## Spatial Partitioning Data Structures

## A Quick Calculation

Number of pixels on screen (1080P):

- $1920 \times 1080=2,073,600$


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Number of triangles

- ~millions

Number of ray-triangle intersections:

- ~10^12 intersections per frame


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- $1920 \times 1080=2,073,600$

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Number of ray-triangle intersections:

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Now add antialiasing, shadow rays, reflection rays, ......

## Bounding Boxes

Fit boxes around objects


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Check ray-box first


## Bounding Boxes

Fit boxes around objects
Check ray-box first
Then check objects


## Bounding Boxes

What if we have a single complex object?


Cut into pieces, treat as separate?

## Bounding Volume Hierarchy

For points:


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## Bounding Volume Hierarchy

Top-down approach:

## BuildBVH(points P)

if $\mathbf{P}$ contains one point return leaf;
compute bounding box
find longest axis
split points into groups $\{\mathbf{L}, \mathbf{R}\}$ along this axis return $\{\operatorname{BuildBVH}(\mathbf{L})$, BuildBVH(R) \};

## Bounding Volume Hierarchy

Bottom-up approach (faster, harder):

- sort along space-filling fractal (z-order curve)

- implement using bit fiddling (Morton codes)



## BVH Traversal

For points:


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## BVH Analysis

## Build time: $\mathrm{O}\left(\mathrm{N} \log ^{\wedge} 2 \mathrm{~N}\right)$ (top-down)

Traverse time:

## BVH Analysis

Build time: $\mathrm{O}\left(\mathrm{N} \log ^{\wedge} 2 \mathrm{~N}\right)$ (top-down)

Traverse time:

- worst case: $\mathrm{O}(\mathrm{N})$
- typical case: $\mathrm{O}(\log \mathrm{N})$

Advanced traversal strategies possible

## BVH in Practice

## Build around triangle primitives


leaves are individual triangles
when building, sort by e.g. triangle center
note: nodes can overlap

## BVH Node Types

Most typical: AABBs

- "axis-aligned bounding boxes"

Other options possible:


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Other options possible:

- sphere trees
- OBBs (oriented bounding boxes)


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Most typical: AABBs

- "axis-aligned bounding boxes"

Other options possible:

- sphere trees
- OBBs
- k-DOPs

6-DOP<br>(AABB)



14-DOP


## BVH Node Types

Most typical: AABBs

- "axis-aligned bounding boxes"

Other options possible
Complex tradeoff between

- tightness of fit
- traverse cost
- build cost
- memory usage


## BVH Visualized



## Spatial Hashing

Divide space into coarse grid
Each grid cell stores its contents


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How to build?

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Divide space into coarse grid
Each grid cell stores its contents

How to build?

- hash function maps points to their cell
- usually very fast (bit twiddling)

Why useful?

## Spatial Hashing

What if primitives aren't point?

## Spatial Hashing

## What if primitives aren't point?


must rasterize objects to grid
object overlaps multiple cells
--> multiple refs

## Spatial Hashing

Pros:

- (relatively) simple to build
- simple data structure (array of pointers)

Cons:

- must pick a good cell size
- works poorly on heterogeneous object distributions


## Quadtree

## Start with spatial hash

Split crowded cells into child squares


## Quadtree

Works also for non-point primitives Danger - must pick maximum depth


## Quadtree

Pros:

- very space-efficient even for heterogeneous object distributions
- simple to build and traverse (bit tricks often used)
Cons:
- must pick max tree depth
- tree not balanced


## Octree

## 3D version of quadtree




## Binary Space Partition

Recursively split space using planes

2.

3.

4.


## Binary Space Partition

Recursively split space using planes
Each node stores splitting plane
Each leaf stores object references


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Each node stores splitting plane
Each leaf stores object references

How to pick good splitting plane?

- heuristics / black magic
- good partitioning vs good balance
- special case: axis-aligned planes


## kD Tree

"k-Dimensional Tree"
BSP where each node is vertical or horizontal plane


## kD Tree

How to pick splitting plane?

Goals:

- balance area of two children
- balance number of objects in children
- avoid splitting objects


## kD Tree

How to pick splitting plane?
Common strategy: split next to median object along longest direction


## 3D Tree



## kD Tree

Pros:

- can tailor cell shape to fit objects
- balanced tree

Cons:

- cells not uniformly placed or shaped
- must pick good max tree depth


## Devils Lurk in the Details

Building the leaves:

- what is the bounding box? (AABBs)
- is my object inside, outside, or crossing a grid cell? (spatial hash/octree)
- is my object on the left, right, or both sides of the split plane? (BSP/kD tree)
- how do I duplicate object references correctly? (all but BVHs)


## Devils Lurk in the Details

Traversing the tree:

- how exactly do I do ray-node intersection?
- ray/box (AABBs, octree)
- ray/plane (BSP and kD trees)


## Devils Lurk in the Details

Traversing the tree:

- how exactly do I do ray-node intersection?
- how do I do it efficiently?
- what if my ray starts inside the scene?


## Kinetic Data Structures

During animation, objects move slowly
Cumulatively update data structures instead of rebuilding every frame

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During animation, objects move slowly
Cumulatively update data structures instead of rebuilding every frame
Easy:

- spatial hash
- octree

Annoying:

- BSP trees (kD trees)

