

# Fast String Searching

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# The Problem

One of the classic problems in computing is *string searching*: find the first occurrence of one character string ( “the *pattern*” ) in another ( “the *text*” ).

Generally, the text is *very* large (e.g., gigabytes) but the patterns are relatively small.

# Examples

Find the word “comedy” in this *NY Times* article:

Fred Armisen’s office at “Saturday Night Live” is deceptively small, barely big enough to fit a desk, a couch, and an iPod. The glorified closet, the subject of a running joke on the comedy show, now in its 31st season, can simultaneously house a wisecracking . . .

AAAAAAAAAAAAACAAAGACAGGGGCAACAAAGTGAGACCCTAAAAAAAAAAAAACCCCA  
AAACGGAGAACTTGGAATCCTGTGTCCAAAAAAAAAAGCAGGAAGAGAGCGTGTAGAAAC  
TGAAGCTGAAGTGGAIAAAAAAAAAAGTCGCCAGCACCTACTGTGGAGACCAGAAAGGAAAA  
AAAAAATTGGCAGTCTCGTAGCATACCAAACTAGGCTTGAAAAAAAAAACACACAAAAA  
AACACAGGCTACCCAGTATTTTATCGTCCAAAAAAAAAAGAGGGAAGAAGGACATTTATAT  
TTGCCTTCTGCCAAAAAAAAAAGTACCTCCCGCCTAGAAGAGAGTTTAGAAATCACCAAA  
AAAAAATAGAGAGTCCCAAAATGTTTCGGAATACTCAGAAAAAAAAAATCTTAGTCAGTGCT  
CACTCAGAGGGACCGGGTATTTAAAAAAAAACCTAGACCAGATGCAGCAGGTACAAATTAA  
TCAATCCCAAAAAAAAAAGACCTTCTACCCTTCCAAAAAATGATAGTTGTCTGCAATCCAAA  
AAAAAGACTCTCCGGAAGGTGGACATGCAGAACCTACCAAAAAAAAAAGAGAAGAAAGAAT  
TGCCGGGCAAAAAGTTCCACGTAAAAAAAAAAGGAAATGGGAATGGAGTGTTGTTCTCCT  
TCCTACCTAGTTTTTGAAAAAAAAAGGATGGATGTGGGTACCTGCTCACGTTCTCCAAAAA  
AAAGTGGGTGCTCTCTCACAATATTCTTAGAGGTGGCAAAAAAAAAATAAAGTTGATGGAAA  
CAGTACTGTGTGGGCCAAACAAAAAAAAAAATGGCACCACCTTTTCATTGGCTGAAAAAAAA  
AATTCAACTGAAAAACACAAGTCATACCTTCCTGTTTTATTTGCAAAAAAAAAATTTTTCAA  
ACCCACGGCAACAAACGACAGTATCAAAAAACAACCTTCATTTGACATTCTGCTATATT  
AATGCTCTATGTGGAAAAAAAAAACCATCAAGTTGTGCCTTTTTTTCAAAGAAATCCATGCA  
AAAAAAGACCCATGAAATAATTTTCTGGATCATCCATACAGAACCAAAAAAAAAAGAGGTG



Variants of the problem allow *wildcards* in the pattern and/or the text. *Exact* matching is when no wildcards are allowed.

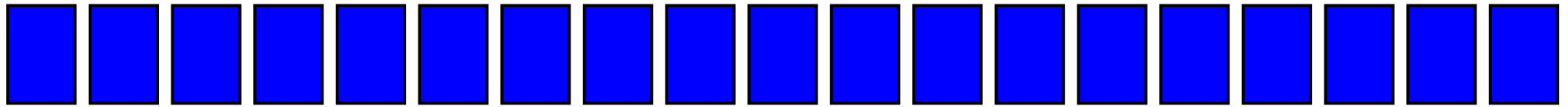
We describe the fastest sequential algorithm for solving the exact string searching problem. The algorithm is called the *Boyer-Moore fast string searching algorithm*.

## Example

Find the word “comedy” in this *NY Times* article:

Fred Armisen’s office at “Saturday Night Live” is deceptively small, barely big enough to fit a desk, a couch, and an iPod. The glorified closet, the subject of a running joke on the comedy show, now in its 31st season, can simultaneously house a wisecracking . . .

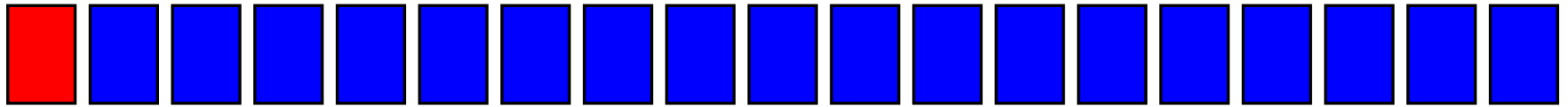
**C O M E D Y**



**J O K E      O N      T H E      C O M E D Y**

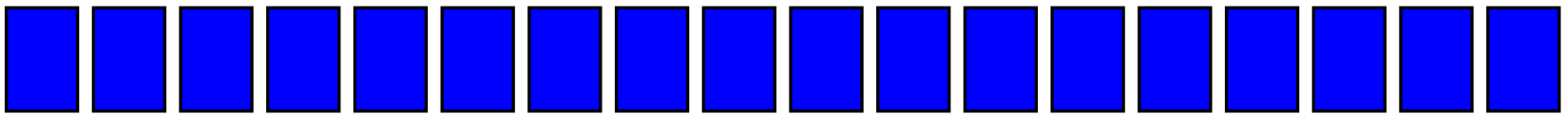


**C O M E D Y**



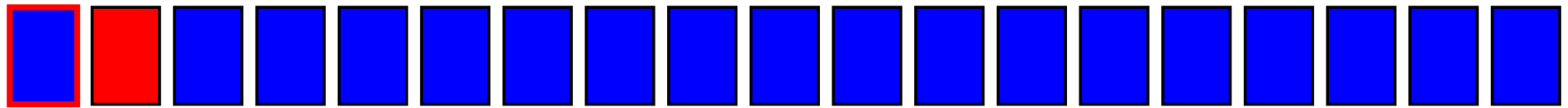
**J O K E      O N      T H E      C O M E D Y**

C O M E D Y

J 

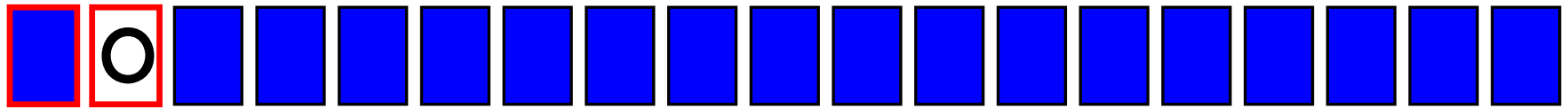
J O K E      O N      T H E      C O M E D Y

COMEDY



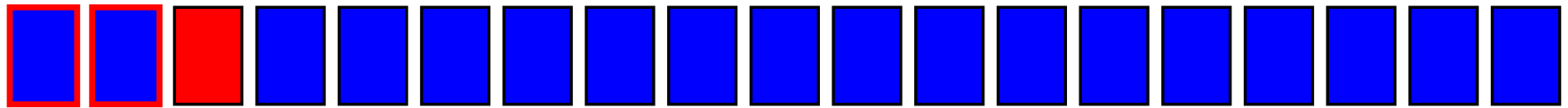
J O K E      O N      T H E      C O M E D Y

COMEDY



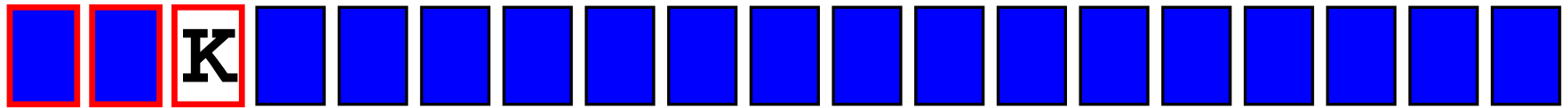
J O K E      O N      T H E      C O M E D Y

COMEDY



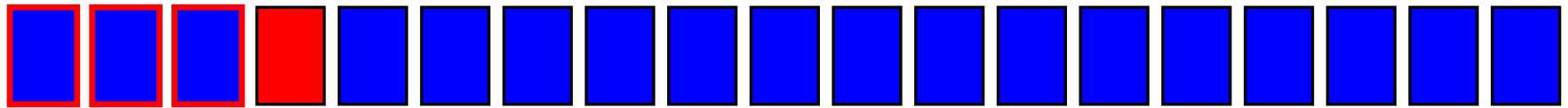
J O K E      O N      T H E      C O M E D Y

C O M E D Y



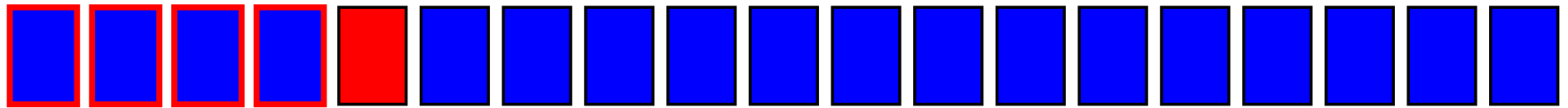
J O K E      O N      T H E      C O M E D Y

COMEDY



J O K E      O N      T H E      C O M E D Y

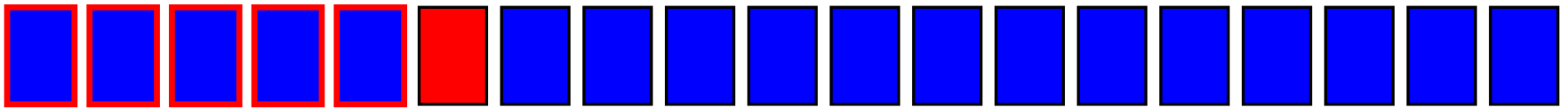
COMEDY



J O K E      O N      T H E      C O M E D Y



COMEDY

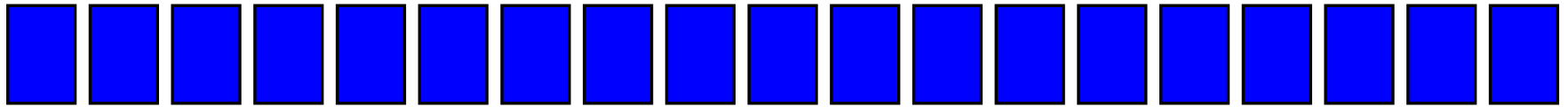


J O K E      O N      T H E      C O M E D Y

COMEDY  
COMEDY

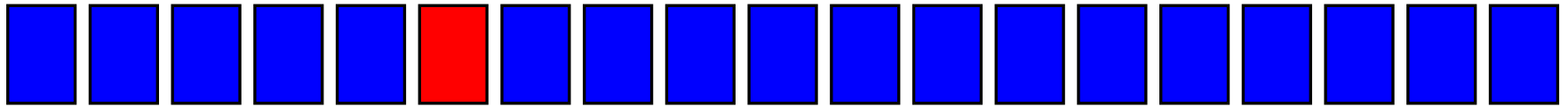
J O K E   O N   T H E   C O M E D Y

**C O M E D Y**



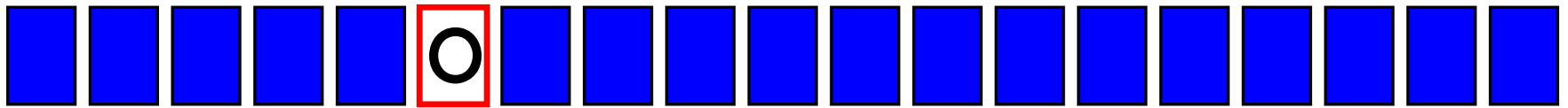
**J O K E      O N      T H E      C O M E D Y**

**C O M E D Y**



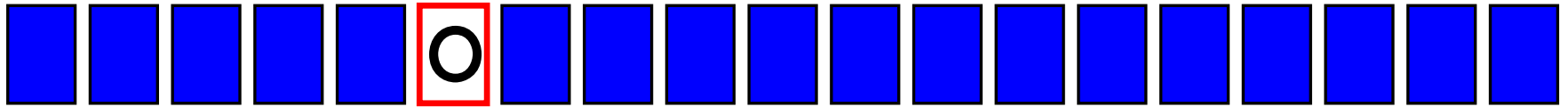
**J O K E      O N      T H E      C O M E D Y**

C O M E D Y



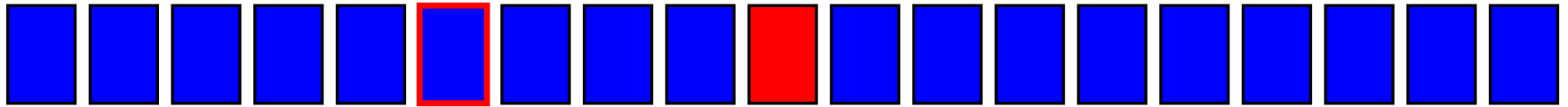
J O K E      O N      T H E      C O M E D Y

C O M E D Y



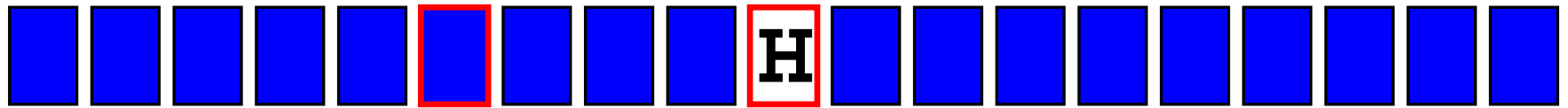
J O K E    O N    T H E    C O M E D Y

COMEDY



J O K E    O N    T H E    C O M E D Y

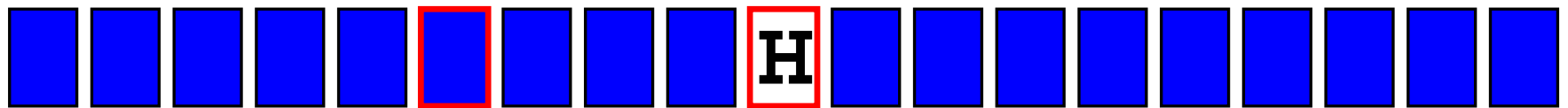
C O M E D Y



J O K E      O N      T H E      C O M E D Y

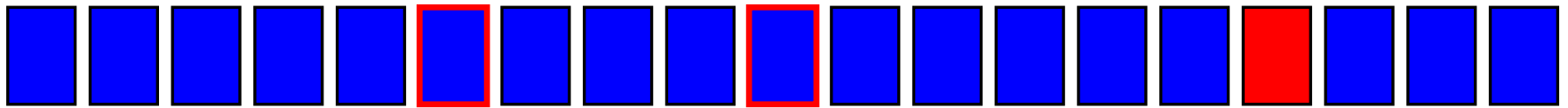


C O M E D Y



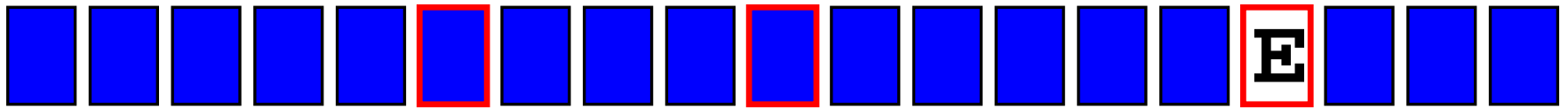
J O K E      O N      T H E      C O M E D Y

C O M E D Y



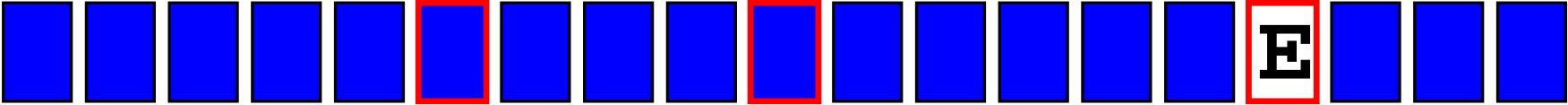
J O K E    O N    T H E    C O M E D Y

C O M E D Y



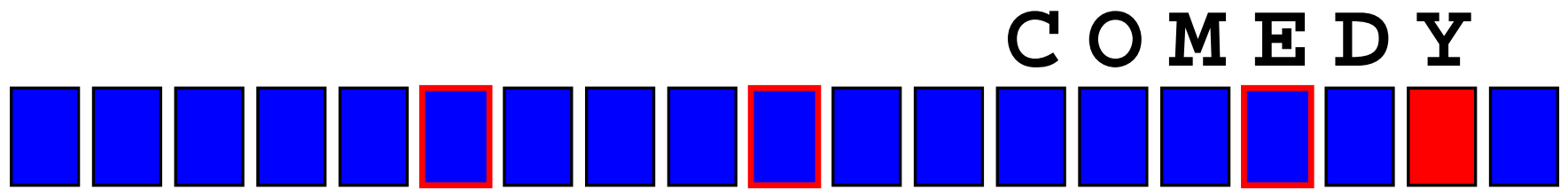
J O K E    O N    T H E    C O M E D Y

COMEDY

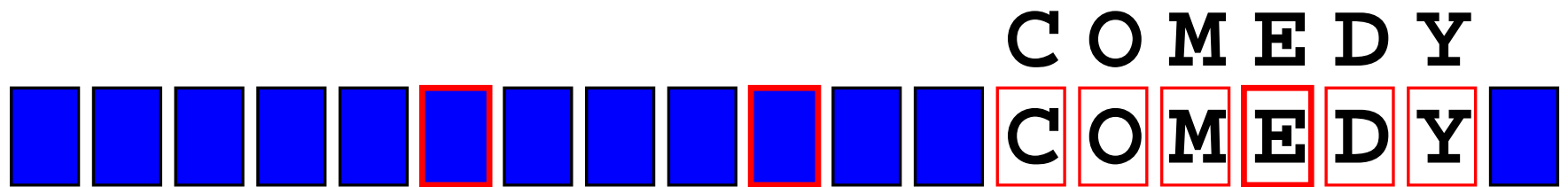


A sequence of 18 blue squares, each with a black border. The 6th and 10th squares from the left are outlined with a red border and are empty. The 14th square from the left contains the letter 'E' in a bold, black, serif font.

J O K E    O N    T H E    C O M E D Y



J O K E    O N    T H E    C O M E D Y



J O K E    O N    T H E    C O M E D Y

Key Property: The longer the pattern, the faster the search!

# Pre-Computing the Skip Distance

*pat*: 543210

COMEDY

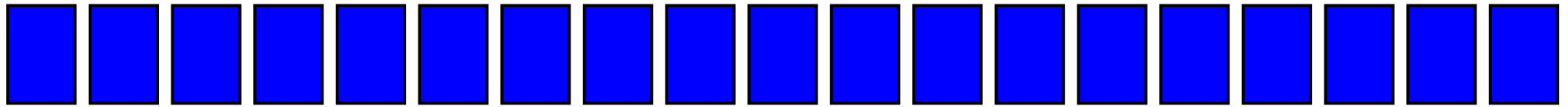
*txt*: xxxxx0xxxxxxxxxxxxx...

↑

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

This is a 1-dimensional array, `skip[c]`, as big as the alphabet.

**C O M E D Y**



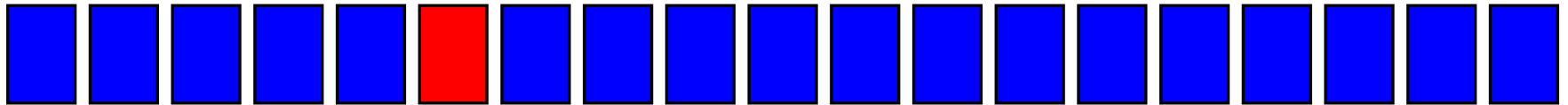
**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6



**C O M E D Y**

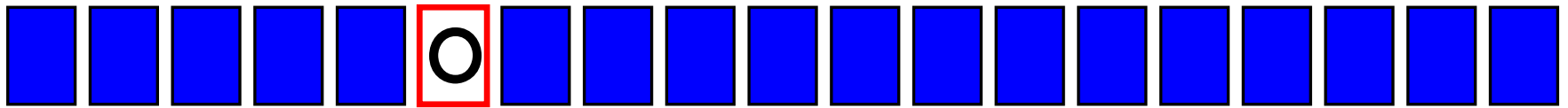


**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

**C O M E D Y**

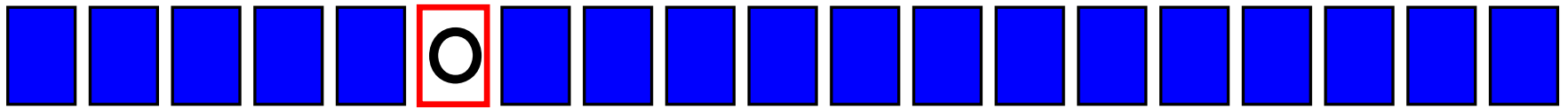


**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

**C O M E D Y**

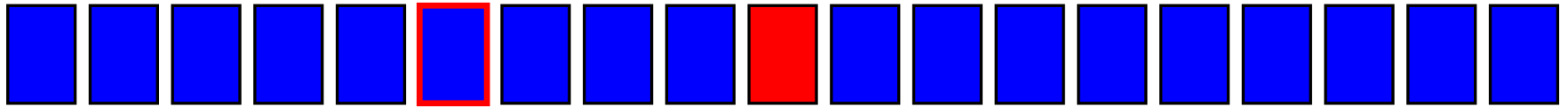


**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

**C O M E D Y**

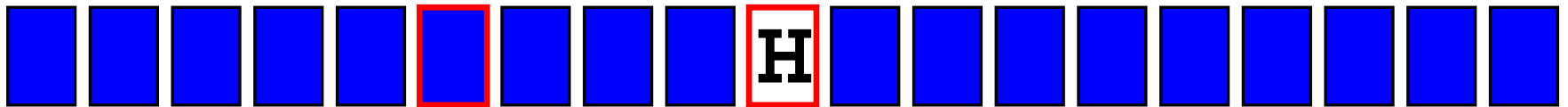


**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

C O M E D Y

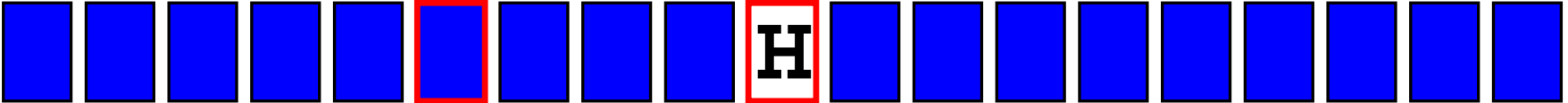


J O K E      O N      T H E      C O M E D Y

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

COMEDY

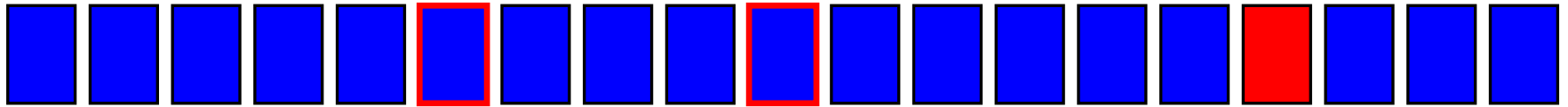


J O K E    O N    T H E    C O M E D Y

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

COMEDY

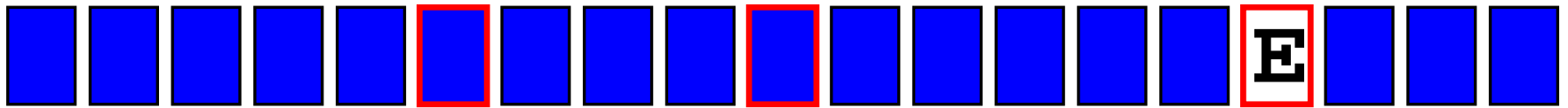


J O K E      O N      T H E      C O M E D Y

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

C O M E D Y

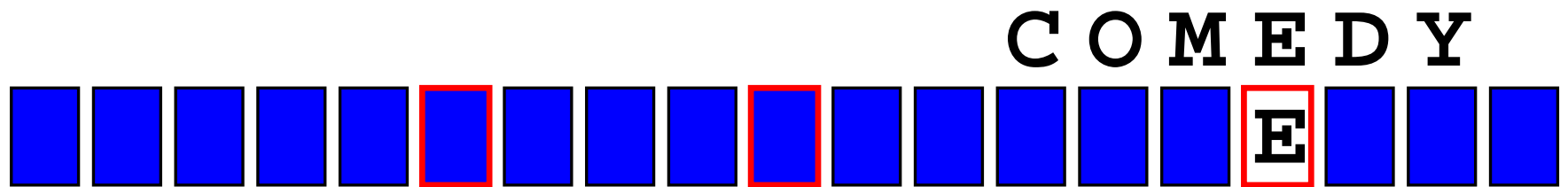


J O K E      O N      T H E      C O M E D Y

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

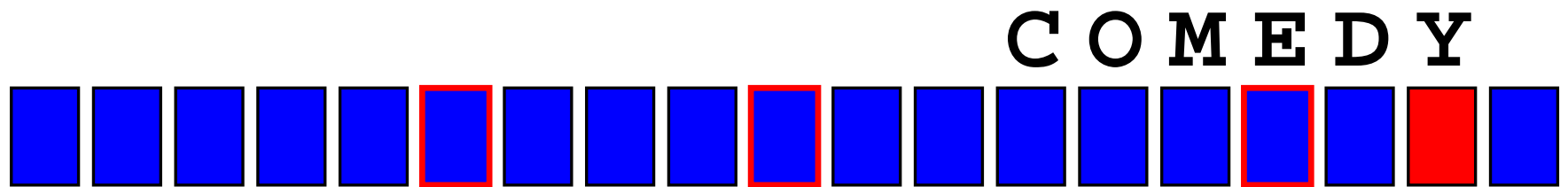




**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6



**J O K E      O N      T H E      C O M E D Y**

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

C O M E D Y  
 [ ] [ ] [ ] [ ] [ ] [ ] [ ] [ ] [ ] [ ] [ ] [ ] C O M E D Y [ ]

J O K E      O N      T H E      C O M E D Y

skip[c]:

A 6	F 6	K 6	P 6	U 6
B 6	G 6	L 6	Q 6	V 6
C 5	H 6	M 3	R 6	W 6
D 1	I 6	N 6	S 6	X 6
E 2	J 6	O 4	T 6	Y 0
				Z 6

# But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----

|

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----R-----  
                  |

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----A-----  
                          |

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----P-----  
                  |

## But Wait! There's More!

*pat*:      NONPARTIPULAR

*txt*: -----P-----  
                  |

Slide 2 to match the discovered character.



## But Wait! There's More!

*pat*:      NONPARTIPULAR

*txt*: -----P??-----  
                          |

## But Wait! There's More!

*pat*:      NONPARTIPULAR

*txt*:    -----PAR-----  
                                 |

# But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----

|

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----R-----  
                  |

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----AR-----

|

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----PAR-----  
                          |

## But Wait! There's More!

*pat*: NONPARTIPULAR

*txt*: -----PAR-----  
                          |

## But Wait! There's More!

*pat*:                   NONPARTIPULAR  
*txt*: -----PAR-----  
                          |

Slide 7 to match the *discovered substring*!



	$j$	$ pat $
$pat:$	NONPARTIPULAR	
$txt:$	-----PAR-----	
	$i$	
$dt:$	$txt[i]$	$pat[j + 1] \dots pat[ pat ]$
	P	A R

$dt: \text{txt}[i] \text{ pat}[j + 1] \dots \text{pat}[|\text{pat}|]$

$dt$  can be computed given  $\text{txt}[i]$  and index  $j$  in  $\text{pat}$ !

There are only  $|\alpha| \times |\text{pat}|$  combinations,  
where  $|\alpha|$  is the alphabet size.

## The Skip Distance – Delta

Given  $pat$ , the skip can be pre-computed for every combination of character read,  $c$ , and pattern index,  $j$ , by finding how far we must slide to find the *last* occurrence of  $dt$  in  $pat$ .

*pat*: NONPARTIPULAR

*txt*: -----PAR-----

|

*pat*:                   NONPARTIPULAR  
*txt*: -----PAR-----  
                          |

*pat*: BC-ABC-BBC-CBC

*txt*: -----BBC-----

|

*pat*:           BC-ABC-BBC-CBC

*txt*: -----BBC-----

|

*pat*: BC-ABC-BBC-CBC

*txt*: -----ABC-----

|



*pat*: BC-ABC-BBC-CBC

*txt*: -----ABC-----

|

*pat*: BC-ABC-BBC-CBC

*txt*: -----DBC-----

|

*pat*: BC-ABC-BBC-CBC

*txt*: -----DBC-----

|

*pat*: EE-ABC-BBC-CBC

*txt*: -----DBC-----

|

*pat*: EE-ABC-BBC-CBC

*txt*: -----DBC-----

|

## The Delta Array

$\text{delta}[c,j]$  is an array of size  $|\alpha| \times |\text{pat}|$  that gives the skip distance when a mismatch occurs after comparing  $c$  from  $\text{txt}$  to  $\text{pat}[j]$ .

# The Algorithm

*fast(pat, txt)*

```
if pat = ""  
  then  
    if txt = ""  
      then return Not-Found;  
      else return 0; end;  
end;
```

*preprocess pat to produce delta;*

*j*  $\coloneqq$   $|pat| - 1$ ;

*i*  $\coloneqq$  *j*;



```

while  $(0 \leq j \wedge i < |txt|)$ 
do
  if  $pat[j] = txt[i]$ 
    then
       $i := i - 1;$ 
       $j := j - 1;$ 
    else
       $i := i + delta[txt[i], j];$ 
       $j := |pat| - 1;$ 
    end;

```

```
If ( $j < 0$ )  
    then return  $i + 1$ ;  
    else return Not-Found; end;  
  
end;
```

# Performance

How does the algorithm perform?

This depends on the size of the alphabet.  
We only have data on English text right now.

In our test:

txt: English text of length 177,985.

pat: 100 randomly chosen patterns of length 5 – 30, chosen from another English text and filtered so they do not occur in the search text.

The naive string searching algorithm would look at all 177,985 characters of the search text. In fact, it would look at some characters more than once.

