# Security of the Grid Routing Protocol In Sensor Networks 

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The Grid Routing Protocol

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$\mathcal{A}$ sensor network consists of large number of tiny computers; each capable of sensing magnetism, movement, heat, or sound in the ir vicinities. The computers in this network collaborate to achieve a globalsensing objective. The characteristics of each computer usually include constrained battery power, small memory resources, and limited computational power. Moreover, the failure rate of each tiny computer is high. The computers communicate wirelessly througf radio signals, and because eacf computer fias a limited communication radius, the sensor network is in fact a multi-hop system. Sensor networks may be used in various applications including monitoring and surveillance, object tracking and inventory Keeping, military awareness, naturaldisaster detection in remote places, monitoring sensitive areas, and so on. Because of the nature of these applications, it is essential for the message transmission in these ne tworks to be secure from an adversary who might attempt to compromise the networkeffectiveness.

In this thesis, we formally specify a simple routing protocol, called the grid routing protocol, that can be used for routing data messages in a sensor network. We also specify several enfancements of this protocol to make it secure against mote impersonation and infiltration attacks.

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1 The Grid Routing Protocol

The Logical Grid Routing Protocolis a protocolfor routing datamessages in sensor networks. [2], [4] This protocol overcomes random message loss and mote failure.
1.1 The Grid

We consider a network that consists of a number of tiny computers called motes. The characteristics of each mote usually include constrained battery power, small memory resources, and limited computational power. Moreover, the failure rate of each mote is high. These motes communicate wirelessly through radio signals, and because each mote has a limited communication radius, this network is in fact a multi-fop system.

The motes in the network are placed in an arbitrary physicalconfiguration, but they are labeled as if they are points in an $\mathfrak{M}^{*} \mathcal{N}$ logicalgrid. Therefore, each mote fas a label( $\left.i, j\right)$ where $i:=0$.. $\mathcal{M}-1$ and $j:=0 . . \mathcal{N}-1$.

It is required that the physicalconnectivity of the motes is a superset of the grid connectivity implied by the mote labels. As an example,

$(1,1)$


Figure 1 shows a network with six motes; the edges between the motes describe which motes can communicate with which other motes. Thus, figure 1 describes the physicalconnectivity in the network. Figure 2 describes the logicalconnectivity in the same network based on the chosen labels of the motes. Note that the edges in Figure 1 (i.e. the physicalconnectivity of the network) are a superset of the edges in Figure 2 (i.e. the grid connectivity of the same network).

### 1.2 Logical Neighbors

Each mote [ $i, j$ ] in the middle of the grid has four logicalneighbors. These logicalneighbors are mote $[i, j+1], \operatorname{mote}(i, j-1)$, mote $[i+1, j]$ and mote $[i-1, j]$. Two of those four motes are called low neighbors, and the other two are called high neighbors. The two lowneighbors of mote [i,j] are motes $[i, j-1]$ and $[i-1, j]$, and the two high neighbors are motes $[i+1, j]$ and $[i, j+1]$. If mote $[i, j]$ is located on the boundaries of the grid, then it has a smaller number of logicalneighbors. There are four cases to consider. In the first case, where $i=0$, mote [ $0, j$ ] has only one lowneightor, namely mote $[0, j-1]$. In the second case, where $j=0$, mote $[i, 0]$ has only one lowneighbor, namely mote [i-1,0]. (Therefore, mote [0, 0] has no lowneighbors.) In the third case, where $i=\mathcal{M}-1$, mote $[\mathcal{M}-1, j]$ has only one figh neighbor, namely mote $[\mathcal{M}-1, j+1]$. In the fourth case, where $j=\mathfrak{N}-1$, mote [i, $\mathcal{N}-1]$ has only one high neighbor, name $\sqrt{2}$ mote $[i+1, \mathcal{N}-1]$. (Therefore, mote [ $\mathcal{M}-1, \mathcal{N}-1]$ has no high neighbors.)

### 1.3 Communication Pattern

Each mote [i, j] in the network Groadcasts messages whose ultimate destination is mote [0, 0]. To facilitate communication between motes, the motes need to maintain an incoming spanning tree whose root is mote [0.0]. As an example, Figure 3 sfows a spanning tree for the grid networkin Figure 2. Each mote in the network maintains a pointer to its parent in the tree, and these pointers form the spanning tree. When a mote receives a message, it forwards the message to its parent in the tree. This process continues, until the message reaches the tree root, namely mote [0, 0].

Figure 3


The parent of a mote in the spanning tree is chosen from the logicalneighbors of this mote so that the parent of the mote is within the communication range of the mote. When a mote [i, j] broadcasts a message, the message reaches to all motes within the communication range of [i, $j]$. All motes within the communication range, excluding the parent, discard the message, and the parent forwards the message to its parent, and so on, until the message reaches mote [0.0]. Clearly, if all logical neighbors of a mote fail, then this mote cannot fave a parent in the spanning tree and so cannot Groadcast any messages to mote [0.0].

### 1.4 Choosing the Parent

Each mote [i,j] chooses its parent from its logicalneighbors based on the distance of each logical neightor. The logicaldistance of a mote [ $i, j]$ is defined to be $i+j$. It is advantageous for a mote $[i, j]$ to choose its parent with as small a distance as possible. Therefore, when a mote chooses its parent from its logicalneighbors, the mote prefers a lowneighbor. However, if both lowneighbors of a mote fail, then the mote chooses one of its high neighbors to be its parent. This situation is called an inversion. Thus, an inversion is defined to be an occurrence where a mote chooses one of its figh neighbors to be its parent. As an example, one inversion occurs at mote (1,2) in the network in Figure 4, because both lowneighbors of mote (1, 2) have failed.


### 1.5 Inversion Count

The inversion count of a mote [ $i, j$ ] is defined to be the number of inversions that occur along the spanning tree route from mote $[i, j]$ to mote $[0.0]$. As an example, Figure 5 shows the inve rsion counts of each mote in the network in Figure 4: the inversion count of mote [1,2] is 1, whereas the inversion count of every other mote is 0 .


The inversion count of a mote has an upper bound, namely $\mathcal{M}+\mathcal{N}$, and a lower bound, namely 0 . We can Cimit the upper bound of the inversion count artificially to be a smaller number. One advantage of having an artificial upper bound on the inversion count is that a message fas a shorter distance to the root. $\mathcal{A}$ disadvantage of having this artificial upper bound is that a mote could potentially be isolated from the network and therefore unable to forward messages to mote [0.0]. As an example, in Figure 6, if cmax equals 1 , then mote ( 2,0 ) is disconnected from the network and cannot forward any messages.

Figure 6

1.6 Protocol Message

When, and only when, a mote $[i, j]$ has a parent $(x, y)$, every t seconds mote $[i, j]$ broadcasts a connected message to all motes within its communication range. This connected message fas three
fields: $(i, j, c)$, where $(i, j)$ is the label of the mote broadcasting the message and c represents its current inversion count. All motes within the communication range of mote [i, $j$ ], excluding the neightors of mote $[i, j]$, discard the connected $(i, j, c)$ message broadcasted by mote $[i, j]$. Mote [0.0] Groadcasts a connected ( $0,0,0$ ) message every t seconds.

If all logicalneighbors of mote [i,j]fail, then mote [i,j] has no parent, and it will not broadcast any messages. In this case, mote $[i, j]$ becomes isolated from the spanning tree and can no longer forward any message to mote [0.0].
1.7 Acquiring a Parent

Initially, mote $[i, j]$ has no parent. When mote $[i, j]$ has no parent and receives a connected $(x, y, d)$ message from a neighbor $(x, y)$, mote $[i, j]$ chooses this neighbor as its parent in two cases. The first case occurs when mote [ $x, y$ ] is a lowneighbor. The second case occurs when mote [ $x, y$ ] is a figh neighbor and the inversion count $d$ is less than cmax.

When mote $[i, j]$ receives a connected $(x, y, d)$ message where $(x, y)$ is a lowneightor of mote $[i, j]$, mote $[i, j]$ chooses this neighbor to be its parent and computes its inversion count using $c:=d$. If the parent $[x, y]$ is a figh neighbor and $d$ is less thancmax, mote [i,j] computes its inversion count using $c:=d+1$.

Consider the networkin Figure 6. Mote [0.0] Groadcasts the message connected ( $0,0,0$ ) every $t$ seconds. When mote [0, 1] receives this message, it recognizes that [0.0] is its lowneighbor, and so it chooses (0.0) to be its parent in the spanning tree and makes its own inversion count equal 0 . From this point on, mote [0, 1] Groadcasts the message connected ( $0,1,0$ ) every teconds. When mote $[0,2]$ receives the message connected $(0,1,0)$ and recognizes that mote $[0,1]$ is its lowneightor, it
chooses mote $[0,1]$ to be its parent and its inversion count to be 0 , and the cycle repeats. When finally mote [2, 1] receives the message connected (2,2,0) and recognizes that mote [2, 2] is its figh neighbor, it chooses mote [2, 2] to be its parent and its inversion count to be 1. From this point on, mote [2, 1] starts to Groadcast the message connected (2, 1, 1) every tseconds. When mote [2, 0] receives the message connected (2, 1, 1), it will not choose mote [2, 1] to be its parent because that would make its own inversion count 2, violating the upper bound of 1 on the inversion count. Thus, mote [2, 0] remains without a parent, cannot join the spanning tree, and cannot forward any message toward mote [0.0].

### 1.8 Keeping the Parent

Once a mote $[i, j]$ has a parent $(x, y)$ and receives any connected $(x, y, d)$ message, mote [i,j]uses the received e to update its own inversion count $c$ as follows. The inversion count $c$ is calculated as $c:=d$ if the parent $(x, y)$ is a lowneighbor of $[i, j]$, and it is calculated as $c:=d+1$ if the parent $(x, y)$ is a figh neighbor of $[i, j]$ and $d$ is less than cmax. When the parent $(x, y)$ is a figh neighbor and e equals cmax, then mote $[i, j]$ loses its parent.

### 1.9 Losing the Parent

There are two cases where a mote [i,j] loses its parent $(x, y)$. In the first case, mote [i,j] receives a connected $(x, y, \operatorname{cmax})$ message from its parent $(x, y)$ and the parent is a figh neightor of $[i, j]$. In the second case, mote $[i, j]$ does not receive a connected $(x, y, d)$ message from its parent $(x, y)$ for $4^{*} t$ seconds.

Consider the networkin Figure 6. Based on this network, mote [2, 2] has its parent to be mote [1, 2]. In Figure 7, mote [2, 2] loses its parent, after receiving no message connected (1, 2, 0) for $4{ }^{*}$ t
seconds. From this point on, mote [2, 2] is disconnected from the network, so it is unable to Groadcast connected $(2,2,0)$ messages. Since mote $[2,1]$ does not receive any connected $(2,2,0)$ message from its parent for $4^{*}$ t seconds, it also loses its parent and is disconnected from the network as shown in Figure 7.
failed $\quad(2,2)$

1.10 Replacing the Parent

There is one case where mote $[i, j]$ replaces its parent $(x, y)$ with a new parent ( $u, v)$. This case occurs only when mote $[i, j]$ has a parent $(x, y)$ and receives a connected $(u, v, f)$ message, where $(u, v)$ is the label of a neighbor and $f$ is the inversion count of this neighbor. Mote $[i, j]$ chooses $(u, v)$ as its parent, if using $f$ to compute the inversion count $c$ of mote $[i, j]$ reduces the value of $c$. In this case, mote $[i, j]$ chooses its parent to be $(u, v)$ and computes its inversion count using $f$. Mote $[i, j]$ always chooses the parent with the smallest inversion count in order to minimize the length of the route from mote $[i, j]$ to mote [0.0] in the incoming spanning tree.

Consider the network in Figure 6 and assume that mote [1, 1] wakes up. When mote [1, 1] wakes up, receives a message connected ( $0,1,0$ ), and recognizes that mote [0, 1] is its lowneightor, mote [1, 1] chooses $(0,1)$ to be its parent and makes its inversion count 0. From this point on, mote [1, 1]

Groadcasts a connected (1, 1, 0) message every teconds. When mote [2, 1] receives the connected
(1, 1, 0) message and recognizes that mote [1, 1] is its lowneighbor, mote [2, 1] replaces its parent (2, 2) with mote [1, 1] and reduces its inversion count from 1 to 0. From this point on, mote [2, 1] broadcasts a connected (2, 1, 0) message every t seconds. Whenmote [2, 0] receives a message connected (2, 1, 0) and recognizes that mote [2, 1] is its highneighbor, mote [2, 0] chooses mote [2, 1] to be its parent and sets its inversion count to 1. The resulting spanning tree is shown in Figure
8.


2 Formal Definition of the Grid Routing Protocol

It is beneficial to specify the above grid routing protocolusing an abstract notation, called the $\mathcal{S} P$ (Sensor Protocol) notation [3] to explain the protocol precisely. The Englisflanguage, or any natural language for that matter, is too imprecise to describe such a protocol. Precision provides a clearer understanding of the protocol. Uling the $\mathcal{S}$ P notation, we modeleach mote in the network as a process. Each process has constants, inputs, variables, and actions.

### 2.1 Constants, Inputs and Variables

Each process mote [i, j] has one constant, cmax, that represents the maximum possible value for the inversion count of mote $[i, j]$. The constant cmax is declared as follows:
const cmax : integer

Each process mote [i,j] has two set inputs. The first is called 'L', and it contains the indices of the

Lowneighbors of mote [i,j]. The second set is called 'H', and it contains the high neighbors of mote $[i, j]$. These two sets are declared as follows:
$\operatorname{inp} \quad \mathcal{L}: \quad \operatorname{set}\{(i, \max (j-1,0)),(\max (i-1,0), j)$, $\mathcal{H}: \quad \operatorname{set}\{(i, \min (j+1, n-1)),(\min (i+1, m-1), j)\}$

Each process mote [ $i, j]$ has five variables. The first variable, named pid, stores the identity of the parent of mote $[i, j]$. Recall that the value of pid is to be taken from the set $L \mathcal{U} \mathcal{H}$. The second variable, named trc, is discussed in the next paragraph. The third variable, named $c$, stores the inversion count of mote $[i, j]$. The fourth variable, named $d$, stores the inversion count of the parent of mote [ $i, j$ ]. The fifth variable, named tout, is a timeout variable. The timeout variable and the concept of time out is explained below in sections 3.2 and 3.3.

The second variable tre represents the remaining time period that mote [i,j] fas a parent and is connected to the spanning tree. Each time mote [i,j] receives a connected message from its parent, tre is set to 4. Each tseconds trc is decremented by 1. Thus, if mote [i,j]does not receive a connected message from its parent for a period of $4 t$ seconds, trc becomes zero, and mote [ $i, j$ ] is no longer connected to the spanning tree. In section 2.9, Losing a Parent, recall that one way mote loses its parent is to receive no connected message from its parent for $4 t$ seconds.

The five variables of each process mote $[i, j]$ are declared as follows:

| var | pid | $:$ | $\perp \mathcal{U H} \mathcal{H}$ |
| :--- | :--- | :--- | :--- |
| trc | $:$ | $0 . .4$ |  |
| c, $d$ | $:$ | o..cmax |  |
| tout | $:$ | boolean |  |

In the initial state of the network, mote [0.0] has the following values for its variables:

$$
\text { pid }=(0,0)
$$

$$
\operatorname{trc}=4
$$

$$
\begin{aligned}
& c=0 \\
& \text { tout }=\text { true }
\end{aligned}
$$

Every other mote $[i, j]$ has the following values for its variables:
$\operatorname{trc}=0$
$c=0$
tout $=$ false

### 2.2 Timeout Variables

In the initial state of the protocol, variable trc has the value 4 in mote $[0,0]$ and has the value 0 in every other mote. If a mote $[i, j]$ receives a connected message from a neighbor and chooses that neighbor to be its parent, the value of tric in mote $[i, j\}$ becomes 4 , and variable tout is set to true. While tout in mote $[i, j]$ is true, mote $[i, j]$ times out and broadcasts a connected message every $t$ seconds, the timeout actiondecrements the value of trc by 1 and activates another timeout after seconds, until the value of tric becomes 0 . Once the tric variable becomes zero, the mote loses its parent, is no longer connected to the spanning tree, and finally tout becomes false and no timeout is activated. Recall that a mote loses its parent if the mote receives no connected message for $4 t$ seconds.
$\mathcal{A} s$ an example, consider a network where a mote $[i, j]$ receives a connected message $(x, y, d)$ and chooses mote $[x, y]$ to be its parent. The pid of mote $[i, j]$ becomes $(x, y)$, the trc variable becomes 4, and tout becomes true. Mote [i,j] waits to receive another connected message. After tseconds, the timeout action is executed, and trc is decremented by 1. If mote $[i, j]$ waits $t$ more seconds and receives no connected message, once again the timeout action is executed, and trc is decremented by 1. Finally, when trc becomes zero, mote [i,j] loses its parent and is disconnected from the spanning tree. The tout variable is declared as follows:
tout : boolean

In the initial state of the network, for mote $[0,0]$, tout $=$ true. Otherwise, tout $=$ false.

### 2.3 Timeout Actions

The timeout action in mote [i,j] can be vie wed as consisting of two parts. In the first part, mote [i,j] checks whether it is mote [0,0]. If not, mote $[i, j]$ sets its trc variable to the maximum of tri-1 and 0. If so, mote [0, 0] does nothing. This first action of the timeout is defined as follows:

```
time out \(\rightarrow\) if \(i \neq 0^{\wedge} j \neq 0 \rightarrow \operatorname{trc}=\max (\operatorname{trc}-1,0)\)
        /] \(i=0^{\wedge} j=0 \rightarrow\) skip
        fi;
```

In the second part of the timeout, each mote [i, $j]$ Groadcasts a connected $(i, j, c)$ message and activates the timeout to expire next after tseconds. If tre equals 0 , the value of tout becomes false. The second part of the timeout action is defined as follows:

$$
\begin{aligned}
& \text { if } \operatorname{trc}>0 \rightarrow \text { broadcast conn }(i, j, c) ; \\
& \text { activate time out in } t \text { seconds } \\
& {[/ \operatorname{trc}=0 \rightarrow} \text { tout }:=\text { false } \\
& f_{i}
\end{aligned}
$$

The entire timeout action is as follows:


```
    /] i=0 ^ j = 0 -> skip
    fi;
    if trc>0 Groadcastconn(i,j,c);
        activate timeout in t seconds
    [] trc = 0 T tout := false
    fi
```

2.4 Receive Action

The receive action of each mote [i,j] has one if ...fistatement that consists of branches. This action is specified as follows:
[]$r \operatorname{coconn}(x, y, d) \rightarrow$

$$
\begin{array}{ll}
\text { if } \sim((x, y) \text { in } \mathcal{L} \mathcal{H} \mathcal{H}) \rightarrow \text { skip } & \text { \{discard conn\} } \\
{\left[/(x, y) \text { in } \mathcal{L}^{\wedge}(\operatorname{trc}=0) \rightarrow\right.} & \text { <statement } S_{0}>
\end{array}
$$

| []$(x, y) \operatorname{in} L^{\wedge}(\operatorname{trc}>0) \rightarrow$ | <statement $S_{1}>$ |
| :---: | :---: |
| []$(x, y)$ in $\mathcal{H}^{\wedge}(\operatorname{trc}=0) \rightarrow$ | <statement $S_{2}>$ |
| []$(x, y)$ in $\mathcal{H}^{\wedge}(\operatorname{trc}>0) \rightarrow$ | <statement $S_{3}>$ |
| $f i$ |  |

$\mathcal{N}$ Note that statement $S_{0}$ is executed if the received conn $(x, y, d)$ was broadcast by a lowneighbor of mote $[i, j]$, and mote $[i, j]$ currently has no parent. Statement $S_{1}$ is executed if the received conn ( $\left.x, y, d\right)$ was broadcast by a lowneighbor of mote [i,j], and mote [i,j]currently fas a parent. S tatement $\mathcal{S}_{2}$ is executed if the received conn $(x, y, d)$ is broadcast by a high neighbor of mote $[i, j]$, and mote $[i, j]$ currently fas no parent. Statement $S_{3}$ is executed if the received conn $(x, y, d)$ was broadcast $6 y$ a figh neighbor of mote $[i, j]$, and mote $[i, j]$ currently fas a parent.

The four statements $S_{0}$ through $S_{3}$ can be specified as follows:

```
    S tatement S S Pid, trc,c := (x,y), 4,d;
                            if ~tout }->\mathrm{ activate timeout in t seconds; tout := true
                            | tout }->\mathrm{ skip
                            fi
```



```
            [] pid }\ddagger=(x,y)^(d<c)-> pid, trc,c:= (x,y), 4,
    [] pid }\ddagger(x,y)^(d\geqc)->\mathrm{ skip {discard message}
        fi
    Statement }\mp@subsup{S}{2}{}->\mathrm{ if }d<cmax -> pid, trc, c:= (x,y), 4,d+1
                                    if ~tout }->\mathrm{ activate timeout in t seconds; tout:= true
                                    [] tout }->\mathrm{ skip
                            fi
    || = cmax }->\mathrm{ skip {discard message}
    fi
    S tatement S S }->\mathrm{ if pid = (x,y)^ (d<cmax ) }->\mathrm{ trc, c:= 4,d+1
    |/ pid = (x,y)^ (d=cmax ) 
    |] pid }\ddagger=(x,y)^(d+1<c)-> pid, trc,c:=(x,y),4,d+
    | pid }\ddagger=(x,y\mp@subsup{)}{}{\wedge}(d+1\geqc)->\mathrm{ skip {discardconn}
    fi
```

2.5 Formal Specification

The Grid Routing Protocolcan be specified formally as follows:

| const | cmax | : | integer |
| :---: | :---: | :---: | :---: |
| inp | $\mathcal{L}$ | : | set $\{(i, \max (j-1,0)),(\max (i-1,0), j)$, |
|  | $\mathcal{H}$ | : | $\operatorname{set}\{(i, \min (j+1, n-1)),(\min (i+1, m-1), j)\}$ |
|  | $x, y$ | : | integer |
| var | pid | : | $\mathcal{L} \mathcal{U H}$ |
|  | trc | : | 0 .. 4 |
|  | c, $d$ | : | 0 .. cmax |
|  | tout | : | boole an |

begin
time out $\rightarrow$ if $i \neq 0^{\wedge} j \neq 0 \rightarrow \operatorname{trc}=\max (\operatorname{trc}-1,0)$
[] $i=0^{\wedge} j=0 \rightarrow$ skip
$f$;
if $\operatorname{trc}>0 \rightarrow$ broadcastconn $(i, j, c)$;
activate timeout in $t$ seconds
[] trc $=0 \rightarrow$ tout $:=$ false
fi
[] $\operatorname{rcv} \operatorname{conn}(x, y, d) \rightarrow$
if $\sim((x, y)$ in $\mathcal{L} \mathcal{H}) \rightarrow$ skip $\quad\{$ discard conn\}
[]$(x, y) \operatorname{in} \mathcal{L}^{\wedge}(\operatorname{trc}=0) \rightarrow$ pid, $\operatorname{trc}, c:=(x, y), 4, d$;
if $\sim$ tout $\rightarrow$ activate timeout in $t$ seconds; tout $:=$ true
[] tout $\rightarrow$ skip
fi
[]$(x, y)$ in $L^{\wedge}(\operatorname{trc}>0) \rightarrow$ if pid $=(x, y) \rightarrow \operatorname{trc}, c:=4, d$
[] pid $\ddagger(x, y)^{\wedge}(d<c) \rightarrow$ pid, $\operatorname{trc}, c:=(x, y), 4, d$
[/ pid $\ddagger(x, y)^{\wedge}(d \geq c) \rightarrow$ skip $\quad$ \{discardmessage\} ${ }_{p 16}$
fi
[] $(x, y)$ in $\mathcal{H}^{\wedge}(\operatorname{trc}=0) \rightarrow$ if $d<c m a x \rightarrow p i d, \operatorname{trc}, c:=(x, y), 4, d+1$;
if $\sim$ tout $\rightarrow$ activate timeout in $t$ seconds; tout $:=$ true
[] tout $\rightarrow$ skip
fi
[]$d=$ cmax $\rightarrow$ skip $\quad\{d i s c a r d m e s s a g e\}$
fi
[]$(x, y)$ in $\mathcal{H}^{\wedge}(\operatorname{trc}>0) \rightarrow$ if pid $=(x, y)^{\wedge}(d<c \max ) \rightarrow \operatorname{trc}, c:=4, d+1$
/] pid $=(x, y)^{\wedge}(d=c \max ) \rightarrow \operatorname{trc}:=0$
I] pid $\ddagger(x, y)^{\wedge}(d+1<c) \rightarrow$ pid, $\operatorname{trc}, c:=(x, y), 4, d+1$
[/ pid $\ddagger(x, y)^{\wedge}(d+1 \geq c) \rightarrow$ skip
end
initial state: if $i=0^{\wedge} j=0$ then pid $=(0,0), \operatorname{trc}=4, c=0$, tout $=$ true and timeout is activated else trc $=0$, tout $=$ false, and the timeout is not activated

3 Ulsing the Grid Routing Protocol

The function of the Grid Routing Protocol, discussed in the last section, is for each mote [i,j] to maintain two variables tre and pid. When trc $>0$ then mote $[i, j]$ is connected to the spanning tree via its parent mote [pid]. In this case, mote [i,j]canforward any datamessage to its parent until the data message reaches the network root, namely mote [0,0]. Whentrc $=0$, then mote $[i, j]$ can forward any data message to its parent which in turn forwards it to its parent until the data message reaches the network root, mote $[0,0]$. When $\operatorname{trc}=0$, then mote $[i, j]$ is not connected to the spanning tree and can no longer forward data messages toward the network root.

The data transfer protocol, that uses the grid routing protocol, can be specified as follows:

```
process mote [i:0 .. m-1, j:0 .. n-1]
inp L : set {(i,max (j-1,0)), (max (i-1,0),j),
    H}:\quad\operatorname{set}{(i,\operatorname{min}(j+1,n-1))(\operatorname{min}(i+1,m-1),j)
    pid : &\mathcal{H}}{fromgrid routing protocol}
    trc : 0..4 {from grid routing protocol}
var t : integer
    x,y : integer
begin
```



```
    rcv data (x,y,t) -> if (x\not=i)v(y\not=j)v(trc=0)^(x\not=0vy\not=0) -> skip {discard data}
    [] (x=i)^ ( }y=j\mp@subsup{)}{}{\wedge}(trc>0)^(x\not=0vy\not=0)->\mathrm{ broadcast data (pid, t)
    [] (x=i)^ ( y = j)^ (trc>0)^^ x=0^^y=0 \ skip {store data}
    fi
```

end
$4 \mathcal{A d v e r s a r i a l} \mathcal{A c t i o n s}$

In order to secure the grid routing protocol, it is necessary to consider what types of scenarios the adversary could use to disrupt the protocol. One of these scenarios is mote impersonation. Mote impersonation occurs when an adversary removes one of the legitimate motes out of the network and replaces it with an illegitimate adversarial mote. Another scenario is networkinfiltration. This scenario occurs when an adversary adds an adversarial mote to the network. We describe these scenarios in more detailnext.
4.1. Impersonating motes in a network without shared secrets

One action that an adversary may take to disrupt the Grid Routing Protocol is to remove alegitimate mote from the network and replace it with an illegitimate foreign mote. This action is called impersonating a mote. As an example, consider a network where an adversary removes mote [0, 1] from the network. $\mathcal{A}$ foreign mote takes the place of mote [0, 1]. The foreign mote then broadcasts connected ( $0,1,0$ ) messages every $t$ seconds. In this network, assume motes [0, 2] and [1, 1] choose the foreign mote to be their parent, when they receive a connected ( $0,1,0$ ) message from the adversary that is impersonating mote [0, 1] and recognize that mote [0, 1] is their lowneighbor. Mote [0, 2] then broadcasts a connected $(0,2,0)$ message every t seconds, and mote $[1,1]$ Groadcasts a connected (1, 1, 0) message every $t$ seconds. Mote $[0,3]$ chooses mote $[0,2]$ to be its parent; motes [1, 2] and [2, 1] choose mote [1, 1] to be their parent and so on.

Each parent is the root of a subtree. In this example, the root of a subtree is mote [0, 1], and the subtree includes all of the motes that have chosen mote [0, 1] to be their parent, namely motes [0, 2] and [1, 1], all of the motes that have chosen mote [0, 2] or [1, 1] to be the ir parent, and all of the motes that have chosen motes $[0,3],[1,2]$, or $[2,1]$ to be their parent and so on.
$\mathcal{A l l}$ the motes in this subtree forward the ir messages to the ir parent, until they get to the foreign mote. One action that the adversary may take to disrupt the network is to have the foreign mote discard all of the messages it receives. This action is extremely disruptive, since all of the messages in this subtree instead of being forwarded to the root are discarded. Cle arly the result of this action is message loss. Another action the adversary can take is to receive a connected message, alter it, and then broadcast the altered message. This action results in message corruption.
4.2 Impersonating Motes in a Network with Shared Secrets To counter the adversarial attack called mote impersonation, it is necessary to enfance the grid routing protocol by adding shared secrets. Each mote shares a separate secret witheach of its neighbors. Thus, a mote has the same number of shared secrets as it has neighbors. Each mote computes a value using each of its shared secrets, one value per secret. These values are appended to the connected message before broadcasting it. When a mote receives a connected message from one of its logical neighbors, the mote uses the shared secret to authenticate the connected message.

In this more secure network, the adversary may once again remove a mote from the network and replace it with a foreign mote. The legitimate mote broadcasts a connected message every teconds, but in this network the shared secret provides an authentication value verifiable by the receiver. For example, in this more secure network, mote $[0,1]$ broadcasts a connected ( $0,1,0$ ) message and appends a message digest value computed using the shared secret. A neightor of the mote, mote [0, 2], receives the message, recognizes that the message contains the computed value using its shared secret, verifies this value, and accepts the message. Mote [0, 2] recognizes that mote [0, 1] is a lowneightibor and chooses mote [0, 1] to be its parent in the spanning tree. This process continues throughout the network; mote
chooses mote [0, 2] to be its parent and so on. In this network, Gefore the foreign mote removes mote [0, 1] from the network, the foreign mote accepts one of the connected ( $0,1,0$ ) messages from mote [0, 1] with the appended value computed using the shared secret. The foreign mote then removes mote $[0,1]$ from the network and replays this connected $(0,1,0)$ message with the computed values appended for each neighbor using their respective secret keys. Thus, when mote [0, 2] receives this message, it chooses the foreign mote to be its parent, since the value mote [0, 2] computed using the shared secret is the same as the received value. Iust as in the example of mote impersonation in a network without shared secrets, mote [1, 1] chooses this foreign mote to be its parent when mote [1, 1] receives the connected $(0,1,0)$ message, verifies the appended message digest value, and recognizes that mote $[0,1]$ is its low neighbor, and the process continues. This second scenario also disrupts the grid routing protocol, since the integrity of the subtree whose root is the foreign mote is compromised by message replay.
4.3 Infiltrating the $\mathfrak{N e t w o r k}$

In this attack, the adversary adds an illegitimate mote to the network which broadcasts wrong data messages containing the identity of a legitimate mote. The legitimate motes continue to broadcast their data messages, but the infiltrator also broadcasts data messages with inaccurate data.

For example, assume that mote [2, 1] is alive and is broadcasting a data (1, 1, t) message. Then an illegitimate mote infiltrates the network and pretends to be this mote. The adversary mote broadcasts a data (1, $1, t_{a}$ ) message, where $t_{a}$ is the data fabricated by the adversary. Mote [1, 1] receives the data message and forwards it to its parent, mote [1, 0], who forwards it to mote [0, 0]. Clearly the integrity of the data transfer protocol is compromised.

## 5 Countering Mote Impersonation

In order to provide integrity to the Logical Grid Routing Protocol, it is necessary to add shared secrets. Each mote [ $i, j]$ has one shared secret for each of its neighbors.
5.1 Enkancing the Network

In this more secure protocl, mote $[i, j]$ and its high neighbor mote $[i, j+1]$ share one secret. This shared secret is called $\mathcal{N}$ in mote $[i, j]$. Mote [ $i, j]$ and its other high neighbor, mote $[i+1, j]$, share another secret. This secret is called $\mathcal{E}$ in mote $[i, j]$. In the same manner, mote $[i, j]$ shares a different secret with mote [i, $j-1$ ]; this secret is called $S$ in mote $[i, j]$ Mote $[i, j]$ shares yet another secret with its other low neighbor, mote [i-1, j]. This last secret is called $\mathcal{W}$ in mote [ $i, j$ ]. Therefore, mote [ $i, j$ ] has one shared secret for each of its neighbors. Each time that mote $[i, j]$ Groadcasts a connected message, this mote computes a message digest function (MD) over the message text and each shared secret that mote [i, $j$ ] shares with a neighbor.
$\mathcal{A}$ message digest $\mathcal{M D}$ is a function that computes a unique integer value for any data itemd lof type integer), a data item $\mathcal{M D}(d)$ in the range of $0 . . \mathcal{K}-1$ such that the following condition is satisfied:

Finger Printing: There is no efficient algorithm that computes, for any $\mathfrak{M D}(d)$, a
data item d'such that $\mathfrak{M D}(d)=\operatorname{MD}\left(d^{\prime}\right)$. Thus, $\mathcal{M D}(d)$ is a finger print of data item $d$. [1] $\mathcal{B e f o r e}$ Groadcasting a message, each mote $[i, j]$ computes a message digest of $i, j, c$, and the shared secret for each neighbor. The value $\mathcal{M D}(i|j| c \mid s c)$ represents the message digest of the concatenation of $i, j, c$, and the shared secret. Each time that a mote broadcasts a message, the mote computes the message digest for each neighbor, using the shared secret of that neighbor. For example, if a mote $[i, j]$ has four neighbors, assume $S$ represents the secret mote $[i, j]$ shares with mote $[i, j-1]$, $\mathcal{W}$ represents the secret mote $[i, j]$ shares with mote $[i-1, j], \mathcal{N}$ represents the secret mote $[i, j]$ shares with mote
$[i, j+1]$, and Erepresents the secret mote $[i, j]$ shares with mote $[i+1, j]$. The message mote $[i, j]$ Groadcasts would looklike the following. Let $s d=\mathcal{M D}(i|j| c \mid S)$ (where a verticalline represents concatenation), $w d=\mathcal{M D}(i|j| c \mid \mathcal{W}), n d=\mathcal{M D}(i|j| c \mid \mathcal{N})$, and ed $=\mathcal{M D}(i|j| c \mid \mathcal{E})$. The message that mote $[i, j]$ Groadcasts will be connected ( $i, j, c, s d, w d, n d, e d)$. If mote $[i, j$ - 1] receives the connected message, it will compute a message digest function for $x, y, d$, and the shared key, where the shared key for mote $[i, j-1]$ is $\mathfrak{N} . S o$, mote $[i, j-1]$ will have a value $n d^{\prime}=\mathcal{M D}(\chi|y| d \mid \mathcal{N})$. If $n d^{\prime}=s d$, mote $[i, j-1]$ will acce $p t$ the connected message; if nd'łsd, mote $[i, j-1]$ will discard the connected message. If mote [i-1, $j]$ receives the connected $(x, y, d, s d, w d, n d, e d)$ message from mote $[i, j]$, mote $[i-1, j]$ uses its shared secret $\mathcal{E}$ to compute amessage digest function of $x, y, d$, and the shared secret. Mote $[i, 1, j]$ will have a value ed' $=\mathfrak{M D}(\chi|y| d \mid \mathcal{E})$. If $\boldsymbol{d}^{\prime}=w d$, then mote $[i-1, j]$ receives the connected message, and if ed'? wd, then mote [i-1, j] discards the connected message. If mote $[i, j+1]$ receives the connected $(x, y, d, s d$, $w d, n d, e d)$ message, mote $[i, j+1]$ uses its shared secret $S$ to compute a message digest function of $x, y$, d, and the shared secret. Mote $[i, j+1]$ computes the value $s d^{\prime}=\mathcal{M D}(x|y| d \mid S)$. If $s d^{\prime}=n d$, then mote $[i, j+1]$ receives the message; otherwise mote $[i, j+1]$ discards the message. Finally, if mote $[i+1, j]$ receives the connected $(i, j, c, s d, w d, n d, e d)$ message from mote $[i, j]$, it computes a value wd'using the message digest function with $x, y, d$, and $\mathcal{W}$ concatenated. Thus, $w d^{\prime}=\mathcal{M D}(x|y| d \mid \mathcal{W})$, and mote $[i+1, j]$ receives the message if $w d^{\prime}=e d$ and discards it otherwise.

This protocol provides a solution to the firstattack, impersonating a mote in a network without shared secrets. However, this protocol provides no solution to the attack where the foreign mote replays one of the messages from the mote that it replaces in the network. Upon receiving a message where the message digest value equals its own computed value, i.e. $s d^{\prime}=n d, w d^{\prime}=e d, n d^{\prime}=s d$, or $e d^{\prime}=w d$, each mote will assume that this connected message is from a legitimate mote. Thus, a foreign
mote may disrupt the protocol by replaying one of these connected messages, causing other motes to choose the adversarial mote as the ir parent and form a subtree, giving the adversary an opportunity to discard or alter messages.
5.2 Formal Definition of the Enkanced Protocol

In order to prevent the adversary from impersonating a mote in the network, the grid routing protocol needs added security. The description of the constants, inputs, variables, and statements added to the grid routing protocol to provide security follows.

When the grid routing protocol is enfanced to include shared secrets, the inputs added represent the secrets mote $[i, j]$ shares witheach of its neighbors: $\mathcal{S}, \mathcal{W}, \mathcal{N}$ and $\mathcal{E}$. These inputs are declared as follows:

$$
\begin{array}{ll}
\mathcal{S}, \mathcal{W}, \mathcal{N}, \mathcal{E}: \quad \text { integer } & \{\mathcal{S} \cdot(i, j)=\mathcal{N} \cdot(i, j-1), \\
& \mathcal{N} \cdot(i, j)=\mathcal{S} \cdot(i, j+1), \\
& \mathcal{W} \cdot(i, j)=\mathcal{E} \cdot(i-1, j) \\
& \mathcal{E} \cdot(i, j)=\mathcal{W} \cdot(i+1, j)\}
\end{array}
$$

Recall that the secret mote $[i, j]$ shares with mote $[i, j-1]$ is the $S$ secret for mote $[i, j]$ and the $\mathcal{N}$ secret for mote $[i, j-1]$. Similarly, the secret mote $[i, j]$ shares with mote $[i-1, j]$ is $\mathcal{W}$ for mote $[i, j]$ and $\mathcal{E}$ for mote $[i-1, j]$. The secret mote [i, $j]$ shares with mote $[i, j+1]$ is $\mathcal{N}$ for mote $[i, j]$, 6 ut the same secret for mote $[i, j]$ is $S$. Finally, the secret that mote $[i, j]$ shares with mote $[i+1, j]$ is $\mathcal{E}$ for mote $[i, j]$ and $\mathcal{W}$ for mote $[i+1, j]$.

The additional variables representing the message digest values are these:

$$
\begin{array}{lll}
s d, w d, n d, e d & : & \text { integer } \\
s d ; w d ; n d ; e d, & : & \text { integer }
\end{array}
$$

The timeout inputs have the secrets $\mathcal{S}, \mathcal{W}, \mathcal{N}$ and $\mathcal{E}$, as well as the variables representing the message digest values $s d, e d, n d$, and wd. The guard for the timeout actions is still the same, and the first
statements are also unchanged.

$$
\begin{aligned}
& \text { if } i \neq 0 v j \neq 0 \rightarrow \operatorname{trc}=\max (\operatorname{trc}-1,0) ; \\
& \text { I/ } i=0^{\wedge} j=0 \rightarrow \text { skip } \quad \text { \{store data\} }
\end{aligned}
$$

$\mathcal{N e} x$, mote $[i, j]$ compares the value of its trc variable to 0 . If the value is more than 0 , then mote $[i, j]$ calculates its message digest values, Groadcasts a message including these values, and activiates its timeout to expire next after tseconds. The statement added is the one where mote [i,j] computes the message digest values.

```
if trc>0 > sd,wd,nd, ed:= \mathcal{MDD}(i|j|c|S),\mathcal{MDD}(i|j|c|\mathcal{W}),\mathcal{MD}(i|j|c|\mathcal{N}),\mathcal{MD}(i|j|c|\mathcal{E});
    Groadcast conn (i,j,c,sd,wd,nd,ed);
    activate timeout in t seconds
```

The timeout is unchanged, except for the additional computation of the message digest values.

$$
[] \operatorname{trc}=0 \rightarrow \text { tout }:=\text { false }
$$

The complete timeout action of the secure grid routing protocol is:

```
timeout \(\rightarrow\) if \(i \neq 0 v j \neq 0 \rightarrow \operatorname{trc}=\max (\operatorname{trc}-1,0)\);
    [/ \(i=0^{\wedge} j=0 \rightarrow\) skip
    fi;
    if \(\operatorname{trc}>0 \rightarrow\)
            \(s d, w d, n d, e d:=\mathcal{M D}(i|j| c \mid S), \mathcal{M D}(i|j| c \mid \mathcal{W}), \mathcal{M D}(i|j| c \mid \mathcal{N}), \mathcal{M D}(i|j| c \mid \mathcal{E}) ;\)
            Groadcast conn ( \(i, j, c, s d, w d, n d, e d)\);
            activate timeout in \(t\) seconds
        [] trc \(=0 \rightarrow\) tout \(:=\) fatse
        fi
```

There are several localguards added to the originalgrid routing protocol, in order to provide security using shared secrets. The reason for adding these guards is each time that a connected message is received from aneighbor, mote [i,j] has an extra step to identify by which neighbor the message was Groadcast, so that mote [i,j] candetermine whether to use $\mathcal{S}, \mathcal{W}, \mathcal{N}$ or $\mathcal{E}$ in its message digest function.

Instead of receiving a connected $(x, y, d)$ message, now mote $[i, j]$ receives a connected $(x, y, d, s d, w d$, nd, ed) message from its neighbor. Thus, mote $[i, j]$ determines which neighbor the message is from and then computes its own message digest value to compare with the $\mathcal{M D}$ value received. For example, if the message is from mote $[i, j-1]$, then mote $[i, j]$ uses the shared secret $S$ to calculate a value called $s d$; where $s d^{\prime}=\operatorname{MD}(\chi|y| d \mid S)$. The $\mathcal{L}$ and $\mathcal{H}$ for high neighbors and lowneighbors are no longer specific enough to use, since each high neighbor has a different secret, and each lowneighbor has a different secret. The added localguards are as follows:

$$
\begin{aligned}
& {[]((x, y)=(i, j-1))^{\wedge}(\operatorname{trc}=0) \rightarrow} \\
& {[]((x, y)=(i-1, j))^{\wedge}(\operatorname{trc}=0) \rightarrow} \\
& {[]((x, y)=(i, j-1))^{\wedge}(\operatorname{trc}>0) \rightarrow} \\
& {[]((x, y)=(i-1, j))^{\wedge}(\operatorname{trc}>0) \rightarrow} \\
& {[]((x, y)=(i, j+1))^{\wedge}(\operatorname{trc}=0) \rightarrow} \\
& {[]((x, y)=(i+1, j))^{\wedge}(\operatorname{trc}=0) \rightarrow} \\
& {[]((x, y)=(i, j+1))^{\wedge}(\operatorname{trc}>0) \rightarrow} \\
& {[]((x, y)=(i+1, j))^{\wedge}(\operatorname{trc}>0) \rightarrow}
\end{aligned}
$$

Each process mote $[i, j]$ has the additional statements needed to compute its message digest value using the secret that mote $[i, j]$ shares with the neighbor Groadcasting the message and to compare that value to the one received from the neighbor. This is the additional statement, when mote [i,j] receives a message from its lowneighbor, mote $[i, j-1]$.

$$
\begin{aligned}
& s d^{\prime}:=\mathcal{M D}(i|j| c \mid S) ; \\
& \text { if } s d^{\prime}=n d \rightarrow S_{0}
\end{aligned}
$$

There is a similar statement for each message received by mote $[i, j]$ from motes $[i+1, j],[i, j-1]$, and $[i-1, j]$. Thus, the enfanced protocolincludes the constants, inputs, variables, and actions of the
original grid routing protocolalong with other enfancements to ensure security with respect to mote impersonation.

```
5.2.e Formal Definition of Enkanced Protocol
process mote [i:0..m-1,j:0 .. n-1]
const cmax : integer
inp LL Set {(i,max (j-1,0)),(max (i-1,0)}
    H}:\quad\operatorname{set}{(i,\operatorname{min}(j+1,n-1)),(\operatorname{min}(i+1,m-1),j)
    S,\mathcal{W},\mathcal{N}\mathcal{E}:\quad\mathrm{ integer {S.(i,j)={N.(i,j-1),},\mp@code{N}={
        WW.(i,j) =\mathcal{E}.(i-1,j),
        N
        EE.(i,j)=\mathcal{N}.(i,j)}
var pid : & Ul\mathcal{H}
    trc : O .. 4
    c,d : O ..cmax
    tout : boolean
    sd,wd,nd,ed: integer
    sd',wd',nd', ed': integer
begin
    timeout }->\mathrm{ if i }\ddagger0vj\not=0->\operatorname{trc}=\operatorname{max}(\operatorname{trc}-1,0)
    []i=0 ^}j=0->ski
    fi
    if trc>0 
        sd,wd,nd, ed:= \mathscr{MDP}(i|j|c|S ), \mathscr{MDP}(i|j|c|\mathcal{W}),\mathcal{MD}(i|j|c|\mathcal{N}),\quad\mathcal{MD}(i|j|c|\mathcal{E});
        broadcastconn (i,j,c,sd,wd,nd,ed);
        activate timeout in t seconds
    [] trc = 0 tout := false
    fi
    [] rcv conn (x,y,d,sd,wd,nd,ed)->
    if ~((x,y) in &\mathcal{UH})->\mathrm{ skip {discard conn}}
    |] ((x,y) = (i,j-1))^(trc =0) -> sd':= \mathcal{MDD}(x|y|d|S);
            if sd'=nd }->\mathrm{ 'pid, trc,c:= (x,y),4,d;
                if ~tout }->\mathrm{ activate timeout in t seconds; tout := true
                |] tout }->\mathrm{ skip
                fi
            [] sd
            fi
```

```
[] ((x,y)=(i-1,j))^(trc=0) -> wd':= \mathcal{MD}(x|y|d|\mathcal{W});
    if wd'= ed }->\mathrm{ pid, trc, c:= (x,y), 4,d;
                                    if ~tout }->\mathrm{ activate timeout in t seconds; tout := true
                    |] tout }->\mathrm{ skip
                            fi
    |] wd'\ddagger ed -> skip {discardconn}
    fi
[] ((x,y)=(i,j-1))^(trc>0)->s\mp@subsup{d}{}{\prime}:= \mathscr{MD}(x|y|d|S);
    if (sd'=nd)}\mp@subsup{)}{}{\wedge}(\mathrm{ pid }=(x,y))->trc,c:=4,
    |] (s\mp@subsup{d}{}{\prime}=nd)}\mp@subsup{)}{}{\wedge}(\mathrm{ pid }\ddagger(x,y))->\mathrm{ if }d<c->pid,\operatorname{trc},c:=(x,y),4,
                                    |]d\geqc}->\mathrm{ skip {discard conn}
                                fi
    ||(s\mp@subsup{d}{}{\prime}\not=nd) -> skip {discardconn}
    fi
|] ((x,y) = (i-1,j))^(trc>0) -> wd':= \mathcal{MDD}(x|y|c|\mathcal{W});
    if (wd'=ed)^}(pid=(\chi,y))->trc,c:=4,
    |] (wd'=ed )^ (pid }\ddagger(x,y))->\mathrm{ if }d<c->\mathrm{ pid, trc,c:= (x,y), 4, d }\mp@subsup{}{}{32
                                    []d\geqc}->\mathrm{ skip {discardconn}
                                    fi
    |](wd'\ddaggered) -> skip {discard conn}
    fi
    [] ((x,y)=(i,j+1))^(trc = 0) -> nd':= \mathscr{MD (x y | c |N ;}
        if (nd'=sd)^ (d<cmax ) 
                        if ~tout }->\mathrm{ activate timeout in t seconds; tout:= true
                        [] tout }->\mathrm{ skip
                            fi
    |](nd'\ddaggersd)v(d=cmax)}->\mathrm{ skip {discard conn}
    fi
|] ((x,y)=(i+1,j))^(trc = 0) >e ed}\mp@subsup{}{}{\prime}:=\mathcal{MDD}(x|y|c|\mathcal{E})
    if (ed'= wd ^^(d<cmax ) > pid, trc, c:= (x,y),4,d+1;
                                    if ~tout }->\mathrm{ activate timeout in t seconds; tout:= true
                    [] tout }->\mathrm{ skip
                            fi
    ||(ed'\not=wd)v(d=cmax)}->\mathrm{ skip {discard conn}
    fi
```



```
    if (nd'=sd)^}(pid=(x,y))^(d<cmax) -> trc,c:=4,d+
    [] (nd'=sd)^ (pid = (x,y))^ (d=cmax ) }->\operatorname{trc}:=
    |] (nd'=sd)}^(pid f (x,y))^(d+1<c)-> pid, trc,c:=(x,y),4,d+
    /] (nd'=sd)^ (pid }\ddagger=(x,y))^(d+1\geqc)-> ski
    /] nd'=sd}->\mathrm{ skip {discard conn}
    fi
```

[]$((x, y)=(i+1, j))^{\wedge}(\operatorname{trc}>0) \rightarrow e d^{\prime}:=\mathcal{M D}(x|y| c \mid \mathcal{E}) ;$
if $\left(e d^{\prime}=w d\right)^{\wedge}(\text { pid }=(x, y))^{\wedge}(d<c \max ) \rightarrow \operatorname{trc}, c:=4, d+1$
[]$\left(e d^{\prime}=w d\right)^{\wedge}(p i d=(x, y))^{\wedge}(d=c \max ) \rightarrow \operatorname{trc}:=0$

```
[ \(/\left(e d^{\prime}=w d\right)^{\wedge}(\text { pid } \neq(x, y))^{\wedge}(d+1<c) \rightarrow\) pid, \(\operatorname{trc}, c:=(x, y), 4, d+1\)
\(\left[/\left(e d^{\prime}=w d\right)^{\wedge}(p i d \neq(x, y))^{\wedge}(d+1 \geq c) \rightarrow\right.\) skip
[/ ed'ł wd \(\rightarrow\) skip \{discard conn\}
fi
```

fi
end
initial state: if $i=0^{\wedge} j=0$ then pid $=(0,0), \operatorname{trc}=4, c=0$, tout $=$ true and timeout is activated else trc $=0$, tout $=$ false, and the timeout is not activated

6 Countering $\mathcal{N e}$ twork Infiltration

There is a way to secure a sensor network against networkinfiltration using a message digest function. In the data transfer protocol, a message digest value is added using a sfared secret in order to provide security. This way, any message that originates from an adversarial mote can easily be detected. This concept is similar to that of the secure grid routing protocol.
6.1 Enfancing the Protocol In the data transfer protocol, in order to prevent mote infiltration, a message digest value is added to the data message. Thus, there are these added inputs:

```
PS,S,\mathcal{W},\mathcal{N}\mathcal{E}\quad:\quad\mathrm{ integer}
```

$\mathcal{P S}$ is the secret that mote $[i, j]$ shares with its parent in the spanning tree.

There are also some added variables. The variable drepresents the message digest value computed by mote [i, $j]$, Gefore it broadcasts the data message. There are six additional variables in the entianced protocolcalled $s d, w d, n d, e d, p d$, and $d$. The variable pd stores the message digest value that mote [i,j]computes before Groadcasting data to its parent. Therefore, pd is the message digest of pid concatenated with $t$ concatenated with $P S$. The variable d stores the message digest value calculated by
the broadcasting mote. These variables are declared as follows:

```
pd,sd,wd,nd,ed,d : integer
```

In the first action, the only statement added to the data transfer protocol is the statement where mote $[i, j]$ computes the message digest value using the secret shared with its parent. This variable is called $p d$. The added statement is this: pd := $\mathcal{M D}(p i d|t| \mathcal{P S})$, and the $p d$ value is included in the data message.

The first action including its statements is defined as follows:


In the second action, mote $[i, j]$ computes the message digest values $s d$ ', wd', nd', and ed'to verify the authenticity of the message it has received. Next, mote $[i, j]$ compares $s d$ ', wd', nd', and ed'with d to see whether the values are equal. If not, the message is discarded. Otherwise, if the message digest value is equal to that computed by mote $[i, j]$, and if $(i, j)$ is other than $(0,0)$, then the message is forwarded to the parent as in the original data transfer protocol. If $(i, j)$ equals $(0,0)$, then the message is stored; thus mote $[i, j]$ skips. The second action including its statements is as follows:

```
rcvdata \((x, y, t, d) \rightarrow\)
    if \((x \neq i) \mathcal{V}(y \neq j) \mathcal{V}(t r c=0) \rightarrow\) skip \(\quad\) \{discard data\}
    []\((x=i)^{\wedge}(y=j)^{\wedge}(\operatorname{trc}>0) \rightarrow\)
                                    \(s d, w d, n d\), ed \(:=\mathcal{M D}(\chi|y| t \mid S), \mathcal{M D}(\chi|y| t \mid \mathcal{W}), \mathcal{M D}(\chi|y| t \mid \mathcal{N}), \mathcal{M D}(\chi|y| t \mid \mathcal{E}) ;\)
                if \(((s d=d) \mathcal{V}(w d=d) \mathcal{V}(n d=d) \mathcal{V}(e d=d)) \wedge(x \neq 0 v y \neq 0) \rightarrow\)
                    \(p d:=\mathcal{M D}(\) pid \(|t| \mathcal{P S}) ;\) broadcast data (pid, \(t, p d)\)
                [] \(((s d=d) v(w d=d) v(n d=d) v(e d=d))^{\wedge} x=0 \wedge y=0 \rightarrow\) skip \{store data\}
                []\((s d \neq d)^{\wedge}(w d \neq d)^{\wedge}(n d \neq d) \wedge(e d \neq d) \rightarrow\) skip \{discard data\}
                fi
    fi
```

Thus, the secure data transfer protocol has the same number of actions as the original protocol. It uses the same message digest function that is in the secure grid routing protocol.
6.3 Formal Definition of Enkanced Protocol

```
processmote [i:0 .. m-1, j:0 .. n-1]
inp L : set{(i,max (j-1,0)), (max (i-1,0),j),
    H : set {(i,min }(j+1,n-1))(\operatorname{min}(i+1,m-1),j)
    pid : &\mathcal{UH}
    trc : 0..4 {from grid routing protocol}
    PS,S,\mathcal{W},\mathcal{N},\mathcal{E}:\quad\mathrm{ integer {from grid routing protocol}}
    x,y :
    pd,sd,wd,nd,ed,d: integer
begin
    trc>0 
    rcv data (x,y,t,d) }
                if (x\not=i)v(y\ddaggerj)v(trc=0)-> skip {discard data}
            [] (x=i)^ (y=j)^(trc>0) ->
                            sd,wd,nd, ed := \mathscr{MD}(\chi|y|t|S),\mathcal{MD}(x|y|t|\mathcal{W}),\mathcal{MD}(\chi|y|t|\mathcal{N},\mathcal{MD}(\chi|y|t|\mathcal{E});
            if }((sd=d)v(wd=d)v(nd=d)v(ed=d))^(x\not=0vy\ddagger0)
```



```
                            |] ( sd=d v v (wd = d)v (nd=d)v (ed=d))^ x=0 ^ y = 0 > skip {store data}
```



```
                                    {discard data}
                fi
            fi
end
```

7 Concluding Remarks

The grid routing protocol provides a straightforward abstraction of the sensor network. In this abstraction, each mote is defined to be a process. Each mote broadcasts messages to its neighbors, chooses one of them to be its parent in the spanning tree, and forwards data toward the root of the spanning tree, via its parent. Due to the sensitive nature of most applications of the sensor network, the protocol requires security. The secure grid routing protocol and the secure data transfer protocol protect the sensor networkfrom mote impersonation. The addition of the shared secrets between
neighbors and the message digest function provides a solution to the problem of one adversarial mote replacing a legitimate mote in a sensor network. This shared secret enhancement also secures the network against mote infiltration.

One attack that the adversary may make against the network with shared secrets is that of message replay. One solution to provide security to the network against anti-replay is to add sequence numbers and a dynamic memory window in which to store whether or not a message fas been received. Using this protocol, a mote may determine whether a message is new or is being replayed. However, the description of this protocol is beyond the scope of this paper.
References
[1] M.G. Gouda, Elements of $\mathfrak{N e}$ etwork Protocol Design, Iofn Wiley $\mathfrak{H}$ Sons, New York New York 1998
[2] Young-ri Choi, Mofiamed Gouda, Moon C. Kim, and Anish Arora "The Mote Connectivity Protocol", in Proceedings of $12^{\text {th }}$ International Conference on Computer Communications and $\mathfrak{N e}$ tworks (ICCCN 2003 ), pages 522-538, Dallas, Texas, October 20-22, 2003
[3] Young-RiChoi, Sensor NetworkProtocols, Ph. D. thesis, in progress, 2003
[4] Mohamed Gouda, Young-ri Choi, Anish Arora, and Vinayak $\mathcal{N a}$ (K, The Logical Grid Routing Protocol, Presentation given in $P$ meeting of $\mathcal{N E S} \mathcal{T}$ program in $\mathcal{D A R P \mathcal { A } , \mathcal { I } u l y , 2 0 0 3}$

