Abstract—Software defined networks (SDNs) are receiving significant attention in the computer networking community, with increasing adoption by the industry. The key feature of SDNs is a centralized controller which programs the packet forwarding behavior of a distributed underlying network. This centralized view of control—which is absent in traditional networks—opens up opportunities for full formal verification.

While there is recent research in formal verification of these networks, model checking the controller behavior as it updates the underlying network has only seen limited application. Existing approaches are limited to verifying the controller for a small number of exchanged packets in the network. In this case study, we extend the state of the art by presenting abstractions for model checking controllers for an arbitrarily large number of packets exchanged in the network. We validate the utility of these abstractions through two applications: a learning switch and a stateful firewall.

I. INTRODUCTION

Software defined networks (SDNs) (such as ones based on Openflow [1]) have recently received significant attention in the computer networking community, with increasing relevance to and adoption by industry, e.g., [2]. The key feature of SDNs is a centralized controller (control plane) which programs a distributed underlying network (data plane). While providing a centralized view of control, any bugs in the controller code can be an Achilles heel to the functioning of the entire network [3]. In this case study, we explore abstractions for proving the correctness of controllers using model checking.

Fig. 1 shows an example topology of an SDN. The data plane consists of three hosts $H_A$, $H_B$ and $H_C$ which exchange packets $pkt_1$ and $pkt_2$ with each other via the network switches $S_1$, $S_2$ and $S_3$. These switches consist of ports $p_0$, $p_1$ and $p_2$. Each location in the network (switch ports and hosts) consists of an input and output buffer (referred to as the data state). Each switch enqueues packets in its input port buffers, and eventually forwards them to a set of output ports (or drops them) based on the packet processing logic.

The packet processing logic is encoded into the switches in the form of switch flow tables (also referred to as the network state). Based on the flow table, the switch applies one of the following 3 actions to an incoming packet: (1) it forwards the packet to a set of output ports of that switch, (2) drops the packet or (3) forwards it to the controller. The switch forwards packets to the controller by reporting them as events. The controller is a piece of software which updates switch flow tables through a standard interface (e.g., Openflow [1]), either in response to events forwarded by switches or spontaneously.

In this paper, we prove the correctness of the network controller program for a given network topology, and an arbitrarily large number of packets. We focus on per-packet properties, which assert the correctness of packet processing in the presence of updates from the controller. Note that these updates may themselves occur in response to events reported due to other packets, i.e., due to interference from other packets. Examples of such properties include no forwarding loop (i.e., a packet does not loop back to a switch which it has already visited) and no invalid drop (i.e., a packet is not dropped due to an invalid controller update to some switch).

Challenges in Verification: The key challenge in model checking SDNs is the state space explosion resulting from the following factors. (1) There can be a large number of packets alive in the network, resulting in a large buffer state—commodity switches can have of the order of ten megabytes of packet buffering per switch (e.g., [5]). Further, these packets create interference for each other by sending events to the controller which then trigger updates to the network state. (2) These packets and the corresponding events can have arbitrary interleavings. (3) The switch flow tables store a mapping from the packet header and the input port to the output port, resulting in a large network state—modern switches can have tens of thousands of flow table entries [6].

Related Work: Existing work in the verification of SDNs exploits the fact that the time between updates to the network state by the controller is much larger than the lifetime of a packet through the network. Thus, the state evolution of the network can be viewed as updates from one network configuration to another via intermediate (transient) states, as per the commands from the controller.

Static verification verifies a fixed configuration of the network by using either symbolic simulation [7], by reduction to SAT [4], [8] or by model checking [9].

Incremental verification approaches extend the static verification approach and incrementally verify the network for
all the network configurations [10], [11]. The property may however be violated in the transient stage.

Safe update builds upon the incremental verification approach by guaranteeing that the property under check holds during the transient stage by using specific update protocols [12]. This work is specific to enforcing properties for which the update protocols are designed—more complex properties may not be enforced with this approach.

Dynamic checking seeks to verify the properties on the network in the presence of arbitrary updates from the controller, even when no specific update protocol has been implemented to ensure the property. This is the space of our work—the other works we are aware of in this space are NICE [3] and FlowLog [13]. They use a model checking based approach to successfully find important bugs in controller code. However, they check the controller for a bounded number of exchanged packets. In this work we extend dynamic checking and scale to an arbitrarily large number of packets.

Key Contribution: This work addresses the challenges outlined above by first constructing a data state abstraction, and then, a network state abstraction which builds upon the data state abstraction to significantly reduce the model size.

The data state abstraction is based on the standard data type reduction [14] and addresses challenges (1) and (2) by keeping just one packet (concrete packet), $pkt^c$, in the system and replacing the effect of all the other packets on the network state by non-deterministically injecting an arbitrarily large number of environment packets ($pkt^e$). These packets have arbitrary header values, unless constrained by user-added lemmas, and can be injected at any port of any switch. When injected, these environment packets may be forwarded as events to the controller and trigger updates to the network state. Thus, these packets simulate the updates to the network state triggered by an arbitrarily large number of other packets. Further, the environment packets need not traverse the links and occupy data state as they are directly injected at arbitrary ports—this enables abstracting away all the buffers.

Since there is only one alive packet ($pkt^c$) in the system after the data state abstraction, the network state abstraction exploits this to address challenge (3) by case splitting on the source and destination hosts of this packet: the switch flow table can then be abstracted to contain information specific to only these hosts, which are fixed for a concrete packet. This significantly reduces the network state.

Mechanical Construction: The data state abstraction is constructed by adding a special host for injecting environment packets—this host is independent of the controller application under verification. The network state abstraction adds a runtime check to the flow table to only allow updates corresponding to the selected source and destination hosts.

Experimental Setup: We model the controller code to closely resemble the original (typically Python) code in the Murphi language (CMurphi 5.4.6). To verify the controller for a specified topology and property, we use a Murphi model with (1) the controller code, and (2) the switches and hosts connected according to the specified topology with the property specified on it. The abstractions are also implemented on this model.

We demonstrate the utility of the abstraction by verifying no forwarding loop for a learning switch application (controller), PySwitch [15] and no invalid drop property for a stateful firewall application. We were able to find bugs in the buggy version of these applications and prove correctness for the correct ones for an arbitrary number of packets.

Limitation: While our approach verifies topologies larger than the state of the art for dynamic checking, it cannot scale to realistically large sizes (e.g., data centers). However, in certain cases it is possible to extend controllers proved on smaller topologies to larger ones through topology abstractions [16].

II. Modeling Network Controllers

The network consists of a controller, switches (switch $S_i$ has an id $i$) with ports ($p_i$ has an id $i$) and hosts ($H_i$ has an id $i$). Packets traverse the network by hopping from one location to another (unless they get dropped). Each packet consists of a header and payload (data information). The source and destination host id of a packet $pkt$ are denoted by $pkt.src$ and $pkt.dst$, respectively.

When a packet arrives at a switch port, the switch processes the packet in accordance with the flow table. For sake of brevity, we assume that the flow table of a switch $S$ (denoted by $S.ft$) matches on the source, destination, and input port ($p_i$) of the incoming packet and applies a set of actions to the packet—in general our approach extends to cases where it matches other fields as well. Formally, a flow table is a mapping $S.ft : (pkt.src, pkt.dst, p_i) \rightarrow A$, where $A$ is a set containing one or more actions from the following: (1) forward the packet to a set of output ports $P_o$ of the switch (denoted by Forward ($P_o$)), (2) drop the packet (Drop), or (3) forward it to the controller ($SendToController$). We denote the set of the above three actions by $A$.

Controller-switch interaction: The controller-switch interaction happens in accordance with the Openflow [1] specification: (1) switches report events to the controller which are enqueued in a per-switch event buffer at the controller, and (2) the controller sends commands to the switch which are enqueued in a command buffer at the switch. Following the approach of Foster et al. [17], the relevant events and commands are described below.

Events: The event used in this paper is the $packet\_in(swID, portID, packet)$ event, which tells the controller that $packet$ has arrived at port with id $portID$ of switch with id $swID$.

Controller Commands: The controller can either react to events reported by the switch through event handlers, or spontaneously program the switch. The controller commands can be one of the following: (1) install($swID, match, actions$): this command updates the flow table of switch $swID$ to apply actions (a subset of $A$) to all packets which match the pattern specified by match. The string match is of the form $\{src : H_1, dst : H_2, inport : p_i\}$, i.e., match all incoming packets with $pkt.src = H_1, pkt.dst = H_2$, and ingress port $p_i$ at switch $swID$. (2) send($swID, packet, action$) sends the packet to switch $swID$ where action is

\[\text{Packet rewritings are discussed at the end of §III.}\]
applied to it at the switch. Here action is one of \{Forward, Drop, Flood\}, where Flood instructs the switch to forward the packet on all its ports except the packet’s ingress port.

**Property:** We verify invariants of the form $\forall \text{pkt} : \phi(B_{\text{pkt}})$, where $\phi$ is a propositional logic formula and $B_{\text{pkt}}$ is some per-packet book-keeping state. For example, this state can log the packet history, *i.e.*, switches which the packet has visited, in order to detect loops.

### Running example (MAC learning switch)

**MAC address learning switch:** We use a layer 2 MAC address learning switch application, Pyswitch [15] with topology as shown in Fig. 1, as a running example to describe key concepts. The controller algorithm is shown in Fig. 2. At a high level, for each switch $\text{swID}$, the controller learns a mapping (denoted by $\text{ctrlState}[$swID$]$) from host MAC addresses to ports. This allows the switch to forward packets destined to these hosts. As an example, suppose the packet $\text{pkt}_{1}$, with source $\text{HA}$ and destination $\text{HB}$, arrives at port $p_{0}$ of switch $S_{2}$. In case no match exists for the packet, it is matched to a default flow table entry which forwards a packet_in event to the controller. The packet_in event handler learns that the host $\text{HA}$ is reachable through port $p_{0}$ on switch $S_{2}$ (line 2). In case the port leading to the destination $\text{HB}$ is unknown, the if condition on line 3 evaluates to false, and the packet is flooded on all ports, except the incoming port (line 11). However, if the destination is found in $\text{ctrlState}$, the flow table is updated to forward all subsequent packets with the same src, dst and import to $p_{1}$ (line 8).

**Property:** We verify the no forwarding loop property for the Pyswitch controller. Due to flooding on a topology (Fig. 1) with a loop, the property is violated. However, if the controller only sends packets along a spanning tree (*e.g.*, no packets between port $p_{2}$ of $S_{2}$ and $p_{1}$ of $S_{3}$), the property holds.

### III. ABSTRACTION

#### Data state abstraction

As discussed in §I, the data state abstraction exploits the fact that the property under check is a per-packet property: it checks the property on one concrete packet $\text{pkt}^{c}$, and abstracts away all the other packets. Continuing on the Pyswitch example from §II, suppose $\text{pkt}^{c}$ is injected at port $p_{2}$ of switch $S_{2}$ in Fig. 1, such that $\text{pkt}^{c}.\text{src} = \text{HA}$. This leads the switch to send a packet_in to the controller which updates $\text{ctrlState}[S_{2}] [\text{HA}]$ to $p_{2}$. Next, suppose the concrete packet $\text{pkt}^{c}$ with source $\text{HB}$ and destination $\text{HA}$ arrives at port $p_{1}$ of $S_{2}$. The switch sends this packet to the controller, and since $\text{ctrlState}[S_{2}] [\text{HA}] = p_{2}$, the controller commands the switch to forward the packet out port $p_{2}$ (line 9 of Fig. 2) to $S_{3}$. If there are no matching entries for $\text{pkt}^{c}$ at $S_{3}$ and $S_{1}$ both in flow tables and $\text{ctrlState}$, the packet gets flooded at both switches (line 11). Thus, $\text{pkt}^{c}$ loops back to $S_{2}$, which is a violation of the forwarding loop property.

**Refinement:** Since the header of $\text{pkt}^{c}$ can take arbitrary values, the updates triggered by $\text{pkt}^{c}$ are highly unconstrained. This leads to both scalability bottlenecks as well as functional incorrectness due to over-abstraction, *i.e.*, the model exhibiting more behaviors than are realistically expected. We follow the approach of the CMP (CoMpositional) method [18]: the model is iteratively model checked and refined by the user by adding non-interference lemmas in order to constrain $\text{pkt}^{c}$. The non-interference lemmas we used typically constrain the model according to reachability in the topology. For example a packet with source $\text{HA}$ cannot be injected at port $p_{1}$ of $S_{2}$, *i.e.*, $(\text{port} = p_{1}) \& (\text{switch} = S_{2}) \rightarrow (\text{pkt}.\text{src} \neq \text{HA})$. (Since these lemmas are application-independent, they were added pre-emptively to mechanically constrain the data state abstraction.) As per the CMP method, these non-interference lemmas do not over-constrain the environment packet $\text{pkt}^{c}$: they are also model checked by validating them on $\text{pkt}^{c}$ [18].

**Network state abstraction:** As discussed in §I, the network state abstraction case splits on the source and destination of $\text{pkt}^{c}$ to abstract the flow tables. Suppose we assume that $\text{pkt}^{c}$ has source $\text{HA}$ and destination $\text{HB}$. Then, for each switch $S$, the flow table mapping $S.f_{t}$ can be abstracted to $S.f_{t}^{\text{abs}}$ where $S.f_{t}^{\text{abs}}(\text{pkt}^{c}, p) = S.f_{t}(\text{pkt}^{c}, p)$ for all ports $p$ of the switch, and $S.f_{t}^{\text{abs}}(\text{pkt}^{c}, p) = \{\text{SendToController}\}$ for all other packets (*i.e.*, $\text{pkt}^{c}$). The Forward action is not applied to $\text{pkt}^{c}$ as it is non-deterministically injected at all ports.

**Packet rewrites:** In order to handle packet rewrites, the network state abstraction can be refined by including flow rules for rewritten header values as well. These rules are needed to process the concrete packet when its header is rewritten.

### IV. EXPERIMENTS

We verified two applications: Pyswitch and a stateful firewall on a 2.40 GHz Intel Core 2 Quad processor, with 3.74 GB RAM. Murphi source code is available online [19].

**MAC learning switch (Pyswitch):** For the Pyswitch application, we verified loop freedom for the star topology shown in Fig. 1, with non-interference lemmas from §III added pre-emptively for scalability. The loop was found in 0.1 sec with 159 states explored. Next, on constraining the topology to forward packets only along the spanning tree, the model checker proved correctness with an arbitrary number of packets exchanged between $\text{HA}$ and $\text{HB}$ in 600s with 1.45M states. We note that model checking did not finish in a day without the abstractions. Finally, we ran a stress test with a larger fat tree topology with 20 switches, 16 hosts and 48 links. While model checking did not finish for an arbitrarily large number of packets, it finished in 68352s for the single packet case with network state abstraction.

**Stateful firewall:** We consider a simple firewall policy which may be used to prevent direct connections from the Internet into an enterprise network, *e.g.*, to implement Network Address Translation (NAT). Fig. 3 shows an enterprise network
connected to the Internet via a firewall implemented on two switches $S_1$ and $S_2$. The controller (not shown in Fig. 3 for brevity) initializes the default behavior of $S_1$ and $S_2$ as follows: (1) $S_1$ sends all incoming traffic at port $p_1$ to the controller, in addition to forwarding out of $p_2$, (2) $S_1$ forwards incoming traffic at $p_2$ directly to the enterprise host $H_1$, (3) $S_2$ sends all incoming traffic at $p_1$ directly to the Internet, and (4) $S_2$ forwards incoming traffic at $p_2$ to the controller. As packets arrive, the controller dynamically updates the switch flow tables to implement the following high-level policy (Fig. 4): (a) All traffic originating from any enterprise host $H_1$ and destined to any Internet host $H_2$ is allowed to pass freely. In particular $S_1$ forwards all traffic to port $p_2$ bypassing the controller after the first packet in (line 5). (b) Traffic from an Internet host $H_2$ destined to an enterprise host $H_1$ is only allowed if the communication was initiated by $H_1$ first (line 8). (c) If $H_2$ attempts to communicate with $H_1$ without prior initiation by $H_1$, then $H_2$ is considered malicious and is explicitly blacklisted (line 12).

Verification: We verify the no invalid drop property by checking if traffic from Internet host $H_2$ replying to a request sent by enterprise host $H_1$ does not get dropped. Due to a race condition between the events reported by $S_1$ and $S_2$, the controller erroneously blacklists host $H_2$. This happens when $H_1$ sends a first request to $H_2$. The request goes to $S_1$ first which forwards it via $S_2$ to $H_2$, and also forwards an event $e_1$ reporting the request to the controller. However, this event gets delayed and in the meantime $H_2$ replies, and $S_2$ forwards this to the controller as an event $e_2$. Since $e_2$ is processed by the controller before $e_1$, $H_2$ is erroneously blacklisted. (Note that events across switches can be processed out of order.) Our approach found this race condition in 0.13 sec with 482 states, without requiring any lemmas.

Fixing the violation: This bug can be fixed by requiring $S_1$ to wait for the controller before forwarding requests from $H_1$ to $H_2$ via $S_2$. Our approach was able to prove correctness for an arbitrarily large number of packets in 0.19 sec with 613 states, without requiring any lemmas.

V. CONCLUSION AND ONGOING WORK

We have presented abstractions for model checking controllers for software defined network applications. These abstractions extend the state of the art by enabling correctness proofs for SDN controllers for an arbitrarily large number of packets and their ensuing controller state updates. As a next step, we plan to explore abstractions to further scale model checking for larger topologies. In particular, since properties are typically violated along a particular path taken by packets in the network, we plan to focus on validating properties for packets taking fixed paths in the topology instead of all possible paths.

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