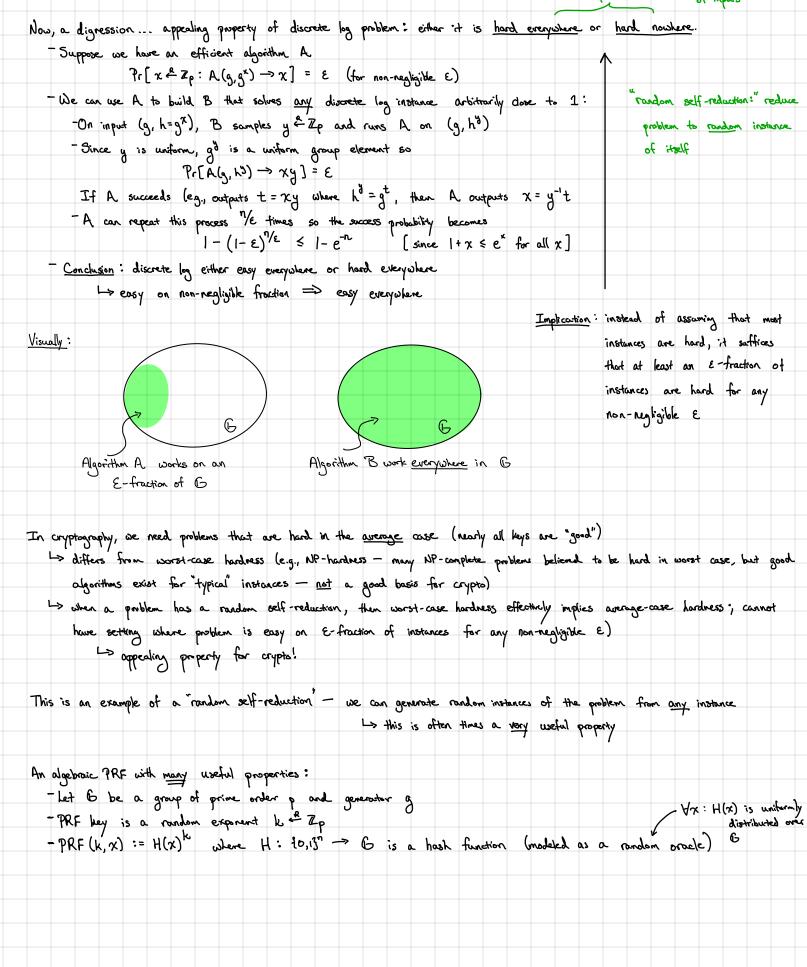
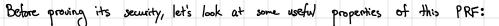
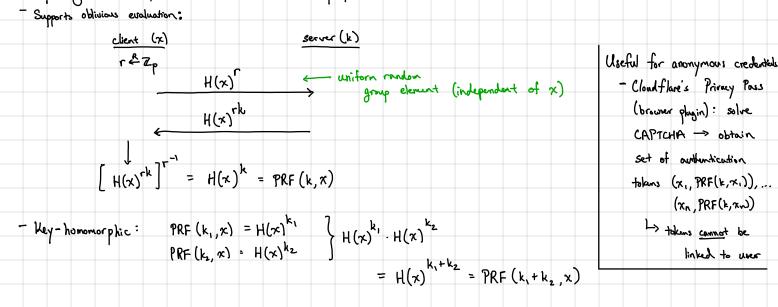
up to a realigible fraction of inputs







Useful building block for updatable encryption:
- Server has many ciphertexts encrypted under
$$k_1$$

 $ct_1 = (x_1, PRF(k, x_1) \cdot m_1)$
 $ct_1 = (x_1, PRF(k, x_1) \cdot m_1)$
 $ct_1 = (x_1, PRF(k, x_1) \cdot m_1)$
 $ct_1 = (x_n, PRF(k, x_n) \cdot m_n)$
 $ct_1 = (x_n, PRF($

The rondom oracle model: assume parties have oracle access to a truly random function

adversaries are modeled as cracle Twing machines (with a randomness tape) success probability taken over its own randomness and the randomness of prock outputs

when a reduction runs an adversary, it is responsible for answering oracle gueries by the adversary

There is it is a conserved with the indext as a rankow cone, the PRF(x,x) == H(x)^h is a serve TR
Proof Ide DDH assumption:
$$(g_1, g^h, g^h, g^h)$$
 indistinguishable from (g_1, g^h, g^h, g^h) where $h(x)^h \in g^h$
Is by a set $h \to a$ is the $H(x)^h \in g^h$
Is a basis indistinguishable from (g_1, g^h, g^h, g^h) : $[a is shared in TRE]$
Core (g_1, h, u, v) where $h \circ g^h, g^{hh}$ is a fixed in TRE]
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Core (g_1, h, u, v) where $h \circ g^h, g^{hh}$ is a fixed in the fixed in the constant of the

When A queries PRF on X: 1. Check if X +> (y, 2) is in the table. If so, reply with 2.

2. Otherwise, sample s, t
$$\leftarrow \mathbb{Z}p$$
 and add $\chi \mapsto (u^{s}g^{t}, v^{s}h^{t})$ to the table.
3. Reply to A with $v^{s}g^{t}$

By the analysis above, if $T = g^{ab}$, then B perfectly simulates the PRF security game where the key is a and H(x) is $u^{s}g^{t}$ for s, $t \in \mathbb{Z}p$ (namely, H(x) is random group element). If $T \in \mathbb{G}$, then the responses to the PRF gueries are uniform and independent of x (from the analysis of the self-reduction above).