Abstract
This report describes a growth path for the area referred to as formal methods within the computing education community. We define the term formal methods and situate it within our field by highlighting its role in Computing Curricula 1991, Computing Curriculum 2001, and the SoftWare Engineering Body Of Knowledge (SWEBOK). The working group proposes an enhancement to an existing web resource, which is a rich collection of materials and links related to formal methods. The new section is designed to provide a bridge between the general computing education community and the "formal methodist" community. The goal is to allow the latter to provide useful support for the former for the ultimate benefit of all of our students. Eventually, the working group aspires to see the concepts of formal methods integrated seamlessly into the computing curriculum so that it is not necessary to separate them in our discussions.

1 Introduction
We support the use of discrete mathematics and formal methods in the teaching and learning of computer science and software engineering. We believe graduates of programs that use and emphasize formal methods will be better prepared for advanced study and research in computing, and/or be able to apply mathematic techniques to the development and verification of software artifacts (such as requirements specifications or design specifications). We see formal methods as the "calculus" of software engineering; without formal methods, the engineering is non-existent or suspect.

Each of the members of this working group is a strong proponent of including topics from the area called formal methods as a vital component of computing education at all levels. During our pre-conference preparations, the working group’s focus evolved to concentrate on providing mechanisms to allow the computing education community at large to more easily incorporate formal methods across the curriculum. This focus reflects the experiences and biases of a wide collection of concerned educators, since we invited a number of individuals with strong backgrounds in this area to serve on an “advisory board”. The advisory board, which is acknowledged in Appendix A, have contributed to the work in a variety of ways, among them position papers (listed in Appendix A), pointers to other documents, on-line (and on-line) discussions, and reviews of the in-progress work.

Even though formal methods are very widely used in the semiconductor industry —indeed, this is the area of computing in which they have had their greatest success to date— the emphasis in this report is on software. In part this reflects the background of the committee, but it is also consistent with the greater emphasis on software in computing education.

The remainder of this report is divided into four major sections. Section 2 defines what we mean by formal methods, addresses some of the challenges and problems related to its adoption, and considers what can be done to address the communication gap between formal methodists and the computing education community at large. Section 3 defines formal methods in the context of current curriculum models and frameworks. Section 4 is an overview of resources that are currently available as sources of support for teaching formal methods. Section 5 describes the key contribution of this working group. We have set the stage for a new web-based resource that targets computing educators who would either like to begin using formal methods or who would like to expand their repertoire of use. We fit our proposal into the framework of a well-
established project with broad community support, which bodes well for its long-term potential to affect the way the computing community views the prospect of teaching “formal methods”.

2  Formal Methods: Its nature and relevance

**Definition**

In our study and interaction about the nature of formal methods, we found various beliefs about the character and content of this area. A widely prevalent view (especially in an industrial context) is Nancy Leveson’s definition [21]:

> A broad view of formal methods includes all applications of (primarily) discrete mathematics to software engineering problems. This application usually involves modeling and analysis where the models and analysis procedures are derived from or defined by an underlying mathematically-precise foundation.

Robert Vienneau [31] offers a focused definition of formal methods:

> A formal method in software development is a method that provides a formal language for describing a software artifact (e.g. specifications, designs, source code) such that formal proofs are possible, in principle, about properties of the artifact so expressed.

In subsequent sections, we assert the need and rationale for including formalism throughout the computer science curriculum. This motivates the more general definition that the working group adopted:

> Formal methods involves the use of discrete mathematics and mathematical logic in the study and practice of computer science and software engineering.

With this definition, we intend to encapsulate within formal methods all its associated concepts and techniques, and both their informal and formal application.

Note: We also view “formal methods” as a single entity within mathematics (with related methods, techniques and applications) rather than as a set of discrete entities. Hence, we use the singular when referring to formal methods.

**Foundations of Computing**

From its beginning in the 1930s, computing was regarded as an abstract, mathematical science. The work of pioneers like Turing, Church and Von Neumann used mathematics to establish the essences and boundaries of the computing discipline. Although computer technology is crucial in computer science education and practice, we should not forget that the underpinnings are mathematical in nature and that computing deals with purely logical processes [22, p. 2]. However, there is often resistance by students (and some faculty) to the use of mathematics in the study of computing. There are a variety of reasons for this resistance. For example, students may lack the proper preparation or motivation; many in the education community have neither an understanding nor appreciation for the role of mathematics (formal methods) in computing [18]; and many individuals feel intimidated by (and even fearful of) the level of mathematical knowledge and capability they believe is required.

Using the working group’s general definition given above, formal methods is found throughout the computing discipline. Although the connection is not always made clear to them, our students begin by studying and using formal languages (the syntax and semantics of programming languages); programs could simply be viewed as a string of symbols from the language (similar to formulae in other mathematical system). In a later section, we explore how formal methods is or may be used throughout a computing curriculum.

**Software Development**

Software is playing an increasingly important and central role in almost all aspects of daily life. The number, size, complexity, and application domains of programs being developed are growing dramatically. Unfortunately, there are serious problems in the cost, timeliness, and quality of development of many software products. Most software projects spend more than half their development time in testing and many delivered products contain an unacceptably high number of defects. For the software discipline, this is not just a commercial issue, but a professional and ethical problem, which would not be tolerated in other fields of science and engineering. Parnas contrasts traditional CS programs with most engineering programs, arguing that SE programs should follow the traditional engineering approach to professional education.

Although the term software engineer is becoming a popular title for software developers, there is little evidence to show that the practice of software engineering compares with the rigor and discipline that is required for practice in other engineering fields. The quality problems arise from incomplete and imprecise requirements specifications, shoddy designs with poor documentation, and the almost sole reliance on testing for software quality assurance. Although there is increasing interest in the use of formal methods for specification and design, the concepts of mathematical modeling and rigorous verification (the staple of other engineering fields) are still used sparingly in commercial software development. This is partly revealed in a survey of software developers by Timothy Lethbridge [20], where the developers ranked the importance of 75 knowledge areas. “Formal Specification Methods” was ranked 37th and “Predicate Logic” was ranked 39th. (Areas like “specific programming languages”, “data structures”, “software architectures” and “requirements elicitation” were ranked at the top, while areas such as “differential equations” and “VLSI” were ranked at the bottom.)
However, there are examples of where formal methods has been used effectively to develop high-quality products. Most of these successes have been in safety critical areas and have involved the integration of formal methods with more traditional non-formal approaches [4, 11, 13, 14, 33]. For many years the use of formal methods has been mandated or encouraged in critical national security systems. Especially with the explosive growth of electronic commerce, there is growing interest in formal methods for achieving higher confidence in other critical infrastructure systems [5, 26].

A more prevalent view of formal methods is that it is intended to support the “specification and verification of hardware and software systems” [34]. Under this view, current curricula have a low level of emphasis on formal methods. This is surely due, at least in part, to a lack of interest on the part of the software industry, but much of the responsibility must be attributed to the state of conceptual curriculum design. The computing education community has adopted a curriculum strategy of dividing curricula elements into areas of “theory” and “practice”. This causes both faculty and students to view the theory of computing as separate and distinct from the practice of computing. Too often, the result is theorists who are viewed as the mathematical elite and practitioners with little respect for the applicability of formal methods to their work. [slg10] This mindset inhibits the use and integration of formal methods into the software development process. Because of this (and other reasons mentioned previously), there is little guidance and support available to faculty that would like to introduce formal methods into their curricula. Also, the currently available software tools are, for the most part, designed for use in research or industrial settings. We explore these issues in more depth in the following sections.

3 FM in Computing-Related Curricula

Computing Curricula ‘91 and 2001

The significance of formal methods topics in model computer science curricula has been quite evident, especially in the most recent versions: Computing Curricula ‘91 [30] and the draft of Computing Curricula 2001 [6]. Because CC2001 is still very much a work in progress, details will change by the time a finished product is published (our analysis is based on a version that resulted from a Steering Committee meeting in June 2000). In this section we examine the role of formal methods, both explicit and implicit, in these curricula. We also mention some implementations of formal methods modules.[vla12]

Computing Curricula ‘91 (CC91) organized the body of computer science into ten “knowledge areas,” each consisting of a set of knowledge units. The Computing Curriculum 2001 (CC2001) committee determined that the evolution of the discipline necessitated important modifications and additions to the earlier organization. The committee therefore added four new knowledge areas and shuffled, modified, added, and deleted topics among the CC91 set of knowledge areas. Most significant for this working group topic, perhaps, is the recommendation that Discrete Structures be added as a separate area in its own right, rather than as a mathematics prerequisite (which was and is the role of continuous mathematics). This reflects the opinion of the CC2001 committee that many topics in the Discrete Structures knowledge area, such as basic logic and proof techniques, are so fundamental in other knowledge areas that they should be taught in a computer science environment with those areas in mind. Thus formal methods topics appear explicitly in the Discrete Structures knowledge area of CC2001.

Within each of CC91 and CC2001, sets of topics are associated with each general knowledge area. Links among the topics and various pedagogical suggestions are also being developed for CC2001, but, at the time of this writing, most of those details have not been finalized. In CC91, topics were cross-referenced with certain “recurring concepts”. Among the possible recurring concepts that could be associated with a topic was one called “conceptual and formal models”. Therefore, this working group began with specific topics in examining the place of formal methods across the curriculum. We started with the units in CC91 that correlated with conceptual and formal models as a recurring concept, and located those topics in CC2001 that are based on (or identical to) those units. This led to using the more recent nomenclature.

Appendices B and C are related to this classification. Appendix B shows a top-level mapping between the curricula, together with the number of suggested core hours in CC2001. Note that the mapping is not precise, as some knowledge areas were added, and many units were reassigned among the areas. According to Clarke [4], the core was determined as “those subjects that we would be embarrassed to have computer science majors graduate without knowing”. Appendix C lists the topics (or units) from both model curricula that correlate with formal methods [DRJ13].

In order to do a small status check on the computing education community’s view of the role of formal methods, the working group conducted a small survey during the poster session during the ITiCSE conference; the results are given in Appendix D. While the number of responses was small, the results did show us that the respondents do perceive a strong relationship between the model curricula and the importance of formal methods, in contrast to the “math-phobic” evidence presented by Clarke [4].

Software Engineering Body of Knowledge

A current project of the Software Engineering Coordinating Committee (SWECC) is the development of a Guide for the software Engineering Body of Knowledge (SWEBOK) [8]. The SWEBOK states as one of its objectives to provide support for “the students learning the software
engineering profession and educators and trainers engaged in defining curricula and course content”. The SWEBOK is being developed in phases and the final version is due in 2002. The guide divides software engineering knowledge into ten areas, providing description and guidance for each area. In order to enhance the SWEBOK as a tool for designing course material, programs, and accreditation criteria, the committee used Bloom’s Taxonomy \[\text{via15}\] to evaluate the required or desired capability for each of the topics included in the knowledge areas. Appendix E lists the ten SWEBOK knowledge areas and shows examples (drawn from the SWEBOK, our working group discussions, and other sources [2, 34]) of parts of formal methods that would apply in each area. The table provides a possible framework for the introduction and use of formal methods in software development courses. At a minimum, it provides faculty and students with an understanding and appreciation for how and where formal methods can be used. Those knowledge areas that benefit most from the use of formal methods are requirements, design, construction, and quality.

The SWEBOK does not emphasize or promote formal methods. It appears to rely more on semi-formal methods, such as using inspections and reviews throughout the development life-cycle. However, the SWEBOK, with its organization and descriptions of knowledge areas and its extensive list of references, provides an excellent resource for curriculum and course designers trying to determine where and how to introduce formal methods.

Note: SWEBOK also includes a number of non-discrete, statistical techniques used in software management for risk management, project estimation and tracking, and process and product assessment.

4 The Current State of Formal Methods Resources

There are a variety “resources” available that support the study and application of formal methods (software tools, books, web pages, handouts, mail lists, tutors/teaching assistants, fellow students, etc.). In the context of this report, however, we restrict ourselves to software tools and web-based resources together with any other resources that may support these (for example, a book on how to use a particular tool). In this section, we consider this issue from three angles:

- Reports and papers submitted to the FM Working Group (WG), including a range of statements from the FM Advisory Board (AB).
- Surveys conducted by the WG.
- The FM Educational site.

Reports and statements submitted to the WG

In the position statements and other materials submitted to the WG, several members of the WG and the AB make reference to Resource Issues. In addition, Randolph Johnson has alerted the working group to two relevant documents, which are included here as items 2) and 3). The following highlights some key points from each of these documents:

1) Jan Smith position statement [28]

This statement outlines an approach to teaching proofs using a tool based on type theory (specifically, Alfa, developed at Chalmers University, and Coq, developed at INRIA).

“Experience of using formal proof systems in undergraduate education is limited, mostly to deductions in logic. We are proposing to present conventional mathematical subjects in a formal, machine checked, but still careful and explanatory manner. Students will be able to browse the formal definitions and proofs at a level of detail they choose, and will work their exercises using the formal proof tool.”

“We are rapidly moving towards an information society which will change both how and what we teach our students. In mathematics there is already a trend towards computations, but we expect a more radical change: a renaissance of proof in education. For the first time, the art of making proofs is on its way to become an engineering discipline because of the fundamental importance of correct hardware and software. For undergraduate students it is difficult to understand the rules by which proofs are made and even more difficult for them to develop their own proofs. The fulfillment of this project will give powerful tools to increase students’ understanding of what a proof is and how to develop proofs.”


This is an extensive survey of tools used in Formal Methods. It includes a framework for classifying formal methods tools and the responses to a survey investigating the use of twelve tools. The survey addressed the nature of each tool, its availability and cost, prerequisite knowledge, and platforms. All of these tools are essentially practitioner tools and include ACL2, HOL, Larch Prover, PVS, Z/EVES, Concurrency Factory, Murphy, SVM Cadence, SPIN, NRL Protocol Analyzer, SCR, and Tatami.

3) M. Barjaktarovic and WetStone Technologies, Report: State of the Art in Formal Methods, 1998, (Communicated by Randolph Johnson) [0]

“Formal methods are in different stages of development, in a wide spectrum from formal languages with no tool support, to internationally standardized languages with tool support and industrial users. The field of formal methods is in a great flux and evolving rapidly, leaving research laboratories and making inroads into industrial practice.”

“The major task of the formal methods community will be to provide the assistance sought. Expressed needs include: more user-friendly tools; more powerful and robust tools;
more real-life applications; more infrastructure such as verified libraries; more publicity of success stories and available technologies; and more user training.”

4) Jeannette Wing. Weaving Formal Methods into the Undergraduate Computer Science Curriculum. [34]
“There is no excuse not to be using model checkers in our undergraduate courses today. With a verification tool, we can more easily teach that verification complements the testing and simulation activities of practicing hardware and software engineers. … it behooves us as educators to ensure that our students are well-versed in the state of the art verification technology.”

“Theorem provers require more expertise than we can expect of our students to acquire in one semester, all the while learning other course material.”

5) Dan Craigen position statement [7]
“Our Z/EVES system has been extensively used for teaching purposes. … Overall, Z/EVES appears to being used in a lightweight perspective for teaching. Few students/lecturers move through the adoption curve to performing complex proofs. Obviously, time and experience is an issue. However, there have been a number of undergraduate and graduate projects that have used the full capabilities of the system (with varying degrees of success). Various researchers and commercial types have pushed Z/EVES to its full extent.”

6) Kathi Fisler position statement [9]
“Formal methods education should address how to identify, develop, and prove formal statements—in particular, theorems—about programs and systems. This encompasses activities ranging from type-checking (where the theorem is stated implicitly and proved automatically) to model-checking (theorem stated explicitly and proved automatically) to theorem-proving (theorem stated explicitly and proved manually).”

“Students at all levels should be encouraged to think about the theorems associated with computer science. In particular, a student should be able to answer the following questions:

1. What kinds of formal statements can be made about a system?
2. When is a formal statement about a system provable?
3. When is a formal statement about a system useful?
4. What resources are needed to prove a given formal statement?
5. What tools and techniques exist for validating formal statements about systems?”

7) Randolph Johnson position statement [17]
“I think that tool support for formal methods is essential. I have used various Z tools, most recently version 1.5 and version 2.0 of Z/EVES. See Dan Craigen’s position paper for more information on Z/EVES. Among its strong points are that it runs on a variety of platforms and is free for academic use. In my experience, the biggest drawback of version 1.5, at least for student use, is that you had to know LaTeX and emacs in addition to learning formal methods and Z. Version 2.0 added a GUI and eliminated the need to know LaTeX and emacs. This is MUCH better for beginners.”

“For educational use, maybe the biggest value of Z/EVES (and many other formal methods tools) is that it does syntax checking and type checking at the push of a button. Some students may never do much more than that. A nice feature of Z/EVES which I haven’t seen in other tools is that it goes beyond type checking to automatically generate domain conditions. These state that the argument to which a partial function is applied in a spec is actually in the domain of the function. Not only does it generate the conditions, it tries and often succeeds in proving them. With no effort on the part of the instructor, the tool repeatedly draws the attention of the student to an aspect of their specification which is often ignored, even by very experienced Z specifiers.”

8) Peter Gorm Larsen position statement [19]
“I believe that formal methods education should be introduced in stages and that in order to keep the interest for the students the use of tools is extremely important. Furthermore I feel that it is important to the students that the use of formal methods in themselves simply is a means to achieve better systems/software and not a goal in itself. It is my experience from some formal methods promoters that this is not sufficiently stressed. Thus it is in my opinion important to be able to envisage how one’s formal method and the associated tools could be applied in a real system/software development environment.”

9) J Strother Moore position statement [23]
“Why teach just one tool? Why ACL2 among all the choices? … ACL2 is the tool I know best. … Enthusiastic teachers who deeply understand the subject matter tend to be good teachers. However, when one teaches a course based upon a particular tool, it is incumbent upon the teacher to explore the tool’s inadequacies, especially those that result from fundamental design decisions.”

“The argument for teaching just one tool is simple: a semester is not very long. If I were teaching a course on programming, I would rather the students learn one “first language” than several.”

“ACL2 is a good choice for the following reasons. … There is now a textbook introduction… The tool is free and runs on many platforms. The tool is rugged, well-documented online, and widely used. Within the ACL2 setting there is a natural way to study some other tools… Finally, and very importantly, ACL2 is not a pedagogical toy but an advanced industrial-strength theorem prover …”

10) Lesley Semmens position statement [27]
"I see the main problem in the early teaching of formal methods to be the students’ limited ability to model. The notifications are not the main problem. I therefore try to build on other experience and understanding they already have. [slg20] I have tried many different approaches over the ten years I have been teaching formal methods. I have done it with and without tools (fUZZ, Formaliser, ZTC). We have even built tools to translate from ERDs to Z. But, always it comes back to the students’ ability (or lack of ability) in modeling. Using tools student beginners produce syntactically correct Z, but often it is semantic nonsense; they concentrate far too much on the syntax and coping with the idiosyncrasies of the tool."

“I am not totally against tools. With the final year, who have more understanding of what they are doing (and more ability in modeling), I use tools, such as fUZZ and ZTC if time permits. In any case I encourage them to try out the tools, in the same way as they might any other software engineering tool. This seems to work, they are not trying to learn two things at once and appreciate the help the tool gives them.”


This position statement specifically addresses the issue of web-based teaching of the formal notation Z. The author describes his experiences of delivering an FM course in this manner, including the use of books, and software tools (LaTeX, ZTC and ZANS).

“No one book was followed exactly. It was recommended that a Z textbook be obtained by students and used to complement the course unit with additional reading outside lectures.”

“Student understanding of producing a Z specification increased significantly after the practical sessions. Many seemed to appreciate using tools far more than just pencil and paper. However, a danger with the use of an animator is the possibility of confusion between a (possibly non-executable) formal specification and an executable program. A few always seem to stubbornly fail to recognize the difference even after this is emphasized repeatedly in lectures.”

“Note that students were given much of this material in printed form. Otherwise having on-line material encourages students to simply print it out anyway. This is more expensive than mass photocopying and clogs the department’s printers when they could be used for more productive purposes, such as printing out individual student’s personal work. However, having the material online is useful in those cases where the students lose their printed notes since it is readily accessible if needed quickly (i.e., near deadlines!). It also makes the material easily accessible and updatable by the lecturer. This is especially helpful in revising the material each year for a course unit delivered and developed over a number of years.”

“In the experience of the author, using tools in supporting formal methods course units helps the students in their understanding and increases their appreciation of the usefulness (or at least decreases their negativity) of formal methods.

By insisting that students type-check their Z specifications (using the ZTC tool on the course unit described here) and check for explicitness (or otherwise) at least using the related ZANS animation tool, many errors in Z specifications can be discovered and eliminated by the students themselves, sometimes with no help from demonstrators in the case of bright students. This allows demonstrators (and markers) to concentrate on the more interesting and difficult aspects of formulating a Z specification that require human inspection.[slg21]

Web support for formal methods and other course units is a useful adjunct. A benefit is the accessibility of material by students, the staff involved, other colleagues, internal and external examiners, etc. It also helps in the maintenance of course unit material as a unit develops since this can be easily added and information can quickly be corrected in the case of errors. However, it is recommended that all essential material is still given to students in paper form, even if it is available on the web, since students will tend to print this anyway, which is still relatively expensive compared to photocopying. Of course the web resource can contain considerable extra supplementary material if desired at very little cost once it is installed.”

Conclusions regarding position statements

From these, we can see several themes emerging:

1) The need for more robust and user-friendly tools.
2) There is a wide spectrum of tools available[slg22].
3) The value of including industrial strength tools in the curriculum, particularly with regard to model checking[slg23].
4) Students need more educationally oriented tools to help learn the concepts of theorem proving rather than being overwhelmed by the power of industrial strength tools.
5) Ancillary issues (such as the operating system a tool runs under, and the need to learn other software tools, such as LaTeX and emacs) can have major adverse effects on the students’ learning experience[slg24].
6) Tools can be extremely important in keeping the interest of students and enhancing the learning experience.
7) Tools are not necessarily a good idea at the introductory stages, indeed they may hinder the learning, or even mislead the student into a mindset where formal methods are seen as yet another programming approach!
8) Web support is useful, if only as a means of providing access to the (latest) handout materials.
Surveys related to FM Resources

Several questionnaires were circulated both before and during the ITiCSE conference. Of these only one produced a reasonable number of responses (30, all collected from the Formal Methods focus group of the (UK based) Learning and Teaching Group for Computer Science and Information Technology). Appendix F lists the questions and gives information about the responses.

These surveys show that a wide variety of tools are used, mostly industrial strength. Very few are designed specifically to help develop FM skills in students. Z is very popular in the UK but other FM approaches are also used. In follow up communications to the respondents, it seems that many tools (especially the Z tools) create problems for their use: some only work on a Unix platform; several require the use of LaTeX or troff; others have editors that students find difficult to use. For example, Formaliser uses a structure editor; students find this difficult, although it could be argued that thinking more structurally is a skill to be developed (in which case Formaliser can be seen as a tool having an educational function). There also seems to be a dearth of good backup material (tutorials, handouts, books), although at least one respondent produces some good material on LaTeX and CadiZ. One exception to this seems to be Toolbox Lite (for VDM); this is an educational version of the Toolbox tool, and comes packaged with a textbook on VDM—Fitzgerald & Larson, “Modelling Systems”.

The survey reveals there is very little use of web-based resources. There are however a wide variety of textbooks available and in use. About a quarter of respondents indicated that their courses tend to “traditional” —book-based and hand-worked exercises.

There also seems to some variability in opinion of what constitutes a FM and an FM tool. Are declarative languages like Prolog and ML to be considered as FMs or FM tools?

Generally, the state of the art in resources for teaching FM seems to be a maze which the novice has to navigate: “which FM shall I teach?”; “which tool shall I use?”; “what materials are available?”. The temptation may be to start with the available resources and to choose (perhaps somewhat randomly) those that seem most convenient or which are used on apparently similar courses. But the WG and AB see this as a recurring theme in our investigations. Certainly, there is a need for more thought and study about providing tools to aid learning; and that the tools should be supported by suitable tutorial and other materials such as books.

There is also the issue of what attributes a good tool should have if it is to be used for educational purposes. Moore (see above) makes a good start at this. But the WG and AB see this as another important area of investigation.

For the teacher, the problem is to define clearly what the aims and objectives are at each stage in the students’ learning and to relate these to the resources available. Currently there seems to be little help to guide the educator through the maze. The WG proposes that a web resource be developed to this end.

Our investigations also indicate that there is very little use of web-based resources. Even when the web is used, it is often used simply as a means of providing copies of the latest versions of a handout. The web is largely viewed as a repository of useful information.

FM Educational Site

In March of 1998, the 21st Century Engineering Consortium Workshop was held in Melbourne, Florida. The workshop’s principal concern was to promote formal methods education in computer science and computer engineering programs. Toward this end, the workshop gathered leading practitioners, experienced academics, and government advocates interested in the educational issues relevant to formal methods development. One outcome of that Workshop was the Formal Methods Education Resources site, which was created and has been maintained by Kathi Fisler of Rice University. The general philosophy of the site is to provide a collecting point for materials related to teaching formal methods. The site has evolved to include several sections, including course pages, tools, reading materials, instructional materials, benchmarks and examples related to formal methods, and position announcements.

5 A Resource to Support FM Teaching

While the Formal Methods Education site presented in Section 4 is a rich and varied resource, at this time it is primarily useful for educators who are already teaching formal methods and want to find materials for their existing courses. The wealth of information available at the site is somewhat overwhelming; it would be a daunting task for someone who wishes to begin teaching formal methods to
navigate all of the information in order to come up with the “right” materials for a particular situation.

This working group proposes a new area for inclusion in the Formal Methods Educational site, with a vision toward creating a set of pages to assist computing educators who are either new to teaching formal methods or who would like to move along to the “next level” of teaching formal methods.

The remainder of this section describes our proposal for the organization of this sub-site and some of its features. The actual implementation will be an on-going process, which will require cooperation by a number of individuals and institutions. We address our plan of action where such a plan exists.

We propose the following sections for the new sub-site:

- **Introduction:** What is Formal Methods? *(can be drawn from Section 2 of this report)*
- **Problems and Challenges:** *(can be drawn from section 2 of this report)*
- **FAQs** *(we have suggestions of several questions and answer, which will be used to seed this page)*
- **FM Motivation** *(advantages; statistics and reactions such as those in this survey by alumni of an introductory mathematics course at SUNY Stony Brook [29]; information to help in “selling” the idea of teaching formal methods within a department; pointers to success stories in which formal methods has been used in real, large scale projects; pointers to standards in which the use of formal methods is mandated or encouraged, especially in the safety-critical and security areas)*
- **FM across the curriculum**
  - Current computing curricula guidance *(links)*
  - Courses matrix and FM components *(drawn from appendices B and C)*
  - Guidelines for designing an FM course
  - Modules that can be incorporated into other courses *(reflecting the results from projects proposed by Rice University and a proposal mentioned by Tom Hilburn)*
  - Evaluation of Formal Methods in computing-related curricula *(such an evaluation could be done after a course, after graduation, or after students have started to work; a positive evaluation may be the best motivation; evaluation is also a necessary basis for improvement of a curriculum; for an example survey, see [29])
  - Resource Navigation Assistant: As a key addition to the FM Educational web site, we propose the addition of a resource navigation assistant (RNA). We feel such a capability would be invaluable in surveying the maze of resources. The RNA would be more than a search engine. It would build a searchable network of interrelated resources that would allow cross-referencing among courses and curriculum modules, tutorials, software tools, textbooks, and relevant case studies, examples, and benchmarks. Since the FM Educational web site will continue to change as people submit additional relevant material, the RNA itself will need ongoing maintenance.
- **Educational tools wish list** *(Currently, tools that can be used to support the teaching of formal methods are primarily for practitioners, not for educators or first-time users. The wish list can provide a basis for enhancing existing tools for educational settings or for creating customized tools that address academic concerns. The key question is: What do tools for teaching and learning FM need in order to be useful? Some features we have identified are that they should enhance the learning, should provide a good learning curve trade-off (that is, the time invested in learning the tool should not outweigh the ultimate benefit of using the tool), the user interface should be intuitive and accessible, and the tool should help highlight the underlying principles)*

The initial plan for implementing the proposed web pages is to extend the existing FM Educational site [10]. The webmaster of that site is committed to refining and improving the site and is a very member of the advisory board. We visualize this as an evolutionary process, which will respond to suggestions and newly emerging needs. The logistics for bringing the site into use include encouraging contributions and publicizing the site. [slg32]As one aspect of publicizing the FM Ed resource, the working group proposes a simple flyer that can be readily available on the web site. This will allow FM proponents to print out the flyer and have it available on the hand-out table during appropriate conferences. We will also devise a plan for distributing information about the resource via relevant mailing lists.

**6 Conclusions**

The working group has presented a proposal for extending the work started elsewhere in order to create a resource that provides a solid basis of support for computing educators who wish to begin teaching formal methods, as well as for educators already teaching formal methods who wish to move to the next level. [slg33]The working group’s web site, http://www.cs.utexas.edu/users/csed/formal-methods/, will be a source of information about these efforts. The goal, however, is to incorporate these results into the Formal Methods Education site [10] by the time this report is published.

**References**


http://www.cs.utexas.edu/users/csed/FM/docs/StateFM.pdf


Appendix A: Advisory Board Members and Materials Contributed

- **Jonathan Bowen**, South Bank University, London, UK
  - Position Statement [3]
- **Dan Craigen**, ORA Canada, Ottawa, Ontario, Canada
  - Position Statement [7]
- **Kathi Fisler**, Rice University, Houston, TX USA
  - Position Statement [7]
  - Joint position statement: Integrating Logic into the Computer Science Curriculum. [Barland 00]
- **Susan Gerhart**, Embry-Riddle Aeronautical University, Prescott AZ USA
- **David Gries**, University of Georgia, Athens GA USA
  - Position Statement [12]
- **Ebba Thora Hvannberg**, University of Iceland, Reykjavik, Iceland
  - Position Statement [15]
- **Randolph Johnson**, National Security Agency, Fort Meade MD USA
  - *Formal Methods Framework, final month status report* [32]
  - Position Statement [17]
- **Peter Gorm Larsen**, IFAD A/S, Odense M, Denmark
  - Position Statement [19]
- **J Strother Moore**, University of Texas at Austin, Austin, TX USA
  - Position Statement [23]
- **Lesley Semmens**, Leeds Metropolitan University, Leeds, UK
  - Position Statement [27]
- **Moshe Vardi**, Rice University
  - Joint position statement: Integrating Logic into the Computer Science Curriculum. [1]
- **Jeannette M. Wing**, Carnegie Mellon University, Pittsburgh, PA USA
  - Weaving Formal Methods into the Undergraduate Computer Science Curriculum [34]
- **J. C. P. Woodcock**, Oxford University Software Engineering Centre, Oxford, UK
## Appendix B: Top-level Mapping between Knowledge Areas CC2001 and CC91

<table>
<thead>
<tr>
<th>Computing Curricula 2001 Knowledge Area and Number of Core Hours</th>
<th>Computing Curricula 91 Knowledge Area</th>
</tr>
</thead>
<tbody>
<tr>
<td>DS: Discrete Structures (40)</td>
<td>None (refer to discussion in Section 3)</td>
</tr>
<tr>
<td>PF: Programming Fundamentals (59)</td>
<td>AL: Algorithms and Data Structures</td>
</tr>
<tr>
<td>AL: Algorithms and Complexity (31)</td>
<td>AL: Algorithms and Data Structures</td>
</tr>
<tr>
<td>PL: Programming Languages (6)</td>
<td>PL: Programming Languages</td>
</tr>
<tr>
<td>AR: Architecture (36)</td>
<td>AR: Architecture</td>
</tr>
<tr>
<td>OS: Operating Systems (14)</td>
<td>OS: Operating Systems</td>
</tr>
<tr>
<td>HC: Human-Computer Interaction (6)</td>
<td>HU: Human-Computer Communication</td>
</tr>
<tr>
<td>GR: Graphics and Visualization (5)</td>
<td>HU: Human-Computer Communication</td>
</tr>
<tr>
<td>IS: Intelligent Systems (10)</td>
<td>AI: Artificial Intelligence and Robotics</td>
</tr>
<tr>
<td>IM: Information Management (10)</td>
<td>DB: Database and Information Retrieval</td>
</tr>
<tr>
<td>NC: Net-Centric Computing (15)</td>
<td>OS: Operating Systems</td>
</tr>
<tr>
<td>SE: Software Engineering (35)</td>
<td>SE: Software Methodology and Engineering</td>
</tr>
<tr>
<td>CN: Computational Science (0)</td>
<td>NU: Numeric and Symbolic Computing</td>
</tr>
<tr>
<td>SP: Social and Professional Issues (16)</td>
<td>SP: Social, Ethical and Professional Issues</td>
</tr>
</tbody>
</table>
## Appendix C: Specific Topics Correlated with Formal Methods in CC91 and CC2001

<table>
<thead>
<tr>
<th>CC 2001 Topic</th>
<th>CC 91 Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>DS1: Functions, relations, and sets</td>
<td>None (refer to discussion in Section 3)</td>
</tr>
<tr>
<td>DS2: Basic logic</td>
<td>None</td>
</tr>
<tr>
<td>DS3: Proof techniques</td>
<td>None</td>
</tr>
<tr>
<td>DS4: Basics of counting</td>
<td>None</td>
</tr>
<tr>
<td>DS5: Graphs and trees</td>
<td>None</td>
</tr>
<tr>
<td>PF1: Fundamental programming constructs</td>
<td>None</td>
</tr>
<tr>
<td>PF2: Algorithms &amp; problem solving</td>
<td>AL8: Problem-solving strategies</td>
</tr>
<tr>
<td>PF3: Object-oriented programming</td>
<td>PL11: Programming paradigms</td>
</tr>
<tr>
<td>PF4: Fundamental data structures</td>
<td>AL1: Basic data structures</td>
</tr>
<tr>
<td>PF5: Recursion</td>
<td>AL3: Recursive algorithms</td>
</tr>
<tr>
<td>AL5: Basic computability theory</td>
<td>AL7: Computability and undecidability</td>
</tr>
<tr>
<td>AL6: The complexity classes P and NP</td>
<td>AL5: Complexity classes</td>
</tr>
<tr>
<td>AL7: Automata theory</td>
<td>PL7: Finite-state automata and regular expressions</td>
</tr>
<tr>
<td>PL1: History of programming languages</td>
<td>PL1: History and overview of programming languages</td>
</tr>
<tr>
<td>PL3: Virtual machines</td>
<td>PL2: Virtual machines</td>
</tr>
<tr>
<td>PL4: Introduction to language translation</td>
<td>PL9: Language translation systems</td>
</tr>
<tr>
<td>PL5: Language translation systems</td>
<td>PL9: Language translation systems</td>
</tr>
<tr>
<td>PL6: Type systems</td>
<td>PL3: Representation of data types</td>
</tr>
<tr>
<td>PL7: Models of execution control</td>
<td>PL4: Sequence control</td>
</tr>
<tr>
<td>PL8: Declaration, modularity, and storage management</td>
<td>PL6: Run-time storage system</td>
</tr>
<tr>
<td>PL9: Programming language semantics</td>
<td>PL10: Programming language semantics</td>
</tr>
<tr>
<td>PL10: Programming paradigms</td>
<td>PL11: Programming paradigms</td>
</tr>
<tr>
<td>AR1: Digital logic and digital systems</td>
<td>AR1: Digital logic</td>
</tr>
<tr>
<td>AR6: CPU implementation</td>
<td>AR1: Digital logic</td>
</tr>
<tr>
<td>OS2: Concurrency</td>
<td>OS3: Process coordination and synchronization</td>
</tr>
<tr>
<td>OS3: Scheduling and dispatch</td>
<td>OS4: Scheduling and dispatch</td>
</tr>
<tr>
<td>OS6: Security and protection</td>
<td>OS8: Security and protection</td>
</tr>
<tr>
<td>OS8: Real-time systems</td>
<td>OS10: Distributed and real-time systems</td>
</tr>
<tr>
<td>HC2: Modeling the user</td>
<td>HU1: User interfaces</td>
</tr>
<tr>
<td>GR3: Modeling</td>
<td>HU2: Computer graphics</td>
</tr>
<tr>
<td>IS2: Search and optimisation methods</td>
<td>AI2: Problems, state spaces, and search strategies</td>
</tr>
<tr>
<td>IS3: Knowledge representation and reasoning</td>
<td>AI2: Problems, state spaces, and search strategies</td>
</tr>
</tbody>
</table>

Appendix continues on the next page
## Appendix C, continued: Specific Topics Correlated with Formal Methods in CC91 and CC2001

<table>
<thead>
<tr>
<th>CC 2001 Topic</th>
<th>CC 91 Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>IS6: Machine learning</td>
<td>AI2: Problems, state spaces, and search strategies</td>
</tr>
<tr>
<td>IS7: Natural language processing</td>
<td>AI1: History and applications of artificial intelligence</td>
</tr>
<tr>
<td>IS10: Knowledge-Based systems</td>
<td>AI1: History and applications of artificial intelligence</td>
</tr>
<tr>
<td>IM2: Data modeling and the relational model</td>
<td>DB2: The relational data model</td>
</tr>
<tr>
<td>IM3: Database query languages</td>
<td>DB2: The relational data model</td>
</tr>
<tr>
<td>IM4: Relational database design</td>
<td>DB2: The relational data model</td>
</tr>
<tr>
<td>IM5: Transaction processing</td>
<td>DB1: Overview, models, and applications of database systems</td>
</tr>
<tr>
<td>IM6: Distributed databases</td>
<td>DB1: Overview, models, and applications of database systems</td>
</tr>
<tr>
<td>IM7: Advanced relational database design</td>
<td>DB2: The relational data model</td>
</tr>
<tr>
<td>NC2: Communication and networking</td>
<td>OS9: Communications and networking</td>
</tr>
<tr>
<td>NC7: Distributed systems</td>
<td>OS10: Distributed and real-time systems</td>
</tr>
<tr>
<td>SE2: Software requirements and specifications</td>
<td>SE3: Software requirements and specifications</td>
</tr>
<tr>
<td>SE3: Software design and implementation</td>
<td>SE4: Software design and implementation</td>
</tr>
<tr>
<td>SE4: Verification and validation</td>
<td>SE5: Verification and validation</td>
</tr>
<tr>
<td>SE5: Software tools and environments</td>
<td>SE2: The software development process</td>
</tr>
<tr>
<td>CN1: Numerical analysis</td>
<td>NU2: Iterative approximation methods</td>
</tr>
</tbody>
</table>
Appendix D: Responses to Conference Survey on Importance of Formal Methods

The working group polled its colleagues at the ITiCSE 2000 conference as to how they would assess the importance of formal methods in the different knowledge areas. Participants could view a poster with the current state of the areas and their topics in CC 2001 (similar to Appendix B), with those topics that correlated to formal methods highlighted. The participants were also able to read the working definition of formal methods discussed in Section 2, as well as a wide variety of definitions drawn from the literature. In order to complete the survey, participants were asked to assign a numerical ranking to each knowledge area using the following scale:

1 – It would be a stretch to use formal methods in teaching this area.
2 – This area could be taught using formal methods.
3 – This area should be taught using formal methods.
4 – This area can’t be taught without using formal methods.

Thus, a rating of 2.5 for a knowledge area could be construed as a neutral stance about the applicability of FMs. The number of respondents was approximately ten.

The results of the survey showed that the respondents feel there is a high degree of correlation between the model curricula and the importance of formal methods. In particular, the attendees polled corroborated the importance of formal methods in the Software Engineering area with a median of 3.8/4.0. In fact, the median rating for Computational Science was 3.9. This supported the correlation posited in CC91, in spite of the fact that many formal methodists do not usually have continuous mathematics in mind when they refer to formal methods. Finally, while the number of respondents is not significant, it is interesting to note the relatively low rating assigned to the Information Management knowledge area. This would seem to indicate that many faculty either are unaware of, or do not assign strong weight to, the central role played by mathematical logic in the relational calculus formal query language.

<table>
<thead>
<tr>
<th>CC 2001 Knowledge Area</th>
<th>Median Rating in Formal Methods Survey (4-point scale as given above)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Discrete Structures</td>
<td>3.8</td>
</tr>
<tr>
<td>Programming Fundamentals</td>
<td>2.9</td>
</tr>
<tr>
<td>Algorithms and Complexity</td>
<td>3.7</td>
</tr>
<tr>
<td>Programming Languages</td>
<td>2.9</td>
</tr>
<tr>
<td>Architecture</td>
<td>2.5</td>
</tr>
<tr>
<td>Operating Systems</td>
<td>2.9</td>
</tr>
<tr>
<td>Human-Computer Interaction</td>
<td>1.4</td>
</tr>
<tr>
<td>Graphics and Visualization</td>
<td>3.2</td>
</tr>
<tr>
<td>Intelligent Systems</td>
<td>3.2</td>
</tr>
<tr>
<td>Information Management</td>
<td>2.0</td>
</tr>
<tr>
<td>Net-Centric Computing</td>
<td>2.7</td>
</tr>
<tr>
<td>Software Engineering</td>
<td>3.8</td>
</tr>
<tr>
<td>Computational Science</td>
<td>3.9</td>
</tr>
</tbody>
</table>
### Appendix E: SWEBOK and Formal Methods

<table>
<thead>
<tr>
<th>SWEBOK Knowledge Area</th>
<th>Applicable Formal Methods</th>
</tr>
</thead>
</table>
| Software requirements            | • formal domain modeling  
• formal requirements specification  
• analysis diagrams - data/control flow, entity-relationship, object diagrams |
| Software design                  | • formal design specification  
• design diagrams - structure charts,  
• object diagrams, state diagrams  
• program design languages         |
| Software construction            | • algorithm/complexity analysis  
• data structures  
• detailed design formalisms (e.g., pre/post conditions, invariants, design tables and diagrams)  
• program syntax and semantics     |
| Software testing                 | • program flow diagrams, case construction, specification decomposition into cases, reliability and coverage arguments |
| Software maintenance             | (any FM used in initial development)                                                      |
| Software configuration management | • configuration process diagrams                                                          |
| Software engineering management  | • task schedule diagrams (PERT, Gantt)                                                    |
| Software engineering tools and methods | • FM tools - analysis and design tools, compilers, type/domain checkers,  
animators, model checkers, theorem provers, test case generators |
| Software engineering process     | • formal process modeling                                                                |
| Software quality                 | • formal analysis and verification - symbolic execution, state machines,  
model checking, theorem proving, "proof by team checking" [slg37] |
## Appendix F: Responses to FM Tool Survey

### 1. What software have you used in teaching formal methods?

Respondents gave the following answers:

- Z (including Z Specific Formaliser (3), CadiZ (3), Fuzz (2), Z/EVES, ZTC, and Z Browser)
- B (B Tool(2))
- SDL (Telelogic TAU)
- Lotos (SEDOS, TOPO, LOLA)
- PVS
- VDM (ToolBox Lite)
- CSP (Kramer & McGee (KM) model checker; FDR model checker)
- Design CPN (Concurrency Workbench)
- ML
- No software used (5)

Note: The numbers in parentheses indicate the number of responses for each tool; all others represent a single response.

### 2. How have you used the software in your teaching?

Respondents indicated they have:

- a) taught its use as a tool for doing formal methods in the case of:
  - Z Specific Formaliser (3), CadiZ(2), Fuzz(2), Z/EVES, TOPO, LOLA, PVS, Tool, KM model checker, Concurrency Workbench, ZTC
- b) used it as a tool for teaching/learning the concepts of FM in the case of:
  - Z Specific Formaliser (2), CadiZ, Telelogic TAU, SEDOS, TOPO,Fuzz, Z/EVES, PVS, ToolBox Lite, B Tool, Concurrency Workbench, FDR model checker, Fuzz, Z Browser

### 3. At what levels have you used the software?

Responses were:

- a) undergraduate courses, or
  - Z Specific Formaliser (2) , CadiZ, Telelogic TAU, SEDOS, TOPO, ToolBox Lite, B Tool, KM model checker, Concurrency Workbench, Fuzz, ZTC
- b) postgraduate courses? (i.e. after the undergraduate degree)
  - B Tool, Telelogic TAU, SEDOS, TOPO, ToolBox Lite (M.Sc. Conversion), Concurrency Workbench, FDR model checker, ZTC

### 4. What resources have you used in support?

Respondents listed the following:

- textbooks;
  - Turner, “Using Formal Description Techniques”
  - Jacky, “The Way of Z”
  - Potter, Sinclair & Till (2), “Introduction to … Z.”
  - Lightfoot, “Z”
  - Spivey, “Z Reference Manual”,
  - Woodcock and Davies, “Using Z”
  - Currie, “The Essence of Z”
  - Diller (2), “Z”
  - Ellsberger et al. “SDL”
  - Fitzgerald & Larson, “Modelling Systems”
  - Unknown (3)
- on-line tutorials/manuals: Fuzz, TOPO, LOLA, Z/EVES, PVS; Own materials, CadiZ; No such material used (3); own handouts (3)
- other web based resources: Z, CadiZ
- mailing lists: Z/EVES, PVS