# Topic 15 Implementing and Using Stacks

"stack n.

The set of things a person has to do in the future. "I haven't done it yet because every time I pop my stack something new gets pushed." If you are interrupted several times in the middle of a conversation, "My stack overflowed" means "I forget what we were talking about."

#### -The Hacker's Dictionary

Friedrich L. Bauer German computer scientist who proposed "stack method of expression evaluation" in 1955.



### **Sharper Tools**





Lists

**Stacks** 



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#### **Stacks**

- Access is allowed only at one point of the structure, normally termed the *top* of the stack
  - access to the most recently added item only
- Operations are limited:
  - push (add item to stack)
  - pop (remove top item from stack)
  - top (get top item without removing it)
  - isEmpty
- Described as a "Last In First Out" (LIFO) data structure



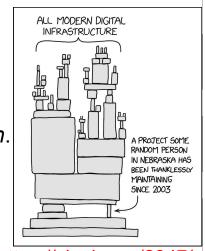
# Implementing a stack

 need an underlying collection to hold the elements of the stack

- 3 obvious choices?
  - native array
  - linked structure of nodes
  - a list!!!

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- Adding a layer of abstraction. A HUGE idea.
- array implementation
- ▶ linked list implementation



https://xkcd.com/2347

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#### Uses of Stacks

- The runtime stack used by a.... process (running program) to keep track of methods in progress
- Search problems
- Undo, redo, back, forward

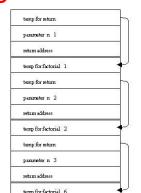


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## Stack Operations

```
Assume a simple stack for integers.
Stack<Integer> s = new Stack<>();
```

```
s.push(12);
```

```
s.push(4);
```

$$s.push(s.top() + 2);$$

//what are contents of stack?

# Clicker 1 - What is Output?

```
Stack<Integer> s = new Stack<>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// Print out contents of stack.
// Assume there is a size method.
for (int i = 0; i < s.size(); i++)
    System.out.print(s.pop() + " ");
A 0 1 2 3 4
                  D 2 3 4
                  E No output due
C 4 3 2
                       to runtime error
```

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#### **Corrected Version**

```
Stack<Integer> s = new Stack<Integer>();
// put stuff in stack
for (int i = 0; i < 5; i++)
    s.push(i);
// print out contents of stack
// while emptying it
final int LIMIT = s.size();
for (int i = 0; i < LIMIT; i++)
    System.out.print(s.pop() + " ");
//or
    while (!s.isEmpty())
//
         System.out.println(s.pop());
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```

# Stack Operations

Write a method to print out contents of stack in reverse order.



Applications of Stacks

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#### **Mathematical Calculations**

- What does 3 + 2 \* 4 equal? 2 \* 4 + 3? 3 \* 2 + 4?
- ▶ The precedence of operators affects the order of operations.
- A mathematical expression cannot simply be evaluated left to right.
- A challenge when evaluating a program.
- Lexical analysis is the process of interpreting a program.

What about 1 - 2 - 4 ^ 5 \* 3 \* 6 / 7 ^ 2 ^ 3

# Infix and Postfix Expressions

- The way we are use to writing expressions is known as infix notation
- Postfix expression does not
- require any precedence rules
- 32 \* 1 + is postfix of 3 \* 2 + 1
- evaluate the following postfix expressions and write out a corresponding infix expression:

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#### Clicker Question 2

What does the following postfix expression evaluate to?

- A. 11
- B. 18
- C. 24
- D. 30
- E. 36

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#### **Evaluation of Postfix Expressions**

- Easy to do with a stack
- given a proper postfix expression:
  - get the next token
  - if it is an operand push it onto the stack
  - else if it is an operator
    - · pop the stack for the right hand operand
    - pop the stack for the left hand operand
    - apply the operator to the two operands
    - push the result onto the stack
  - when the expression has been exhausted the result is the top (and only element) of the stack

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#### Infix to Postfix

Convert the following equations from infix to postfix:

Problems:

Negative numbers?

parentheses in expression

#### Infix to Postfix Conversion

- Requires operator precedence parsing algorithm
  - parse v. To determine the syntactic structure of a sentence or other utterance

Operands: add to expression

Close parenthesis: pop stack symbols until an open parenthesis appears

Operators:

Have an on stack and off stack precedence Pop all stack symbols until a symbol of lower precedence appears. Then push the operator

End of input: Pop all remaining stack symbols and add to the expression

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# Simple Example

Infix Expression: 3 + 2 \* 4

PostFix Expression:

Operator Stack:

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

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# Simple Example

Infix Expression: + 2 \* 4

PostFix Expression: 3

**Operator Stack:** 

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

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# Simple Example

Infix Expression: 2 \* 4

PostFix Expression: 3

Operator Stack: +

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

# Simple Example

Infix Expression: \* 4

PostFix Expression: 3 2

Operator Stack: +

Precedence Table

Symbol	Off Stack Precedence	On Stack Precedence
	ricocacrico	·
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

# Simple Example

Infix Expression: 4

PostFix Expression: 3 2

Operator Stack: + \*

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

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# Simple Example

Infix Expression:

PostFix Expression: 3 2 4

Operator Stack: + \*

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

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# Simple Example

Infix Expression:

PostFix Expression: 3 2 4 \*

Operator Stack: +

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
-	1	1
*	2	2
1	2	2
٨	10	9
(	20	0

# Simple Example

Infix Expression:

PostFix Expression: 3 2 4 \* +

**Operator Stack:** 

Precedence Table

Symbol	Off Stack	On Stack
	Precedence	Precedence
+	1	1
_	1	1
*	2	2
1	2	2
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# Example

Show algorithm in action on above equation

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# **Balanced Symbol Checking**

In processing programs and working with computer languages there are many instances when symbols must be balanced {},[],()

A stack is useful for checking symbol balance. When a closing symbol is found it must match the most recent opening symbol of the same type.

Applicable to checking html and xml tags!

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# Algorithm for Balanced Symbol Checking

- Make an empty stack
- read symbols until end of file
  - if the symbol is an opening symbol push it onto the stack
  - if it is a closing symbol do the following
    - if the stack is empty report an error
    - otherwise pop the stack. If the symbol popped does not match the closing symbol report an error
- At the end of the file if the stack is not empty report an error

# Algorithm in practice

- Ist[i] = 3 \* (44 method(foo(list[2 \* (i + 1) + foo(list[i 1]))/2 \*) list[method(list[0])];
- Complications
  - when is it not an error to have non matching symbols?
- Processing a file
  - Tokenization: the process of scanning an input stream.
     Each independent chunk is a token.
- ▶ Tokens may be made up of 1 or more characters

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