For loops and nested loops

"Always to see the general in the particular is the very foundation of genius."

-Arthur Schopenhauer

Repetition with for loops

- So far, repeating a statement is redundant:
  ```java
  System.out.println("Mike says:);
  System.out.println("Do Practice-It problems!");
  System.out.println("Do Practice-It problems!");
  System.out.println("Do Practice-It problems!");
  System.out.println("Do Practice-It problems!");
  System.out.println("It makes a HUGE difference.");
  ```

- Java's for loop statement performs a task many times.
  ```java
  System.out.println("Mike says:");
  for (int i = 1; i <= 5; i++) {
      // repeat 5 times
      System.out.println("Do Practice-It problems!");
  }
  System.out.println("It makes a HUGE difference.");
  ```

For loop syntax

- Perform `<initialization>` once.
- Repeat the following:
  - Check if the `<test>` is true. If not, stop.
  - Execute the `<statement>`s.
  - Perform the `<update>`.

```
for (<initialization>; <test>; <update>) {
    // header
    <statement>
    <statement>
    ...
    <statement>
}
```

Initialization

```
for(int i = 1; i <= 5; i++) {
    System.out.println("Do Practice-It!");
}
```

- Tells Java compiler what variable to use in the loop
  - Performed once as the loop begins
  - The variable is called a loop counter
    - can use any name, not just `i`
    - can start at any value, not just `1`
for(int i = 1; i <= 5; i++) {
    System.out.println("Do Practice-It!");
}

- Tests the loop counter variable against a limit
  - Uses comparison operators:
    - <  less than
    - <= less than or equal to
    - >  greater than
    - >= greater than or equal to

for(int i = 1; i <= 5; i++) {
    System.out.println("Do Practice-It!");
}

- Perform update step
  - Generally adding one to loop control variable
  - Could be other operations such as subtracting one, multiplying

**Increment and decrement**

*shortcuts to increase or decrease a variable's value by 1*

<table>
<thead>
<tr>
<th>Shorthand</th>
<th>Equivalent longer version</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;variable&gt;++;</td>
<td>&lt;variable&gt; = &lt;variable&gt; + 1;</td>
</tr>
<tr>
<td>&lt;variable&gt;--;</td>
<td>&lt;variable&gt; = &lt;variable&gt; - 1;</td>
</tr>
</tbody>
</table>

```java
int x = 2;
x++; // x = x + 1;
// x now stores 3
double gpa = 2.5;
gpa--; // gpa = gpa - 1;
// gpa now stores 1.5
```

**Modify-and-assign operators**

*shortcuts to modify a variable's value*

<table>
<thead>
<tr>
<th>Shorthand</th>
<th>Equivalent longer version</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;variable&gt; += &lt;exp&gt;;</td>
<td>&lt;variable&gt; = &lt;variable&gt; + (&lt;exp&gt;);</td>
</tr>
<tr>
<td>&lt;variable&gt; -= &lt;exp&gt;;</td>
<td>&lt;variable&gt; = &lt;variable&gt; - (&lt;exp&gt;);</td>
</tr>
<tr>
<td>&lt;variable&gt; *= &lt;exp&gt;;</td>
<td>&lt;variable&gt; = &lt;variable&gt; * (&lt;exp&gt;);</td>
</tr>
<tr>
<td>&lt;variable&gt; /= &lt;exp&gt;;</td>
<td>&lt;variable&gt; = &lt;variable&gt; / (&lt;exp&gt;);</td>
</tr>
<tr>
<td>&lt;variable&gt; %= &lt;exp&gt;;</td>
<td>&lt;variable&gt; = &lt;variable&gt; % (&lt;exp&gt;);</td>
</tr>
</tbody>
</table>

```java
x += 3; // x = x + 3;
gpa -= 0.5; // gpa = gpa - 0.5;
number *= 2 + 1; // number = number * (2 + 1);
```
The for loop is a control structure—a syntactic structure that controls the execution of other statements.

Example:

- “Shampoo hair. Rinse. Repeat.”

```
for (int i = 1; i <= 6; i++) {
    System.out.println(i + " squared = " + (i * i));
}
```

Intuition: "I want to print a line for each number from 1 to 6"

The for loop does exactly that!

```
for (int i = 1; i <= 6; i++) {
    System.out.println(i + " squared = " + (i * i));
}
```

"For each integer i from 1 through 6, print ..."

Loop walkthrough

```
for (int i = 1; i <= 4; i++) {
    System.out.println(i + " squared = " + (i * i));
}
System.out.println("Whoo!");
```

Output:

1 squared = 1
2 squared = 4
3 squared = 9
4 squared = 16
Whoo!

Multi-line loop body

```
System.out.println("+-----+");
for (int i = 1; i <= 3; i++) {
    System.out.println("\ / ");
    System.out.println("/   ");
}
System.out.println("+-----+");
```

Output:

```
+-----+
\ /   
/   
+-----+
```

Repetition over a range

```
System.out.println("1 squared = " + 1 * 1);
System.out.println("2 squared = " + 2 * 2);
System.out.println("3 squared = " + 3 * 3);
System.out.println("4 squared = " + 4 * 4);
System.out.println("5 squared = " + 5 * 5);
System.out.println("6 squared = " + 6 * 6);
```

- Intuition: "I want to print a line for each number from 1 to 6"
Expressions for counter

```java
int highTemp = 5;
for (int i = -3; i <= highTemp / 2; i++) {
    System.out.println(i * 1.8 + 32);
}
```

– This computes the Fahrenheit equivalents for -3 degrees Celsius to 2 degrees Celsius.

Output:
26.6
28.4
30.2
32.0
33.8
35.6

System.out.print

– Prints without moving to a new line
– allows you to print partial messages on the same line

```java
int highestTemp = 5;
for (int i = -3; i <= highestTemp / 2; i++) {
    System.out.print((i * 1.8 + 32) + "  ");
}
```

• Output:
26.6  28.4  30.2  32.0  33.8  35.6

• Concatenate "  " to separate the numbers

Clicker Question

How many asterisks are output by the following code?

```java
for(int i = -2; i <= 13; i++) {
    System.out.print("*");
    System.out.print("**");
}
```

A. 0   B. 15   C. 45
D. 48   E. 68

Counting down

The `<update>` can use -- to make the loop count down.

– The `<test>` must say > instead of < (or logic error)

```java
System.out.println("T-minus ");
for (int i = 10; i >= 1; i-- ) {
    System.out.print(i + ", ");
}
```

System.out.println("blastoff!");
System.out.println("The end.");

Output:
T-minus 10, 9, 8, 7, 6, 5, 4, 3, 2, 1, blastoff!
The end.
Practice Problem

- Newton's method for approximating square roots
  adapted from the Dr. Math website

  The goal is to find the square root of a number. Let's call it num

  1. Choose a rough approximation of the square root of num, call it approx.
     How to choose?
  2. Divide num by approx and then average the quotient with approx,
     in other words we want to evaluate the expression \( \left( \frac{\text{num}}{\text{approx}} \right) + \text{approx} \) / 2
  3. How close are we? In programming we would store the result of the expression back into the variable approx.
  4. How do you know if you have the right answer?

Sample of Newton's Method

<table>
<thead>
<tr>
<th>num</th>
<th>approx</th>
<th>((\text{num/approx})+\text{approx})/2</th>
<th>\text{approx*approx}</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>6</td>
<td>(12 / 6 + 6) / 2 = 4</td>
<td>16</td>
</tr>
<tr>
<td>12</td>
<td>4</td>
<td>(12 / 4 + 4) / 2 = 3.5</td>
<td>12.25</td>
</tr>
<tr>
<td>12</td>
<td>3.5</td>
<td>(12 / 3.5 + 3.5) / 2 = 3.4642857...</td>
<td>12.0012..</td>
</tr>
<tr>
<td>12</td>
<td>3.462857</td>
<td>= 3.46410162...</td>
<td>12.00000003</td>
</tr>
<tr>
<td>12</td>
<td>3.46410162</td>
<td>= 3.46410161...</td>
<td>11.999999999</td>
</tr>
</tbody>
</table>

3.4641016151377544 after 5 steps

3.4641016151377545870548926830117 (from calculator)

Nested loops

- nested loop: A loop placed inside another loop.

```java
for (int i = 1; i <= 5; i++) {
    for (int j = 1; j <= 10; j++) {
        System.out.print("*");
    }
    System.out.println();  // to end the line
}
```

Output:

```
**********
**********
**********
**********
**********
```

- The outer loop repeats 5 times; the inner one 10 times.
  "sets and reps" exercise analogy
Nested for loop exercise

What is the output of the following nested for loops?

```java
for (int i = 1; i <= 5; i++) {
    for (int j = 1; j <= i; j++) {
        System.out.print("*");
    }
    System.out.println();
}
```

Output:

```
* 
** 
*** 
**** 
***** 
```

Nested for loop exercise

What is the output of the following nested for loops?

```java
for (int i = 1; i <= 5; i++) {
    for (int j = 1; j <= i; j++) {
        System.out.print(i);
    }
    System.out.println();
}
```

Output:

```
1 
2 2 
3 3 3 
4 4 4 4 
5 5 5 5 5 
```

clicker Question

What is output by the following code?

```java
int total = 0;
for(int i = 1; i <= 4; i++) {
    for(int j = 1; j <= i; j++) {
        total += i;
    }
}
System.out.println(total);
```

A. 10   B. 20   C. 30   D. 40   E. 50

Common errors

Both of the following sets of code produce infinite loops:

```java
for (int i = 1; i <= 5; i++) {
    for (int j = 1; i <= 10; j++) {
        System.out.print("*");
    }
    System.out.println();
}
```

```java
for (int i = 1; i <= 5; i++) {
    for (int j = 1; j <= 10; i++) {
        System.out.print("*");
    }
    System.out.println();
}
Complex output

- Write a nested `for` loop to produce the following output.
  `inner loop` (repeated characters on each line)

```
...1
...2
..3
..4
 5
```

- We must build multiple complex lines of output using:
  - an `outer "vertical" loop` for each of the lines
  - `inner "horizontal" loop(s)` for the patterns within each line

Outer and inner loop

- First write the outer loop, from 1 to the number of lines.

```
for (int line = 1; line <= 5; line++) {
    ...
}
```

- Now look at the line contents. Each line has a pattern:
  - some dots (0 dots on the last line), then a number

```
... .1
... .2
.. .3
.. .4
 5
```
  - Observation: the number of dots is related to the line number.

Mapping loops to numbers

```
for (int count = 1; count <= 5; count++) {
    System.out.print(...);
}
```

- What statement in the body would cause the loop to print:

```
4 7 10 13 16
```

```
for (int count = 1; count <= 5; count++) {
    System.out.print((3 * count + 1) + " ");
}
```

Loop tables

- What statement in the body would cause the loop to print:

```
2 7 12 17 22
```

- To see patterns, make a table of `count` and the numbers.
  - Each time `count` goes up by 1, the number should go up by 5.
  - But `count * 5` is too great by 3, so we subtract 3.

<table>
<thead>
<tr>
<th>count</th>
<th>number to print</th>
<th>5 * count</th>
<th>5 * count - 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>5</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>7</td>
<td>10</td>
<td>7</td>
</tr>
<tr>
<td>3</td>
<td>12</td>
<td>15</td>
<td>12</td>
</tr>
<tr>
<td>4</td>
<td>17</td>
<td>20</td>
<td>17</td>
</tr>
<tr>
<td>5</td>
<td>22</td>
<td>25</td>
<td>22</td>
</tr>
</tbody>
</table>
Loop tables question

- What statement in the body would cause the loop to print:
  17 13 9 5 1
- Let's create the loop table together.
  - Each time `count` goes up 1, the number printed should ...
  - But this multiple is off by a margin of ...

<table>
<thead>
<tr>
<th>count</th>
<th>number to print</th>
<th>-4 * count</th>
<th>-4 * count + 21</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>17</td>
<td>-4</td>
<td>17</td>
</tr>
<tr>
<td>2</td>
<td>13</td>
<td>-8</td>
<td>13</td>
</tr>
<tr>
<td>3</td>
<td>9</td>
<td>-12</td>
<td>9</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>-16</td>
<td>5</td>
</tr>
<tr>
<td>5</td>
<td>1</td>
<td>-20</td>
<td>1</td>
</tr>
</tbody>
</table>

Another view: Slope-intercept

- The next three slides present the mathematical basis for the loop tables.

<table>
<thead>
<tr>
<th>count (x)</th>
<th>number to print (y)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
</tr>
<tr>
<td>2</td>
<td>7</td>
</tr>
<tr>
<td>3</td>
<td>12</td>
</tr>
<tr>
<td>4</td>
<td>17</td>
</tr>
<tr>
<td>5</td>
<td>22</td>
</tr>
</tbody>
</table>

Another view: Slope-intercept

- Caution: This is algebra, not assignment!
- Recall: slope-intercept form ($y = mx + b$)
- Slope is defined as "rise over run" (i.e. rise / run). Since the "run" is always 1 (we increment along $x$ by 1), we just need to look at the "rise". The rise is the difference between the $y$ values. Thus, the slope ($m$) is the difference between $y$ values; in this case, it is +5.
- To compute the $y$-intercept ($b$), plug in the value of $y$ at $x = 1$ and solve for $b$. In this case, $y = 2$.
  
  $y = m \cdot x + b$
  $2 = 5 \cdot 1 + b$
  Then $b = -3$

- So the equation is
  $y = m \cdot x + b$
  $y = 5 \cdot x - 3$
  $y = 5 \cdot count - 3$

Another view: Slope-intercept

- Algebraically, if we always take the value of $y$ at $x = 1$, then we can solve for $b$ as follows:
  
  $y = m \cdot x + b$
  $y_1 = m \cdot 1 + b$
  $y_1 = m + b$
  $b = y_1 - m$

- In other words, to get the $y$-intercept, just subtract the slope from the first $y$ value ($b = 2 - 5 = -3$)
  
  - This gets us the equation
    $y = m \cdot x + b$
    $y = 5 \cdot x - 3$
    $y = 5 \cdot count - 3$
    (which is exactly the equation from the previous slides)
Nested for loop exercise

- Make a table to represent any patterns on each line.

<table>
<thead>
<tr>
<th>line</th>
<th># of dots</th>
<th>(-1 * ) line</th>
<th>(-1 * ) line + 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4</td>
<td>-1</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>-2</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>2</td>
<td>-3</td>
<td>2</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td>-4</td>
<td>1</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
<td>-5</td>
<td>0</td>
</tr>
</tbody>
</table>

- To print a character multiple times, use a for loop.

```java
for (int j = 1; j <= 4; j++) {
    System.out.print("."); // 4 dots
}
```

Nested for loop solution

- Answer:

```java
for (int line = 1; line <= 5; line++) {
    for (int j = 1; j <= (-1 * line + 5); j++) {
        System.out.print(".");
    }
    System.out.println(line);
}
```

- Output:

....1
...2
..3
..4
5

Nested for loop exercise

- What is the output of the following nested for loops?

```java
for (int line = 1; line <= 5; line++) {
    for (int j = 1; j <= (-1 * line + 5); j++) {
        System.out.print(".");
    }
    for (int k = 1; k <= line; k++) {
        System.out.print(line);
    }
    System.out.println();
}
```

- Answer:

....1
...2.
..3..
..4...
5....

Nested for loop exercise

- Modify the previous code to produce this output:

```java
for (int line = 1; line <= 5; line++) {
    for (int j = 1; j <= (-1 * line + 5); j++) {
        System.out.print(".");
    }
    System.out.println(line);
    for (int k = 1; k <= (line - 1); k++) {
        System.out.print(".");
    }
    System.out.println();
}
```