

Problem A finite state machine has input alphabet $\{1, 2\}$. It accepts a string if the sum of its digits is 0 modulo 3. Thus, 12 is accepted and 112 rejected. The empty string's digits add up to 0.

Solution Let d be the sum of the digits of the string seen so far. I label each state with $d \bmod 3$.

