





## Introduction

- Goal Conditioned Reinforcement Learning suffers from sparse rewards.
- One way to accelerate learning in sparse reward settings is using some form of reward shaping or augmenting sparse rewards with dense signals.
- Reward shaping requires domain information which is either provided by a human or learnt using expert trajectories and interactions with the environment, making it difficult to transfer to unknown environments.
- Reward shaping can be suboptimal and can lead to misalignment.
- We define a GCRL as a **distribution matching** problem as an alternate framework to the conventional reward maximization.
- Distribution matching techniques have been used in several imitation ulletlearning but they require a discriminator which are unstable and require coverage assumptions.
- We present a general framework for GCRL that (a) produces optimal policies, (b) does not use a discriminator - stable and relaxes coverage assumptions, (c) works for any goal distribution, including Dirac, (and corresponding metric based shaping rewards) (d) provides dense signals for policy optimization even when the goal is not seen.

# Method

Use f-Divergence to characterize "distance" between distributions

Let  $p_{\theta}(s)$  be the agent's state visitation distribution for a policy  $\pi_{\theta}$  and  $p_{q}(s)$  is the goal distribution

**Minimize** the following divergence:

 $J(\theta) = D_f(p_{\theta}(s)||p_g(s))$ 

This means the visitation should be high at the goal states and as low as possible at all other states. The objective produces optimal policies for some f-divergences (f-divergences with bounded  $f'(\infty)$ . Optimize using gradients:

$$\nabla_{\theta} J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)} \left[ \left[ \sum_{t=1}^{T} \nabla_{\theta} \log \pi_{\theta}(a_t | s_t) \right] \left[ \sum_{t=1}^{T} f'\left(\frac{p_{\theta}(s_t)}{p_g(s_t)}\right) \right] \right]$$

Gradients of log probabilities

The value of  $f'\left(\frac{p_{\theta}(s_t)}{p_{q}(s_t)}\right)$  will be low at (a) the goal and (b) states with low visitation probability.

# *f*-Policy Gradients: A General Framework for Goal Conditioned RL using <sup>c</sup>-Divergences



### Learning Signals





Dense learning signal

- These gradients look like policy gradients but the term  $f'\left(\frac{p_{\theta}(s_t)}{p_{g}(s_t)}\right)$  is not reward but simply a weight.

# state-MaxEnt RL - A special case

### The commonly used MaxEnt RL ( $\pi$ -MaxEnt RL) maximizes entropy of policy:

 $\max \mathbb{E}_{p_{\theta}(s)}[r(s)] + \mathcal{H}(\pi)$ 

A special case of *f*-PG (using Forward KL): *state*-MaxEnt RL

Can be a Metric based shaping reward for some  $p_g(s)$ 



**Reverse KL** 









### $\max \mathbb{E}_{p_{\theta}(s)} \left[ \log p_g(s) \right] + \mathcal{H} \left( p_{\theta}(s) \right)$

Entropy of state visitation distribution

### state-MaxEnt RL

 $\pi$ -MaxEnt RL