

Uncertain<T>

A First-Order Type for Uncertain Data

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Uncertainty bugs: Applications use estimated data, but languages use discrete types

Using estimates as facts

Discrete types ignore random error. 95% of WinPhone apps ignore GPS error.

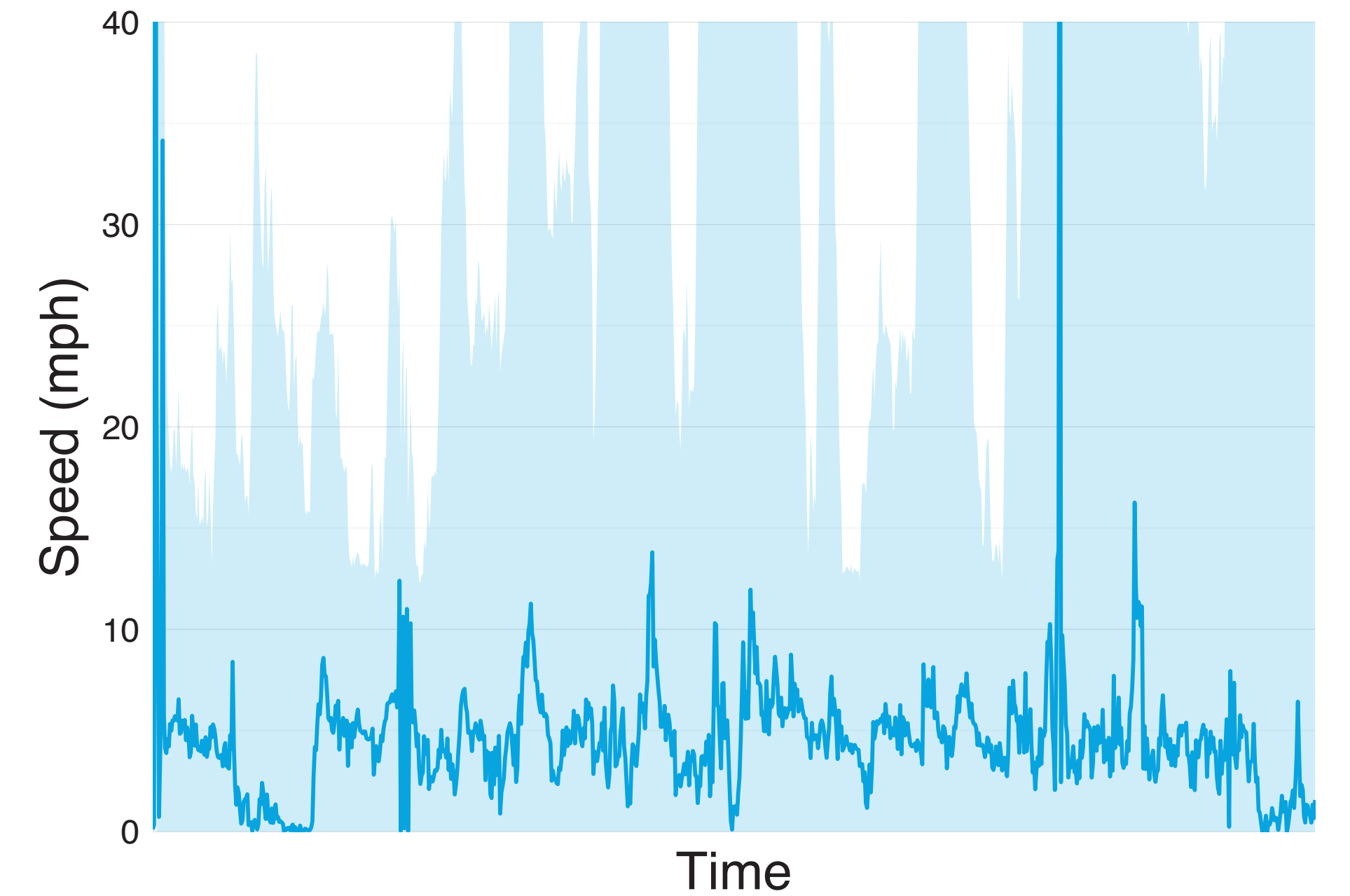
Computation compounds error

Calculations induce more uncertainty, making results even more inaccurate.

Inference asks wrong questions

Code asks boolean questions, but estimated data is probabilistic.

```
Location LastLoc = GetGPSLoc();
while (true) {
  Sleep(dt);
  Location Loc = GetGPSLoc();
  PlotOnMap(Loc);
  double Speed
    = Dist(LastLoc, Loc) / dt;
  if (Speed > 65)
    SpeedLimitWarning();
  LastLoc = Loc;
}
```

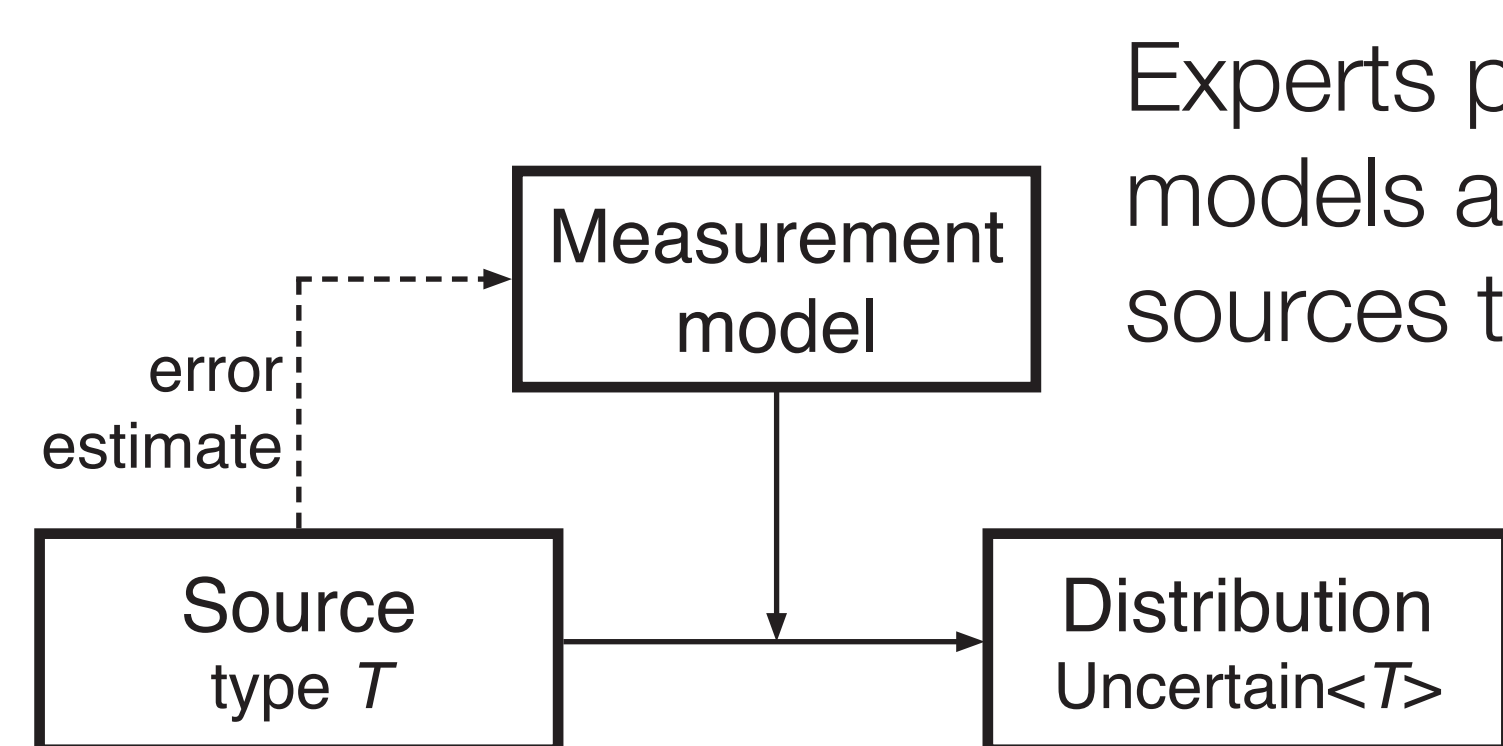


This app measures speeds with GPS, and reports absurd data like walking at 59mph. Compounding error causes a wide 95% confidence interval.

Can application writers handle estimated data without requiring a PhD in statistics?

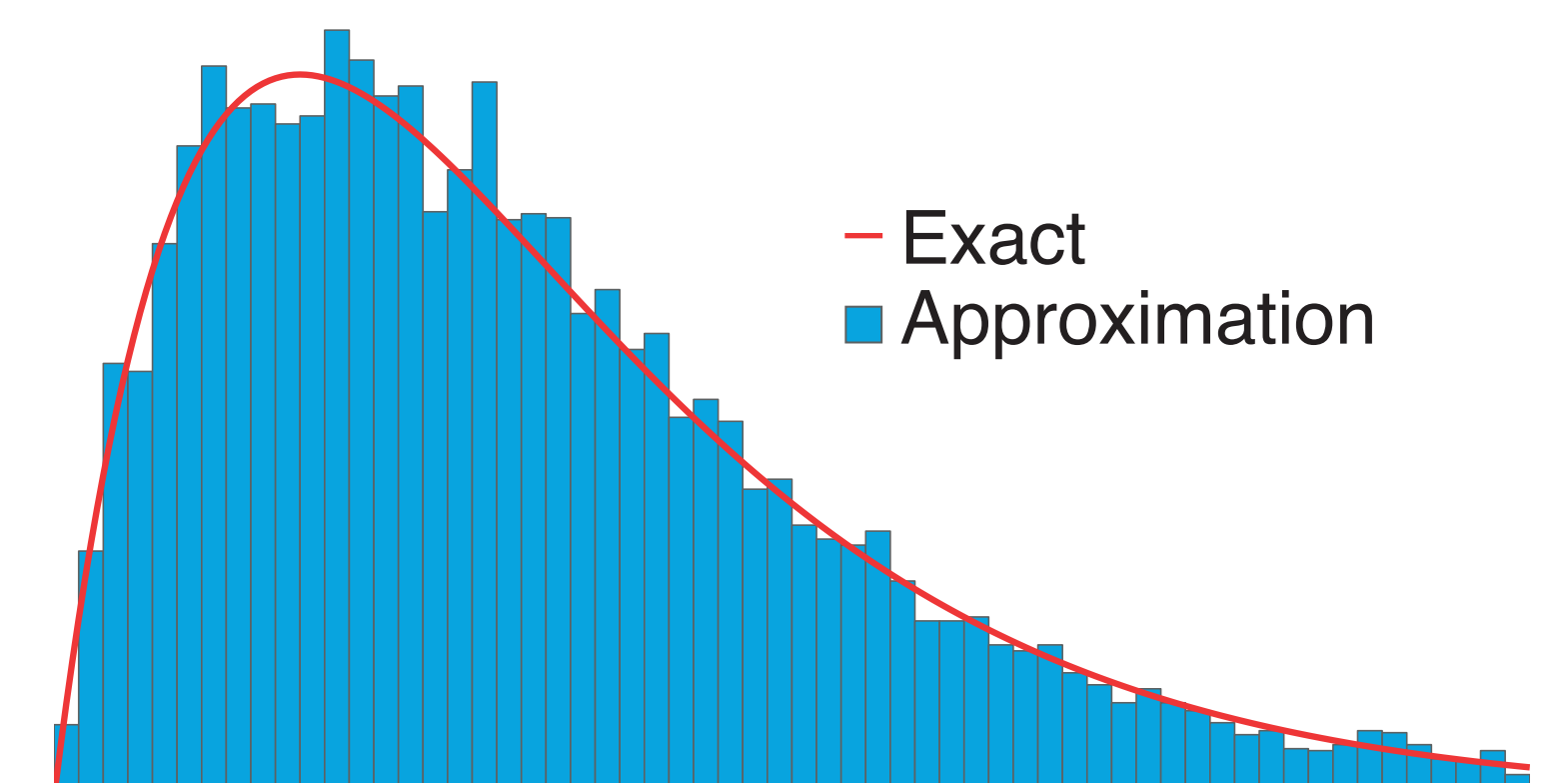
Four steps to using Uncertain<T>, the uncertain type abstraction

1 Identifying distributions

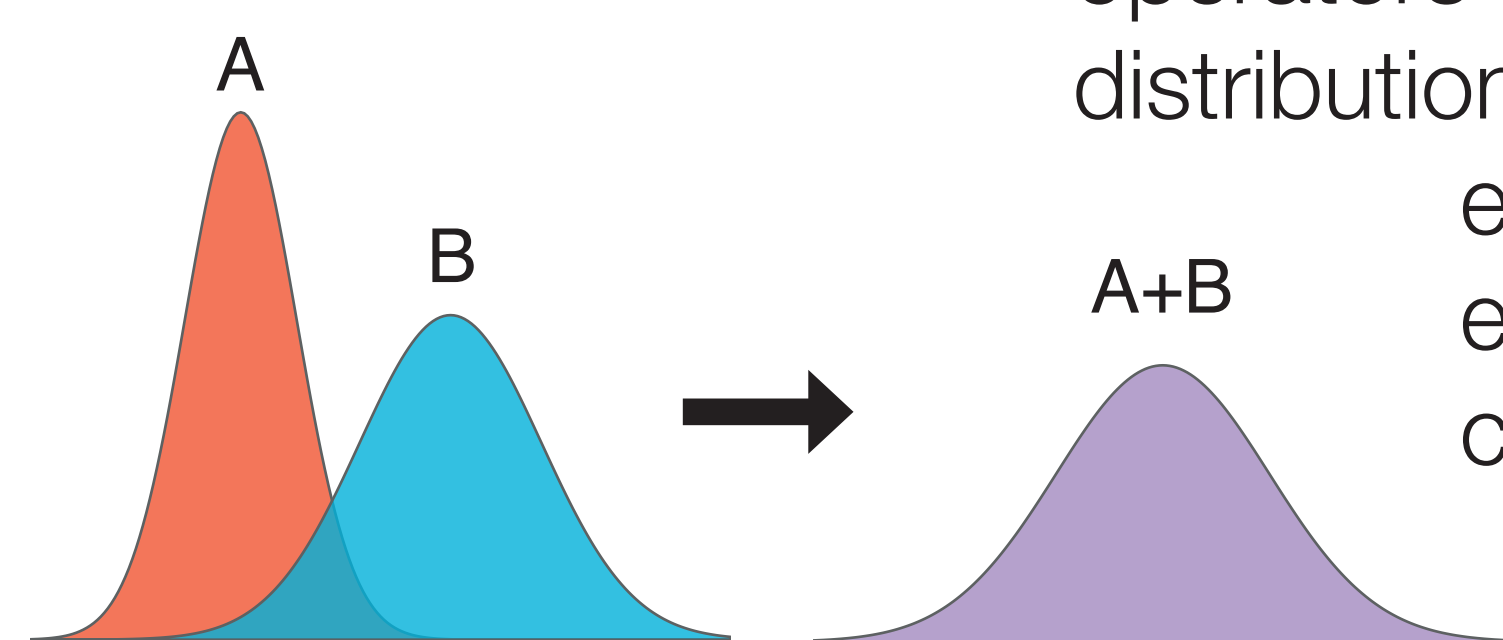


Experts provide measurement models along with uncertain data sources to create distributions.

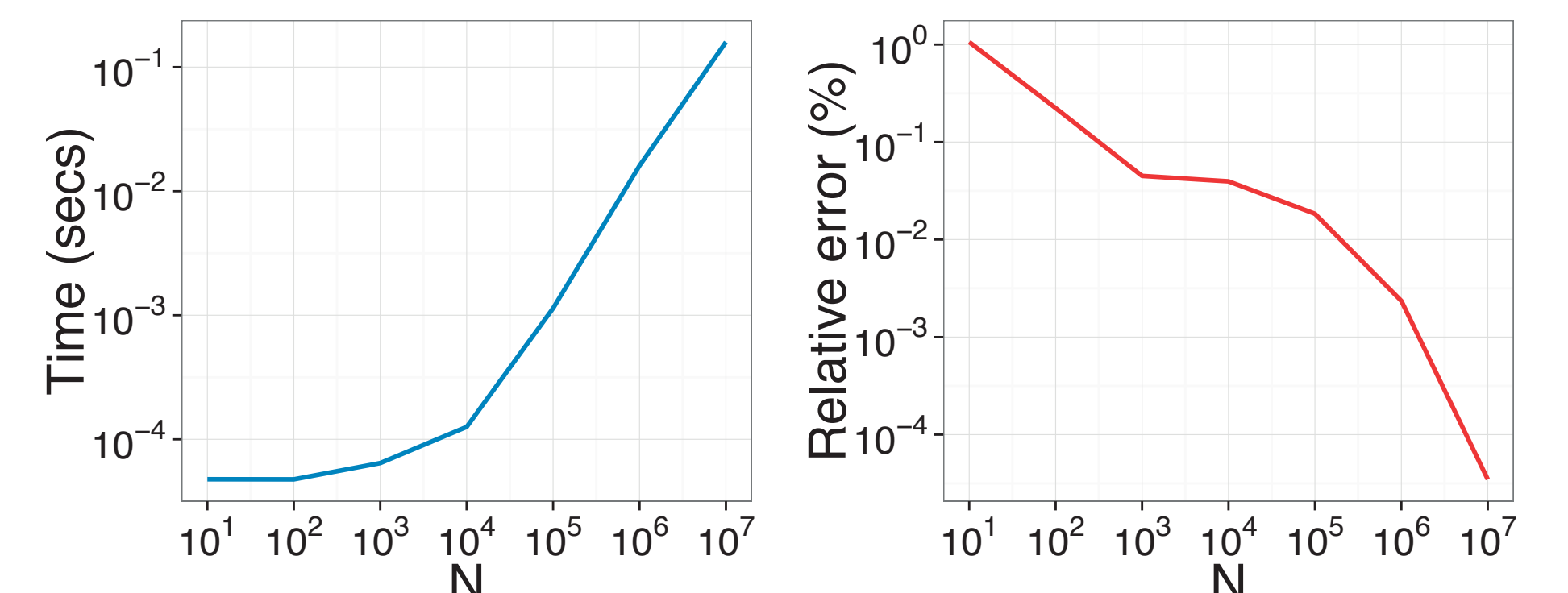
Uncertain<T> approximates arbitrary distributions by Monte Carlo random sampling.



2 Computing with estimates

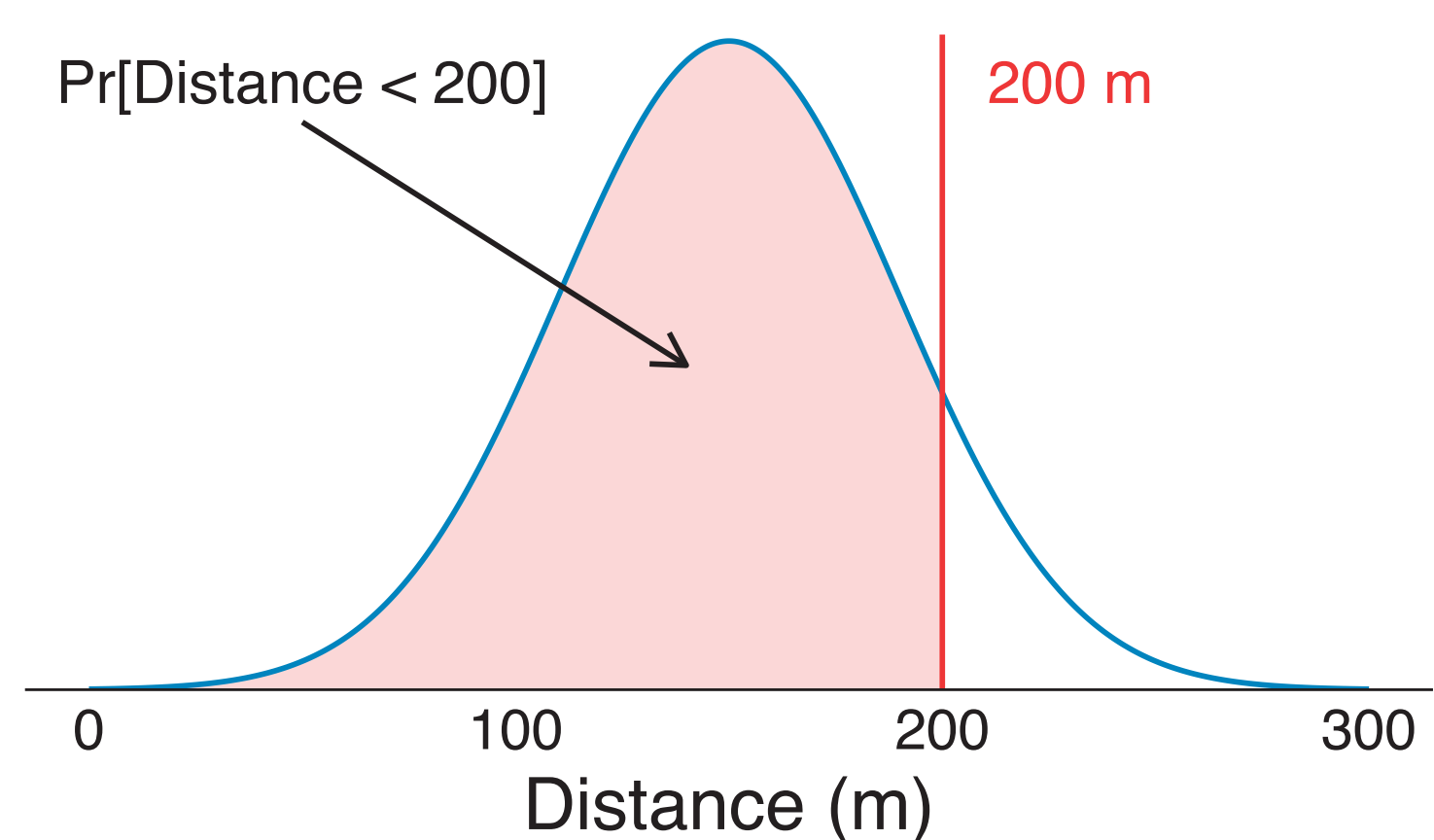


Uncertain<T> lifts arithmetic operators over type *T* to act over distributions of *T*, which captures the effect of compounding error when making calculations.



Sample size trades speed for accuracy.

3 Asking the right questions



The semantics of conditionals are unclear when distributions are involved. There is a *probability* that $A < B$; so comparisons have type $\text{Unc}\langle T \rangle \rightarrow \text{Unc}\langle T \rangle \rightarrow \text{Bernoulli}$. But this does not preserve the total order on *T* if it has one.

Alternatively we can use expected values: the expected value of an Uncertain<T> is of type *T*, so preserves the order properties of *T*.

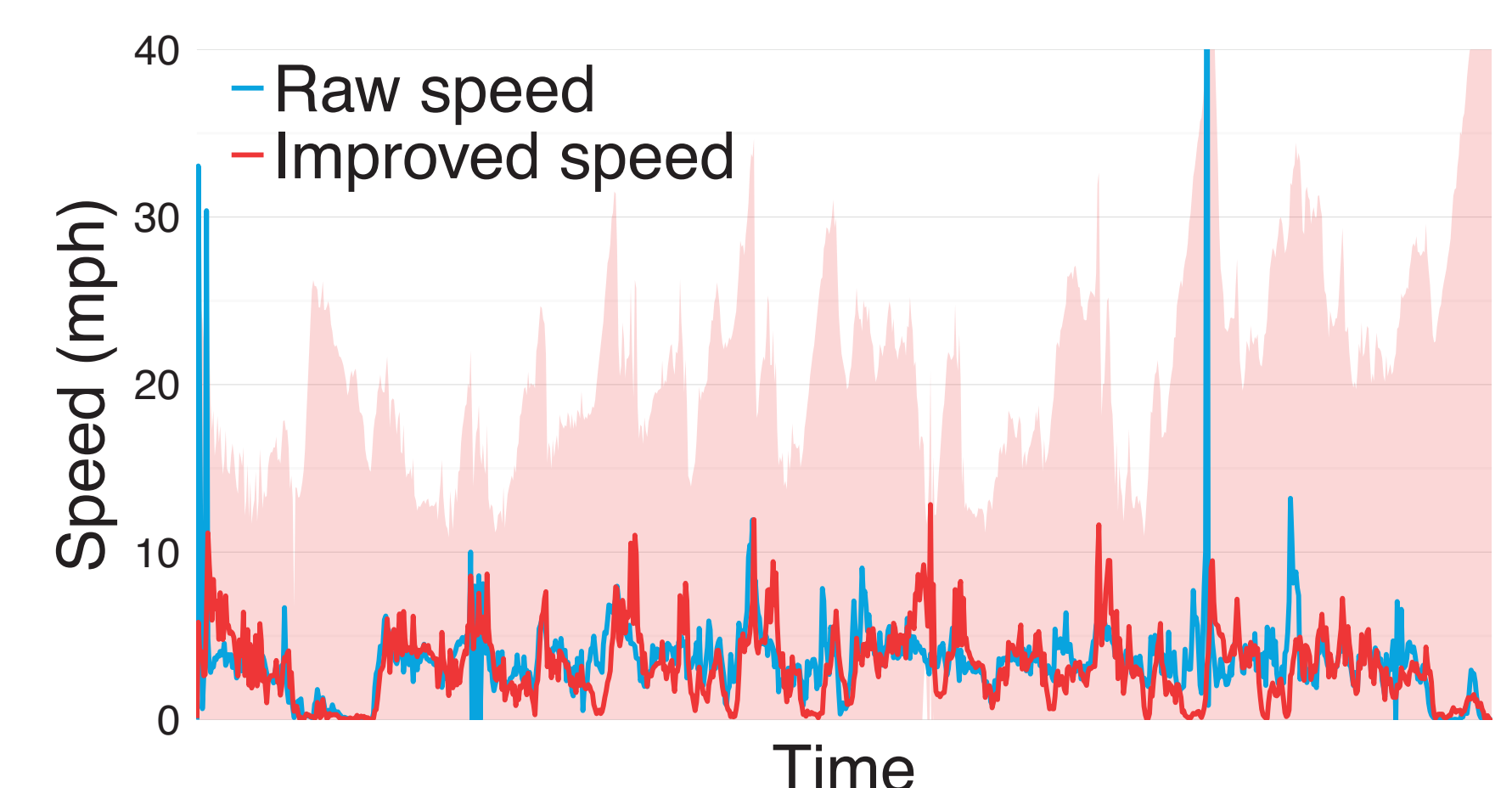
Uncertain<T> uses hypothesis tests to control approximation error.

4 Improving estimates

$$\Pr[H|E] = \frac{\Pr[E|H] \Pr[H]}{\Pr[E]}$$

Distributions allow experts to apply Bayesian methods: combine evidence (observed data, *E*) with a hypothesis (prior knowledge, *H*) to obtain better estimates (a new hypothesis, $H|E$).

For example, we can apply a physics model to the GPS speed data from above. The model removes the absurd values and tightens the confidence interval.



Uncertain<T> makes programs more expressive and more correct