Instructor: Douid Wu (dwult@cs.utexas.edu) TA: Jeff Champion, Nikitha Gollamudi, Charlotte LeMay Overarching goal of cryptography: securing communication over untrusted networks Alice > Bob third party should not be able to (confidentiality) 1) eavesdrop of communication (integrity) 2) tamper with the communication Today: secure communication on web (https://...) TLS protocol (transport layer security) two components: handshake (key exchange) record layer (confidentiality + integrity) protecting data at rest: disk encryption Most of this course: study mechanics for protecting confidentiality + dota - Encryption schemes for confidentiality - Signature schemes for message integrity They exchange for setting up shared secrets End of this course: protecting communication => protecting computation Two users want to learn a joint function of their private inputs training models on private (hidden) data comparing two DNA sequences prevailely bids private auction to determine winner without revealing bids L> private voting mechanisms (can identify winner of election without revealing individual votes) - We can show the following remorkable theorem: "Anything that can be computed with a trusted party can be computed without!" Logistics and administrivia: - Course website: https://www.cs.utexas.edu/~dwu4/courses/fadd - See Ed Discussion for announcements, notes will be posted to course website (1-2 days after lecture) - Homework submission via Gradescape (enroll via Conves) Course consists of 5 homework assignments (worth 75%) and one take-home final (worth 25%) - Five late days for the semester: use in 24-hour increments, max 72 hours (3 late days) for any single assignment T Some office hours will also be askillable on Zoom This semester: Lectures will be recorded using Lectures Online Please participate virtually if you are feeling unwell See protect. utexas edu for suggested guidelines, vaccine information, etc.

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A brief history of cryptography:
    Original good was to protect communication (in times of war)
Basic idea: Alice and Bob have a shared key k
        Alice computes C \leftarrow Encr.pt(k, m)

ciphertext key message (plaintext)
       Bob computes m < Decrypt (k, c) to recover the message
   This tuple (Encrypt, Decrypt) is called a cipher
                                                K, M, C are sets (e.g., K= M= C= {0,1328})
Definition. A cipher is defined over (K, M, C) where K is a key-space, M is a message space and C is
             a ciphertext space, and consists of two aborithms (Encrypt, Decrypt):
                       Encrypt: K×M→C } functions should be "efficiently-computable"

Decrypt: K×C→M } theory: runs in probabilistic polynomial time [algorithm can be randomized]
                                                        practice: fast on an actual computer (e.g., < 10 ms on my laptop)
            Correctness: Ykek, Ymem:
                               Decrypt (k, Encrypt (k, m)) = m
                        "decrypting a ciphertext recovers the original message"
Early ciphers: "shift by 3"
         AHD
                         Not a cipher! There is no key!

Anyone can decrypt!

Algorithm to encrypt is assumed to be public.

NEVER RELY ON SECURITY BY OBSCURITY! - Harder to change system than a key
           BH> E
            C F> F
           A \leftrightarrow X
            4 -> B
                                                                                            - Less scrutiny for secret algorithms
            2 P> C
   - Caesar cipher +t: "shift by k" (k=13: ROT-13)
              Still totally broken since there are only 26 possible keys (simply via broke force guessing)
   - Substitution cipher: the key defines a permutation of the alphabet (i.e., substitution)
           A \mapsto C
B \mapsto X
ABC \mapsto CXJ
C \mapsto J
      Z \mapsto T — substitution table is the key How many keys? For English alphabet, 26! \approx 2^{88} possible keys
                                                                     very large value, cannot brate force the key
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Still broken by frequency analysis

- e is the most frequent character (12%)

- q is the least frequent character (~0.10%)
           Can also look at digram, frigram frequencles
    - Vigener aprec (late 1500s) - "polyalphabetic substitution" key is short phrase (used to determine substitution table):
              k = LTT.

Encrypt (k, m): HELLO

+ CATCA 

repeat the key
                     k = CAT
                                  Linterpret letters as number between 1 and 26
                                        addition is modulo 26
                  if we know the key length, can break using frequency analysis otherwise, can try all possible key lengths l=1,2,...
                       L> general assumption: keys will be much shorter than the message latherwise if we have a
                                                       good mechanism to deliver long keys securely, then can use that mechanism
                                                      to share messages directly
    Fancier substitution ciphers: Enigma (based on rutor machines)
             but .. still breakable by frequency analysis
Today: encryption done using computers, lots of different ciphers

- AES (advanced encryption standard: 2000) "block cipher"

"stream cipher"
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not ideal property ...
One-time pad [ Vigenme cipher where key is as long as the message!]
      K= {0,132
                       Encrypt (k, m): output c= k @ m
     M = {0,13" Decrypt (k,c): output m = k & C
      C = {0,13"
                                                       bituise exclusive or operation (addition mod 2)
Correctness: Take any k & lo,1), m & lo,13":
                      Decrypt (k, Encrypt (k, m)) = k & (k & m) = (k & k) & m = m
                                                                                                (since k \oplus k = 0^n)
Is this secure? How do we define security?
   - Given a ciphertext, cannot recover the key?
         Not Good: Says nothing about hiding message. Encrypt (k, m) = m would be secure under this definition, but this scheme
                    is totally insecure intuitively!
   Given a ciphertext, cannot recover the message.
          NOT GOOD! Can leak part of the missage. Encrypt (k, (mo, m, )) = (mo, m, \oplus k). This encryption might be considered secure
                      but leaks half the message. [Imagine if message was "usernane: alice || password: 123456"
                                                                                                             this might be the string that is lecked!
   - Given a ciphertext, counst recover any bit of the message.
          NOT GOOD! Can still learn parity of the bits (or every poir of bits), etc. Information still leabed...
   - Given a ciphertext, learn nothing about the message.
         GOOD! But how to define this?
Coming up with good definitions is difficult! Definitions have to rule out all adversarial behavior (i.e., capture broad enough dass
of attacks)
       > Big part of crypto is getting the dedinitions right. Pre-1970s: cryptography has relied on intuition, but intuition is often
                                                                         wrong! Just because I counset break it show not mean
How do we capture "kourning nothing about the message"?
                                                                                                  someone else cannot...
    If the key is randown, then ciphertext should not give information about the message.
Definition. A cipher (Encrypt, Decrypt) satisfies perfect secrecy if for all messages mo, m, E M, and all ciphertexts CEC:
                           Pr[k & K: Encrypt (k, m.) = C] = Pr[k & K: Encrypt (k, m,) = C]
                             probability that encryption of mo
is c, where the probability is
taken over the random choice of
Perfect secrecy says that given a ciphertext, any two messages are equally likely.
     => Cannot infer anything about underlying message given only the ciphertext (i.e., ciphertext - only attack)
Theorem. The one-time pad soctisfies perfect secrecy.
Proof. Take any message m & {0113 and ciphertext C & {011) " Then,
                     Pr[k & fo,13": Encrypt (k,m) = c] = Pr[k & fo,13": k @ m = c]
                                                         = Pr[k & foil) : k = m @ c]
         This holds for all messages m and ciphertexts c, so one-time pad satisfies perfect secrecy.
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Are we done? We now have a perfectly-secure cipher!
    No! Keys are very long! In fact, as long as the message...
                                                                if we can share keys of this length, can use some mechanism to share the message itself
        "One-time" restriction
        Malleable
Issues with the one-time pad:
   - One-time: Very important. Never reuse the one-time pod to encrypt two messages. Completely broken!
            Suppose c,= k @ m, and C2 = k @ m2
                                                                   can be recognized this to recover messages
             Then, C_1 \oplus C_2 = (k \oplus m_1) \oplus (k \oplus m_2)
                             = m, 10 m2 | learn the xor of two messages!
             One-time pad reuse:
                  - Project Verona (U.S. counter-intelligence operation against U.S.S.R during Cold War)
                          → Soviets reused some pages in codebook ~ led to decryption of ~ 3000 messages sent by Soviet
                              intelligence over 37-year period [notably exposed espionage by Julius and Ethul Rosenberg]
                  - Microsoft Point-to-Point Tunneling (MS-PPTP) in Windows 98/NT (used for VPN)
                          > Same key (in stream cipher) used for both server -> client communication AND for client -> server
                              communication (RC4)
                  - 802.11 WEP: both client and server use same key to encrypt traffic
                                 many problems just beyond one-time pad reuse (can even recover key after observing small
                                 number of frames!)
      - Malleable: one-time pad provides no integrity; anyone can modify the ciphertext:
                                   m < k 0 c
                                               1 replace c with c⊕m'
                               ⇒ k @ (c @ m') = m @ m' ← adversary's change now xored into original massage
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