“What they used to do … was to assign you this program which nobody was able to ever figure out … It was tricky programming … comments were in Greek and Latin. So I was assigned this program and I actually got it to work. It even printed out its answers in Latin and Greek. I was the first one to get it to work.”

Margaret Hamilton
Director of Apollo Flight Computer Programming
2D Arrays in Java

- Arrays with multiple dimensions may be declared and used
  ```java
  int[][] mat = new int[3][4];
  ```
- The number of pairs of square brackets indicates the dimension of the array.
- By convention, in a 2D array the first number indicates the row and the second the column.
Two Dimensional Arrays

<table>
<thead>
<tr>
<th></th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>column</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>0</td>
<td>12</td>
<td>0</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

`int[][] mat = new int[3][4];
mat[2][1] = 12;`
Remember how 1D arrays are stored in computer memory?

```java
int[] a = new int[3];
```

![Diagram showing the storage of an int array]
And how to access individual elements of a 1D array?

```java
int[] a = new int[3];
a[0] = 2;
a[1] = 7;
a[2] = -5;
```
2D array = array of references

In the computer’s memory:

```
mat
```

```
0x302c75ea9b
```

```
0x302c75ea9b
```

`mat` is a reference (contains a memory address, i.e., “points to” a location in computer’s memory…)
2D array = array of references

In the computer’s memory:

At that memory location is `mat[0]`, followed by `mat[1]` right next to it, followed by `mat[2]`.
2D array = array of references

In the computer’s memory:

```
mat
```

```
0x302c75ea9b
```

```
mat[0]
```

```
0x7345984a3d
```

```
mat[1]
```

```
0x5449ffdad3
```

```
mat[2]
```

```
0x287df3ea3b
```

Each of those array elements are themselves references to other memory locations…
2D array = array of references

In the computer’s memory:

mat

- mat[0]: 0x7345984a3d
- mat[1]: 0x5449ffdab3
- mat[2]: 0x287df3ea3b
2D array = array of references

In the computer’s memory:

mat

0x302c75ea9b

mat[0]
0x7345984a3d

mat[1]
0x5449ffdad

mat[2]
0x287df3ea3b
2D array = array of references

In the computer’s memory:

```plaintext
mat
0x302c75ea9b
mat[0] 0x302c75ea9b
mat[1] 0x7345984a3d
mat[2] 0x5449ffdab3
0x7345984a3d
```

```plaintext
0x7345984a3d
0x5449ffdab3
0x287df3ea3b
0x287df3ea3b
```
2D array = array of references

In the computer’s memory:

mat

0x302c75ea9b

mat[0]

0x7345984a3d

mat[0][0]

0x5449ffdab3

mat[0][1]

0x287df3ea3b

mat[0][2]

mat[0] is an array!

It is a reference to a memory location where mat[0][0] is, followed by mat[0][1] and mat[0][2].
2D array = array of references

In the computer’s memory:

```
mat
  0x302c75ea9b

mat[0]
  0x7345984a3d
  mat[0][0]
    0
  mat[0][1]
    0
  mat[0][2]
    0

mat[1]
  0x5449ffdab3
  mat[1][0]
    0
  mat[1][1]
    0
  mat[1][2]
    0

mat[2]
  0x287df3ea3b
```

Similarly, \texttt{mat[1]} is an array, ...
2D array = array of references

In the computer’s memory:

```
mat[0][0] = 0
mat[0][1] = 0
mat[0][2] = 0
mat[1][0] = 0
mat[1][1] = 0
mat[1][2] = 0
mat[2][0] = 0
mat[2][1] = 12
mat[2][2] = 0
```

...and so is mat[2].
What is What?

int[][] mat = new int[10][12];

// mat is a reference to the whole 2d array

// mat[0] or mat[r] are references to a single row

// mat[0][1] or mat[r][c] are references to single elements

// no way to refer to a single column
Another picture of a 2D array

```java
int[][] mat = new int[5][3];
```
2D Array Problems

- Write a method to find the maximum value in a 2D array of \textit{ints}

- Write a method that finds the sum of values in each column of a 2D array of \textit{doubles}

- Write a method to print out the elements of a 2D array of \textit{ints} in row order.
  - row 0, then row 1, then row 2 ...

- Write a method to print out the elements of a 2D array of \textit{ints} in column order
  - column 0, then column 1, then column 2 ...
Exercise 1 strategy

- Go through entire 2D array and find maximum number. How??
- First, try a simpler problem: try to find the maximum value in a 1D array; just like you would do with a list of numbers on a sheet of paper:
  - Start at the first element of the array, and keep track of the biggest number you’ve seen so far.
  - If the second element is bigger, then set the biggest number you’ve seen so far to that.
  - If the third element is bigger than the biggest number you’ve seen so far, then set the biggest number you’ve seen so far to that.
  - Repeat until you’ve examined every element of the array.
  - Return the biggest value you’ve seen so far.
- A 2D array would work the same; you just need to “run through” the 2D array slightly differently since it has both rows and columns.
public static int getMaxValueOf(int[][] numbers) {
    int max = numbers[0][0];

    for (int i = 0; i < numbers.length; i++) {
        for (int j = 0; j < numbers[i].length; j++) {
            if (numbers[i][j] > max) {
                max = numbers[i][j];
            }
        }
    }

    return max;
}
public class Cs312 {
    public static void main(String[] args) {
        int[][] numbers = {{39, 42, 1, 79, 2},
                          {41, 47, 7, 71, 9},
                          {38, 99, 2, 77, 8}};
        System.out.println("Maximum value is "+ getMaxValueOf(numbers) + ".");
    }

    public static int getMaxValueOf(int[][] numbers) {
        int max = numbers[0][0];

        for (int i = 0; i < numbers.length; i++) {
            for (int j = 0; j < numbers[i].length; j++) {
                if (numbers[i][j] > max) {
                    max = numbers[i][j];
                }
            }
        }

        return max;
    }
}
Exercise 2 strategy

- What should the method return?
  - An array of column sums!
- Iterate over the columns of the 2D array.
  - For a single column, iterate through the rows of the column.
  - Calculate a cumulative sum of the values in the column → store the result in the column sum array.
- Return the column sum array.
Exercise 2 - Possible Answer

```java
public static int[] getColumnSumsOf(int[][] numbers) {
    int numRows = numbers.length;
    int numColumns = numbers[0].length;
    int[] columnSums = new int[numColumns];

    for (int j = 0; j < numColumns; j++) {
        columnSums[j] = 0;
        for (int i = 0; i < numRows; i++) {
            columnSums[j] += numbers[i][j];
        }
    }

    return columnSums;
}
```
public class Cs312 {
    public static void main(String[] args) {
        int[][] numbers = {{39, 42, 1, 79, 2},
                           {41, 47, 7, 71, 9},
                           {38, 99, 2, 77, 8}};
        System.out.println("Column sums are: " + Arrays.toString(getColumnSumsOf(numbers)) + ".");
    }

    public static int[] getColumnSumsOf(int[][] numbers) {
        int numRows = numbers.length;
        int numColumns = numbers[0].length;
        int[] columnSums = new int[numColumns];

        for (int j = 0; j < numColumns; j++) {
            columnSums[j] = 0;
            for (int i = 0; i < numRows; i++) {
                columnSums[j] += numbers[i][j];
            }
        }

        return columnSums;
    }
}
Exercise 3 - Possible Answer

```java
public static void printInRowOrder(int[][] numbers) {
    int numRows = numbers.length;
    int numColumns = numbers[0].length;
    for (int i = 0; i < numRows; i++) {
        System.out.println(Arrays.toString(numbers[i]));
    }
}
```
public static void printInColumnOrder(int[][] numbers) {
    int numRows = numbers.length;
    int numColumns = numbers[0].length;
    for (int j = 0; j < numColumns; j++) {
        System.out.print("Column #" + (j + 1) + ": [");
        System.out.print(numbers[0][j]);
        for (int i = 1; i < numRows; i++) {
            System.out.print(" ");
            System.out.print(numbers[i][j]);
        }
        System.out.println("]");
    }
    System.out.println(""");
}
What is output by the following code?

```java
String[][] strTable = new String[5][8];
System.out.print(strTable.length + " ");
System.out.print(strTable[0].length + " ");
System.out.print(strTable[2][3].length());
```

A. 40 0 0
B. 8 5 0
C. 5 8 0
D. 5 8 then a runtime error occurs
E. No output due to a syntax error.
Use of Two Dimensional Arrays

- 2D arrays are often used when you need a table of data or want to represent things that have 2 dimensions.

- For example, a tic-tac-toe board…
Tic-tac-toe board as a 2D array

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>board[0][0]</strong></td>
<td><strong>board[0][1]</strong></td>
<td><strong>board[0][2]</strong></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>board[1][0]</strong></td>
<td><strong>board[1][1]</strong></td>
<td><strong>board[1][2]</strong></td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>board[2][0]</strong></td>
<td><strong>board[2][1]</strong></td>
<td><strong>board[2][2]</strong></td>
</tr>
</tbody>
</table>
Clicker Question

Write a program to play tic-tac-toe.

What data type do you want to use for the elements of the 2D array?

A. String
B. char
C. int
D. boolean
E. double
```
int[][] board = new int[3][3];
```

0 could mean “not filled”
1 could mean ‘X’
2 could mean ‘O’
char[][] board = new char[3][3];

' ' could mean "not filled"
'X' could mean 'X'
'O' could mean 'O'