

Homework 2: Symmetric Cryptography

Due: October 2, 2025 at 11:59pm (Submit on Gradescope)

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Instructions. You **must** typeset your solution in LaTeX using the provided template:

<https://www.cs.utexas.edu/~dwu4/courses/fa25/static/homework.tex>

You must submit your problem set via [Gradescope](#) (accessible through [Canvas](#)).

Collaboration Policy. You may discuss your general *high-level* strategy with other students, but you may not share any written documents or code. You should not search online for solutions to these problems. If you do consult external sources, you must cite them in your submission. You must include the names of all of your collaborators with your submission. Refer to the [official course policies](#) for the full details.

Problem 1: A Parallel CBC [15 points]. A disadvantage of randomized CBC mode is that CBC encryption is inherently sequential. However, CBC decryption is parallelizable. Suppose we interchanged CBC encryption and decryption. Specifically, let $(\text{Encrypt}_{\text{CBC}}, \text{Decrypt}_{\text{CBC}})$ be CBC encryption constructed from a secure PRP $F: \mathcal{K} \times \{0, 1\}^n \rightarrow \{0, 1\}^n$. Define $(\text{Encrypt}', \text{Decrypt}')$ as follows:

- $\text{Encrypt}'(k, m)$: Sample a random $\text{IV} \xleftarrow{R} \{0, 1\}^n$ and output $\text{Decrypt}_{\text{CBC}}(k, (\text{IV}, m))$.
- $\text{Decrypt}'(k, (\text{IV}, c))$: Output $\text{Encrypt}_{\text{CBC}}(k, (\text{IV}, c))$. Note here that we are running $\text{Encrypt}_{\text{CBC}}$ with the provided IV (i.e., $\text{Encrypt}_{\text{CBC}}$ is *not* sampling a random IV).

Prove formally that $(\text{Encrypt}', \text{Decrypt}')$ is not CPA-secure. You should describe an efficient adversary and compute its advantage. When constructing a CPA adversary, every encryption query (m_0, m_1) the adversary makes to the CPA challenger must be on equal-length messages (i.e., $|m_0| = |m_1|$ in each query).

Note: It is also possible to give a 1-query attack so this scheme is not even semantically secure. However, for this problem, feel free to consider the CPA-security game.

Problem 2: CBC Padding Oracle Attack [14 points]. Recall that when using a block cipher in CBC mode, the message length must be a multiple of the block size. Thus, CBC requires padding to support encryption of arbitrary-length messages. In the TLS protocol (used for securing traffic on the web), if ν bytes of padding are needed, then ν bytes with value $(\nu - 1)$ are appended to the message. As a concrete example, if 1 byte of padding is needed, a single byte with value 0 is appended to the message before applying CBC encryption. In TLS, the record layer is secured using an approach called “MAC-then-Encrypt¹” (which as we will soon see, is not the ideal combination). At decryption time, the ciphertext is first decrypted (and the padding verified) *before* checking the MAC. In older versions of OpenSSL, the library reports whether a decryption failure was due to a “bad pad” or due to a “MAC verification failure.” One might think that it was beneficial to provide an informative error message on decryption failure. As you will show in this problem, this turns out to be a disaster for security.

¹In MAC-then-encrypt, the encryption algorithm first computes a MAC t on the message m , and the ciphertext is the encryption of the message-tag pair (m, t) .

Suppose an adversary has intercepted a ciphertext ct encrypted using AES-CBC and moreover, suppose the adversary can submit ciphertexts to a CBC decryption oracle and learn whether the padding was valid or not. The decryption oracle outputs a *single* bit indicating whether the decrypted plaintext contains a valid pad. Your goal in this problem is to develop an efficient algorithm that allows the adversary to decrypt ct by making a small number of queries to the padding oracle.

We have provided [starter code](#) that contains an implementation of AES-CBC encryption using the Python [cryptography](#) library. Your task is to write an algorithm that takes as input a ciphertext encrypted using AES-CBC (with randomized IV) and outputs the associated message given access to the above decryption oracle. The decryption oracle takes as input a ciphertext and outputs True if the decrypted plaintext has a valid pad (as defined above), and False if not.

Your task is to implement the `decrypt` method in `cbc.py`. You **cannot** change the interface for `decrypt`; otherwise, you are free to implement the algorithm however you prefer (using *standard* Python libraries, including the Python `cryptography` library). Your code will be evaluated only for correctness. Some helper functions are provided in `util.py`. Your attack must satisfy the following requirements:

- Your algorithm should support decrypting messages of *arbitrary* non-zero length. The message you return should *not* include any padding (you can use the `strip_padding` method in `util.py` to remove the padding).
- The input ciphertexts can be encryptions of arbitrary byte sequences (i.e., they are not necessarily ASCII-encoded strings).
- Your algorithm is allowed to make at most 8192 queries to the padding oracle for each non-IV block of the ciphertext. Note that this is an *upper* bound and many algorithms will require significantly fewer queries.
- **Hint:** Start by showing how to test whether the last byte of m_i is some value t by making 2 queries to the decryption oracle.

The following is the output of running `base.py` on our reference implementation (34 lines of code):

```
$ python3 base.py
Plaintext: b'CS 346'
Decrypted output: b'CS 346'
Successful decryption? True
Number of padding oracle queries: 1608
```

Submission instructions: Upload your code (consisting of *only* `cbc.py`) to Gradescope under Homework 2A. Note that your implementation must work with our provided `main.py` and `util.py`. Your submission will be autograded, and upon submission, your code will be run on a simple test case. There is **no** written component for this question.

Remark: Are there settings where the server would repeatedly decrypt ciphertexts of the user's choosing? It turns out that when using IMAP (the protocol email clients use to fetch email) over TLS, the IMAP client will repeatedly send the user's password to the IMAP server to authenticate. With the above padding

oracle (implemented using a “timing channel”), an adversary can recover the client’s password in *less than an hour*! This problem shows that if a decryption failure occurs, the library should provide *minimal* information on the cause of the error. This type of “padding oracle” attack was the basis of the “Lucky 13” attack on TLS 1.0 (2013)—many years after they were first discovered (2002) and thought to be patched!

Problem 3: Cryptographic Combiners [30 points]. Suppose we have two candidate constructions Π_1, Π_2 of a cryptographic primitive, but we are not sure which of them is secure. A cryptographic combiner provides a way to use Π_1 and Π_2 to obtain a new construction Π such that Π is secure if at least one of Π_1, Π_2 is secure (*without* needing to know which of Π_1 or Π_2 is secure). Combiners can be used to “hedge our bets” in the sense that a future compromise of one of Π_1 or Π_2 would not compromise the security of Π . In this problem, we will study candidate combiners for different cryptographic primitives.

- Let $F_1, F_2: \mathcal{K} \times \{0, 1\}^n \rightarrow \{0, 1\}^n$ be efficient functions. Consider the function $F((k_1, k_2), x) := F_1(k_1, x) \oplus F_2(k_2, x)$. **Prove or disprove:** if at least one of F_1 or F_2 is a secure PRF, then F is a secure PRF.
- Let $H_1, H_2: \{0, 1\}^* \rightarrow \{0, 1\}^\lambda$ be arbitrary collision-resistant hash function candidates. Define the function $H(x) := H_1(x) \| H_2(x)$. **Prove or disprove:** if at least one of H_1 or H_2 is collision-resistant, then H is collision-resistant.
- Let $(\text{Sign}_1, \text{Verify}_1)$ and $(\text{Sign}_2, \text{Verify}_2)$ be arbitrary MAC candidates². Define $(\text{Sign}, \text{Verify})$ as follows:
 - $\text{Sign}((k_1, k_2), m)$: Output (t_1, t_2) where $t_1 \leftarrow \text{Sign}_1(k_1, m)$ and $t_2 \leftarrow \text{Sign}_2(k_2, m)$.
 - $\text{Verify}((k_1, k_2), m, (t_1, t_2))$: Output 1 if $\text{Verify}_1(k_1, m, t_1) = 1 = \text{Verify}_2(k_2, m, t_2)$ and 0 otherwise.

Prove or disprove: if at least one of $(\text{Sign}_1, \text{Verify}_1)$ or $(\text{Sign}_2, \text{Verify}_2)$ is a secure MAC, then $(\text{Sign}, \text{Verify})$ is a secure MAC.

Problem 4: Time Spent [1 point]. How long did you spend on this problem set? This is for calibration purposes, and the response you provide does not affect your score.

Optional Feedback. Please answer the following *optional* questions to help us design future problem sets. You do not need to answer these questions. However, we do encourage you to provide us feedback on how to improve the course experience.

- What was your favorite problem on this problem set? Why?
- What was your least favorite problem on this problem set? Why?
- Do you have any other feedback for this problem set?
- Do you have any other feedback on the course so far?

²Namely, you can assume that they are correct (but could be arbitrarily broken).