Homework 17 Solutions CS 336

The important issue is the logic you used to arrive at your answer.

1. Prove that the program segment

$$y := 1$$
$$z := x + y$$

is correct with respect to precondition "x = 0" and postcondition "z = 1".

$$y := 1$$
 $x = 0$
 $z := x + y$ $x = 0 \land y = 1$
 $z := x + y$ $z = 1$

2. Prove that the program segment

if
$$x < 0$$
 then $x := 0$

is correct with respect to precondition " *true*" and postcondition " $x \ge 0$ ".

	true
if $x < 0$ then	<i>x</i> < 0
x := 0	x = 0
endif	$(x=0) \lor (true \land x \ge 0)$
	$x \ge 0$

3. Prove that the program segment

$$\begin{array}{l} x := 0 \\ z := x + y \\ \textbf{if} \ x < 0 \ \textbf{then} \\ z := z + 1 \\ \textbf{else} \\ z := 0 \end{array}$$

is correct with respect to precondition "y = 3" and postcondition "z = 7".

	y = 3
x := 0	$y = 3 \land x = 0$
z := x+y	$y = 3 \land x = 0 \land z = x + y$
	$x = 0 \land z = 3$
if $x < 0$ then	$x = 0 \land z = 3 \land x < 0$
	false
z := z+1	z = 7 (any postcondition holds)
else	$x = 0 \land z = 3 \land x \ge 0$
z := 7	z = 7
end if	$z = 7 \lor z = 7$
	z = 7