( this );
    }
}
```

but this doesn't?

```
public class StaticThis
{
    public static void main(String[] args)
    { System.out.println( this );
    }
}
CS 314 Encapsulation - Implementing Classes 55
```

Topic 4 Inheritance"Question: What is the object oriented way of getting rich?Answer: Inheritance."		 Features of OO Programming Encapsulation abstraction, creating new data types information hiding breaking problem up based on data types Inheritance code reuse specialization "New code using old code."
1	1	CS 314 Inheritance 2

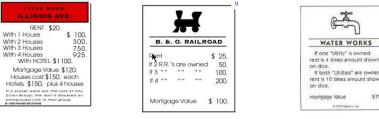
Encapsulation

- Create a program to allow people to play the game Monopoly
 - Create classes for money, dice, players, the bank, the board, chance cards, community chest cards, pieces, etc.
- Some classes use other classes. Are *clients*
 - the board *consists of* spaces
 - a player has properties they own
 - a piece has a position
- Also referred to as composition

Inheritance

Another kind of relationship exists between things in the world and data types in programs

- There are properties in Monopoly
 - a street *is a kind* of property
 - a railroad is a kind of property
 - a utility *is a kind* of property



Inheritance

3

CS 314

Inheritance

 Inheritance In Monopoly there is the concept of a Property All properties have some common traits they have a name they have a position on the board they can be owned by players they have a purchase price But some things are different for each of the three kinds of property determine rent when another player lands on the Property, only Streets can have houses 	 What to Do? If we have a separate class for Street, Railroad, and Utility there is going to be a lot of code copied hard to maintain an anti-pattern Inheritance is a programming feature to allow data types to build on pre-existing data types without repeating code
CS 314 Inheritance 5	CS 314 Inheritance 6
 Mechanics of Inheritance extends keyword inheritance of instance methods inheritance of instance variables object initialization and constructors calling a parent constructor with super() overriding methods partial overriding, super.parentMethod() inheritance requirement in Java the Object class inheritance hierarchies 	 Inheritance in Java Java is designed to encourage object oriented programming all classes, except one, must inherit from exactly one other class The Object class is the cosmic super class The Object class does not inherit from any other class The Object class has several important methods: toString, equals, hashCode, clone, getClass implications: all classes are descendants of Object all classes and thus all objects have a toString, equals, hashCode, clone, and getClass method toString, equals, hashCode, clone normally overridden

Nome	nclature of Inheritance	9	Clicker 1		
In Java the extends keyword is used in the class header to specify which preexisting class a new class is inheriting from public class Student extends Person		What is the primary reason for using inheritance when programming?			
 Person is said to be the parent class of Student the super class of Student the base class of Student an ancestor of Student Student is said to be a child class of Person a sub class of Person a derived class of Person a descendant of Person 		 A. To make a program more complicated B. To copy and paste code between classes C. To reuse pre-existing code D. To hide implementation details of a class E. To ensure pre conditions of methods are met. 			
CS 314	Inheritance	9	CS 314	Inheritance	10
public cla public Fo sy } A. 0 B. null C. Unknown D. No outpur	Clicker 2 out when the main method is run? ss Foo { static void main(String[] args o f1 = new Foo(); stem.out.println(f1.toString()) until code is actually run. t due to a syntax error. t due to a runtime error.	5) {	 any meth overridder same sign may not r may use add more 	Overriding methods od that is not final may n by a descendant class nature as method in ance reduce visibility the original method if sim behavior to existing iginalMethod()	/ be estor
-		• •			12

Constructors

- Constructors handle initialization of objects
- When creating an object with one or more ancestors (every type except Object) a chain of constructor calls takes place
- The reserved word super may be used in a constructor to call a one of the parent's constructors
 - must be first line of constructor
- if no parent constructor is explicitly called the default, 0 parameter constructor of the parent is called
 - if no default constructor exists a syntax error results
- If a parent constructor is called another constructor in the same class may no be called
 - no super();this(); allowed. One or the other, not both

Inheritance

Creating a SortedIntList

- A Cautionary Tale

of Inheritance

- good place for an initialization method

CS 314

The Keyword super

- super is used to access something (any protected or public field or method) from the super class that has been overridden
- Rectangle's toString makes use of the toString in ClosedShape my calling super.toString()
- without the super calling toString would result in infinite recursive calls
- Java does not allow nested supers super.super.toString()

results in a syntax error even though technically this refers to a valid method, Object's toString

Rectangle partially overrides ClosedShapes toString

13

Inheritance

14

A New Class

Assume we want to have a list of ints, but that the ints must always be maintained in ascending order

```
[-7, 12, 37, 212, 212, 313, 313, 500]
sortedList.get(0) returns the min
sortedList.get(list.size() - 1)
returns the max
```

Inheritance

<pre>Implementing SortedIntList Do we have to write a whole new class? Assume we have an IntList class. Clicker 3 - Which of the following methods have to be changed? A. add(int value) B. int get(int location) C. String toString() D. int remove(int location)</pre>	 Overriding the add Method First attempt Problem? solving with insert method double edged sort solving with protected What protected really means
E. More than one of A - D. CS 314 Inheritance 17	CS 314 Inheritance 18
Clicker 4 public class IntList { private int size private int[] con } public class SortedIntList extends IntList { public SortedIntList() { System.out.println(size); // Output? } } A. 0 B. null C. unknown until code is run D. no output due to a compile error E. no output due to a runtime error 19	 Problems • What about this method? void insert(int location, int val) • What about this method? void insertAll(int location, IntList otherList) • SortedIntList is not a good application of inheritance given all the behaviors IntList provides.

				Simple Code Example	
	ore Example Code	es.	- wh - wh - ad - ov • Crea - ad - de - try - co	te a class named Shape hat class does Shape inherit from hat methods can we call on Shape objects? d instance variables for a position <i>erride</i> the toString method te a Circle class that extends Shape d instance variable for radius bug and look at contents to access instance var from Shape instructor calls e of key word <i>super</i>	
CS 314	Inheritance	21	CS 314	Inheritance	22
<pre>- assume a - override C • Possible s - Rectang: - Circle - Ellipse - Square • Possible h</pre>		nates g .pe		<pre>A ClosedShape { private double myX; private double myY; public ClosedShape() { this(0,0); } public ClosedShape (double x, double y) { myX = x; myY = y; } public String toString() { return "x: " + getX() + " y: " + getY(); public double getX() { return myX; } public double getY() { return myY; } Other methods not shown</pre>	}

```
A Rectangle Class
        A Rectangle Constructor
                                                                        public class Rectangle extends ClosedShape {
                                                                          private double myWidth;
public class Rectangle extends ClosedShape {
                                                                          private double myHeight;
   private double myWidth;
                                                                          public Rectangle() {
   private double myHeight;
                                                                             this(0, 0);
   public Rectangle ( double x, double y,
                                                                          public Rectangle(double width, double height) {
            double width, double height ) {
                                                                             myWidth = width;
                                                                             myHeight = height;
         super(x, v);
        // calls the 2 double constructor in
                                                                          public Rectangle(double x, double y,
        // ClosedShape
                                                                                    double width, double height) {
        myWidth = width;
                                                                              super(x, y);
                                                                              myWidth = width;
        myHeight = height;
                                                                              myHeight = height;
   }
                                                                          public String toString() {
                                                                             return super.toString() + " width " + myWidth
                                                                               + " height " + myHeight;
     // other methods not shown
}
  CS 314
                           Inheritance
                                                                  CS 314
                                                                                          Inheritance
                                                        25
                                                                                                                       26
```

Initialization method

```
public class Rectangle extends ClosedShape {
        private double myWidth;
        private double myHeight;
        public Rectangle() {
           init(0, 0);
        public Rectangle(double width, double height) {
            init(width, height);
        }
        public Rectangle (double x, double y,
                   double width, double height) {
           super(x, y);
           init(width, height);
        private void init(double width, double height) {
           myWidth = width;
           myHeight = height;
CS 314
                           Inheritance
```

Result of Inheritance

Do any of these cause a syntax error? What is the output?

```
Rectangle r = new Rectangle(1, 2, 3, 4);
ClosedShape s = new CloseShape(2, 3);
System.out.println(s.getX());
System.out.println(s.toString());
System.out.println(r.getX());
System.out.println(r.getY());
System.out.println(r.toString());
System.out.println(r.toString());
```

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Inheritance

	The Real Picture	_	Access Modifiers and	
ć	Fields from Object class		Inheritance	
	Instance variables declared in Object		 public – accessible to all classes 	
A	Fields from ClosedShape class		 private – accessible only within that class. Hidden from all sub 	
Rectangle object	Instance Variables declared in ClosedShape		 classes. protected accessible by classes within the same package and all 	
Available methods	Fields from Rectangle class		 descendant classes Instance variables are <i>typically</i> private 	
are all methods from Object, ClosedShape, and Rectangle	Instance Variables declared in Rectangle		 protected methods are used to allow descendant classes to modify instance variables in ways other classes can't 	
CS 314	Inheritance	29	CS 314 Inheritance 3	30

Why private Vars and not protected?

In general it is good pr	actice to make
instance variables priva	ate

- hide them from your descendants
- if you think descendants will need to access them or modify them provide protected methods to do this
- Why?
- Consider the following example

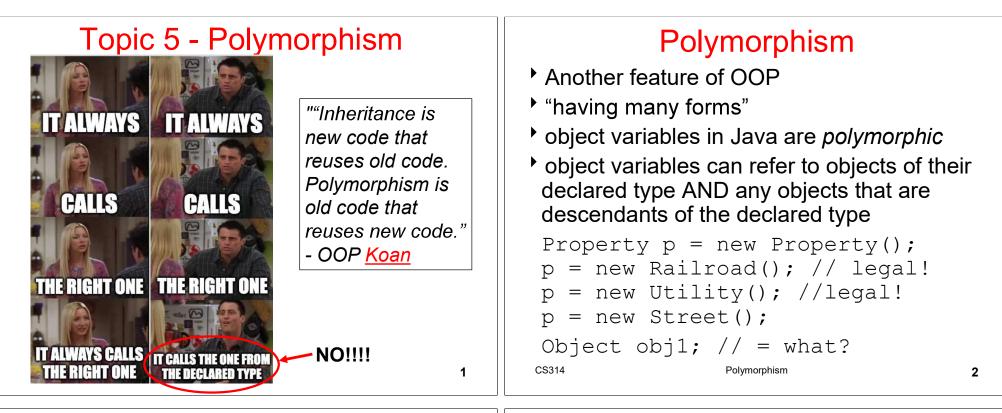
Required update

public class GamePiece { private Board myBoard; private Position myPos;

// whenever my position changes I must
// update the board so it knows about the change

```
protected void alterPos(Position newPos) {
    Position oldPos = myPos;
    myPos = newPos;
    myBoard.update(oldPos, myPos);
}
```

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Data Type

object variables and objects:

- <u>declared type</u>. Also called the static type.
- <u>dynamic type</u>. What is the actual type of the object the variable is referring to at run time or when a particular statement is executed.
- Method calls are syntactically legal if the method is in the declared type <u>or any</u> <u>ancestor</u> of the declared type

The actual method that is executed at runtime is based on the dynamic type

- dynamic dispatch

Clicker Question 1

Consider the following class declarations:

```
public class BoardSpace
public class Property extends BoardSpace
public class Street extends Property
public class Railroad extends Property
```

Which of the following statements would cause a syntax error? (Assume all classes have a zero argument constructor.)

- A.Object obj = new Railroad();
- B.Street s = new BoardSpace();
- C.BoardSpace b = new Street();
- **D**.Railroad r = new Street();
- E. More than one of these

3

Meth	nod LookUp	Clicker	Question 2
 class of the declared to - if it finds it great, if not generating the method was needed to and the method was needed to the method was needed. To determine which method was needed. To determine which method was needed. starts with the actual run method. search the class for the method. if found, execute it, other repeat until a version is 	t method erwise go to the super class and look there of is found, or the Object class is reached ever found. (Compile error) ethod is actually executed the run the run the class of the object that is calling the t method	What is output by the code to the right when run? A. !!live B. !eggegg C. !egglive D. !!! E. Something else	<pre>public class Animal { public String bt() { return "!"; } } public class Mammal extends Animal { public String bt() { return "live"; } } public class Platypus extends Mammal { public String bt() { return "egg"; } } Animal a1 = new Animal(); Animal a2 = new Platypus(); Mammal m1 = new Platypus(); System.out.print(a1.bt()); System.out.print(a2.bt()); System.out.print(m1.bt());</pre>
CS314	Polymorphism 5	CS314 P	olymorphism 6
Clicke What is output by the code to the right when run? Think carefully about the dynamic type. A. MeowWoof B. MeowEm C. EmWoof D. EmEm E. Something else	<pre>public class Animal { public void show() { System.out.print(this.speak()); } public String speak() { return "Em"; } } public class Dog extends Animal { public String speak() { return "Woof"; } } public class Cat extends Animal { public void show(int x) { System.out.print("Meow"); } } Cat patches = new Cat(); Dog velvet = new Dog(); patches.show(); </pre>	 Inheritance allows relationships in the – if the program follow to write Inheritance allows – complete programs large programs) Polymorphism allow in another way Inheritance and po programmers to create 	real world ws the model it may be easier code reuse faster (especially ws code reuse lymorphism allow eate <i>generic algorithms</i>
	velvet.show();	CS314 P	olymorphism 8

 code reus developm If a algoricode would genericity code to e in Java, to e 	ithm is essentially the same Ild vary based on the data ty allows only a single version xist here are 2 ways of doing th orphism and the inheritance req	ogram e, but the ype n of that iis		A Generic List Class	
CS314	Polymorphism	9	CS314	Polymorphism	10
	Back to IntList			Generic List Class	
want a Lis Lists? – What if I Are the L storing St	find IntList useful, but we st of Strings? Rectangle am not sure? ist algorithms different if I a trings instead of ints? we make a generic List class	es? m	– why?!? – A good necess ▶ What ca	es toString have to change	
CS314	Polymorphism	11	CS314	Polymorphism	12

Clicker 4

After altering the data type of the elements to Object in our list class, how many lines of code in the toString method, originally from the IntList class, need to be changed?

A. 0 B. 1 C. 2 D. 3 E. >= 4	need to be changed?		Because public vo if(a Sys	is olean equals(List o id foo(List a, Object .equals(b)) stem.out.println(same s really a List?	b)
CS314	Polymorphism	13	CS314	Polymorphism	14

equals method

- read the javadoc carefully!
- Must handle null
- Parameter must be Object
 - otherwise overloading instead of overriding
 - causes
- must handle cases when parameter is not same data type as calling object
 - instanceof or getClass()
- don't rely on toString and then String's
 equals (efficiency)
 CS314
 Polymorphism
 15

Writing an equals Method

3
How to check if two objects are equal?
if(objA == objA)
// does this work?
Why not this
public boolean equals(List other)
Because
public void foo(List a, Object b)
if(a.equals(b))
System.out.println(same)
- what if b is really a List?
CS314 Polymorphism 14
the createASet example
<pre>public Object[] createASet(Object[] items) {</pre>
pre: items != null, no elements

pre: items != null, no elements
of items = null
post: return an array of Objects
that represents a set of the elements
in items. (all duplicates removed)
*/

 $\{5, 1, 2, 3, 2, 3, 1, 5\} \rightarrow \{5, 1, 2, 3\}$

Polymorphism

createASet examples

CS314

Polymorphism

Topic 6 Generic Type Parameters

"Get your data structures correct first, and the rest of the program will write itself."

- David Jones

Back to our Array Based List

- Started with a list of ints
- Don't want to have to write a new list class for every data type we want to store in lists
- Moved to an array of Objects to store the elements of the list

```
// from array based list
private Object[] con;
```

relatively straight forward

some difficulties

- Type checking

- Casting

CS314

Generics

Difficulties with Object

Using these generic data structrues leads to

Creating generic data structures using the

Object data type and polymorphism is

Code examples on the following slides

Using Object

- In Java, all classes inherit from exactly one other class except Object which is at the top of the class hierarchy
 - therefore all classes are descendants of Object
- object variables can refer to objects of their declared type and any descendants

- polymorphism

- Thus, if the internal storage container is of type Object it can hold anything
 - primitives handled by *wrapping* them in objects.
 int Integer, char Character

CS314

3

CS314

Generics

Clicker 1

Code Example – type checking

//pre: all elements of li are Monopoly Properties

}

CS314

<pre>> What is output by the following code? GenericList list = new GenericList(); // 1 Street s = new Street("Boardwalk", 400, Color.BLUE); list.add(s); // 2 System.out.print(list.get(0).getPrice());// 3 A. 400</pre>	• Ass G(1: S) //
 A. 400 B. No output due to syntax error at line // 1 C. No output due to syntax error at line // 2 D. No output due to syntax error at line // 3 E. No output due to runtime error. CS314 Generics 5 	/ , / , S / , CS314

Code Example - Casting

sume a list class

```
GenericList li = new GenericList();
i.add("Hi");
System.out.println(li.get(0).charAt(0));
/ previous line has syntax error
/ return type of get is Object
/ Object does not have a charAt method
/ compiler relies on declared type
System.out.println(
     ((String) li.get(0)).charAt(0) );
/ must cast to a String
```

Generics

6

"Fixing" the Method

//pre: all elements of li are Monopoly Properties

```
public void printPrices(GenericList li) {
                                                       public void printPrices(GenericList li) {
     for (int i = 0; i < li.size(); i++) {</pre>
                                                             for(int i = 0; i < li.size(); i++) {</pre>
          Property temp = (Property) li.get(i);
                                                                  // GACK!!!!
          System.out.println(temp.getPrice());
                                                                  if (li.get(i) instanceof Property) {
                                                                    Property temp = (Property) li.get(i);
                                                                    System.out.println(temp.getPrice());
// what happens if pre condition not met?
                                                         CS314
                        Generics
                                                 7
                                                                               Generics
                                                                                                        8
```

Clicker 2 - Too Generic?

Does this code compile?

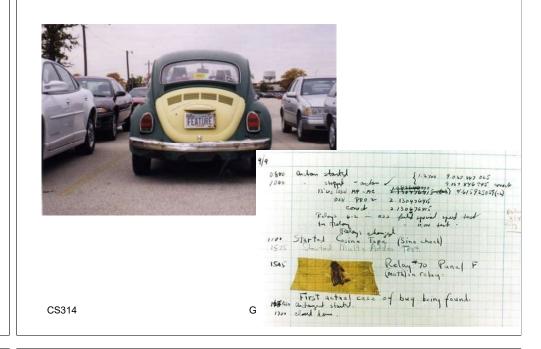
GenericList list = new GenericList(); list.add("Olivia"); list.add(Integer.valueOf(12)); list.add(12); // autobox aka autowrap list.add(new Rectangle(1, 2, 3, 4)); list.add(new GenericList());

A. No

CS314

B. Yes

Is this a bug or a feature?



Generic Types

Generics

- Java has syntax for parameterized data types
- Referred to as *Generic Types* in most of the literature
- A traditional parameter has a data type and can store various values just like a variable

public void foo(int x)

- Generic Types are *like* parameters, but the data type for the parameter is *data type*
 - like a variable that stores a data type
- <u>this is an abstraction</u>. Actually, all data type info is erased at compile time and replaced with casts and, typically, variables of type Object
 CS314 Generics

Making our Array List Generic

Data type variables declared in class header

public class GenericList<E> {

- The <E> is the declaration of a data type parameter for the class
 - any legal identifier: Foo, AnyType, Element, DataTypeThisListStores
 - Java style guide recommends terse identifiers
- The value E stores will be filled in whenever a programmer creates a new GenericList

GenericList<String> li =

new GenericList<>();

9

11

Generics

<pre>Modifications to GenericList instance variable private E[] myCon; Parameters on _ add, insert, remove, insertAll, mayber contains? Return type on get(int index)</pre>	 Modifications to GenericList Careful with the equals method Recall type information is actually erased at compile time. At runtime not sure what data type of elements are. (Unless we get into reflection.) use of wildcard
 Changes to creation of internal storage container myCon = (E[]) new Object[DEFAULT_SIZE]; Equals method. Careful, do not make unsafe cast 	rely on the elements equals methods
CS314 Generics 13	CS314 Generics 14
<pre>Using Generic Types Back to Java's ArrayList ArrayList list1 = new ArrayList(); - still allowed, a "raw" ArrayList - works just like our first pass at GenericList - casting, lack of type safety</pre>	<pre>Using Generic Types ArrayList<string> list2 = new ArrayList<string>(); - for list2 E stores String list2.add("Isabelle"); System.out.println(list2.get(0).charAt(2)); //ok list2.add(new Rectangle());</string></string></pre>
	// syntax error

Parameters and Generic T	ypes	Gene	eric Types and Subclas	ses
Old version		ArrayList	<shape> list5 =</shape>	
<pre>//pre: all elements of li are Strings</pre>	3		new ArrayList <shape>();</shape>	
public void printFirstChar(ArrayList	li){	list5.add	l(new Rectangle());	
New version		list5.add	d(new Square());	
//pre: none		list5.add	l(new Circle());	
<pre>public void printFirstChar(ArrayList<string></string></pre>	· li){	// all ok	cay	
<pre> Elsewhere ArrayList<string> list3 = new ArrayList<stri);="" arraylist<integer="" list3="" ok="" printfirstchar(=""> list4 = new ArrayList<int);="" error<="" list4="" pre="" printfirstchar(="" syntax=""></int></stri></string></pre>			an store Shape objects and any ants of Shape	
CS314 Generics	17	CS314	Generics	18

Topic 7 Interfaces



I once attended a Java user group meeting where James Gosling (one of Java's creators) was the featured speaker. During the memorable Q&A session, someone asked him: "If you could do Java over again, what would you change?" "I'd leave out classes," he replied. After the laughter died down, he explained that the real problem wasn't classes per se, but rather implementation inheritance (the extends relationship). Interface inheritance (the implements relationship) is preferable.

- Allen Holub



Clicker 1

How many sorts do you want to have to write?

```
public static void selSort(double[] data) {
   for (int i = 0; i < data.length; i++) {
      int small = i;
      for(int j = i + 1; j < data.length; j++) {
         if (data[j] < data[small])</pre>
             small = j;
      double temp = data[i];
                                          A. 0
      data[i] = data[small];
                                          B. 1
      data[small] = temp;
                                          C. 2
                                          D. 3
                                          F_{>}=4
 CS314
                       Interfaces
```

Why interfaces?

- Interfaces allow the creation of abstract types
 - "A set of data values and associated operations that are precisely specified independent of any particular implementation."
 - multiple implementations allowed
- Interfaces allow a data type to be specified without worrying about the implementation
 - do design first
 - What will this data type do?
 - Don't worry about implementation until design is done.
 - separation of concerns.
 - allow us to create generic algorithms

CS314

Interfaces

3

Interfaces

public interface List<E> {

- No constructors
- No instance variables
- b abstract instance methods
 public void add(E val);
- default instance methods
- static methods
- class constants (prefer enums)
 public static final int DEFAULT_CAP = 10;
- an interface can (but does not have to) extends other interfaces

 In Java, a cla one other cla A class can im public class Serializabl A class that provide imple method decla or the class r interfaces ca 	<i>plement</i> as many interface ArrayList implement	xactly es as it likes as List, e must lefault	 The Java contains a – names a class lis One of th 	a number of interfaces	boPopup M_FAILURE ment unicationException parable parater pilationMXBean
CS314	Interfaces	5	CS314	Interfaces	6
Cor	nparable Interface			Interfaces	
public } • compareTo mu – an int <0 if the	terface Comparable <t> ic int compareTo(T ot) st return calling object is less than the p</t>	ner);	methods use." (In – Anthony	erfaces to ensure a class ha that other classes or meth other words, clients of you v, Spring 2013 r classes or methods may	nods will r class.)
parameter othe	calling object is greater than th er should be <i>consistent wit</i>		type for th POLYMC	r methods or classes use i ne parameters of methods ORPHISM e using new code	
CS314	Interfaces	7	CS314	Interfaces	8

<pre>Clicker Question 2 • What is output by the following code? Comparable c1 = new Comparable(); Comparable c2 = new Comparable(); System.out.println(c1.compareTo(c2)); A. A value < 0 B. 0 C. A value < 0 D. Unknown until program run E. Compile error</pre>			 Example compareTo Suppose we have a class to model playing cards Ace of Spades, King of Hearts, Two of Clubs each card has a suit and a value, represented by ints this version of compareTo will compare values first and then break ties with suits 		
CS314	Interfaces	9	CS314	Interfaces	10
public class public } // oth } Assume ints	areTo in a Card c s Card implements Comparable : int compareTo(Card otherCar return this.rank - other.ran er methods not shown for ranks (2, 3, 4, 5, 6,) and amonds, 2 is hearts, 3 is spade	<card> { rd) { k; suits (0 is</card>	 Interface for object Can't sin Can refe interface Assume C Card c Compara 	aces and Polymo s may be used as the variables hply create objects of t r to any objects that im or descendants ard implements Compar = new Card(); ble comp1 = new ble comp2 = c;	data type hat type plement the able
CS314	Interfaces	11	CS314	Interfaces	12

Clicker Question 3	Why Make More Work?
Which of the following lines of code causes a syntax error?	 Why bother implementing an interface such as Comparable objects can use method that expect an interface type
Comparable c1; // A c1 = "Ann"; // B Comparable c2 = "Kelly"; // C int x = c2.compareTo(c1); // D // E No syntax errors.	 Example if I implement Comparable: Arrays.sort(Object[] a) public static void sort(Object[] a) All elements in the array must implement the Comparable interface. Furthermore, all elements in the array must be <i>mutually comparable</i>
<pre>// what is x after statement?</pre>	• objects of my type can be stored in data structures that accept Comparables
CS314 Interfaces 13	CS314 Interfaces 14
A List Interface	List Interface
 What if we wanted to specify the operations for a List, but no implementation? Allow for multiple, different implementations. Provides a way of creating <i>abstractions</i>. a central idea of computer science and programming. specify "what" without specifying "how" "Abstraction is a mechanism and practice to reduce and factor out details so that one can focus on a few concepts at a time. " 	<pre>public interface List <e> { public void add(E val); public int size(); public E get(int location); public void insert(int location, E val); public E remove(int location); }</e></pre>

15

One Sort

```
public static void sort(Comparable[] data) {
   final int LIMIT = data.length - 1;
   for(int i = 0; i < LIMIT; i++) {</pre>
      int small = i;
      for(int j = i + 1; j < data.length; j++) {
          int d = data[j].compareTo(data[small]);
          if (d < 0)
             small = j;
      }
      Comparable temp = data[i];
      data[i] = data[small];
      data[small] = temp;
   } // end of i loop
}
  CS314
                                                17
                        Interfaces
```

Topic 8 Iterators

"First things first, but not necessarily in that order "

-Dr. Who



Iterator Interface

- An iterator object is a "one shot" object
 - it is designed to go through all the elements of a Collection once
 - if you want to go through the elements of a Collection again you have to get another iterator object
- Iterators are obtained by calling a method from the Collection





Iterators

- ArrayList is part of the Java Collections Framework
- Collection is an interface that specifies the basic operations every collection (data structure) shall have
- Some Collections don't have a definite order – Sets, Maps, Graphs
- How to access all the items in a Collection with no specified order?

CS314

Iterators

2

Iterator Iterface Methods

The Iterator interface 3 methods we will use: boolean hasNext() //returns true if this iteration has more elements

E next()

//returns the next element in this iteration
//pre: hastNext()

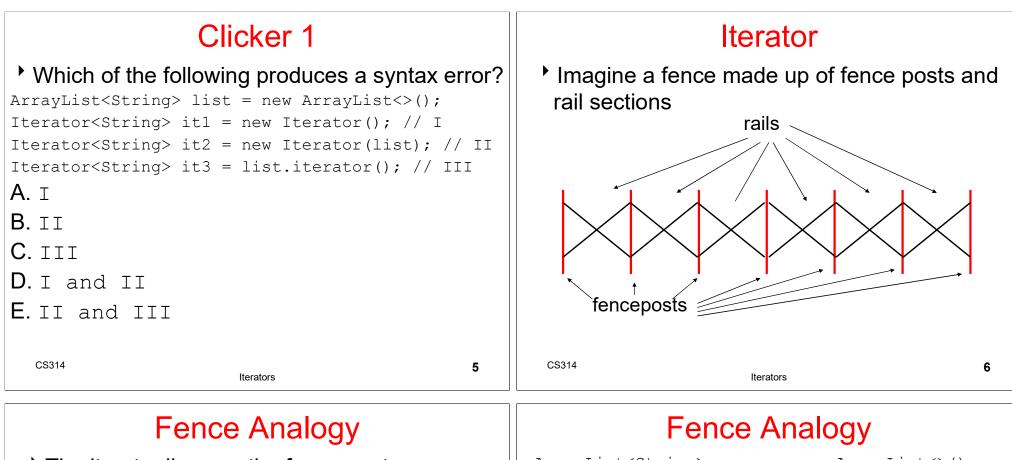
void remove()

/*Removes from the underlying collection the last element returned by the iterator.

pre: This method can be called only once per call to next. After calling, must call next again before calling remove again.

ł

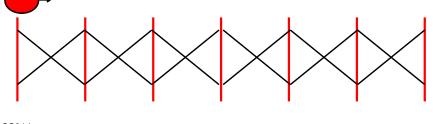
CS314



7

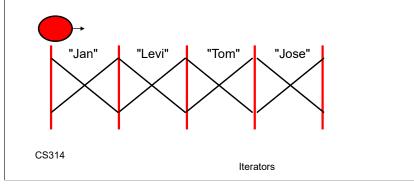
The iterator lives on the fence posts

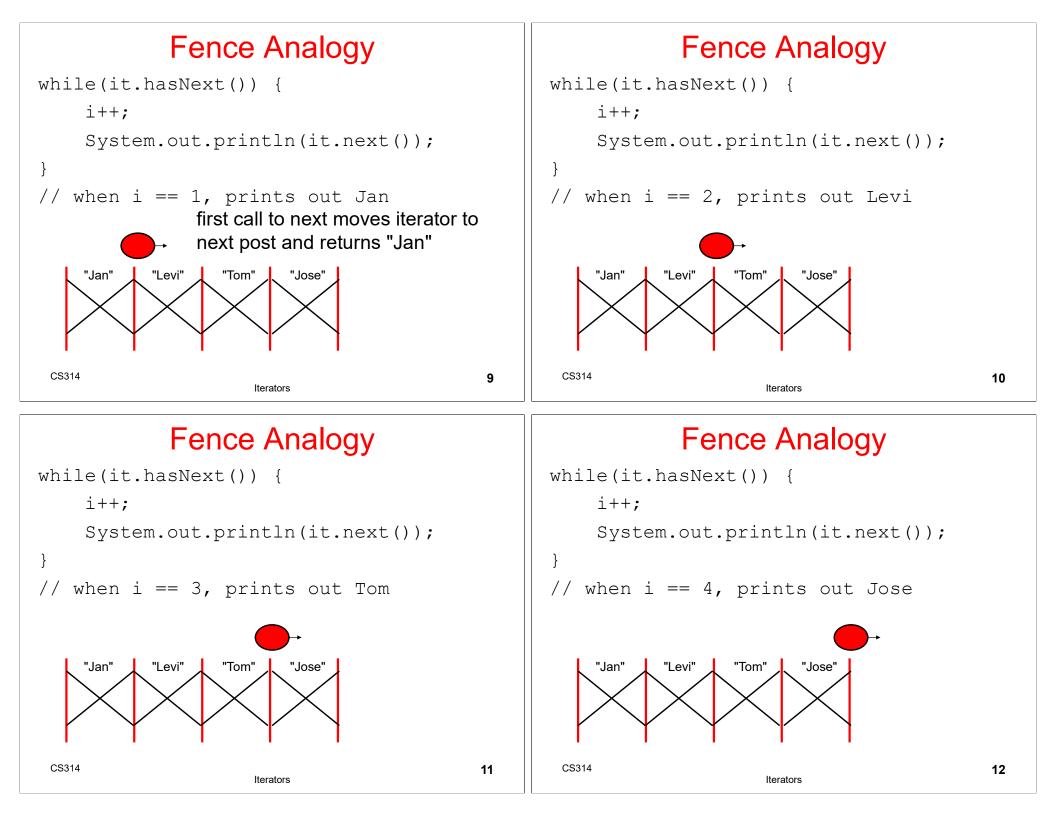
- The data in the collection are the rails
- Iterator created at the far left post
- As long as a rail exists to the right of the Iterator, hasNext() is true iterator object

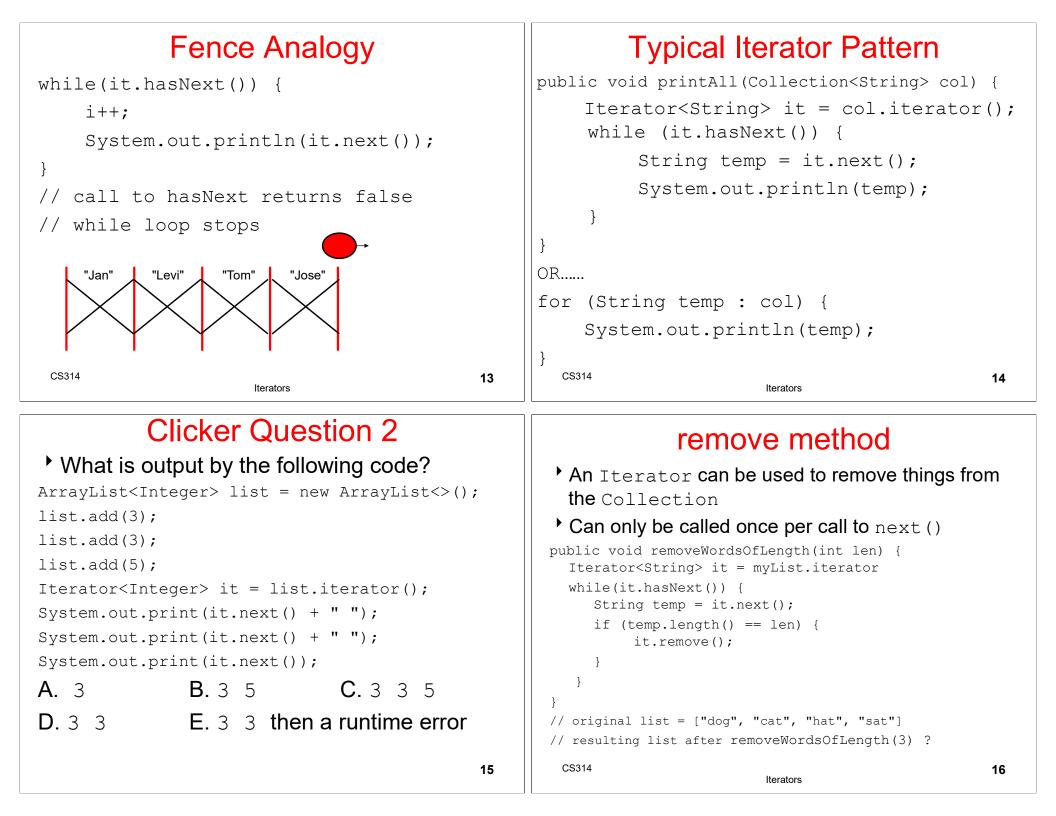


Iterators

ArrayList<String> names = new ArrayList<>(); names.add("Jan"); names.add("Levi"); names.add("Tom"); names.add("Jose"); Iterator<String> it = names.iterator(); int i = 0;







Clicker 3

The Iterable Interface

- A related interface is Iterable
- > The method of interest to us in the interface: public Iterator<T> iterator()
- Why?
- Anything that implements the Iterable interface can be used in the for each loop.

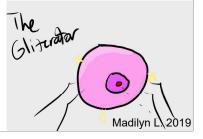
```
ArrayList<Integer> list;
//code to create and fill list
int total = 0;
for (int x : list) {
    total += x;
}
CS314
```

Iterable

- If you simply want to go through all the elements of a Collection (or Iterable thing) use the for each loop
 - hides creation of the Iterator

Implementing an Iterator

- Implement an Iterator for our GenericList class
 - Nested Classes
 - Inner Classes
 - Example of encapsulation
 - checking precondition on remove
 - does our GenricList need an Iterator?



18

19

CS314

Iterators

Comodification

If a Collection (ArrayList) is changed while an iteration via an iterator is in progress an Exception will be thrown the next time the next() or remove() methods are called via the iterator

```
ArrayList<String> names = new ArrayList<>();
names.add("Jan");
Iterator<String> it = names.iterator();
```

```
names.add("Andy");
```

```
it.next(); // exception occurs here
```

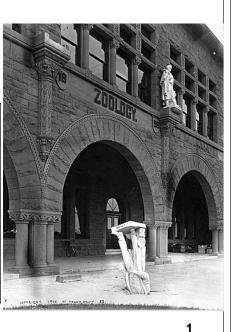
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Iterators

Topic 9 Abstract Classes

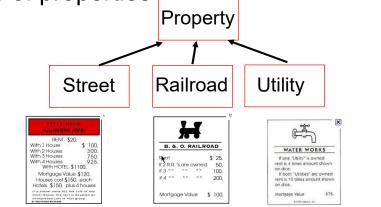
"I prefer Agassiz in the abstract, rather than in the concrete."

 Statue of Biologist Louis Agassiz that fell from a ledge on the Stanford Quad during the 1906 San Francisco earthquake.



Back to the Monopoly Property Example

- There are properties on a monopoly board
- Railroads, Utilities, and Streets are kinds of properties



A getRent Behavior

- One behavior we want in Property is the getRent method
- problem: How do I get the rent of something that is "just a Property"?

The Property class

```
public class Property {
    private int cost;
    private String name;
    public int getRent() {
        return hmmmmm?????;
    }
```

Doesn't seem like we have enough information to get the rent if all we know is it is a Property.

Abstract Classes

3

 Potential Solutions Just leave it for the sub classes. Have each sub class define getRent() Define getRent() in Property and simply return -1. Sub classes override the method with more meaningful behavior. 	<pre>Leave it to the Sub - Classes // no getRent() in Property // Railroad and Utility DO have getRent() methods public void printRents(Property[] props) { for (Property p : props) System.out.println(p.getRent()); } Property[] props = new Property[2]; props[0] = new Railroad("NP", 200, 1); props[1] = new Utility("Electric", 150, false); printRents(props); Clicker 1 - What is result of above code? A. 200150 B. different every time C. Syntax error D. Class Cast Exception E. Null Pointer Exception</pre>	
CS314 Abstract Classes 5	CS314 Abstract Classes 6	
<pre>"Fix" by Casting // no getRent() in Property public void printRents(Property[] props) { for (Property p : props) { if (p instanceof Railroad) System.out.println(((Railroad) p).getRent()); else if (p instanceof Utility) System.out.println(((Utility) p).getRent()); else if (p instanceof Street) System.out.println(((Street) p).getRent()) } // GACK!!!! } Property[] props= new Property[2]; props[0] = new Railroad("NP", 200, 1); props[1] = new Utility("Electric", 150, false); printRents(props); What happens as we add more sub classes of Property?</pre>	<pre>Fix with Placeholder Return // getRent() in Property returns -1 public void printRents(Property[] props) { for (Property p : props) System.out.println(p.getRent()); } Property[] props= new Property[2]; props[0] = new Railroad("NP", 200, 1); props[1] = new Utility("Electric", 150, false); printRents(props); What happens if sub classes don't override getRent()? Is that a good answer?</pre>	
What happens if one of the objects is just a Property?CS314Abstract Classes7	CS314 Abstract Classes 8	

	A Better Fix		Mak	king getRent Abstr	act
 We know we want to be able to get the rent of objects that are instances of Property The problem is we don't know how to do that if all we know is it a Property Make getRent an abstract method Java keyword 			<pre>public class Property { private int cost; private String name; public abstract int getRent(); // I know I want it. // Just don't know how, yet</pre>		
CS314	Abstract Classes	9	an undefine	at are declared abstract have d behavior. nult methods in a Java interfa Abstract Classes	·
Proble	ms with Abstract Met	hods		efined Behavior = to have undefined behav	
what is wi Propert	<pre>tRent() is now an abstract n rong with the following code? y p = new Property(); out.println(p.getRent())</pre>		 If a class the class r 	has 1 or more abstract m must also be declared ab of Property shown would ca	nethods, ostract.
bybcem.	ouc · pr micrii (p · ge citerie (/ / /			

- Even if a class has zero abstract methods a programmer can still choose to make it abstract
 - if it models some abstract thing
 - is there anything that is just a "Mammal"?

If things can go wrong with a tool, provide safeguards to prevent that from happening.

Abstract Classes Safety	Abstract Classes
 A class with one or more abstract methods must be declared abstract. Syntax error if not done. Can still decide to make class abstract even if no abstract methods. 	<pre>public abstract class Property { private int cost; private String name; public abstract double getRent(); // I know I want it.</pre>
 2. Objects of an abstract type cannot be instantiated. Just like interfaces Can still declare variables of this type 	<pre>// Just don't know how, yet } // Other methods not shown</pre>
 A subclass must implement all inherited abstract methods or be abstract itself. 	<pre>if a class is abstract the compiler will not allow constructors of that class to be called Property s = new Property(1, 2); //syntax error</pre>
CS314 Abstract Classes 13	CS314 Abstract Classes 14

Abstract Classes

- In other words you can't create instances of objects where the lowest or most specific class type is an abstract class
- Prevents having an object with an undefined behavior
- Why would you still want to have constructors in an abstract class?
- Object variables of classes that are abstract types may still be declared

```
Property p; //okay
```

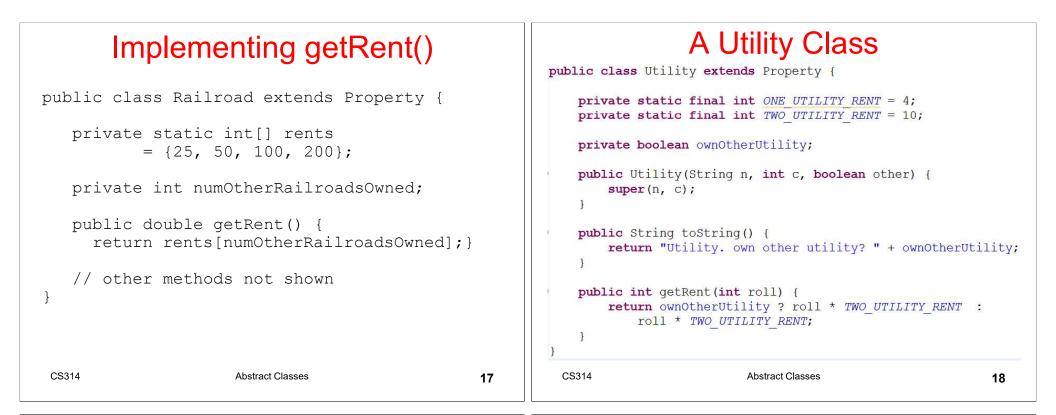
CS314

15

Abstract Classes

Sub Classes of Abstract Classes

- Classes that extend an abstract class must provided a working version of any and all abstract methods from the parent class
 - or they must be declared to be abstract as well
 - could still decide to keep a class abstract regardless of status of abstract methods



Polymorphism in Action

// getRent() in Property is abstract

```
public void printRents(Property[] props) {
    for (Property p : props)
        System.out.println(p.getRent());
```

- Add the Street class. What needs to change in printRents method?
- Inheritance is can be described as new code using old code.
- Koan of Polymorphism: Polymorphism can be described as old code reusing new code.

Comparable in Property

CS314

Abstract Classes

public E get(int location);	<i>mentation</i> interface
<pre>public E remove(int location); public boolean contains(E value); public void addAll(IList<e> other); public boolean containsAll(IList<e> other); for</e></e></pre>	boolean contains(E val) { (E e : this) if val.equals(e) return true;

Topic 10 Using Maps

"He's off the map!"

-Stan (Mark Ruffalo) *Eternal Sunshine of the Spotless Mind*



Data Structures

- More than arrays and lists
- Write a program to determine the frequency of all the "words" in a file.

CS	314	

Maps

2

Performance using ArrayList

Title	Size (kb)	Total Words	Distinct Words	Time (sec)
small sample	0.6	89	25	0.001
2BR02B	34	5,638	1,975	0.051
Alice in Wonderland	120	29,460	6,017	0.741
Adventures of Sherlock Holmes	581	107,533	15,213	4.144
2008 CIA Factbook	10,030	1,330,100	74,042	173.000

Order?

Express change of value as factor of previous file

Title	Size	Total Words	Distinct Words	Time
small sample	0.6	89	25	0.001
2BR02B	57x	63x	79x	51x
Alice in Wonderland	3.5x	5.2x	3.0x	14.5x
Adventures of Sherlock Holmes	4.8x	3.7x	2.5x	6.0x
2008 CIA Factbook	17x	12.3x	5x	42x

O(Total Words * Distinct Words) ??

CS 314

Maps

with 1,330, distinct wor	Clicker 1 econds for the 2008 CIA 100 total words and 74, ds, how long for 1,000x 100x distinct words?	042		Why So Slow?? ntains method for an array base oolean indexOf(Object o	
A. an hour B. a day C. a week D. a month E. half a year					
CS 314	Maps	5	CS 314	Maps	6

A Faster Way - Maps

- Also known as:
 - table, search table, dictionary, associative array, or associative container
- A data structure optimized for a very specific kind of search / access
- In a map we access by asking "give me the value associated with this key."

Keys and Values

Dictionary Analogy:



- The key in a dictionary is a word: foo
- The value in a dictionary is the definition: First on the standard list of metasyntactic variables used in syntax examples
- A key and its associated value form a pair that is stored in a map
- To retrieve a value the key for that value must be supplied
 - A List can be viewed as a Map with integer keys

7

 More on Keys and Values Keys must be unique, meaning a given key can only represent one value but one value may be represented by multiple keys like synonyms in the dictionary. Example: factor: n.See coefficient of X factor is a key associated with the same value (definition) as the key coefficient of X 		A. No B. Yes C. It Depen	ds		
CS 314	Maps	9	CS 314	Maps	10
MovieCharacterWizard of OzDorotWizard of OzDorotMan,Iron ManTonyCoulsPride andElizatPrejudiceMr. DaThe AvengersTony SRogersSense andElinor	g, List <string>> hy, Toto, Scarecrow, Cowardly Lion Stark, Pepper Potts, F on, Obadiah Stane eth Bennet, Jane Be arcy, Mr. Bingley tark, Pepper Potts, Stev s, Bruce Banner, Phil Co Dashwood, Marianne ood, Edward Ferrars, Jo</string>	Fin Phil nnet, re bulson	 void clea Removes a boolean Returns truspecified ka boolean Returns truspecified va Set<k> ka</k> 	all mappings from this map (option containsKey (Object key le if this map contains a mapping ey. containsValue (Object le if this map maps one or more ke alue.	nal operation). y) for the value) eys to the

The Map Interface Continued		The Map Interface Continued			
V get(Object key)		V remove(Object key)			
 Returns the value to which this map maps the specified key. Returns null if key not present. 		 Removes the mapping for this key from this map if it is present 			
<pre>boolean isEmpty()</pre>		<pre>int size()</pre>			
 Returns true if this map contains no key-value mappings. 		 Returns the number of key-value mappings in this map. 			
V put(K key, V value)		<pre>Collection<v> values()</v></pre>			
 Associates the specified value with the specified key in this map 		 Returns a collection view of the values contained in this map. 			
CS 314 Maps	13 C	S 314	Maps	14	

Results with HashMap

Title	Size (kb)	Total Words	Distinct Words	Time List	Time Map
small sample	0.6	89	25	0.001	0.0008
2BR02B	34	5,638	1,975	0.051	0.0140
Alice in Wonderland	120	29,460	6,017	0.741	0.0720
Adventures of Sherlock Holmes	581	107,533	15,213	4.144	0.2500
2008 CIA Factbook	10,030	1,330,100	74,042	173.000	4.0000

Title	Size	Total Words	Distinct Words	Time List	Time Map
small sample	0.6	89	25	0.001	0.0008
2BR02B	57x	63x	79x	51x	18x
Alice in Wonderland	3.5x	5.2x	3.0x	14.5x	5x
Adventures of Sherlock Holmes	4.8x	3.7x	2.5x	5.6x	3.5x
2008 CIA Factbook	17x	12.3x	5x	42x	16x

Order?

O(Total Words)?

Maps

15

Topic 11 Linked Lists

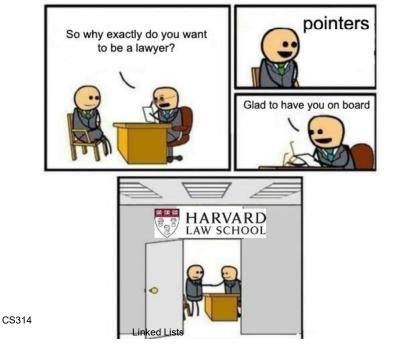
"All the kids who did great in high school writing pong games in BASIC for their Apple II would get to college, take CompSci 101, a data structures course, and when they hit the pointers business their brains would just totally explode, and the next thing you knew, they were majoring in Political Science because law school seemed like a better idea."

-Joel Spolsky

Thanks to Don Slater of CMU for use of his slides.



Sam G. - Fall 2023



Clicker 1

What is output by the following code?

```
ArrayList<Integer> a1 = new ArrayList<>();
ArrayList<Integer> a2 = new ArrayList<>();
a1.add(12);
a2.add(12);
System.out.println(a1 == a2);
```

- A. false
- **B**. true
- C. No output due to syntax error
- D. No output due to runtime error
- E. Varies from one run of the program to the next

Dynamic Data Structures

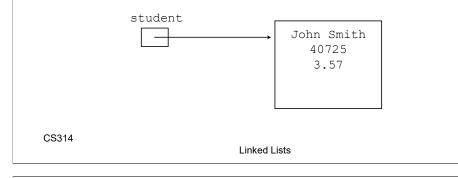
- Dynamic data structures
 - They grow and shrink one element at a time, normally without some of the inefficiencies of arrays
 - as opposed to a static container such as an array
- Big O of Array Manipulations
 - Access the kth element
 - Add or delete an element in the middle of the array while maintaining relative order
 - adding element at the end of array? space avail? no space avail?
 - add element at beginning of an array

3

CS314

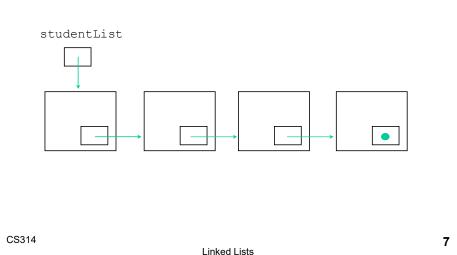
Object References

- Recall that an object reference is a variable that stores the address of an object
- A reference can also be called a *pointer*
- They are often depicted graphically:



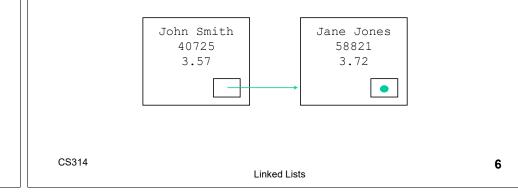
References as Links

References can be used to create a variety of linked structures, such as a *linked list*:



References as Links

- Object references can be used to create links between objects
- Suppose a Student class contained a reference to another Student object



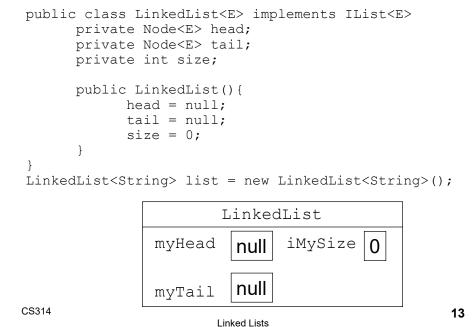
Linked Lists

- A linear collection of self-referential objects, typically called nodes, connected by other links
 - linear: for every node in the list, there is one and only one node that precedes it (except for possibly the first node, which may have no predecessor,) and there is one and only one node that succeeds it, (except for possibly the last node, which may have no successor)
 - self-referential: a node that has the ability to refer to another node of the same type, or even to refer to itself
 - node: contains data of any type, including a reference to another node of the same data type, or to nodes of different data types
 - Usually a list will have a beginning and an end; the first element in the list is accessed by a reference to that class, and the last node in the list will have a reference that is set to null

CS314

Advantages of linked lists	
U	Nodes and Lists
Linked lists are dynamic, they can grow or shrink	A different way of implementing a list
as necessary	 Each element of a Linked List is a separate Node object.
Linked lists are non-contiguous; the logical sequence of items in the structure is decoupled from any physical ordering in memory	Each Node tracks a single piece of data plus a reference (pointer) to the next
	Create a new Node very time we add something to the List
	Remove nodes when item removed from list and allow garbage collector to reclaim that memory
CS314 9	CS314 10 Linked Lists
A Node Class	One Implementation of a Linked List
<pre>public class Node<e> { private E myData; private Node<e> myNext;</e></e></pre>	The Nodes show on the previous slide are singly linked
<pre>public Node() { myData = null; myNext = null; }</pre>	 a node refers only to the next node in the structure
<pre>public Node(E data, Node<e> next) { myData = data; myNext = next; }</e></pre>	 it is also possible to have doubly linked nodes.
<pre>public E getData() { return myData; }</pre>	 The node has a reference to the next node in the structure and the <i>previous</i> node in the structure
<pre>public Node<e> getNext() { return myNext; }</e></pre>	as well
<pre>public void setData(E data) { myData = data: }</pre>	How is the end of the list indicated
public void setNext(Node <e> next)</e>	– myNext = null for last node
public void beenexe(node d) nexe,	 – a separate dummy node class / object
{ myNext = next; }	- a separate duminy node class / object
<pre>public Node(E data, Node<e> next) { myData = data; myNext = next; } public E getData() { return myData; } public Node<e> getNext() { return myNext; }</e></e></pre>	 structure it is also possible to have <i>doubly linked</i> nodes. The node has a reference to the next node in the structure and the <i>previous</i> node in the structure as well How is the end of the list indicated

A Linked List Implementation

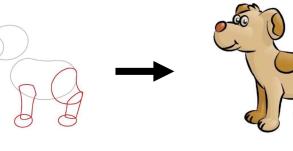


add method

- add to the end of list
- special case if empty
- steps on following slides
- public void add(E obj)

Writing Methods

- When trying to code methods for Linked Lists draw pictures!
 - If you don't draw pictures of what you are trying to do it is very easy to make mistakes!

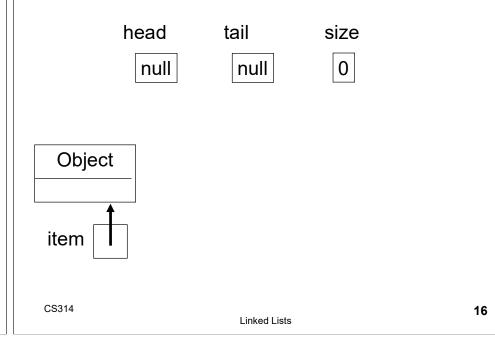




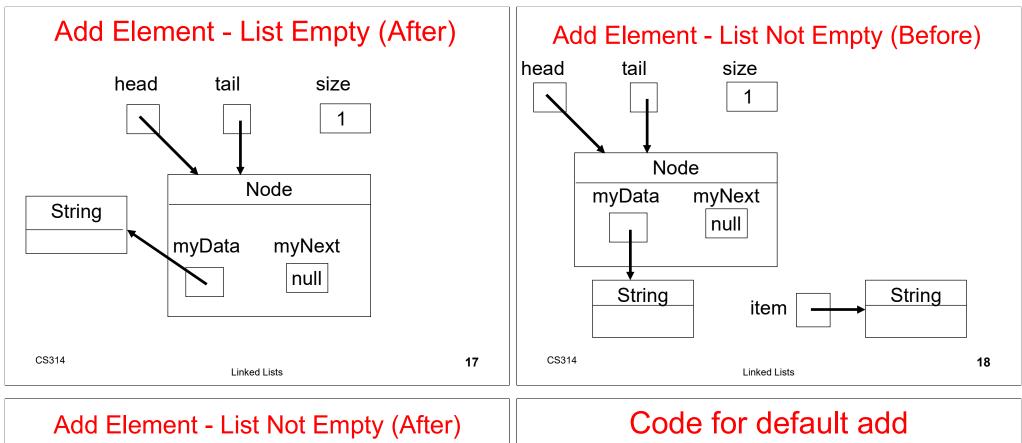
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----	--

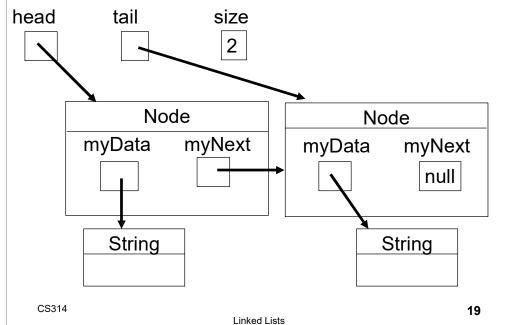
Add Element - List Empty (Before)

Linked Lists



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public void add(E obj)

	Clicker 2		Со	ntains method	
What is the worst case Big O for adding to the end of an array based list and our		Implement a d List class	contains method for	our Linked	
LinkedList314 class? The lists already contain N items.		public boolean o	contains(E val) // va	l != null	
Array based	Linked				
A. O(1)	O(1)				
B. O(N)	O(N)				
C. O(logN)	O(1)				
D. O(1)	O(N)				
E. O(N)	O(1)	21	CS314		22
		4 I			22
			Lin	ked Lists	
Co	de for addFront		Lin	Clicker 3	
Co • add to front o					ne front of
	f list		 What is the B an array base 	Clicker 3 ig O for adding to th d list and a linked lis	
 add to front o public void ad 	f list	he front	 What is the B an array base already contai 	Clicker 3 ig O for adding to th d list and a linked lis in N items.	
 add to front o public void ad 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> 	Clicker 3 ig O for adding to th d list and a linked lis in N items. Linked	
 add to front o public void ac How does thi 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> A. O(1) 	Clicker 3 ig O for adding to th d list and a linked lis in N items. <u>Linked</u> O(1)	
 add to front o public void ac How does thi 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> A. O(1) B. O(N) 	Clicker 3 ig O for adding to th d list and a linked lis in N items. <u>Linked</u> O(1) O(1)	
 add to front o public void ac How does thi 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> A. O(1) B. O(N) C. O(logN) 	Clicker 3 ig O for adding to th d list and a linked lis in N items. <u>Linked</u> O(1) O(1) O(1) O(1)	
 add to front o public void ac How does thi 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> A. O(1) B. O(N) C. O(logN) D. O(1) 	Clicker 3 ig O for adding to th d list and a linked lis in N items. Linked O(1) O(1) O(1) O(N)	
 add to front o public void ac How does thi 	f list ddFront(E obj) s compare to adding at t	he front	 What is the B an array base already contain <u>Array based</u> A. O(1) B. O(N) C. O(logN) 	Clicker 3 ig O for adding to th d list and a linked lis in N items. <u>Linked</u> O(1) O(1) O(1) O(1)	

Code for Insert		Clicker 4	
 public void insert(int pos, E obj) Must be careful not to break the chain! Where do we need to go? Special cases? 	What is the Big O for inserting an element into the middle of an array based list and into the middle of a linked list? Each list already contains N items.		
Special cases?	Array based	Linked	
	A. O(1)	O(1)	
	B. O(1)	O(N)	
	C. O(N)	O(1)	
	D. O(N)	O(N)	
CS314 25	E. O(N)	O(logN)	
CS314 25		Linked Lists 26	

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Clicker Question 5

What is the Big O for getting an element based on position from an array based list and from a linked list? Each list contains N items. In other words E get(int pos)

Array based	d Linked
A. O(1)	O(1)
B. O(1)	O(N)
C. O(N)	O(1)
D. O(logN)	O(N)
E. O(N)	O(N)
	Linked Lists

Code for get

Linked Lists

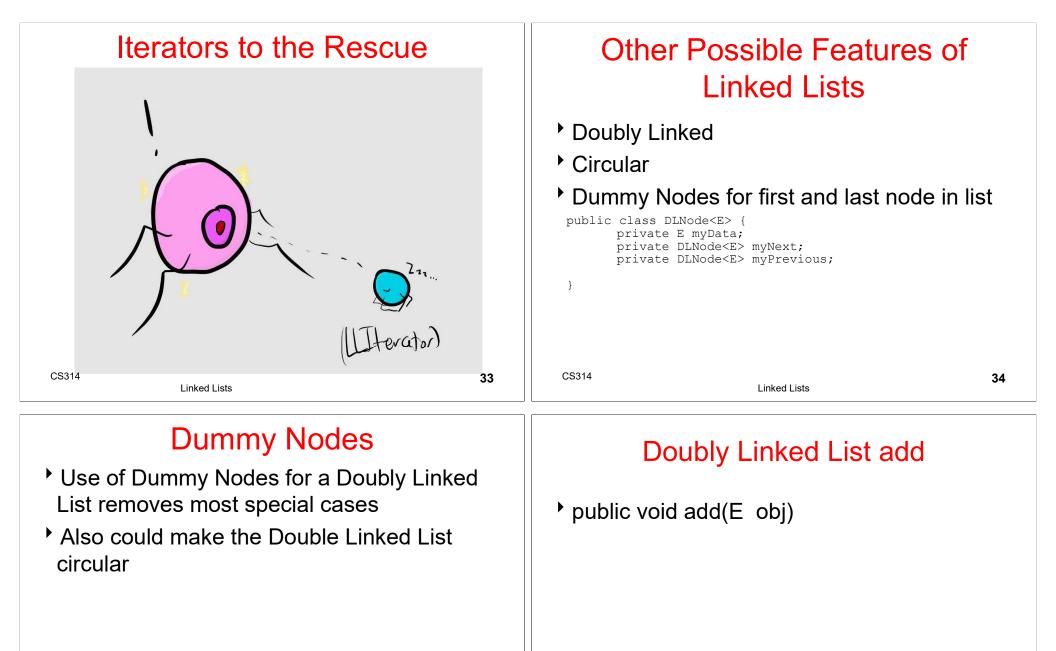
- public E get(int pos)
- The downside of Linked Lists







Code for remove	Clicker 6
public E remove(int pos)	 What is the order to remove the last element of a singly linked list with references to the first and last nodes of the linked structure of nodes? The list contains N elements
	A. O(1)
	B. O(logN)
	C. O(N^0.5)
	D. O(N)
CS314 29	E. O(NlogN))
CS314 29 Linked Lists	CS314 30
Why Use Linked List	Clicker 7 - Getting All Elements in
What operations with a Linked List faster	Order From a Linked List
What operations with a Linked List faster than the version from ArrayList?	Order From a Linked List What is the Order (Big O) of the following code
•	
•	What is the Order (Big O) of the following code
•	<pre> What is the Order (Big O) of the following code LinkedList314<integer> list; list = new LinkedList314<integer>(); // code to fill list with N elements</integer></integer></pre>
•	<pre> What is the Order (Big O) of the following code LinkedList314<integer> list; list = new LinkedList314<integer>(); // code to fill list with N elements int total = 0; //Big O of following code? for (int i = 0; i < list.size(); i++)</integer></integer></pre>
•	<pre> What is the Order (Big O) of the following code LinkedList314<integer> list; list = new LinkedList314<integer>(); // code to fill list with N elements int total = 0; //Big O of following code? for (int i = 0; i < list.size(); i++) total += list.get(i);</integer></integer></pre>



35

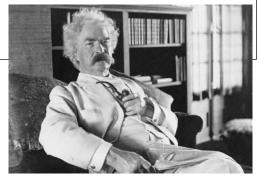
	for Doubly Linke insert(int pos, E obj)	ed List	
P			
CS314	Linked Lists	37	

Topic 12 Introduction to Recursion

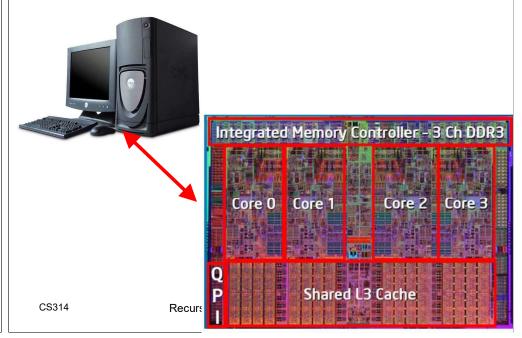
"To a man with a hammer, everything looks like a nail"

-Mark Twain

CS314



Underneath the Hood.



The Program Stack

When you invoke a method in your code what happens when that method is done?

```
public class Mice {
    public static void main(String[] args) {
        int x = 37;
        int y = 12;
        method1(x, y);
        int z = 73;
        int m1 = method1(z, x);
        method2(x, x);
    }
    // method1 and method2
    // on next slide
```

Recursion

method1 and method2

```
// in class Mice
public static int method1(int a, int b) {
    int r = 0;
    if (b != 0) {
        int x = a / b;
        int y = a % b;
        r = x + y;
    }
    return r;
}
public static void method2(int x, int y) {
        x++;
        y--;
        int z = method1(y, x);
        System.out.print(z);
cs314 Recursion
```

<pre>The Program Stack • When your program is run on a processor, the commands are converted into another set of instructions and assigned memory locations. – normally a great deal of expansion takes place public static void main(String[] args) { int x = 37; // 0 int y = 12; // 1 method1(x, y); // 2 int z = 73; // 3 int m1 = method1(z, x); // 4 method2(x, x); // 7 }_{cs314} Recursion Keep Recursion Recursion</pre>	 Basic CPU Operations A CPU works via a fetch command / execute command loop and a program counter Instructions stored in memory (Instructions are data!) int x = 37; // 0 int y = 12; // 1 method1(x, y); // 2 int z = 73; // 3 int m1 = method1(z, x); // 4 What if the first instruction of the method1 is stored at memory location 50? 6
<pre>// in class Mice public static int method1(int a, int b) { int r = 0; // 51 if (b != 0) { // 52 int x = a / b; // 53 int y = a % b; // 54 r = x + y; // 55 } return r; // 56 } public static void method2(int x, int y) { x++; // 60 y; // 61 int z = method1(y, x); // 62 System.out.print(z); // 63 cs314 Recursion 7 </pre>	<pre>Clicker 1 - The Program Stack int x = 37; // 1 int y = 12; // 2 method1(x, y); // 3 int z = 73; // 4 int m1 = method1(z, x); // 5 method2(x, x); // 6 Instruction 3 is really saying jump to instruction 50 with parameters x and y In general what happens when method1 finishes? A. program ends B. goes to instruction 4 C. goes back to whatever method called it </pre>

Activation Records and the	The Program Stack	
 Program Stack When a method is invoked all the relevant information about the current method (variables, values of variables, next line of code to be executed) is placed in an <i>activation record</i> The activation record is <i>pushed</i> onto the 	 Data may either be added (<i>pushed</i>) or removed (<i>popped</i>) from a stack but it is always from the top. A stack of dishes which dish do we have 	
 <i>program stack</i> A <i>stack</i> is a data structure with a single 	easy access to?	
access point, the <i>top</i> .		
CS314 Recursion 9	CS314 Recursion 10	
	A Problem	
	Write a method that determines how much space is take up by the files in a directory	
Using Recursion	A directory can contain files and directories	
	How many directories does our code have to examine?	
	How would you add up the space taken up by the files in a single directory	
	 Hint: don't worry about any sub directories at first 	
	CS314 Recursion 12	

Clicker 2

How many levels of directories have to be visited?

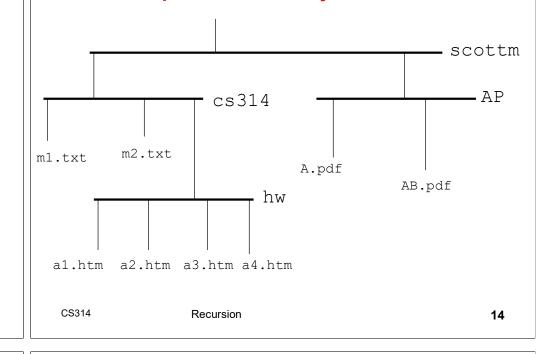
Α.	0
----	---

- B. 1
- C. 8

CS314

- D. Infinite
- E. Unknown

Sample Directory Structure



Java File Class

Recursion

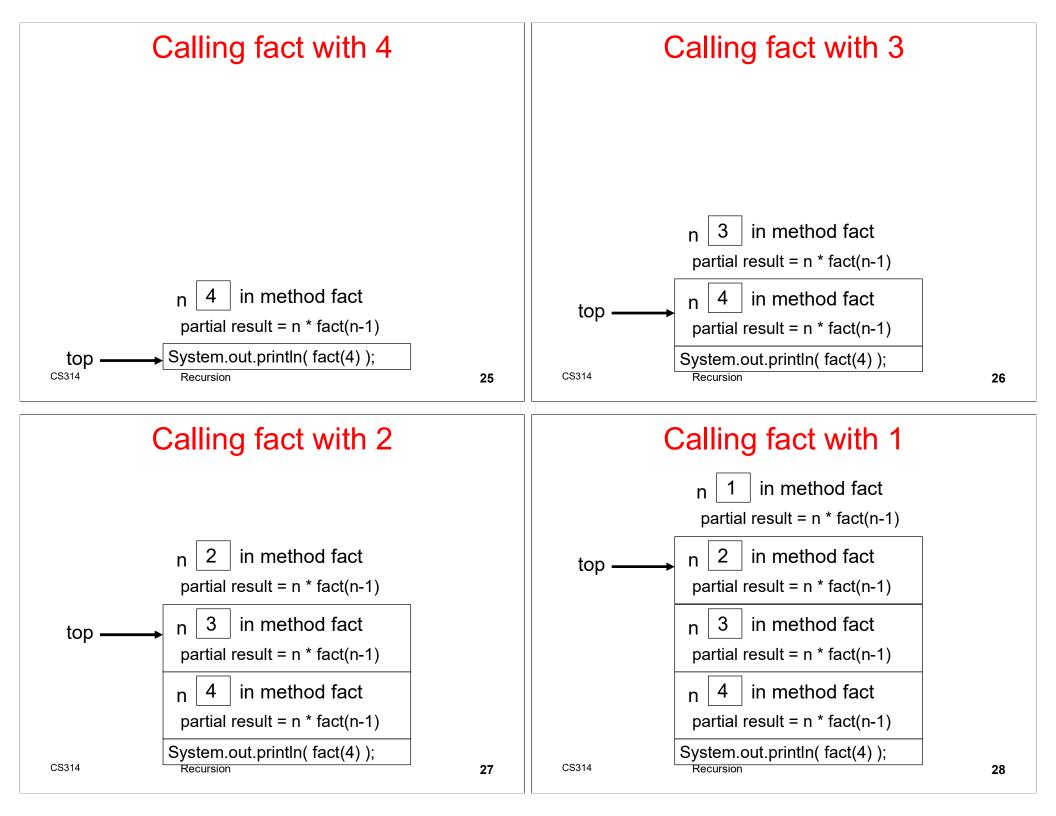
- File (String pathname) Creates a new File instance by converting the given pathname.
- boolean isDirectory() Tests whether the file denoted by this abstract pathname is a directory.
- File[] listFiles() Returns an array of abstract pathnames denoting the files in the directory denoted by this abstract pathname.

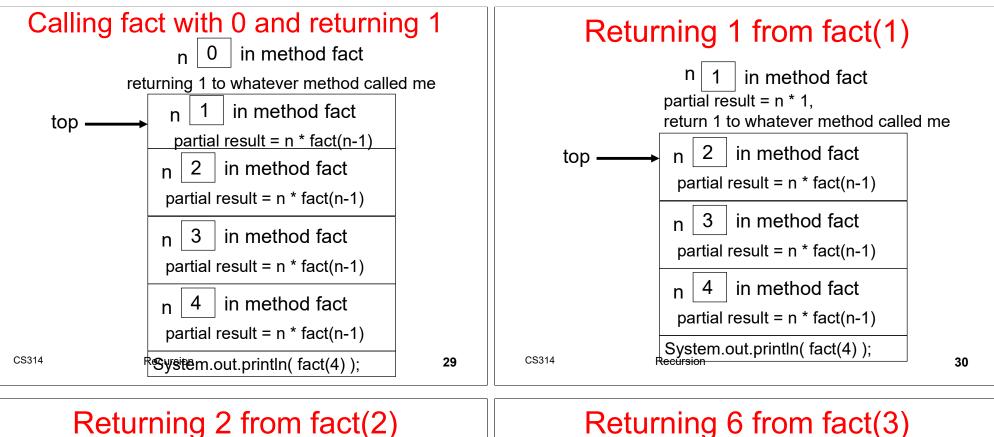
Code for getDirectorySpace()

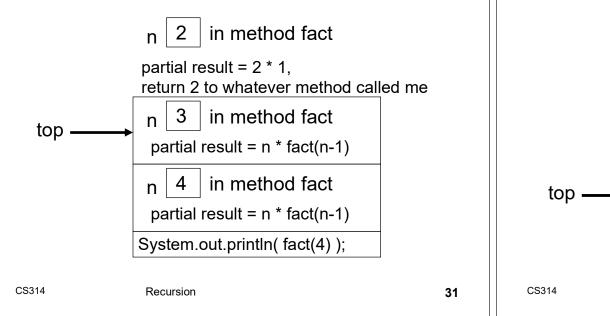
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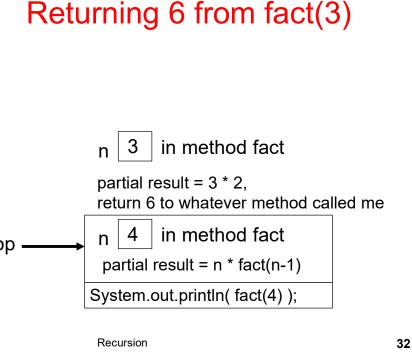
Iterative getDirectorySpace() Clicker 3 public long getDirectorySpace(File d) { Is it possible to write a non recursive method ArrayList<File> dirs = new ArrayList<>(); dirs.add(d); to determine space taken up by files in a long total = 0;directory, including its subdirectories, and while (dirs.size() > 0) { File temp = dirs.remove(dirs.size() - 1); their subdirectories, and their subdirectories, File[] filesAndSubs = temp.listFiles(); if (filesAndSubs != null) { and so forth? for (File f : filesAndSubs) { if (f != null) { A. No if (f.isFile()) total += f.length(); B. Yes else if (f.isDirectory()) dirs.add(f); C. It Depends return total; CS314 17 CS314 Recursion Recursion 18 The 3 plus 1 rules of Recursion 1. Know when to stop 2. Decide how to take one step 3. Break the journey down into that step and a Wisdom for Writing Recursive smaller journey **Methods** 4. Have faith From Common Lisp: A Gentle Introduction to Symbolic Computation by David Touretzky CS314 Recursion 20

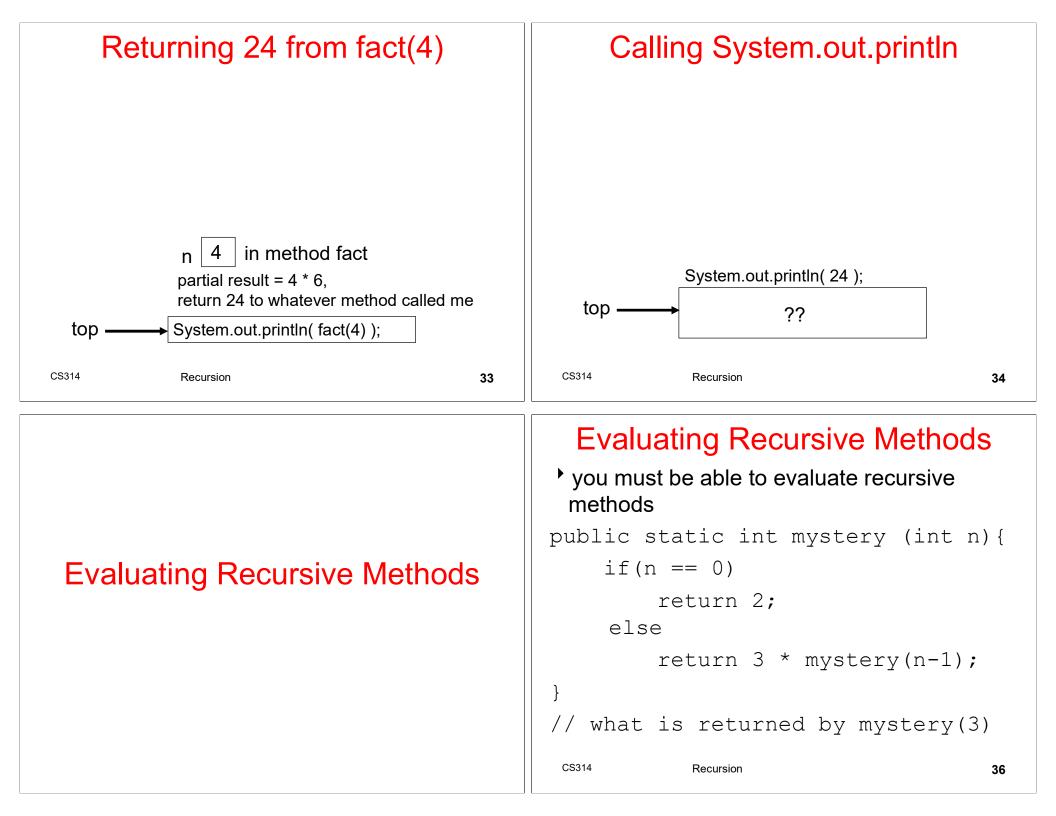
Writing Recursive Methods	N!
 Rules of Recursion Base Case: Always have at least one case that can be solved without using recursion Make Progress: Any recursive call must progress toward a base case. "You gotta believe." Always assume that the recursive call works. (Of course you will have to design it and test it to see if it works or prove that it always works.) A recursive solution solves a small part of the problem and leaves the rest of the problem in the same form as the original 	<pre>> the classic first recursion problem / example > N! 5! = 5 * 4 * 3 * 2 * 1 = 120 int res = 1; for (int i = 2; i <= n; i++) res *= i;</pre>
CS314 Recursion 21	CS314 Recursion 22
Factorial Recursively	Tracing Fact With the
 Factorial Recursively Mathematical Definition of Factorial 	Tracing Fact With the Program Stack
 Mathematical Definition of Factorial for N >= 0, N! is: 0! = 1 	
 Mathematical Definition of Factorial for N >= 0, N! is: 	Program Stack
<pre>Mathematical Definition of Factorial for N >= 0, N! is: 0! = 1 N! = N * (N - 1)! (for N > 0)</pre>	Program Stack











 Evaluating Recursive Methods Draw the program stack! 	Clicker 4 What is returned by fact (-3) ?
m(3) = 3 * m(2) -> 3 * 18 = 54 m(2) = 3 * m(1) -> 3 * 6 = 18	A. 0 B. 1 C. Infinite Icon
m(1) = 3 * m(0) -> 3 * 2 = 6 m(0) = 2 -> 54	C. Infinite loop D. Syntax error E. Runtime error
with practice you can see the result	<pre>public static int fact(int n) { if (n == 0) { return 1; } else { return n * fact(n - 1); } </pre>
CS314 Recursion 37	} } 38
Evaluating Recursive Methods	Evaluating Recursive Methods

What about multiple recursive calls? public static int bar(int n) { if (n <= 0)return 2; else return 3 + bar(n-1) + bar(n-2);Clicker 5 - What does bar(4) return? A. 2 B. 3 C. 12 D. 22 E. 37

```
What is returned by bar(4)?
b(4) = 3 + b(3) + b(2)
b(3) = 3 + b(2) + b(1)
b(2) = 3 + b(1) + b(0)
b(1) = 3 + b(0) + b(-1)
b(0) = 2
b(-1) = 2
```

Evaluating Recursive Method • What is returned by $bar(4)$? b(4) = 3 + b(3) + b(2) b(3) = 3 + b(2) + b(1) b(2) = 3 + b(1) + b(0) //substitute in results b(1) = 3 + 2 + 2 = 7 b(0) = 2 b(-1) = 2			b(2) + b(1)	;
CS314 Recursion	41	CS314	Recursion	42

Evaluating Recursive Methods

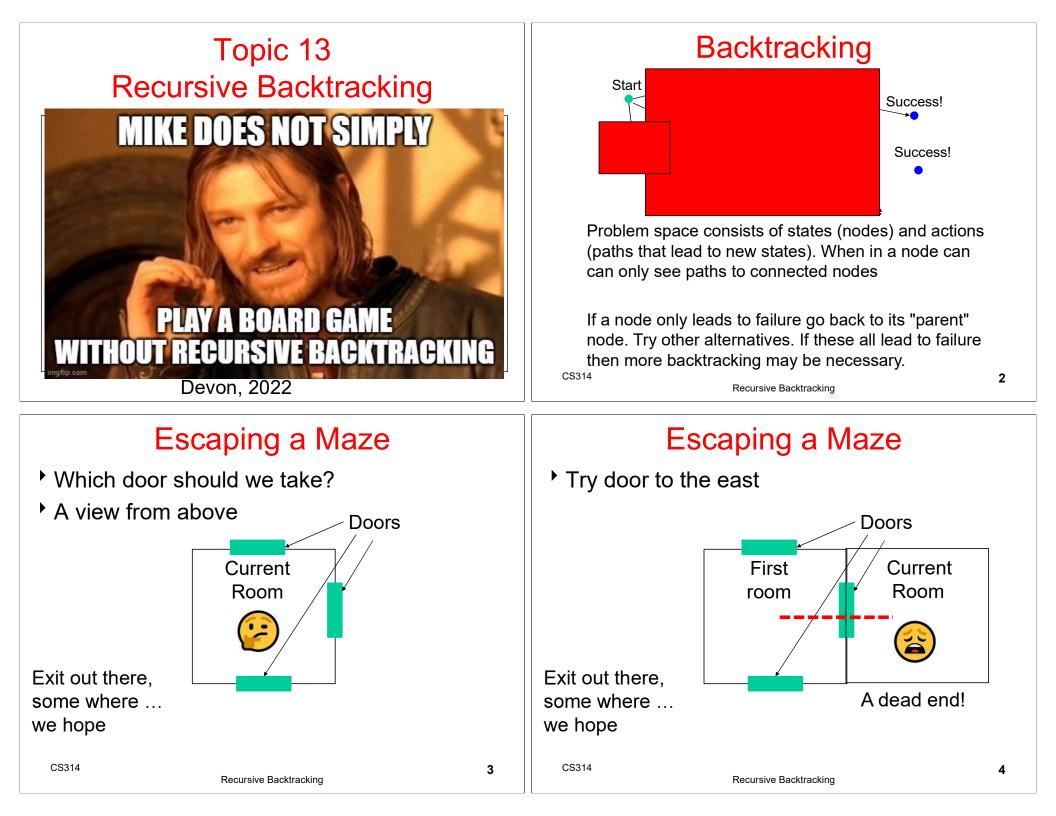
 What is returned by bar(4)? b(4) = 3 + b(3) + b(2) b(3) = 3 + 12 + 7 = 22 b(2) = 12 b(1) = 7 b(0) = 2 b(-1) = 2

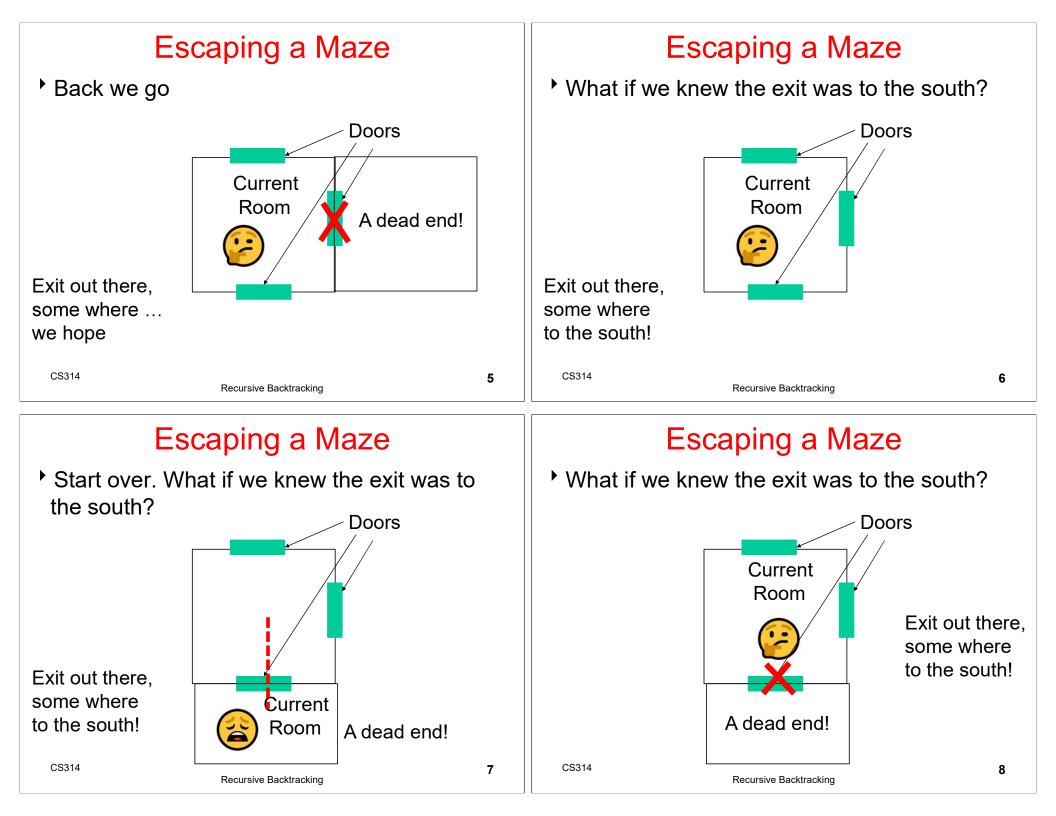
Evaluating Recursive Methods

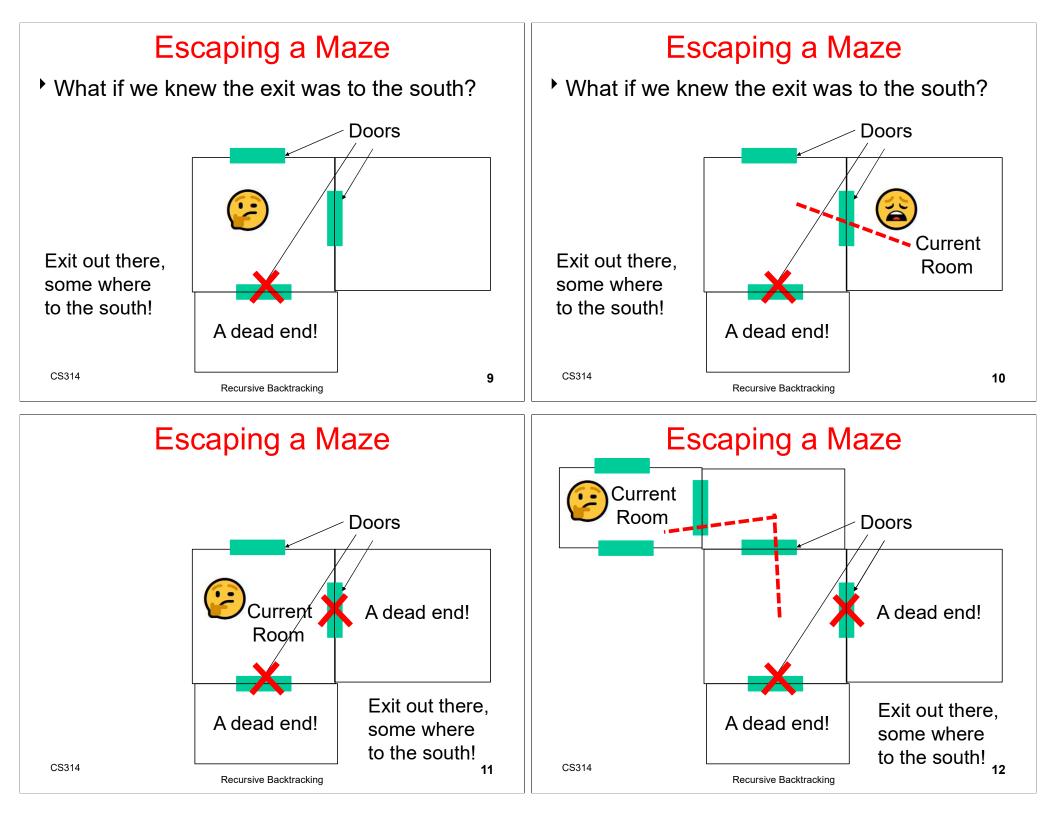
 What is returned by bar(4)? b(4) = 3 + 22 + 12 = 37 b(3) = 22 b(2) = 12 b(1) = 7 b(0) = 2 b(-1) = 2

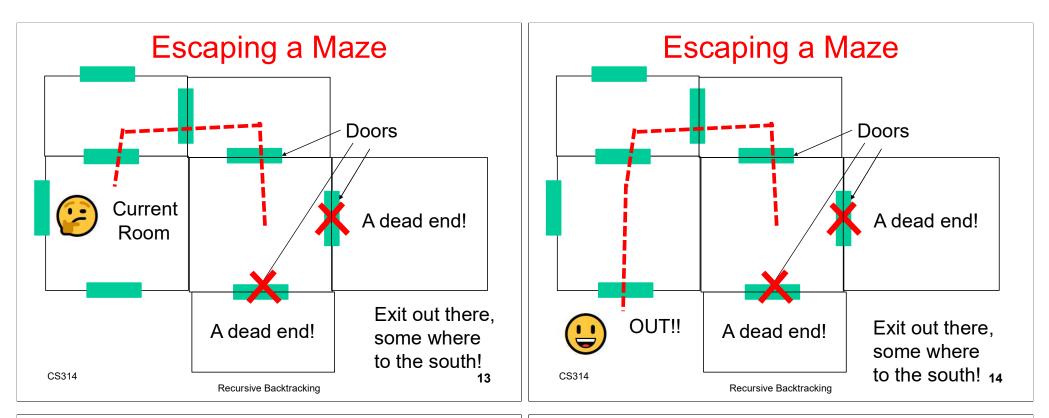
 Recursion Practice Write a method raiseToPower(int bint power) //pre: power >= 0 Simple recursion (also called tail reference) 	oase,	public i	ng the Maximum int max(int[] data) { method or create sm	
CS314 Recursion	45	CS314	Recursion	46
 Clicker 6 When writing recursive methods w be done first? A. Determine recursive case B. Determine recursive step C. Make a recursive call D. Determine base case(s) E. Determine the Big O 	hat should	 Rement It is not In factorization In factorization After le recursion 	bur Meta Cognit nber we are learning t a good tool for <i>all</i> p t we will implement seve ods where an iterative (le sion) solution would wor earning the mechanic on the real skill is kno ns or class of probler	to use a tool. roblems. eral algorithms and ooping without k just fine s and basics of owing what
CS314 Recursion	47	CS314	Recursion	48

 Big O and Recursion Determining the Big O of recursive methods can be tricky. A recurrence relation exits if the function is defined recursively. The T(N), actual running time, for N! is recursive T(N)_{fact} = T(N-1)_{fact} + O(1) This turns out to be O(N) There are N steps involved 	Common Recurrence Relations • $T(N) = T(N/2) + O(1) -> O(logN)$ - binary search • $T(N) = T(N-1) + O(1) -> O(N)$ - sequential search, factorial • $T(N) = T(N/2) + T(N/2) + O(1) -> O(N)$, - tree traversal • $T(N) = T(N-1) + O(N) -> O(N^2)$ - selection sort • $T(N) = T(N/2) + T(N/2) + O(N) -> O(NlogN)$ - merge sort • $T(N) = T(N-1) + T(N-1) + O(1) -> O(2^N)$ - Fibonacci
CS314 Recursion 49	CS314 Recursion 50









Recursive Backtracking

Pseudo code for recursive backtracking algorithms – looking for *a* solution

If at a solution, report success for (every possible choice from current state) Make that choice and take one step along path Use recursion to <u>try</u> to solve the problem for the new state <u>If</u> the recursive call succeeds, report the success to the previous level <u>Otherwise</u> Back out of the current choice to restore the

state at the start of the loop.

Report failure

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Another Concrete Example

- Sudoku
- 9 by 9 matrix with some numbers filled in
- all numbers must be between
 1 and 9
- Goal: Each row, each column, and each mini matrix must contain the numbers between 1 and 9 once each
 - no duplicates in rows, columns, or mini matrices

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8	Î		7	9

15

Solving Sudoku – Brute Force

- A <u>brute force</u> algorithm is a simple but generally inefficient approach
- Try all combinations until you find one that works
- This approach isn't clever, but computers are fast
- Then try and improve on the brute force results

9 8 6	8			8	6	3		3
	8				6	-220		3
	8	9	0	_	6		0	3
6 1 9 5	•	9	8	-	9	5	 6	-

Solving Sudoku

- Brute force Sudoku Soluton
 - if not open cells, solved
 - scan cells from left to right, top to bottom for first open cell
 - When an open cell is found start cycling through digits 1 to 9.
 - When a digit is placed check that the set up is legal
 - now solve the board

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5 3 6 9 5 1 9 8 6 8 6 4 8 3 7 2 6 6 2 8 4 1 9 5 8 7 9

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17

Recursive Backtracking

18

Clicker 1

Recursive Backtracking

After placing a number in a cell is the remaining problem very similar to the original problem?

A. No

B. Yes

5	3	1		7						5	3	1	2
6			1	9	5					6			1
	9	8					6				9	8	
8			Γ	6	8			3		8			
4			8		3			1]→	4			8
7	8			2				6		7			
	6					2	8				6		
			4	1	9	5		5		c			4
				8			7	9					
5	3	1	2	7	4	8				5	3	1	Т
6			1	9	5					6	-		ť
	9	8					6			_	9	8	
8				6				3		8			$^{+}$
4			8		3			1		4			╈
				2				6		7	+		t
7						2	8			_	6		$^{+}$
7	6					4		· · · · ·			10		
7	6		4	1	9	2	U	5		-	+		╈

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	1		7		Г				5	3	1	2	7						5	3	1	2	7	4		
		1	9	5					6			1	9	5					6			1	9	5		
Į	8					6				9	8					6				9	8					6
			6	S.	Т		3		8				6				3		8				6			
		8		3			1]→	4			8		3			1	→	4			8		3		
			2				6		7				2				6		7		43		2			
l					2	8				6					2	8				6					2	8
		4	1	9			5					4	1	9			5					4	1	9		
			8			7	9						8	Ĵ.		7	9						8			7
Γ	1	2	7	Λ	8			_				Т	-					7								
ł	4	1	9	5	0	-	-		5		1	12	7	4	8	9	-	-								
╞	8	-	-		_	6			6	-		1	9	5			_	_								
	•	_	_			0				9	8					6										
L			6				3		8				6				3							-		
		8		3			1		4			8		3			1			, I	uŀ	۱C	bh	!		

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2

1 9 6

5 9

2 8

Sudoku – A Dead End	Backing Up
 We have reached a dead end in our search 	 When the search reaches a dead end in <u>backs up</u> to the previous cell it was trying to fill and goes onto to the next digit We would back up to the cell with a 9 and that turns out to be a dead end as well so we back up again - so the algorithm needs to remember what digit to try next Now in the cell with the 8. We try and 9 and move forward again.
Characteristics of Brute Force and Backtracking Brute force algorithms are slow The first pass attempts typically don't employ	 Key Insights After trying placing a digit in a cell we want to solve the new sudoku board
 a lot of logic But, brute force algorithms are fairly easy to implement as a first pass solution many backtracking algorithms are brute force algorithms 	 Isn't that a smaller (or simpler version) of the same problem we started with?!?!?! After placing a number in a cell the we need to remember the next number to try in case things don't work out. We need to know if things worked out (found a solution) or they didn't, and if they didn't try the next number If we try all numbers and none of them work in our cell we need to <i>report back</i> that things didn't work

 Clicker 2 Grace 2019 Asked: When we reach the base case in the solveSudoku method (9 x 9 board) and before we return true, how many stack frames are on the program stack of the 	 Recursive Backtracking Problems such as Suduko can be solved using recursive backtracking recursive because later versions of the problem are just slightly simpler versions of
solveSudoku method? Pick the closest answer. A. <= 9	 the original backtracking because we may have to try different alternatives
B. 82 C. 81 ⁹	
D. 9 ⁸¹ E. cannot determine ²⁵	CS314 26 Recursive Backtracking
Recursive Backtracking - Repeated Pseudo code for recursive backtracking algorithms – looking for a solution If at a solution, report success for (every possible choice from current state) Make that choice and take one step along path Use recursion to try to solve the problem for the new state If the recursive call succeeds, report the success to the previous level Otherwise Back out of the current choice to restore the state at the start of the loop. Report failure	 Goals of Backtracking Possible goals Find a path to success Find all paths to success Find the best path to success Not all problems are exactly alike, and finding one success node may not be the end of the search Start Success!
CS314 27	CS314 Recursive Backtracking 28

Recursive Backtracking

Recursive Backtracking

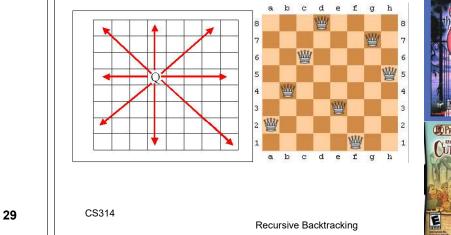


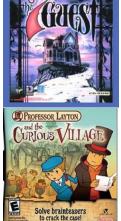
The 8-N Queens Problem



The 8 Queens Problem

- A classic chess puzzle
 - Place 8 queen pieces on a chess board so that none of them can attack one another





The N Queens Problem

Recursive Backtracking

- Place N Queens on an N by N chessboard so that none of them can attack each other
- Number of possible placements?
- In 8 x 8
 - 64 * 63 * 62 * 61 * 60 * 59 * 58 * 57 = 178,462, 987, 637, 760 / 8!
 - = 4,426,165,368

$$\binom{n}{k} = \frac{n \cdot (n-1) \cdots (n-k+1)}{k \cdot (k-1) \cdots 1} = \frac{n!}{k!(n-k)!} \quad \text{if } 0 \leq k \leq n$$

n choose k

- How many ways can you choose k things from a set of n items?
- In this case there are 64 squares and we want to choose 8 of them to put queens on

Clicker 3

- For a safe solution, how many queens can be placed in a given column?
- A. 0
- B. 1
- C. 2
- D. 3

CS314

E. Any number

(1)

Reducing the Search Space

The previous calculation includes set ups like this one

Q

Q

Q

Q

Q

0

- Includes lots of set ups with multiple queens in the same column
- How many queens can there be in one column?
- Number of set ups 8 * 8 * 8 * 8 * 8 * 8 * 8 * 8 = 16,777,216
- We have reduced search space by two orders of magnitude by applying some logic

```
CS314
```

Recursive Backtracking

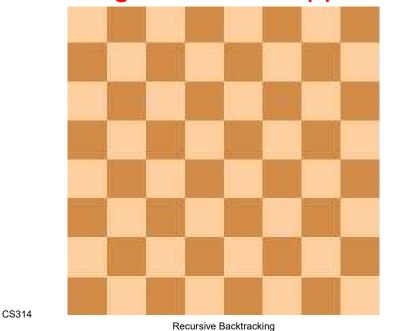
33

A Solution to 8 Queens

 If number of queens is fixed and I realize there can't be more than one queen per column I can iterate through the rows for each column

```
for (int r0 = 0; r0 < 8; r0++) {
       board[r0][0] = 'q';
        for (int r1 = 0; r1 < 8; r1++) {
              board[r1][1] = 'q';
              for (int r2 = 0; r2 < 8; r2++) {
                     board[r2][2] = 'q';
                     // a little later
                     for (int r7 = 0; r7 < 8; r7++) {
                            board[r7][7] = 'q';
                            if( gueensAreSafe(board) )
                                   printSolution(board);
                            board[r7][7] = ' '; //pick up queen
                     board[r6][6] = ' '; // pick up queen
 CS314
                                                               35
                          Recursive Backtracking
```

Solving N Queens Approach



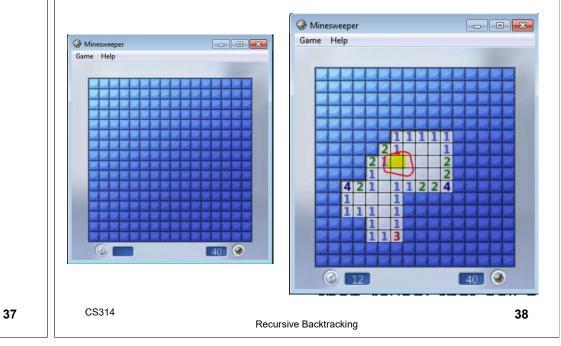
N Queens

- The problem with N queens is you don't know how many for loops to write.
- Do the problem recursively
- Write recursive code with class and demo
 - show backtracking with breakpoint and debugging option

Recursive Backtracking

- You must practice!!!
- Learn to recognize problems that fit the pattern
- Is a kickoff method needed?
- All solutions or a solution?
- Reporting results and acting on results

Minesweeper



Minesweeper Reveal Algorithm

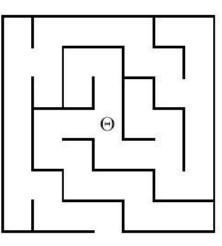
Recursive Backtracking

- Minesweeper
- click a cell

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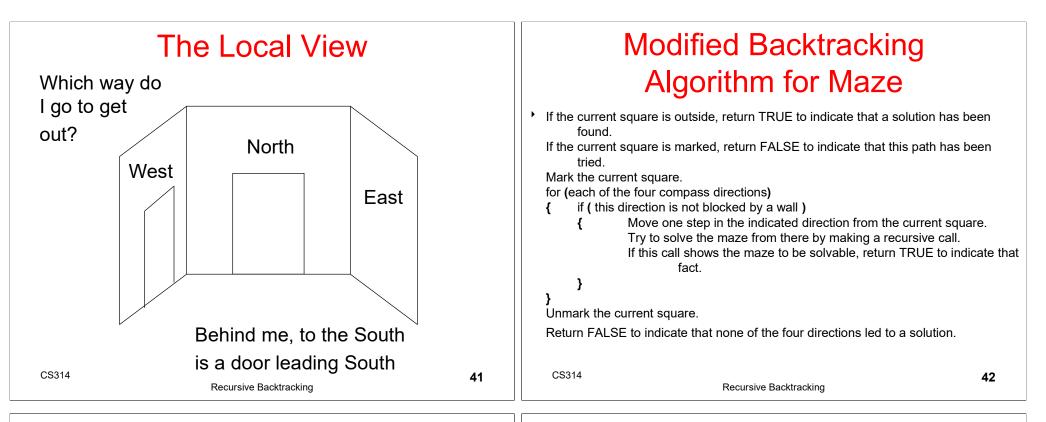
- if bomb game over
- if cell that has 1 or more bombs on border then reveal the number of bombs that border cell
- if a cell that has 0 bombs on border then reveal that cell as a blank and click on the 8 surrounding cells

Another Backtracking Problem A Simple Maze

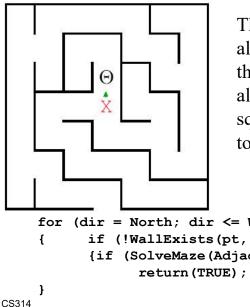


Search maze until way out is found. If no way out possible report that.

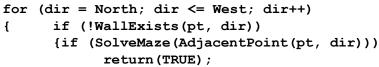
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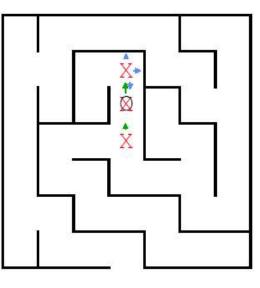
Backtracking in Action



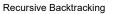
The crucial part of the algorithm is the for loop that takes us through the alternatives from the current square. Here we have moved to the North.



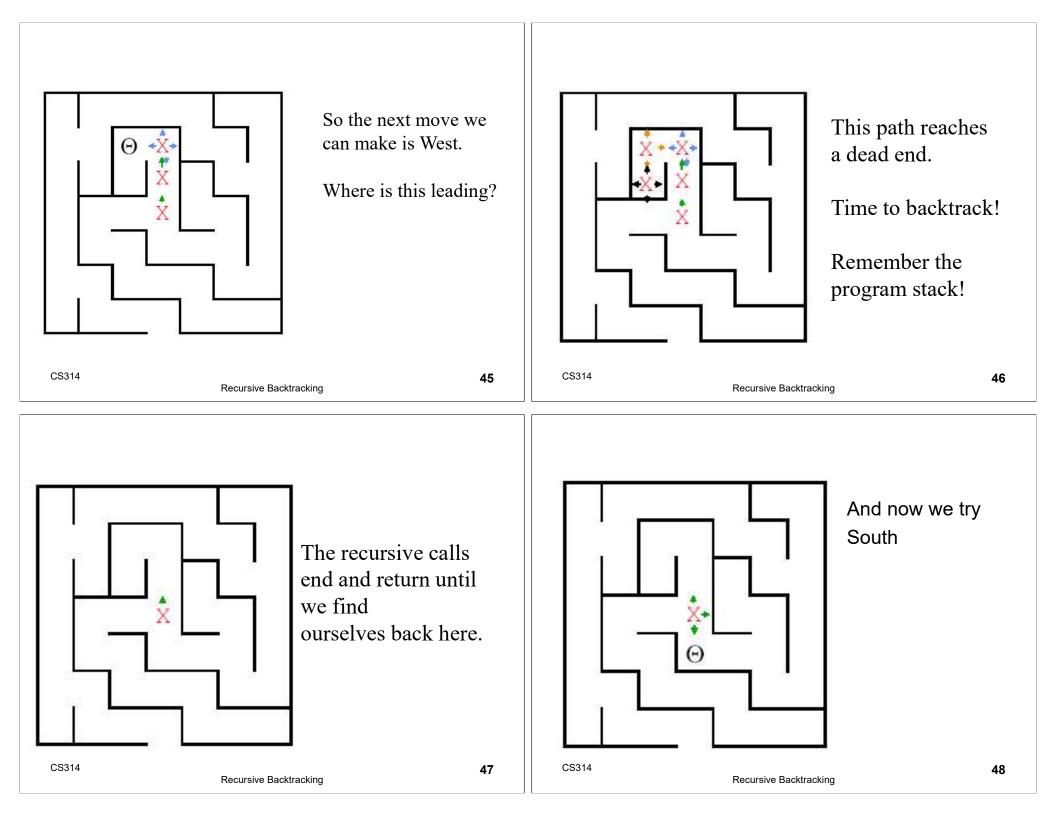
Backtracking in Action

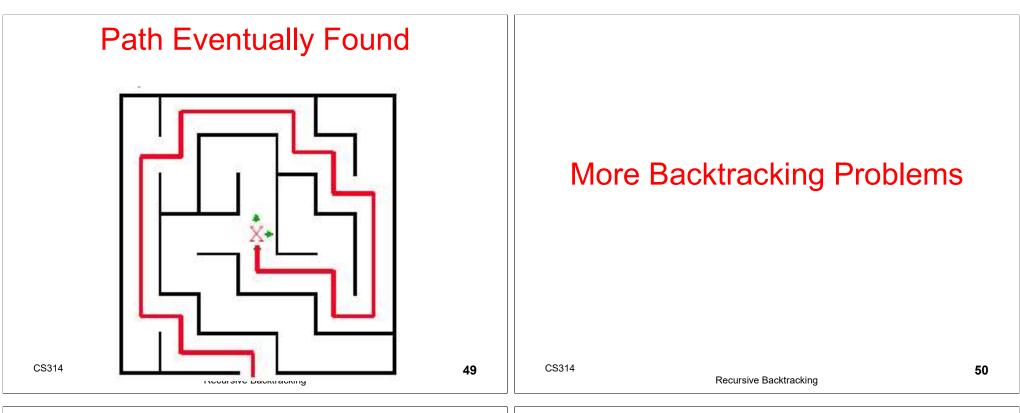


Here we have moved North again, but there is a wall to the North. East is also blocked, so we try South. That call discovers that the square is marked, so it just returns.



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Other Backtracking Problems

- Knight's Tour
- Regular Expressions
- Knapsack problem / Exhaustive Search
 - Filling a knapsack. Given a choice of items with various weights and a limited carrying capacity find the optimal load out. 50 lb. knapsack. items are 1 40 lb, 1 32 lb. 2 22 lbs, 1 15 lb, 1 5 lb. A greedy algorithm would choose the 40 lb item first. Then the 5 lb. Load out = 45lb. Exhaustive search 22 + 22 + 5 = 49.

The CD problem

We want to put songs on a Compact Disc.
 650MB CD and a bunch of songs of various sizes.

If there are no more songs to consider return result else{	
Consider the next song in the list.	
Try not adding it to the CD so far and use recursion to evaluate without it.	best
Try adding it to the CD, and use recursion to evaluate best with Whichever is better is returned as absolute best from here	it
}	

Another Backtracking Problem

- Airlines give out frequent flier miles as a way to get people to always fly on their airline.
- Airlines also have partner airlines. Assume if you have miles on one airline you can redeem those miles on any of its partners.
- Further assume if you can redeem miles on a partner airline you can redeem miles on any of its partners and so forth...
 - Airlines don't usually allow this sort of thing.
- Given a list of airlines and each airlines partners determine if it is possible to redeem miles on a given airline A on another airline B. CS314

Recursive Backtracking

Airline List – Part 1

- Delta
 - partners: Air Canada, Aero Mexico, OceanAir
- United
 - partners: Aria, Lufthansa, OceanAir, Quantas, British Airways
- Northwest
 - partners: Air Alaska, BMI, Avolar, EVA Air
- Canjet

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- partners: Girjet
- Air Canda
 - partners: Areo Mexico, Delta, Air Alaska
- Aero Mexico
 - partners: Delta, Air Canda, British Airways

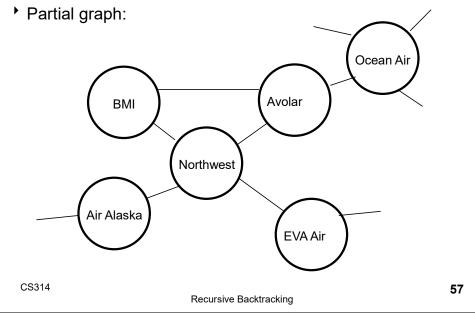
Recursive Backtracking

Airline List - Part 2	Airline List - Part 3
 Ocean Air partners: Delta, United, Quantas, Avolar AlohaAir partners: Quantas Aria partners: United, Lufthansa Lufthansa partners: United, Aria, EVA Air Quantas partners: United, OceanAir, AlohaAir BMI partners: Northwest, Avolar Maxair partners: Southwest, Girjet 	 Girjet partners: Southwest, Canjet, Maxair British Airways partners: United, Aero Mexico Air Alaska partners: Northwest, Air Canada Avolar partners: Northwest, Ocean Air, BMI EVA Air partners: Northwest, Luftansa Southwest partners: Giriet Maxair
- partiers. Southwest, Giljet	– partners: Girjet, Maxair

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Problem Example

If I have miles on Northwest can I redeem them on Aria?



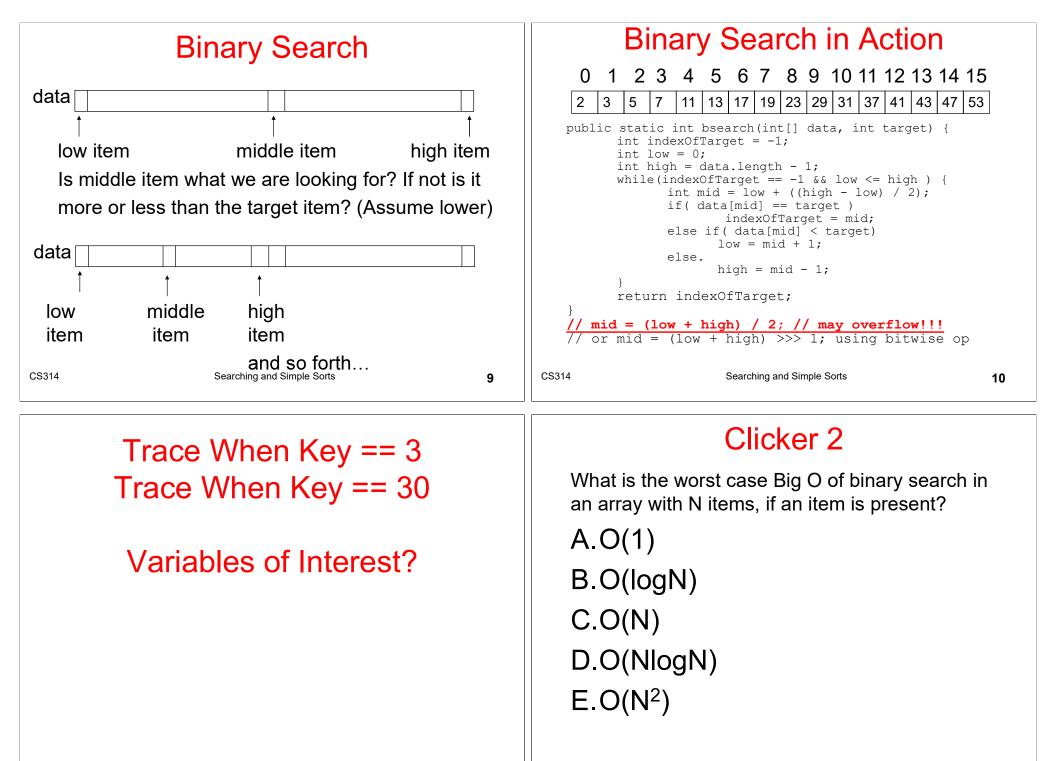
Sorting and Searching Topic 14 Searching and Simple Sorts Fundamental problems in computer science and programming "There's nothing in your head the Sorting done to make searching easier sorting hat can't see. So try me Multiple different algorithms to solve the on and I will tell you where you same problem ought to be." - How do we know which algorithm is "better"? -The Sorting Hat, Harry Potter Look at searching first and the Sorcerer's Stone Examples use arrays of ints to illustrate algorithms CS314 Searching and Simple Sorts Searching Given an array or list of data find the location Searching of a particular value or report that value is not present iTune A Yellow P O polscience Intersearch badmonkey0001 arch Results - intuitive approach? A Yellow Pages - start at first item A Yellow Pag - is it the one I am looking for? Grep in Project Go - if not go to next item - repeat until found or all items checked Advanced Search recursive backtracking Preferences If items not sorted or unsortable this Google Search | I'm Feeling Lucky Language Tools approach is necessary CS314 Searching and Simple Sorts

Linear Search

Linear Search	Linear Search, Generic
<pre>/* pre: data != null post: return the index of the first occurrence of target in data or -1 if target not present in data */ public int linearSearch(int[] data, int target) { for (int i = 0; i < data.length; i++) { if (data[i] == target) { return i; } } return -1; }</pre>	<pre>/* pre: data != null, no elements of data == null target != null post: return the index of the first occurrence of target in data or -1 if target not present in data */ public int linearSearch(Object[] data, Object target) { for (int i = 0; i < data.length; i++) if (target.equals(data[i])) return i; return -1; } T(N)? Big O? Best case, worst case, average case?</pre>
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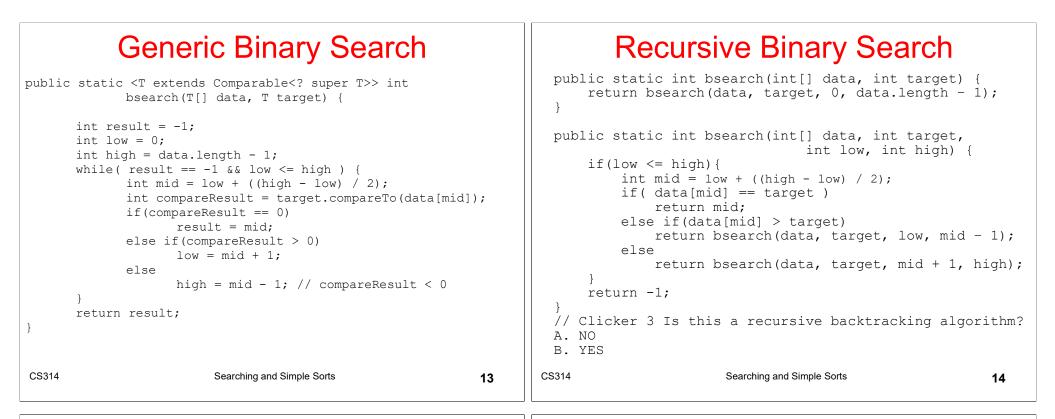
Clicker 1

	Clicker 1		Sear	ching in a Sorted Array or	List
search in an a present once A. O(1) B. O(logN) C. O(N) D. O(NlogN) E. O(N ²)		item is	 conquer dividing genera The Bin Start a is that is that If not is less th greated repeat 	your work in half with each step ally a good thing ary Search with array in ascendir at middle of list the item? s it less than or greater than the item? an, move to second half of list r than, move to first half of list until found or sub list size = 0	ng order
CS314	Searching and Simple Sorts	7	CS314	Searching and Simple Sorts	8



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Other Searching Algorithms

- Interpolation Search
 - more like what people really do
- Indexed Searching
- Binary Search Trees
- Hash Table Searching
- best-first

► A*



Menu

Due Date

	Song Name		Time	Track # A	Artist		Album
	S Letters from the Wasteland	0	4:29	1 of 10	The Wallflowers	0	Breach
	S When You're On Top	0	3:54	1 of 13	The Wallflowers	0	Red Letter Days
	Hand Me Down	0	3:35	2 of 10	The Wallflowers	0	Breach
	How Good It Can Get	0	4:11	2 of 13	The Wallflowers	0	Red Letter Days
	Sleepwalker	0	3:31	3 of 10	The Wallflowers	0	Breach
	Closer To You	0	3:17	3 of 13	The Wallflowers	0	Red Letter Days
	🕑 I've Been Delivered	0	5:01	4 of 10	The Wallflowers	0	Breach
	Severybody Out Of The Water	0	3:42	4 of 13	The Wallflowers	0	Red Letter Days
	S Witness	0	3:34	5 of 10	The Wallflowers	0	Breach
	S Three Ways	0	4:19	5 of 13	The Wallflowers	0	Red Letter Days
	Some Flowers Bloom Dead	0	4:43	6 of 10	The Wallflowers	0	Breach
	S Too Late to Quit	0	3:54	6 of 13	The Wallflowers	0	Red Letter Days
	S Mourning Train	0	4:04	7 of 10	The Wallflowers	0	Breach
	If You Never Got Sick	0	3:44	7 of 13	The Wallflowers	0	Red Letter Days
	S Up from Under	0	3:38	8 of 10	The Wallflowers	0	Breach
	Health and Happiness	0	4:03	8 of 13	The Wallflowers	0	Red Letter Days
	Murder 101	0	2:31	9 of 10	The Wallflowers	0	Breach
	See You When I Get There	0	3:09	9 of 13	The Wallflowers	0	Red Letter Days
	Sirdcage	0	7:42	10 of 10	The Wallflowers	0	Breach
	Seels Like Summer Again	0	3:48	10 of 13	The Wallflowers	0	Red Letter Days
	S Everything I Need	0	3:37	11 of 13	The Wallflowers	0	Red Letter Days
6	d Here in Pleasantville	0	3:40	12 of 13	The Wallflowers	0	Red Letter Days
	Sempire in My Mind (Bonus Track)	0	3:31	13 of 13	The Wallflowers	0	Red Letter Days

U.S. All-time List - Marathon

Deena Kastor nee

Drossin (2)

2:21:21 Joan Benoit Samuelson

Kastor (3)

2:22:43a Benoit (2)

2:24:52a Benoit (3)

2:26:11 Benoit (4)

2:26:26a Julie Brown

2:26:40a Kim Jones

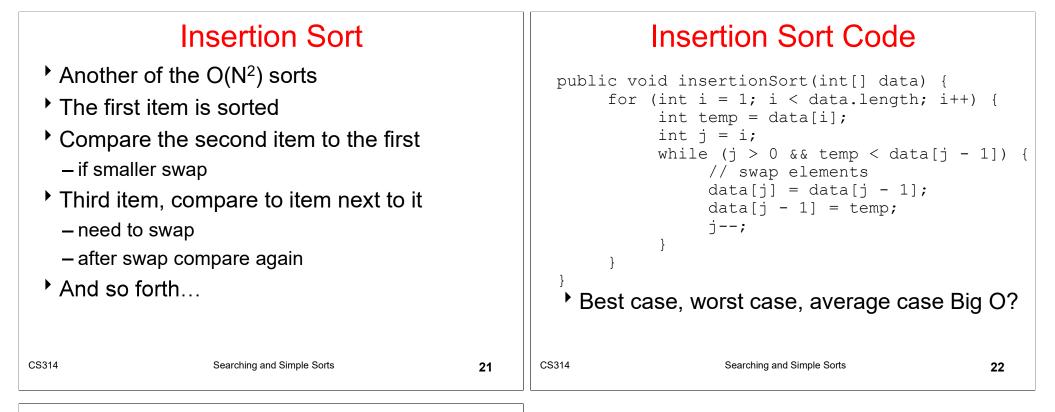
As of 4/24/08

2:19:36

2:21:16

Women

 Sorting A fundamental application for computate Done to make finding data (searching) Many different algorithms for sorting One of the difficulties with sorting is work with a fixed size storage container (array – if resize, that is expensive (slow) The simple sorts are slow bubble sort selection sort insertion sort 	faster orking	<pre>Selection sort Algorithm - Search through the data and find the smallest element - swap the smallest element with the first element - repeat starting at second element and find the second smallest element public static void selectionSort(int[] data) { for (int i = 0; i < data.length - 1; i++) { int min = i; for (int j = i + 1; j < data.length; j++)</pre>
CS314 Searching and Simple Sorts	17	CS314 Searching and Simple Sorts 18
Insertion Sort in Practice		Generic Selection Sort
44 68 191 119 119 37 83 What is the T(N), <i>actual</i> number of statements executed, of the selection so code, given an array of N elements? What is the Big O?		<pre>public static <t comparable<?="" extends="" super="" t="">> void selectionSort(T[] data) { for(int i = 0; i < data.length - 1; i++) { int min = i; for(int j = i + 1; j < data.length; j++) if(data[min].compareTo(data[j]) > 0) min = j; T temp = data[i]; data[i] = data[min]; data[i] = temp; } }</t></pre>
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Clicker 4 - Comparing Algorithms

- Which algorithm do you think has a smaller T(N) given random data, selection sort or insertion sort?
- A. Insertion Sort
- B. Selection Sort
- C. About the same

Topic 15 **Implementing and Using Stacks**

"stack n.

The set of things a person has to do in the future. "I haven't done it yet because every time I pop my stack something new gets pushed." If you are interrupted several times in the middle of a conversation, "My stack overflowed" means "I forget what we were talking about."

-The Hacker's Dictionary

Friedrich L. Bauer German computer scientist who proposed "stack method of expression evaluation" in 1955.



Sharper Tools



Lists



Stacks





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Stacks

Stacks

- Access is allowed only at one point of the structure, normally termed the *top* of the stack
 - access to the most recently added item only
- Operations are limited:
 - push (add item to stack)
 - pop (remove top item from stack)
 - top (get top item without removing it)
 - isEmpty
- Described as a "Last In First Out" (LIFO) data structure

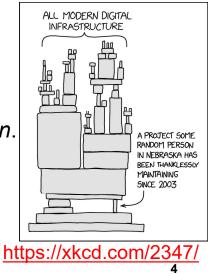


Implementing a stack

- need an underlying collection to hold the elements of the stack
- 3 obvious choices?
 - native array
 - linked structure of nodes
 - a list!!!

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- Adding a layer of abstraction. A HUGE idea.
- array implementation
- Inked list implementation



3

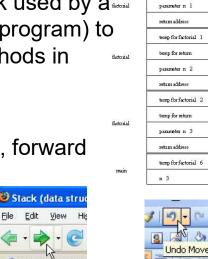
Stacks

Uses of Stacks

- The runtime stack used by a main process (running program) to keep track of methods in progress
- Search problems
- Undo, redo, back, forward



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temp for return



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Stack Operations

Assume a simple stack for integers. Stack<Integer> s = new Stack<>(); s.push(12); s.push(4);s.push(s.top() + 2);s.pop(); s.push(s.top()); //what are contents of stack? CS314 Stacks

Clicker 1 - What is Output?

Stacks

```
Stack<Integer> s = new Stack<>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// Print out contents of stack.
// Assume there is a size method.
for (int i = 0; i < s.size(); i++)
    System.out.print(s.pop() + " ");
A 0 1 2 3 4
                  D 2 3 4
  4 3 2 1 0
                  E No output due
B
C 4 3 2
                       to runtime error
CS314
```

Stacks

Corrected Version

```
Stack<Integer> s = new Stack<Integer>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// print out contents of stack
// while emptying it
final int LIMIT = s.size();
for (int i = 0; i < LIMIT; i++)
    System.out.print(s.pop() + " ");
//or
    while (!s.isEmpty())
//
//
         System.out.println(s.pop());
CS314
                                        8
                   Stacks
```

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CS314

Stacks

Clicker Question	n 2 Ev	aluation of Postfix Expressions	
What does the following postfix	x expression 🛛 🗎 🕨 Eas	sy to do with a stack	
evaluate to?	•	en a proper postfix expression:	
632+*		et the next token	
A. 11		it is an operand push it onto the stack	
		se if it is an operator	
B. 18		pop the stack for the right hand operand	
C. 24		pop the stack for the left hand operand	
D. 30	•	apply the operator to the two operands	
E. 36		push the result onto the stack	
		nen the expression has been exhausted the sult is the top (and only element) of the stack	
CS314 Stacks	13 CS314	Stacks 14	
Infix to Postfix	[Infix to Postfix Conversion	
Infix to Postfix		Infix to Postfix Conversion	
Infix to Postfix Convert the following equation postfix:	s from infix to	Infix to Postfix Conversion uires operator precedence parsing algorithm urse v. To determine the syntactic structure of a ntence or other utterance	
Convert the following equation	es from infix to - pa se	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a	
Convert the following equation postfix:	es from infix to - pa se Opera	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance	
 Convert the following equation postfix: 2^3^3+5*1 	ns from infix to - pa se Operat Close	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression	
 Convert the following equation postfix: 2 ^ 3 ^ 3 + 5 * 1 11 + 2 - 1 * 3 / 3 + 2 ^ 2 / 3 	es from infix to Para Se Operat Close pare Operat	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression parenthesis: pop stack symbols until an open nthesis appears	
 Convert the following equation postfix: 2 ^ 3 ^ 3 + 5 * 1 11 + 2 - 1 * 3 / 3 + 2 ^ 2 / 3 Problems: 	es from infix to Para Se Operat Close pare Operat Have	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression parenthesis: pop stack symbols until an open nthesis appears cors: e an on stack and off stack precedence	
 Convert the following equation postfix: 2 ^ 3 ^ 3 + 5 * 1 11 + 2 - 1 * 3 / 3 + 2 ^ 2 / 3 Problems: Negative numbers? 	es from infix to Para Para Operat Close pare Operat Have Pop	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression parenthesis: pop stack symbols until an open nthesis appears cors: e an on stack and off stack precedence all stack symbols until a symbol of lower	
 Convert the following equation postfix: 2 ^ 3 ^ 3 + 5 * 1 11 + 2 - 1 * 3 / 3 + 2 ^ 2 / 3 Problems: Negative numbers? 	es from infix to Para Se Operat Close pare Operat Have Pop prec End of	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression parenthesis: pop stack symbols until an open nthesis appears cors: e an on stack and off stack precedence all stack symbols until a symbol of lower edence appears. Then push the operator input: Pop all remaining stack symbols and	
 Convert the following equation postfix: 2 ^ 3 ^ 3 + 5 * 1 11 + 2 - 1 * 3 / 3 + 2 ^ 2 / 3 Problems: Negative numbers? 	es from infix to Para Se Operat Close pare Operat Have Pop prec End of	uires operator precedence parsing algorithm rse v. To determine the syntactic structure of a ntence or other utterance nds: add to expression parenthesis: pop stack symbols until an open nthesis appears cors: e an on stack and off stack precedence all stack symbols until a symbol of lower edence appears. Then push the operator	

Simple Example

Infix Expression:

PostFix Expression:

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
٨	10	9
(20	0

CS314

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Simple Example

3

+

Stacks

Infix Expression:

2*4

PostFix Expression:

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Stacks

Simple Example

Infix Expression:

PostFix Expression: 3

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

CS314

Stacks

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Simple Example

Infix Expression:	* 4
PostFix Expression:	32

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
-	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

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Simpl	e l	Exar	mp	e
-------	-----	------	----	---

4

+ *

PostFix Expression: 32

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
٨	10	9
(20	0

Stacks

Simple Example

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Simple Example

Infix Expression:

PostFix Expression: 324

Operator Stack: + *

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
٨	10	9
(20	0

CS314

Stacks

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Simple Example

Infix Expression:

PostFix Expression: 324*+

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(20	0

Operator Stack:

Infix Expression:

PostFix Expression:

Precedence Table

+

324*

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
/	2	2
٨	10	9
(20	0

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Stacks

	Example - ((4 + 5) * 6) ^ 2 m in action on above ed	quation	 In processi computer la instances v { } , [] , () A stack is When a cl the most r type. 	ced Symbol Che ing programs and work anguages there are ma when symbols must be useful for checking symbol osing symbol is found it m recent opening symbol of t to checking html and x	ting with any balanced of balance. nust match the same
CS314	Stacks	25	CS314	Stacks	26
 Make an en read symbol if the symbol the stack if it is a clos if the stack otherwise 	orithm for Balance ymbol Checking npty stack ols until end of file ol is an opening symbol pu sing symbol do the followin k is empty report an error pop the stack. If the symbol po the closing symbol report an e	ish it onto g pped does	 list[i] = 3 * (4 list[i - 1]))/2 Complication – when is it no Processing a – Tokenization Each independent 	ot an error to have non matchi a file <i>n</i> : the process of scanning an endent chunk is a token.	i + 1) + foo(ng symbols? input stream.
At the end of report an err CS314	of the file if the stack is n ror	not empty 27	CS314	be made up of 1 or more	characters

Topic 16 Queues

"FISH queue: n.

[acronym, by analogy with FIFO (First In, First Out)] 'First In, Still Here'. A joking way of pointing out that processing of a particular sequence of events or requests has stopped dead. Also FISH mode and FISHnet; the latter may be applied to any network that is running really slowly or exhibiting extreme flakiness."

-The Jargon File 4.4.7

Queues

- A sharp tool, like stacks
- A line
 - –In England people don't "get in line" they "queue up".





CS314

Queues

2

Queue Properties

- Queues are a first in first out data structure
 - FIFO (or LILO, but I guess that sounds a bit silly)
- Add items to the end of the queue
- Access and remove from the front
 - Access to the element that has been in the structure the *longest* amount of time
- Used extensively in operating systems
 - Queues of processes, I/O requests, and much more



Queues in Operating Systems

- On a computer with N cores on the CPU, but more than N processes, how many processes can actually be executing at one time?
- One job of OS, schedule the processes for the CPU

Processes Resources File Syste	ms						
Load averages for the last 1, 5,	15 minutes	1.28, 1.4	9, 1.40				Quit Proc
Process Name	Status	% CPU	Nice	ID	Memory	A	Proces
at-spi-registryd	Sleeping	0	0	3683	2.4 MiB	-	361
bonobo-activation-server	Sleeping	0	0	3158	332.0 KiB		366
bt-applet	Sleeping	0	0	3179	212.0 KiB		346
Clock-applet	Sleeping	0	0	3241	676.0 KiB		371
dbus-daemon	Sleeping	0	0	3118	164.0 KIB		368
dbus-launch	Sleeping	0	0	3120	0 bytes		374
eggcups	Sleeping	0	0	3165	1.6 MiB		360
escd	Sleeping	0	0	3200	44.0 KiB		359
🛞 firefox	Sleeping	0	0	15110	0 bytes		
firefox-bin	Sleeping	0	0	15126	143.5 MIB		
gam server	Sleeping	0	0	3220	156.0 KiB		
qconfd-2	Sleeping	0	0	3126	504.0 KiB		
🮅 qedit	Sleeping	0	0	1464	6.9 MIB	-	
					End Proc	ess	
						16	

it Process Ir		Filter			Show		
Process ID	Process	Name	User	* % CPI	J # Threads	Real Memory	VSIZE
361	E Fi	nder	steve	0.0	0 4	21.05 MB	238.26 MB
366	👩 Si	afari	steve	0.0	0 6	23.53 MB	252.85 MB
346		ginwindow	steve	0.0	0 2	3.80 MB	185.66 MB
367	(j) (T	unes	steve	4.0	0 10	22.03 MB	239.66 MB
371	1 A	ctivity Monitor	steve	2.8	2 2	20.11 MB	246.64 MB
368	🐔 iP	hoto	steve	0.0	0 3	33.39 MB	281.90 MB
374	ER T.	erminal	steve	0.0	0 4	12.98 MB	244.08 MB
360	SI SI	stemUlServer	steve	0.0	0 2	5.35 MB	227.74 MB
359	N D	ock	steve	0.0	0 2	6.43 MB	200.11 MB
	CPU	System Memory	Disk Ad	tivity	Disk Usage	Network	}
		_				CPU Usage	
% U	Iser: 4.50		Threads:	213			
% Syst	em: 4.00		Processes:	65			
% N	lice: 0.00						
	dle: 91.5					unitalita.	
	ule. 91.3	•					

	Queue operations		(Queue interface, versio	n 1
 void en -a.k.a. ad E front - a.k.a. E E deque - a.k.a. E boolean 	equeue (E item) d(E item) () peek() ue() remove() isEmpty() hethods in an interface, alle	ow multiple		<pre>lic interface Queue314<e> { //place item at back of this o public void enqueue(E item); //access item at front of this //pre: !isEmpty() public E front(); //remove item at front of this //pre: !isEmpty() public E dequeue(); public boolean isEmpty();</e></pre>	queue s queue
CS314	Queues	5	} CS314	Queues	6
 Implementing a Queue Given the internal storage container and choice for front and back of queue what are the Big O of the queue operations? 			with r and ta	Clicker 1 Ilementing a queue with a singly eferences to the first and last no ail) which end of the list should b queue in order to have all queue	odes (head be the front

enqueue front dequeue isEmpty	ArrayList	LinkedList (Singly Linked)	LinkedList (Doubly Linked)	 of the queue in order to have all queue operations O(1)? A. The front of the list should be the front of the queue. B. The back of the list should be the front of the queue. C. Either end will work to make all ops O(1). D. Neither end will allow all ops to be O(1).
CS314		Queues	7	CS314 Queues 8

Alternate Implementation	Application of Queues				
How about implementing a Queue with a mative amount	Radix Sort				
native array?	– radix is a synonym for <i>base</i> . base 10, base 2				
– Seems like a step backwards	Multi pass sorting algorithm that only looks at individual digits during each pass				
AWhack	• Use queues as <i>buckets</i> to store elements				
On the Side of the Head How You Can Be More Creative	 Create an array of 10 queues 				
	 Starting with the least significant digit place 				
	value in queue that matches digit				
	empty queues back into array				
Roger von Oech	repeat, moving to next least significant digit				
CS314 9	CS314 10				
Queues	Queues				
Radix Sort in Action: 1s place	Radix Sort in Action: 1s				
Radix Sort in Action: 1s place	Radix Sort in Action: 1s				
 Radix Sort in Action: 1s place original values in array 	Radix Sort in Action: 1s • original values in array				
Radix Sort in Action: 1s place • original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12	Radix Sort in Action: 1s original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 				
 Radix Sort in Action: 1s place original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place <u>9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12</u> 	Radix Sort in Action: 1s original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place 				
 Radix Sort in Action: 1s place original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place 	 Radix Sort in Action: 1s original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place <u>9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12</u> 				
 Radix Sort in Action: 1s place original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Array of Queues (all empty initially): 	 Radix Sort in Action: 1s original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Queues: 				
 Radix Sort in Action: 1s place original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 Array of Queues (all empty initially): 0 5 	Radix Sort in Action: 1s • original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Queues: 0 70, 40 5				
Radix Sort in Action: 1s place • original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Array of Queues (all empty initially): 0 5 1 6	Radix Sort in Action: 1s• original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12• Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12• Queues: 0 70, 405 6 86				
Radix Sort in Action: 1s place • original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12 • Array of Queues (all empty initially): 0 5 1 6 2 7	Radix Sort in Action: 1s• original values in array 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12• Look at ones place 9, 113, 70, 86, 12, 93, 37, 40, 252, 7, 79, 12• Queues: 0 70, 405 1 6 86 2 12, 252, 12• $37, 7$				

Radix So	ort in Action: 10s	Radix Sort in Action: 100s			
array	n order from 0 to 9 back	 Empty queues in order from 0 to 9 back into array 7, 9, 12, 12, 113, 37, 40, 252, 70, 79, 86, 93 			
70, 40, 12, 252, 12	2, 113, 93, 86, 37, 7, 9, 79		Now look at 100's place		
Now look at 10's	place		7,9,12,12, <u>1</u> 13,37,4	40, <u>2</u> 52, _70, _79, _86, _93	
<u>7</u> 0, <u>4</u> 0, <u>1</u> 2, 2 <u>5</u> 2, <u>1</u> 2	2, 1 <u>1</u> 3, <u>9</u> 3, <u>8</u> 6, <u>3</u> 7, _7, _9, <u>7</u> 9	• Queues:			
• Queues:			0 _7, _9, _12, _12, _37, _40, _7	70, _79, _86, _93 5	
0 _7, _9 1 <u>1</u> 2, <u>1</u> 2, 1 <u>1</u> 3 2 3 <u>3</u> 7 4 <u>4</u> 0	5 2 <u>5</u> 2 6 7 <u>7</u> 0, <u>7</u> 9 8 <u>8</u> 6 9 <u>9</u> 3		$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		
CS314	Queues	13	CS314 Queues	14	
Radix Sort in Action: Final Step			Radix Sor	t Code	
Empty queues in array	n order from 0 to 9 back	<pre>public static void sort(int[] da ArrayList<queue<integer>> = new ArrayList<queue for(int i = 0; i < 10; i++</queue </queue<integer></pre>	queues <integer>>();</integer>		

15

7, 9, 12, 12, 40, 70, 79, 86, 93, 113, 252

```
for (int i = 0; i < 10; i++)
        queues.add(new LinkedList<Integer>());
    int passes = numDigits(getMax(data));// helper methods
    for(int i = 0; i < passes; i++) {</pre>
        for(int j = 0; j < data.length; j++) {
            int digit = valueOfDigit(data[j], i);
            queues.get(digit).add(data[j]);
        }
        int pos = 0;
        for(Queue<Integer> q : queues) {
            while(!q.isEmpty())
                data[pos++] = q.remove();
        }
}CS314
                                                       16
                          Queues
```

CS314

Topic 17 Faster Sorting

"The bubble sort seems to have nothing to recommend it, except a catchy name and the fact that it leads to some interesting theoretical problems."

- Don Knuth



Previous Sorts

- Insertion Sort and Selection Sort are both average case O(N²)
- Today we will look at two faster sorting algorithms.
 - quicksort
 - mergesort

Fast Sorting

Properties of Sorting Algorithms

In place?

- Do we use another data structure or not?
- Program stack *typically* not considered another data structure if only using O(log N) space

Comparison?

- Works by comparing the items to be sorted to each other?
- How could we not?
- Stable?
 - Next slide!

CS314

Fast Sorting

3

Stable Sorting

- A property of sorts
- If a sort guarantees the relative order of equal items stays the same then it is a stable sort
- [7₁, 6, 7₂, 5, 1, 2, 7₃, -5] original data
 subscripts added for clarity
- [-5, 1, 2, 5, 6, 7₁, 7₂, 7₃] sorted data – result of stable sort
- Real world example:
 - sort a table in Wikipedia by one criteria, then another
 - sort by country, then by major wins

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Quicksort

- Created by C.A.R. (Tony) Hoare
- A divide and conquer approach
- 1. If the list has 0 or 1 elements it is sorted
- otherwise, pick any element p in the list. This is called the *pivot* value - If we are unlucky with the chosen pivot, things can go poorly.
- 3. *Partition* the list minus the pivot into two sub lists according to values less than or greater than the pivot. (equal values go to either)
- 4. return the quicksort of the first list followed by the quicksort of the second list

Fast Sorting

Quicksort in Action 39 23 17 90 33 72 46 79 11 52 64 5 71 Pick middle element as pivot: 46 Partition list 23 17 5 33 39 11 46 79 72 52 64 90 71 quick sort the less than list Pick middle element as pivot: 33 23 17 5 11 33

quicksort the less than list, base case quicksort the greater than list Pick middle element as pivot: 17 and so on....

guicksort the less than list, pivot now 5

23 17 11

5

Object tmp = a[index1];

{}

CS314

5

7

Fast Sorting

private static void swapReferences(Object[] a, int index1, int index2) {

```
Quicksort on Another Data Set
```

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
44	68	191	119	119	37	83	95	191	45	158	130	76	153	39	25
									I		1	I	1		

```
a[index1] = a[index2];
a[index2] = tmp;
    private void quicksort(Comparable[] data, int start, int stop) {
         if(start < stop) {
             int pivotIndex = (start + stop) / 2;
              // Place pivot at start position
              swapReferences(data, pivotIndex, start);
              Comparable pivot = data[start];
              // Begin partitioning
              int j = start;
              // from first to j are elements less than or equal to pivot
              // from j to i are elements greater than pivot
              // elements beyond i have not been checked yet
              for(int i = start + 1; i <= stop; i++ ) {
                  //is current element less than or equal to pivot
                  if (data[i].compareTo(pivot) <= 0) {
                      // if so move it to the less than or equal portion
                      j++;
                      swapReferences(data, i, j);
              //restore pivot to correct spot
              swapReferences(data, start, j);
              quicksort( data, start, j - 1 );
                                                   // Sort small elements
              quicksort( data, j + 1, stop ); // Sort large elements
            // else start >= stop, 0 or 1 element, base case, do nothing
CS314
                                Fast Sorting
```



Big O of Quicksort?

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Clicker 1				Clicker 2	
What are the best case and worst case Orders (Big O) for quicksort?			A. N		
Best	Worst		B. Y	es	
A. O(NlogN)	O(N ²)				
B. O(N ²)	O(N ²)				
C. O(N ²)	O(N!)				
D. O(NlogN)	O(NlogN)				
E. O(N)	O(NlogN)				
CS314	Fast Sorting	9	CS314	Fast Sorting	10

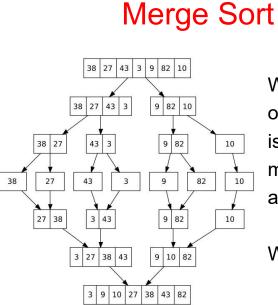
Merge Sort Algorithm

Don Knuth cites John von Neumann as the creator of this algorithm

- 1. If a list has 1 element or 0 elements it is sorted
- 2. If a list has more than 1 split into 2 separate lists
- 3. Perform this algorithm on each of those smaller lists
- 4. Take the 2 sorted lists and merge them together







When implementing one temporary array is used instead of multiple temporary arrays.

Why?

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Merge Sort code	Merge Sort Code	
<pre>/** * perform a merge sort on the elements of data * @param data data != null, all elements of data * are the same data type */ public static void mergeSort(Comparable[] data) { Comparable[] temp = new Comparable[data.length]; sort(data, temp, 0, data.length - 1); } private static void sort(Comparable[] data, Comparable[] temp,</pre>	<pre>private static void merge(Comparable[] data, Comparable[] temp,</pre>	
} CS314 Fast Sorting 13	CS314 Fast Sorting 1	
Clicker 3	Clicker 4	
What are the best case and worst case Orders (Big O) for mergesort? BestA. O(NlogN)O(N²)A. O(NlogN)O(N²)B. O(N²)O(N²)C. O(N²)O(N!)D. O(NlogN)O(NlogN)E. O(N)O(NlogN)	 Is mergesort always stable? A. No B. Yes 	

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15

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Fast Sorting

Clicker 5

You have 1,000,000 distinct items in random order that you will be searching. How many searches need to be performed before the data is changed to make it worthwhile to sort the data before searching?

A. ~40

B. ~100

C.~500

D. ~2,000

E. ~500,000

```
CS314
```

Fast Sorting

Comparison of Various Sorts (2001)

Num Items	Selection	Insertion	Quicksort
1000	0.016	0.005	0 ??
2000	0.059	0.049	0.006
4000	0.271	0.175	0.005
8000	1.056	0.686	0??
16000	4.203	2.754	0.011
32000	16.852	11.039	0.045
64000	expected?	expected?	0.068
128000	expected?	expected?	0.158
256000	expected?	expected?	0.335
512000	expected?	expected?	0.722
1024000	expected?	expected?	1.550

times in seconds

17

CS314	Fast Sorting

N 11	0 1 1	1 0	0.1.1.1		<u> </u>
Num Items	Selection	Insertion	Quicksort	Merge	Arrays.sort
1000	0.002	0.001	-	-	-
2000	0.002	0.001	-	-	-
4000	0.006	0.004	-	-	-
8000	0.022	0.018	-	-	-
16000	0.086	0.070	0.002	0.002	0.002
32000	0.341	0.280	0.004	0.005	0.003
64000	1.352	1.123	0.008	0.010	0.007
128000	5.394	4.499	0.017	0.022	0.015
256000	21.560	18.060	0.035	0.047	0.031
512000	86.083	72.303	0.072	0.099	0.066
1024000	???	???	0.152	0.206	0.138
2048000			0.317	0.434	0.287
4096000			0.663	0.911	0.601
8192000			1.375	1.885	1.246

Comparison of Various Sorts (2011) Comparison of Various Sorts (2020)

		-					
Num Items	Selection	Insertion	Quicksort	Mergesort	Arrays. sort(int)	Arrays.so rt(Integer)	Arrays. parallelSort
1,000	<0.001	<0.001	-	-	-	1	-
2,000	0.001	<0.001	-	-	-	-	-
4,000	0.004	0.003	-	-	-	-	Speeds
8,000	0.017	0.010	-	-	-	-	up????
16,000	0.065	0.040	0.002	0.002	0.003	0.011	0.007
32,000	0.258	0.160	0.002	0.003	0.002	0.008	0.003
64,000	1.110	0.696	0.005	0.008	0.004	0.011	0.001
128,000	4.172	2.645	0.011	0.015	0.009	0.024	0.002
256,000	16.48	10.76	0.024	0.034	0.018	0.051	0.004
512,000	70.38	47.18	0.049	0.068	0.040	0.114	0.008
1,024,000	-	-	0.098	0.143	0.082	0.259	0.017
2,048,000	-	-	0.205	0.296	0.184	0.637	0.035
4,096,000	-	-	0.450	0.659	0.383	1.452	0.079
8,192,000	-	-	0.941	1.372	0.786	3.354	0.148

 Concluding Thoughts Language libraries often have sorting algorithms in them Java Arrays and Collections classes C++ Standard Template Library Python sort and sorted functions Hybrid sorts when size of unsorted list or portion of array is small use insertion sort, otherwise use O(N log N) sort like Quicksort or Mergesort 	 Concluding Thoughts Sorts still being created! Timsort (2002) created for python version 2.3 now used in Java version 7.0+ takes advantage of real world data real world data is usually partially sorted, not totally random Library Sort (2006) Like insertion sort, 			
Fast Sorting 21	but leaves gaps for later elements Fast Sorting 22			

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Topic 18 Binary Trees

"A tree may grow a thousand feet tall, but its leaves will return to its roots."

-Chinese Proverb



Definitions

- A tree data structure
 - one entry point, the *root*
 - Each node is either a *leaf* or an *internal node*
 - An internal node has 1 or more children, nodes that can be reached directly from that internal node.
 - The internal node is said to be the *parent* of its child nodes

nodes indes indes leaf nodes

internal

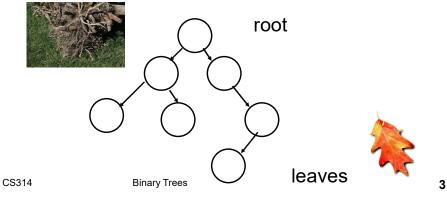
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Binary Trees

root node

Properties of Trees

- Only access point is the root
- All nodes, except the root, have one parent
 like the inheritance hierarchy in Java
- Traditionally trees drawn upside down

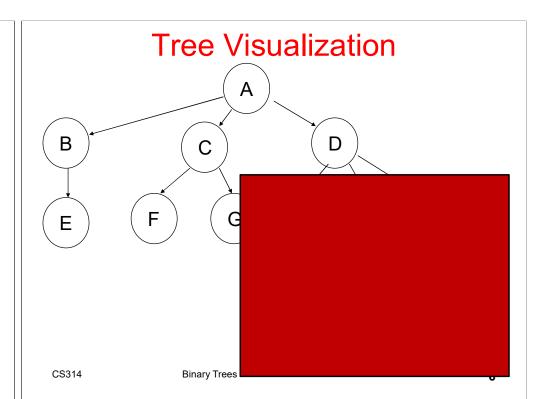


Properties of Trees and Nodes

root siblings: two nodes that have the same parent edge 0 edge: the link from one node to another 2 path length: the number of siblings edges that must be traversed to get from one 3 node to another 5 path length from root to this node is 3

More Properties of Trees

- *depth:* the path length from the root of the tree to this node
- height of a node: The maximum distance (path length) of any leaf from this node
 - a leaf has a height of 0
 - the height of a tree is the height of the root of that tree
 - what if only one node, the root?
 - what if empty? Discover OptionalInt
- descendants: any nodes that can be reached via 1 or more edges from this node
- ancestors: any nodes for which this node is a descendant



Clicker 1

What is the depth of the node that contains M on the previous slide?

A. 0

B. 1

- C. 2
- D. 3

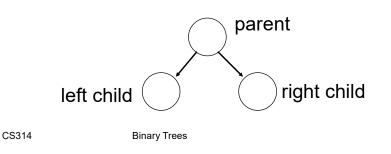
E. 4

Clicker 2 - Same tree, same choices What is the height of the node that contains D?

7

Binary Trees

- There are many variations on trees but we will start with *binary trees*
- binary tree: each node has at most two children
 - the possible children are usually referred to as the left child and the right child



Full Binary Tree	Clicker 3
full binary tree: a binary tree in which each node has 2 or 0 children	What is the maximum height of a full binary tree with 11 nodes?
	A. 3
	B. 5
	C. 7
	D. 10
	E. Not possible to have full binary tree with 11 nodes.
CS314 Binary Trees 9	CS314 Binary Trees 10

Complete Binary Tree

complete binary tree: a binary tree in which every level, except possibly the deepest is completely filled. At depth n, the height of the tree, all nodes are as far left as possible

Clicker 4

- What is the height of a complete binary tree that contains N nodes?
- A. O(1)
- B. O(logN)
- C. O(N^{1/2})
- D. O(N)

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- E. O(NlogN)
- Recall, order can be applied to any function. It doesn't just apply to running time.

Binary Trees

11

Binary Trees

Perfect Binary Tree

- perfect binary tree: a binary tree with all leaf nodes at the same depth. All internal nodes have exactly two children.
- a perfect binary tree has the maximum number of nodes for a given height
- ▶ a perfect binary tree has (2⁽ⁿ⁺¹⁾ 1) nodes where n is the height of the tree
 - height = $0 \rightarrow 1$ node
 - height = 1 -> 3 nodes
 - height = $2 \rightarrow 7$ nodes
 - height = 3 -> 15 nodes

```
CS314
```

Binary Trees

13

15

Binary Tree Traversals

- Many algorithms require all nodes of a binary tree be visited and the contents of each node processed or examined.
- There are 4 traditional types of traversals
 - preorder traversal: process the root, then process all sub trees (left to right)
 - in order traversal: process the left sub tree, process the root, process the right sub tree
 - post order traversal: process the left sub tree, process the right sub tree, then process the root
 - level order traversal: starting from the root of a tree, process all nodes at the same depth from left to right, then proceed to the nodes at the next depth.

```
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```

A Binary Node class

```
public class Bnode<E> {
     private E myData;
     private Bnode<E> myLeft;
     private Bnode<E> myRight;
```

```
public BNode();
public BNode(Bnode<E> left, E data,
     Bnode<E> right)
public E getData()
public Bnode<E> getLeft()
public Bnode<E> getRight()
```

```
public void setData(E data)
public void setLeft(Bnode<E> left)
public void setRight(Bnode<E> right)
```

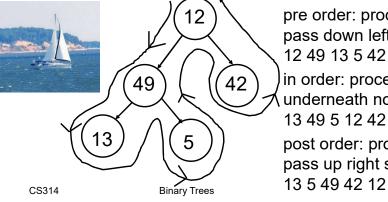
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Binary Trees

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Results of Traversals

- To determine the results of a traversal on a given tree draw a path around the tree.
 - start on the left side of the root and trace around the tree. The path should stay close to the tree.



pre order: process when pass down left side of node 12 49 13 5 42 in order: process when pass underneath node 13 49 5 12 42 post order: process when pass up right side of node

Clicker 5 - Tree	What is a the result of a post order traversal of the tree to the left?		Implement Traversals Implement preorder, inorder, and post order traversal Big O time and space? 			
ZGHJJ	A. ZCGAQHLDJ B. ZGCQLHJDA		Implement a level order traversal using a queue			
	C. ACZGDF		 Big O time and space? Implement a level order traversal without a 			
	D. ACDZGH					
	E. None of thes	se	queue			
			– target de	epth		
Binary Trees		17	CS314	Binary Trees	1	18

Breadth First Search Depth First Search

from NIST - DADS

- breadth first search: Any search algorithm that considers neighbors of a vertex (node), that is, outgoing edges (links) of the vertex's predecessor in the search, before any outgoing edges of the vertex
- depth first search: Any search algorithm that considers outgoing edges (links of children) of a vertex (node) before any of the vertex's (node) siblings, that is, outgoing edges of the vertex's predecessor in the search. Extremes are searched first.

Clicker 6

- Which traversal of a tree is a breadth first search?
- A. Level order traversal
- B. Pre order traversal
- C. In order traversal
- D. Post order traversal
- E. More than one of these

Binary Trees

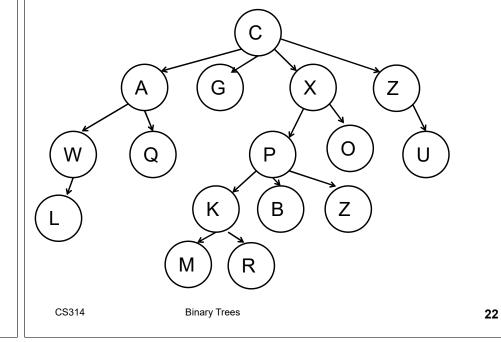
Breadth First

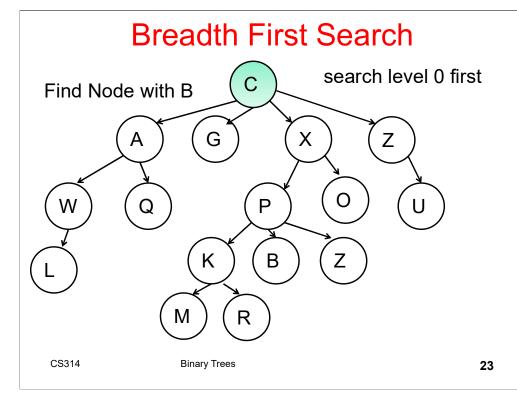
- A level order traversal of a tree could be used as a breadth first search
- Search all nodes in a level before going down to the next level

Binary Trees

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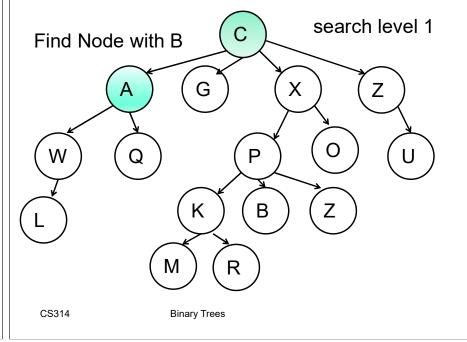
Breadth First Search of Tree



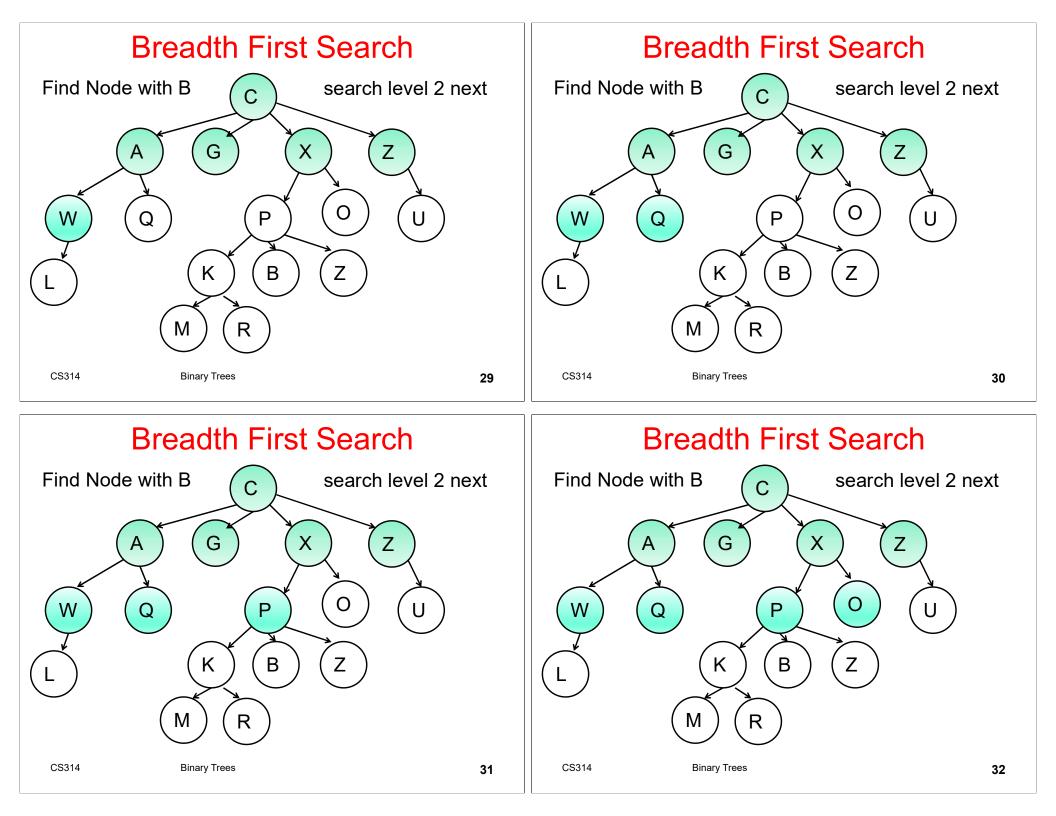


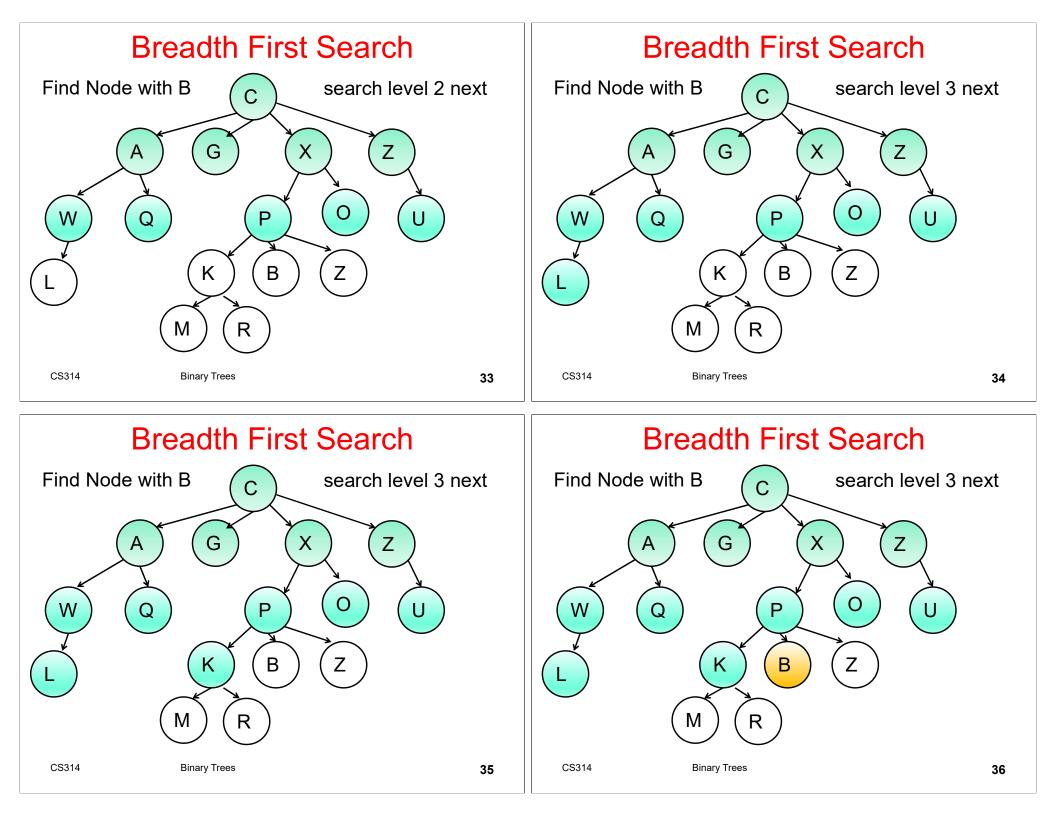
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Breadth First Search



Breadth First Search Breadth First Search search level 1 search level 1 С С Find Node with B Find Node with B G Х Ζ G Х Ζ A 0 0 Ρ Q Ρ U W Q U W В Ζ В Ζ Κ Κ L Μ Μ R R CS314 **Binary Trees** 25 CS314 **Binary Trees** 26 **Breadth First Search Breadth First Search** search level 1 Find Node with B search level 1 next С С Find Node with B G Х G Х Ζ Α Ζ А 0 0 Q Ρ U Q Ρ U W W Ζ Ζ В В Κ Κ L Μ Μ R R CS314 **Binary Trees** CS314 **Binary Trees** 27 28





BFS - DFS

- Breadth first search typically implemented with a Queue
- Depth first search typically implemented with a stack, implicit with recursion or iteratively with an explicit stack

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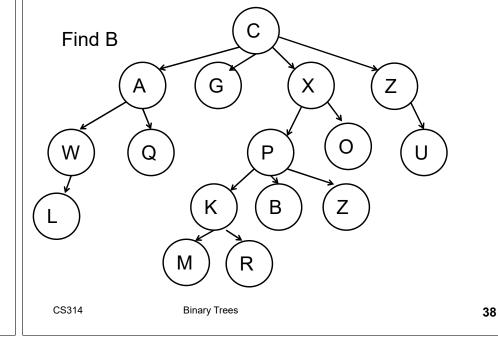
which technique do I use?

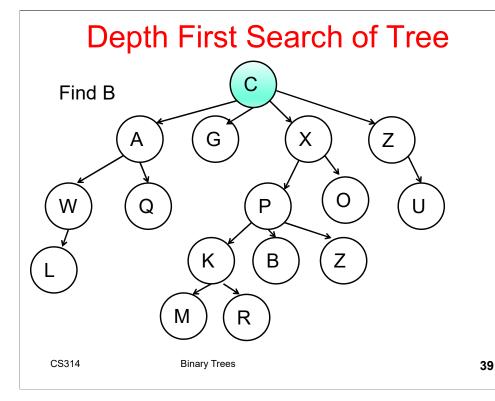
Binary Trees

- depends on the problem

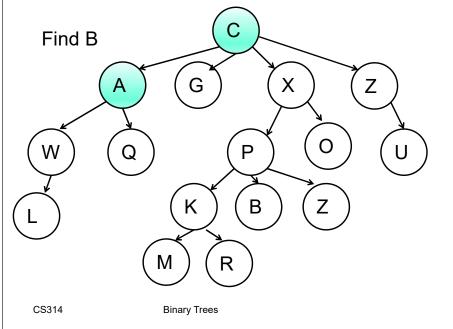
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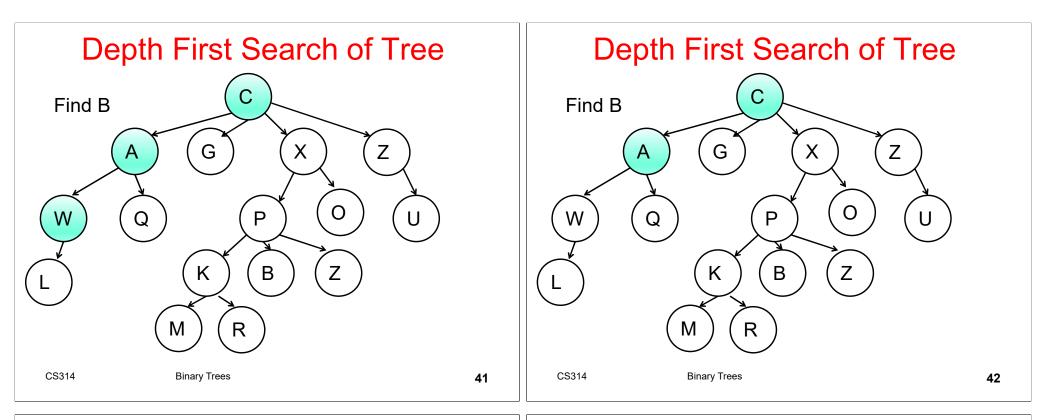
Depth First Search of Tree





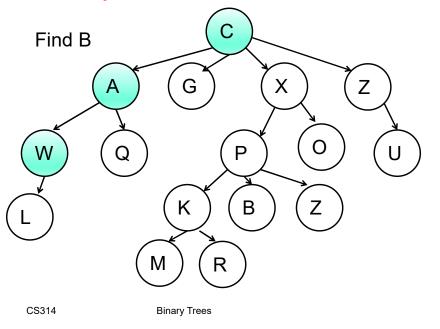
Depth First Search of Tree



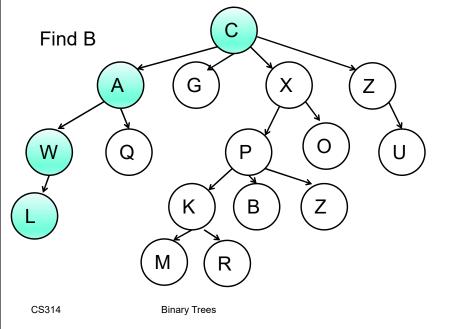


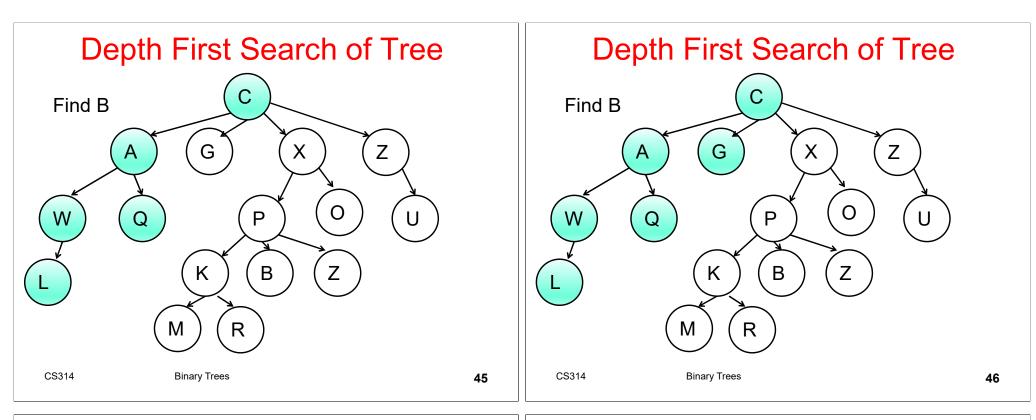
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Depth First Search of Tree

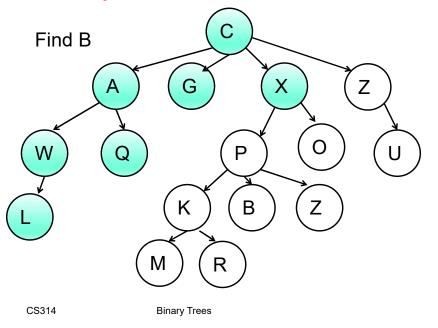


Depth First Search of Tree

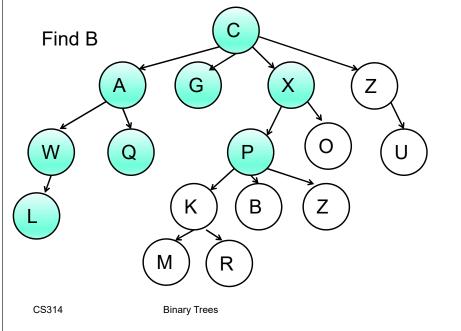


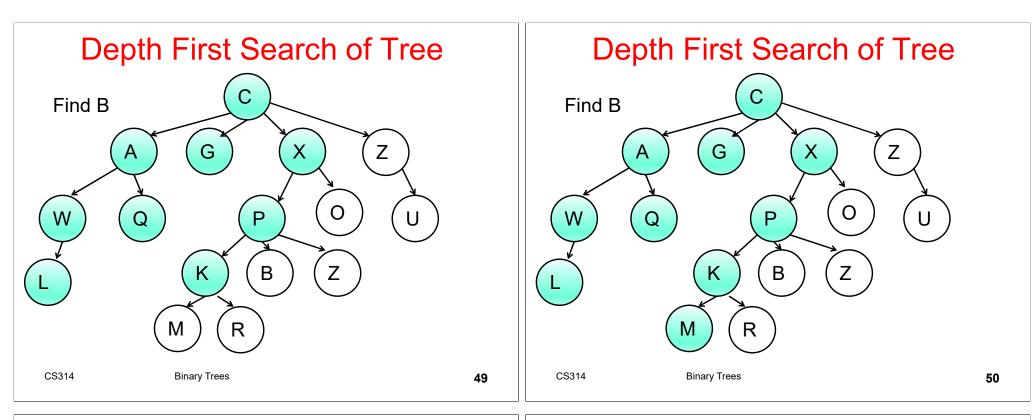


Depth First Search of Tree

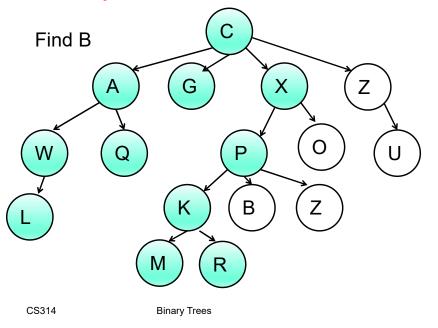


Depth First Search of Tree

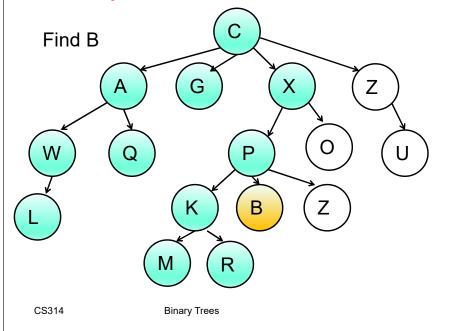




Depth First Search of Tree



Depth First Search of Tree



Topic 19 Binary Search Trees

"Yes. Shrubberies are my trade. I am a shrubber. My name is 'Roger the Shrubber'. I arrange, design, and sell shrubberies."

-Monty Python and The Holy Grail



The Problem with Linked Lists

- Accessing a item from a linked list takes O(N) time for an arbitrary element
- Binary trees can improve upon this and reduce access to O(log N) time for the average case
- Expands on the binary search technique and allows insertions and deletions
- Worst case degenerates to O(N) but this can be avoided by using balanced trees (AVL, Red-Black)

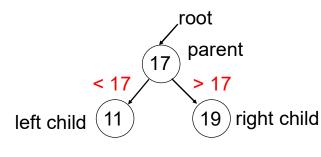
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Binary Search Trees

2

Binary Search Trees

- A binary search tree is a binary tree in which every node's left subtree holds values less than the node's value, and every right subtree holds values greater than the node's value.
- A new node is added as a leaf.



BST Insertion

Add the following values one at a time to an initially empty binary search tree using the simple algorithm:

50 90 20 78 10 20 28 -25

What is the resulting tree?

Traversals	Clicker 1							
 What is the result of an inorder traversal of the resulting tree? How could a preorder traversal be useful? 	 After adding N distinct elements in random order to a Binary Search Tree what is the expected height of the tree? (using the simple insertion algorithm) A. O(logN) B. O(N^{1/2}) C. O(N) D. O(NlogN) E. O(N²) 							
CS314 Binary Search Trees 5	CS314 Binary Search Trees 6							
Clicker 2	Worst Case Performance							
After adding N distinct elements to a Binary Search Tree what is the worst case height of the tree? (using the simple insertion algorithm)	Insert the following values into an initially empty binary search tree using the simple, naïve algorithm:							

A. O(logN)

- B. O(N^{1/2})
- C. O(N)
- D. O(NlogN)
- E. O(N²)

2 3 5 7 11 13 17

- What is the height of the tree?
- What is the worst case height of a BST?

7

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<pre>Node for Binary Search Trees public class BSTNode<e comparable<e="" extends=""> { private Comparable<e> myData; private BSTNode<e> myLeft; private BSTNode<e> myRightC; public BinaryNode(E item) { myData = item; } }</e></e></e></e></pre>	 More on Implementation Many ways to implement BSTs Using nodes is just one and even then many options and choices
<pre>public E getValue() { return myData; } public BinaryNode<e> getLeft() { return myLeft; }</e></pre>	<pre>public class BinarySearchTree<e comparable<e="" extends="">>> { private BSTNode<e> root; private int size;</e></e></pre>
<pre>public BinaryNode<e> getRight() { return myRight; } public void setLeft(BSTNode<e> b) { myLeft = b; } // setRight not shown CS314 } BinarySearchTrees</e></e></pre>	9 CS314 Binary Search Trees 10

Add an Element, Recursive

Add an Element, Iterative

Clicker 3 Performance of Binary Trees What are the best case and worst case order For the three core operations (add, access, to add N distinct elements, one at a time, to remove) a binary search tree (BST) has an an initially empty binary search tree using the average case performance of O(log N) simple add algorithm? Even when using the naïve insertion / // given int[] data **Best** Worst removal algorithms // no duplicates in no checks to maintain balance Α. O(N)O(N)// data BST<Integer> b = - balance achieved based on the randomness of B. O(NlogN)O(NlogN)new BST<Integer>(); the data inserted for(int x : data) O(NlogN) C. O(N)b.add(x);D. O(NlogN) $O(N^2)$ Ε. $O(N^2)$ O(N)CS314 **Binary Search Trees** 13 14 Remove an Element Properties of a BST The minimum value is in the left Five (four?) cases most node - not present

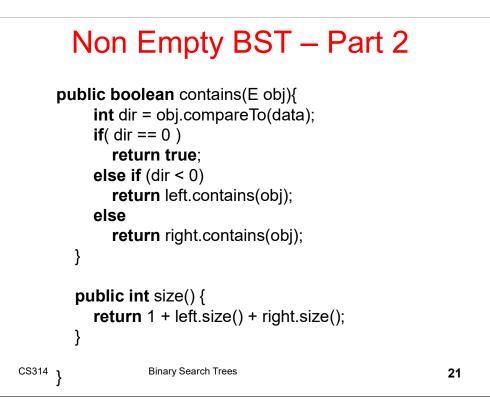
- The maximum value is in the right most node
 - –useful when removing an element from the BST

- node is a leaf, 0 children (easy)

- node has 1 child, left or right (easy)

- node has 2 children ("interesting")

```
Alternate Implementation
                                                                                      BST Interface
  In class examples of dynamic data structures
   have relied on null terminated ends.
                                                                    public interface BST<E extends
                                                                                        Comparable<? super E>> {
    - Use null to show end of list or no children
  Alternative form
                                                                       public int size();
    - use structural recursion and polymorphism
                                                                       public boolean contains(E obj);
                                                                       public BST<E> add(E obj);
                                                                     }
   CS314
                    Binary Search Trees
                                                                      CS314
                                                                                       Binary Search Trees
                                                           17
                                                                                                                              18
                                                                            Non Empty BST – Part 1
                      EmptyBST
                                                                    public class NEBST <E extends Comparable<? super E>> implements BST<E> {
public class EmptyBST<E extends Comparable<? super E>>
                                                                     private E data;
    implements BST<E> {
                                                                     private BST left;
                                                                     private BST right;
  private static final EmptyBST theOne = new EmptyBST();
                                                                     public NEBST(E d) {
                                                                       data = d;
  private EmptyBST() {}
                                                                       right = EmptyBST.getEmptyBST();
                                                                       left = EmptyBST.getEmptyBST();
                                                                     3
  public static EmptyBST getEmptyBST(){ return theOne; }
                                                                     public BST add(E obj) {
  public BST<E> add(E obj) { return new NEBST(obj); }
                                                                       int direction = obj.compareTo( data );
                                                                       if (direction < 0)
                                                                        left = left.add(obj);
  public boolean contains(E obj) { return false; }
                                                                       else if (direction > 0)
                                                                        right = right.add ( obj );
                                                                       return this:
  public int size() { return 0; }
   CS314
                    Binary Search Trees
                                                                      CS314
                                                                                       Binary Search Trees
                                                           19
                                                                                                                              20
```





Topic 20 <mark>Red</mark> Black Trees



"Welcome to L.A.'s Automated Traffic Surveillance and Control Operations Center. See, they use video feeds from intersections and specifically designed algorithms to predict traffic conditions, and thereby control traffic lights. So all I did was come up with my own... **kick ass algorithm** to sneak in, and now we own the place."

-Lyle, the Napster, (Seth Green), The Italian Job

Red Black Trees were created by Leonidas J. Guibas and Robert Sedgewick in 1978

Clicker 1

2000 elements are inserted one at a time into an initially empty binary search tree using the simplenaive algorithm. What is the maximum possible height of the resulting tree?

A. 1

B. 11

C. 21

D. 500

E. 1999

CS314

CS314

Red Black Trees

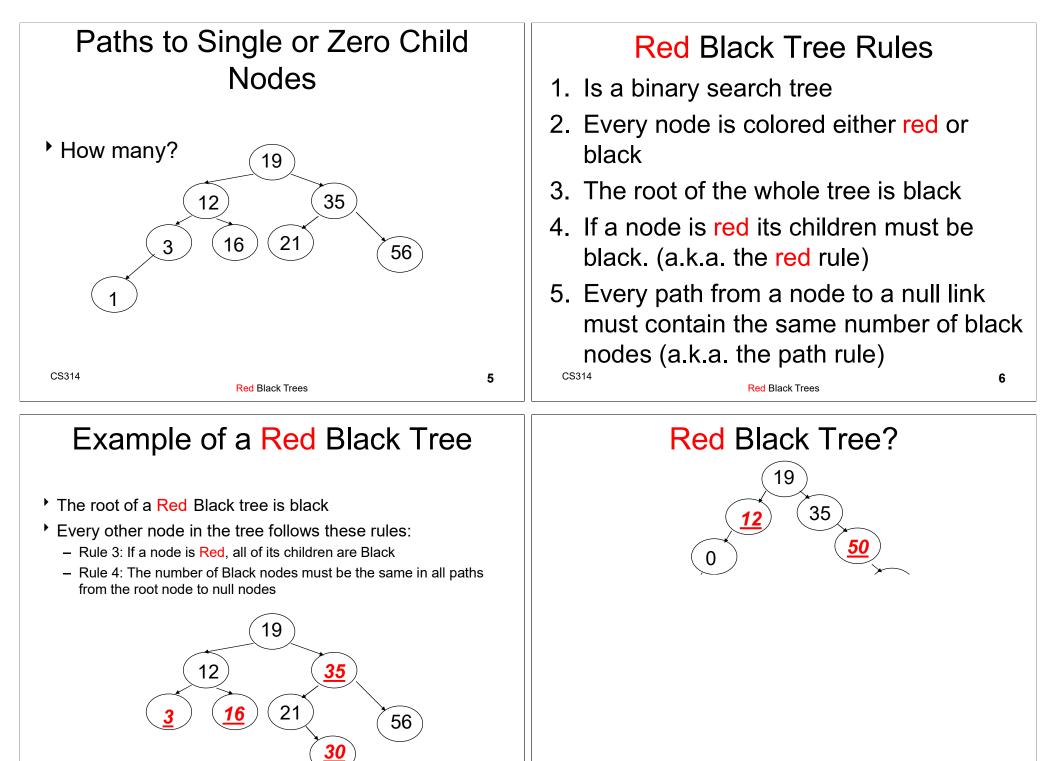
2

Binary Search Trees

- Average case and worst case Big O for
 - insertion
 - deletion
 - access
- Balance is important. Unbalanced trees give worse than log N times for the basic tree operations
- Can balance be guaranteed?

Red Black Trees

- A BST with more complex algorithms to ensure balance
- Each node is labeled as Red or Black.
- Path: A unique series of links (edges) traverses from the root to each node.
 - The number of edges (links) that must be followed is the path length
- In Red Black trees paths from the root to elements with 0 or 1 child are of particular interest



CS314

Red Black Trees

8

7

CS314

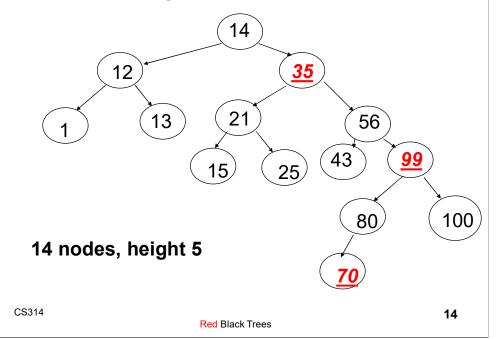
Red Black Trees

	Clicker 2 on the previous slide a bin ? Is it a red black tree? Red-Black? No Yes No	ary	Red Black Tree? 19 3 3 16 3
D. Yes	Yes Red Black Trees	9	Perfect? Full? CS314 Red Black Trees 10
	Clicker 3 on the previous slide a bin ? Is it a red black tree? Red-Black? No Yes No Yes	ary	 Implications of the Rules If a Red node has any children, it must have two children and they must be Black. (Why?) If a Black node has only one child that child must be a Red leaf. (Why?) Due to the rules there are limits on how unbalanced a Red Black tree may become. on the previous example may we hang a new node off of the leaf node that contains 0?
CS314	Red Black Trees	11	CS314 12 Red Black Trees

Properties of Red Black Trees

- If a Red Black Tree is complete, with all Black nodes except for Red leaves at the lowest level the height will be minimal, ~log N
- To get the max height for N elements there should be as many Red nodes as possible down one path and all other nodes are Black
 - This means the max height would b **approximately** 2 * log N (don't use this as a formula)
 - typically less than this
 - see example on next slide
 - interesting exercise, draw max height tree with N nodes

Max Height Red Black Tree

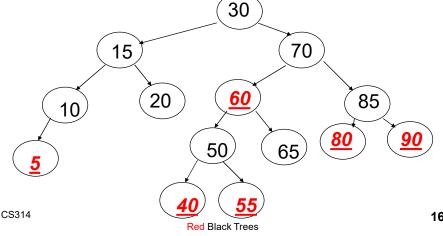


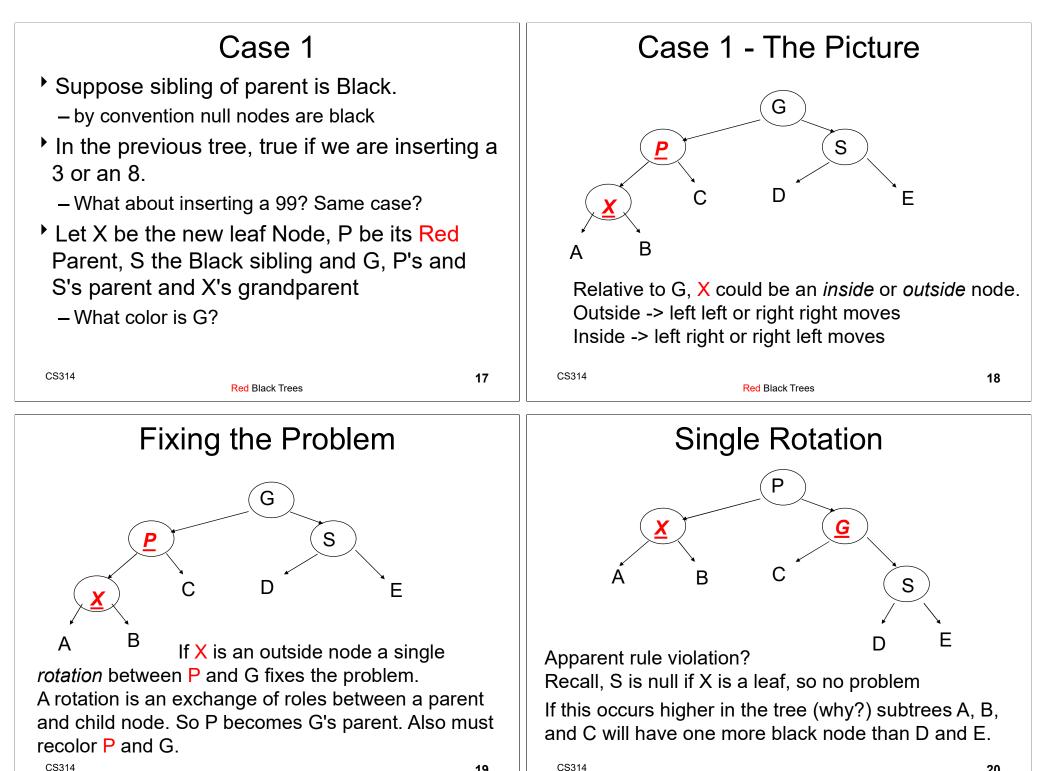
Maintaining the **Red** Black Properties in a Tree

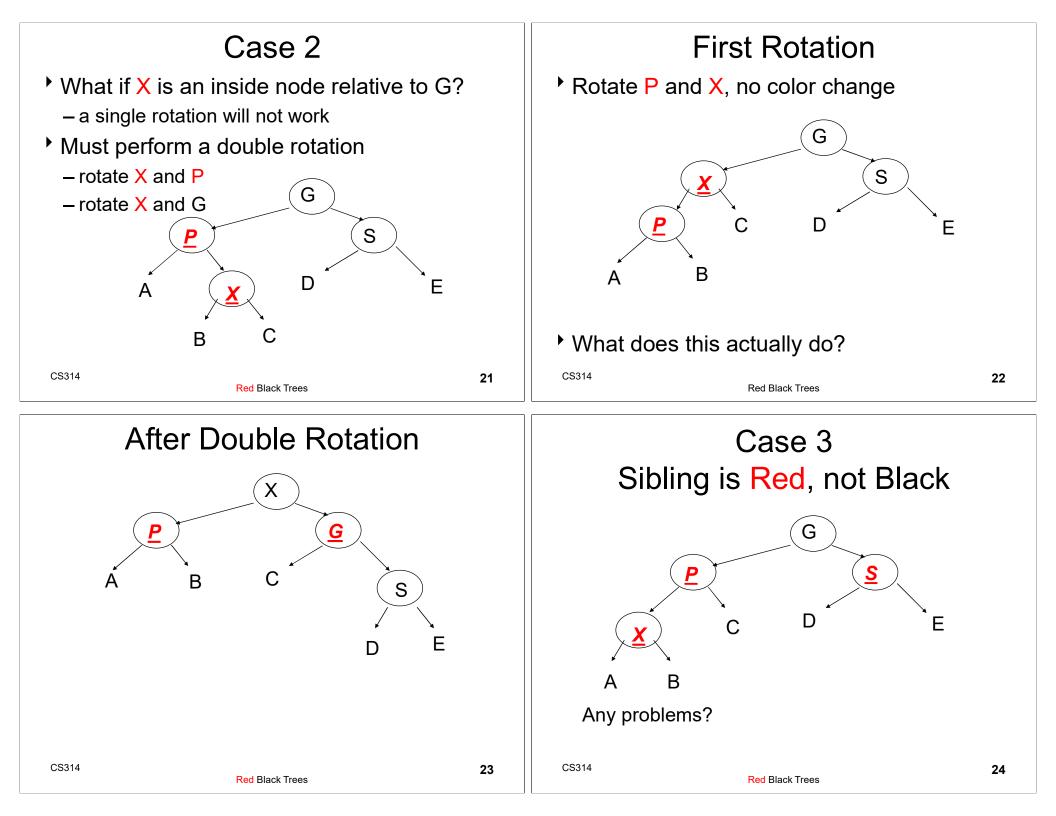
- Insertions
- Must maintain rules of Red Black Tree.
- New Value always in a new leaf, to start
 - can't be black or we will violate rule 4
 - therefore the new leaf must be red
 - If parent is black, done (trivial case)
 - if parent red, things get interesting because a red leaf with a red parent violates rule 3

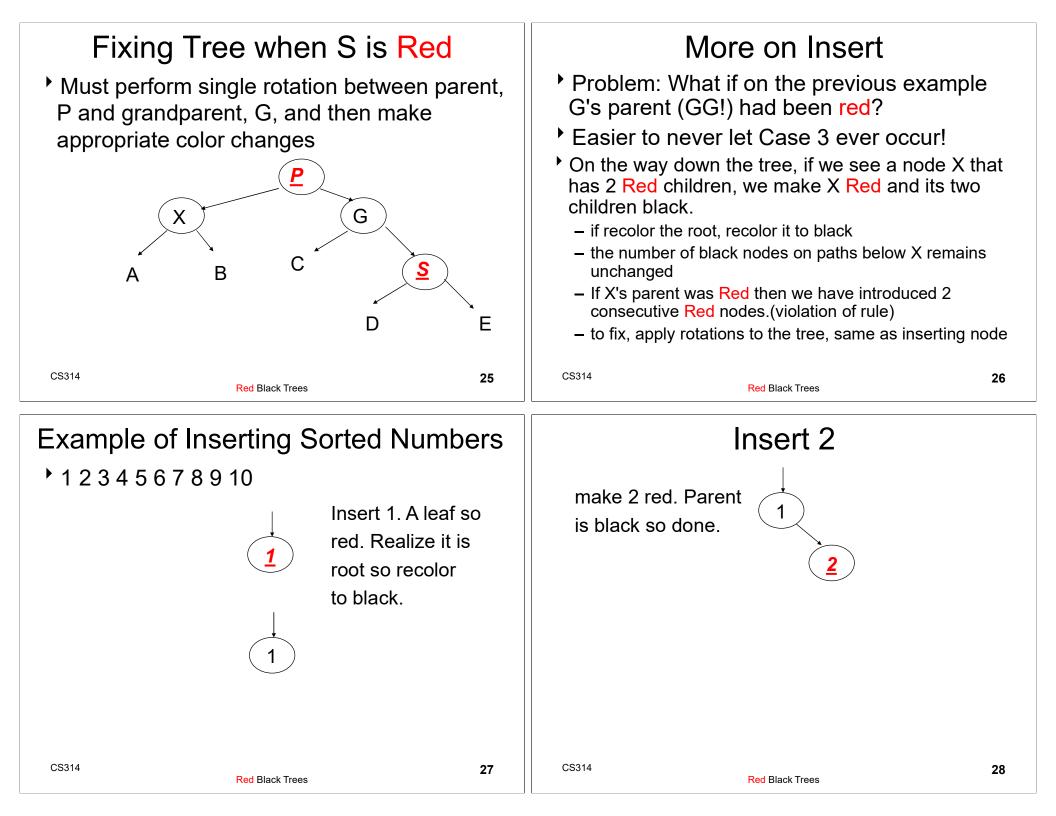
Insertions with Red Parent - Child

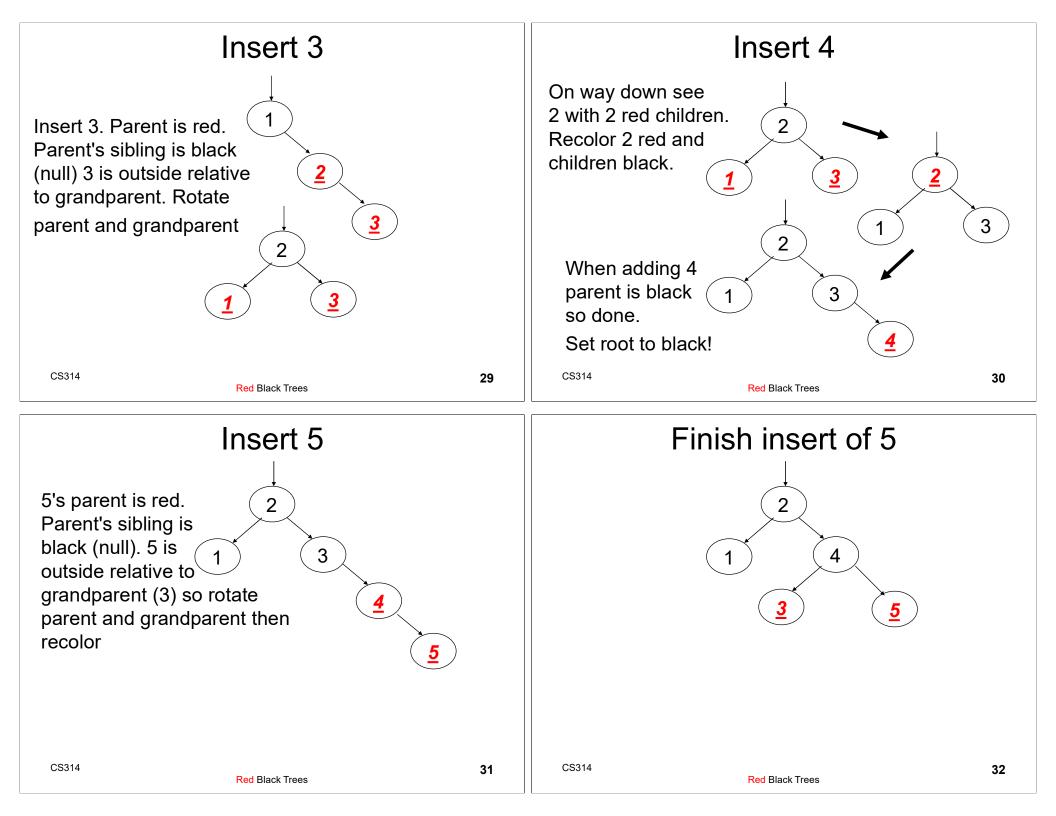
Must modify tree when insertion would result in Red Parent - Child pair using color changes and rotations.

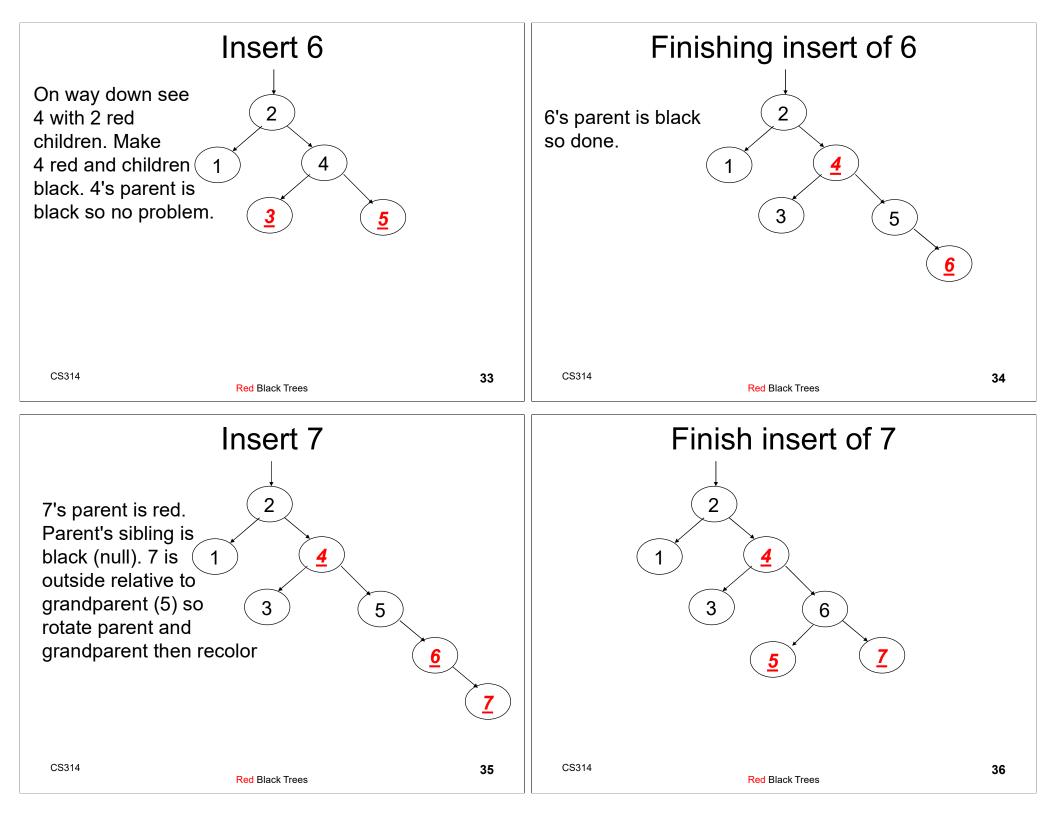


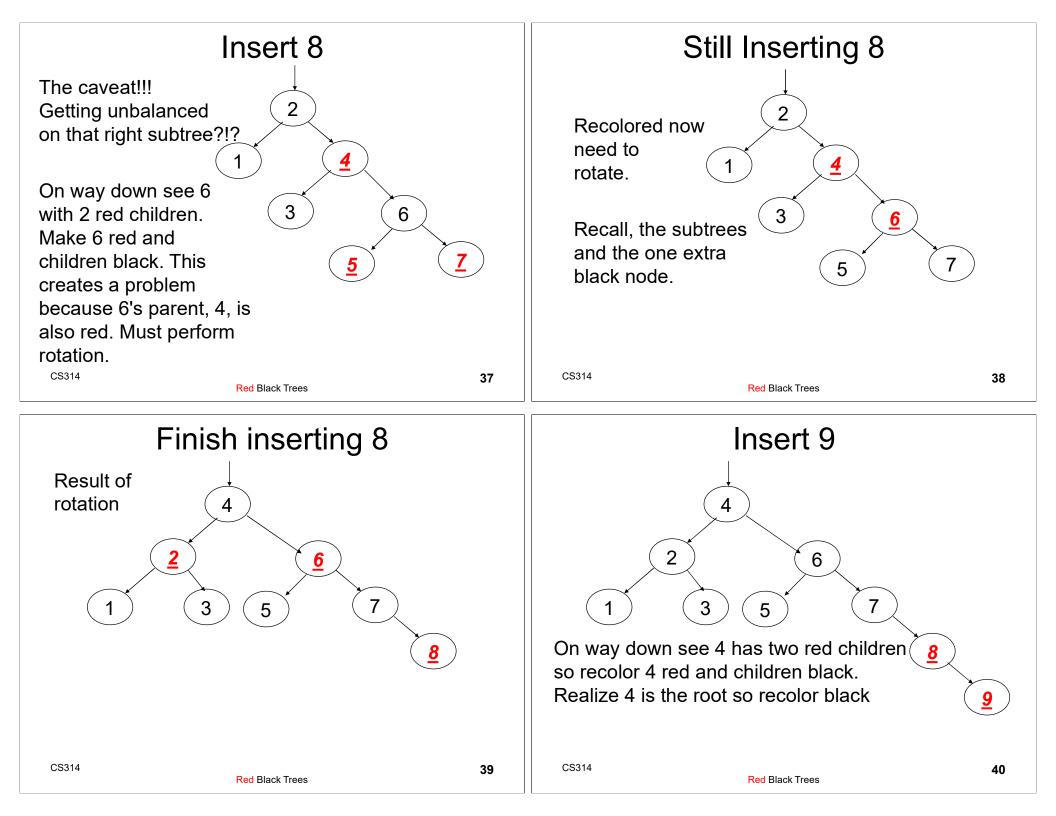


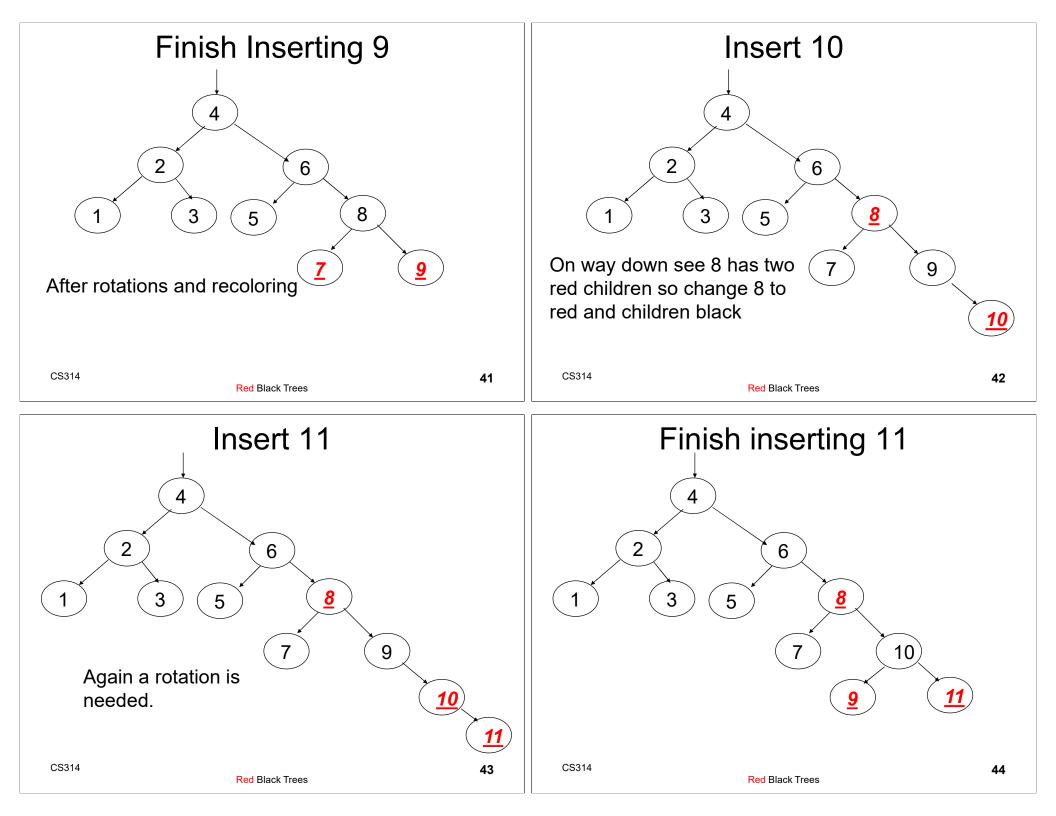








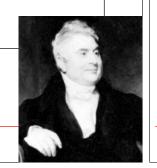




Topic 21: Huffman Coding

The author should gaze at Noah, and ... learn, as they did in the Ark, to crowd a great deal of matter into a very small compass.

Sydney Smith, Edinburgh Review



3

Agenda

- Encoding
- Compression
- Huffman Coding





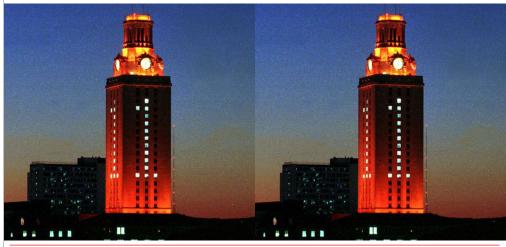
- UTCS
- 85 84 67 83
- 01010101 01010100 01000011 01010011
- What is stored in a jpg file? A text file? A Java file? A png file? A pdf file? An mp3 file? An mp4 file? An excel spreadsheet file? A zip file?
- open a bitmap in a text editor

	Binary	Oct	Dec	Hex	Glyph	Binary	Oct	Dec	Hex	Glyph		Binary	Oct	Dec	Hex	Glyph
	010 0000	040	32	20	(space)	0000 0000	100	64	40	@		110 0000	140	96	60	2
	010 0001	041	33	21	1	100 0001	101	65	41	A		110 0001	141	97	61	а
	010 0010	042	34	22	· B)	100 0010	102	66	42	В		110 0010	142	98	62	b
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	010 0100	044	36	24	\$	100 0100	104	68	44	D		110 0100	144	100	64	d
	010 0101	045	37	25	%	100 0101	105	69	45	E		110 0101	145	101	65	е
	010 0110	046	38	26	&	100 0110	106	70	46	F		110 0110	146	102	66	f
	010 0111	047	39	27	1 5	100 0111	107	71	47	G		110 0111	147	103	67	g
	010 1000	050	40	28	(100 1000	110	72	48	Н		110 1000	150	104	68	h
	010 1001	051	41	29)	100 1 <mark>00</mark> 1	111	73	49	1		110 1001	151	105	69	i
	010 1010	052	42	2A	*	100 1010	112	74	4A	J		110 1010	152	106	6A	j
	010 1011	053	43	2B	+	100 1011	113	75	4B	К		110 1011	153	107	6B	ĸ
	010 1100	054	44	2C	140	100 1100	114	76	4C	L		110 1100	154	108	6C	T
	010 1101	055	45	2D	12	100 1101	115	77	4D	М		110 1101	155	109	6D	m
-	010 1110	056	46	2E	125	100 1110	116	78	4E	N		110 1110	156	110	6E	n
	010 1111	057	47	2F	1	100 1111	117	79	4F	0		110 1111	157	111	6F	0
	011 0000	060	48	30	0	101 0000	120	80	50	Р		111 0000	160	112	70	р
	011 0001	061	49	31	1	101 0001	121	81	51	Q		<mark>111 0001</mark>	161	113	71	q
	<mark>011 001</mark> 0	062	50	32	2	101 0010	100	92	52	R		111 0010	162	114	72	r
	011 0011	063	51	33	3	101 0011	123	83	53	5		111 0011	163	115	73	s
	011 0100	064	52	34	4	101 0100	124	84	54	Т)	111 0100	164	116	74	t
	011 0101	065	53	35		101 0101	125	85	55	U		111 0101	165	117	75	u
	011 0110	066	54	36	6	101 0110	126	86	50	V		111 0110	166	118	76	v
	011 0111	067	55	37	7	101 0111	197	87	57	W		111 0111	167	110	77	1M

Text File	Text File???									
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This eBook is for the use of anyone anywhere at almost no restrictions whatsoever. You may cop re-use it under the terms of the Project Gutenb with this eBook or online at www.gutenberg.net	67 27 73 20 54 68 65 20 41 64 76 65 6E 74 75 72 g's The Adventure 65 73 20 6F 66 20 53 68 65 72 6C 6F 63 6B 20 48 es of Sherlock 6F 6F 6C 6D 65 73 2C 20 62 79 20 41 72 74 68 75 72 olmes, by Arthur 20 43 6F 6E 61 6E 20 44 6F 79 6C 65 0D 0A OD 0A Conan Doyle<									
Title: The Adventures of Sherlock Holmes	72 20 74 68 65 20 75 73 65 20 6F 66 20 61 6E 79 r the use of an 6F 6E 65 20 61 6E 79 77 68 65 72 65 20 61 74 20 one anywhere at									
Author: Arthur Conan Doyle	6E 6F 20 63 6F 73 74 20 61 6E 64 20 77 69 74 68 no cost and wit 0D 0A 61 6C 6D 6F 73 74 20 6E 6F 20 72 65 73 74almost no res									
Posting Date: April 18, 2011 [EBook #1661] First Posted: November 29, 2002	72 69 63 74 69 6F 6E 73 20 77 68 61 74 73 6F 65 rictions whatso									
	5									

Bitmap and JPEG File

Bitmap File????



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	03	01	04	07	05	09	0Ĉ	0A	07	0A	08	02	05	03	00	04	
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	FF	94	FD	FF	À5	ÀÀ	9F	6B	02	03	ÔÓ.	οō.	00	16	42	81	ÿ∎ýÿ¥ª∎kB
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	0C	0B	0C	13	10	06	0D	08	ōō	07	00	00	04	00	00	01	
	00	02	07	06	04	09	08	00	04	03	00	03	02	05	0A	09	
	06	OB	0Å	01	06	05	12	06	12	03	05	0D	00	0E	00	28	
	6C	17	E5	FA	7B	EE	FF	ÀÀ	FB	FB	DD	F5	F8	DB	FF	FD	l.åú{îÿªûûŶõøØÿý
	C5	FA	F4	B3	F7	FA	BC	F9	FD	D9	FF	FF	FÅ	FC	F5	F8	Åúô³÷ú¼ùýÙÿÿúüõø
	FF	FB	E9	FF	F8	CC	C9	FC	82	F1	FA	C8	FF	F4	F5	FB	yûéyølÉu ñúÉyôôû
	F5	E8	F9	FD	DA	FF	FF	E8	62 FF	FF	FB	BC	D7	CE	31	50	öèùýÚÿÿèÿÿû¼×Î1P
	2B	01	16	00	00	02	00	01	03	04	09	08	04	OE	OD	03	그래도 잘 넣어야 한 것이 많은 것이 없는 것이 없는 것이 없는 것이 없다. 것이 없는 것이 없다. 것이 없는 것이 않는 것이 않은 것이 없는 것이 않은 것이 없는 것이 없 않 않 않 않이
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JPEG File	JPEG VS BITMAP
<image/>	Image: Tower-number1-1024x768.bmp Bitmap image 2,305 KB Image: Tower-number1-1024x768.jpg JPEG Image 283 KB Image: Description of the state o
Encoding Schemes	Why So Many Encoding / Decoding Schemes?
 "It's all 1s and 0s" What do the 1s and 0s mean? 50 121 109 ASCII -> 2ym Red Green Blue-> dark teal? 	 Image file formats: bmp, png, jpg, gif, tiff, svg, cgm, pgm How StanDards Proliferate: (see Arc characters, characters encodings, instant messacing, erc) SITUATION: THERE ARE H COMPETING STANDARDS, VEAH! STANDARDS, STANDARDS, SKCD, Standards: https://xkcd.com/927/

Agenda	 Compression Compression: Storing the same information but in a form that takes less memory lossless and lossy compression Recall: 							
 Encoding Compression Huffman Coding 								
	Tower-number1-1024x768.bmp Bitmap image 2,305 KB Tower-number1-1024x768.jpg JPEG Image 283 KB							
	13							
Lossy Artifacts	Compression							
Sam M 228	• 000000000000000000000000000000000000							
Sam M 321	• 0 00100000 1 00011110							

Why Bother?

• Is compression really necessary?





List Price: \$139.99 \rightarrow Prime FREE One-Day & FREE Returns You Save: \$20.00 (15%) Get \$70 off Instantly: Pay \$39.99 \$109.99 Via Gard. No annual fee. Free Amazon tech support included \rightarrow



5 Terabytes. ~5,000,000,000,0000 bytes

Little Pipes and Big Pumps

Home Internet Access

- 400 Mbps roughly \$65 per month
- 12 months * 3 years * \$115 =
- 400,000 000 bits /second
 5 * 10⁷ bytes / sec

CPU Capability

- \$2,000 for a good laptop or desktop
- Intel® Core™ i9-7900X
- Assume it lasts 3 years.

Memory bandwidth 40 GB / sec

 $= 4.0 * 10^{10}$ bytes / sec

on the order of 6.4 10¹¹instructions / second

Clicker 1

• With computer storage so cheap, is compression really necessary?

A. No

B. Yes

17

19

C. It Depends

Mobile Devices?

Cellular Network

- Your mileage may vary
- Mega bits per second
- AT&T
 17 mbps download, 7 mbps upload
- T-Mobile & Verizon
 12 mbps download, 7 mbps upload
- 17,000,000 bits per second = 2.125 x 10⁶ bytes per second http://tinyurl.com/g6o7wan

iPhone CPU

• Apple A6 System on a Chip

18

- Coy about IPS
- 2 cores
- Rough estimates: 1 x 10¹⁰ nstructions per second



Huffman Coding

- Proposed by Dr. David A. Huffman
 - Graduate class in 1951 at MIT with Robert Fano
 - term paper or final
 - term paper: prove min bits needed for binary coding of data
 - A Method for the Construction of Minimum Redundancy Codes
- Applicable to many forms of data transmission
 - Our example: text files
 - still used in fax machines, mp3 encoding, others

The Basic Algorithm

- Huffman coding is a form of statistical coding
- Not all characters occur with the same frequency, in typical text files. (can be true when reading raw bytes as well)
- Yet in ASCII all characters are allocated the same amount of space
 - 1 char = 1 byte, be it <mark>e</mark> or X
 - -fixed width encoding

The Basic Algorithm

- Any savings in tailoring codes to frequency of character?
- Code word lengths are no longer fixed like ASCII or Unicode
- Code word lengths vary and will be shorter for the more frequently used characters
- Examples use characters for clarity, but in reality just read raw bytes from file.

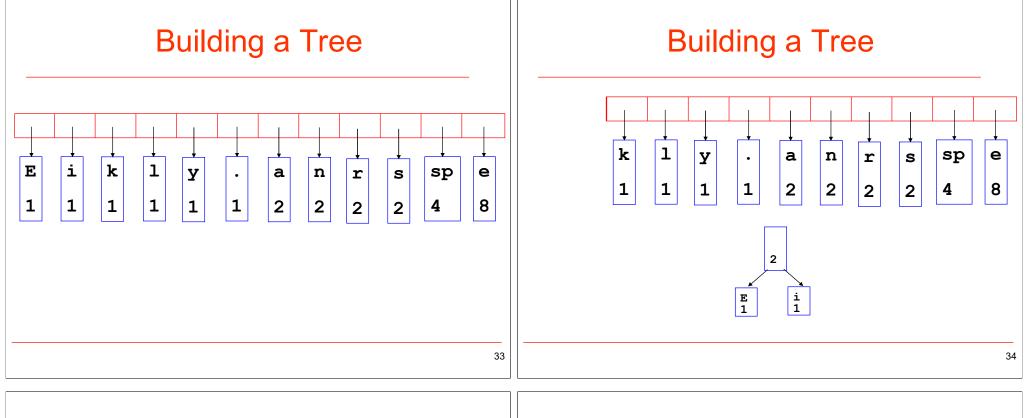
The Basic Algorithm

- Scan file to be compressed and determine frequency of all values.
- Sort or prioritize values based on frequency in file.
- Build Huffman code tree based on prioritized values.
- 4. Perform a traversal of tree to determine new codes for values.
- 5. Scan file again to create new file using the new Huffman codes

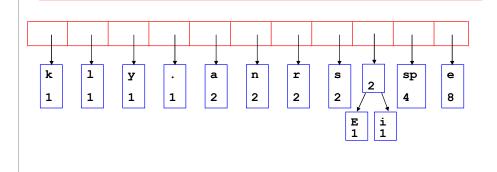
Building a Tree
Scan the original textBuilding a Tree
Scan the original text• Consider the following short text
Eerie eyes seen near lake.Eerie eyes seen near lake.• Determine frequency of all numbers (values
or in this case characters) in the textE e r i space
y s n a r l k .

25

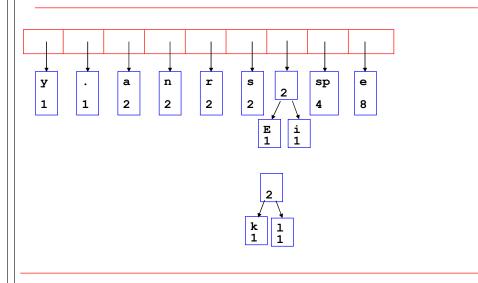
Building a Tree Scan the original textEerie eyes seen near lake.Eerie eyes seen near lake.• What is the frequency of each character in the text?Char Freq. Char Freq.E11211k1r2ni1a2i1a2i1i1	 Building a Tree Prioritize values from file Create binary tree nodes with a value and the frequency for each value Place nodes in a priority queue The <i>lower</i> the frequency, the <i>higher</i> the priority in the queue
29	30
 Building a Tree The queue after enqueueing all nodes 	 Building a Tree While priority queue contains two or more
frontbackEik1y.anrsspe1111122248• Null Pointers are not shown• sp = space• See slide 67 for actual PQ and tree formedby following assignment specification31	 nodes Create new node Dequeue node and make it left child Dequeue next node and make it right child Frequency of new node equals sum of frequency of left and right children New node does not contain value Enqueue new node back into the priority queue

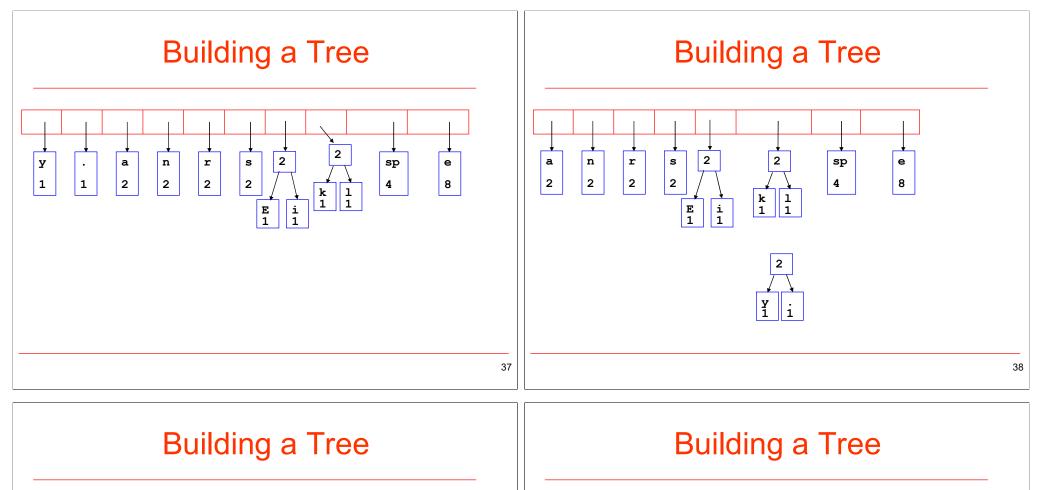


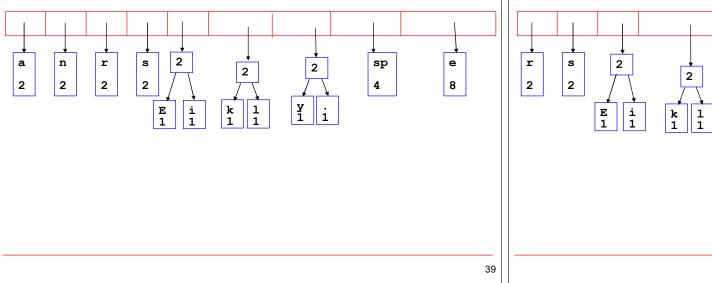












sp

4

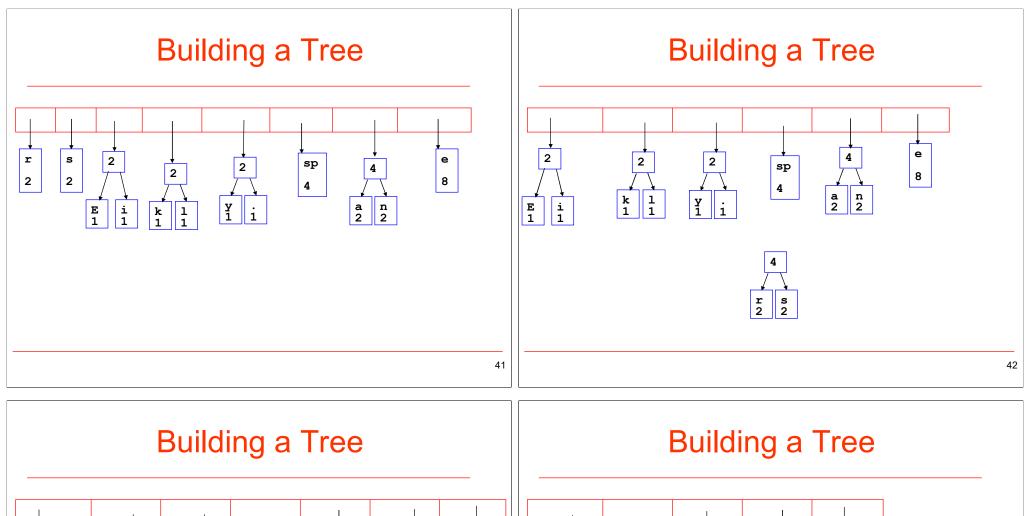
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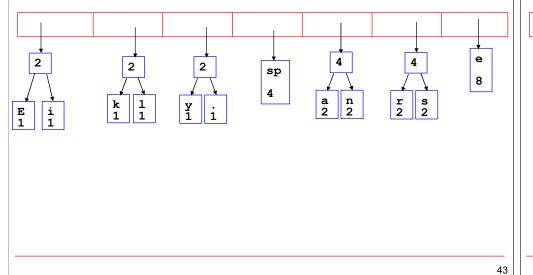
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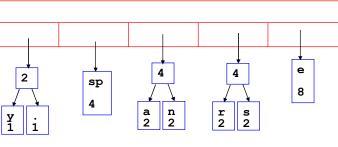
n 2 а 2

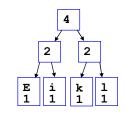
2

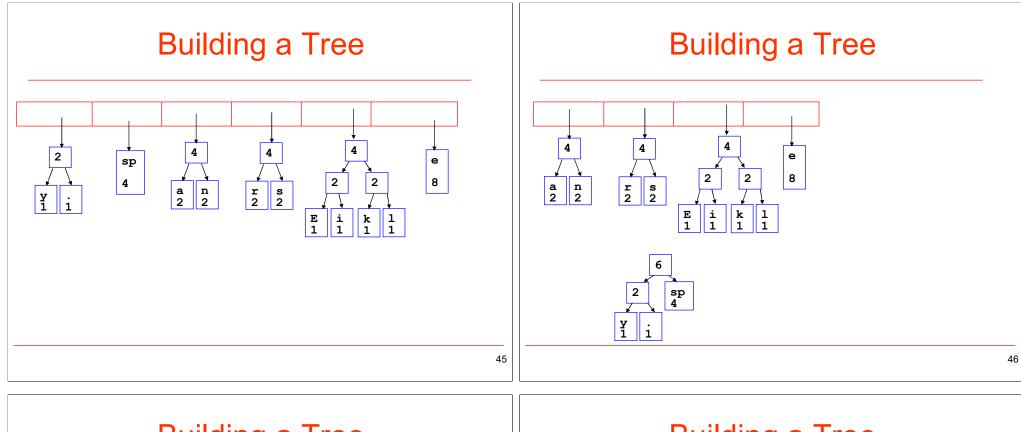
е





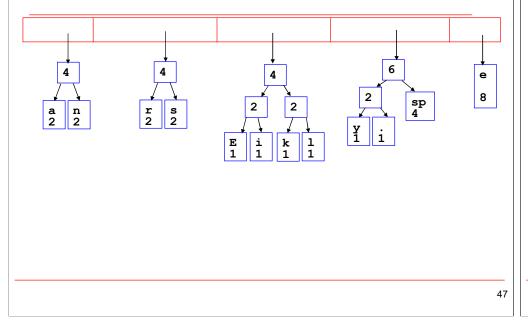


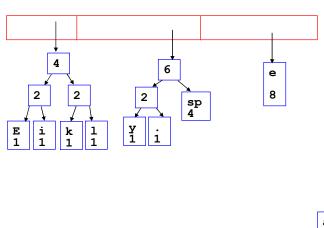


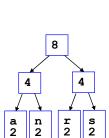


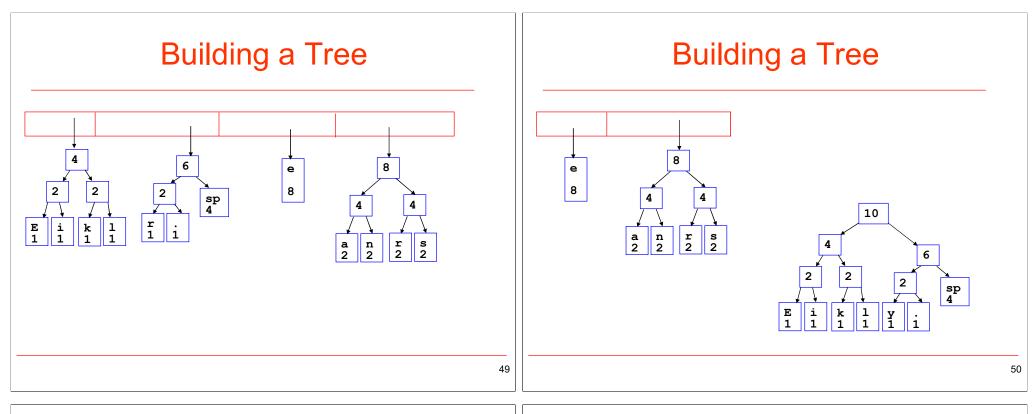


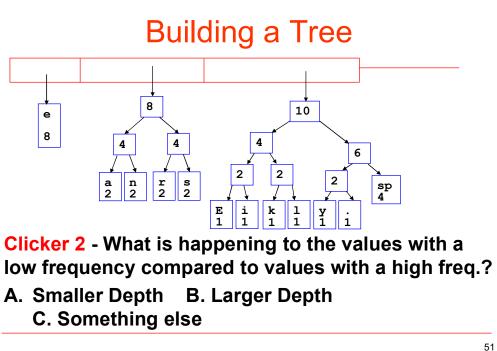
Building a Tree

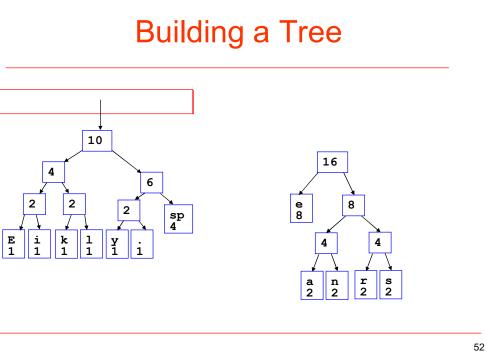


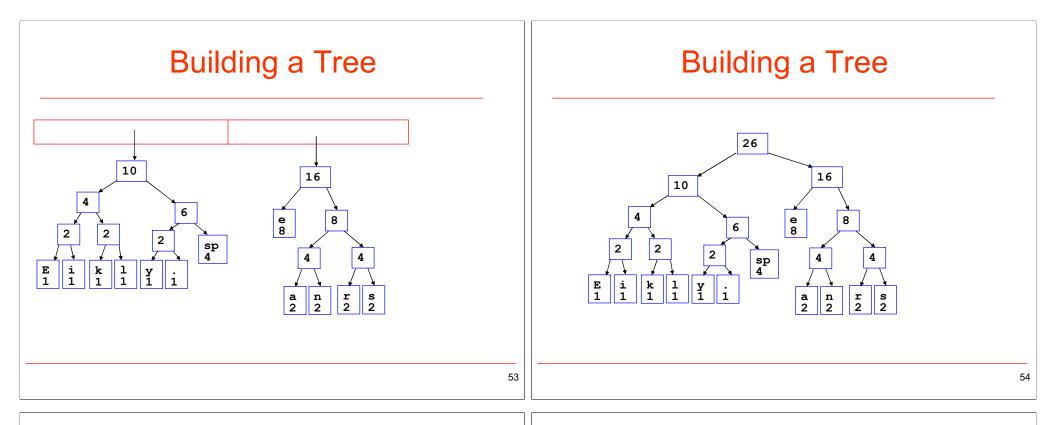




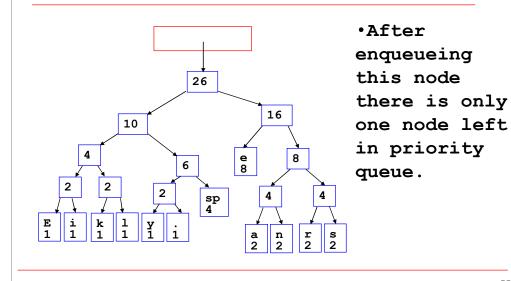








Building a Tree



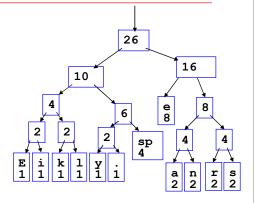
Building a Tree

Dequeue the single node left in the queue.

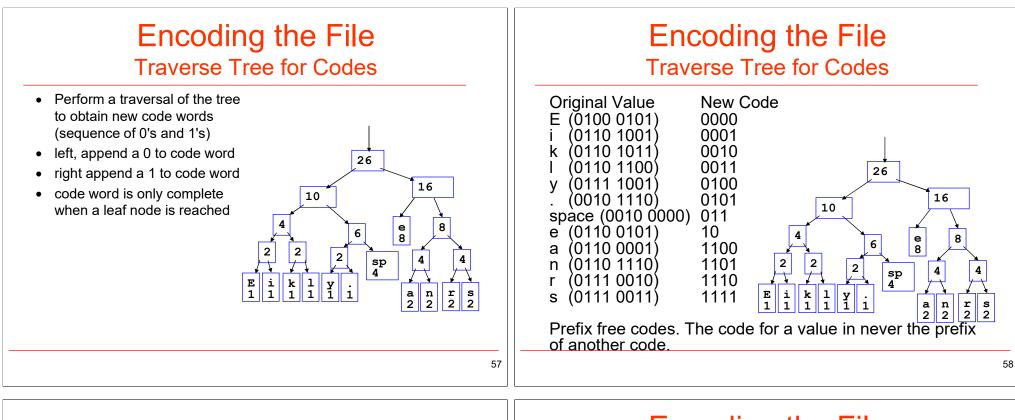
This tree contains the new code words for each character.

Frequency of root node should equal number of characters in text.

Eerie eyes seen near lake.



4 spaces, 26 characters total

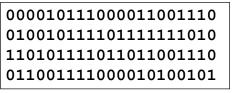


Encoding the File

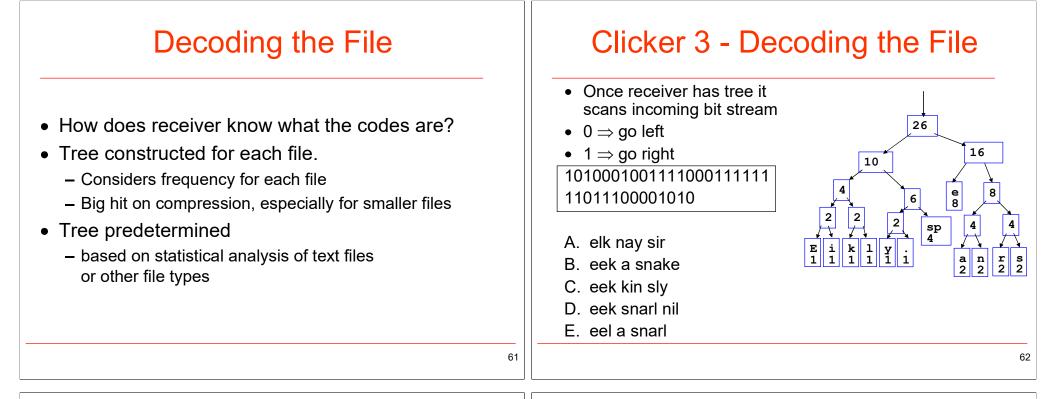
 Rescan original file and encode file using new code words Eerie eyes seen near lake. 	Char E i k	New Code 0000 0001 0010
000010111000011001110 010010111101111111	y space e	0011 0100 0101 011 10
	a n r s	1100 1101 1110 1111

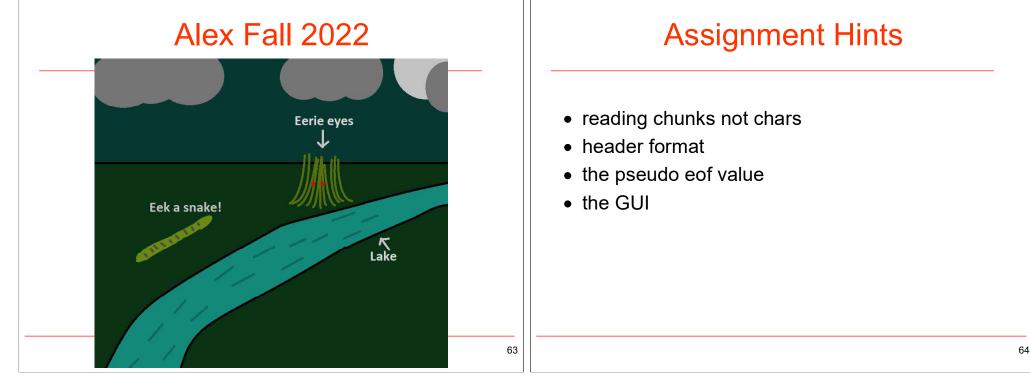
Encoding the File Results

- Have we made things any better?
- 84 bits to encode the file
- ASCII would take 8 * 26 = 208 bits



If modified code used 4 bits per character are needed. Total bits 4 * 26 = 104. Savings not as great.

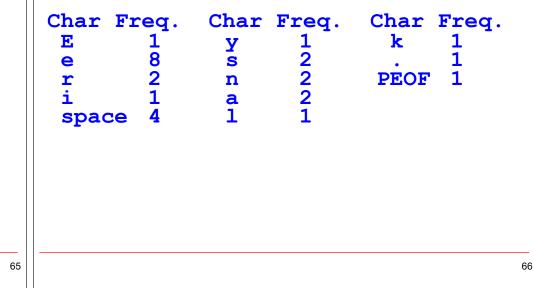




Assignment Example

- "Eerie eyes seen near lake." will result in different codes than those shown in slides due to:
 - adding elements in order to PriorityQueue
 - required pseudo eof value (PEOF)

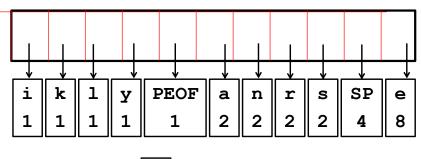
Assignment Example

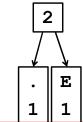


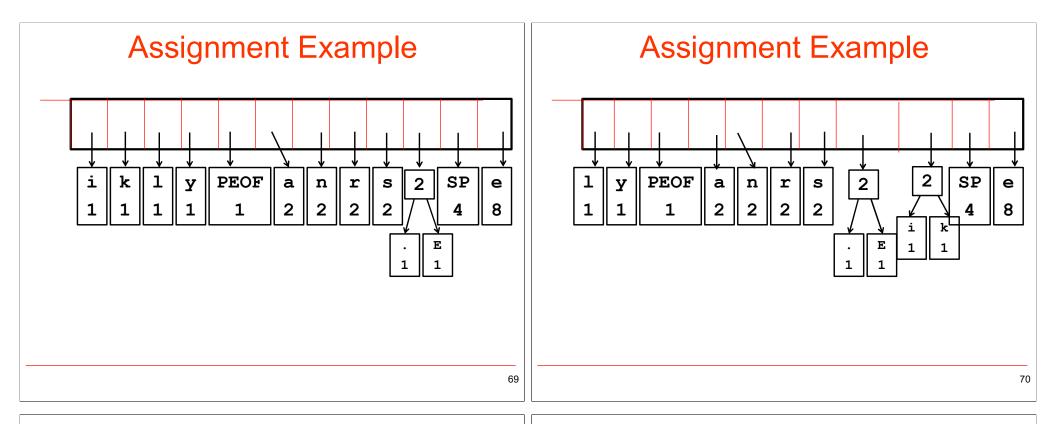
Assignment Example

•	Е	i	k	1	У	PEOF	a	n	r	s	SP	e
1	1	1	1	1	1	1	2	2	2	2	4	8

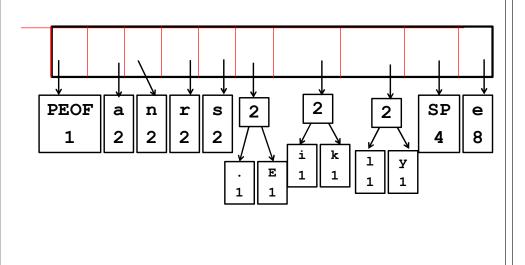
Assignment Example



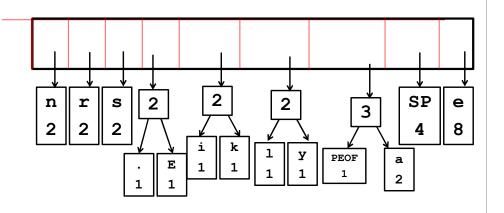


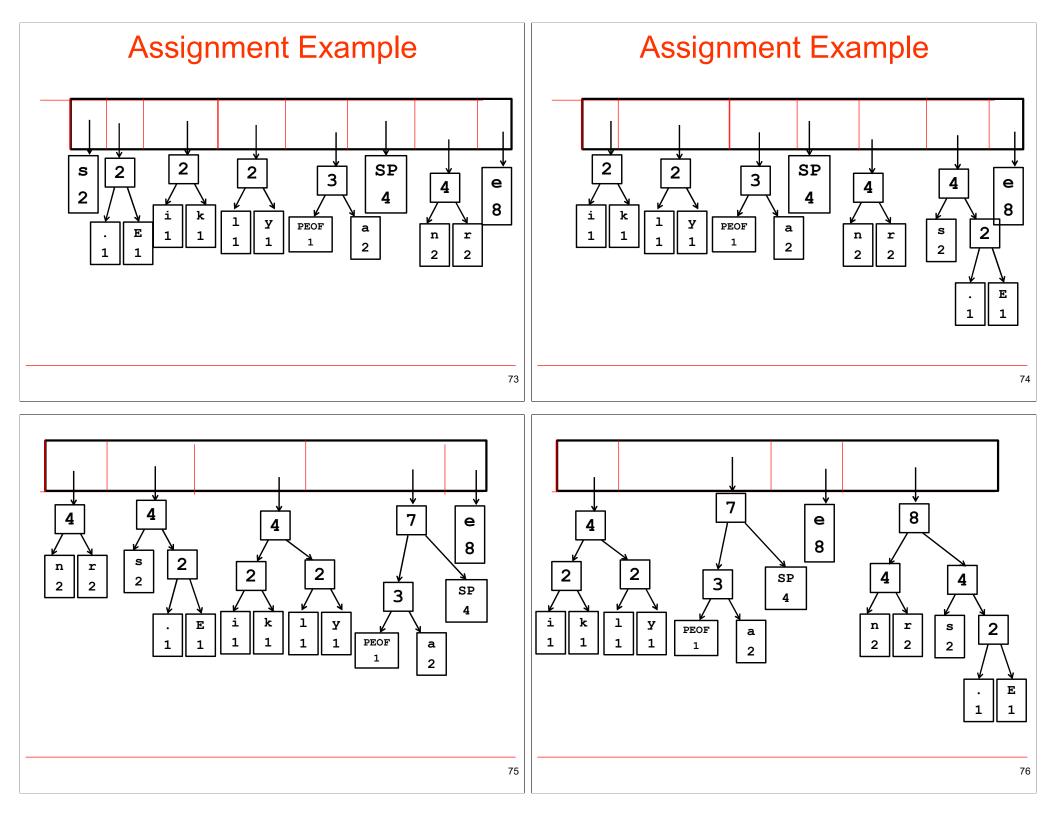


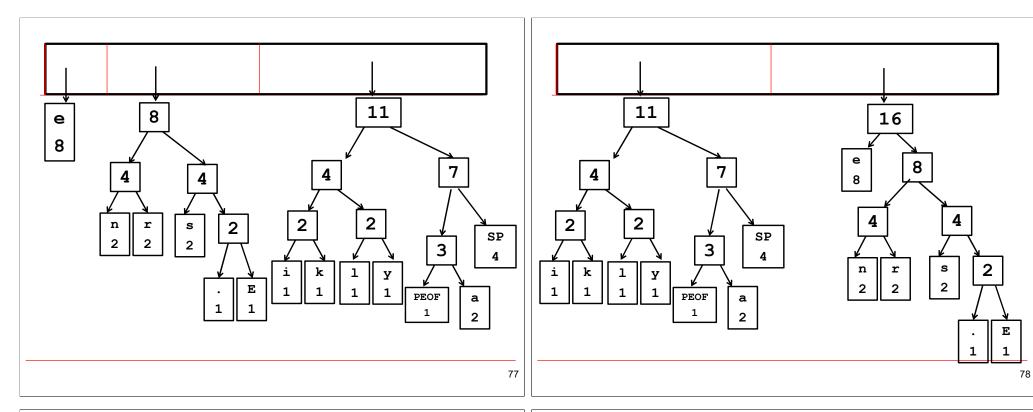
Assignment Example

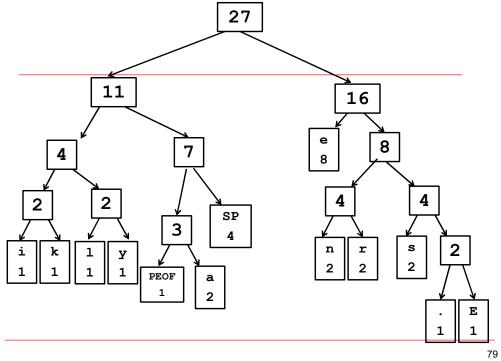


Assignment Example









Codes

value:	32,	equivalent	char:	,	frequency:	4,	new (code (011
value:	46,	equivalent	char:	۰,	frequency:	1,	new o	code i	11110
value:	69,	equivalent	char:	Ε,	frequency:	1,	new o	code i	11111
value:	97,	equivalent	char:	a,	frequency:	2,	new o	code (0101
value:	101,	equivalent	char:	e,	frequency:	8,	new	code	10
value:	105,	equivalent	char:	i,	frequency:	1,	new	code	0000
value:	107,	equivalent	char:	k,	frequency:	1,	new	code	0001
value:	108,	equivalent	char:	l,	frequency:	1,	new	code	0010
value:	110,	equivalent	char:	n,	frequency:	2,	new	code	1100
value:	114,	equivalent	char:	r,	frequency:	2,	new	code	1101
value:	115,	equivalent	char:	s,	frequency:	2,	new	code	1110
value:	121,	equivalent	char:	y,	frequency:	1,	new	code	0011
value:	256,	equivalent	char:	?,	frequency:	1,	new	code	0100

Λ	. این مرکز			_
A	Iterii	ng i	IIe	S

 Tower bit map (Eclipse/Huffman/Data). Alter the first 300 characters of line 16765 to this

~00~00~00~00~00~00~00~00 xxx

Compression - Why Bother?

- Apostolos "Toli" Lerios
- Facebook Engineer
- Heads image storage group
- jpeg images already compressed

- look for ways to compress even more
- 1% less space = millions of dollars in savings





Graphs Topic 22

" Hopefully, you've played around a bit with <u>The Oracle of Bacon at</u> <u>Virginia</u> and discovered how few steps are necessary to link just about anybody who has ever been in a movie to Kevin Bacon, but could there be some actor or actress who is even closer to the center of the Hollywood universe?.

By processing all of the almost half of a million people in the <u>Internet</u> <u>Movie Database</u> I discovered that there are currently 1160 people who are *better* centers than Kevin Bacon! ... By computing the average of these numbers we see that the average (Sean) <u>Connery Number</u> is about 2.682 making Connery a better center than Bacon"

-Who is the Center of the Hollywood Universe?,

University of Virginia

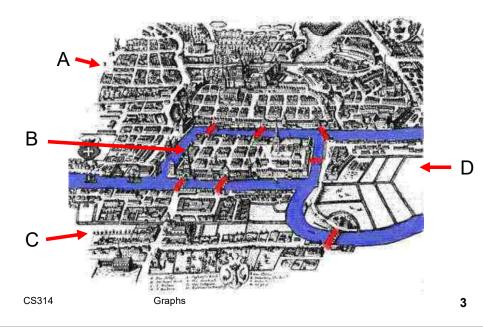
That was in 2001.

In 2013 Harvey Keitel has become the center of the Hollywood Universe. Connery is 136th. Bacon has moved up to 370^{th.}

An Early Problem in Graph Theory

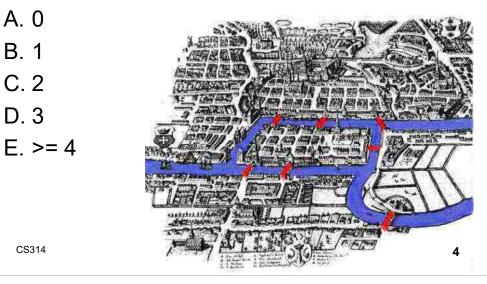
- Leonhard Euler (1707 1783)
 - One of the first mathematicians to study graphs
- The Seven Bridges of Konigsberg Problem
 Konigsberg is now called Kaliningrad
- A puzzle for the residents of the city
- The river Pregel flows through the city
- 7 bridges crossed the river
- Can you cross all bridges while crossing each bridge only once? An Eulerian Circuit Graphs

Konigsberg and the River Pregel



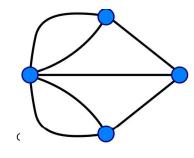
Clicker 1

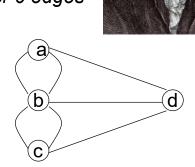
How many solutions does the Seven Bridges of Konigsberg Problem have?



How to Solve

- Brute Force?
- Euler's Solution
 - Redraw the map as a graph (really a multigraph as opposed to a simple graph, 1 or 0 edges per pair of vertices)





5

Euler's Proposal

- A connected graph has an Euler tour (cross every edge exactly one time and end up at starting node) if and only if every vertex has an even number of edges
 - Eulerian Circuit
- Clicker 2 What if we reduce the problem to only crossing each edge (bridge) exactly once?
 - Doesn't matter if we end up where we started

Definitions

In a weighted graph the edge has cost or weight that measures the cost of traveling along the edge

• A *path* is a sequence of vertices connected by

- The weighted path length is the sum of the cost of the

A cycle is a path of length 1 or more that starts and

ends at the same vertex without repeating any

- a *directed acyclic graph* is a directed graph with

- The path length is the number of edges

- Eulerian Trail
- A. 0 B. 1 C. 2 D. 3 E. >= 4 Graphs

CS314

edges

6

Graph Definitions

- A graph is comprised of a set of *vertices* (nodes) and a set of *edges* (links, arcs) connecting the vertices
 - An edge connects 2 vertices
- in a *directed* graph edges are one-way
 - movement allowed from first node to second, but not second to first
 - directed graphs also called *digraphs*
- in an undirected graph edges are two-way
 - movement allowed in either direction

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Graphs

7

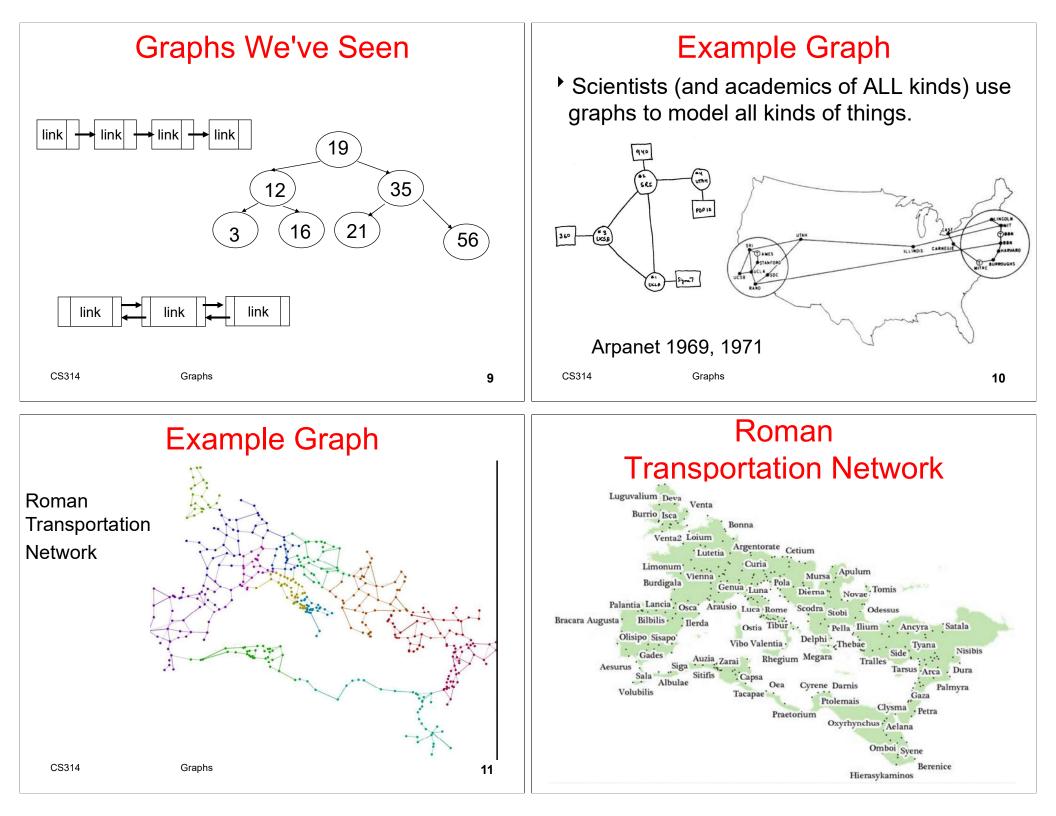
Graphs

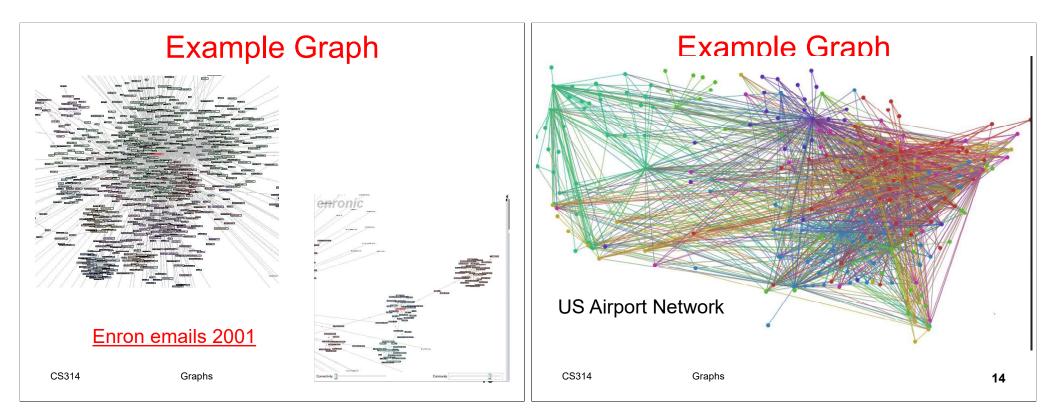
edges in a path

other vertices

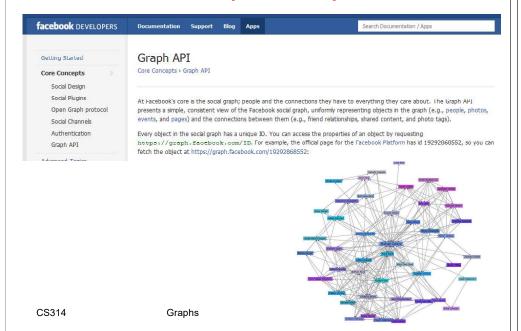
no cycles

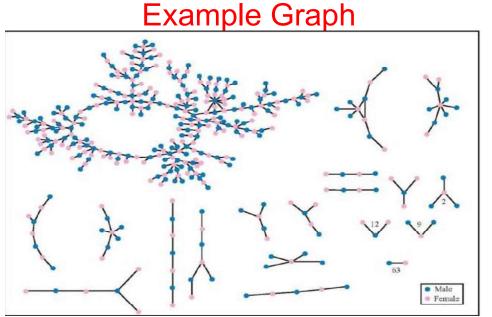
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Example Graph





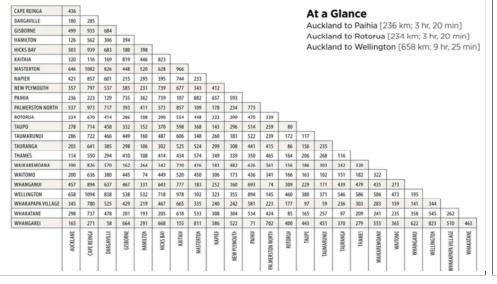
"Jefferson" High School, Ohio <u>Chains of Affection: The Structure of Adolescent Romantic</u> and Sexual Networks, 2005,

Representing Graphs How to store a graph as a data structure?	Adjacency Matrix Representation	
Tiow to store a graph as a data structure:	Country Code	
A LO LEAST	A Br Bl Ch Co E FG G Pa Pe S U V	
the of the stand	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	
	BI 1 0 1 0 0 0 1 1 0 0 0 Bolivia BI	
1 Sun	Ch 1 0 1 0 0 0 0 0 1 0 0 0 Chile Ch	
	Co 0 1 0 0 1 0 0 1 0 0 1 Colombia Co	
Nard /	E 0 0 0 0 1 0 0 0 1 0 0 0 Ecuador E	
	FG 0 1 0 0 0 0 0 0 0 1 0 0 French Guiana FG	
	G 0 1 0 0 0 0 0 0 0 1 0 1 Guyana G	
	Pa 1 1 1 0 0 0 0 0 0 0 0 0 0 Paraguay Pa	
	Pe 0 1 1 1 1 0 0 0 0 0 0 0 Peru Pe	
BIL S	S 0 1 0 0 0 0 1 1 0 0 0 0 0 U 1 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	
S S	V 0 1 0 0 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0	
and the second sec	V O I O O I O O I O O O O O Venezuela V	
CS314 Graphs 17	CS314 Graphs 1	18

Undirected Graph?

Use a ragged 2d array to save space

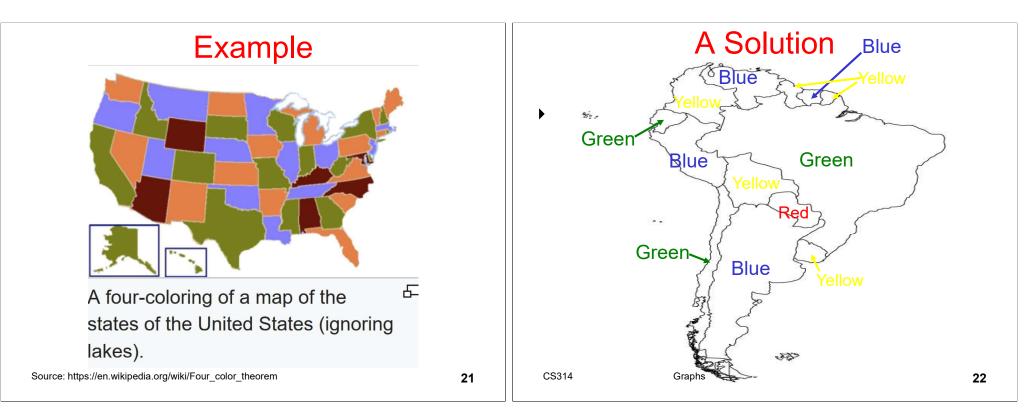
NORTH ISLAND DISTANCE CHART



The Map Coloring Problem

- How many colors do you need to color a map, so that no 2 countries that have a common border (not a point) are colored the same?
- How to solve using Brute Force?

Graphs



What About the Ocean?

A Br Bl Ch Co E FG G Pa Pe S U V Oc А Br 1 1 1 Bl Ch 1 0 Co 0 Ε FG G 1 0 1 1 Pa 1 Pe 0 0 0 1 0 0 S 0 0 0 1 U V 0 0 0 1 1 1 1 0 Oc 1 1 Graphs

Make the Ocean Blue Red Se . Green en Green Blue Green Red Blue CS314 Graphs

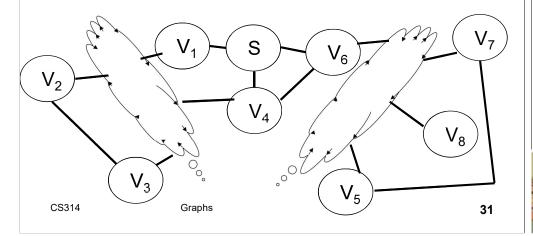
<section-header><list-item><list-item><list-item><list-item><list-item><list-item></list-item></list-item></list-item></list-item></list-item></list-item></section-header>	 Graph Representation For dense graphs the adjacency matrix is a reasonable choice For weighted graphs change booleans to double or int Can the adjacency matrix handle directed graphs? Most graphs are sparse, not dense For sparse graphs an <i>adjacency list</i> is an alternative that uses less space Each vertex keeps a list of edges to the vertices it is connected to.
<pre>Graph Implementation public class Graph private static final double INFINITY</pre>	 Graph Class This Graph class stores vertices Each vertex has an adjacency list what vertices does it connect to? shortest path method finds all paths from start vertex to every other vertex in graph after shortest path method called queries can be made for path length from start node to destination node

Vertex Class (nested in Graph)	Edge Class (nested in Graph)
<pre>private static class Vertex private String name; private List<edge> adjacent; public Vertex(String n)</edge></pre>	private static class Edge private Vertex dest; private double cost;
<pre>// for shortest path algorithms private double distance; private Vertex prev; private int scratch;</pre>	private Edge(Vertex d, double c)
<pre>// call before finding new paths public void reset()</pre>	
CS314 Graphs 29	CS314 Graphs 30

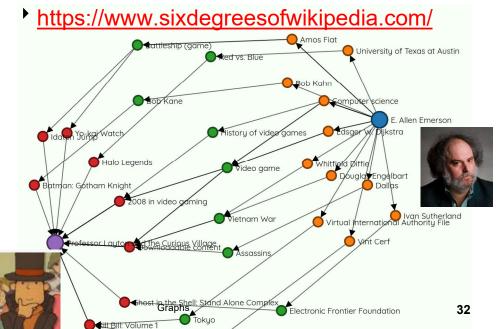
Unweighted Shortest Path

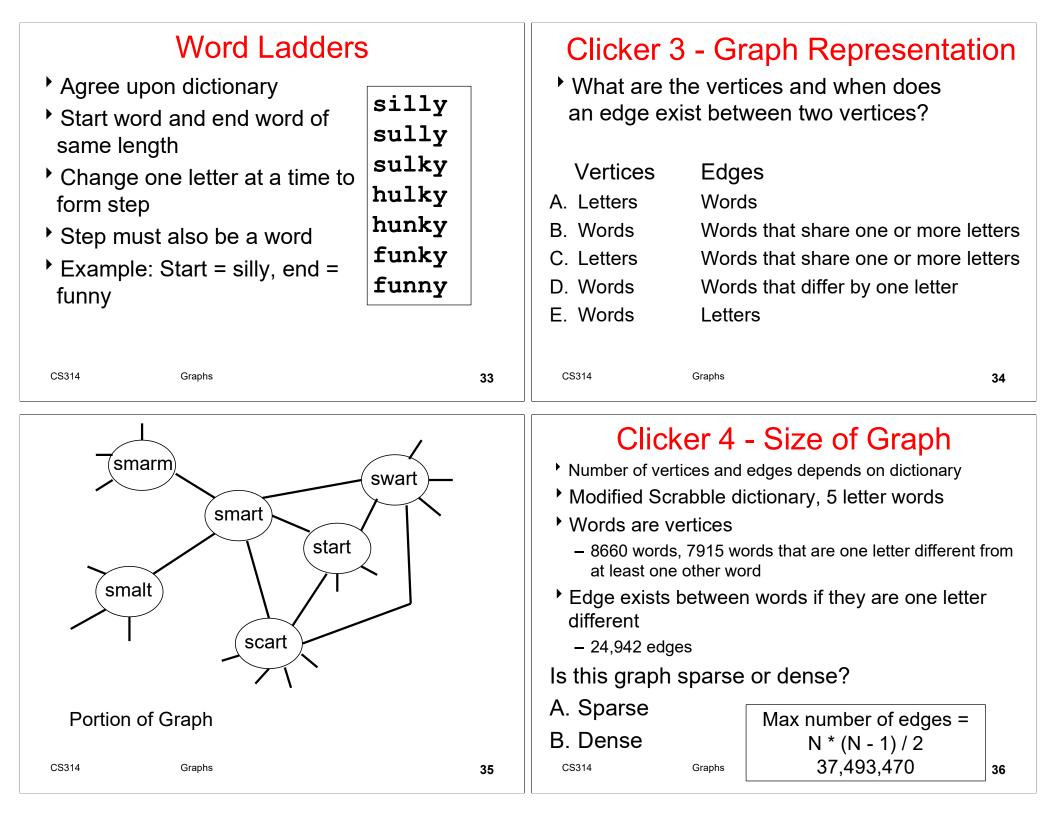
 Given a vertex, S (for start) find the shortest path from S to all other vertices in the graph

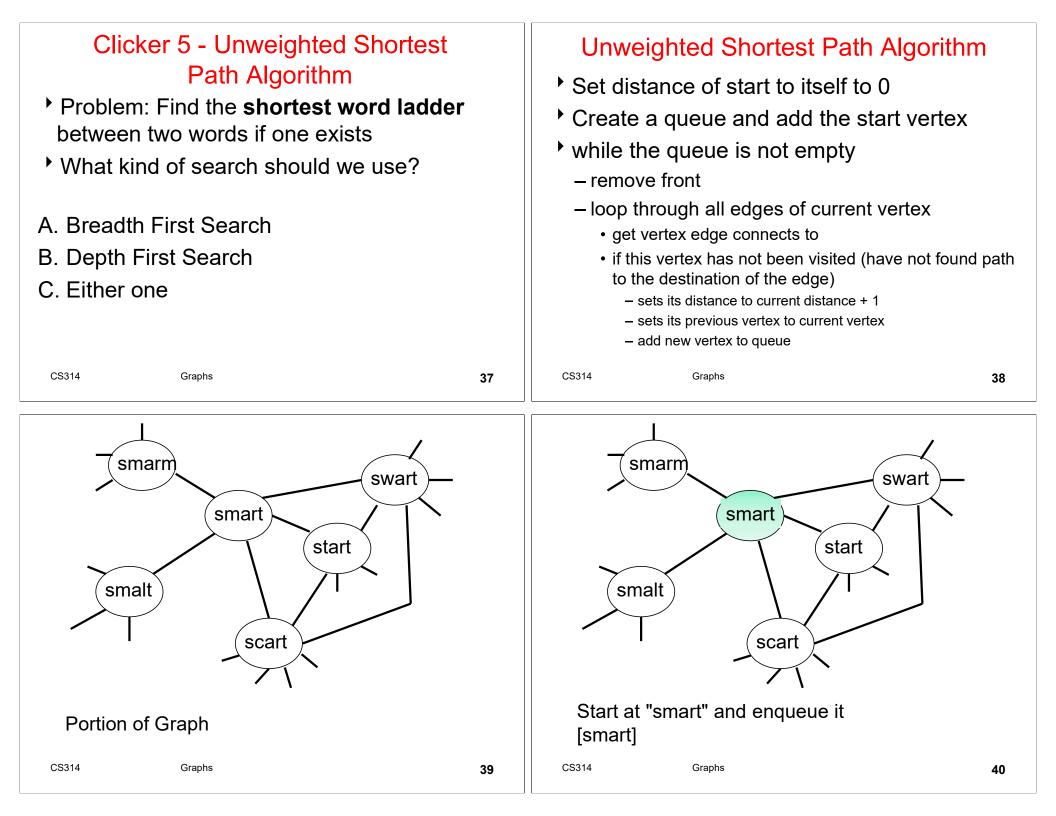
Graph is unweighted (set all edge costs to 1)

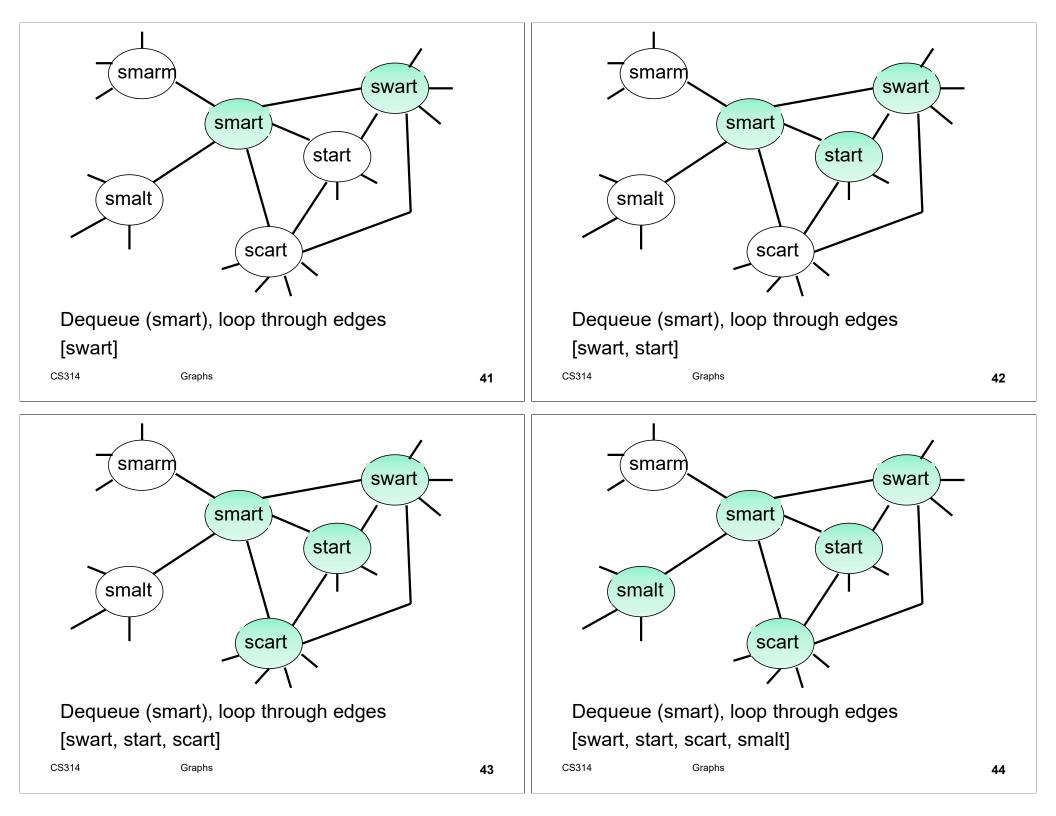


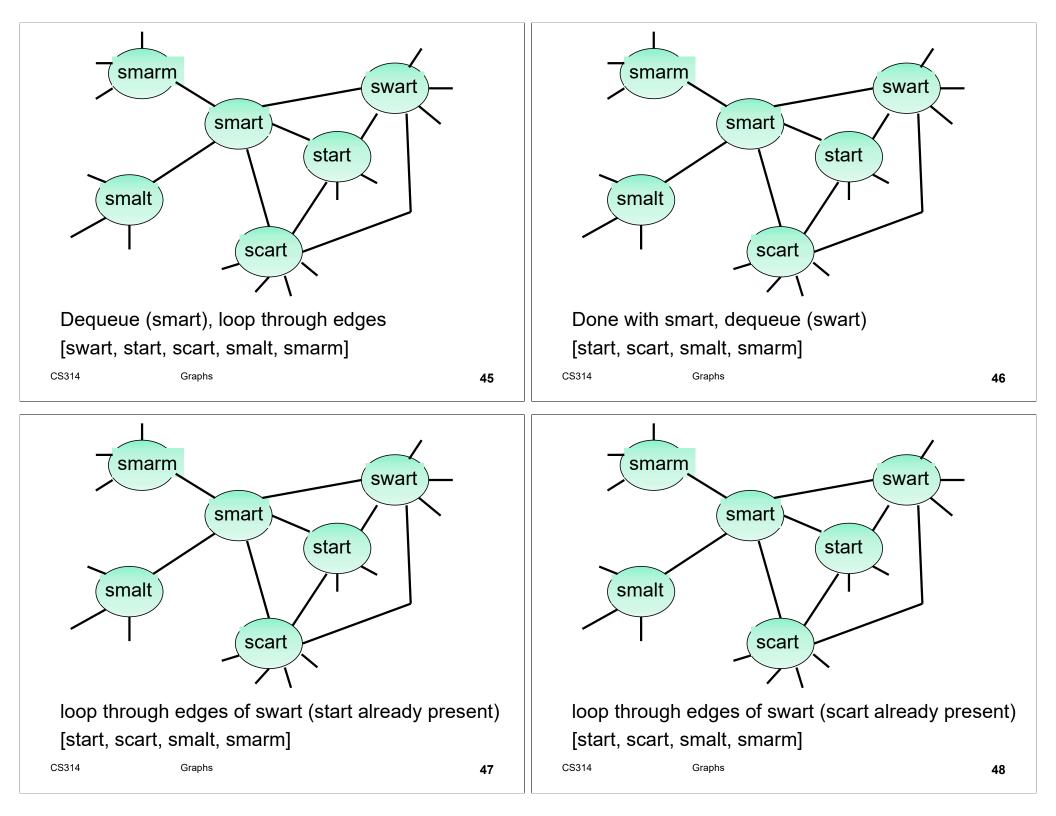
6 Degrees of Wikipedia

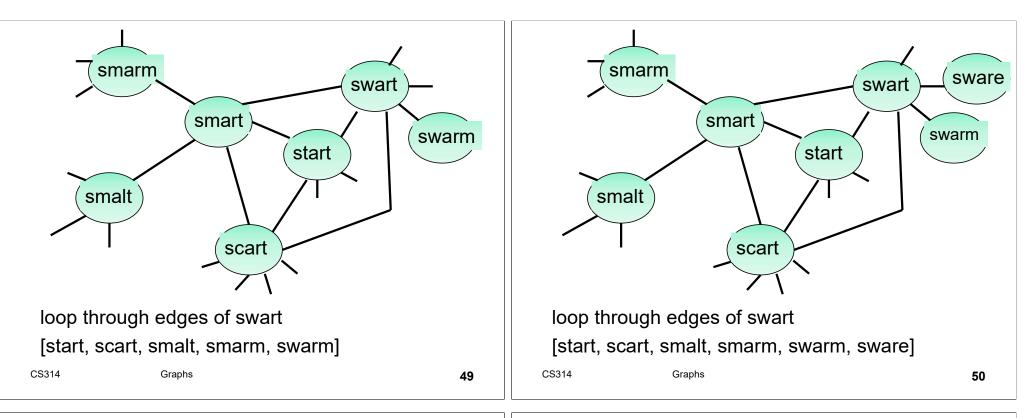












Unweighted Shortest Path

- Implement method
- ▶ demo
- how is path printed?
- The diameter of a graph is the longest shortest past in the graph
- How to find?
- How to find center of graph?
 - many measures of centrality
 - ours: vertex connected to the largest number of other vertices with the shortest average path length
 ^{CS314} Graphs 51

Positive Weighted Shortest Path

- Edges in graph are weighted and all weights are positive
- Similar solution to unweighted shortest path
- Dijkstra's algorithm
- Edsger W. Dijkstra, 1930–2002
- UT Professor 1984 2000
- Algorithm developed in 1956 and published in 1959.
 - other algorithms developed independently around this time



Dijkstra on Creating the Algorithm

- What is the shortest way to travel from Rotterdam to Groningen, in general: from given city to given city. It is the algorithm for the shortest path, which I designed in about twenty minutes. One morning I was shopping in Amsterdam with my young fiancée, and tired, we sat down on the café terrace to drink a cup of coffee and I was just thinking about whether I could do this, and I then designed the algorithm for the shortest path. As I said, it was a twenty-minute invention. In fact, it was published in '59, three years later. The publication is still readable, it is, in fact, quite nice. One of the reasons that it is so nice was that I designed it without pencil and paper. I learned later that one of the advantages of designing without pencil and paper is that you are almost forced to avoid all avoidable complexities. Eventually that algorithm became, to my great amazement, one of the cornerstones of my fame.
- <u>Edsger Dijkstra, in an interview with Philip L. Frana,</u>
 <u>Communications of the ACM, 2001</u> (wiki page on the algorithm)

Vertex Class (nested in Graph)

```
private static class Vertex
    private String name;
    private List<Edge> adjacent;
```

public Vertex(String n)

// for shortest path algorithms
private double distance;
private Vertex prev;
private int scratch;

// call before finding new paths
public void reset()

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Dijkstra's Algorithm

- Pick the start vertex
- Set the distance of the start vertex to 0 and all other vertices to INFINITY
- While there are unvisited vertices:
 - Let the current vertex be the vertex with the lowest cost path from start to it that has **not yet been visited**
 - mark current vertex as visited
 - for each edge from the current vertex
 - if the sum of the cost of the current vertex and the cost of the edge is less than the cost of the destination vertex
 - update the cost of the destination vertex
 - set the previous of the destination vertex to the current vertex
 - enqueue this path (not vertex) to the priority queue
 - THIS IS NOT VISITING THE NEIGHBORING VERTEX

Dijkstra's Algorithm

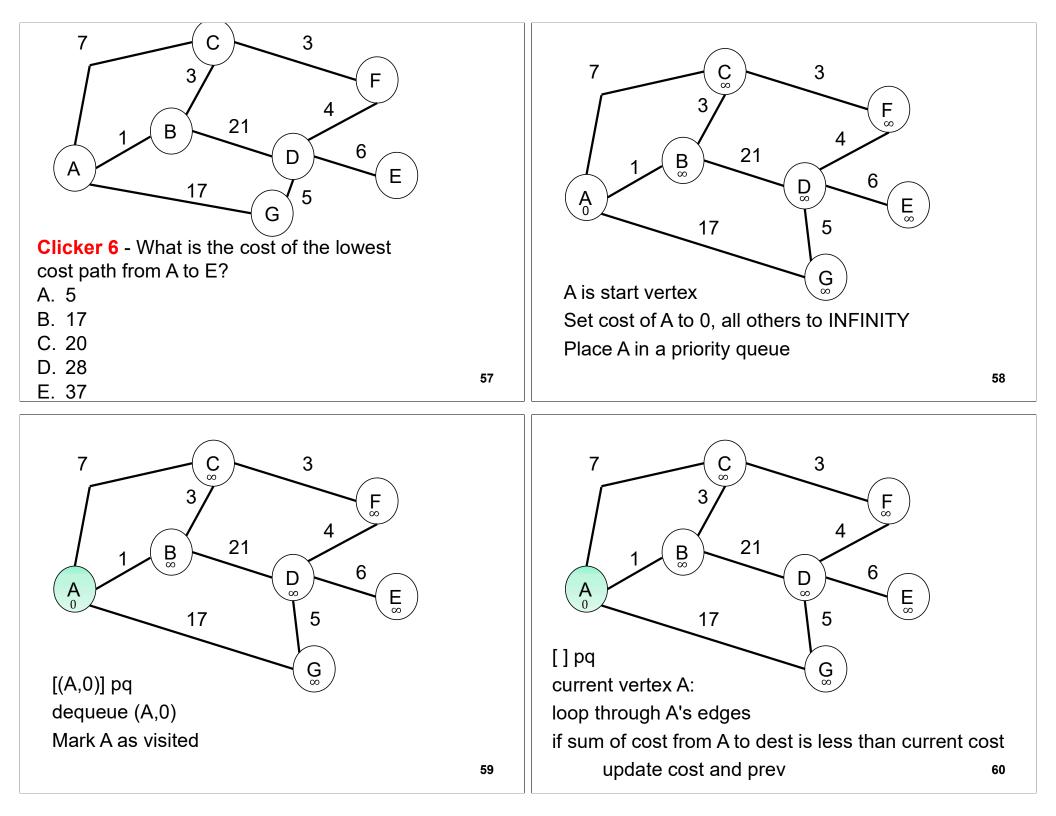
Example of a Greedy Algorithm

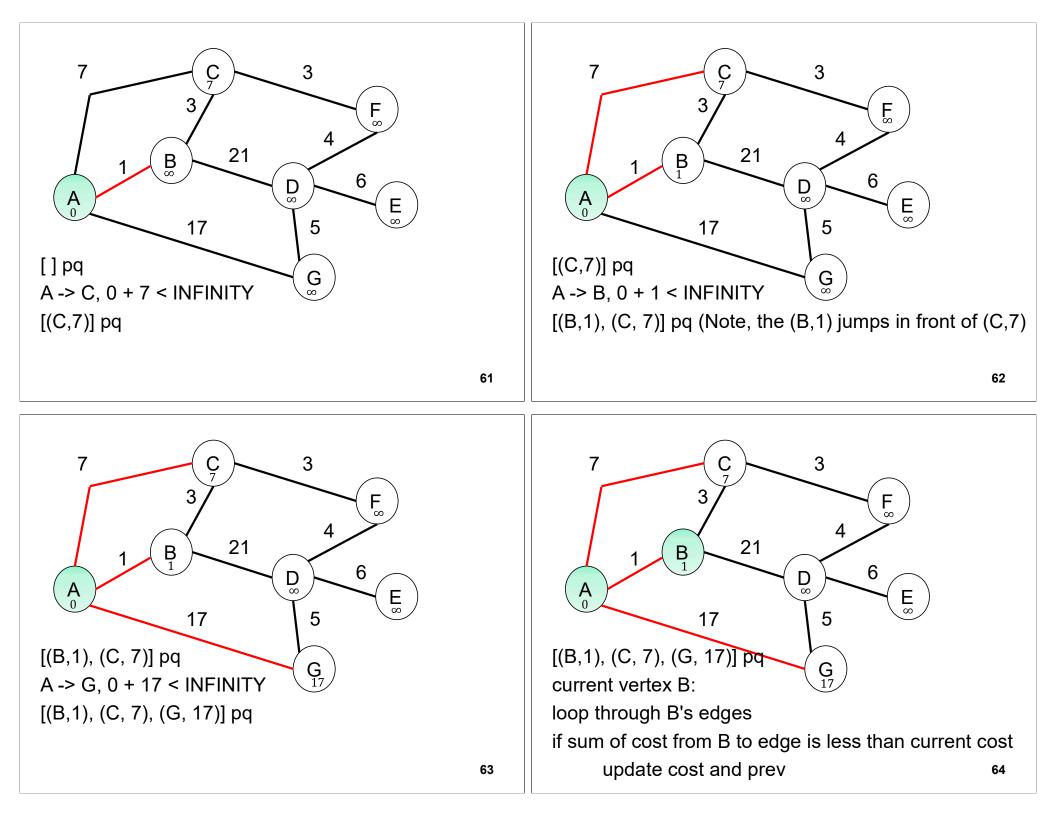
Graphs

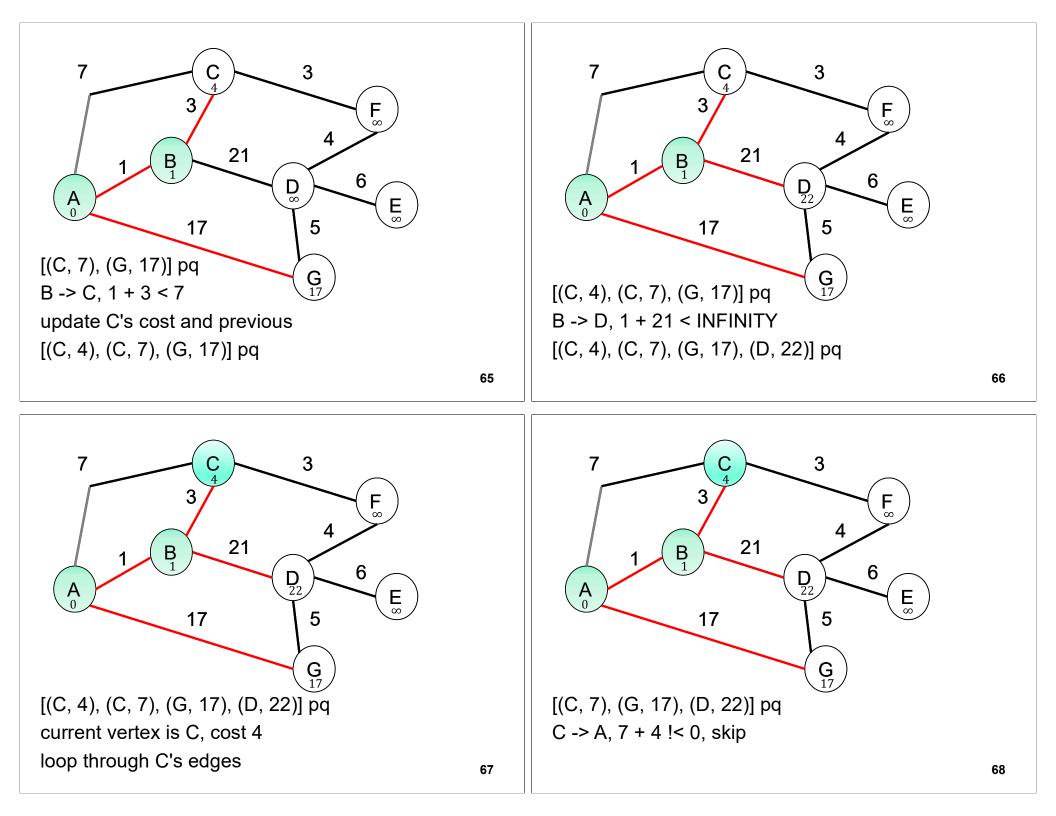
- A Greedy Algorithm does what appears to be the best thing at each stage of solving a problem
- Gives best solution in Dijkstra's Algorithm
- Does NOT always lead to best answer
- Fair teams:
 - (10, 10, 8, 8, 8), 2 teams
- Making change with fewest coins

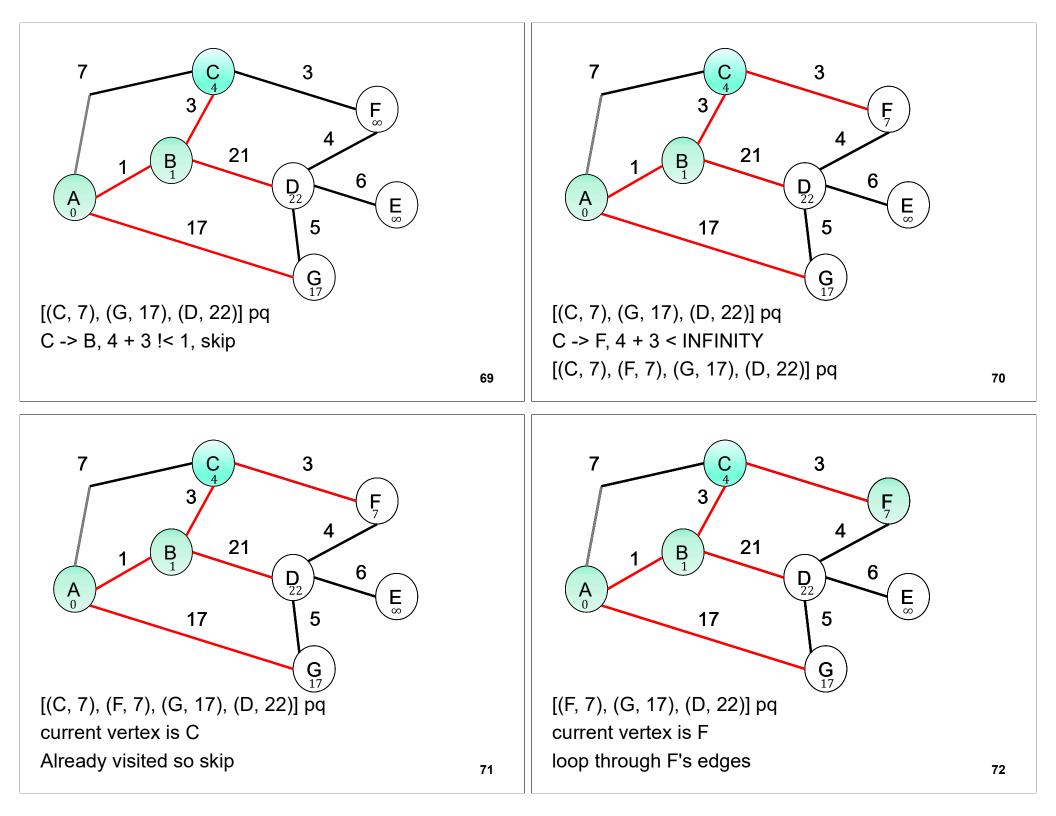
Graphs

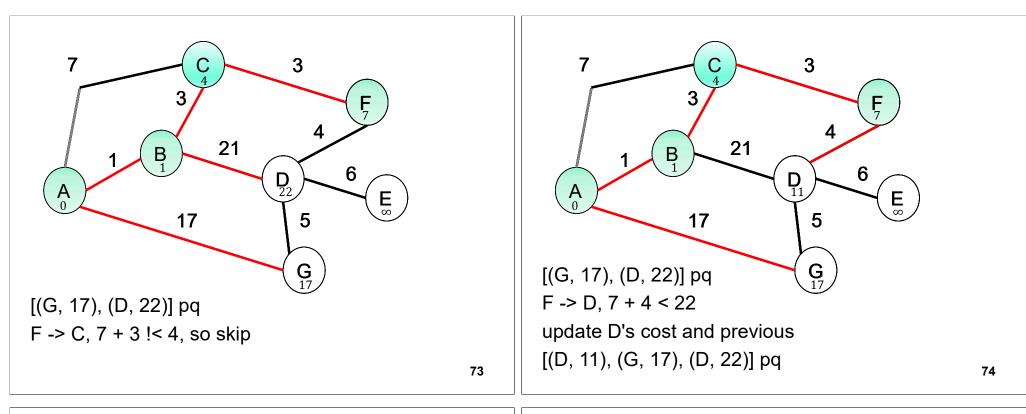
- (1, 5, 10) 15 cents
- (1, 5, 12) 15 cents











Aside - Implementing Dijkstra's

Create a Path class to allow for multiple paths and distances (costs) to a given vertex private static class Path

implements Comparable<Path> {

private Vertex dest;

private double cost;

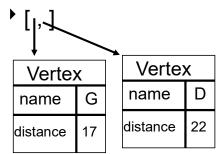
 Use a priority queue of Paths to store the vertices and distances

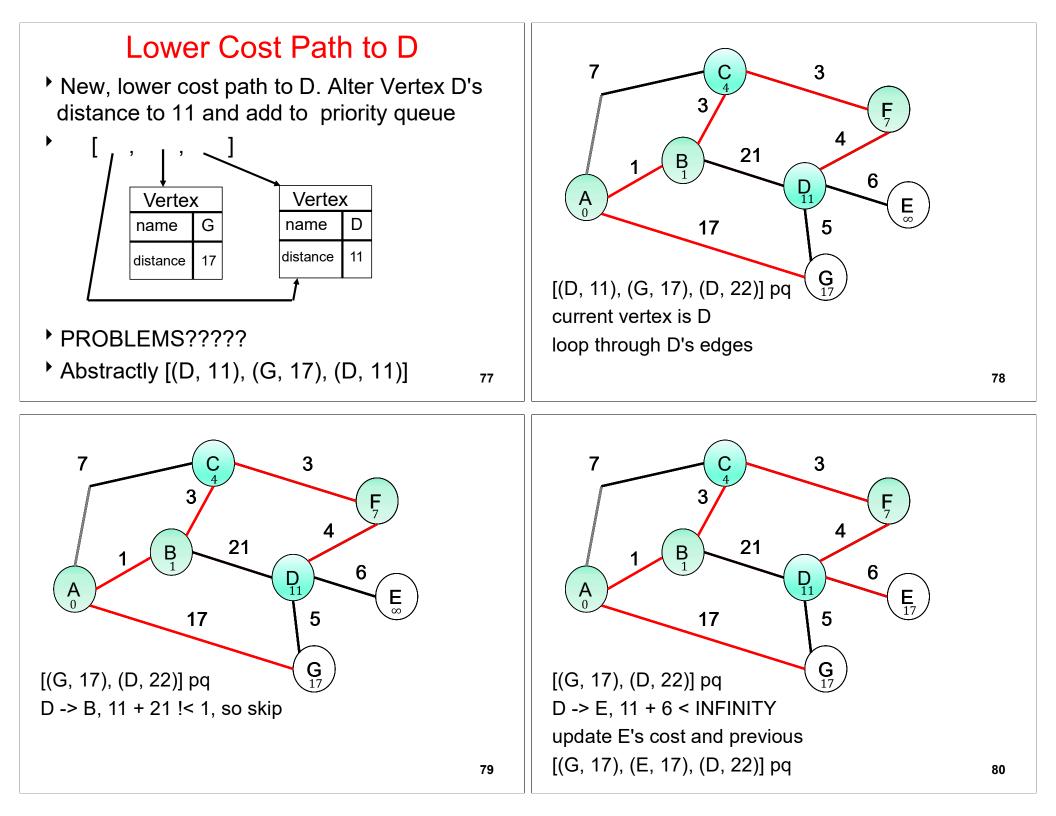
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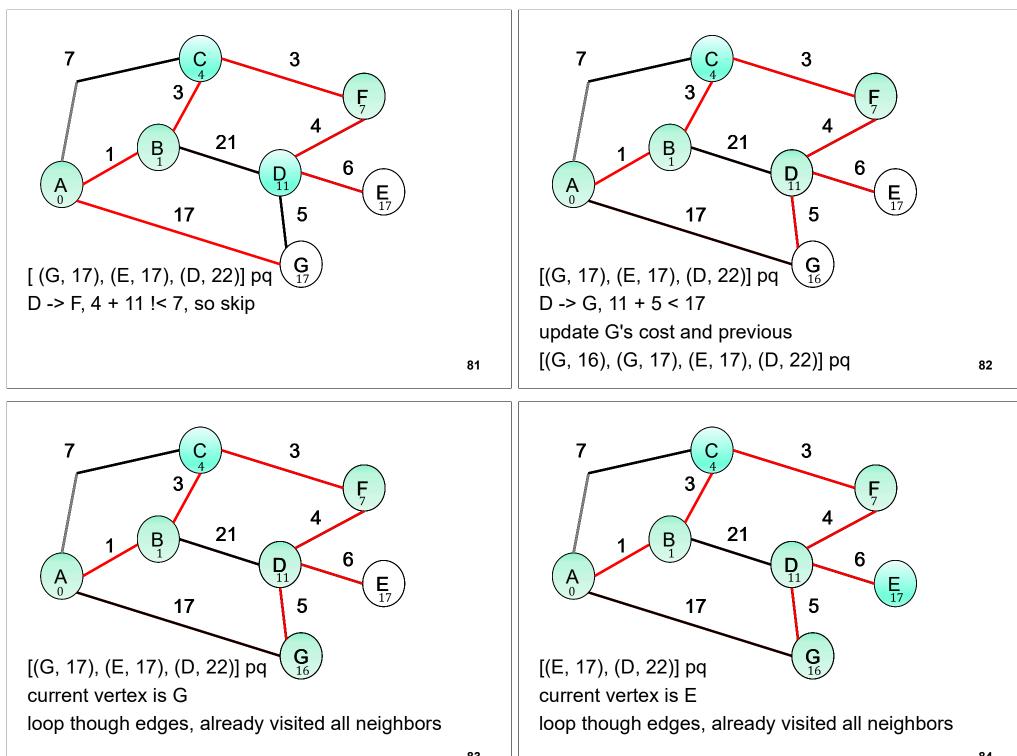
Graphs

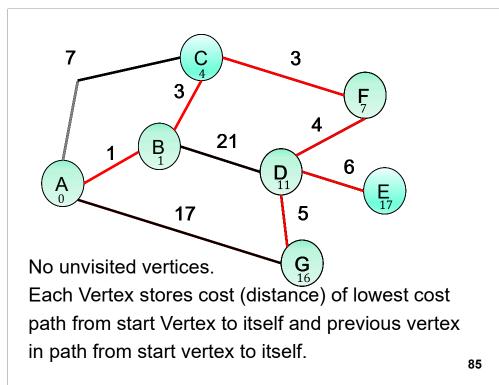
Why? References!!!

- Slide 74 and 78, adding new, lower cost path to Vertex D
- Abstractly: [(G, 17), (D, 22)] becomes [(D, 11) (G, 17), (D, 22)]
- What does priority queue store? References to Vertex Objects









Alternatives to Dijkstra's Algorithm

- A*, pronounced "A Star"
- A heuristic, goal of finding shortest weighted path from single start vertex to goal vertex
- Uses actual distance like Dijkstra's but also estimates remaining cost or distance

Graphs

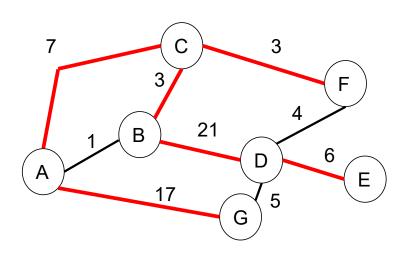
- distance is set to current distance from start PLUS the estimated distance to the goal
- For example when finding a path between towns, estimate the remaining distance as the straight-line (as the crow flies) distance between current location and goal.

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Spanning Tree

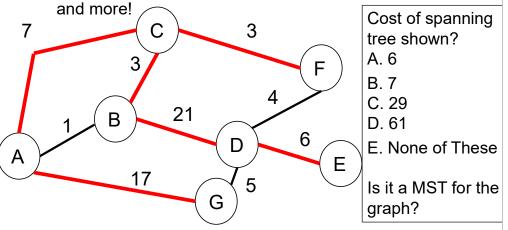
Spanning Tree: A tree of edges that connects all the vertices in a graph



Clicker 7 -

Minimum Spanning Tree

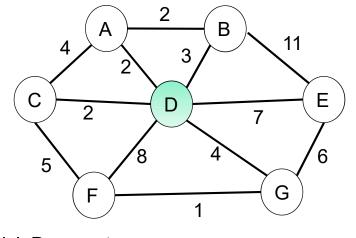
- Minimum Spanning Tree: A spanning tree in a weighted graph with the lowest total cost
 - used in network design, taxonomy, Image registration,



Prim's Algorithm

- Initially created by Vojtěch Jarník
- Rediscovered by Prim (of Sweetwater, TX) and Dijkstra
- Pick a vertex arbitrarily from graph - In other words, it doesn't matter which one
- Add lowest cost edge between the tree and a vertex that is not part of the tree UNTIL every vertex is part of the tree
- Greedy Algorithm, very similar to Dijkstra's

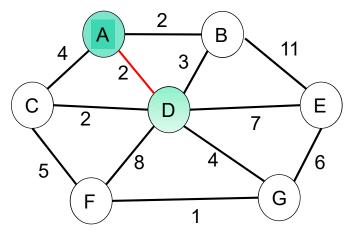




Pick D as root

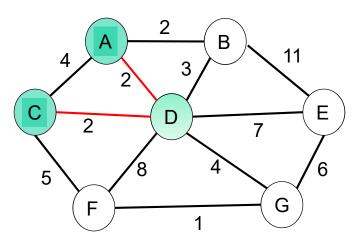


Prim's Algorithm



Lowest cost edge from tree to vertex not in Tree? 2 from D to A (or C) Graphs

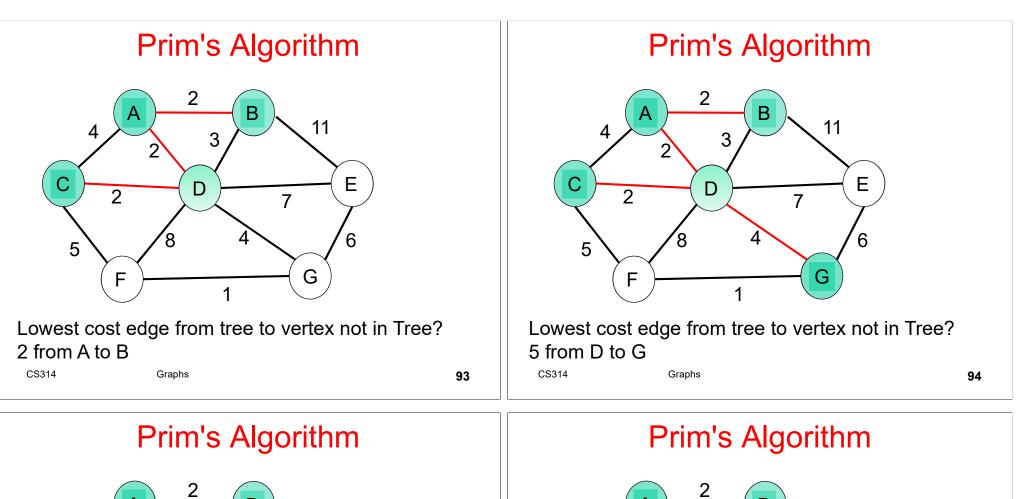
Prim's Algorithm

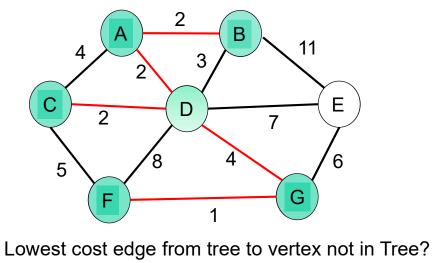


Lowest cost edge from tree to vertex not in Tree? 2 from D to C (OR from A to B)

Graphs

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1 from G to F

CS314

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2

4

2

F

С

5

6 from G to E

CS314

В

3

1

Lowest cost edge from tree to vertex not in Tree?

D

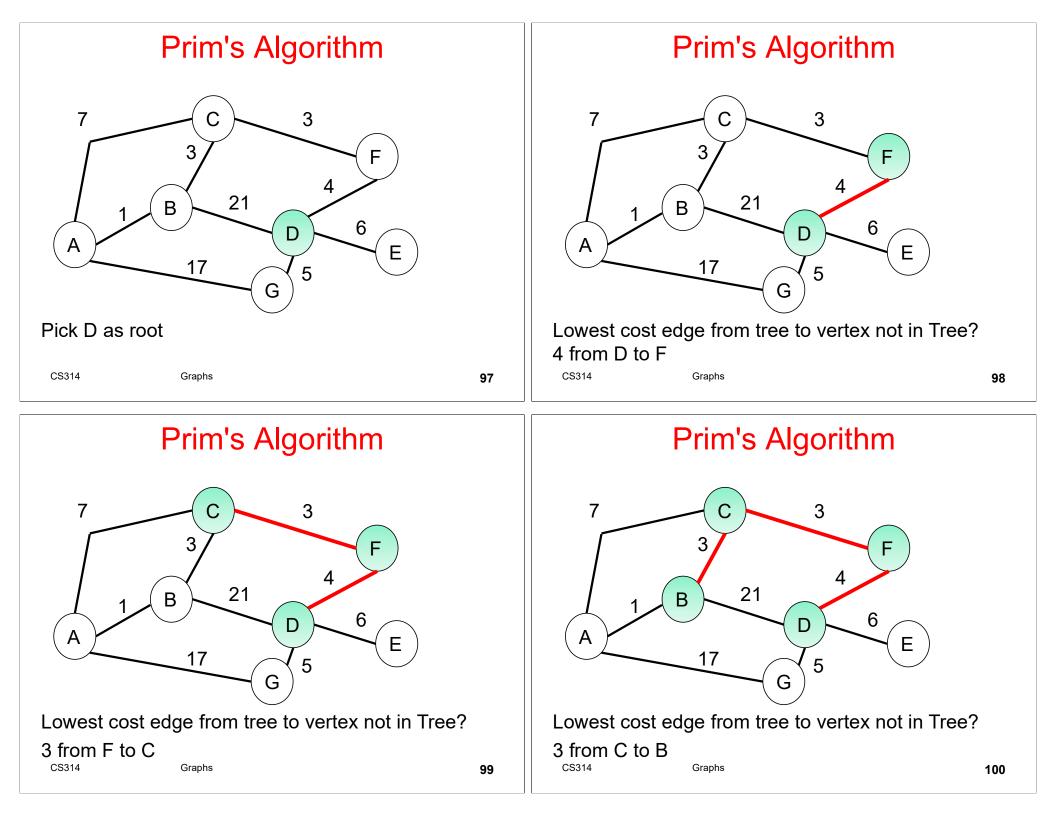
11

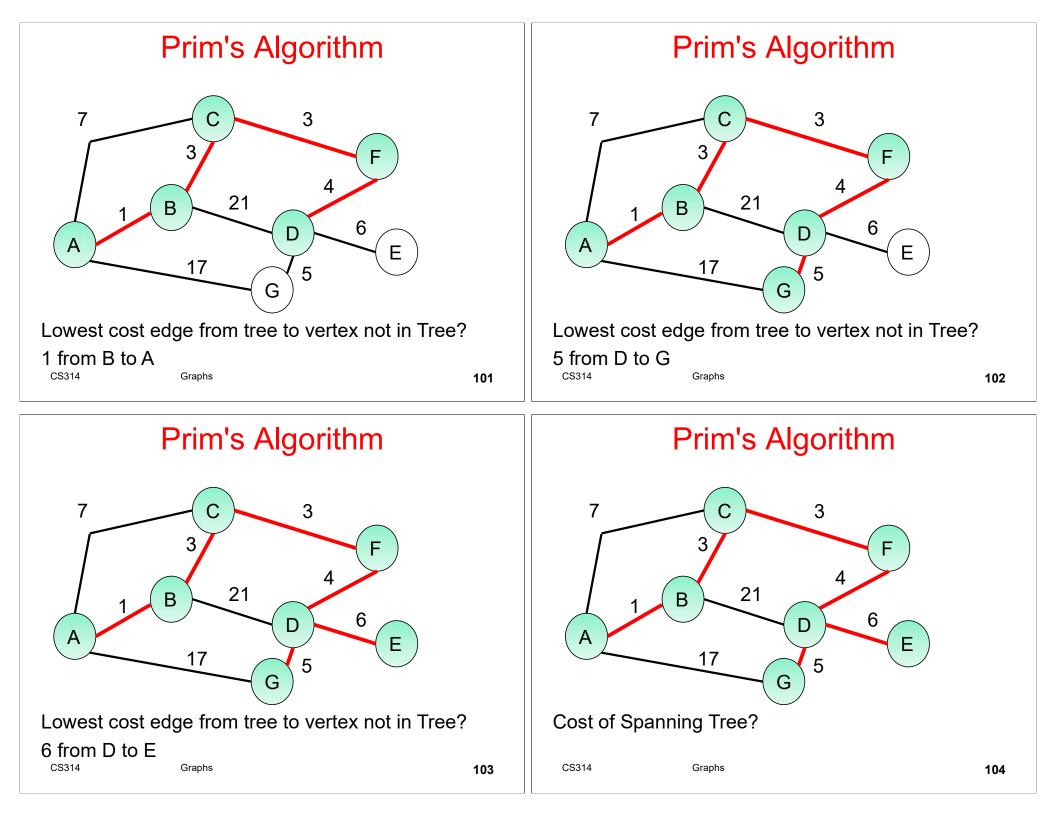
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6





Ot	her Grapl	h Algorithms	
 Lots! <u>http://en.wik</u> 	ipedia.org/wiki/C	Category:Graph_algorith	<u>ms</u>
CS314	Graphs		105

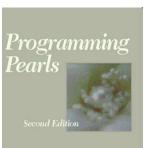
Topic 23 Hash Tables

"hash collision n. [from the techspeak] (var. `hash clash') When used of people, signifies a confusion in associative memory or imagination, especially a persistent one (see thinko).

True story: One of us was once on the phone with a friend about to move out to Berkeley. When asked what he expected Berkeley to be like, the friend replied: 'Well, I have this mental picture of naked people throwing Molotov cocktails, but I think that's just a collision in my hash tables."

-The Hacker's Dictionary

Programming Pearls by Jon Bentley







Jon was senior programmer on a large programming project.

Senior programmer spend a lot of time helping junior programmers.

Junior programmer to Jon: "I need help writing a sorting algorithm."

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Hash Tables

2

A Problem From Programming Pearls (Jon in Italics)

Why do you want to write your own sort at all? Why not use a sort provided by your system?

I need the sort in the middle of a large system, and for obscure technical reasons, I can't use the system file-sorting program.

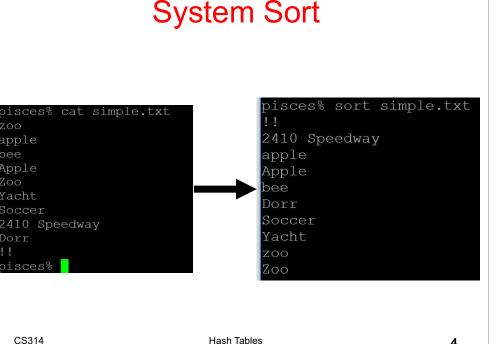
What exactly are you sorting? How many records are in the file? What is the format of each record?

The file contains at most ten million records: each record is a seven-digit integer.

Wait a minute. If the file is that small, why bother going to disk at all? Why not just sort it in main memory?

Although the machine has many megabytes of main memory, this function is part of a big system. I expect that I'll have only about a megabyte free at that point.

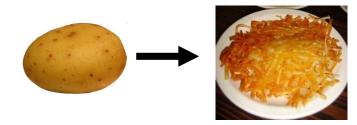
Is there anything else you can tell me about the records? Each one is a seven-digit positive integer with no other associated data, and no integer can appear more than once.



Starting Other Programs Starting Other Programs exec getRuntime public Process exec(String command) throws IOException public static Runtime getRuntime() Executes the specified string command in a separate process. Returns the runtime object associated with the current Java This is a convenience method. An invocation of the form application. Most of the methods of class Runtime are instance exec(command) behaves in exactly the same way as the invocation exec(command, null, null). methods and must be invoked with respect to the current runtime object. **Parameters: Returns:** command - a specified system command. the Runtime object associated with the current Java application. **Returns:** A new Process object for managing the subprocess CS314 Hash Tables CS314 Hash Tables 5 6 Clicker 1 and 2 A Solution When did this conversation take place? /* phase 1: initialize set to empty */ for i = [0, n]A. circa 1965 bit[i] = 0B. circa 1975 /* phase 2: insert present elements into the set */ C. circa 1985 for each num in file in the input file D. circa 1995 bit[num in file] = 1 E. circa 2005 /* phase 3: write sorted output */ What were they sorting? for i = [0, n]if bit[i] == 1 write i on the output file A. SSNs. B. Random values C. Street Addresses D. Personal Incomes E. Phone Numbers CS314 Hash Tables CS314 Hash Tables 7 8

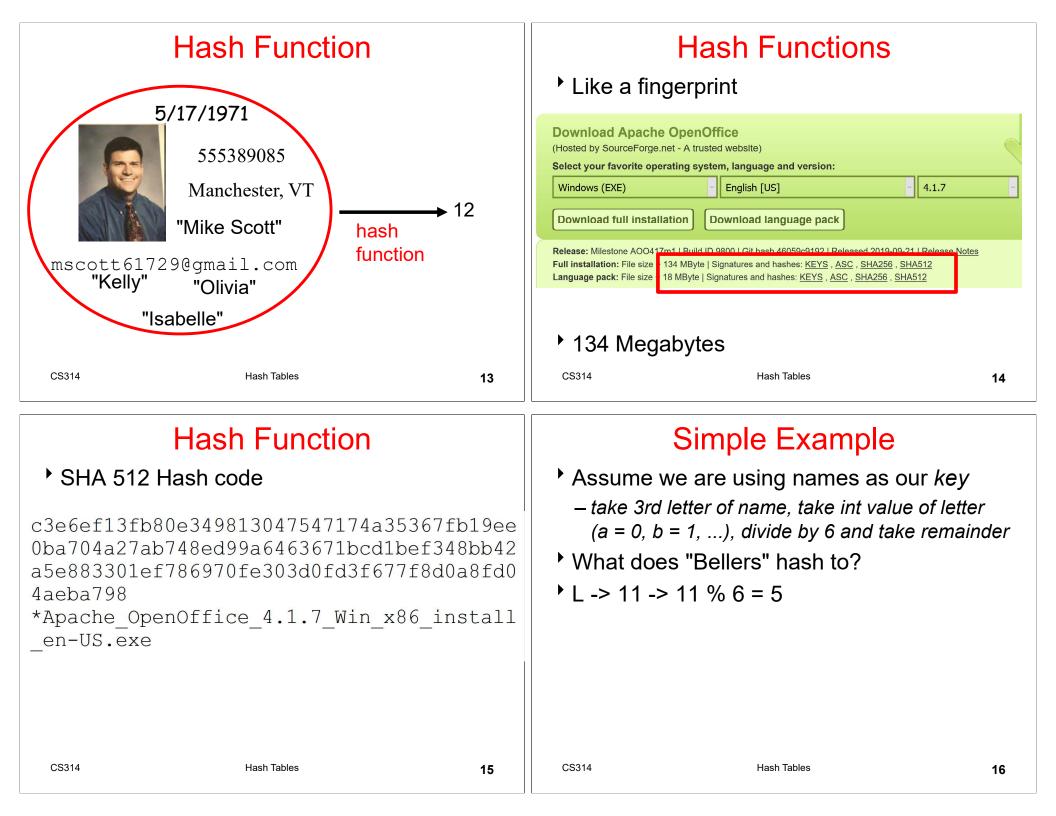
Some Structures so Far ArrayLists – O(1) access	 Why are Binary Trees Better? Divide and Conquer - splitting problem into smaller problems 		
 O(N) insertion (average case), better at end O(N) deletion (average case) LinkedLists 	Can we reduce the work by a bigger factor? 3? 10? More?		
 O(N) access O(N) insertion (average case), better at front and back O(N) deletion (average case), better at front and back Binary Search Trees 	 An ArrayList does this in a way when accessing elements but must use an integer value each position holds a single element given the index in an array, I can access that element rather quickly 		
 O(log N) access if balanced O(log N) insertion if balanced O(log N) deletion if balanced 			
CS314 Hash Tables 9	 determining the address of the element requires a multiply op and an add op 		
Hash Tables	Hash Functions		

Hash Tables maintaining the fast access of arrays but improve the order for insertion, and deletion compare to array based lists.



Hash tables use an array and hash functions to determine the index for each element.

- Hash: "From the French hatcher, which means 'to chop'. "
- to hash to mix randomly or shuffle (To cut up, to slash or hack about; to mangle)
- Hash Function: Take a piece of data and transforms it to a different piece of data (typically smaller), usually a single integer.
 - A function or algorithm
 - The input need not be integers!



Result of Hash Function • Mike = $(10 \% 6) = 4$ • Kelly = $(11 \% 6) = 5$ • Olivia = $(8 \% 6) = 2$ • Isabelle = $(0 \% 6) = 0$ • David = $(21 \% 6) = 3$ • Margaret = $(17 \% 6) = 5$ (uh oh) • Wendy = $(13 \% 6) = 1$ • This is an imperfect hash function. A perfect hash function yields a one to one mapping from the keys to the hash values. • What is the maximum number of values this function can hash perfectly?	<pre>Clicker 3 - Hash Function Assume the hash function for String adds up the Unicode value for each character. public static int hashCode(String s) { int result = 0; for (int i = 0; i < s.length(); i++) result += s.charAt(i); return result; } Hashcode for "DAB" and "BAD"? A. 301 103 B. 4 4 C. 412 214 D. 5 5</pre>		
 More on Hash Functions transform the key (which may not be an integer) into an integer value The transformation can use one of four techniques 	 Hashing Techniques Mapping As seen in the example integer values or things that can be easily converted to integer values in key 		

- Mapping

- Folding
- Shifting
- Casting

- eneu lo integer values in key
- Folding
 - partition key into several parts and the integer values for the various parts are combined
 - the parts may be hashed first
 - combine using addition, multiplication, shifting, logical exclusive OR

Hash Tables

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Shifting

More complicated with shifting

```
int hashVal = 0;
int i = str.length() - 1;
while(i > 0)
{ hashVal = (hashVal << 1) + (int) str.charAt(i);
    i--;
}
```

different answers for "dog" and "god"

Shifting may give a better range of hash values when compared to just folding

Casts

CS314

- Very simple
 - essentially casting as part of fold and shift when working with chars.

```
The Java String class hashCode method
```

```
public int hashCode() {
    int h = hash;
    if (h == 0 && value.length > 0) {
        char[] val = value;
        for (int i = 0; i < val.length; i++) {
            h = 31 * h + val[i];
        }
        hash = h;
    }
    return h;
}
CS314 HashTables</pre>
```

Mapping Results

Hash Tables

- Transform hashed key value into a legal index in the hash table
- Hash table is normally uses an array as its underlying storage container
- Normally get location on table by taking result of hash function, dividing by size of table, and taking remainder

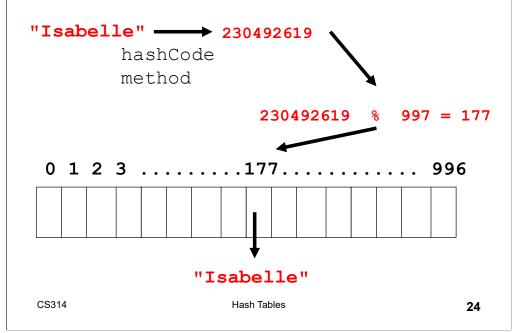
index = key mod n

n is size of hash table

empirical evidence shows a prime number is best

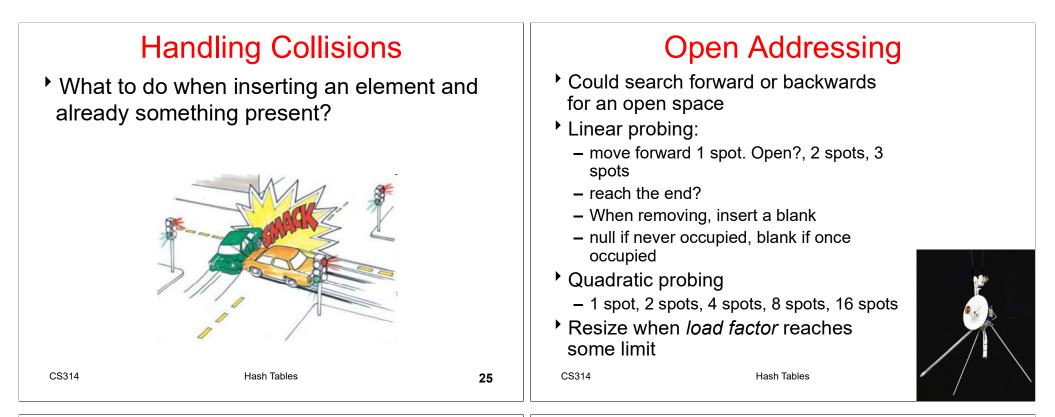
10 element hash table, move up to 11 or 13 elements

Mapping Results



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Closed Addressing: Chaining

- Each element of hash table be another data structure
 - linked list, balanced binary tree
 - More space, but somewhat easier
 - everything goes in its spot
- What happens when resizing?
 - Why don't things just collide again?



Hash Tables in Java

- hashCode method in Object
- hashCode and equals
 - "If two objects are equal according to the equals (Object) method, then calling the hashCode method on each of the two objects must produce the same integer result."
 - if you override equals you need to override hashCode
- Overriding one of equals and hashCode, but not the other, can cause logic errors that are difficult to track down if objects added to hash tables.

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Н	ash Tables in Jav	a		Comparison	
 HashTable class HashSet class implements Set interface with internal storage container that is a HashTable compare to TreeSet class, internal storage container is a Red Black Tree HashMap class implements the Map interface, internal storage container for keys is a hash table 			 Java Hasł Java Tree 	Set Binary Search Tree Fable	r speed:
CS314	Hash Tables	29	CS314	Hash Tables	30
A. HashSet B. HashSet C. TreeSet D. HashTab E. None of t	Clicker 4 • What will be order from fastest to slowest? A. HashSet TreeSet HashTable314 BST B. HashSet HashTable314 TreeSet BST C. TreeSet HashSet BST HashTable314 D. HashTable314 HashSet BST TreeSet E. None of these				
CS314	Hash Tables	31			

Topic 24 Clicker 1 Tries How would you pronounce "Trie" "In 1959, (Edward) Fredkin recommended A. "tree" that BBN (Bolt, Beranek and Newman, now B. "tri – ee" BBN Technologies) purchase the very first PDP-1 to support research projects at C. "try" BBN. The PDP-1 came with no software D. "tiara" whatsoever. E. something else Fredkin wrote a PDP-1 assembler called FRAP (Free of Rules Assembly Program);" Tries were first described by René de la Briandais in File searching using variable length keys. CS314 Tries 2 Tries aka Prefix Trees Predictive Text and AutoComplete Pronunciation: Search engines and texting applications guess what you want after typing only a few From retrieval characters Name coined by Computer Scientist **Edward Fredkin** Hel Retrieval so "tree" hello hellboy • ... but that is very confusing so most people hello fresh helen keller pronounce it "try" helena christensen

3

hello may

hell or high water hello neighbor helzberg help synonym

	AutoComplete		Searching a Dictionary			
So do other programs such as IDEs			• How?			
String name = "Kelly J";			Could search a set for all values that start with the given prefix.			
name.s			•	O(N) (search the whole dat	а	
<pre>while substring(int beginIndex, int endIndex) : String - String - 0.11% split(String regex) : String[] - String split(String regex, int limit) : String[] - String startsWith(String prefix) : boolean - String startsWith(String prefix, int toffset) : boolean - String subSequence(int beginIndex, int endIndex) : CharSequence - Stri substring(int beginIndex) : String - String</pre>			•	prove if possible to do a bi prefix and then localize s	•	
CS314	Tries	5	CS314	Tries	6	
	Tries		René de	la Briandais Origina	al Paper	
A general	tree (more than 2 children p	possible)	lst Letter	Table * CF		
Root node	e (or possibly a list of root no	odes)	2nd Letter	Tables AO IAO		
 Nodes can have many children not a binary tree 			·3rd Letter		XU	
 not a binary tree In simplest form each node stores a character and a data structure (list?) to refer to its children 		4th Letter 5th Letter 6th Letter		(№		
			1			

- and a data structure (list?) to refer to its children
- "Stores" all the words or phrases in a dictionary.

▶ How?

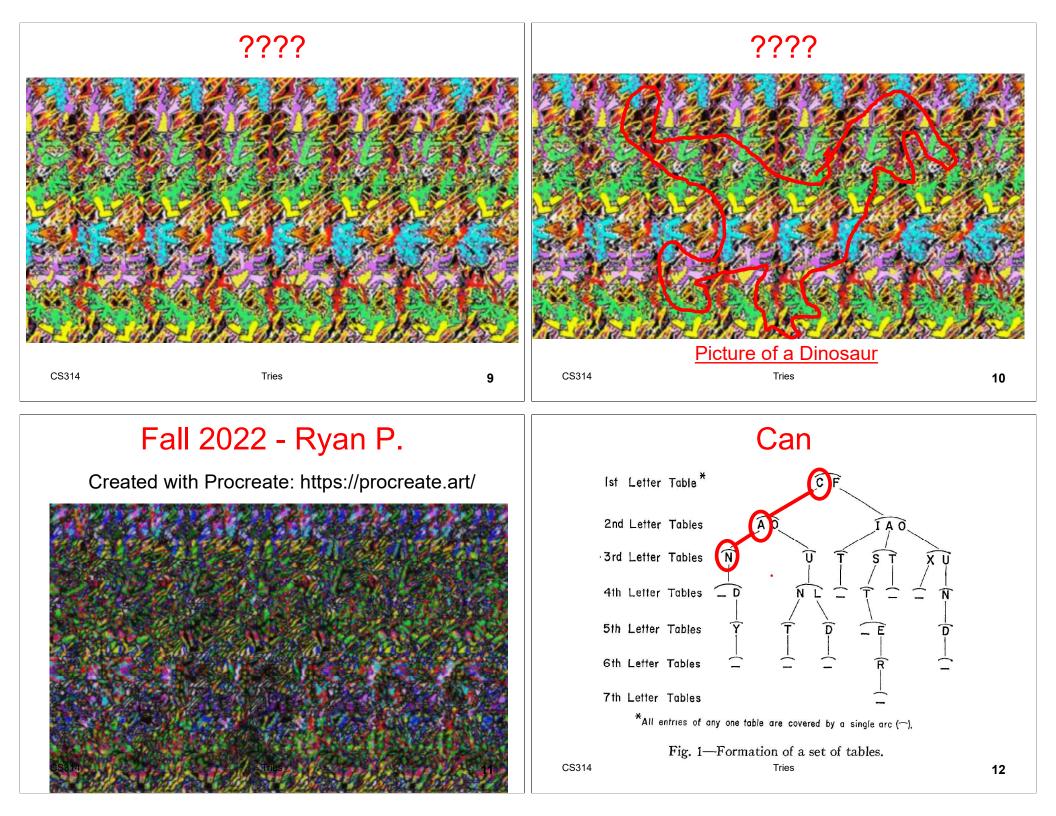
7

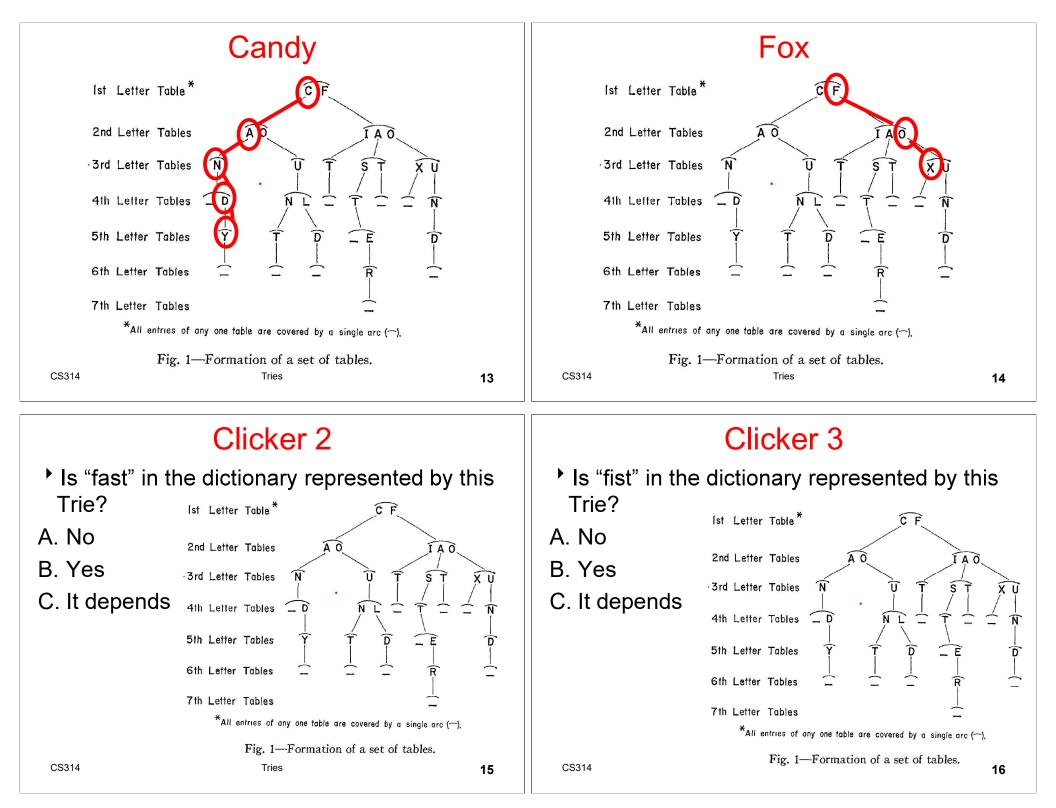
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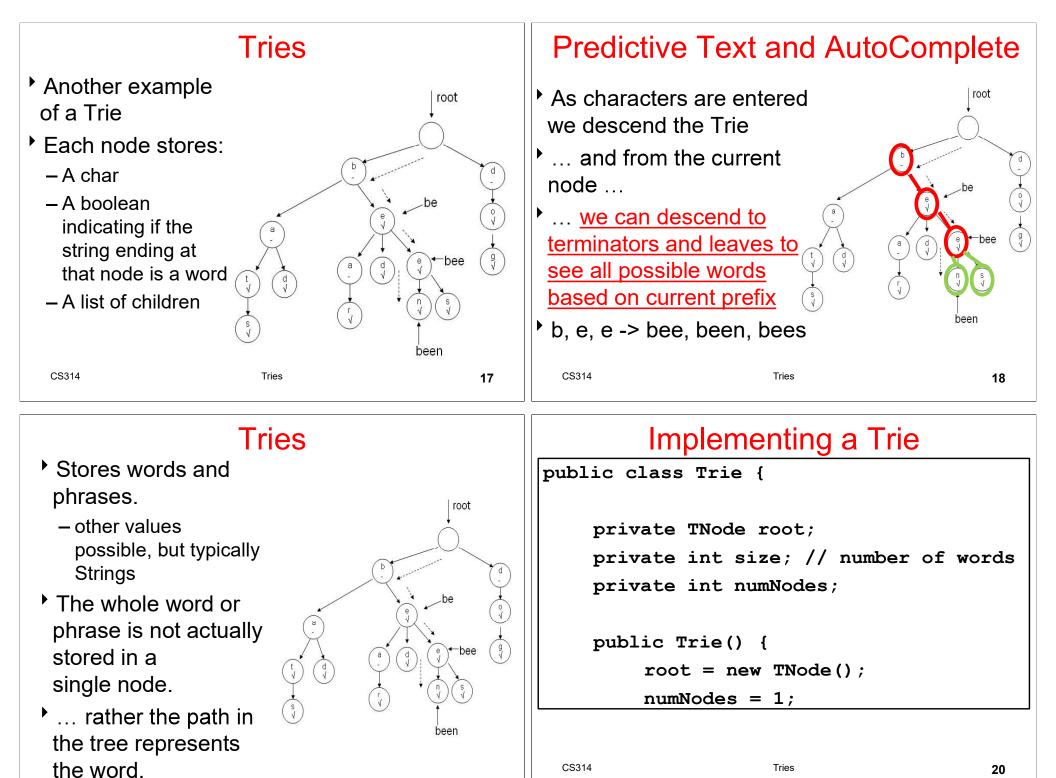
7th Letter Tables

Fig. 1-Formation of a set of tables. Tries

*All entries of any one table are covered by a single arc (--).







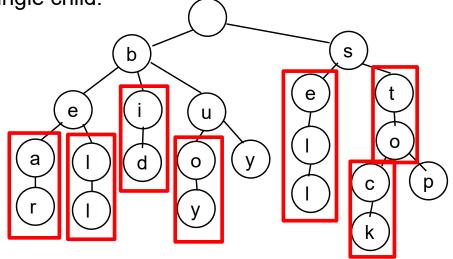
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Tries

	TNode Class		Basic Operations				
1-	class TNode {		 Adding a word to the Trie Getting all words with given prefix 				
private boolean word; private char ch; private LinkedList <tnode> children;</tnode>		 Demo in 	v .				
•	ementation uses a Link ects for children	edList of					
Other optic – ArrayList?							
CS314	Tries	21	CS314	Tries	22		

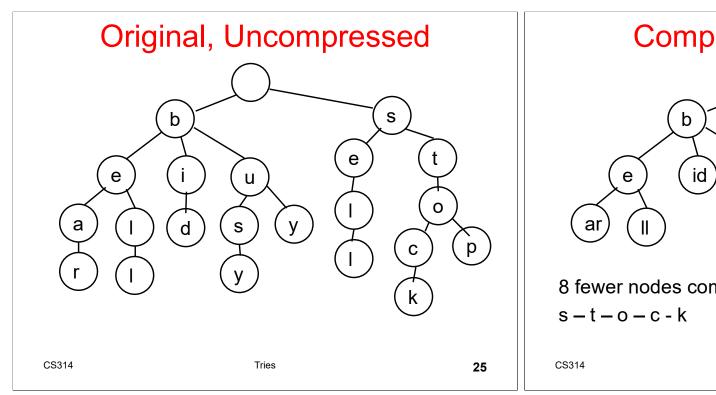
Compressed Tries

Some words, especially long ones, lead to a chain of nodes with single child, followed by single child:

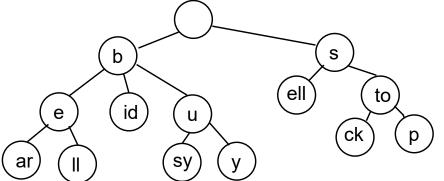


Compressed Trie

- Reduce number of nodes, by having nodes store Strings
- A chain of single child followed by single child (followed by single child ...) is compressed to a single node with that String
- Does not have to be a chain that terminates in a leaf node
 - Can be an internal chain of nodes



Compressed Version



8 fewer nodes compared to uncompressed version s - t - o - c - k

C	CS314	Tries	26

Topic 25 Heaps

"You think you know when you can learn, are more sure when you can write, even more when you can **teach**, but certain when you can program."

- Alan Perlis



Another Option

- The heap data structure
 - not to be confused with the runtime heap (portion of memory for dynamically allocated variables)
- Typically a complete binary tree (variations) with more than 2 children possible)
 - all levels have maximum number of nodes except deepest where nodes are filled in from left to right
- Maintains the heap order property
- in a min heap the value in the root of any subtree is less than or equal to all other values in the cs314 subtree

Heaps

- Recall priority queue
 - elements enqueued based on priority
 - dequeue removes the highest priority item
- Options?
 - List? Binary Search Tree? Clicker 1
- Array List enqueue **BST** enqueue A. O(N)
- C. O(N)
- D. O(logN) E. O(1)

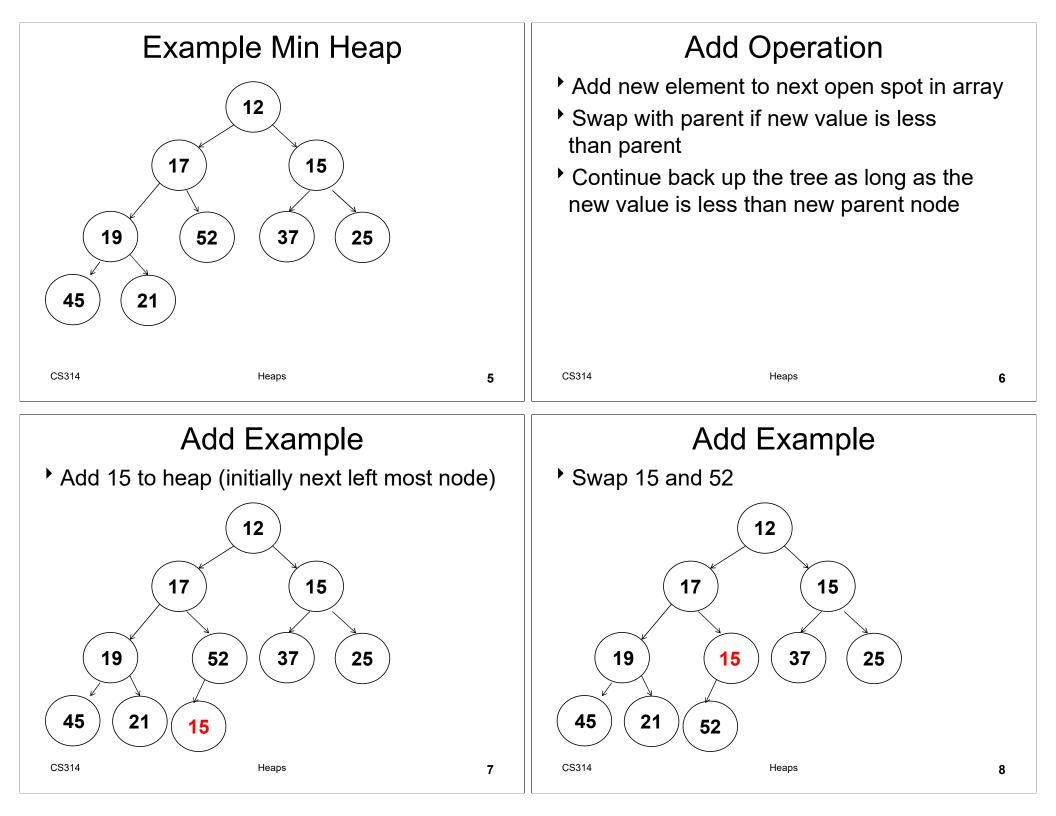
B. O(N)

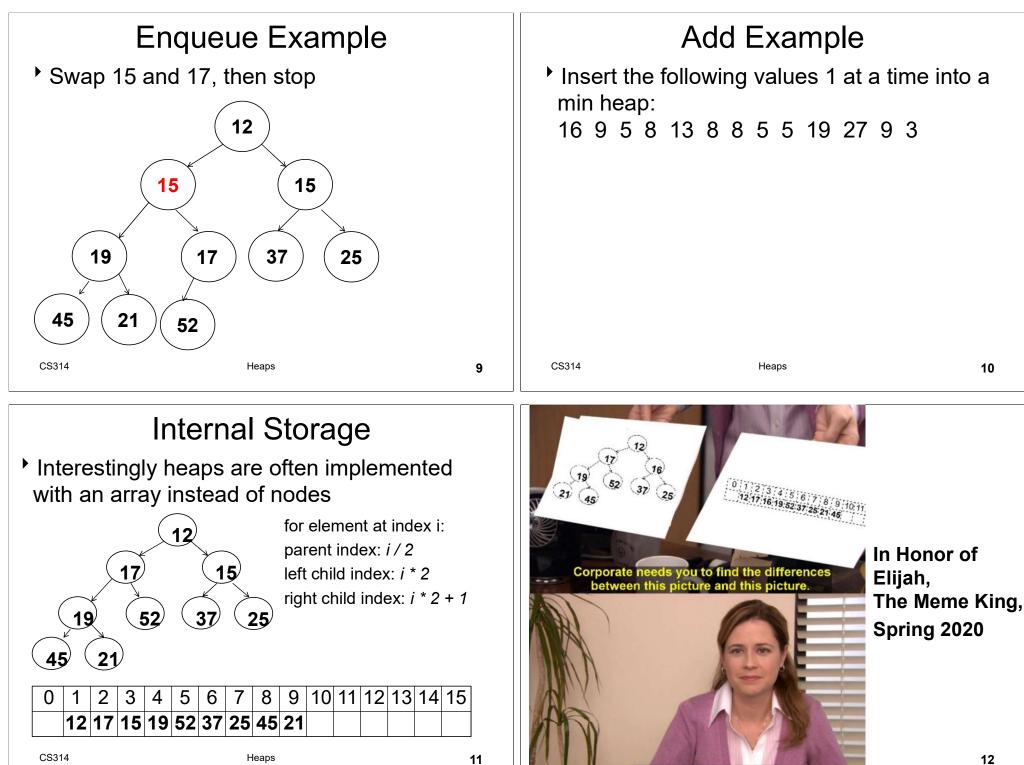
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O(1) O(logN) O(N) $O(\log N)$ O(logN) Heaps

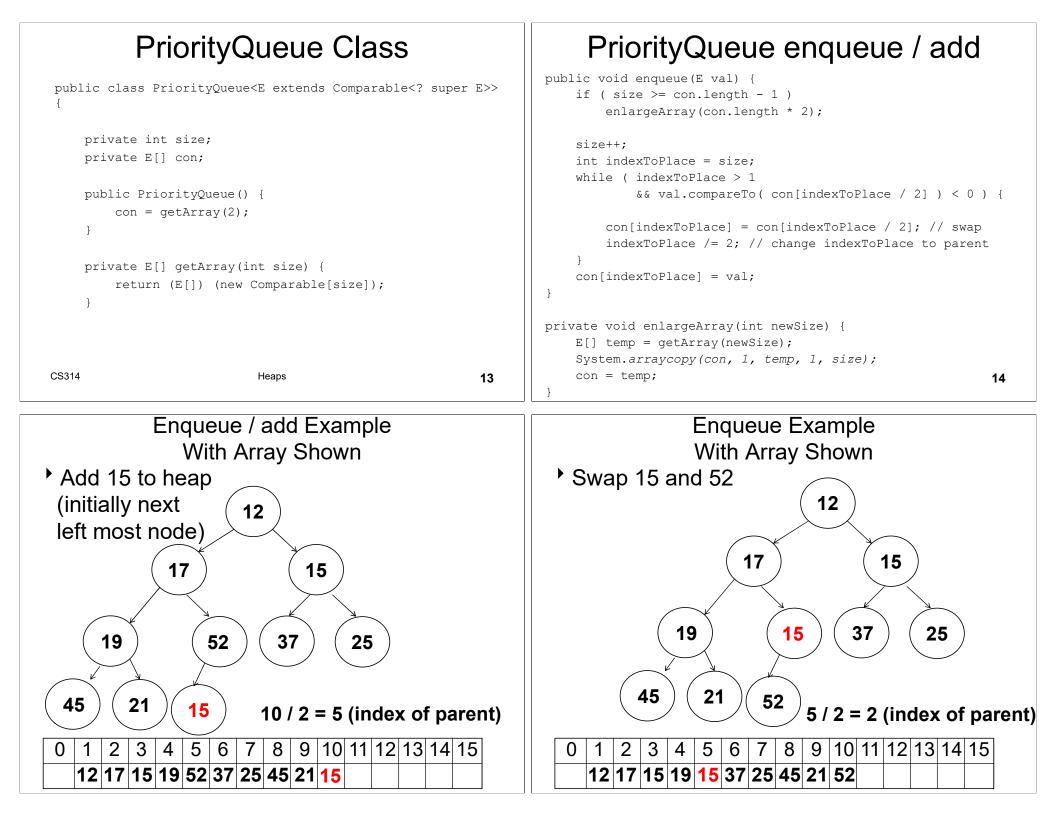
Clicker 2

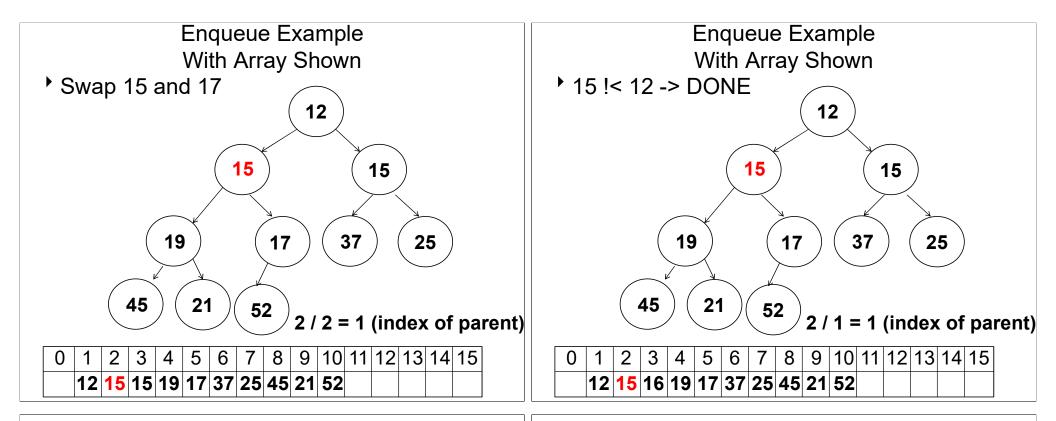
- In a max heap with no duplicates where is the largest value?
- A. the root of the tree
- B. in the left-most node
- C. in the right-most node
- D, a node in the lowest level
- E. none of these





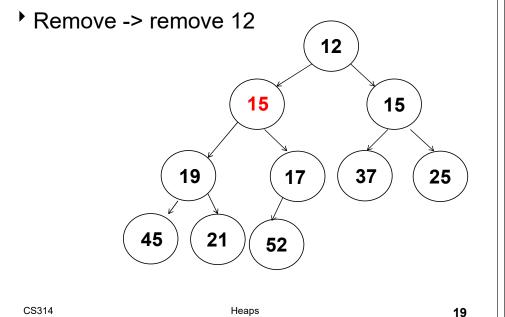
're the same pictu





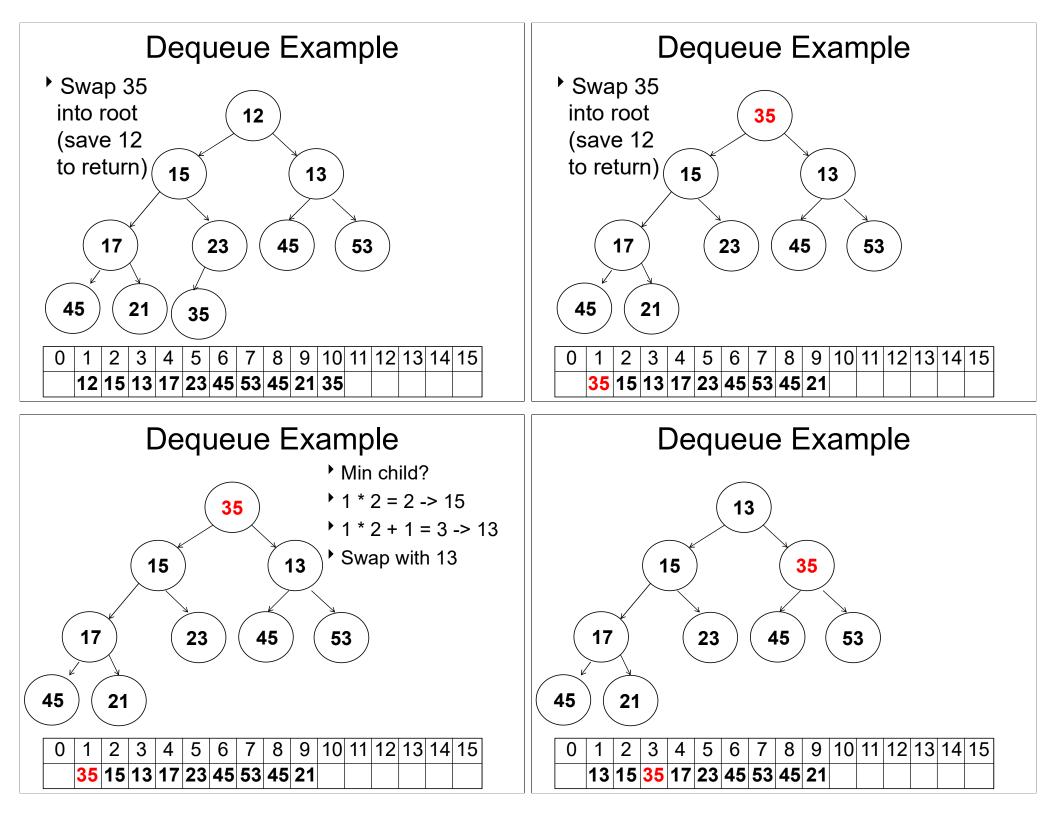
CS314

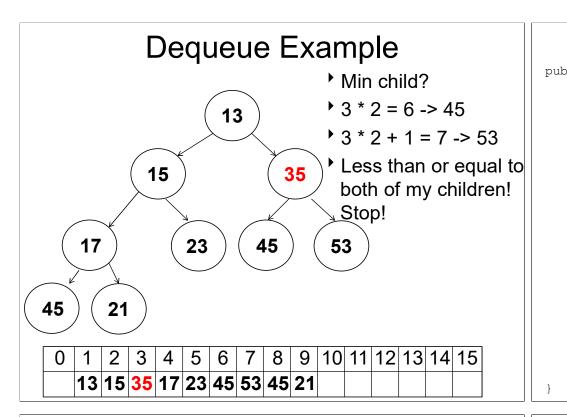
Remove / Dequeue



- min value / front of queue is in root of tree
- swap value from last node to root and move down swapping with smaller child unless values is smaller than both children

Heaps





Clicker 3 - PriorityQueue Comparison

- Run a Stress test of PQ implemented with Heap and PQ implemented with BinarySearchTree
- What will result be?
- A. Heap takes half the time or less of BST
- B. Heap faster, but not twice as fast
- C. About the same
- D. BST faster, but not twice as fast
- E. BST takes half the time or less of Heap

```
Dequeue Code
public E dequeue() {
    E \text{ top} = \text{con}[1];
    int hole = 1;
    boolean done = false;
    while ( hole * 2 < size \&\& ! done ) {
        int child = hole * 2;
        // see which child is smaller
        if ( con[child].compareTo( con[child + 1] ) > 0 )
            child++;
                        // child now points to smaller
        // is replacement value bigger than child?
        if (con[size].compareTo( con[child] ) > 0 ) {
            con[hole] = con[child];
            hole = child;
        }
        else
            done = true:
    con[hole] = con[size];
    size--;
    return top;
```

Data Structures

- Data structures we have studied
 - arrays, array based lists, linked lists, maps, sets, stacks, queues, trees, binary search trees, graphs, hash tables, red-black trees, priority queues, heaps, tries
- Most program languages have some built in data structures, native or library
- Must be familiar with performance of data structures
 - best learned by implementing them yourself

CS314

			D	ata Stru	ictures	
	ata typ iative an	pes [ed	it source edit beta] nary	Covered ed Array [edit source edit texe] Array Bidirectional map Bit aray Bit field Bitmap Cricular buffer Control table Image Dynamic aray Gap buffer Sached array tree Heightmap Lookup table Matrix Parallel array Sorted aray Sparse arary Sparse matrix	Heaps [edit source] edit Heaps [edit source] edit Heaps Heaps [edit source] edit Heaps Horacch heap AF-heap AF-heap AF-heap AF-heap AF-heap AF-heap AF-heap AF-heap Be	Structure Graphs [edit source edit bess] • Graph • Adjacency list • Adjacency matrix • Graph-structured stack • Scene graph • Binary decision diagram • And-inverter graph • Directed graph
Structure	Ctable	Ilaigue	Cells per Node	Variable-length array Lists [edit source] edit beta]	Radix tree Suffix tree	Other [edit source edit beta]
Bag (multiset)	000000000000	no	1	Doubly linked list	 Suffix array 	Lightmap
Set	no	1873	1	 Linked list Self-organizing list 	 Compressed suffix array FM-index 	Winged edge
		yes		Skip list	Generalised suffix tree	Doubly connected edge list
List Map Stable" means	yes no that inp	no yes put order	1 2 is retained. Other st	Unrolled linked list VList Xor linked list Zipper Doubly connected edge list Difference list	B-tree Judy array X-fast tree Y-fast tree Cree Multiway trees Ledit sou	Quad-edge Routing table Symbol table

Data Structures

- deque, b-trees, quad-trees, binary space partition trees, skip list, sparse list, sparse matrix, union-find data structure, Bloom filters, AVL trees, 2-3-4 trees, and more!
- Must be able to learn new and apply new data structures

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Heaps

Topic 26 Dynamic Programming

"Thus, I thought *dynamic programming* was a good name. It was something not even a Congressman could object to. So I used it as an umbrella for my activities"

- Richard E. Bellman



Origins

- A method for solving complex problems by breaking them into smaller, easier, sub problems
- Term *Dynamic Programming* coined by mathematician Richard Bellman in early 1950s
 - employed by Rand Corporation
 - Rand had many, large military contracts
 - Secretary of Defense, <u>Charles Wilson</u> "against research, especially mathematical research"
 - how could any one oppose "dynamic"?

CS314

Dynamic Programming

Dynamic Programming

- Break big problem up into smaller problems ...
- Sound familiar?

Recursion?
 N! = 1 for N == 0
 N! = N * (N - 1)! for N > 0

Failing Spectacularly	Failing Spectacularly
Naïve recursive method	1th fibonnaci number: 1 - Time: 4.467E-6 2th fibonnaci number: 1 - Time: 4.47E-7
<pre>// pre: n > 0 // post: return the nth Fibonacci number public int fib(int n) { if (n <= 2) return 1; else return fib(n - 1) + fib (n - 2); }</pre>	<pre>3th fibonnaci number: 2 - Time: 4.46E-7 4th fibonnaci number: 3 - Time: 4.46E-7 5th fibonnaci number: 5 - Time: 4.47E-7 6th fibonnaci number: 8 - Time: 4.47E-7 7th fibonnaci number: 13 - Time: 1.34E-6 8th fibonnaci number: 21 - Time: 1.787E-6 9th fibonnaci number: 34 - Time: 2.233E-6 10th fibonnaci number: 55 - Time: 3.573E-6 11th fibonnaci number: 89 - Time: 1.2953E-5</pre>
Clicker 1 - Order of this method?A. O(1)B. O(log N)C. O(N)D. O(N²)E. O(2N)CS314Dynamic Programming5	12th fibonnaci number: 144 - Time: 8.934E-6 13th fibonnaci number: 233 - Time: 2.9033E-5 14th fibonnaci number: 377 - Time: 3.7966E-5 15th fibonnaci number: 610 - Time: 5.0919E-5 16th fibonnaci number: 987 - Time: 7.1464E-5 17th fibonnaci number: 1597 - Time: 1.08984E-4

Failing Spectacularly

42th 43th 44th 45th 46th 47th	fibonnaci fibonnaci fibonnaci fibonnaci fibonnaci fibonnaci fibonnaci	number: number: number: number: number: number:	165580141 - Time: 0.498588795 267914296 - Time: 0.793824734 433494437 - Time: 1.323325593 701408733 - Time: 2.098209943 1134903170 - Time: 3.392917489 1836311903 - Time: 5.506675921 -1323752223 - Time: 8.803592621 512559680 - Time: 14.295023778 -811192543 - Time: 23.030062974
38th 39th	fibonnaci fibonnaci fibonnaci fibonnaci	number: number:	24157817 - Time: 0.071195386 39088169 - Time: 0.116922086 63245986 - Time: 0.186926245 102334155 - Time: 0.308602967
0.000	fibonnaci		14930352 - Time: 0.045372057

Clicker 2 - Failing Spectacularly

50th fibonnaci number: -298632863 - Time: 37.217

- How long to calculate the 70th Fibonacci Number with this method?
- A. 37 seconds
- B. 74 seconds
- C. 740 seconds
- D. 14,800 seconds
- E. None of these

	Aside - Overflow		Aside - BigInteger	
• at 47 th Fi	bonacci number overflows	s int Answe	rs correct beyond 46 th Fibonad	cci number
Could us	e BigInteger class instead	J	lower, math on BigIntegers,	
-	c final BigInteger one BigInteger("1");		creation, and garbage collection	on
	c final BigInteger two BigInteger("2");	38th fibon	naci number: 39088169 - Time: 3.	406739213 680196724 941275208
	<pre>BigInteger fib(BigInteger n) { compareTo(two) <= 0) return one; BigInteger firstTerm = fib(n.subt BigInteger secondTerm = fib(n.sub return firstTerm.add(secondTerm);</pre>	<pre>ract(two)); tract(one));</pre> 40th fibon 41th fibon 42th fibon 43th fibon 43th fibon 45th fibon 46th fibon	naci number: 102334155 - Time: 9 naci number: 165580141 - Time: 1 naci number: 267914296 - Time: 2 naci number: 433494437 - Time: 4 naci number: 701408733 - Time: 6 naci number: 1134903170 - Time: naci number: 1836311903 - Time:	.63855468 5.659745756 5.404417949 0.867030512 6.391845965 106.9643699 178.9818198 287.0523653
CS314	Dynamic Programming	9 CS314	Dynamic Programming	10
▸ Why so	Slow Fibonacci		Fast Fibonacci ad of starting with the big p	
Algorith value ov	m keeps calculating the ver and over	e same 🔰 sta work	orking down to the small p art with the small problem a up to the big problem	
number	alculating the 40 th Fibo the algorithm calculate ci number <u>24,157,817</u>	es the 4 th times!!!	atic BigInteger fastFib(int n) { bigInteger smallTerm = one; bigInteger largeTerm = one; br (int i = 3; i <= n; i++) { BigInteger temp = largeTerm; largeTerm = largeTerm.add(smallTerm) smallTerm = temp;);
		}		

Fast Fibonacci
1th fibonnaci number: 1 - Time: 4.467E-6
2th fibonnaci number: 1 - Time: 4.47E-7
3th fibonnaci number: 2 - Time: 7.146E-6
4th fibonnaci number: 3 - Time: 2.68E-6
5th fibonnaci number: 5 - Time: 2.68E-6
6th fibonnaci number: 8 - Time: 2.679E-6
7th fibonnaci number: 13 - Time: 3.573E-6
8th fibonnaci number: 21 - Time: 4.02E-6
9th fibonnaci number: 34 - Time: 4.466E-6
10th fibonnaci number: 55 - Time: 4.467E-6
11th fibonnaci number: 89 - Time: 4.913E-6
12th fibonnaci number: 144 - Time: 6.253E-6
13th fibonnaci number: 233 - Time: 6.253E-6
14th fibonnaci number: 377 - Time: 5.806E-6
15th fibonnaci number: 610 - Time: 6.7E-6
16th fibonnaci number: 987 - Time: 7.146E-6
17th fibonnaci number: 1597 - Time: 7.146E-6

Memoization

- Store (cache) results from computations for later lookup
- Memoization of Fibonacci Numbers

```
public class FibMemo {
    private static List<BigInteger> lookupTable;
    private static final BigInteger ONE
        = new BigInteger ("1");
    static {
        lookupTable = new ArrayList<>();
        lookupTable.add(null);
        lookupTable.add(ONE);
        look
```

5

Fast Fibonacci 45th fibonnaci number: 1134903170 -Time: 1.7419E-5 46th fibonnaci number: 1836311903 -Time: 1.6972E-5 47th fibonnaci number: 2971215073 -Time: 1.6973E-5 48th fibonnaci number: 4807526976 -Time: 2.3673E-5 49th fibonnaci number: 7778742049 -Time: 1.9653E-5 50th fibonnaci number: 12586269025 -Time: 2.01E-5 51th fibonnaci number: 20365011074 -Time: 1.9207E-5 52th fibonnaci number: 32951280099 -Time: 2.0546E-5 67th fibonnaci number: 44945570212853 - Time: 2.3673E-5 68th fibonnaci number: 72723460248141 - Time: 2.3673E-5 69th fibonnaci number: 117669030460994 -Time: 2.412E-5 70th fibonnaci number: 190392490709135 -Time: 2.4566E-5 71th fibonnaci number: 308061521170129 -Time: 2.4566E-5 72th fibonnaci number: 498454011879264 -Time: 2.5906E-5 73th fibonnaci number: 806515533049393 -Time: 2.5459E-5 74th fibonnaci number: 1304969544928657 -Time: 2.546E-5

200th fibonnaci number: 280571172992510140037611932413038677189525 - Time: 1.0273E-5

Fibonacci Memoization public static BigInteger fib(int n) { // check lookup table if (n < lookupTable.size()) {</pre> return lookupTable.get(n); ł // Calculate nth Fibonacci. // Don't repeat work. Start with the last known. BigInteger smallTerm = lookupTable.get(lookupTable.size() - 2); BigInteger largeTerm = lookupTable.get(lookupTable.size() - 1); for(int i = lookupTable.size(); i <= n; i++) {</pre> BigInteger temp = largeTerm; largeTerm = largeTerm.add(smallTerm); lookupTable.add(largeTerm); // memo smallTerm = temp; ł return largeTerm;

Dynamic Programming	DP Algorithms
 When to use? When a big problem can be broken up into sub 	Step 1: Define the *meaning* of the subproblems (in English for sure, Mathematically as well if you find it helpful).
 problems. Solution to original problem can be calculated from results of smaller problems. – larger problems depend on previous solutions Sub problems must have a natural ordering from smallest to largest (simplest to hardest) Multiple techniques within DP 	 Step 2: Show where the solution will be found. Step 3: Show how to set the first subproblem. Step 4: Define the order in which the subproblems are solved. Step 5: Show how to compute the answer to each subproblem using the previously computed subproblems. (This step is typically polynomial, once the other subproblems are solved.)
CS314 Dynamic Programming 17	CS314 Dynamic Programming 18
Dynamic Programming Requires: • overlapping sub problems: – problem can be broken down into sub problems – obvious with Fibonacci – Fib(N) = Fib(N - 2) + Fib(N - 1) for N >= 3 • optimal substructure: – the optimal solution for a problem can be constructed from optimal solutions of its sub problems – In Fibonacci just sub problems, no optimality – min coins opt(36) = 1_{12} + opt(24) [1, 5, 12] ^(X314)	 Dynamic Programing Example Another simple example Finding the best solution involves finding the best answer to simpler problems Given a set of coins with values (V₁, V₂, V_N and a target sum S, find the fewest coins required to equal S What is Greedy Algorithm approach? Does it always work? {1, 5, 12} and target sum = 15 (12, 1, 1, 1) Could use recursive backtracking CS314 Dynamic Programming 20

 Minimum Number of Coins To find minimum number of coins to sum to 15 with values {1, 5, 12} start with sum 0 recursive backtracking would likely start with 15 Let M(S) = minimum number of coins to sum to S At each step look at target sum, coins available, and previous sums pick the smallest option 			Minimum Number of Coins M(0) = 0 coins M(1) = 1 coin (1 coin) M(2) = 2 coins (1 coin + M(1)) M(3) = 3 coins (1 coin + M(2)) M(4) = 4 coins (1 coin + M(3)) M(5) = interesting, 2 options available: 1 + others OR single 5 if 1 then 1 + M(4) = 5, if 5 then 1 + M(0) = 1 clearly better to pick the coin worth 5		
CS314	Dynamic Programming	21	CS314	Dynamic Programming	22
Minim M(0) = 0 M(1) = 1 (1 coin M(2) = 2 (1 coin M(3) = 3 (1 coin M(4) = 4 (1 coin M(5) = 1 (1 coin M(6) = 2 (1 coin M(7) = 3 (1 coin M(8) = 4 (1 coin M(9) = 5 (1 coin M(10) = 2 (1 coi options: 1, 5	 + M(1)) + M(2)) + M(3)) + M(0)) + M(5)) + M(6)) + M(7)) + M(8)) M(12) = 1 (1 coin options: 1, 5, 12 M(13) = 2 (1 coin options: 1, 12 M(14) = 3 (1 coin options: 1, 12 	+ M(10)) + M(0)) + M(12)) + M(13))	RECI	PSACK PROBLEM - JRSIVE BACKTRACK DYNAMIC PROGRAM	
CS314	Dynamic Programming	23	CS314	Dynamic Programming	24

Knapsack Problem

- A variation of a *bin packing* problem
- Similar to fair teams problem from recursion assignment
- You have a set of items

CS314

- Each item has a weight and a value
- You have a knapsack with a weight limit
- Goal: Maximize the <u>value</u> of the items you put in the knapsack without exceeding the weight limit

Knapsack Example

Items:	ltem Number	Weight of Item	Value of Item	Value per unit Weight
	1	1	6	6.0
	2	2	11	5.5
Weight	3	4	1	0.25
	4	4	12	3.0
Limit = 8	5	6	19	3.167
	6	7	12	1.714

- A greedy solution: Take the highest ratio item that will fit: (1, 6), (2, 11), and (4, 12)
- Total value = 6 + 11 + 12 = 29
- Clicker 3 Is this optimal? A. No B. Yes

Knapsack - Recursive Backtracking

Dynamic Programming

25

```
private static int knapsack(ArrayList<Item> items,
        int current, int capacity) {
   int result = 0;
   if (current < items.size()) {</pre>
        // don't use item
        int withoutItem
            = knapsack(items, current + 1, capacity);
        int withItem = 0;
        // if current item will fit, try it
        Item currentItem = items.get(current);
        if (currentItem.weight <= capacity) {
            withItem += currentItem.value;
            withItem += knapsack(items, current + 1,
                    capacity - currentItem.weight);
        result = Math.max(withoutItem, withItem);
    }
   return result;
```

Knapsack - Dynamic Programming

- Recursive backtracking starts with max capacity and makes choice for items: choices are:
 - take the item if it fits
 - don't take the item
- Dynamic Programming, start with simpler problems
- Reduce number of items available
- AND Reduce weight limit on knapsack
- Creates a 2d array of possibilities
 Dynamic Programming

Knapsack - Optimal Function	Knapsack Optimal Function
OptimalSolution(items, weight) is best solution given a subset of items and a weight	OptimalSolution(items, weight limit) =
limit	0 if 0 items
2 options:	OptimalSolution(items - 1, weight) if weight of
 OptimalSolution does not select ith item – select best solution for items 1 to i - 1with weight limit of w 	ith item is greater than allowed weight $w_i > w$ (In others i th item doesn't fit)
 OptimalSolution selects ith item New weight limit = w - weight of ith item select best solution for items 1 to i - 1with new 	max of (OptimalSolution(items - 1, w), value of i th item +
weight limit 29	OptimalSolution(items - 1, w - w _i) CS314 Dynamic Programming 30

Knapsack - Algorithm

 Create a 2d array to store value of best option given subset of items and possible weights

1	6
2	11
4	1
4	12
6	19
7	12
	4 4 6

- In our example 0 to 6
 items and weight limits of of 0 to 8
- Fill in table using OptimalSolution Function

Knapsack Algorithm

Given N items and WeightLimit

Create Matrix M with N + 1 rows and WeightLimit + 1 columns

For weight = 0 to WeightLimit M[0, w] = 0

```
For item = 1 to N
for weight = 1 to WeightLimit
if(weight of ith item > weight)
M[item, weight] = M[item - 1, weight]
```

else

M[item, weight] = max of M[item - 1, weight] AND value of item + M[item - 1, weight - weight of item]

Knar	ารล	ick	- T	abl	e		Item	Weight	t Value	Knap	sac	:k -	Сс	omr	olet	ed	Ta	ble	
i ti i ci j			•		Ŭ		1	1	6	ittap	040			····r					
							2	2	11	items / weight	0	1	2	3	4	5	6	7	8
							3	4	1										
							4	4	12	8	0	0	0	0	0	0	0	0	
							5	6	19		U	U	U	U	U	U	U	U	
							6	7	12	{1}	0	6	6	6	6	6	6	6	
tems / capacity	0	1	2	3	4	5	6	7	8	[1, 6]	U	U	U	U	U	U	U	U	
0								_		{1,2}	0	6	11	17	17	17	17	17	1
}	0	0	0	0	0	0	0	0	0	[2, 11]	Ŭ	Ŭ	••		• •	• •		• •	
1}										{1, 2, 3}	0	6	11	17	17	17	17	18	1
{1, <u>2</u> }										[4, 1]	Ŭ	Ŭ	•••	• •	• •	• •	• •	10	
										{1, 2, 3, 4}	0	6	11	17	17	18	23	29	29
[1, 2, <u>3</u>]										[4, 12]	Ŭ	Ŭ	•••		• •	10	20	20	2
{1, 2, 3, <u>4</u> }										{1, 2, 3, 4, 5}	0	6	11	17	17	18	23	29	3(
{1, 2, 3, 4, <u>5</u> }										[6, 19]	Ű	Ŭ	••		• •			_0	•
										{1, 2, 3, 4, 5, 6}	0	6	11	17	17	18	23	29	30
{1, 2, 3, 4, 5, <u>6</u> }										[7, 12]	5	5			• •	10	20	20	0

Knapsack - Items to Take

items / weight	0	1	2	3	4	5	6	7	8
0	0	0	0	0	0	0	0	0	0
{1} [1, 6]	0	6	6	6	6	6	6	6	6
{1,2} [2, 11]	0	6	11	17	17	17	17	17	17
{1, 2, 3} [4, 1]	0	6	(11	17	17	17	17	17	17
{1, 2, 3, 4} [4, 12]	0	6	(11	17	17	18	23	29	29
{1, 2, 3, 4, 5} [6, 19]	0	6	11	17	17	18	23	29	30
{1, 2, 3, 4, 5, 6} [7, 12]	0	6	11	17	17	18	23	29	30

Dynamic Knapsack

```
// dynamic programming approach
public static int knapsack(ArrayList<Item> items, int maxCapacity) {
    final int ROWS = items.size() + 1;
    final int COLS = maxCapacity + 1;
    int[][] partialSolutions = new int[ROWS][COLS];
    // first row and first column all zeros
    for(int item = 1; item <= items.size(); item++) {</pre>
        for(int capacity = 1; capacity <= maxCapacity; capacity++) {</pre>
            Item currentItem = items.get(item - 1);
            int bestSoFar = partialSolutions[item - 1][capacity];
            if( currentItem.weight <= capacity) {</pre>
                int withItem = currentItem.value;
                int capLeft = capacity - currentItem.weight;
                withItem += partialSolutions[item - 1][capLeft];
                if (withItem > bestSoFar) {
                    bestSoFar = withItem;
                }
            }
            partialSolutions[item][capacity] = bestSoFar;
        }
    }
    return partialSolutions[ROWS - 1][COLS - 1];
```

Topic 27 Functional Programming

Functional Programming with Java 8

"It's a long-standing principle of programming style that the functional elements of a program should not be too large. If some component of a program grows beyond the stage where it's readily comprehensible, it becomes a mass of complexity which conceals errors as easily as a big city conceals fugitives. Such software will be hard to read, hard to test, and hard to debug." – Paul Graham

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What is FP?

- functional programming: A style of programming that emphasizes the use of functions (methods) to decompose a complex task into subtasks.
 - Examples of functional languages: LISP, Scheme, ML, Haskell, Erlang, F#, Clojure, ...
- Java is considered an object-oriented language, not a functional language.
- But Java 8 added several language features to facilitate a partial functional programming style.
 - Popular contemporary languages tend to be *Multi Paradigm Languages*

Java 8 FP features

- 1. Effect-free programming
- 2. First-class functions
- 3. Processing structured data via functions
- 4. Function closures
- 5. Higher-order operations on collections

Effect-free code (19.1)

2

- **side effect**: A change to the state of an object or program variable produced by a call on a function (i.e., a method).
 - example: modifying the value of a variable
 - example: printing output to System.out
 - example: reading/writing data to a file, collection, or network

int result = f(x) + f(x); int result = 2 * f(x);

- Are the two above statements equivalent?
 - Yes, **if** the function f() has no *side effects.*
 - One goal of functional programming is to minimize side effects.

Code w/ side effects	First-class functions (19.2)
<pre>public class SideEffect { public static int x; public static int f(int n) { x = x * 2; return x + n; } // what if it were 2 * f(x)? public static void main(String[] args) { x = 5; int result = f(x) + f(x); System.out.println(result); } }</pre>	 first-class citizen: An element of a programming language that is tightly integrated with the language and supports the full range of operations generally available to other entities in the language. In functional programming, functions (methods) are treated as first-class citizens of the languages. can store a function in a variable can pass a function as a parameter to another function can return a function as a value from another function can create a collection of functions
Lambda expressions	MathMatrix add / subtract

```
• lambda expression ("lambda"): Expression that describes a function by specifying its parameters and return value.
```

- Java 8 adds support for lambda expressions.
- Essentially an anonymous function (aka method)

```
• Syntax:
```

```
(parameters) -> expression
```

```
• Example:
```

}

(x) -> x * x // squares a number

- The above is roughly equivalent to: public static int squared(int x) { return x * x;

```
• Recall the MathMatrix class:
```

```
public MathMatrix add(MathMatrix rhs) {
    int[][] res = new int[cells.length][cells[0].length];
    for (int r = 0; r < res.length; r++)
        for (int c = 0; c < res[0].length; c++)
            res[r][c] = cells[r][c] + rhs.cells[r][c];
    return new MathMatrix(res);
}
public MathMatrix subtract(MathMatrix rhs) {</pre>
```

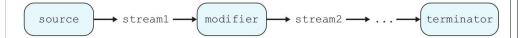
```
int[][] res = new int[cells.length][cells[0].length];
for (int r = 0; r < res.length; r++)
for (int c = 0; c < res[0].length; c++)
res[r][c] = cells[r][c] - rhs.cells[r][c];
return new MathMatrix(res);
```

```
7
```

MathMatrix add / subtract	Code w/ lambdas
 GACKIII How do we generalize the idea of "add or subtract"? How much work would it be to add other operators? Can functional programming help remove the repetitive code? 	<pre>• We can represent the math operation as a lambda: public MathMatrix add(MathMatrix rhs) { return getMat(rhs, (x, y) -> x + y); } public MathMatrix subtract(MathMatrix rhs) { return getMat(rhs, (x, y) -> x - y); }</pre>
getMat method	Clicker 1
<pre>private MathMatrix getMat(MathMatrix rhs,</pre>	 •Which of the following is a lambda that checks if x divides evenly into y? A. (x, y) -> y / x == 0 B. (x, y) -> x / y == 0 C. (x, y) -> y % x == 0 D. (x, y) -> x % y == 0 E. (x, y) -> y * x == 0

Streams (19.3)

- **stream**: A sequence of elements from a data source that supports aggregate operations.
- Streams operate on a data source and modify it:



- example: print each element of a collection
- example: sum each integer in a file
- example: concatenate strings together into one large string
- example: find the largest value in a collection

```
- ...
```

Code w/o streams

• Non-functional programming sum code:

13

15

```
// compute the sum of the squares of integers 1-5
int sum = 0;
for (int i = 1; i <= 5; i++) {
    sum += i * i;
}</pre>
```

14

The map modifier

- The map modifier applies a lambda to each stream element: – **higher-order function**: Takes a function as an argument.
- Abstracting away loops (and data structures)

```
// compute the sum of the squares of integers 1-5
int sum = IntStream.range(1, 6)
.map(n -> n * n)
.sum();
// the stream operations are as follows:
```

The filter modifier

• The filter stream modifier removes/keeps elements of the stream using a boolean lambda:

```
// compute the sum of squares of odd integers
int sum =
    IntStream.of(3, 1, 4, 1, 5, 9, 2, 6, 5, 3)
    .filter(n -> n % 2 != 0)
    .map(n -> n * n)
    .sum();
```

```
// the stream operations are as follows:
IntStream.of -> [3, 1, 4, 1, 5, 9, 2, 6, 5, 3]
    -> filter -> [3, 1, 1, 5, 9, 5, 3]
        -> map -> [9, 1, 1, 25, 81, 25, 9]
        -> sum -> 151
```

Streams and methods	The reduce modifier
 using streams as part of a regular method: // Returns true if the given integer is prime. // Assumes n >= 2. public static boolean isPrime(int n) { return IntStream.range(1, n + 1) .filter(x -> n % x == 0) .count() == 2; } How to make this method faster? 	 The reduce modifier (method) combines elements of a stream using a lambda combination function. Accepts two parameters: an initial value and a lambda to combine that initial value with each subsequent value in the stream. // Returns n!, or 1 * 2 * 3 * * (n-1) * n. // Assumes n is non-negative. public static int factorial(int n) { return IntStream.range(2, n + 1) .reduce(1, (a, b) -> a * b); }

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Stream operators

Method name	Description	
anyMatch(f)	returns true if any elements of stream match given predicate	
allMatch(f)	returns true if all elements of stream match given predicate	
average()	returns arithmetic mean of numbers in stream	
collect(f)	convert stream into a collection and return it	
count()	returns number of elements in stream	
distinct()	returns unique elements from stream	
filter(f)	returns the elements that match the given predicate	
forEach(f)	performs an action on each element of stream	
limit(size)	returns only the next size elements of stream	
map(f)	applies the given function to every element of stream	
noneMatch (\mathbf{f})	returns true if zero elements of stream match given predicate	
		19

Stream operators

Method name	Desc	ription		
parallel()	return	returns a multithreaded version of this stream		
peek (f)	exami	examines the first element of stream only		
reduce(f)	applie	s the given binary reduction function to stream elements		
sequential()	single	-threaded, opposite of parallel()		
skip(n)	omits	omits the next n elements from the stream		
sorted()	return	s stream's elements in sorted order		
sum()	returns sum of elements in stream			
toArray()	conve	rts stream into array		
Static method		Description		
concat(s1, s2)		glues two streams together		
empty()		returns a zero-element stream		
iterate(seed ,	f)	returns an infinite stream with given start element		
of (values)		converts the given values into a stream		
range (start, er	nd)	returns a range of integer values as a stream 20		

 What is output by the following code? What is output by the following code? (int x1 = IntStream.of(-2, 5, 5, 10, -6) (.map(x -> x / 2) (.int w(x); System.out.print(x1); A. (-2, 5, 5, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 5, 5, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 5, 5, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 6, 7, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 6, 7, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 6, 7, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20 A. (-2, 6, 4, -2, 62, 30) (.filter(n -> n % 10 =-0) (.max()) (.filter(n -> n % 10 =-0) (.max()) (.filter(n -> n % 10 =-0) (.max()) (.filter(n -> n % 10 =-0) (.max()) (.getAsInt(); System.out.println(largest); A method reference lets you pass a method where a lambda would otherwise be expected: A method reference lets you pass a method where a lambda would otherwise be expected: (/ compute sum of absolute values of even ints int[1 numbers = {3, -4, 8, 4, -2, 17, 9, -10, 14, 6, -12); int sum = Arrays.stream(numbers) (.filter(n -> n % 10 == 0) (.distinct()) (.sum()? 	Clicker 2	Optional results
<pre>• To extract the optional result, use a "get as" terminator.</pre>	<pre>int x1 = IntStream.of(-2, 5, 5, 10, -6) .map(x -> x / 2) .filter(y -> y > 0) .sum(); System.out.print(x1);</pre> A. (-2, 5, 5, 10, -6) B. 6 C. (-1, 2.5, 2.5, 5, -3) D. 9 E. 20	<pre>because the stream might be empty or not contain the result: // print largest multiple of 10 in list // (does not compile!) int largest = IntStream.of(55, 20, 19, 31, 40, -2, 62, 30) .filter(n -> n % 10 == 0) .max(); System.out.println(largest);</pre>
<pre>- Converts type OptionalInt to Integer // print largest multiple of 10 in list // (this version compiles and works.) int largest = IntStream.of(55, 20, 19, 31, 40, -2, 62, 30) .filter(n -> n % 10 == 0) .max() .getAsInt(); System.out.println(largest); </pre> • A method reference lets you pass a method where a lambda would otherwise be expected: // compute sum of absolute values of even ints int[] numbers = {3, -4, 8, 4, -2, 17, 9, -10, 14, 6, -12}; int sum = Arrays.stream(numbers) .map(Math::abs) .filter(n -> n % 2 == 0) .distinct()	Optional results fix	Method references
	<pre>- Converts type OptionalInt to Integer // print largest multiple of 10 in list // (this version compiles and works.) int largest = IntStream.of(55, 20, 19, 31, 40, -2, 62, 30) .filter(n -> n % 10 == 0) .max() .getAsInt();</pre>	<pre>• A method reference lets you pass a method where a lambda would otherwise be expected: // compute sum of absolute values of even ints int[] numbers = {3, -4, 8, 4, -2, 17, 9, -10, 14, 6, -12}; int sum = Arrays.stream(numbers) .map(Math::abs) .filter(n -> n % 2 == 0) .distinct()</pre>

Ramya, Spring 2018	Stream exercises
 "Okay, but why?" Programming with Streams is an alternative to writing out the loops ourselves Streams "abstract away" the loop structures we have spent so much time writing 	 Write a method sumAbsVals that uses stream operations to compute the sum of the absolute values of an array of integers. For example, the sum of {-1, 2, -4, 6, -9} is 22. Write a method largestEven that uses stream operations to find and return the largest even number from an array of integers. For example, if the array is {5, -1, 12, 10, 2, 8}, your method should return 12. You may assume that the array contains at least one even integer.
Why didn't we just start with these?	
•Why didn't we just start with these?	26
	(19.4) Higher Order
25	
25 Closures (19.4) • bound/free variable: In a lambda expression, parameters are bound variables while variables in the outer containing	(19.4) Higher Order Operations on Collections

Method references	Streams and lists
ClassName : : methodName	• A collection can be converted into a stream by calling its stream method:
<pre>• A method reference lets you pass a method where a lambda would otherwise be expected: // compute sum of absolute values of even ints int[] numbers = {3, -4, 8, 4, -2, 17, 9, -10, 14, 6, -12}; int sum = Arrays.stream(numbers) .map(Math::abs) .filter(n -> n % 2 == 0) .distinct() .sum(); </pre>	<pre>// compute sum of absolute values of even ints ArrayList<integer> list = new ArrayList<integer>(); list.add(-42); list.add(-17); list.add(68); list.stream() .map(Math::abs) .forEach(System.out::println); 30</integer></integer></pre>
Streams and strings	Streams and files
<pre>// convert into set of lowercase words List<string> words = Arrays.asList("To", "be", "or", "Not", "to", "be"); Set<string> words2 = words.stream() .map(String::toLowerCase) .collect(Collectors.toSet()); System.out.println("word set = " + words2); output: word set = [not, be, or, to]</string></string></pre>	<pre>// find longest line in the file int longest = Files.lines(Paths.get("haiku.txt")) .mapToInt(String::length) .max() .getAsInt(); stream operations: Files.lines -> ["haiku are funny", "but sometimes they don't make sense", "refrigerator"] -> mapToInt -> [15, 35, 12] -> max -> 35</pre>

Stream exercises

- Write a method **fiveLetterWords** that accepts a file name as a parameter and returns a count of the number of unique lines in the file that are exactly five letters long. Assume that each line in the file contains at least one word.
- Write a method using streams that finds and prints the first 5 perfect numbers. (Recall a perfect number is equal to the sum of its unique integer divisors, excluding itself.)