

Methodological Hints About Constructing *unless* Properties

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A typical informal description from which an *unless* property is to be constructed is the following: If process x and process y are both waiting then both will continue waiting until y stops waiting. Denoting by xw and yw that x, y are waiting, respectively, the above requirement can be translated to Hoare-triples,

for any transition S : $\{xw \wedge yw\} S \{xw\}$

Note: The informal description is confusing. A possible interpretation is to allow the postcondition, $xw \vee \neg yw$, i.e., allow for both processes to stop waiting simultaneously. \square

An *unless* property can be constructed from the above triple as follows (see Exercise 3.8 in [?]). Given that

$(\forall S :: \{u\} S \{v\})$

We can assert p *unless* q for *any* p, q satisfying:

- $u \Rightarrow p \Rightarrow v$,
- $q \equiv \neg u \wedge v$

These observations are justified by solving

$$u \equiv p \wedge \neg q \quad \text{and} \quad v \equiv p \vee q$$

for p, q .

Note: The given conditions show that we cannot deal with a triple $\{u\} S \{v\}$ where u does not imply v . \square

Applying to the given example, obtain from $\{xw \wedge yw\} S \{xw\}$

$$xw \wedge yw \Rightarrow p \Rightarrow xw$$

$$\begin{aligned} \text{and } q &\equiv \neg(xw \wedge yw) \wedge xw \\ &\equiv \neg yw \wedge xw \end{aligned}$$

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A simple choice for p is, xw .

Similarly, $\{xw \wedge yw\} S \{xw \vee \neg yw\}$ can be translated to

$$\begin{aligned} & xw \text{ unless } \neg(xw \wedge yw) \wedge (xw \vee \neg yw) \\ \text{i.e., } & xw \text{ unless } \neg yw \end{aligned}$$

Two Simplifications:

The following identities (see Exercise 3.7.2 in [?]) are often useful for simplifications.

$$\begin{aligned} p \text{ unless } q &\equiv p \wedge \neg q \text{ unless } q \\ p \text{ unless } q &\equiv p \vee q \text{ unless } q \end{aligned}$$

The first identity suggests that we may start by defining an *unless* whose left and right sides are disjoint (i.e., $p \wedge \neg q$ and q); then, manipulate it to a simpler form. Since the informal meaning of $p \text{ unless } q$ is that, once p holds it continues to hold until q holds, it may be simpler to translate informally stated properties to an *unless* when p, q do not hold simultaneously.